

```
1 import numpy as np
2 from scipy.integrate import quad
```

```
1 # Define the wave function for the ground state
2 def psi(x):
3     L = 2
4     return np.sqrt(1 / L) * np.sin(np.pi * x / L)
5
6 # Define the integrands for the expectation values
7 def integrand_x(x):
8     return x * (psi(x) ** 2)
9
10 def integrand_2_minus_x(x):
11     return (2 - x) * (psi(x) ** 2)
12
13 def integrand_x_times_2_minus_x(x):
14     return x * (2 - x) * (psi(x) ** 2)
```

```
1
2 # Calculate the expectation values
3 x_expectation, _ = quad(integrand_x, 0, 2)
4 expectation_2_minus_x, _ = quad(integrand_2_minus_x, 0, 2)
5 expectation_x_times_2_minus_x, _ = quad(integrand_x_times_2_minus_x, 0, 2)
6
7 # Print the results
8 print(f"Expectation value  $\langle x \rangle$ : {x_expectation:.5f}")
9 print(f"Expectation value  $\langle 2 - x \rangle$ : {expectation_2_minus_x:.5f}")
10 print(f"Expectation value  $\langle x(2 - x) \rangle$ : {expectation_x_times_2_minus_x:.5f}")
```

```
↳ Expectation value  $\langle x \rangle$ : 0.50000
   Expectation value  $\langle 2 - x \rangle$ : 0.50000
   Expectation value  $\langle x(2 - x) \rangle$ : 0.43465
```