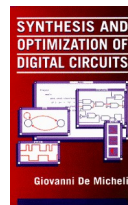


Boolean Methods for Multi-level Logic Synthesis

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Module 1

◆ Objectives

- ▲ What are Boolean methods
- ▲ How to compute *don't care* conditions
 - ▼ Controllability
 - ▼ Observability
- ▲ Boolean transformations

Boolean methods

- ◆ Exploit Boolean properties of logic functions
- ◆ Use *don't care* conditions
- ◆ More complex algorithms
 - ▲ Potentially better solutions
 - ▲ Harder to reverse the transformations
- ◆ Used within most synthesis tools

External *don't care* conditions

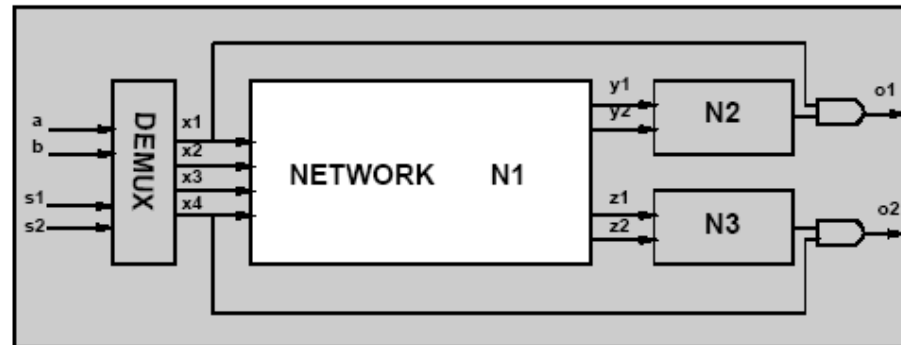
◆ Controllability *don't care* set CDC_{in}

- ▲ Input patterns never produced by the environment at the network's input

◆ Observability *don't care* set ODC_{out}

- ▲ Input patterns representing conditions when an output is not observed by the environment
- ▲ Relative to each output
- ▲ Vector notation

Example



- Inputs driven by a de-multiplexer.
- $CDC_{in} = x'_1 x'_2 x'_3 x'_4 + x_1 x_2 + x_1 x_3 + x_1 x_4 + x_2 x_3 + x_2 x_4 + x_3 x_4$.
- Outputs observed when $\begin{bmatrix} x_1 \\ x_4 \end{bmatrix} = \mathbf{1}$

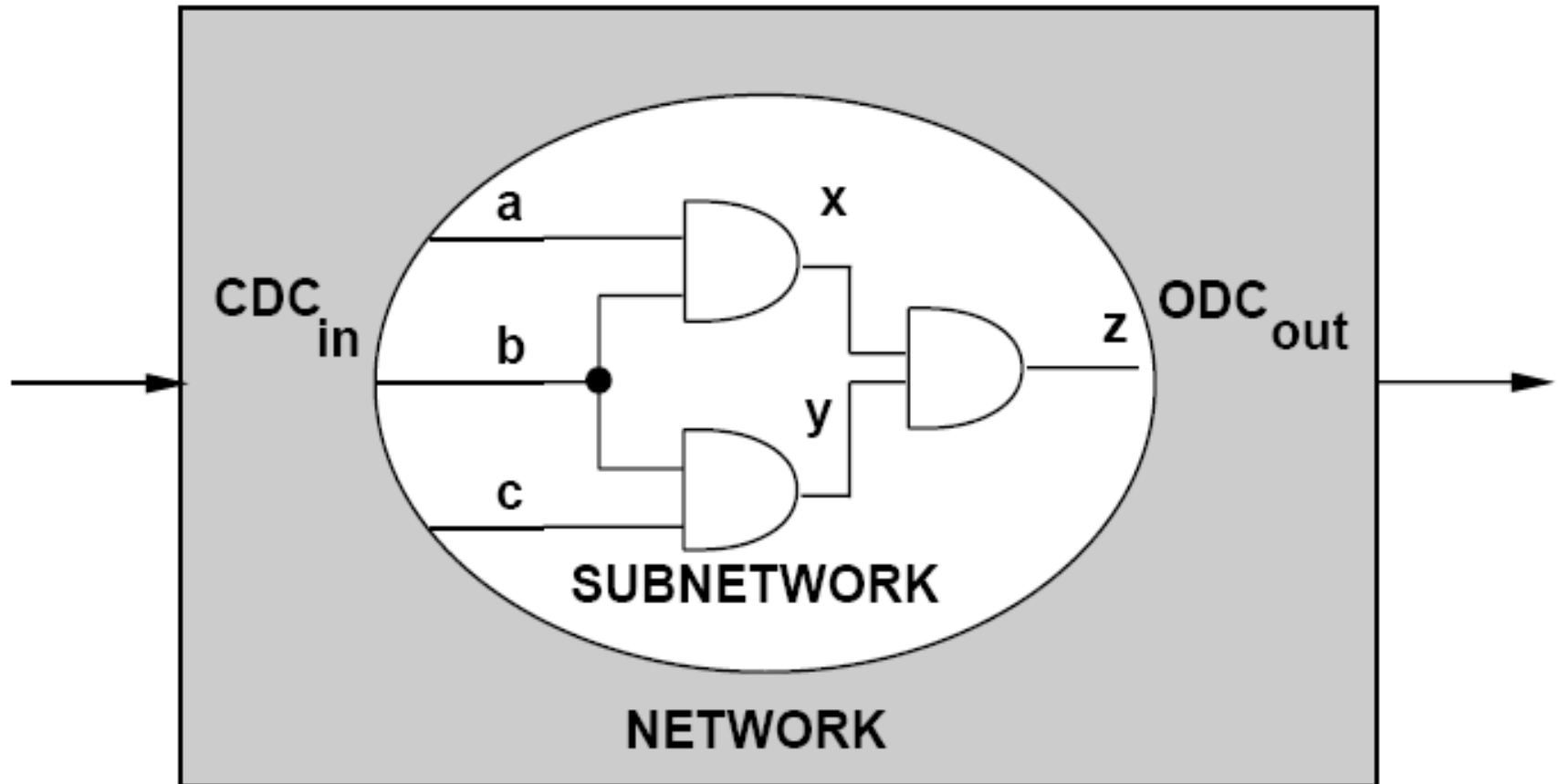
$$ODC_{out} = \begin{bmatrix} x'_1 \\ x'_1 \\ x'_4 \\ x'_4 \end{bmatrix}$$

Overall external *don't care* set

- ◆ Sum the controllability *don't cares* to each entry of the observability *don't care* set vector

$$\mathbf{DC}_{ext} = \mathbf{C} \mathbf{DC}_{in} + \mathbf{O} \mathbf{DC}_{out} = \begin{bmatrix} x'_1 + x_2 + x_3 + x_4 \\ x'_1 + x_2 + x_3 + x_4 \\ x'_4 + x_2 + x_3 + x_1 \\ x'_4 + x_2 + x_3 + x_1 \end{bmatrix}$$

