## Data Stream Analysis

Big Data Management





#### **Knowledge objectives**

- Explain the difference between generic one-pass algorithms and stream processing
- 2. Name the two challenges of stream processing
- 3. Name two solutions to limited processing capacity
- 4. Name three solutions to limited memory capacity





#### **Understanding Objectives**

- 1. Decide the probability of keeping a new element or removing an old one from memory to keep equi-probability on load shedding
- Decide the parameters of the hash function to get a representative result on load shedding
- 3. Decide the optimum number of hash functions in a Bloom filter
- 4. Approximate the probability of false positives in a Bloom filter
- 5. Calculate the weighted average of an attribute considering an exponentially decaying window
- 6. Decide if heavy hitters will show false positives





## Challenges and approaches





#### **Constraints**

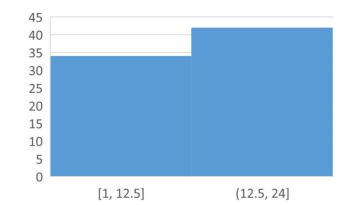
- Data cannot be stored
  - One-pass algorithms with
    - Bounded processing time
    - Bounded resources (i.e., memory)
      - At most, logarithmic on the size of the stream
    - Answer available at any time
- Processing must be on-line
  - Bounded response time for both
    - a) Summary update
    - b) Response retrieval

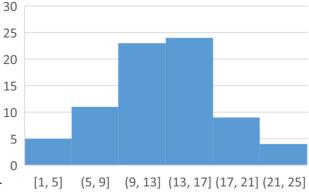




#### Challenges and approaches

- Limited computation capacity
  - Sampling (i.e., Load shedding)
    - Probabilistically drop stream elements
  - Filtering (i.e., Bloom filters)
- Limited memory capacity
  - Sliding window -> Discard elements
    - Aging (use only most recent data)
  - Exponentially decaying window -> Weight elements
  - Synopsis -> Approximate solutions
    - Examples:
      - Histograms Works under uniform distribution of values in a bucket
      - Concise sampling Works under a limited number of distinct values
      - Heavy hitters Uses logarithmic memory space
      - Sketching Space needed depends on error and probability of that error









## Load shedding

Sampling data streams





#### Load shedding (Keeping equi-probability)

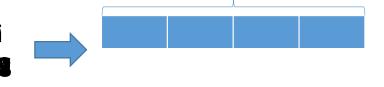
- Mistakes in case of infinite streams:
  - a) Fix the values at the beginning
  - b) Remove old values from memory



- All past elements have the same probability of being in memory at any time
- Do not want to store any additional information
- Definitions:
  - Memory positions: *p*
  - Elements seen: *n*
- Solution:
  - Probability of keeping the new element n+1
    - p/(n+1)
  - Probability of removing an element from memory
    - 1/p









#### Load shedding (Statement)

"Select a subset of the stream so that answering ad-hoc queries gives a statistically representative result."

Example: Given a stream of tuples [user, query, time], we can store 10% of the tuples. If we randomly keep 1/10 of the tuples, then we would get the wrong answer to "Percentage of duplicate queries for a user"!!!

#### Definitions:

s = queries issued once by a user

d = queries issued twice by a user

No queries issued more than twice

The sample will contain:

s/10+18d/100 queries issued once

d/100 queries issued twice

The answer would be:

 $(d/100)/(s*10/100+d*18/100+d/100) = d/(10s+19d) \neq d/(s+d)$ 

Solution:

Keep 1/10 of the users (use a hash function of the key)

Before/After	Twice	Once	None
Once	0	s*1/10	s*9/10
Twice	d*1/100	d*(9/10*1/10+1/10*9/10)	d*9/10*9/10
Total	d*1/100	s*10/100+d*18/100	•••

A. Rajaraman and J. Ullman





#### Load shedding (Generalization)

- Queries may need different grouping keys or the key can be compound
  - Use the "group by" set in the hash function
- Memory is limited
  - Take a hash function to a large number of values M and keep only elements mapping to a value bellow t
    - Dynamically reduce t as you are running out of memory

$$h(GB) = f(GB) \mod M < 3$$









## **Bloom Filters**

Filtering data streams





#### **Bloom filters (Statement)**

"Accept those elements in the stream that meet a criterion (based on looking for membership in a set), others are dropped."

