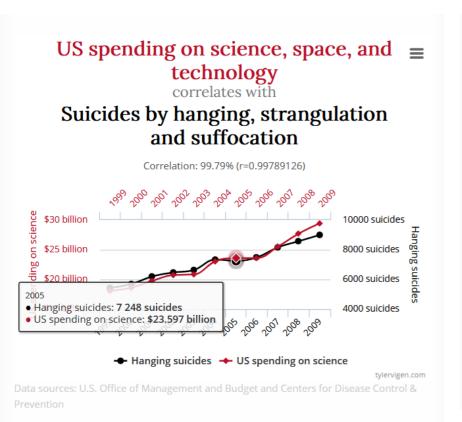
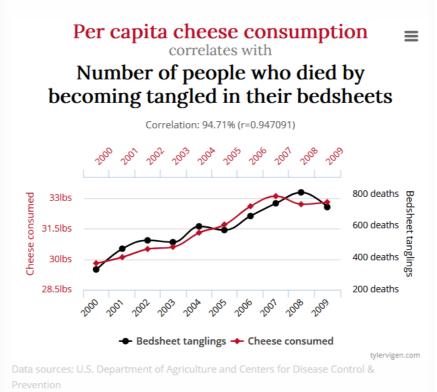


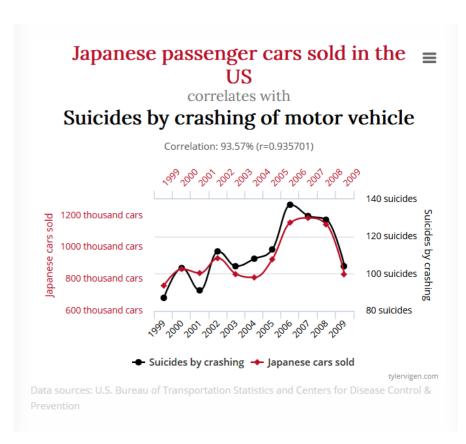
# Objectives of this lecture

- Time Series data: Different data points represent different points in time
- This introduces some additional challenges
- We will discuss how to deal with those

# What's the challenge of time series data?







Can you spot the problem?

Time becomes a confounding variable
Non-stationary: characteristics of data vary with time

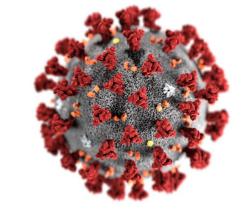
## COVID vs GDP

What you

think is

## week WEI Index cases deaths Inindex lockshare

## coince to



```
## 1 2008-01-05 1.42 1.00000 0 0 0.0000000000 0 0 ## 2 2008-01-12 1.46 1.00028 0 0 0.0005498488 0 ## 4 2008-01-26 0.96 1.00073 0 0 0.0007297337 0 ## 5 2008-02-02 0.73 1.00088 0 0 0.0008796130 0 ## 6 2008-02-09 0.78 1.00103 0 0 0.0010294699 0
```

More COVID = more GDP? 100K more = 5% more GDP?

#### In 100K of cases

```
2.50

2.00

1.00

Colour

Covid Cases per 100K

Conomic Activity Index

0.50

0.50

0.50

0.00

0.00

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```

```
lm(lnindex~cases,df) %>% summary()
```

```
##
## Call:
## lm(formula = lnindex ~ cases, data = df)
## Residuals:
        Min
                   10
                        Median
## -0.108375 -0.064942 -0.002043 0.05
                                           0.121388
##
## Coefficients:
              Estimate Std.
                            rror t value Pr(>|t|)
## (Intercept) 0.082359 0.002731 30.156 < 2e-16 ***
## cases
              0.050576 0.007800
                                   6.484 1.74e-10 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.06928 on 669 degrees of freedom
## Multiple R-squared: 0.05913, Adjusted R-squared: 0.05772
## F-statistic: 42.04 on 1 and 669 DF, p-value: 1.736e-10
```

## Taking control of time....with a timeline