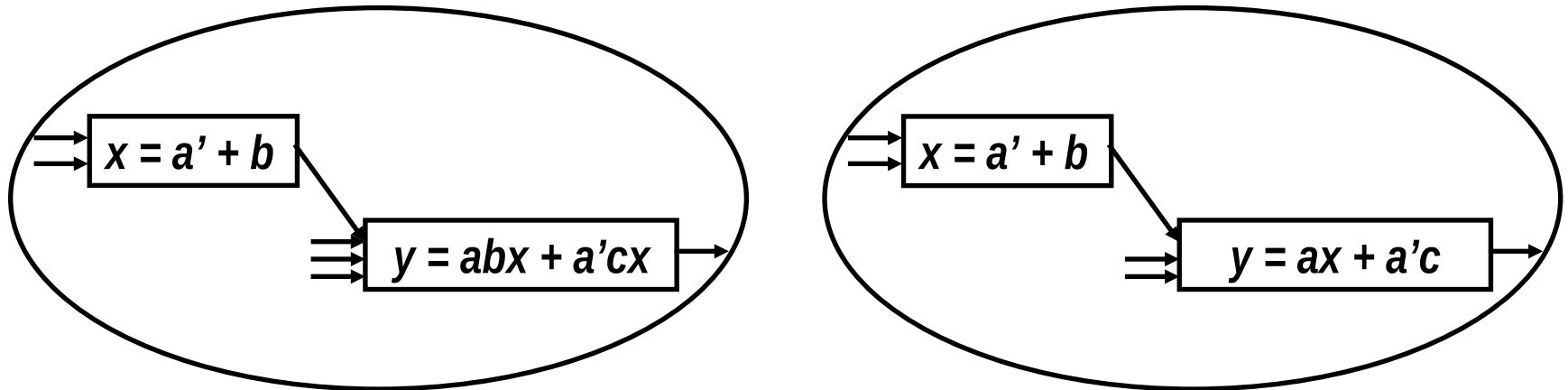
Internal *don't care* conditions



Internal *don't care* conditions

- ◆ Induced by the network structure
- ◆ Controllability *don't care* conditions:
 - ▲ Patterns never produced at the inputs of a sub-network
- ◆ Observability *don't care* conditions
 - ▲ Patterns such that the outputs of a sub-network are not observed

Example of optimization with *don't cares*



- ◆ CDC of y includes $ab'x + a'x'$
- ◆ Minimize f_y to obtain: $g_y = ax + a'c$

Satisfiability *don't care* conditions

- ◆ Invariant of the network:

$$x = f_x \rightarrow x \neq f_x \subseteq SDC$$

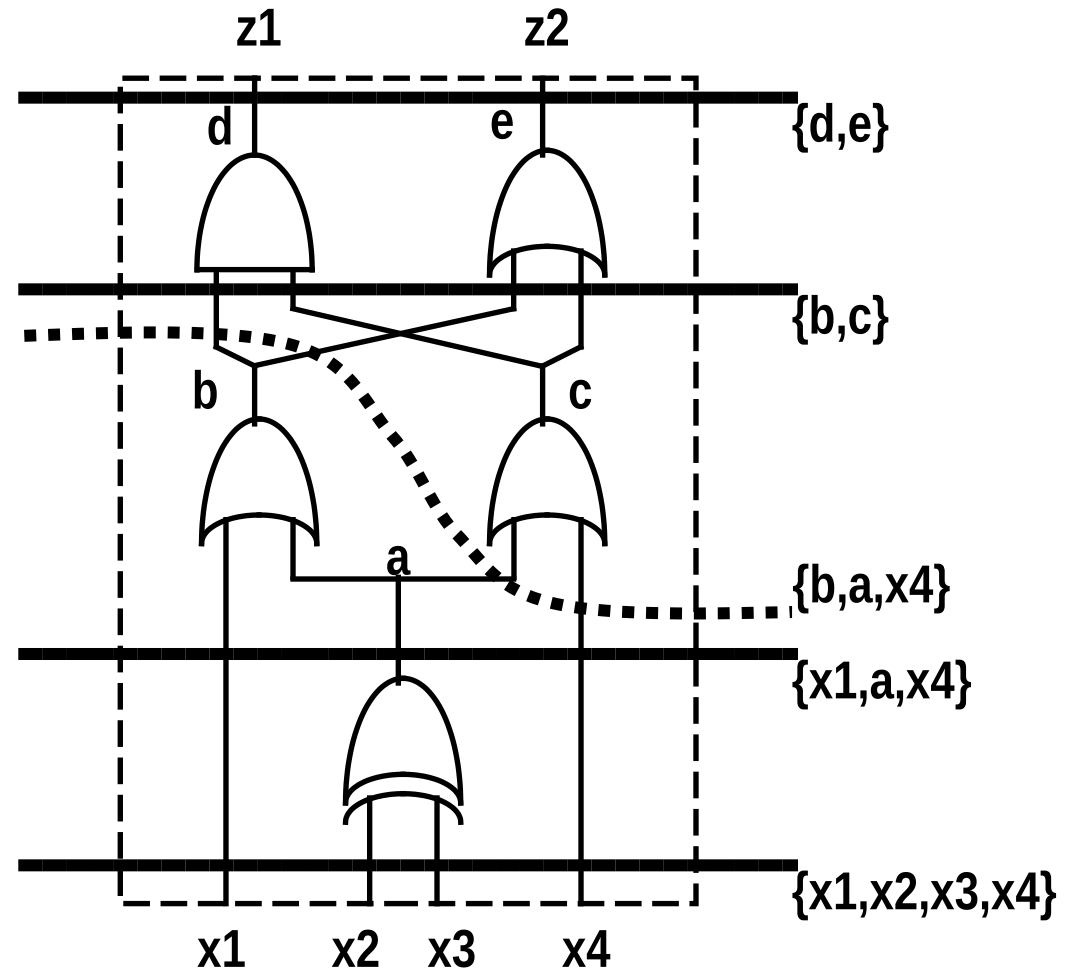
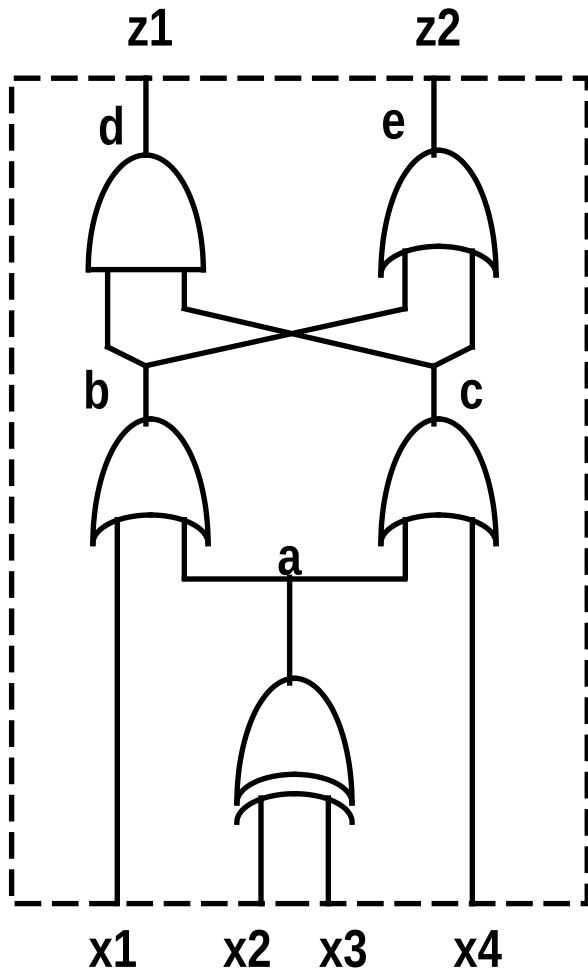
- ◆ $SDC = \sum_{all\ internal\ nodes} x \oplus f_x$

