



Working with Network Data in R: Loading, Visualizing, Heuristically Analyzing, and Statistically Modeling

Momin M. Malik, PhD

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<https://www.mominmalik.com/icqcm2026c.pdf>

Outline

Why
networks?

Represen-
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networks

Disclaimers

Basic
network
terms

Heuristic
analysis

Statistical
analysis

Conclusions

Works cited

- Why networks?
- Representation of networks
- Disclaimers
- Basic network terms
- Heuristic analyses
- Statistical analysis



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Why networks?

Runaways from “reformatory” for delinquent girls

Why networks?

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Basic network terms

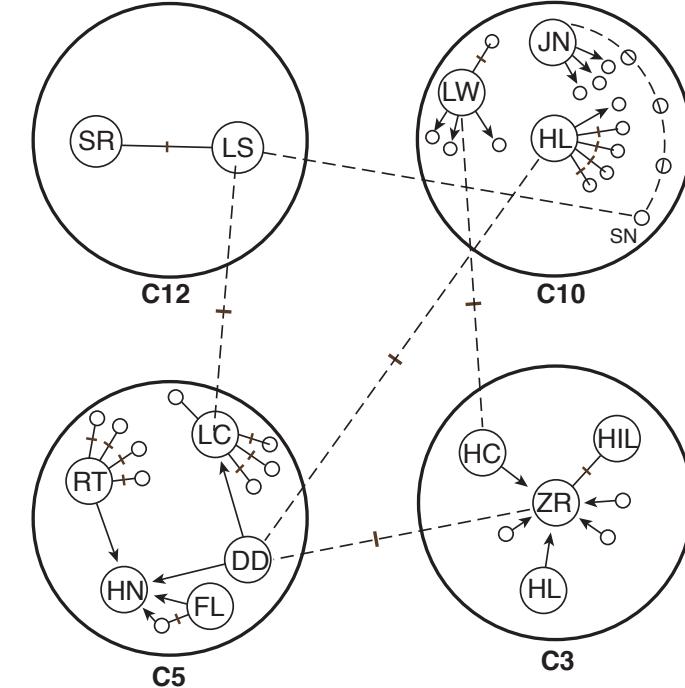
Heuristic analysis

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Moreno (1934); Borgatti et al. (2009)



Competing factions in a karate club

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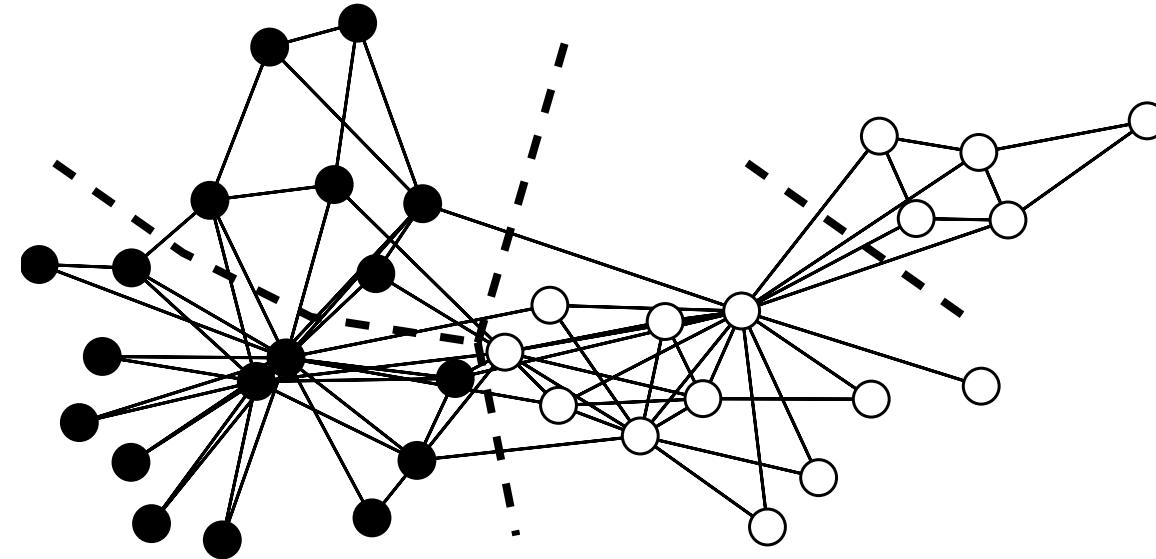
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Zachary (1977); Porter et al. (2009)

Org hierarchy versus informal network

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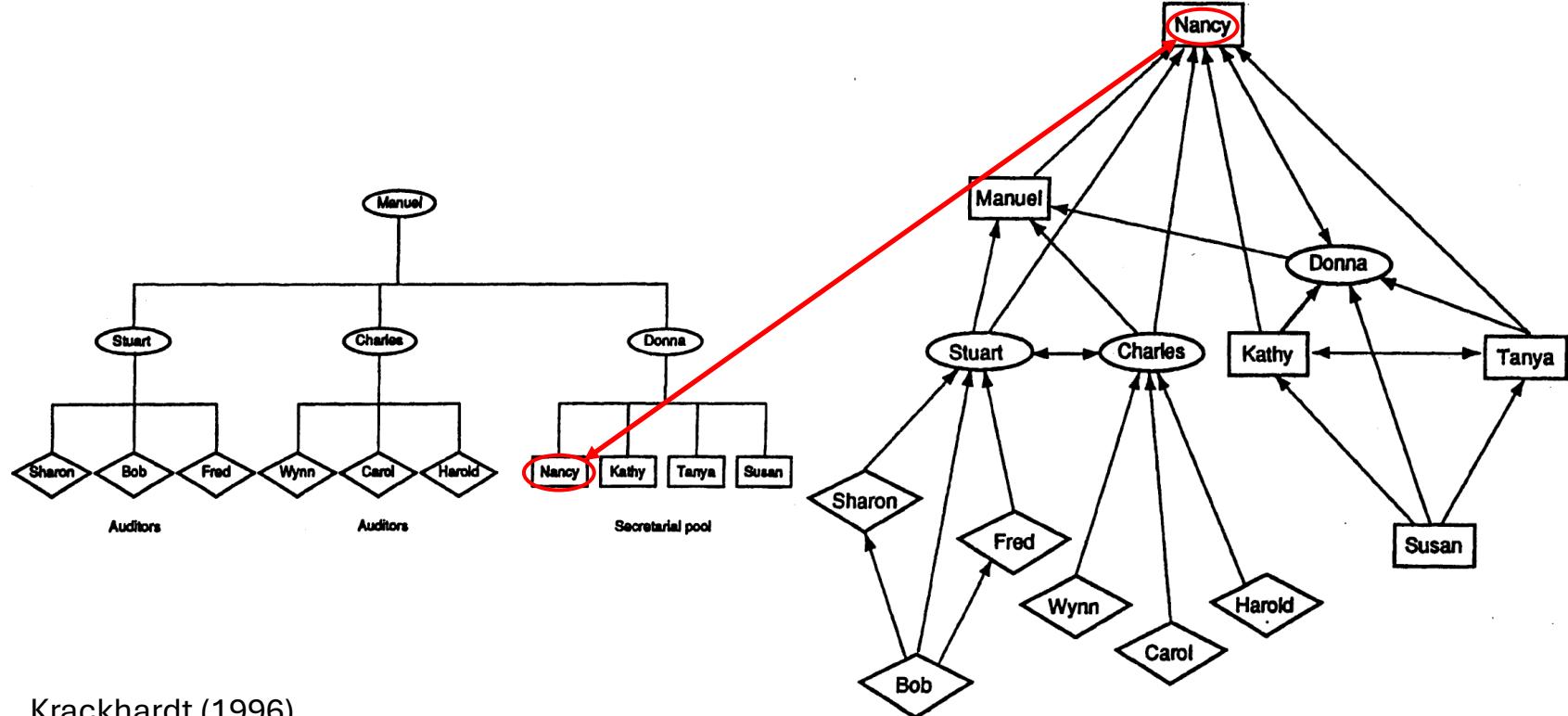
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Krackhardt (1996)

Not dating a ex's ex in a high school

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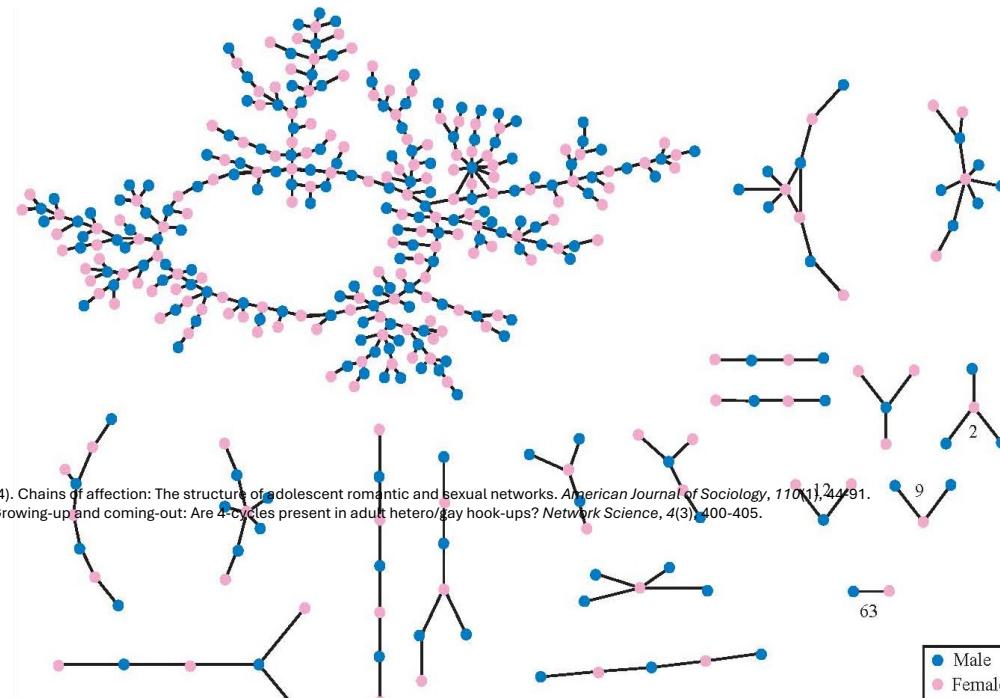
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Bearman et al. (2004); Marcum et al. (2016)

