

# HW 8

## Mohsen Nabian

### Problem 1)

Sep  
Oct  
Nov  
Dec

- Production starts 12 months before selling season

- distributor places order with manufacturer six month after begining of production

| Demand | P    |
|--------|------|
| 10,000 | 0.12 |
| 12,000 | 0.15 |
| 14,000 | 0.20 |
| 16,000 | 0.25 |
| 18,000 | 0.18 |
| 20,000 | 0.1  |

dis

man

distributors sells 80\$/unit

✓ Pays 60\$/unit

Fixed Prod. Cost = 75000\$

Prod. Cost = 50\$/unit

not sold by dis

will be bought 25\$/unit

P1) Make-to-stock (no contract)

| Manufacture Produce 10000 |      |         |        |        |  |
|---------------------------|------|---------|--------|--------|--|
| Demand                    | P    | Revenue | Cost   | Profit |  |
| 10000                     | 0.12 | 600000  | 575000 | 25000  |  |
| 12000                     | 0.15 | 600000  | 575000 | 25000  |  |
| 14000                     | 0.2  | 600000  | 575000 | 25000  |  |
| 16000                     | 0.25 | 600000  | 575000 | 25000  |  |
| 18000                     | 0.18 | 600000  | 575000 | 25000  |  |
| 20000                     | 0.1  | 600000  | 575000 | 25000  |  |
| Expected Profit           |      |         |        | 25000  |  |

| Manufacture Produce 12000 |      |         |        |        |  |
|---------------------------|------|---------|--------|--------|--|
| Demand                    | P    | Revenue | Cost   | Profit |  |
| 10000                     | 0.12 | 650000  | 675000 | -25000 |  |
| 12000                     | 0.15 | 720000  | 675000 | 45000  |  |
| 14000                     | 0.2  | 720000  | 675000 | 45000  |  |
| 16000                     | 0.25 | 720000  | 675000 | 45000  |  |
| 18000                     | 0.18 | 720000  | 675000 | 45000  |  |
| 20000                     | 0.1  | 720000  | 675000 | 45000  |  |
| Expected Profit           |      |         |        | 36600  |  |

| Manufacture Produce 14000 |      |         |        |        |  |
|---------------------------|------|---------|--------|--------|--|
| Demand                    | P    | Revenue | Cost   | Profit |  |
| 10000                     | 0.12 | 700000  | 775000 | -75000 |  |
| 12000                     | 0.15 | 770000  | 775000 | -5000  |  |
| 14000                     | 0.2  | 840000  | 775000 | 65000  |  |
| 16000                     | 0.25 | 840000  | 775000 | 65000  |  |
| 18000                     | 0.18 | 840000  | 775000 | 65000  |  |
| 20000                     | 0.1  | 840000  | 775000 | 65000  |  |
| Expected Profit           |      |         |        | 37700  |  |

Optimal = 14000

| Manufacture Produce 16000 |      |         |        |         |  |
|---------------------------|------|---------|--------|---------|--|
| Demand                    | P    | Revenue | Cost   | Profit  |  |
| 10000                     | 0.12 | 750000  | 875000 | -125000 |  |
| 12000                     | 0.15 | 820000  | 875000 | -55000  |  |
| 14000                     | 0.2  | 890000  | 875000 | 15000   |  |
| 16000                     | 0.25 | 960000  | 875000 | 85000   |  |
| 18000                     | 0.18 | 960000  | 875000 | 85000   |  |
| 20000                     | 0.1  | 960000  | 875000 | 85000   |  |
| Expected Profit           |      |         |        | 24800   |  |

| Manufacture Produce 18000 |      |         |        |         |  |
|---------------------------|------|---------|--------|---------|--|
| Demand                    | P    | Revenue | Cost   | Profit  |  |
| 10000                     | 0.12 | 800000  | 975000 | -175000 |  |
| 12000                     | 0.15 | 870000  | 975000 | -105000 |  |
| 14000                     | 0.2  | 940000  | 975000 | -35000  |  |
| 16000                     | 0.25 | 1010000 | 975000 | 35000   |  |
| 18000                     | 0.18 | 1080000 | 975000 | 105000  |  |
| 20000                     | 0.1  | 1080000 | 975000 | 105000  |  |
| Expected Profit           |      |         |        | -5600   |  |