- ◆ Useful to compute controllability don't cares

CDC Computation

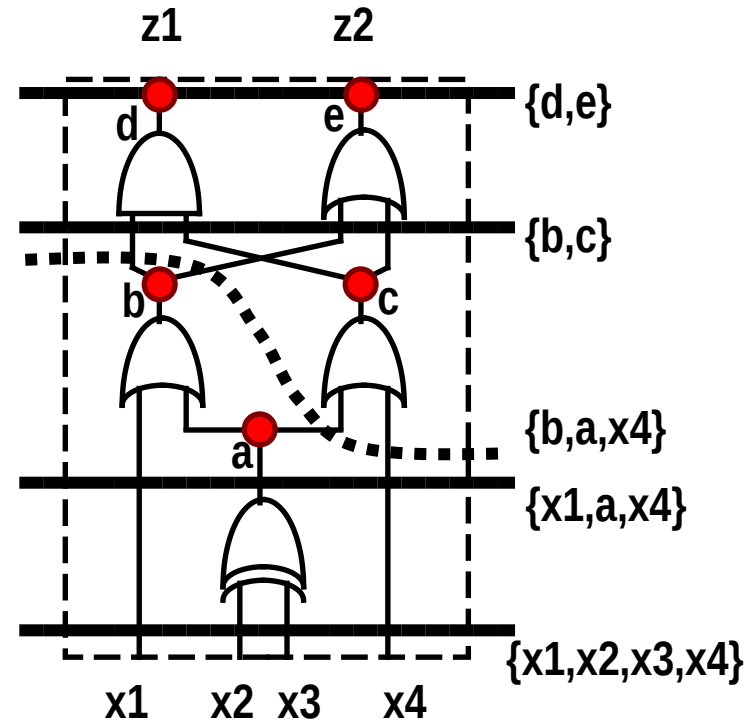
- ◆ **Method 1: Network traversal algorithm**
 - ▲ Consider initial **CDC** = **CDC_{in}** at the primary inputs
 - ▲ Consider different cutsets moving through the network from inputs to outputs
 - ▲ As the cutset moves forward
 - ▼ Consider **SDC** contribution of the newly considered block
 - ▼ Remove unneeded variables by consensus

Example



Example

- ◆ Assume $\text{CDC}_{\text{in}} = x_1'x_4'$
- ◆ Select vertex v_a
 - ▲ Contribution of v_a to $\text{CDC}_{\text{cut}} = a \oplus (x_2 \oplus x_3)$
 - ▲ Updated $\text{CDC}_{\text{cut}} = x_1'x_4' + a \oplus (x_2 \oplus x_3)$
 - ▲ Drop variables $D = \{x_2, x_3\}$ by consensus:
 - ▲ $\text{CDC}_{\text{cut}} = x_1'x_4'$
- ◆ Select vertex v_b
 - ▲ Contribution to $\text{CDC}_{\text{cut}}: b \oplus (x_1 + a)$.
 - ▼ Updated $\text{CDC}_{\text{cut}} = x_1'x_4' + b \oplus (x_1 + a)$
 - ▲ Drop variables x_1 by consensus:
 - ▼ $\text{CDC}_{\text{cut}} = b'x_4' + b'a$
- ◆ ...
- ◆ $\text{CDC}_{\text{out}} = e' = z_2'$



CDC Computation

```
CONTROLLABILITY( $G_n(V,E)$  ,  $CDC_{in}$ ) {  
     $C = V$ ;  
     $CDC_{cut} = CDC_{in}$ ;  
    foreach vertex  $v_x \in V$  in topological order {  
         $C = C \cup v_x$ ;  
         $CDC_{cut} = CDC_{cut} + f_x \oplus x$ ;  
         $D = \{v \in C \text{ s.t. all direct successors of } v \text{ are in } C\}$   
        foreach vertex  $v_y \in D$   
             $CDC_{cut} = C_y(CDC_{cut})$ ;  
         $C = C - D$ ;  
    };  
     $CDC_{out} = CDC_{cut}$ ;  
}
```

CDC Computation

- ◆ Method 2: **range** or **image** computation
- ◆ Consider the function **f** expressing the behavior of the cutset variables in terms of primary inputs
- ◆ CDC_{cut} is the complement of the **range** of **f** when $CDC_{in} = 0$
- ◆ CDC_{cut} is the complement of the **image** of $(CDC_{in})'$ under **f**
- ◆ The range and image can be computed recursively
 - ▲ Terminal case: scalar function
 - ▲ The range of $y = f(x)$ is $y + y'$ (any value)
unless **f** (or **f'**) is a tautology and the range is **y** (or **y'**)

Example

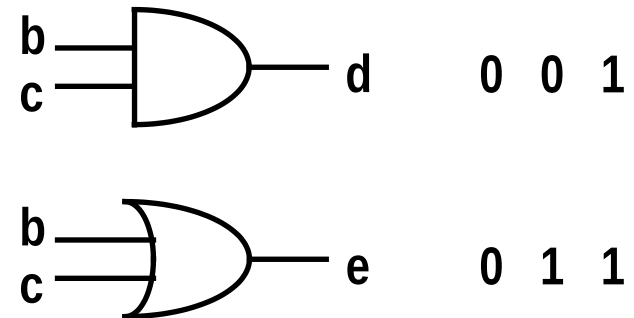
◆ $range(f) = d \ range((b+c)|_{d=bc=1}) + d' \ range((b+c)|_{d=bc=0})$

◆ When $d = 1$, then $bc = 1 \rightarrow b + c = 1$ is **TAUTOLOGY**

◆ If I choose 1 as top entry in output vector:

▲ the bottom entry is also 1.

▲ $\begin{bmatrix} 1 \\ ? \end{bmatrix} \rightarrow \begin{bmatrix} 1 \\ 1 \end{bmatrix}$



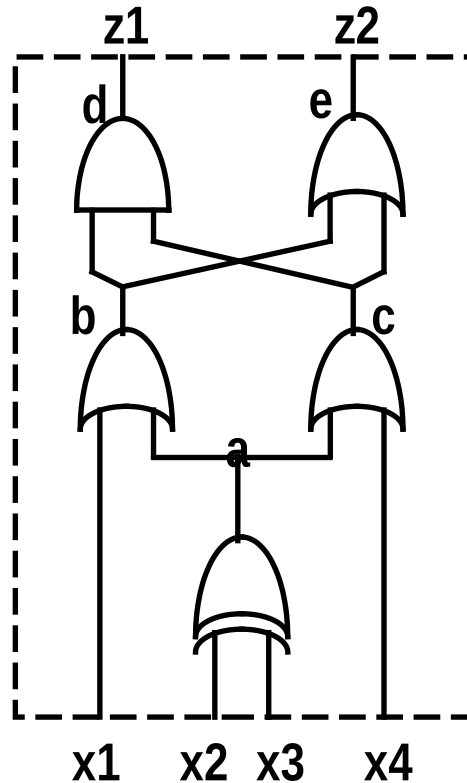
◆ When $d = 0$, then $bc = 0 \rightarrow b+c = \{0,1\}$

◆ If I choose 0 as top entry in output vector:

▲ The bottom entry can be either 0 or 1.

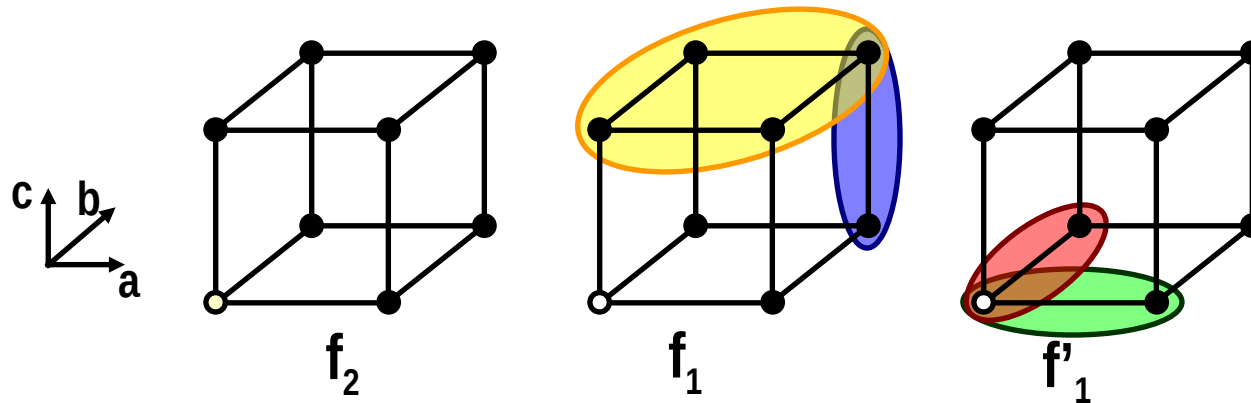
◆ $range(f) = de + d'(e + e') = de + d' = d' + e$