Shared events among southern debutants

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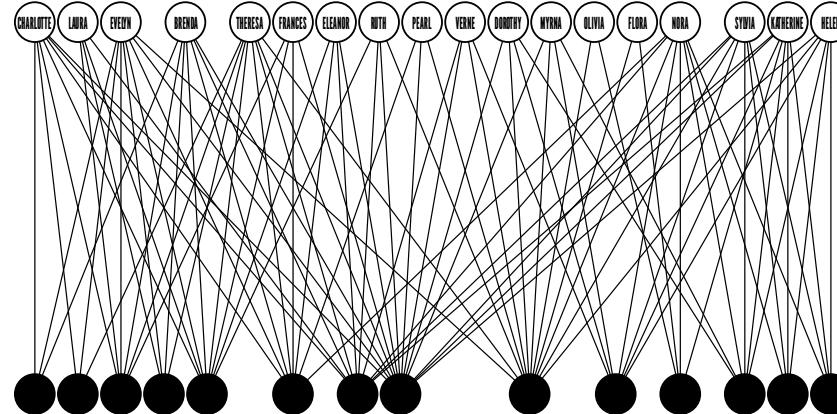
Basic network terms

Heuristic analysis

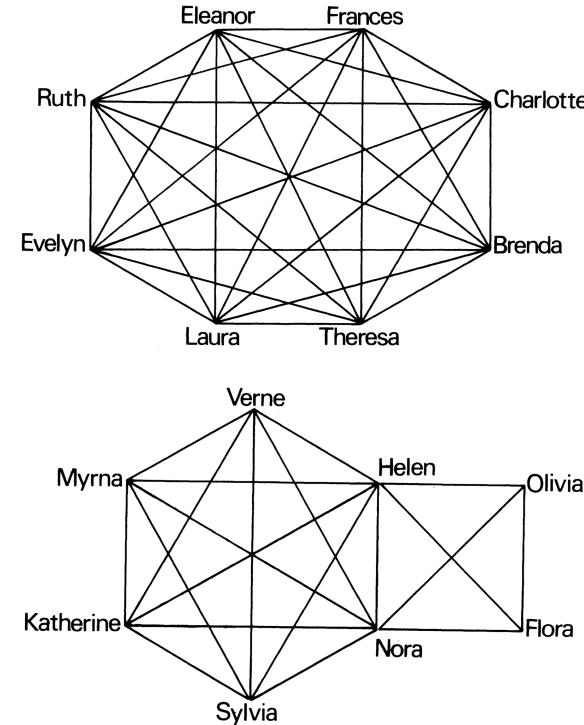
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Davis & Gardner (1941); Breiger (1974)



(Same principles was behind recommendations for about a decade)

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Customers who bought this item also bought

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Observe, Collect, Draw!: A Visual Journal
› Giorgia Lupi
Diary
\$12.76



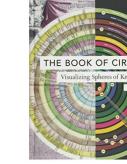
Dear Data Postcard Kit: For Two Friends to Draw and Share
Giorgia Lupi
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Medieval Moscow at center of river trade (Pitts, 1978/1979)

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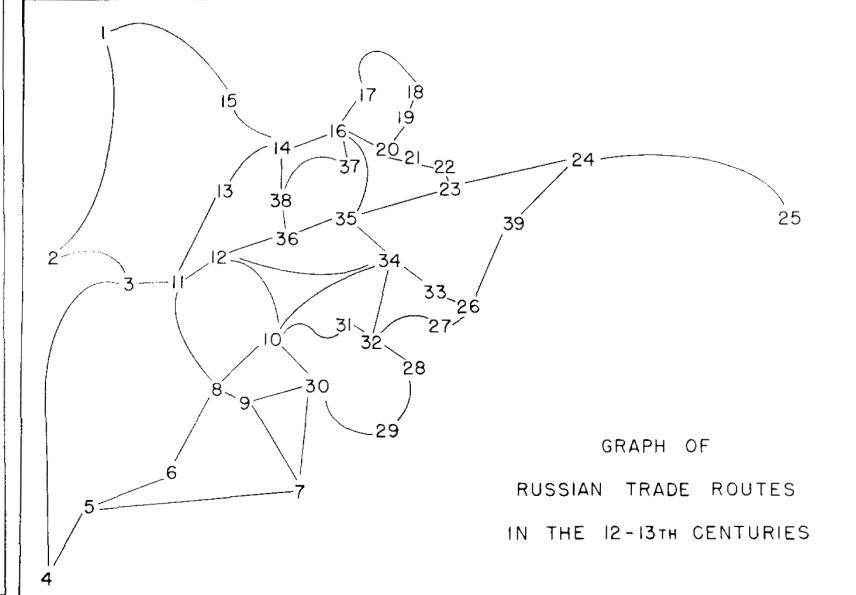
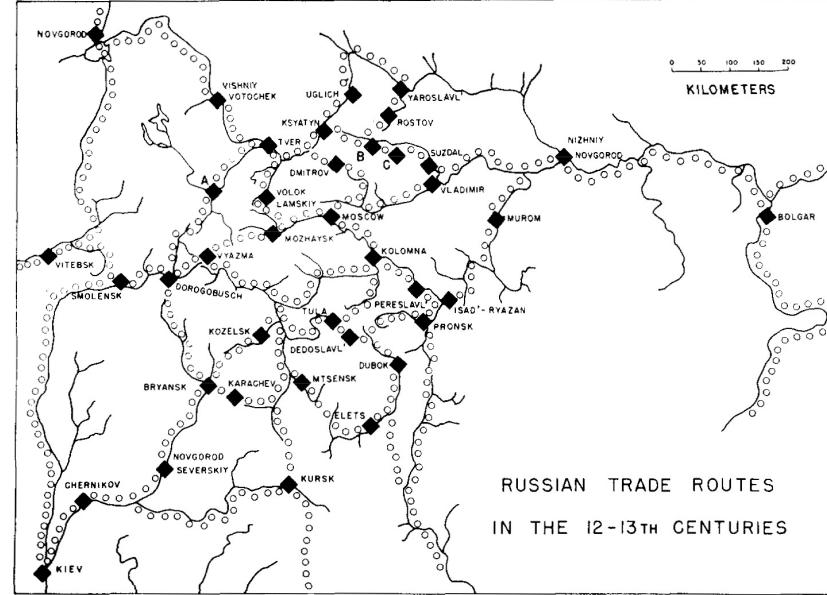
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Pitts (1978/1979)

Similar idea (centrality) behind original Pagerank

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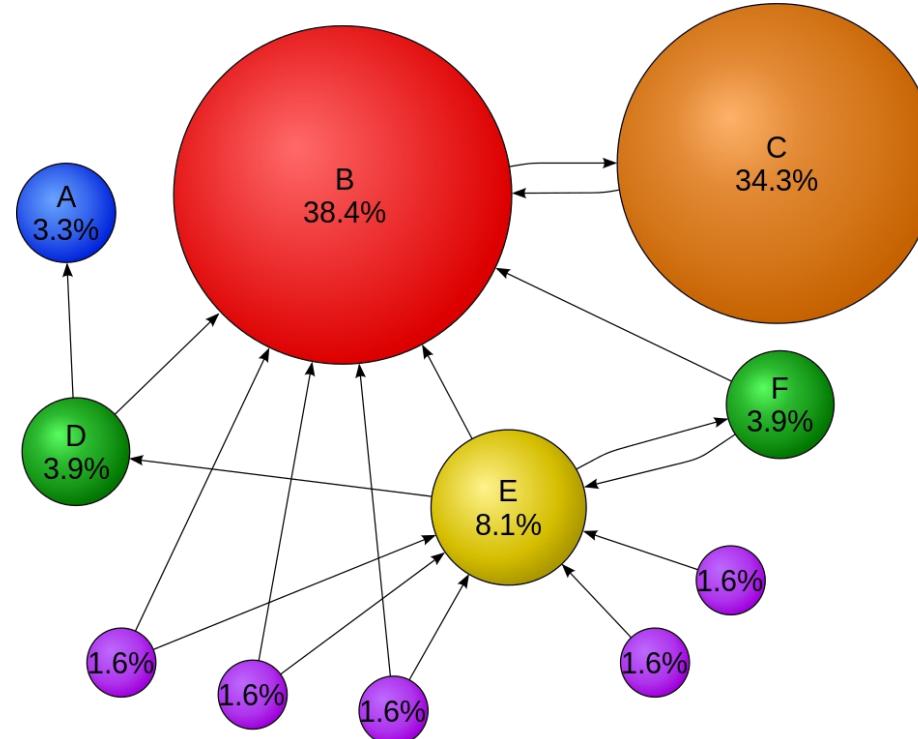
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Notice also problems

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- Ella Fitzgerald may have been one of the girls studied among “runaways”! (she was at the same training school at the same time) (Immarigeon, 2014; Cherry, 1995)
- Managers who surveil employee networks may get strategic information
- Surveillance into teens’ sexuality??
- Social network analysis, at least at some points, was used heavily by the US military in counterinsurgency (Knobe, 2013; Mac Ginty, 2010)
- The idea that the most important information is in the *structure*, and we can ignore the content, is limiting

Places used

- Basic research in sociology, anthropology, social psychology, epidemiology
- US military
- Organizational behavior, management science
- “Complexity science”, sociophysics, “computational social science”
- (Are also networks in operations research and optimization, and in computer science research, but those are less relevant)

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Representations of networks

A “network” can be formed by any sort of relations (but be careful of similarities)

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	Similarities			Social Relations				Interactions	Flows
Disclaimers	Location e.g., Same spatial and temporal space	Membership e.g., Same clubs	Attribute e.g., Same gender	Kinship e.g., Mother of Sibling of	Other role e.g., Friend of Boss of Student of Competitor of	Affective e.g., Likes Hates etc.	Cognitive e.g., Knows Knows about Sees as happy etc.	e.g., Sex with Talked to Advice to Helped Harmed etc.	e.g., Information Beliefs Personnel Resources etc.
Basic network terms	Same events	Same attitude	etc.						
Heuristic analysis	etc.	etc.	etc.						
Statistical analysis									
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Borgatti et al. (2009)

Getting network data

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- Survey instruments: include “name generators”
 - Are now some nice digital tools for this (e.g., Network Canvas)
- Observation
- Administrative data
 - Includes co-authorships or citations (bibliometrics/scientometrics), org charts, attendance
- Digital trace data: Tempting but dangerous!
- Similarity data (including correlations between variables): BAD!!