```
df=df %>% mutate(t=1:n())
lm(lnindex~cases+t,df) %>% summary()
```

```
##
## Call:
## lm(formula = lnindex ~ cases + t, data = df)
## Residuals:
        Min
                 1Q Median
                                              Max
## -0.024859 -0.004965 -0.001175 0.003861 0.038124
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -3.850e-02 9.170e-04 -41.98 <2e-16 ***
         -2.262e-02 1.393e-03 -16.23 <2e-16 ***
             3.752e-04 2.466e-06 152.11 <2e-16 ***
## t
## Signif. c s: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
                      or: 0.01161 on 668 degrees of freedom
## Residual
## Multiple
                           26, Adjusted R-squared: 0.9735
## F-statist:
                               d 668 DF, p-value: < 2.2e-16
```

100k more cases = 2.26% lower GDP



#### What if time is not linear?

- Seasonal effects
- Recessions
- Natural disasters

- Political turmoil
- War
- Pandemic

#### Panel data to the rescue

```
head(statsbyweek %>% arrange(state,week))
```

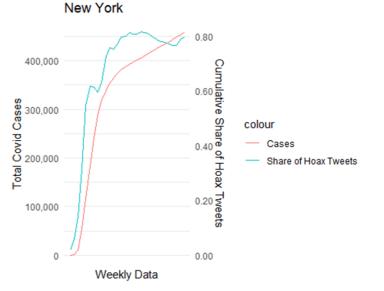
```
A tibble: 6 x 9
            state [1]
 Groups:
  state
          week
                      hoax tweets cases deaths hoaxsh Dcases Ddeaths
  <chr>
          <date>
                             <int> <int>
                                          <int>
                                                 <dbl>
                                                        <int>
                                                                 <int>
1 Alabama 2020-03-15
                         4
                             1503
                                      51
                                                 0.266
                                              0
                                                           NA
                                                                    NA
2 Alabama 2020-03-22
                              4198
                                     386
                                              1 1.48
                                                           335
                                                                     1
                         62
3 Alabama 2020-03-29
                                   1108
                                                                    27
                        14
                             5218
                                             28 0.268
                                                           722
4 Alabama 2020-04-05
                        12
                              4793
                                    2498
                                             67
                                                 0.250
                                                         1390
                                                                    39
5 Alabama 2020-04-12
                         9
                              4486
                                    4241
                                                 0.201
                                                          1743
                                                                    56
                                            123
6 Alabama 2020-04-19
                                                         1369
                                                                    78
                              3570
                                    5610
                                            201
                                                 0.168
```

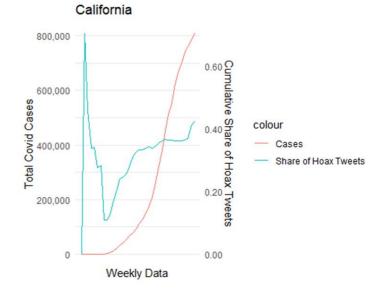
```
\verb|statsbyweek| \$>\$ \  \, \verb|group_by(state)| \$>\$ \  \, \verb|summarise(n())|
```

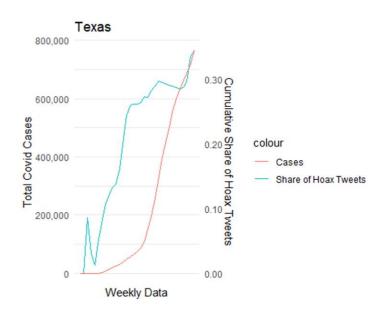
```
## `summarise()` ungrouping output (override with `.groups` argument)
```