Example



$$f = \begin{bmatrix} f^1 \\ f^2 \end{bmatrix} = \begin{bmatrix} (x_1 + a)(x_4 + a) \\ (x_1 + a) + (x_4 + a) \end{bmatrix} = \begin{bmatrix} x_1 x_4 + a \\ x_1 + x_4 + a \end{bmatrix}$$

Example

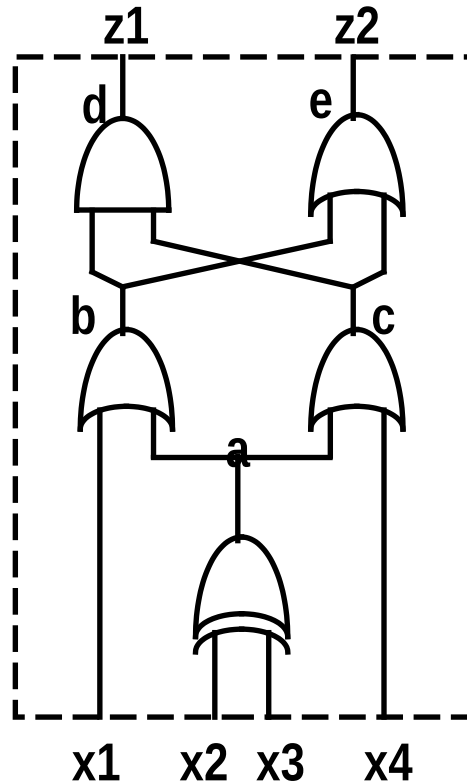


$$\begin{aligned}
 \text{range}(f) &= d \text{ range}(f^2|_{(x_1x_4 + a)=1}) + d' \text{ range}(f^2|_{(x_1x_4 + a)=0}) \\
 &= d \text{ range}(x_1 + x_4 + a|_{(x_1x_4 + a)=1}) + d' \text{ range}(x_1 + x_4 + a|_{(x_1x_4 + a)=0}) \\
 &= d \text{ range}(1) + d' \text{ range}(a'(x_1 \oplus x_4)) \\
 &= de + d'(e + e') \\
 &= e + d'
 \end{aligned}$$

◆ $\text{CDC}_{\text{out}} = (e + d')' = de' = z_1z_2'$

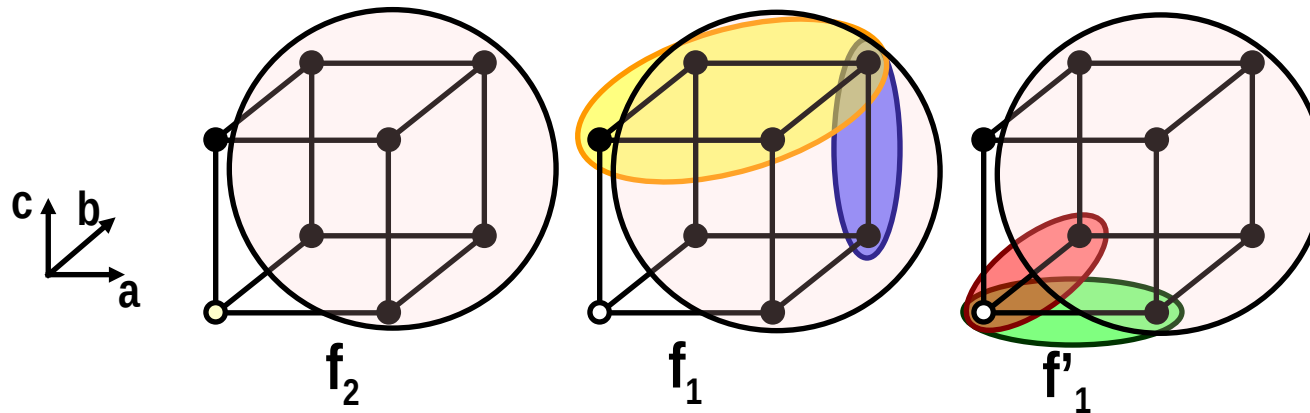
Example

$$CDC_{in} = x'_1 x'_4$$



$$f = \begin{bmatrix} f^1 \\ f^2 \end{bmatrix} = \begin{bmatrix} (x_1 + a)(x_4 + a) \\ (x_1 + a) + (x_4 + a) \end{bmatrix} = \begin{bmatrix} x_1 x_4 + a \\ x_1 + x_4 + a \end{bmatrix}$$

Example



$$\begin{aligned}
 \text{image}(f) &= d \text{ image}(f^2|_{(x_1x_4 + a)=1}) + d' \text{ image}(f^2|_{(x_1x_4 + a)=0}) \\
 &= d \text{ image}(x_1 + x_4 + a|_{(x_1x_4 + a)=1}) + d' \text{ image}(x_1 + x_4 + a|_{(x_1x_4 + a)=0}) \\
 &= d \text{ image}(1) + d' \text{ image}(1) \\
 &= de + d'e \\
 &= e
 \end{aligned}$$

◆ $\text{CDC}_{\text{out}} = e' = z_2'$

Observability analysis

- ◆ **Complementary to controllability**
 - ▲ Analyze network from outputs to inputs
- ◆ **More complex because network has several outputs and observability depends on output**
- ◆ **Observability may be understood in terms of perturbations**
 - ▲ If you flip the polarity of a signal at net **x**, and there is no change in the outputs, then **x** is not observable

Observability *don't care* conditions

- ◆ Conditions under which a change in polarity of a signal **x** is not perceived at the output
- ◆ If there is an explicit representation of the function, the **ODC** is the complement of the Boolean difference
$$\text{ODC} = (\partial f / \partial x)'$$
- ◆ Often, the terminal behavior is described implicitly
 - ▲ Applying chain rule to Boolean difference is computationally hard

Tree-network traversal

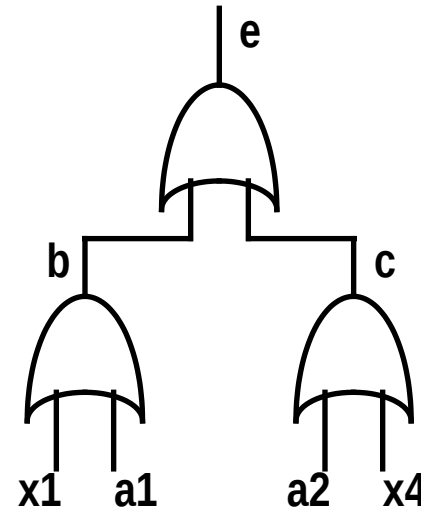
- ◆ Consider network from outputs to input
- ◆ At root
 - ▲ ODC_{out} is given
 - ▲ It may be empty
- ◆ At internal nodes:
 - ▲ Local function $y = f_y(x)$
 - ▲ $ODC_x = (\partial f_y / \partial x)' + ODC_y$
- ◆ Observability don't care set has two components:
 - ▲ Observability of the local function and observability of the network beyond the local block