Key representations: Graph; adjacency matrix; edgelist

Why networks?

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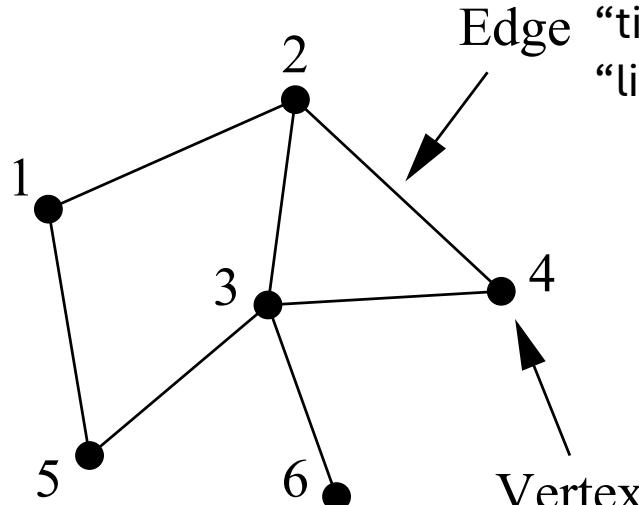
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$$\mathbf{A} = \begin{pmatrix} 0 & 1 & 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 & 1 \\ 0 & 1 & 1 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \end{pmatrix}$$

Newman (2010)

Edgelist shows, we go from n to n^2

	Y	X_1	X_2	\dots	X_k
v_1	y_1	x_{11}	x_{12}	\dots	x_{1k}
v_2	y_2	x_{21}	x_{22}	\dots	x_{2k}
\vdots	\vdots	\vdots	\vdots	\ddots	\vdots
v_n	y_n	x_{n1}	x_{n2}	\dots	x_{nk}



	<i>from</i>	<i>to</i>	Y	W_1	W_2	W_3	\dots	
	e_1	v_1	v_2	y_{12}	$\mathbb{1}(x_{11} = x_{21})$	$x_{12} - x_{22}$	x_{13}	\dots
Heuristic analysis	e_2	v_2	y_3	y_{23}	$\mathbb{1}(x_{11} = x_{31})$	$x_{12} - x_{32}$	x_{13}	\dots
	\vdots	\vdots	\vdots	\vdots	\vdots	\vdots	\vdots	
Statistical analysis	e_{n+1}	v_2	v_1	y_{21}	$\mathbb{1}(x_{21} = x_{11})$	$x_{22} - x_{12}$	x_{23}	\dots
	\vdots	\vdots	\vdots	\vdots	\vdots	\vdots	\vdots	
Conclusions	$e_{2\binom{n}{2}}$	v_{n-1}	v_n	$y_{(n-1)n}$	$\mathbb{1}(x_{(n-1)1} = x_{n1})$	$x_{(n-1)2} - x_{n2}$	$x_{(n-1)3}$	\dots



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1: I have a limited perspective

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- I mostly stopped working with networks in 2019, so my knowledge may be outdated by a few years
- The social networks world is overwhelmingly white (one of the reasons I increasingly lost interest); there probably is critical race work, but based on my training, I don't know it
 - Jacob Moreno, the first inventor of social network analysis, was purportedly an egomaniac (why SNA died for a few decades after him)
 - Harrison White's 1970s group at Harvard: lots of sexism (Edling, 2009)? Where most of the current field leadership came out of

2: Graphs are an overloaded representation

Why networks?

Representation of networks

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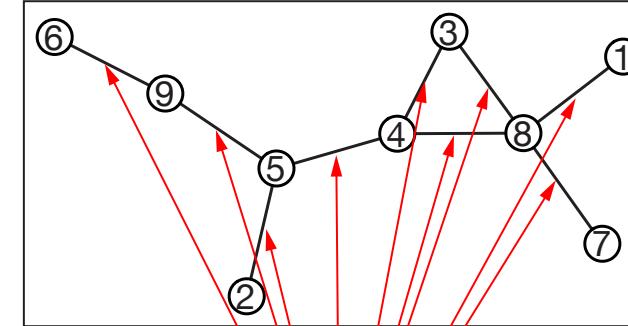
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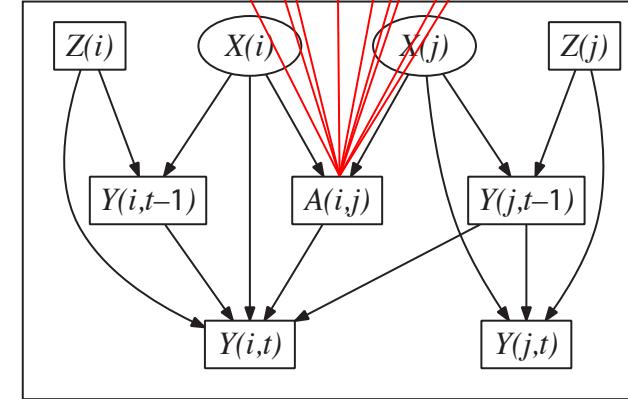
Statistical analysis

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Network mode (observations)



Graphical
model
(variables), e.g.
representing
causality



Note: This is also a Markov chain, as it has a tie from $Y(t-1)$ to $Y(t)$. Markov chains are themselves graphs, but also have *transition* graphs, which is yet another type of graph.

Bottom: Shalizi & Thomas (2009)

3: Networks are similarities (heatmaps can be used), but similarities are not networks

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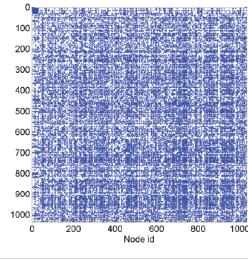
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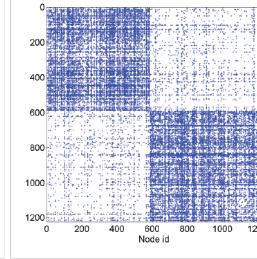
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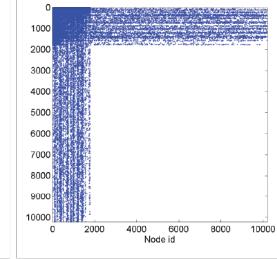
Works cited



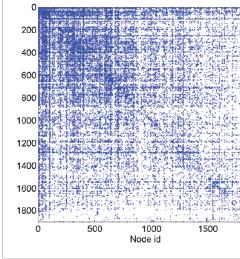
(a) facebook107



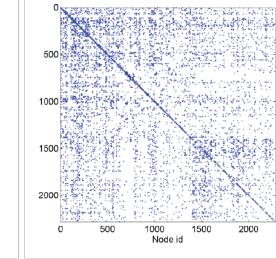
(b) polblogs



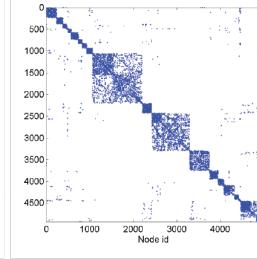
(c) USairport



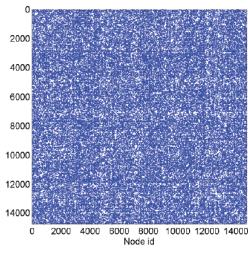
(d) UC Irvine



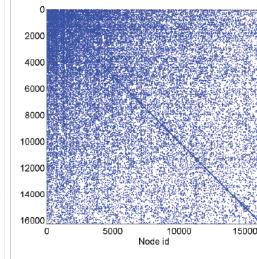
(e) yeast



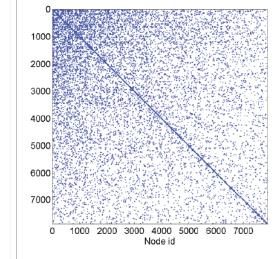
(f) USpower



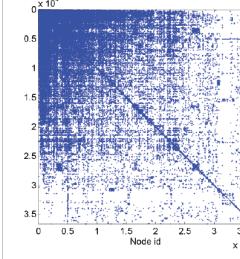
(g) IMDB



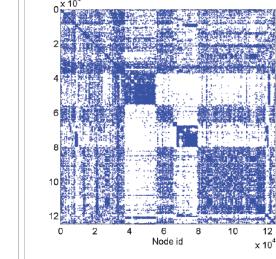
(h) cond-mat1



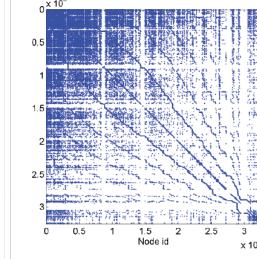
(i) cond-mat2



(j) enron



(k) internet



(l) www

Caron & Fox (2015)

Theoretical benefits...?

