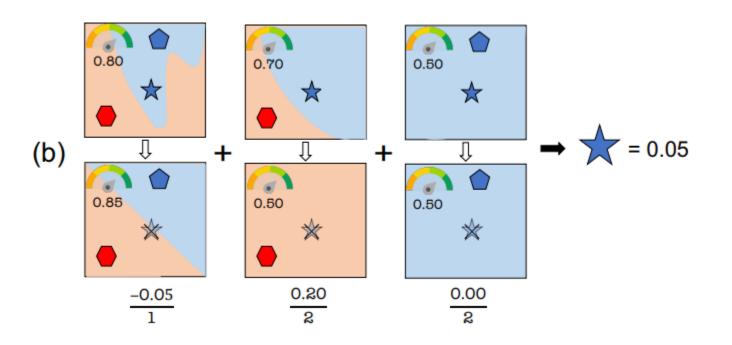
### FML论文分享

11.30

Evaluate data by Shapley value 《 What is your data worth? Equitable Valuation of Data 》



### How to evaluate shapley value

$$s_i = \frac{1}{N!} \sum_{\pi \in \Pi(D)} \left[ U(P_i^{\pi} \cup \{i\}) - U(P_i^{\pi}) \right]$$

$$s_i = \sum_{S \subseteq I \setminus \{i\}} \frac{1}{N\binom{N-1}{|S|}} \left[ U(S \cup \{i\}) - U(S) \right]$$

### Truncated Monte Carlo Shapley

#### **Algorithm 1 Truncated Monte Carlo Shapley**

```
Input: Train data D = \{1, \dots, n\}, learning algorithm \mathcal{A}, performance score V
Output: Shapley value of training points: \phi_1, \ldots, \phi_n
Initialize \phi_i = 0 for i = 1, ..., n and t = 0
while Convergence criteria not met do
   t \leftarrow t + 1
   \pi^t: Random permutation of train data points
   v_0^t \leftarrow V(\emptyset, \mathscr{A})
   for j \in \{1, ..., n\} do
      if |V(D) - v_{j-1}^t| < Performance Tolerance then
         v_j^t = v_{j-1}^t
      else
         v_j^t \leftarrow V(\{\pi^t[1], \dots, \pi^t[j]\}, \mathscr{A})
      end if
      \phi_{\pi^{t}[j]} \leftarrow \frac{t-1}{t} \phi_{\pi^{t-1}[j]} + \frac{1}{t} (v_{j}^{t} - v_{j-1}^{t})
   end for
end while
```

**Lemma 4.2.** Given the range of an agent's marginal contributions, r, an error bound,  $\epsilon$ , and a confidence  $1 - \delta$ , the sample size required such that  $\Pr(|\bar{\Phi}_{SRS} - \mathbb{E}[\Phi]| \ge \epsilon) \le \delta$  is:

$$m \ge \frac{\ln(2/\delta) r^2}{2 \epsilon^2} \tag{4.3}$$

$$P[\max_{i} |\hat{s}_{i} - s_{i}| \leq \epsilon] \geqslant 1 - \delta. \qquad \frac{r^{2}}{2\epsilon^{2}} \log \frac{2N}{\delta}.$$

Dog vs Fish Retraining Inception-V3 top layer 10% noisy 0.0005 0.0004 0.0003 Average 0.0002 0.0001 -- Clean Images - Noisy Images 0.0000 0.1 0.2 0.3 0.4 0.5 Noise level

Noise Level = 0.1 Value = 0.00151

Noise Level = 0.3 Value = 0.00146

Noise Level = 0.5 Value = -0.00118

## 《Towards Efficient Data Valuation Based on the Shapley Value》

**Lemma 1.** For any  $i, j \in I$ , the difference in SVs between i and j is

$$s_i - s_j = \frac{1}{N - 1} \sum_{S \subseteq I \setminus \{i, j\}} \frac{U(S \cup \{i\}) - U(S \cup \{j\})}{\binom{N - 2}{|S|}} \tag{4}$$

$$\sum_{i=1}^{N} \hat{s}_i = U_{tot} \tag{5}$$

$$|(\hat{s}_i - \hat{s}_j) - C_{i,j}| \le \epsilon/(2\sqrt{N}) \quad \forall i, j \in \{1, \dots, N\}$$
 (6)