Example

$$e = b + c$$

$$b = x_1 + a_1$$

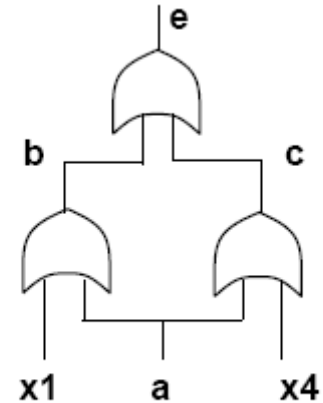
$$c = x_4 + a_2$$



- ◆ Assume $ODC_{out} = ODC_e = 0$
- ◆ $ODC_b = (\partial f_e / \partial b)' = (b + c)|_{b=1} \underline{\oplus} (b + c)|_{b=0} = c$
- ◆ $ODC_c = (\partial f_e / \partial c)' = b$
- ◆ $ODC_{x_1} = ODC_b + (\partial f_b / \partial x_1)' = c + a_1$

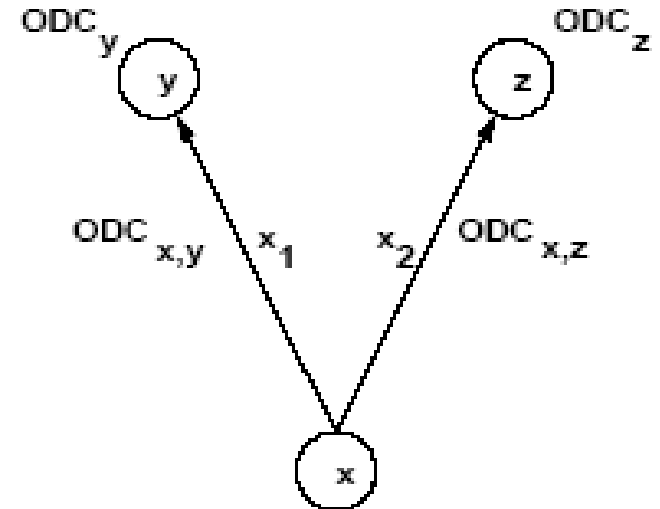
Non-tree network traversal

- ◆ General networks have forks and fanout reconvergence
- ◆ For each fork point, the contribution to the **ODC** depends on both paths
- ◆ Network traversal cannot be applied in a straightforward way
- ◆ More elaborate analysis is needed



Two-way fork

- ◆ Compute **ODC** sets associated with edges
- ◆ Recombine ODCs at fork point
- ◆ Theorem:
 - ▲ $\text{ODC}_x = \text{ODC}_{x,y|x=x'} \oplus \text{ODC}_{x,z}$
 - ▲ $\text{ODC}_x = \text{ODC}_{x,z|x=x'} \oplus \text{ODC}_{x,y}$
- ◆ Multi-way forks can be reduced to a sequence of two-way forks



ODC formula derivation

$$\begin{aligned}\mathbf{ODC}_x &= \mathbf{f}^{x_1, x_2}(1, 1) \oplus \mathbf{f}^{x_1, x_2}(0, 0) \\ &= \mathbf{f}^{x_1, x_2}(1, 1) \oplus \mathbf{f}^{x_1, x_2}(0, 0) \\ &\quad \oplus (\mathbf{f}^{x_1, x_2}(0, 1) \oplus \mathbf{f}^{x_1, x_2}(0, 1)) \\ &= (\mathbf{f}^{x_1, x_2}(1, 1) \oplus \mathbf{f}^{x_1, x_2}(0, 1)) \\ &\quad \oplus (\mathbf{f}^{x_1, x_2}(0, 1) \oplus \mathbf{f}^{x_1, x_2}(0, 0)) \\ &= \mathbf{ODC}_{x, y | \delta_2=1} \oplus \mathbf{ODC}_{x, z | \delta_1=0} \\ &= \mathbf{ODC}_{x, y | x_2=x'} \oplus \mathbf{ODC}_{x, z | x_1=x} \\ &= \mathbf{ODC}_{x, y | x=x'} \oplus \mathbf{ODC}_{x, z}\end{aligned}$$

- Because $x = x_1 = x_2$.

Example

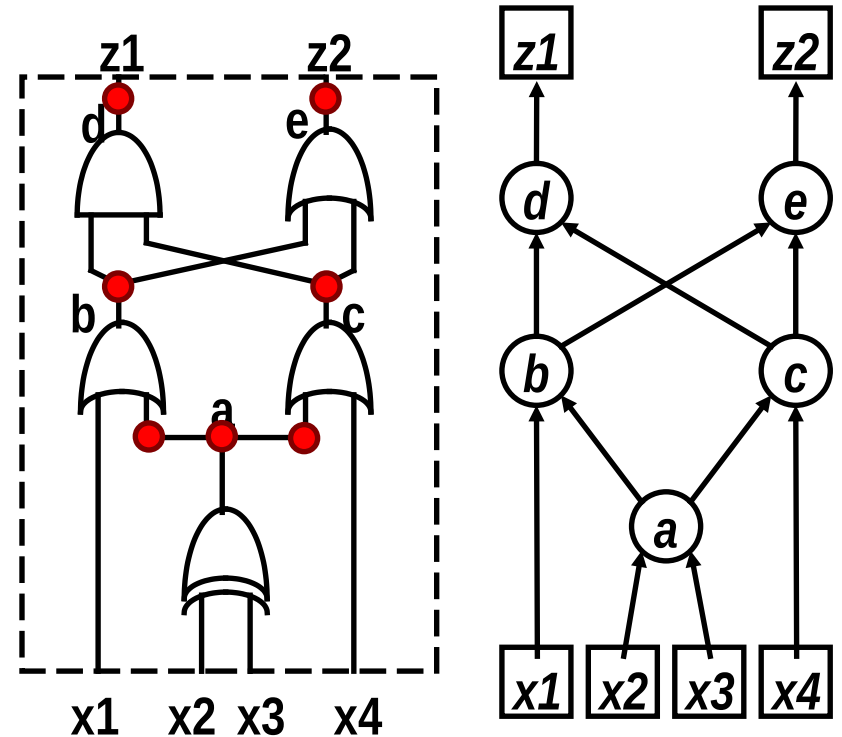
$$\text{ODC}_d = \begin{pmatrix} 0 \\ 0 \end{pmatrix}; \quad \text{ODC}_e = \begin{pmatrix} 0 \\ 0 \end{pmatrix};$$

$$\text{ODC}_c = \begin{pmatrix} b' \\ b \end{pmatrix}; \quad \text{ODC}_b = \begin{pmatrix} c' \\ c \end{pmatrix};$$

$$\text{ODC}_{a,b} = \begin{pmatrix} c' + x_1 \\ c + x_1 \end{pmatrix} = \begin{pmatrix} a'x_4' + x_1 \\ a + x_4 + x_1 \end{pmatrix}$$

$$\text{ODC}_{a,c} = \begin{pmatrix} b' + x_4 \\ b + x_4 \end{pmatrix} = \begin{pmatrix} a'x_1' + x_4 \\ a + x_1 + x_4 \end{pmatrix}$$

$$\text{ODC}_a = \text{ODC}_{a,b}|_{a=a'} \oplus \text{ODC}_{a,c} = \begin{pmatrix} a x_4' + x_1 \\ a' + x_4 + x_1 \end{pmatrix} \oplus \begin{pmatrix} a'x_1' + x_4 \\ a + x_1 + x_4 \end{pmatrix} = \begin{pmatrix} x_1 x_4 \\ x_1 + x_4 \end{pmatrix}$$



Don't care computation summary

- ◆ Controllability *don't cares* are derived by image computation
 - ▲ Recursive algorithms and data structure are applied
- ◆ Observability *don't cares* are derived by backward traversal
 - ▲ Exact and approximate computation
 - ▲ Approximate methods compute *don't care* subsets

Transformations with don't cares

◆ Boolean simplification

- ▲ Generate local DC set for local functions
- ▲ Use heuristic minimizer (e.g., Espresso)
- ▲ Minimize the number of literals