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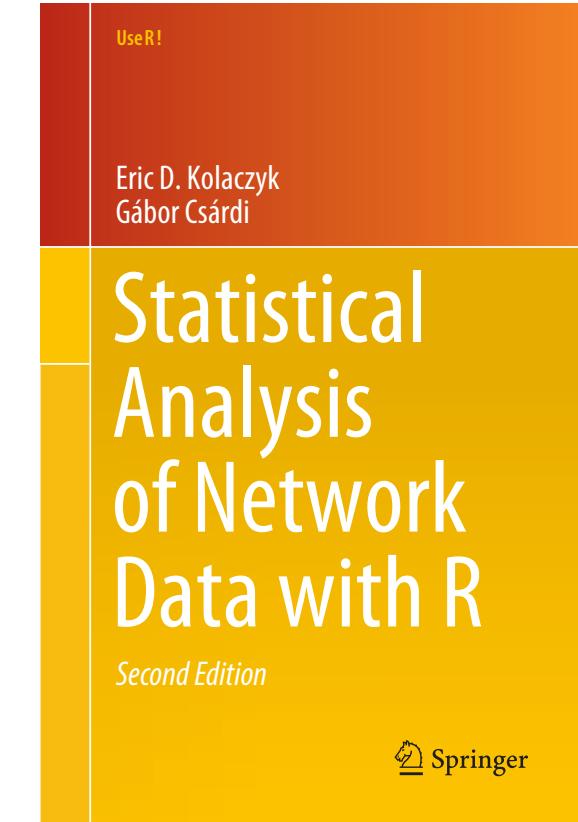
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Works cited

Basic network terms

To work through some of these in R, following Kolaczyk & Csárdi (2020)

- Directed and undirected
- Multigraph
- Weighted
- Bipartite; projection
- Ego and alters
- Ego network
- Neighbors, incident, walks
- Connected components (strong and weak)
- Induced subgraph
- Degree distribution
- Node properties vs edge properties
- Graph motifs: k -stars, trees, triads
- Triad census
- Community detection
- Density, diameter



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Download data

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- https://www.stats.ox.ac.uk/~snijders/siena/Lazega_Lawyers.zip
- Install igraph in R
- Optional: download Cytoscape

Other software

- Pajek: Windows-only (I once successfully used Wine for Macs, but it was tricky) GUI software that is really powerful for big networks. Some really nice features (connected components layout), but very user-hostile. Is a book about it
- Gephi: Was abandoned then revived. Lite web version
- Cytoscape: Mostly for biology, but I switched to it when Gephi was abandoned, and still use it

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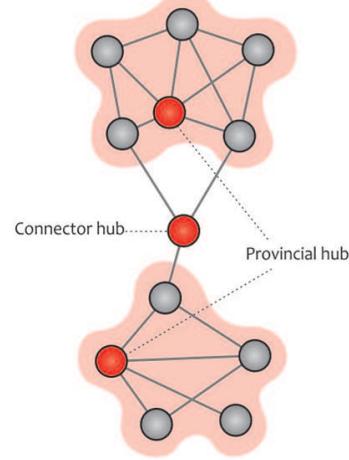
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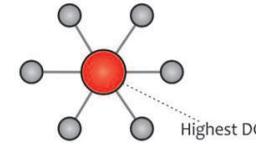
A

Centrality and hubs

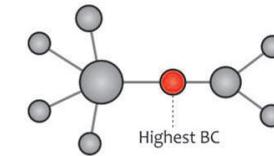


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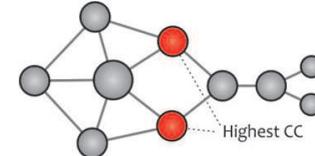
Degree centrality



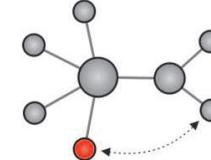
Betweenness centrality



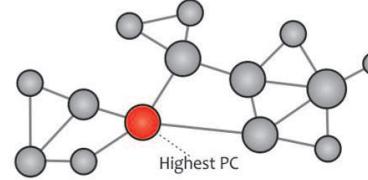
Closeness centrality



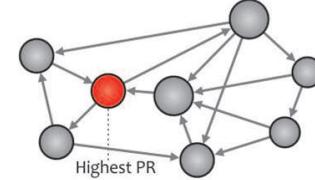
Eigenvector centrality



Participation coefficient



PageRank



Increasing nodal degree

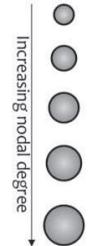
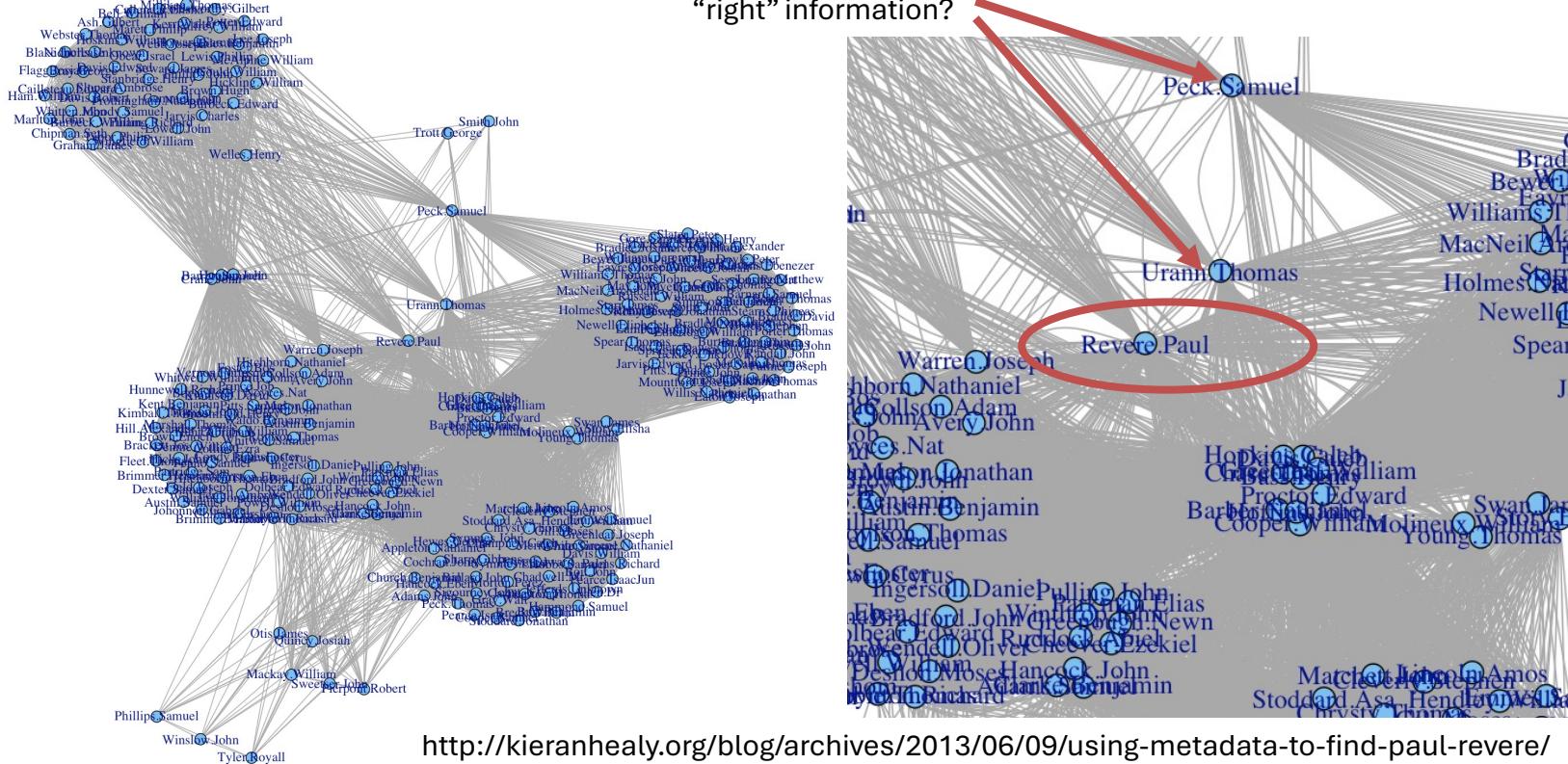


Image: Farahani, F. V., Karwowski, W., & Lighthall, N. R. (2019). Application of graph theory for identifying connectivity patterns in human brain networks: A systematic review. *Frontiers in Neuroscience*, 13, 585. <https://doi.org/10.3389/fnins.2019.00585>

Problems: Retrospective, just-so storytelling

Important but neglected historically? Or is the network diagram not capturing the

Important but neglected historically? Or is the network diagram not capturing the “right” information?



Clustering and “blocks”

Why networks?