- Example
  - Given an e-mail stream of tuples [address,text], we have a list of 10<sup>9</sup> allowed addresses (20 bytes each) and only 1GB of memory available.
- Solution

- 1
- Use the memory as an array of bits and map the addresses by means of a hash function (approximately 1/8 bits will be set)
- Note: Some spam will still get through the filter





#### Bloom filters (Example with one hash function)





#### Bloom filters (Example with two hash functions)





#### **Bloom filters (Generalization)**

- Elements:
  - A set of m key values



- A list of k hash functions (h; key  $\rightarrow n$ )
- One array of n bits (n >> m)
- Build:
  - For each element in the probing set, apply all k hash functions and set to 1 the corresponding bits
- Probing:
  - For each element in the stream, apply all k hash functions, it will pass only if all corresponding bits are set to 1
- False positives:
  - $(1-e^{-km/n})^k$
- Optimal
  - $k = (n/m) \cdot \ln 2 \rightarrow (1-e^{-km/n})^k = (1/2)^k \approx 0.618^{n/m}$





#### Bloom filters (Rationale)

- Probability of a bit being set by a hash function at build phase 1/n
- Probability of a bit NOT being set by a hash function at build phase 1-1/n
- Probability of a bit NOT being set by a hash function of ANY key at build phase  $(1-1/n)\cdot(1-1/n)\cdot...\cdot(1-1/n)=(1-1/n)^m=(1-1/n)^{n(m/n)}$ 
  - A good approximation of  $(1-\epsilon)^{1/\epsilon}$  for small  $\epsilon$  is  $1/\epsilon$   $(1/\epsilon)^{m/n} = (e^{-1})^{m/n} = e^{-m/n}$
- Probability of a bit NOT being set by ANY hash function of ANY key at build phase  $(e^{-m/n})^k$
- Probability of a bit set by SOME hash function of ANY key at build phase  $1-(e^{-m/n})^k=1-e^{-km/n}$
- Probability of all hash functions finding the bit set in the probing phase  $(1-e^{-km/n})^k$





# Exponentially decaying window





#### **Exponentially decaying window (Statement)**

"Do not make a distinction between old and young element, but just weight them."



- Example
  - Find the currently most popular movie/topic.
- Solution:
  - Keep one weighted counter per movie/topic
- Definitions:
  - $c = small\ constant\ (e.g.,\ 10^{-6}\ or\ 10^{-9})$
  - T = current time
  - $f(t) = a_t = element \ at \ time \ t \ (or \ 0 \ if \ there \ is \ no \ element)$



- $g(T-t) = (1-c)^{(T-t)}$  = weight at time T of an item obtained at time t
- Value:  $\Sigma f(i) \cdot g(T-i) = \sum_{i=0}^{T} a_i (1-c)^{T-i}$
- Process: Multiply the current counter by (1-c) and add  $a_t$ 
  - $\sum_{i=0}^{T+1} a_i (1-c)^{T-i} = (\sum_{i=0}^{T} a_i (1-c)^{T-i}) * (1-c) + a_{T+1}$
  - Being X the time since the last update, we can multiply by  $(1-c)^X$ , instead





### **Exponentially decaying window (Example)**

c=0.5 Counter = **0.383**25 Stream 0 1 0 0 1 0 0 ...







## **Heavy Hitters**





#### **Heavy hitters (Statement)**

"Given a stream, identify the items that occur more than a given percentage ( $\theta$ ) of times."

- We do not know which will be frequent enough
- We cannot store all items
  - An exact solution needs to store all items seen
    - O(n log(N)) in the worst case
- Solution Approximate with <u>false positives</u>
  - Structure:
    - Set of  $1/\theta$  pairs [element, counter]
  - Actions on receiving an element:
    - If the element is in the structure, increase its counter
    - If the element is not in the structure, insert it
    - If the set overflows, decrease all counters and remove those with value zero





#### Heavy hitters (example)

Required frequency: 33% Heavy hitters: a b c

ababacccaab defgh



Summary (capacity: 1/0.33 = 3)



- [a,**&**]
- [g,3]
- [b,**3**]
- [6,11]

a: 5/16 = 31.25%

b: 3/16 = 18.75%

c: 3/16 = 18.75%

d: 1/16 = 6.25%

e: 1/16 = 6.25%

f: 1/16 = 6.25%

q: 1/16 = 6.25%

h: 1/16 = 6.25%





## Closing





#### Summary

- Stream processing techniques
  - Load shedding
  - Bloom filters
  - Exponentially decaying window
  - Heavy hitters





#### References

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