◆ Boolean substitution:

- ▲ Simplify a function by adding one (ore more) inputs
- ▲ Equivalent to simplification with *global don't care* sets

Example – Boolean substitution

- ◆ Substitute $q = a + cd$ into $f_h = a + bcd + e$

- ▲ Obtain $f_h = a + bq + e$

- ◆ Method

- ▲ Compute SDC including $q \oplus (a+cd) = q'a + q'cd + qa'(cd)'$

- ▲ Simplify $f_h = a + bcd + e$ with $DC = q'a + q'cd + qa'(cd)'$

- ▲ Obtain $f_h = a + bq + e$

- ◆ Result

- ▲ Simplified function has one fewer literal by changing the support of f_h

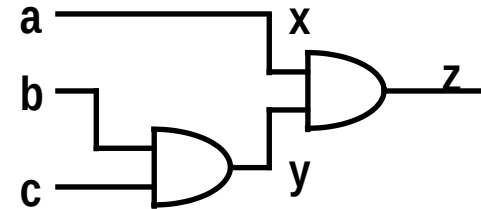
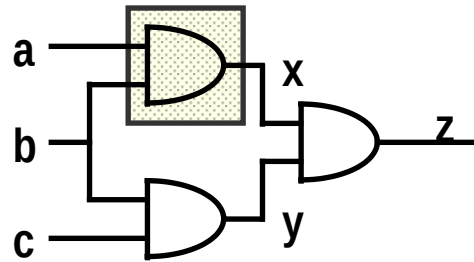
Simplification operator

- ◆ **Cycle over the network blocks**
 - ▲ **Compute local don't care conditions**
 - ▲ **Minimize**
- ◆ **Issues:**
 - ▲ **Don't care sets change as blocks are being simplified**
 - ▲ **Iteration may not have a fixed point**
 - ▲ **It would be efficient to parallelize some simplifications**

Optimization and perturbation

- ◆ Minimizing a function at a block x is the replacement of a local function f_x with a new function g_x
- ◆ This is equivalent to perturbing the network locally by
 - ▲ $\delta_x = f_x \oplus g_x$
- ◆ Conditions for a feasible replacement
 - ▲ Perturbation bounded by local don't care sets
 - ▲ δ_x included in $DC_{ext} + ODC + CDC$
- ◆ Smaller, approximate *don't care* sets can be used
 - ▲ But have smaller degrees of freedom

Example



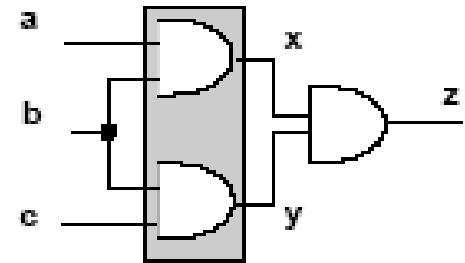
- ◆ No external *don't care* set.
- ◆ Replace **AND** by wire: $g_x = a$
- ◆ Analysis:
 - ▲ $\delta = f_x \oplus g_x = ab \oplus a = ab'$
 - ▲ $ODC_x = y' = b' + c'$
 - ▲ $\delta = ab' \subseteq DC_x = b' + c' \Rightarrow \text{feasible!}$

Parallel simplification

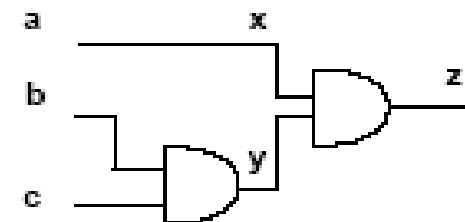
- ◆ **Parallel minimization of logic blocks is always possible when blocks are logically independent**
 - ▲ **Partitioned network**
- ◆ **Within a connect network, logic blocks affect each other**
- ◆ **Doing parallel minimization is like introducing multiple perturbations**
 - ▲ **But it is attractive for efficiency reasons**
- ◆ **Perturbation analysis shows that degrees of freedom cannot be represented by just an upper bound on the perturbation**
 - ▲ **Boolean relation model**

Example

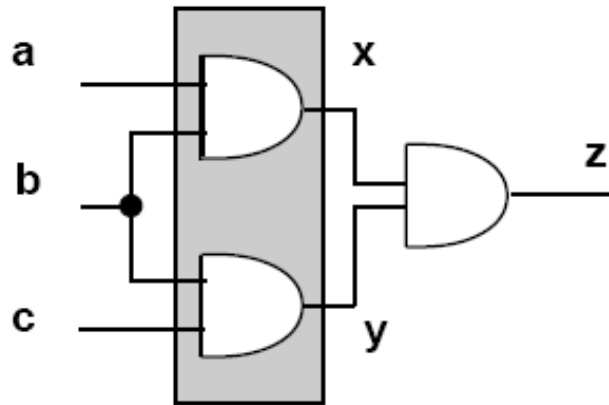
- ◆ Perturbations at **x** and **y** are related because of the reconvergent fanout at **z**
- ◆ Cannot change simultaneously
 - ▲ **ab** into **a**
 - ▲ **cb** into **c**



(a)



Boolean relation model



a	b	c	x, y
0	0	0	{ 00, 01, 10 }
0	0	1	{ 00, 01, 10 }
0	1	0	{ 00, 01, 10 }
0	1	1	{ 00, 01, 10 }
1	0	0	{ 00, 01, 10 }
1	0	1	{ 00, 01, 10 }
1	1	0	{ 00, 01, 10 }
1	1	1	{ 11 }

a	b	c	x, y
1	*	*	10
*	1	1	01

Boolean relation model

- ◆ **Boolean relation minimization is the correct approach to handle Boolean optimization at multiple vertices**
- ◆ **Necessary steps**
 - ▲ Derive equivalence classes for Boolean relation
 - ▲ Use relation minimizer
- ◆ **Practical considerations**
 - ▲ High computational requirement to use Boolean relations
 - ▲ Use approximations instead

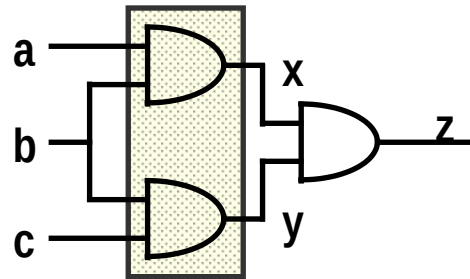
Parallel Boolean optimization compatible *don't care* sets

- ◆ Determine a subset of *don't care* sets which is safe to use in a parallel minimization
 - ▲ Remove those degrees of freedom that can lead to transformations incompatible with others effected in parallel
- ◆ Using **compatible *don't care* sets**, only upper bounds on the perturbation need to be satisfied
- ◆ Faster and efficient method

Example

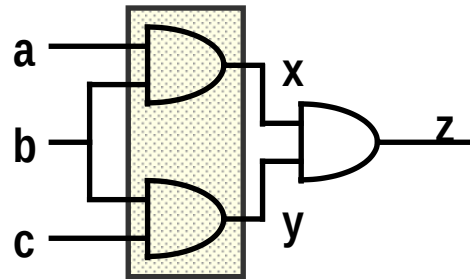
- ◆ Parallel optimization at two vertices
- ◆ First vertex x
 - ▲ CODC equal to ODC set
 - ▲ $\text{CODC}_x = \text{ODC}_x$
- ◆ Second vertex y
 - ▲ CODC is smaller than its ODC to be safe enough to allow for transformations permitted by the first ODC
 - ▲ $\text{CODC}_y = C_x(\text{ODC}_y) + \text{ODC}_y \text{ODC}'_x$
- ◆ Order dependence