Representation of networks

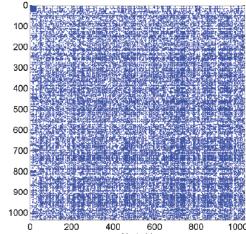
Disclaimers

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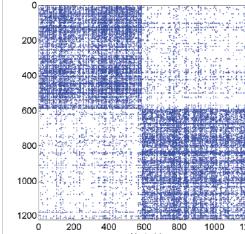
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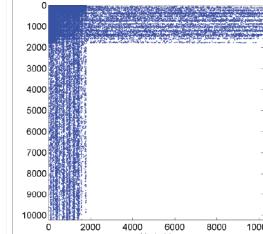
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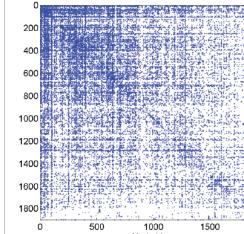
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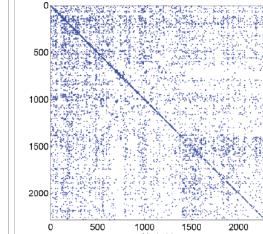
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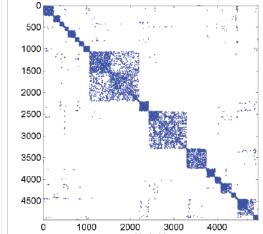
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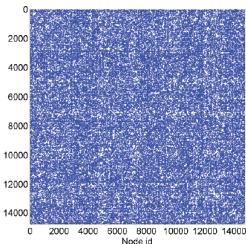
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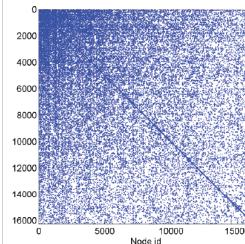
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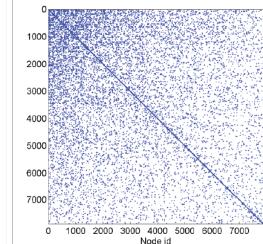
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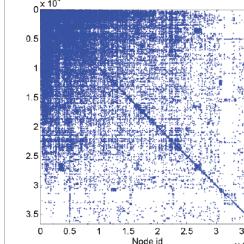
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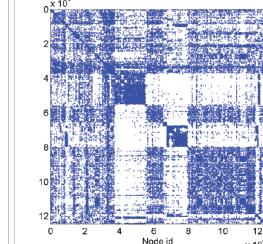
(h) cond-mat1



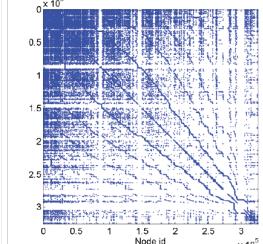
(i) cond-mat2



(j) enron



(k) internet



(l) www

Caron & Fox (2015)

Visualization

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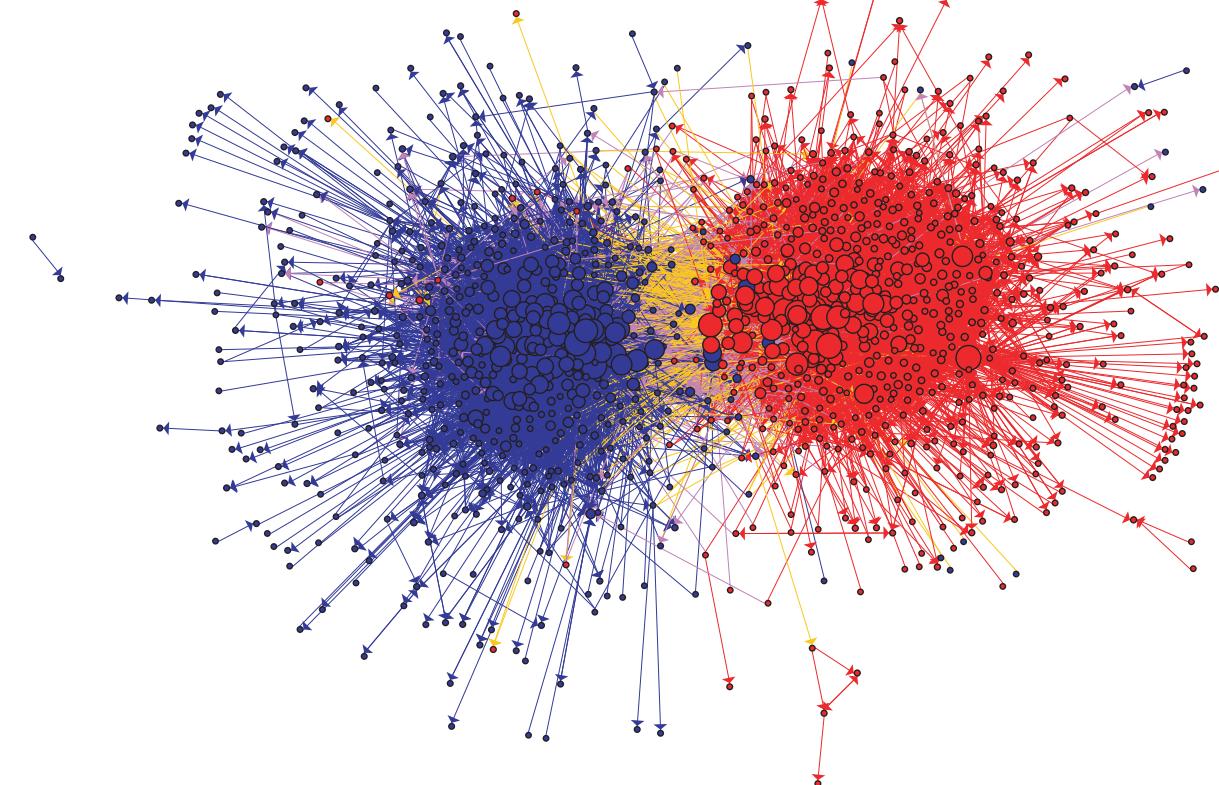
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Adamic & Glance (2005); Foucault Welles (2014)

Problems: “Spaghetti”

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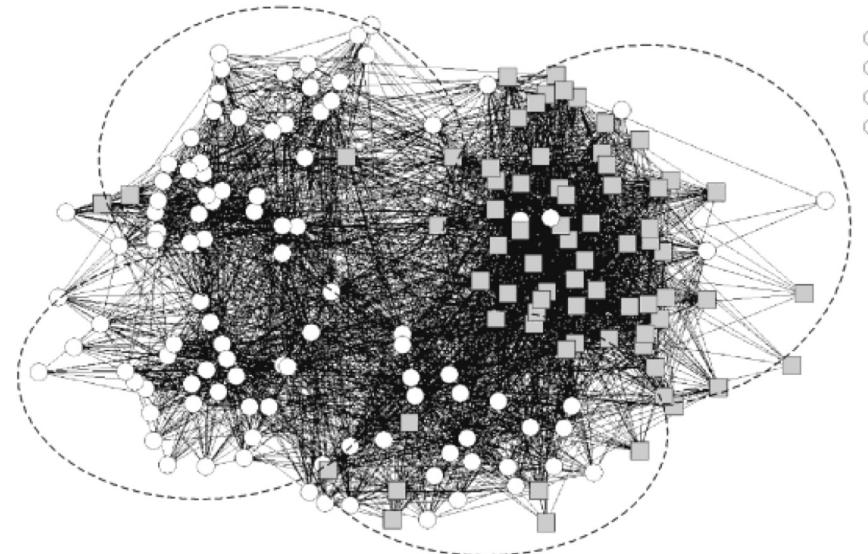
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Durland (2005)

Problems: This image was massaged (17-core) until it showed something

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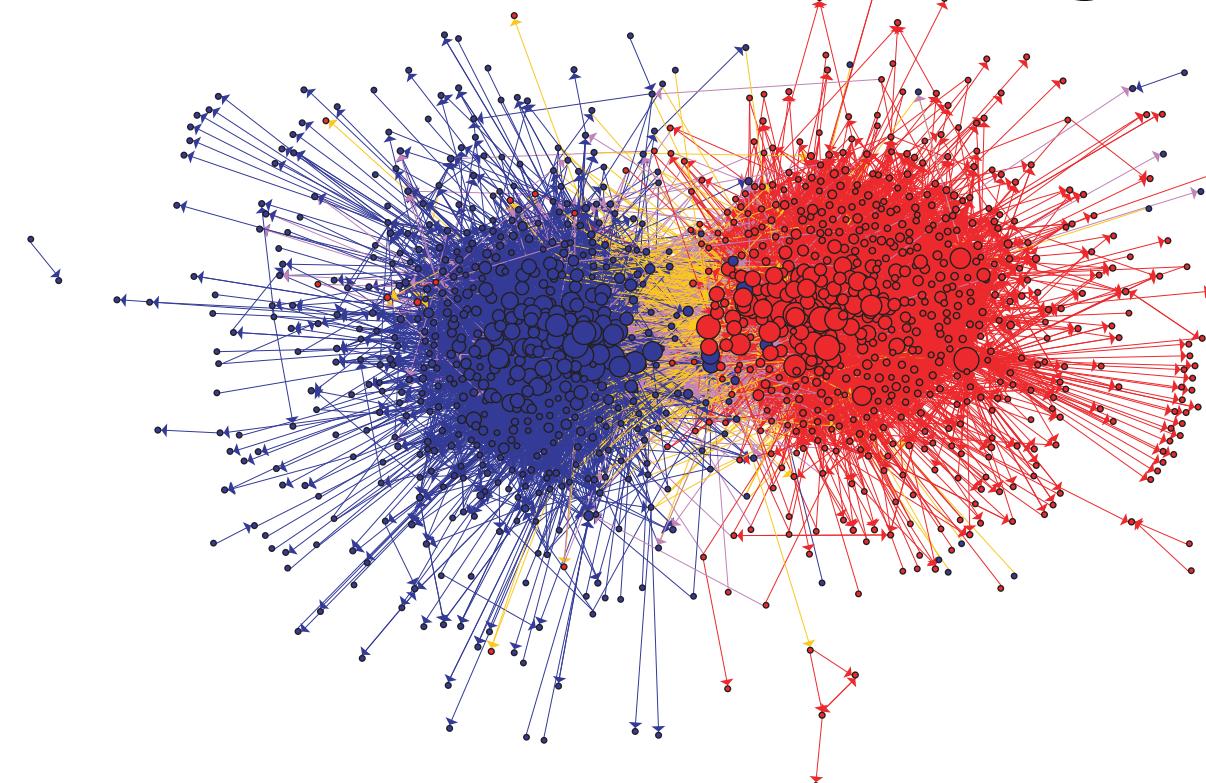
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Adamic & Glance (2005); Foucault Welles (2014)

