

Paper Title*

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Abstract—
Index Terms—

I. INTRODUCTION

II. SYSTEM MODEL

A. Graph Model

V^c is set of cloud nodes. V^f is set of fog nodes. V^e is set of edge nodes. V^s is set of sensor nodes.

$$V^c = \{v_1^c, v_2^c, \dots, v_{l_c}^c\} \Rightarrow |V^c| = l_c \quad (1a)$$

$$V^f = \{v_1^f, v_2^f, \dots, v_{l_f}^f\} \Rightarrow |V^f| = l_f \quad (1b)$$

$$V^e = \{v_1^e, v_2^e, \dots, v_{l_e}^e\} \Rightarrow |V^e| = l_e \quad (1c)$$

$$V^s = \{v_1^s, v_2^s, \dots, v_{l_s}^s\} \Rightarrow |V^s| = l_s \quad (1d)$$

C^c is set of capacity of cloud nodes. C^f is set of capacity of fog nodes. C^e is set of capacity of edge nodes.

$$C^c = \{c_1^c, c_2^c, \dots, c_{l_c}^c\} \quad (2a)$$

$$C^f = \{c_1^f, c_2^f, \dots, c_{l_f}^f\} \quad (2b)$$

$$C^e = \{c_1^e, c_2^e, \dots, c_{l_e}^e\} \quad (2c)$$

T is set of tasks.

$$T = \{t_1, t_2, \dots, t_{l_t}\} \Rightarrow |T| = l_t \quad (3a)$$

$$(3b)$$

Each task expresses as follows:

$$t_k \in T \Rightarrow t_k = (w_k, \delta_k, o_k) \quad (4)$$

w_k shows computation workload of task. δ_k is completion deadline of task and o_k determines the owner of task.

Price unit sets are defined as following:

$$P^c = \{p_1^c, p_2^c, \dots, p_{l_c}^c\} \quad (5a)$$

$$P^f = \{p_1^f, p_2^f, \dots, p_{l_f}^f\} \quad (5b)$$

$$P^e = \{p_1^e, p_2^e, \dots, p_{l_e}^e\} \quad (5c)$$

P^c , P^f and P^e are unit price set of using cloud nodes, fog nodes and edge nodes respectively.

Transmission delay sets that show required time for transmitting packets from sensors to each computational node are defined as follows:

$$T^{c,tr} = \{\tau_1^{c,tr}, \tau_2^{c,tr}, \dots, \tau_{l_c}^{c,tr}\} \quad (6a)$$

$$T^{f,tr} = \{\tau_1^{f,tr}, \tau_2^{f,tr}, \dots, \tau_{l_f}^{f,tr}\} \quad (6b)$$

$$T^{e,tr} = \{\tau_1^{e,tr}, \tau_2^{e,tr}, \dots, \tau_{l_e}^{e,tr}\} \quad (6c)$$

We define execution rate for each computational node as follows:

$$R^c = \{r_1^c, r_2^c, \dots, r_{l_c}^c\} \quad (7a)$$

$$R^f = \{r_1^f, r_2^f, \dots, r_{l_f}^f\} \quad (7b)$$

$$R^e = \{r_1^e, r_2^e, \dots, r_{l_e}^e\} \quad (7c)$$

B. Variables

We define three integer variables for allocating tasks between nodes.

$$x_{k,h}^c = \begin{cases} 1 & \text{task } k \text{ is allocated to cloud node } h \\ 0 & \text{o.w.} \end{cases} \quad (8a)$$

$$x_{k,j}^f = \begin{cases} 1 & \text{task } k \text{ is allocated to fog node } j \\ 0 & \text{o.w.} \end{cases} \quad (8b)$$

$$x_{k,i}^e = \begin{cases} 1 & \text{task } k \text{ is allocated to edge node } i \\ 0 & \text{o.w.} \end{cases} \quad (8c)$$

$$\begin{aligned} \tau_k = & \sum_{i=1}^{l_e} x_{k,i}^e (\tau_i^{e,tr} + \frac{w_k}{r_i^e}) \\ & + \sum_{j=1}^{l_f} x_{k,j}^f (\tau_j^{f,tr} + \frac{w_k}{r_j^f}) \\ & + \sum_{h=1}^{l_c} x_{k,h}^c (\tau_h^{c,tr} + \frac{w_k}{r_h^c}) \end{aligned} \quad (8d)$$

C. Constraints

$$\tau_k \leq \delta_k \quad \forall k \in \{1, 2, \dots, l_t\} \quad (9a)$$

$$\sum_{k=1}^{l_t} x_{k,h}^c w_k \leq c_h^c \quad \forall h \in \{1, 2, \dots, l_c\} \quad (9b)$$

$$\sum_{k=1}^{l_t} x_{k,j}^f w_k \leq c_j^f \quad \forall j \in \{1, 2, \dots, l_f\} \quad (9c)$$

$$\sum_{k=1}^{l_t} x_{k,i}^e w_k \leq c_i^e \quad \forall i \in \{1, 2, \dots, l_e\} \quad (9d)$$

$$\sum_{i=1}^{l_e} x_{k,i}^e + \sum_{j=1}^{l_f} x_{k,j}^f + \sum_{h=1}^{l_c} x_{k,h}^c = 1 \quad \forall k \in \{1, 2, \dots, l_t\} \quad (9e)$$

D. Objective

$$\begin{aligned} p_k = & \sum_{i=1}^{l_e} x_{k,i}^e C(v_i^e, t_k) \\ & + \sum_{j=1}^{l_f} x_{k,j}^f C(v_j^f, t_k) \\ & + \sum_{h=1}^{l_c} x_{k,h}^c C(v_h^c, t_k) \end{aligned} \quad (10a)$$

$$\min \sum_{k=1}^{l_t} p_k \quad (11a)$$

subject to: 9

REFERENCES