**Theorem 3.** Algorithm 1 returns an  $(\epsilon, \delta)$ -approximation to the SV with respect to  $l_2$ -norm if the number of tests T satisfies  $T \geq 8\log\frac{N(N-1)}{2\delta}/\left((1-q_{tot}^2)h\left(\frac{\epsilon}{Zr\sqrt{N}(1-q_{tot}^2)}\right)\right)$ , where  $q_{tot} = \frac{N-2}{N}q(1) + \sum_{k=2}^{N-1}q(k)[1+\frac{2k(k-N)}{N(N-1)}]$ ,  $h(u) = (1+u)\log(1+u) - u$ ,  $Z = 2\sum_{k=1}^{N-1}\frac{1}{k}$ , and r is the range of the utility function.

#### **Algorithm 1:** Group Testing Based SV Estimation.

input: Training set -  $D = \{(x_i, y_i)\}_{i=1}^N$ , utility function  $U(\cdot)$ , the number of tests - T

**output :** The estimated SV of each training point -  $\hat{s} \in \mathbb{R}^N$ 

$$Z \leftarrow 2\sum_{k=1}^{N-1} \frac{1}{k};$$
  
 $q(k) \leftarrow \frac{1}{Z}(\frac{1}{k} + \frac{1}{N-k}) \text{ for } k = 1, \dots, N-1;$   
Initialize  $\beta_{ti} \leftarrow 0, t = 1, \dots, T, i = 1, \dots, N;$ 

for t = 1 to T do

Draw  $k \sim q(k)$ ;

for j = 1 to  $k_t$  do

Uniformly sample a length-k sequence S from  $\{1, \dots, N\}$ ;  $\beta_{ti} \leftarrow 1$  for all  $i \in S$ ;

end

$$u_t \leftarrow U(\{i: \beta_{ti} = 1\});$$

#### end

$$\Delta U_{ij} \leftarrow \frac{Z}{T} \sum_{t=1}^{T} u_t (\beta_{ti} - \beta_{tj}) \text{ for } i = 1, ..., N,$$
  
 $j = 1, ..., N \text{ and } j \geq i;$ 

Find  $\hat{s}$  by solving the feasibility problem

$$\sum_{i=1}^{N} \hat{s}_i = U(D), |(\hat{s}_i - \hat{s}_j) - \Delta U_{i,j}| \le \epsilon/(2\sqrt{N}), \forall i, j \in \{1, \dots, N\};$$

# 《Rewarding High-Quality Data via Influence for Linear Regression》

$$\begin{split} &\inf(z_j,T,\theta) = R(T,\hat{\theta}_{/j}) - R(T,\hat{\theta}). \\ &\inf(z_{test},z_j) = \frac{1}{n} \nabla_{\theta} L(z_{test},\hat{\theta}) H_{\theta}^{-1} \nabla_{\theta} L(z,\hat{\theta}) \end{split}$$

$$\partial \theta_j = \frac{1}{n} H_{\theta}^{-1} \nabla_{\theta} L(z_i, \hat{\theta}) + \frac{1}{n^2} H_{\theta}^{-1} H_i H_{\theta}^{-1} \nabla_{\theta} L(z_i, \hat{\theta})$$

$$ext{infl}(z_{ ext{test}},z) = \left( 
abla_{ heta} L(z_{ ext{test}},\hat{ heta}) + rac{1}{2} H_{ heta,z_{ ext{test}}} \cdot \partial heta 
ight) \cdot \partial heta$$

## 《Measure Contribution of Participants in Federated Learning》

 Vertical Federated Learning raises new issues for measuring contributions of multiple parties where the feature space is divided into different part

**Proposition 4.** If either of Assumption 1 and 2 holds, then the Shapley group value for a party  $g \in G$  with feature set  $X^g$  is given by

$$\phi_{X^g} = \sum_{Q \subseteq S \setminus \{j^{fed}\}} \frac{|Q|!(|S| - |Q| - 1)!}{|S|!} (\Delta_{Q \cup \{j^{fed}\}}(x) - \Delta_Q(x)),$$

where  $j^{fed}$  is the index of the united federated feature  $x^{fed}$ .