Problems: Bad visualization

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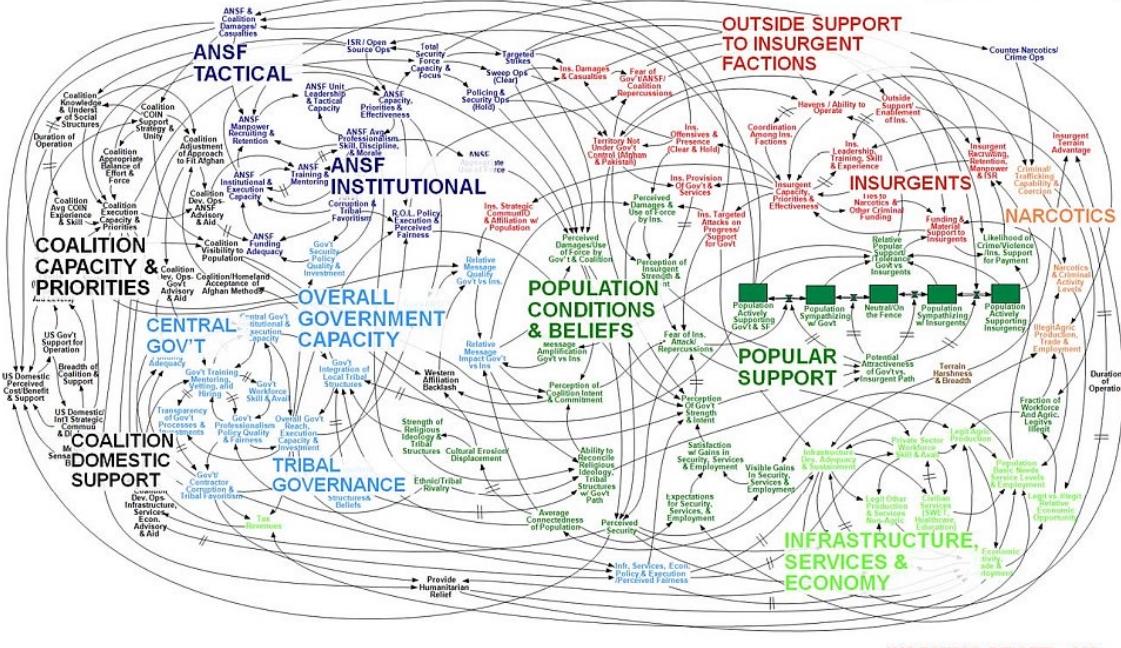
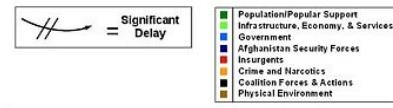
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Afghanistan Stability / COIN Dynamics





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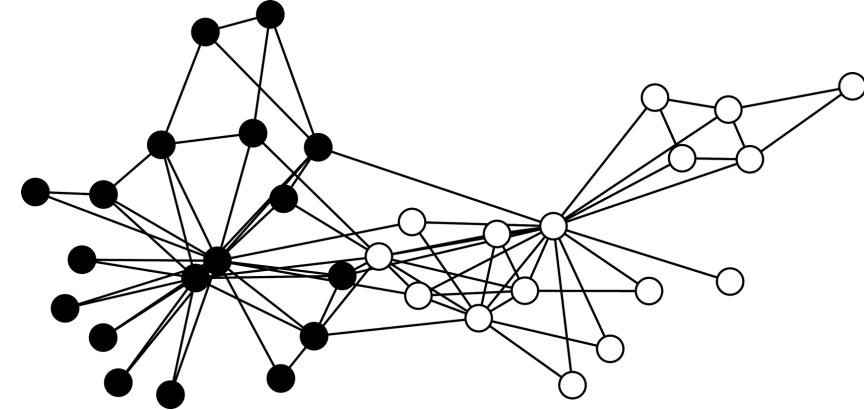
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	Y	X_1	X_2	\dots	X_k
v_1	y_1	x_{11}	x_{12}	\dots	x_{1k}
v_2	y_2	x_{21}	x_{22}	\dots	x_{2k}
\vdots	\vdots	\vdots	\vdots	\ddots	\vdots
v_n	y_n	x_{n1}	x_{n2}	\dots	x_{nk}



Social scientists: “Obvious” first pass

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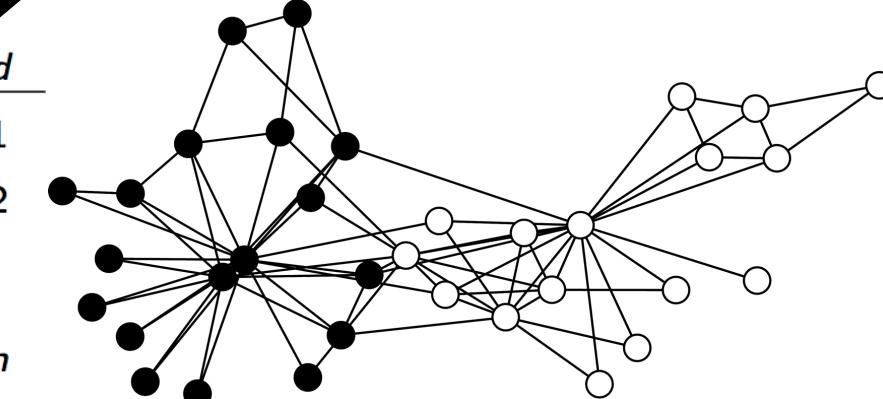
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	Y	X_1	X_2	\dots	X_k	C_d
v_1	y_1	x_{11}	x_{12}	\dots	x_{1k}	d_1
v_2	y_2	x_{21}	x_{22}	\dots	x_{2k}	d_2
\vdots	\vdots	\vdots	\vdots	\ddots	\vdots	\vdots
v_n	y_n	x_{n1}	x_{n2}	\dots	x_{nk}	d_n

The problem for statisticians

- *Ceteris paribus* (“holding all else constant”) interpretation
- How do we change the (undirected) degree of one node (or some centrality like eigenvector, betweenness, closeness) and hold those of all other nodes constant
- Deeper question: **what are we trying model?**

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What are we trying to model?

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- Centralities are a very crass way of capturing network structure
 - Are a *by-product* of network structure/processes, not what produces them
- Even if we have a directed graph, e.g. an advice network,
 - Modeling in-degree centrality would be getting at who is sought out
 - But not *by whom*
 - Out-degree centrality would be getting at who seeks out advice
 - But not *from whom*
- Model the *process* also to manage dependencies

Network: explanatory or response?

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Network as cause? (as explanatory/IV?)

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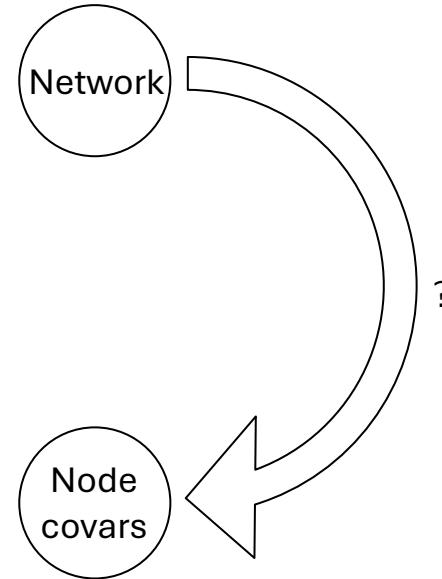
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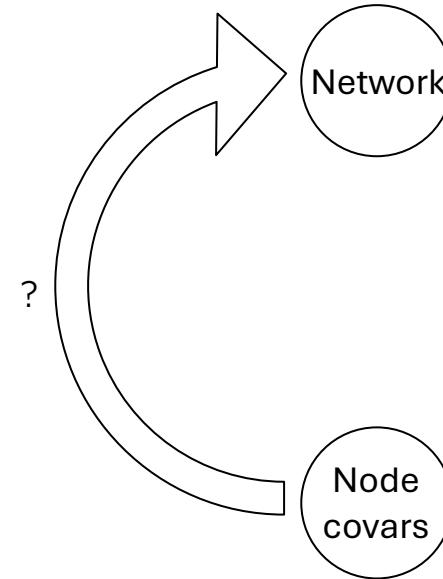
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Network as effect? (as response/DV?)



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The problem: both happen.

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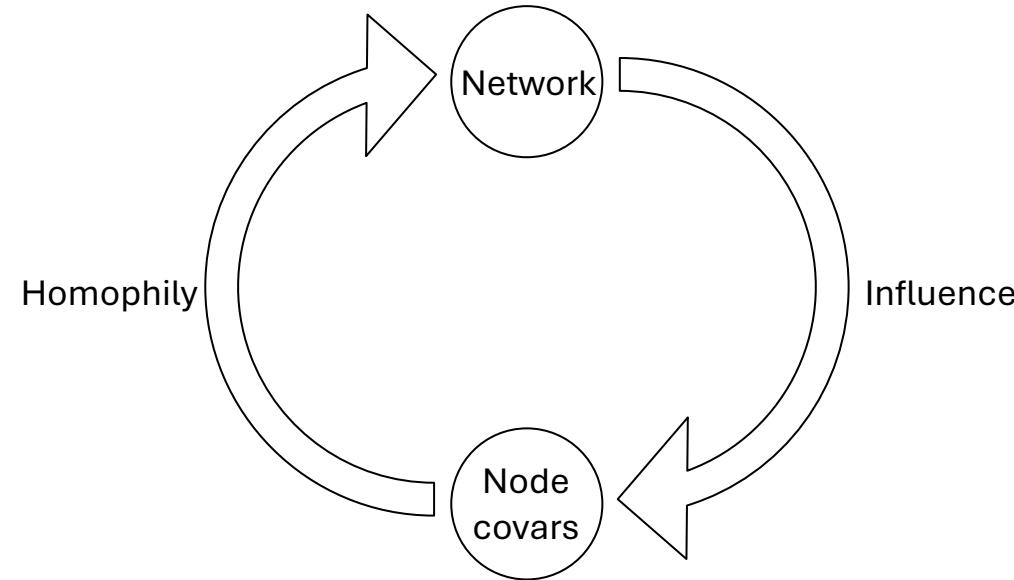
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And they aren't the only things.