Example



- ◆ $\text{CODC}_y = \text{ODC}_y = x' = b' + a'$
- ◆ $\text{ODC}_x = y' = b' + c'$
- ◆ $\text{CODC}_x = C_y(\text{ODC}_x) + \text{ODC}_x(\text{ODC}_y)'$
 $= C_y(y') + y'x = y'x$
 $= (b' + c')ab = abc'$

Example (2)



◆ Allowed perturbation:

▲ $f_y = bc \rightarrow g_y = c$

▲ $\delta_y = bc \oplus c = b'c \subseteq \text{CODC}_y = b' + a'$

◆ Disallowed perturbation:

▲ $f_x = ab \rightarrow g_x = a.$

▲ $\delta_x = ab \oplus a = ab' \not\subseteq \text{CODC}_x = abc'$

Boolean methods Summary

- ◆ Boolean methods are powerful means to restructure networks
 - ▲ Computationally intensive
- ◆ Boolean methods rely heavily on *don't care* computation
 - ▲ Efficient methods
 - ▲ Possibility to subset the *don't care* sets
- ◆ Boolean method often change the network substantially, and it is hard to undo Boolean transformations

Module 2

◆ Objectives

▲ Testability

▲ Relations between testability and Boolean methods

Testability

- ◆ Generic term to mean easing the testing of a circuit
- ◆ Testability in logic synthesis context
 - ▲ Assume combinational circuit
 - ▲ Assume single/multiple stuck-at fault
- ◆ Testability is referred to as the possibility of generating test sets for all faults
 - ▲ Property of the circuit
 - ▲ Related to fault coverage

Test for *stuck-ats*

- ◆ Net **y stuck-at 0**

- ▲ Input pattern that sets **y** to TRUE
- ▲ Observe output
- ▲ Output of faulty circuit differs from correct circuit

- ◆ Net **y stuck-at 1**

- ▲ Input pattern that sets **y** to FALSE
- ▲ Observe output
- ▲ Output of faulty circuit differs from correct circuit

- ◆ Testing is based on *controllability* and *observability*

Test sets – *don't care* interpretation

- ◆ Stuck-at 0 on net y

- ▲ { Input vector t such that $y(t) \text{ ODC}'y(t) = 1$ }

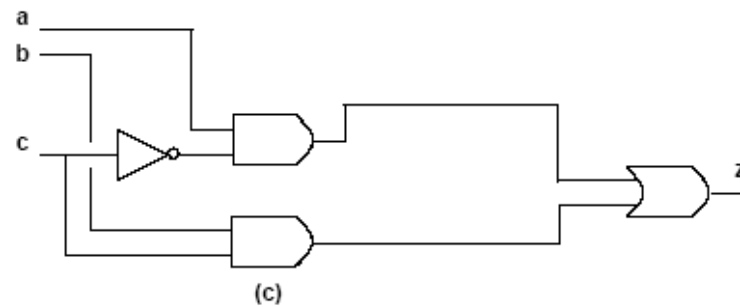
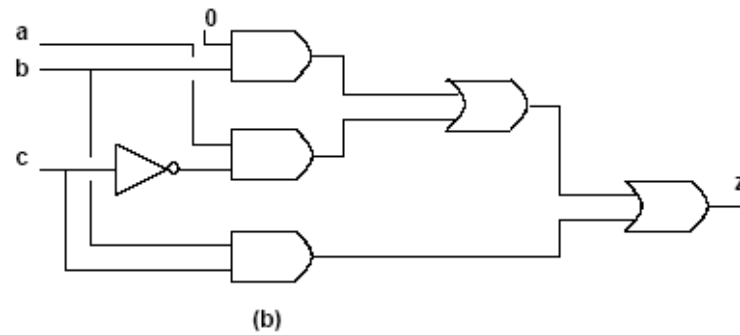
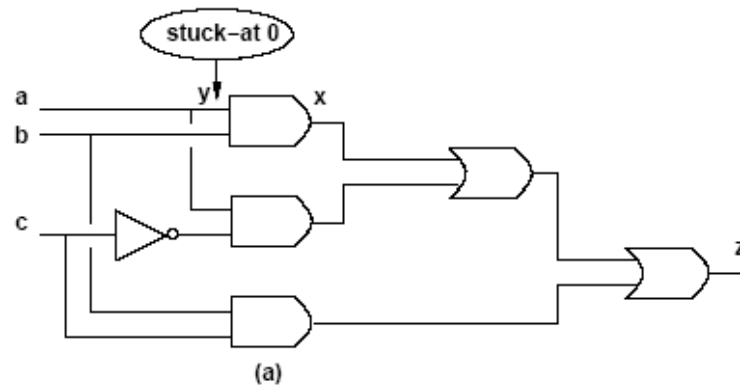
- ◆ Stuck-at 1 on net y

- ▲ { Input vector t such that $y'(t) \text{ ODC}'y(t) = 0$ }

Using testing methods for synthesis

- ◆ Redundancy removal
 - ▲ Use ATPG to search for untestable fault
- ◆ If stuck-at 0 on net y is untestable:
 - ▲ Set $y = 0$
 - ▲ Propagate constant
- ◆ If stuck-at 1 on net y is untestable
 - ▲ Set $y = 1$
 - ▲ Propagate constant
- ◆ Iterate for each untestable fault

Example



Redundancy removal and perturbation analysis

◆ Stuck-at 0 on y

▲ y set to 0. Namely $g_x = f_x|_{y=0}$



▲ Perturbation:

$$\nabla \delta = f_x \oplus f_x|_{y=0} = y \cdot \partial f_x / \partial y$$

◆ Perturbation is feasible \Leftrightarrow fault is untestable

▲ No input vector t can make $y(t) \cdot ODC_y'(t)$ true

▲ No input vector t can make $y(t) \cdot ODC_x'(t) \cdot \partial f_x / \partial y$ true

$$\nabla \text{Because } ODC_y = ODC_x + (\partial f_x / \partial y)'$$

Redundancy removal and perturbation analysis

- ◆ Assume untestable stuck-at 0 fault.

- ◆ $y \cdot \text{ODC}_x' \cdot \partial f_x / \partial y \subseteq \text{SDC}$

- ◆ Local don't care set:

- ▲ $\text{DC}_x \supseteq \text{ODC}_x + y \cdot \text{ODC}_x' \cdot \partial f_x / \partial y$