| Manufacture Produce 20000 |      |         |         |         |  |
|---------------------------|------|---------|---------|---------|--|
| Demand                    | P    | Revenue | Cost    | Profit  |  |
| 10000                     | 0.12 | 850000  | 1075000 | -225000 |  |
| 12000                     | 0.15 | 920000  | 1075000 | -155000 |  |
| 14000                     | 0.2  | 990000  | 1075000 | -85000  |  |
| 16000                     | 0.25 | 1060000 | 1075000 | -15000  |  |
| 18000                     | 0.18 | 1130000 | 1075000 | 55000   |  |
| 20000                     | 0.1  | 1200000 | 1075000 | 125000  |  |
| Expected Profit           |      |         |         | -48600  |  |

Expected Profit = 37700



P2) (Pay-back Contract)

| Manufacture Produce 10000 |      |         |        |        |  |
|---------------------------|------|---------|--------|--------|--|
| Demand                    | P    | Revenue | Cost   | Profit |  |
| 10000                     | 0.12 | 600000  | 575000 | 25000  |  |
| 12000                     | 0.15 | 600000  | 575000 | 25000  |  |
| 14000                     | 0.2  | 600000  | 575000 | 25000  |  |
| 16000                     | 0.25 | 600000  | 575000 | 25000  |  |
| 18000                     | 0.18 | 600000  | 575000 | 25000  |  |
| 20000                     | 0.1  | 600000  | 575000 | 25000  |  |
| Expected Profit           |      |         |        | 25000  |  |

| Manufacture Produce 12000 |      |         |        |        |  |
|---------------------------|------|---------|--------|--------|--|
| Demand                    | P    | Revenue | Cost   | Profit |  |
| 10000                     | 0.12 | 680000  | 675000 | 5000   |  |
| 12000                     | 0.15 | 720000  | 675000 | 45000  |  |
| 14000                     | 0.2  | 720000  | 675000 | 45000  |  |
| 16000                     | 0.25 | 720000  | 675000 | 45000  |  |
| 18000                     | 0.18 | 720000  | 675000 | 45000  |  |
| 20000                     | 0.1  | 720000  | 675000 | 45000  |  |
| Expected Profit           |      |         |        | 40200  |  |

| Manufacture Produce 14000 |      |         |        |        |  |
|---------------------------|------|---------|--------|--------|--|
| Demand                    | P    | Revenue | Cost   | Profit |  |
| 10000                     | 0.12 | 760000  | 775000 | -15000 |  |
| 12000                     | 0.15 | 800000  | 775000 | 25000  |  |
| 14000                     | 0.2  | 840000  | 775000 | 65000  |  |
| 16000                     | 0.25 | 840000  | 775000 | 65000  |  |
| 18000                     | 0.18 | 840000  | 775000 | 65000  |  |
| 20000                     | 0.1  | 840000  | 775000 | 65000  |  |
| Expected Profit           |      |         |        | 49400  |  |

Optimal = 16000

| Manufacture Produce 16000 |      |         |        |        |  |
|---------------------------|------|---------|--------|--------|--|
| Demand                    | P    | Revenue | Cost   | Profit |  |
| 10000                     | 0.12 | 840000  | 875000 | -35000 |  |
| 12000                     | 0.15 | 880000  | 875000 | 5000   |  |
| 14000                     | 0.2  | 920000  | 875000 | 45000  |  |
| 16000                     | 0.25 | 960000  | 875000 | 85000  |  |
| 18000                     | 0.18 | 960000  | 875000 | 85000  |  |
| 20000                     | 0.1  | 960000  | 875000 | 85000  |  |
| Expected Profit           |      |         |        | 50600  |  |