```
A tibble: 50 x 2
      state
                   `n() `
      <chr>
                   <int>
   1 Alabama
    2 Alaska
                      29
   3 Arizona
                      36
    4 Arkansas
    5 California
    6 Colorado
    7 Connecticut
    8 Delaware
                      30
   9 Florida
                      31
## 10 Georgia
## # ... with 40 more rows
```

Multiple periods for the same cross section unit







## Panel data

•	state		hoax ‡	tweets 🕏	cases ‡	deaths 🕏	hoaxsh ‡	Dcases <sup>‡</sup>	Ddeaths 🕏	cumhoax ‡	cumtweets	cumhoaxsh ‡	Dcumhoaxsh ‡
1	Alabama	2020-03-08	1	443	12	0	0.22573363	NA	NA	1	443	0.22573363	NA
2	Alabama	2020-03-15	13	2098	131	0	0.61963775	119	0	14	2541	0.55096419	3.252306e-01
3	Alabama	2020-03-22	57	5824	720	4	0.97870879	589	4	71	8365	0.84877466	2.978105e-01
4	Alabama	2020-03-29	10	4750	1632	44	0.21052632	912	40	81	13115	0.61761342	-2.311612e-01
5	Alabama	2020-04-05	16	4477	3262	93	0.35738218	1630	49	97	17592	0.55138699	-6.622643e-02
6	Alabama	2020-04-12	6	4180	4723	151	0.14354067	1461	58	103	21772	0.47308470	-7.830230e-02
7	Alabama	2020-04-19	7	3294	6213	213	0.21250759	1490	62	110	25066	0.43884146	-3.424324e-02
8	Alabama	2020-04-26	5	2435	7611	289	0.20533881	1398	76	115	27501	0.41816661	-2.067485e-02
9	Alabama	2020-05-03	20	593	9668	390	3.37268128	2057	101	135	28094	0.48052965	6.236304e-02
10	Alabama	2020-05-10	21	429	11674	485	4.89510490	2006	95	156	28523	0.54692704	6.639739e-02
11	Alabama	2020-05-17	5	816	14149	549	0.61274510	2475	64	161	29339	0.54875763	1.830585e-03
21	Alabama	2020-09-00	0	4 321	15/040	2550	1.22324139	<b>5045</b>	75	205	59050	U.32400734	<b>5.</b> 090404e-05
28	Alabama	2020-09-13	3 2	1 381	144164	2437	5.51181102	6518	87	226	39437	0.57306590	4.817856e-02
29	Alabama	2020-09-20	0	0 280	151591	2506	0.00000000	7427	69	226	39717	0.56902586	-4.040045e-03
30	Alaska	2020-03-08	В	1 59	1	0	1.69491525	NA	NA	1	59	1.69491525	NA
31	Alaska	2020-03-15	5	5 300	21	0	1.66666667	20	0	6	359	1.67130919	-2.360606e-02
32	Alaska	2020-03-22	2	1 776	102	1	0.12886598	81	1	7	1135	0.61674009	-1.054569e+00
33	Alaska	2020-03-29	9 3	8 863	169	3	4.40324450	67	2	45	1998	2.25225225	1.635512e+00
34	Alaska	2020-04-05	5	7 993	255	6	0.70493454	86	3	52	2991	1.73854898	-5.137033e-01
35	Alaska	2020-04-12	2 .	7 805	312	7	0.86956522	57	1	59	3796	1.55426765	-1.842813e-01
36	Alaska	2020-04-19	9 (	6 842	337	7	0.71258907	25	0	65	4638	1.40146615	-1.528015e-01
37	Alaska	2020-04-26	5	3 741	363	7	0.40485830	26	0	68	5379	1.26417550	-1.372907e-01
38	Alaska	2020-05-03	3	1 105	377	8	0.95238095	14	1	69	5484	1.25820569	-5.969808e-03
39	Alaska	2020-05-10	) :	3 109	392	8	2.75229358	15	0	72	5593	1.28732344	2.911775e-02
40		2020 05 45	,	1 113	400		0.0000574.4	47	_	72	F 705	1 27057022	774424 03

## Panel data example