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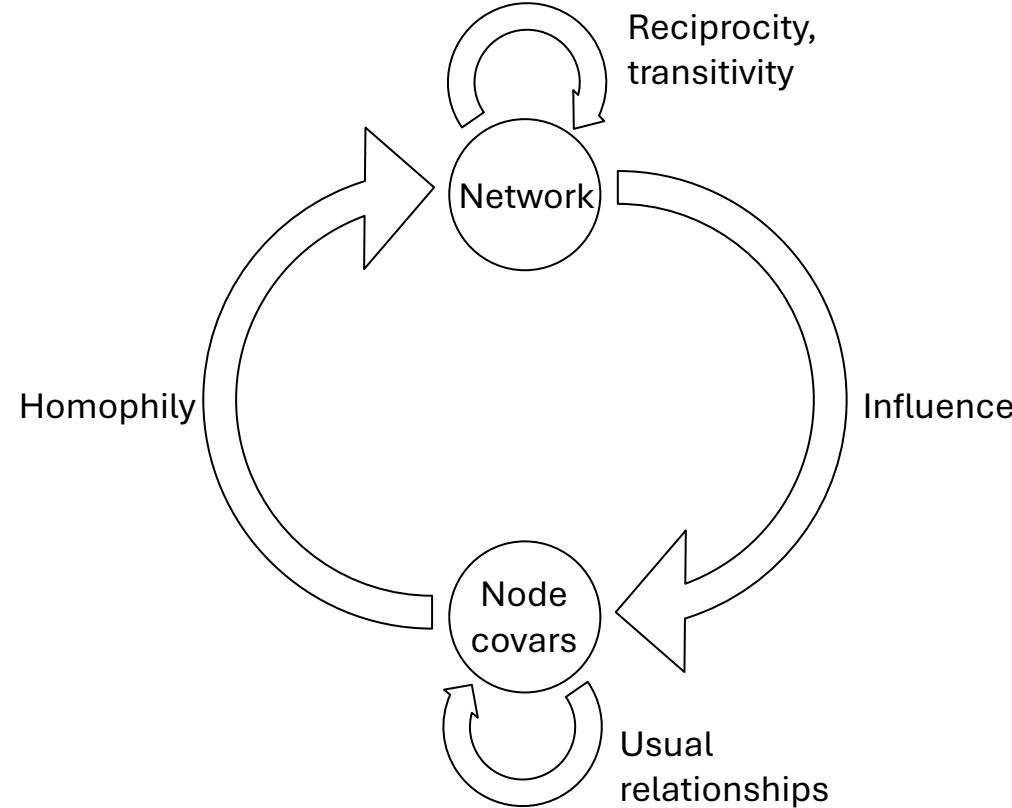
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Technical vocabulary

- “Model misspecification”
 - The wrong functional form, and/or
 - The wrong variables
- Omitted variable bias (OVB)
- Synonymous: “Non-iid data,” “dependent data,” “autocorrelation,” “endogeneity,” “pseudoreplication”

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Dependencies

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- From Wikipedia: “Asking two people in the same household whether they watch TV, for example, does not give you statistically independent answers. The sample size, n , for independent observations in this case is one, not two.”
- Networks are an interconnected entity, and **statistics cannot do anything with an n of 1.**
- So we have to make independence assumptions
- See <https://www.mominmalik.com/sunbelt2019.pdf>

Models of network structure

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	Y	X_1	X_2	\dots	X_d
1	y_1	x_{11}	x_{12}	\dots	x_{1d}
2	y_2	x_{21}	x_{22}	\dots	x_{2d}
\vdots	\vdots	\vdots	\vdots	\ddots	\vdots
n	y_n	x_{n1}	x_{n2}	\dots	x_{nd}



	$index$	$from$	to	Y	W_1	W_2	W_3	\dots
Heuristic analysis	e_1	1	2	y_{12}	$\mathbf{1}(x_{11} = x_{21})$	$x_{12} - x_{22}$	x_{13}	\dots
	e_2	2	3	y_{23}	$\mathbf{1}(x_{11} = x_{31})$	$x_{12} - x_{32}$	x_{13}	\dots
	\vdots	\vdots	\vdots	\vdots	\vdots	\vdots	\vdots	\vdots
Statistical analysis	e_{n+1}	2	1	y_{21}	$\mathbf{1}(x_{21} = x_{11})$	$x_{22} - x_{12}$	x_{23}	\dots
	\vdots	\vdots	\vdots	\vdots	\vdots	\vdots	\vdots	\vdots
Conclusions	$e_{2\binom{n}{2}}$	$n-1$	n	$y_{(n-1)n}$	$\mathbf{1}(x_{(n-1)1} = x_{n1})$	$x_{(n-1)2} - x_{n2}$	$x_{(n-1)3}$	\dots

Model the edges

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- For maybe two years, I didn't realize that you actually transform your data set
- The edges are dependencies between observations
- Problem: the edges are dependent, too!
- Transitivity, reciprocity, Dunbar's number: these are dependencies between dependencies
- Not only are we not measuring important forces, but we assume them away (get OVB!)
- (Useful language: “dyad dependent” vs. “dyad independent”)

Exponential[-family] Random Graph Models (ERGMs)

- The crown jewel of 30+ years of research, came out of p2 model
- (Main version treats graphs as the response: graphs as explanatory are called “autologistic actor attribute models” [ALAAMs], aren’t really done)
- Logic: specify a set of sufficient statistics, calculated over whole network
- These can include terms for anything you can think of
- By construction, these are the sufficient statistics for a graph. Question is if there is any weighting of these statistics that can produce the observed graph

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Terms in ERGMs

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$$S_l(y) = \sum_{1 \leq i < j \leq n} y_{ij}$$

$$S_k(y) = \sum_{1 \leq i \leq n} \binom{y_i +}{k}$$

$$T(y) = \sum_{1 \leq i < j < h \leq n} y_{ij} y_{ih} y_{jh}$$

number of edges

number of k -stars ($k \geq 2$)

number of triangles

Network statistics	Description	Structural signature
Univariate parameters		
<i>Dyadic parameters</i>		
Reciprocity	Occurrence of mutual ties	
<i>Degree parameters</i>		
Mixed 2-star	Correlation of indegrees and outdegrees	
Alternating-in-star (A-in-S)	Network centralisation around indegree	
Isolate	Occurrence of actors with zero indegree and zero outdegree	
Sink	Occurrence of actors with an outdegree of zero and indegree of at least one	
<i>Triangle parameters</i>		
Multiple connectivity (A2P-T)	Multiple paths of indirect connectivity	
Shared out-ties (A2P-U)	Activity based structural equivalence: multiple sets of out-ties to the same third others	
Shared in-ties (A2P-D)	Popularity based structure equivalence: multiple sets of in-ties from the same third others	
Transitive closure (AT-T)	Transitive closure of multiple 2-paths	
Activity closure (AT-U)	Closure of multiple in-2-stars	
Popularity closure (AT-D)	Closure of multiple out-2-stars	

Simpson (2015)

ERGMs as a graphical model

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Factor graph	Parameter name	Network Motif	Parameterization	Matrix notation
	-mutual dyads		$\sum_{i < j} A_{ij} A_{ji}$	$\frac{1}{2} \text{tr}(\mathbf{AA}^T)$
	-in-two-stars		$\sum_{(i,j,k)} A_{ji} A_{ki}$	$\text{sum}(\mathbf{AA}^T) - \text{tr}(\mathbf{AA}^T)$
	-out-two-stars		$\sum_{(i,j,k)} A_{ij} A_{ik}$	$\text{sum}(\mathbf{A}^T \mathbf{A}) - \text{tr}(\mathbf{A}^T \mathbf{A})$
	-geom. weighted out-degrees		$\sum_i \exp\{-\alpha \sum_k A_{ik}\}$	$\text{sum}(\exp\{-\alpha \text{rowsum}(\mathbf{A})\})$
	-geom. weighted in-degrees		$\sum_j \exp\{-\alpha \sum_k A_{kj}\}$	$\text{sum}(\exp\{-\alpha \text{colsum}(\mathbf{A})\})$
	-alternating transitive k-triplets		$\lambda \sum_{i,j} A_{ij} \left\{ 1 - \left(1 - \frac{1}{\lambda}\right) \sum_{k \neq i,j} A_{ik} A_{kj} \right\}$	$\lambda \text{sum}(\mathbf{A}^{(1)} \left(1 - \left(1 - \frac{1}{\lambda}\right) \mathbf{AA} - \text{diag}(\mathbf{AA}) \right))$
	-alternating indep. two-paths		$\lambda \sum_{i,j} \left\{ 1 - \left(1 - \frac{1}{\lambda}\right) \sum_{k \neq i,j} A_{ik} A_{kj} \right\}$	$\lambda \text{sum} \left(1 - \left(1 - \frac{1}{\lambda}\right) \mathbf{AA} - \text{diag}(\mathbf{AA}) \right)$
	-two-paths (mixed two-stars)		$\sum_{(i,k,j)} A_{ij} A_{ik} A_{kj}$	$\text{sum}(\mathbf{AA}) - \text{tr}(\mathbf{AA})$
	-transitive triads		$\sum_{(i,j,k)} A_{ij} A_{jk} A_{ik}$	$\text{tr}(\mathbf{AAA}^T)$
	-activity effect		$\sum_i X_i \sum_j A_{ij}$	$\text{sum}(\mathbf{X}^{(1)} \text{rowsum}(\mathbf{A}))$
	-popularity effect		$\sum_j X_j \sum_i A_{ij}$	$\text{sum}(\mathbf{X}^{(1)} \text{colsum}(\mathbf{A}))$
	-similarity effect		$\sum_{i,j} A_{ij} \left(1 - \frac{ X_i - X_j }{\max_{k,l} X_k - X_l } \right)$	$\text{sum}(\mathbf{A}^{(1)} \mathbf{S})$