- ▲ $\text{DC}_x \supseteq \text{ODC}_x + y \cdot \partial f_x / \partial y$

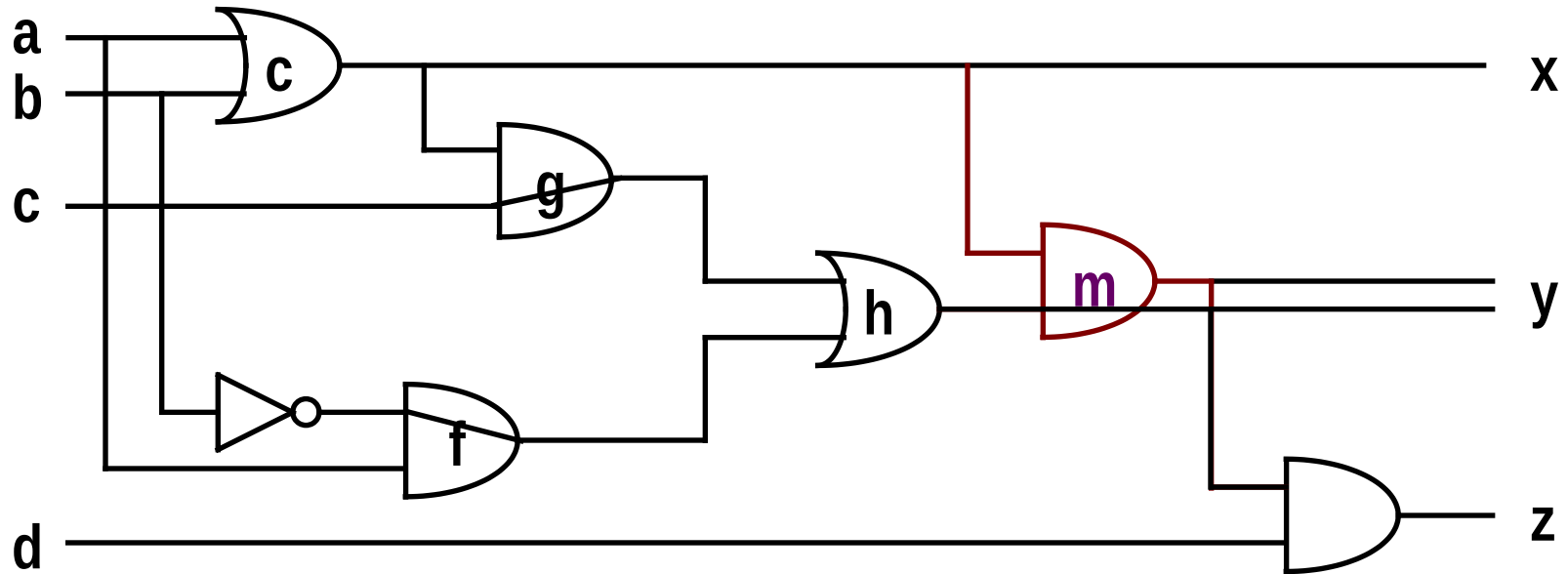
- ◆ Perturbation $\delta = y \cdot \partial f_x / \partial y$

 - ▲ Included in the local don't care set

Rewiring

- ◆ **Extension to redundancy removal**
 - ▲ Add connection in a circuit
 - ▲ Create other redundant connections
 - ▲ Remove redundant connections
- ◆ **Iterate procedure to reduce network**
 - ▲ A connection corresponds to a wire
 - ▲ Rewiring modifies gates and wiring structure
 - ▲ Wires may have specific costs due to distance

Example



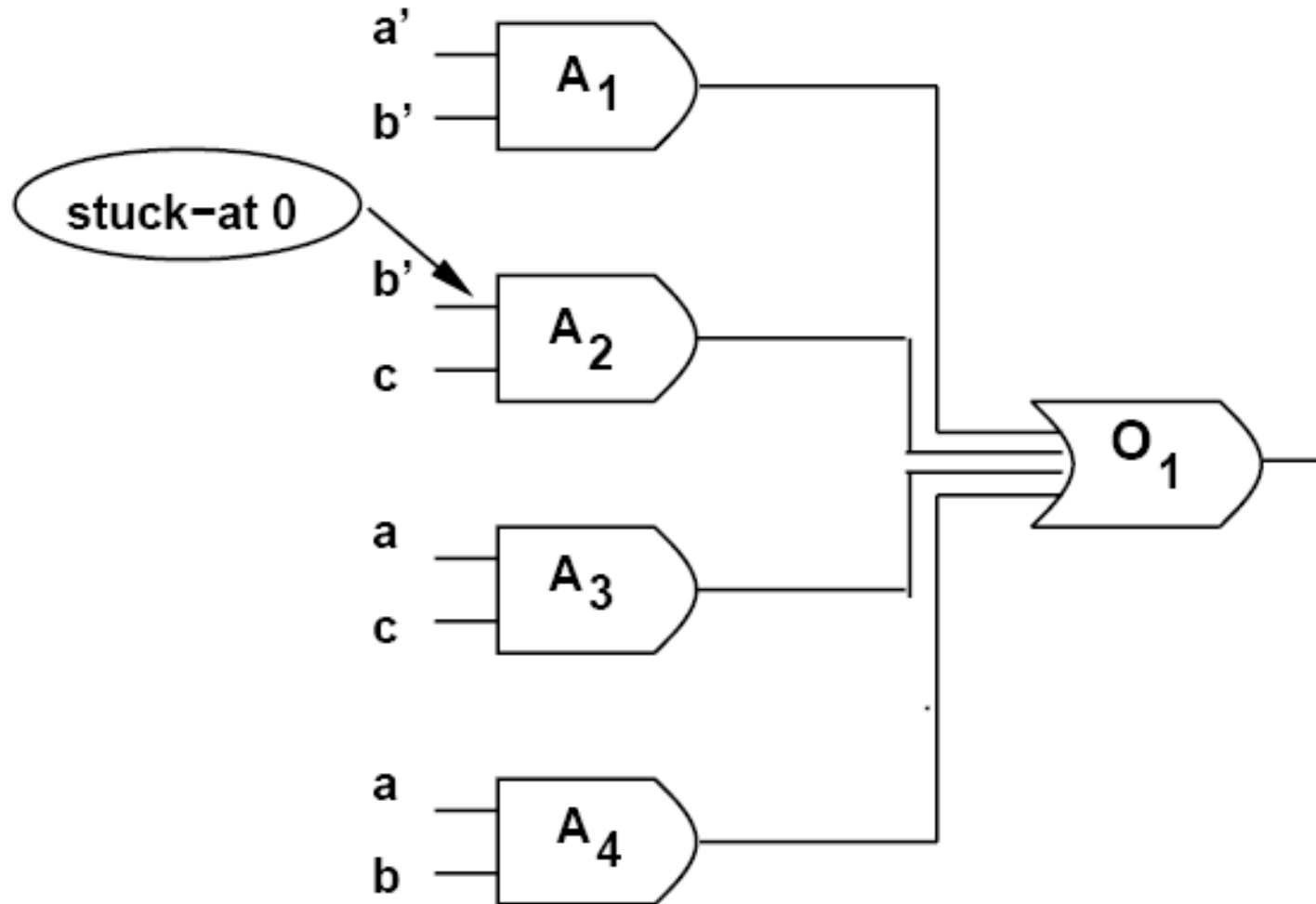
Synthesis for testability

- ◆ **Synthesize fully testable circuits**
 - ▲ For single or multiple stuck-at faults
- ◆ **Realizations**
 - ▲ Two-level forms
 - ▲ Multi-level networks
- ◆ **Since synthesis can modify the network properties, testability can be addressed during synthesis**

Two-level forms

- ◆ **Full testability for single stuck-at faults:**
 - ▲ Prime and irredundant covers
- ◆ **Full testability for multiple stuck-at faults**
 - ▲ Prime and irredundant cover when
 - ▼ Single output function
 - ▼ No product-term sharing
 - ▼ Each component is prime and irredundant

Example $f = a'b' + b'c + ac + ab$



Multiple-level networks

- ◆ Consider logic networks with local functions in *sop* form
- ◆ Prime and irredundant network
 - ▲ No literal and no implicant of any local function can be dropped
 - ▲ The AND-OR implementation is fully testable for single *stuck-at* faults
- ◆ Simultaneous prime and irredundant network
 - ▲ No subsets of literals and no subsets of implicants can be dropped
 - ▲ The AND-OR implementation is fully testable for multiple *stuck-ats*

Synthesis for testability

- ◆ Heuristic logic minimization (e.g., Espresso) is sufficient to insure testability of two-level forms
- ◆ To achieve fully testable networks, simplification has to be applied to all logic blocks with full *don't care* sets
- ◆ In practice, don't care sets change as neighboring blocks are optimized
- ◆ Redundancy removal is a practical way of achieving testability properties

Summary – Synthesis for testability

- ◆ **There is synergy between synthesis and testing**
 - ▲ **Don't care conditions play a major role in both fields**
- ◆ **Testable network correlate to a small area implementation**
- ◆ **Testable network do not require to slow-down the circuit**
- ◆ **Algebraic transformations preserve multi-fault testability, and are preferable under this aspect**