```
Hoax share up by 1
                                                 percentage point means
lm(cases~cumhoaxsh, statsbyweek) %>% summary()
                                                   121120 more cases
##
## Call:
## lm(formula = cases ~ cumhoaxsh, data = stats
## Residuals:
               10 Median
      Min
                              3Q
   -294697 -38574
                             3608
                  -24113
## Coefficients:
              Estimate Std. Fror t value Pr(>|t|)
                                   5.348 1.02e-07 ***
                 22072
## (Intercept)
## cumhoaxsh
                121120
                           11220
                                 10.796 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 103100 on 1518 degrees of freedom
## Multiple R-squared: 0.0713, Adjusted R-squared: 0.07069
## F-statistic: 116.5 on 1 and 1518 DF, p-value: < 2.2e-16
lm(cases~cumhoaxsh+factor(week), statsbyweek) %>% summary()
## Call:
## lm(formula = cases ~ cumhoaxsh + factor(week), data =
statsbyweek)
                                               Smaller effect when
##
## Residuals:
                                               controlling for time
       Min
                1Q Median
                                 3Q
                                                  (week) effects
                                    6656
  -182000 -36269
                      -9070
                               5947
##
   Coefficients:
                           Estimate Std
                                          ror t value Pr(>|t|)
## (Intercept)
                                          55848
                                                  0.000
                                                          1.0000
## cumhoaxsh
                              72056
                                          11578
                                                  6.224 6.31e-10 ***
## factor(week)2020-01-26
                             -10172
                                          70662
                                                 -0.144
                                                          0.8856
## factor(week)2020-02-02
                              -5521
                                          68406
                                                 -0.081
                                                          0.9357
                              -3486
## factor(week)2020-02-09
                                          66754
                                                 -0.052
                                                          0.9584
## factor(week)2020-02-16
                              -3073
                                          65490
                                                -0.047
                                                          0.9626
## factor(week)2020-02-23
                             -17368
                                          63738
                                                -0.272
                                                          0.7853
## factor(week)2020-03-01
                              -3010
                                          58410
                                                -0.052
                                                          0.9589
                              -4210
## factor(week)2020-03-08
                                          57537 -0.073
                                                          0.9417
                                                -0.104
## factor(week)2020-03-15
                              -5968
                                          57509
                                                          0.9174
## factor(week)2020-03-22
                              -4942
                                          57512 -0.086
                                                          0.9315
```

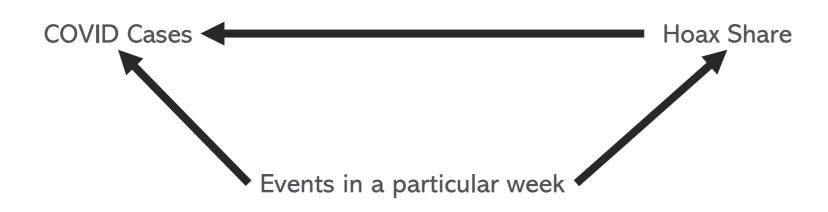
```
lm(cases~cumhoaxsh+factor(state)+factor(week),statsbyweek) %>% summary()