ERGMs: Procedure

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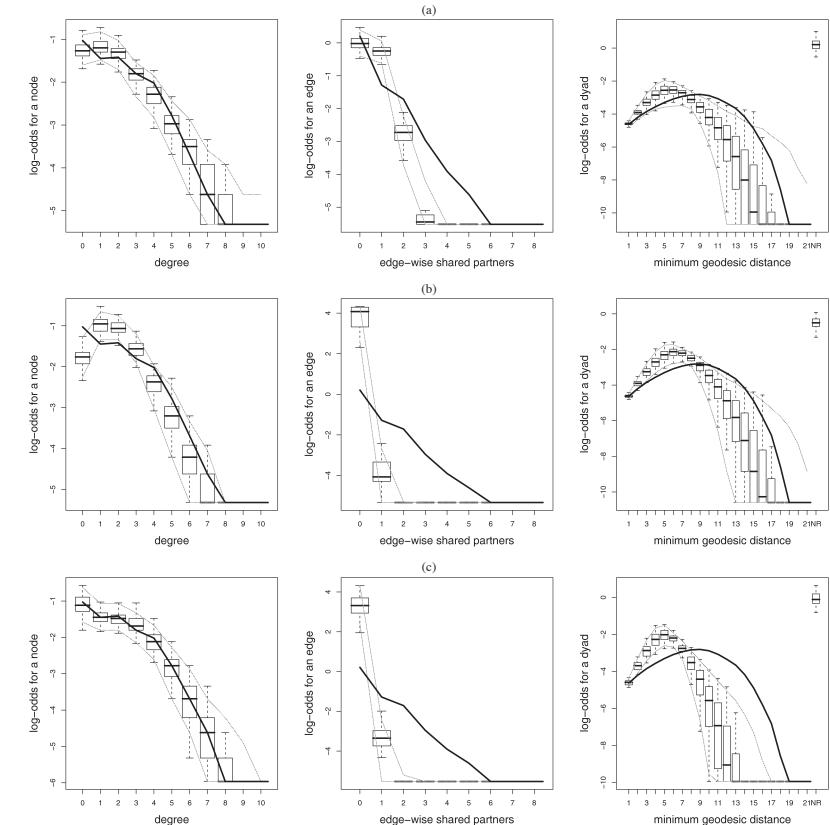
Conclusions

- Take the observed graph, do counts of sufficient statistics, and initialize weights of terms (through logistic regression)
- Holding the rest of the graph constant, consider a single edge.
- How would removing this edge (if present) or adding it (if absent) change the count of sufficient statistics? Would a higher/lower count make the graph more likely based on current weights?
- If yes, adjust weights so that the observed graph remains most likely.
- Do this for some time to explore the parameter space (an MCMC procedure)
- At the end: if the terms put in were indeed the “correct” ones, these would be their weights

ERGMs: Goodness-of-fit testing

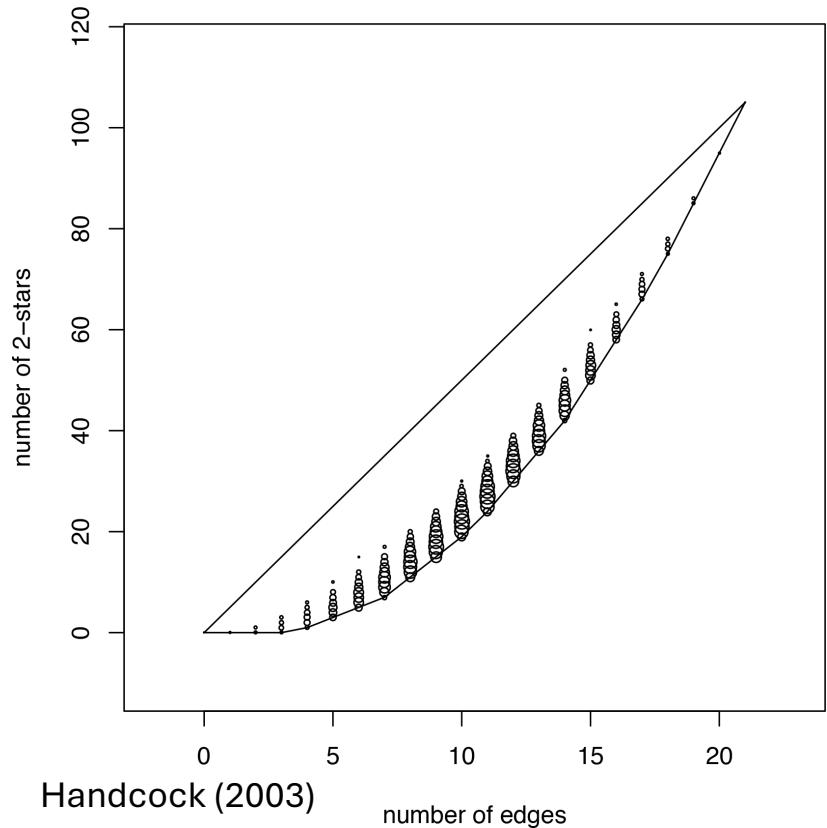
- Excellent goodness-of-fit (GOF) testing framework.
- See if the sufficient statistics that you put into the model can recover the distribution of statistics that were not among your sufficient statistics
- E.g., can density, reciprocity and transitivity alone as sufficient statistics recover the graph's degree distribution?
- Can test with anything (e.g., any subgraph/graph motif density), but should be theoretically important
- Gives a complete framework for finding a parsimonious explanation

Adamic & Glance (2005); Foucault Welles (2014)



ERGMs: The bad news

- LOTS of problems.
- The space of graphs doesn't play nice with probabilities
- There are only a certain number of graphs of any given size, and only a certain number of graphs with a combination of sufficient statistics
- Slight differences in sampling frame can vastly change results (Shalizi & Rinaldo, 2013)



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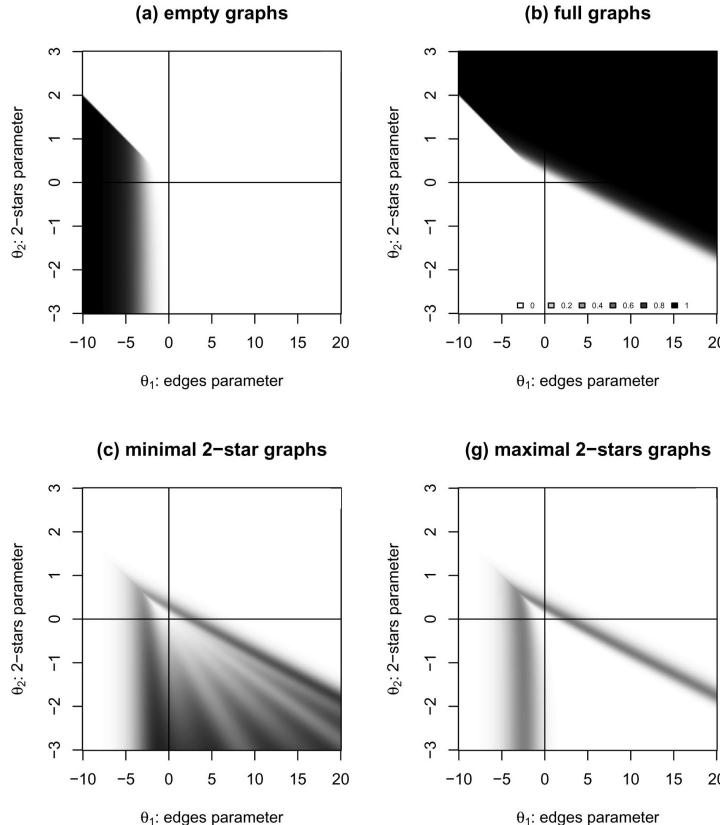
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- Sometimes, under large portions of the parameter space, the most likely graph is either the complete graph or the empty graph: such specifications are *degenerate*
- Because the space of graphs is so large, don't know if a model is degenerate or if our MCMC procedure is bad
- Model degeneracy (arguably) has nothing to do with the social phenomena of interest
- Better specifications are (arguably) technical, not sociological, entities: e.g., “geometrically weighted edgewise shared partners”

Models to avoid

- Comparing to an Erdős-Renyi random graph: Don't do
- QAP: Don't use
- Configuration model: Don't use
- Graph neural networks are only random-walk based: Don't use
- Small world networks, preferential attachment: aren't actual *models*, just isolated mechanism (and don't use them as a null model, either)
- Network autocorrelation: On the margin. Treats networks as a nuisance parameter

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- Latent space models: They “work” (statistically), but I find them useless
- Stochastic Block Models: Use, sometimes
- Relational event models: ERGMs for event data, as legit (or not) as ERGMs
- Stochastic Actor-Oriented Models: Similar to ERGMs but require timesteps, use something like agent-based simulation to fit parameters of a statistical models. Are also version of these for event data. Maybe the most statistically sophisticated and principled model



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- Networks (network science) had a lot of hype in the 2000s, much of which came from physicists (statistical mechanics) colonizing social science spaces and topics and methods, but that has mostly been eclipsed by ML and AI
- Network analysis is a specialized area, even if it cuts across disciplines; it is possible to have a few tools in your toolkit, but it can be hard to engage with the entirety of the literature without specific study

Take-aways

- Everything is terrible and nothing works... quantitatively
- Qualitative network analysis can use quantitative tools: to tell stories, to visualize networks to talk about them with research participants, to do *interpretive* analysis (heuristics might *coincide*, and so can be used to present, but I think hermeneutics are distinct from heuristics)

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Your next steps

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- Work through Kolaczyk & Csárdi, *Statistical Analysis of Network Data with R* (2nd edition). After using i graph to manipulate networks, they go over loading older R packages and running ERGMs and other models; all sections are great as a tutorial
- Learn to use Gephi and/or Cytoscape for visual interactive analysis
- Find places to get network data and incorporate into your work

Works Cited

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