| Manufacture Produce 18000 |      |         |        |        |  |
|---------------------------|------|---------|--------|--------|--|
| Demand                    | P    | Revenue | Cost   | Profit |  |
| 10000                     | 0.12 | 920000  | 975000 | -55000 |  |
| 12000                     | 0.15 | 960000  | 975000 | -15000 |  |
| 14000                     | 0.2  | 1000000 | 975000 | 25000  |  |
| 16000                     | 0.25 | 1040000 | 975000 | 65000  |  |
| 18000                     | 0.18 | 1080000 | 975000 | 105000 |  |
| 20000                     | 0.1  | 1080000 | 975000 | 105000 |  |
| Expected Profit           |      |         |        | 41800  |  |

| Manufacture Produce 20000 |      |         |         |        |  |
|---------------------------|------|---------|---------|--------|--|
| Demand                    | P    | Revenue | Cost    | Profit |  |
| 10000                     | 0.12 | 1000000 | 1075000 | -75000 |  |
| 12000                     | 0.15 | 1040000 | 1075000 | -35000 |  |
| 14000                     | 0.2  | 1080000 | 1075000 | 5000   |  |
| 16000                     | 0.25 | 1120000 | 1075000 | 45000  |  |
| 18000                     | 0.18 | 1160000 | 1075000 | 85000  |  |
| 20000                     | 0.1  | 1200000 | 1075000 | 125000 |  |
| Expected Profit           |      |         |         | 25800  |  |

expected = 50600  
profit

P3) Cost-Saving Contract

| Manufacture Produce 10000 |      |         |        |        |
|---------------------------|------|---------|--------|--------|
| Demand                    | P    | Revenue | Cost   | Profit |
| 10000                     | 0.12 | 500000  | 460000 | 40000  |
| 12000                     | 0.15 | 500000  | 460000 | 40000  |
| 14000                     | 0.2  | 500000  | 460000 | 40000  |
| 16000                     | 0.25 | 500000  | 460000 | 40000  |
| 18000                     | 0.18 | 500000  | 460000 | 40000  |
| 20000                     | 0.1  | 500000  | 460000 | 40000  |
| Expected Profit           |      |         |        | 40000  |

| Manufacture Produce 12000 |      |         |        |        |
|---------------------------|------|---------|--------|--------|
| Demand                    | P    | Revenue | Cost   | Profit |
| 10000                     | 0.12 | 550000  | 540000 | 10000  |
| 12000                     | 0.15 | 600000  | 540000 | 60000  |
| 14000                     | 0.2  | 600000  | 540000 | 60000  |
| 16000                     | 0.25 | 600000  | 540000 | 60000  |
| 18000                     | 0.18 | 600000  | 540000 | 60000  |
| 20000                     | 0.1  | 600000  | 540000 | 60000  |
| Expected Profit           |      |         |        | 54000  |

| Manufacture Produce 14000 |      |         |        |        |
|---------------------------|------|---------|--------|--------|
| Demand                    | P    | Revenue | Cost   | Profit |
| 10000                     | 0.12 | 600000  | 620000 | -20000 |
| 12000                     | 0.15 | 650000  | 620000 | 30000  |
| 14000                     | 0.2  | 700000  | 620000 | 80000  |
| 16000                     | 0.25 | 700000  | 620000 | 80000  |
| 18000                     | 0.18 | 700000  | 620000 | 80000  |
| 20000                     | 0.1  | 700000  | 620000 | 80000  |
| Expected Profit           |      |         |        | 60500  |