## Call:
  lm(formula = cases ~ cumhoaxsh + factor(state) + factor(week),
       data = statsbyweek)
##
##
  Residuals:
      Min
                10 Median
                                3Q
                                       Max
  -244737 -21562
                      1446
                             21041 463246
##
  Coefficients:
                               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                -109303
                                             41227 -2.651 0.008107 **
                                  61619
  cumhoaxsh
                                             19128
                                                     3.221 0.001304 **
  factor(state)Alaska
                                 -96560
                                             22677
                                                    -4.258 2.20e-05 ***
  factor(state)Arizona
                                  34689
                                             16951
                                                     2.046 0.040899
                                  -9094
  factor(state)Arkansas
                                             18337
                                                    -0.496 0.620015
                                 224047
  factor(state)California
                                             17120
                                                    13.087 < 2e-16 ***
  factor(state)Colorado
                                  -8425
                                             17692
                                                    -0.476 0.634008
## factor(state)Connecticut
                                   4626
                                             18572
                                                     0.249 0.803343
## factor(state)Delaware
                                 -31191
                                             17875
                                                   -1.745 0.081207
## factor(state)Florida
                                 206617
                                             17752 11.639 < 2e-16 ***
```

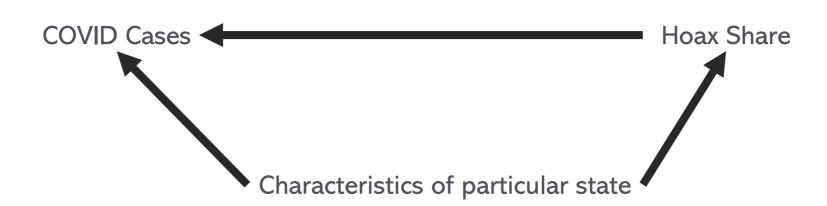
#### Also controlling for state

e.g.: more rural and less densely populated states have also less people engaged in hoax conspiracies

Example issue: suppose in some weeks there are school holidays (and hence a lower number of covid cases). Also suppose that hoax tweeters are more active over the holidays

## Time and cross sectional unit as co-founder



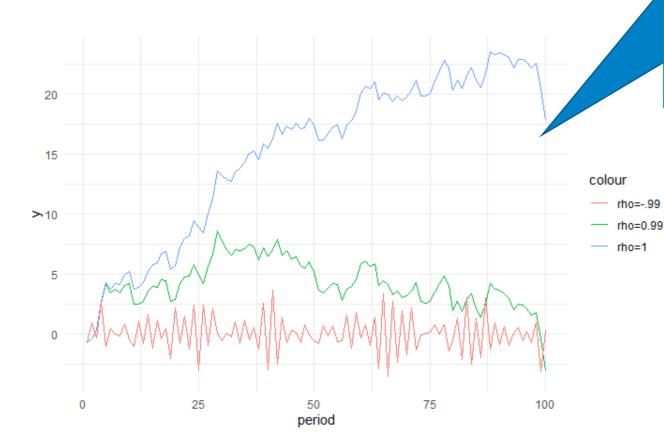


## Autoregression

- A particular concern in time series is the possibility that observations are correlated over time
- Simplest way to model this is via an Auto regression:

• 
$$Y_t = \beta_0 + \rho Y_{t-1} + \epsilon_t$$

 $Y_{t-1}$  becomes the X variable We can do normal OLS as long as  $-1 < \rho < 1$ 



- With  $\rho = 1$  we have non-stationarity because of path dependence
- The series can wander off into any direction and neve come back
- If that happens OLS is no longer un-biased (different observations are too related to each other)
- Also: if you are interested in  $Y = \beta X$  (i.e. the casual effect of X on Y) you get biased estimates
- Random Walk
- Of course we don't know if this is the case in our data before we start any analysis

Need to test  $\hat{\rho}=1$  but cannot use simple t or F test because under HO it would be biased



## Dickey-Fuller test to the rescue



Rewrite original model by subtracting  $Y_{t-1}$  on both sides of the model equation:

$$Y_{t} = \beta_{0} + \rho Y_{t-1} + \epsilon_{t}$$

$$\downarrow \qquad \qquad \qquad \downarrow$$

$$Y_{t} - Y_{t-1} = \Delta Y_{t} = \beta_{0} + \underbrace{(\rho - 1)}_{=\delta} Y_{t-1} + \epsilon_{t}$$

Testing for a random walk (aka unit root) now boils down to

H0:  $\delta$ =0

H1:  $\delta$ <0 i.e. stationary process

- We cannot just compare the implied test statistic to a normal t-table
- Luckily R will help us

## R to the rrrrrescue