Optimal = 14000

| Manufacture Produce 16000 |      |         |        |        |
|---------------------------|------|---------|--------|--------|
| Demand                    | P    | Revenue | Cost   | Profit |
| 10000                     | 0.12 | 650000  | 700000 | -50000 |
| 12000                     | 0.15 | 700000  | 700000 | 0      |
| 14000                     | 0.2  | 750000  | 700000 | 50000  |
| 16000                     | 0.25 | 800000  | 700000 | 100000 |
| 18000                     | 0.18 | 800000  | 700000 | 100000 |
| 20000                     | 0.1  | 800000  | 700000 | 100000 |
| Expected Profit           |      |         |        | 57000  |

| Manufacture Produce 18000 |      |         |        |        |
|---------------------------|------|---------|--------|--------|
| Demand                    | P    | Revenue | Cost   | Profit |
| 10000                     | 0.12 | 700000  | 780000 | -80000 |
| 12000                     | 0.15 | 750000  | 780000 | -30000 |
| 14000                     | 0.2  | 800000  | 780000 | 20000  |
| 16000                     | 0.25 | 850000  | 780000 | 70000  |
| 18000                     | 0.18 | 900000  | 780000 | 120000 |
| 20000                     | 0.1  | 900000  | 780000 | 120000 |
| Expected Profit           |      |         |        | 41000  |

| Manufacture Produce 20000 |      |         |        |         |
|---------------------------|------|---------|--------|---------|
| Demand                    | P    | Revenue | Cost   | Profit  |
| 10000                     | 0.12 | 750000  | 860000 | -110000 |
| 12000                     | 0.15 | 800000  | 860000 | -60000  |
| 14000                     | 0.2  | 850000  | 860000 | -10000  |
| 16000                     | 0.25 | 900000  | 860000 | 40000   |
| 18000                     | 0.18 | 950000  | 860000 | 90000   |
| 20000                     | 0.1  | 1000000 | 860000 | 140000  |
| Expected Profit           |      |         |        | 16000   |

e. profit = 60500



## Problem 4 :

Average demand/week = ~~100~~ 150  $\pm$  75

Holding Cost = 40%

Cycle service Level = 0.95

Reliable : 5000 \$/unit

Component

minimum order = 150

lead time = 7  $\pm$  0.1

Value : 4000 \$/unit

Electric

minimum order = 1500

lead time = 5  $\pm$  4

---

Reliable Comp :

$$\text{Material Cost} = 150 \times 52 \times 5000 = \underline{39,000,000}$$

$$\text{Cycle inventory} = \frac{150}{2} = 75$$

$$\text{Cycle inventory Cost} = 75 \times 5000 \times 0.4 = \underline{1,500,000}$$

$$\sigma_L = \sqrt{L\sigma_D^2 + D^2S_L^2} = \sqrt{1 \times 75^2 + \frac{150^2 \times (0.1)^2}{28}} = 76.49$$

$$SS = F_z^{-1}(\text{CSL}) \sigma_L = \overset{1.645}{F_z^{-1}(0.95)} \times 76.49 = 125.83$$

$$\text{Safety inventory Cost} = \underset{\downarrow 125.83}{SS} \times 5000 \times 0.4 = \underline{2,516,520}$$

$$\begin{aligned} \text{Total Cost} &= 39,000,000 + 1,500,000 + 2,516,520 \\ &= \underline{39,401,652} \$ \end{aligned}$$

## Value Electric :

$$\text{Material Cost} = 150 \times \$2 \times 4000 = \textcircled{312,000,000}$$

$$\text{Cycle inventory Cost} = \frac{1500}{2} \times \textcircled{4000} \times 0.4 = \textcircled{1,200,000}$$

$$\sigma_L = \sqrt{\frac{5 \times 75^2}{28125} + \frac{150 \times 4^2}{360000}} = 623$$

$$SS = \frac{F_S^{-1}(0.99)}{1.645} \times \sigma_L = 1.645 \times 623 = 1024.8$$

$$\text{Safety inventory Cost} = \underset{1024.8}{SS} \times 4000 \times 0.4 = \textcircled{1,639,680}$$

$$\begin{aligned} \text{Total Cost} &= 312,000,000 + 1,200,000 \\ &+ 1,639,680 = \textcircled{314,839,680} \\ &\underline{\underline{34,039,680 \$}} \end{aligned}$$

⇒ Value Electric is preferred due to Lower Cost.  
Supplier II