```
library(urca)
 ur.df(df$lnindex) %>% summary()
##
## # Augmented Dickey-Fuller Test Unit Root Test #
##
## Test regression none
##
##
## Call:
## lm(formula = z.diff ~ z.lag.1 - 1 + z.diff.lag)
##
## Residuals:
##
        Min
                         Median
                   1Q
                                      3Q
                                               Max
## -8.343e-04 -2.643e-05 4.240e-06 4.131e-05 1.922e-04
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## z.lag.1 -2.155e-05 2.703e-05 -0.797
                                         0.426
## z.diff.lag 9.924e-01 5.596e-03 177.334 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' '
1
##
## Residual standard error: 7.414e-05 on 667 degrees of freedom
## Multiple R-squared: 0.9812, Adjusted R-squared: 0.9811
## F-statistic: 1.739e+04 on 2 and 667 DF, p-value: < 2.2e-16
##
##
## Value of test-statistic is: -0.7971
##
## Critical values for test statistics:
       1pct 5pct 10pct
## tau1 -2.58 -1.95 -1.62
```

We cannot reject unit root because -0.7971>-1.95

## Getting rid of unit roots – Economic Activity index

```
ur.df(diff(df$lnindex,1),type="none",lags=1) %>% summary()
## # Augmented Dickey-Fuller Test Unit Root Test #
                                                         Differencing: \Delta y_t = y_t - y_{t-1}
## Test regression none
                                                         Checking that differenced
##
## Call:
                                                         series is not unit rood
## lm(formula = z.diff ~ z.lag.1 - 1 + z.diff.lag)
## Residuals:
            1Q Median
        Min
## -8.236e-04 -3.079e-05 3.980e-06 4.133e-05 1.963e-04
## Coefficients:
          Estimate Std. Error t value Pr(>|t|)
## z.lag.1 -0.010977 0.005233 -2.098 0.0363 *
## z.diff.lag 0.195464 0.038082 5.133 3.75e-07 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 7.28e-05 on 666 degrees of freedom
## Multiple R-squared: 0.04215, Adjusted R-squared: 0.03927
## F-statistic: 14.65 on 2 and 666 DF, p-value: 5.92e-07
##
## Value of test-statistic is: -2.0976
                                                      We can reject unit root (at
                                                           least at 5%)
## Critical values for test statistics:
       1pct 5pct 10pct
## tau1 -2.58 -1.95 -1.62
```

## Revisiting COVID vs GDP

```
df=df %>% arrange(week) %>% mutate( Dlnindex=lnindex - dplyr::lag(lnindex) ,Llnindex=dplyr::lag(lnindex) )
lm(Dlnindex~cases+t,df) %>% summary()
##
## Call:
## lm(formula = Dlnindex ~ cases + t, data = df)
##
## Residuals:
                            Median
         Min
                     1Q
                                           3Q
                                                     Max
## -2.175e-03 -6.473e-05 7.992e-05 1.627e-04 1.327e-03
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 1.729e-04 3.019e-05 5.726 1.55e-08 ***
              -9.290e-04 4.573e-05 -20.314 < 2e-16 ***
## cases
               3.831e-07 8.113e-08 4.723 2.84e-06 ***
## t
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.0003811 on 667 degrees of freedom
   (1 observation deleted due to missingness)
## Multiple R-squared: 0.3856, Adjusted R-squared: 0.3838
## F-statistic: 209.3 on 2 and 667 DF, p-value: < 2.2e-16
```

100k more cases = 0. 0929% lower GDP...

## Lagging

```
df=df %>% arrange(week) %>% mutate( Dlnindex=lnindex - dplyr::lag(lnindex) ,Llnindex=dplyr::lag(lnindex) )
lm(Dlnindex~cases+t,df) %>% summary()
##
## Call:
## lm(formula = Dlni
##
## Residuals:
            Min
##
## -2.175e-03 -6.473
                                 Note how to create lagged values: use the
##
                                                     dplyr::lag() function
## Coefficients:
                     Est
## (Intercept)
                   1.72
                  -9.29
## cases
## t
                   3.83
## ---
                       0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual
                          T Filter
      (1 ob:
                                                                                        † t
                               WEI
                                       Index
                                                                   Inindex
                                                                               lockshare
                                                                                                   Dlnindex
                                                                                                                LInindex
## Multipl
                                                                                        0
                                                                                                            NA
                                                                                                                         NA
## F-stati:
                   1 2008-01-05
                                   1.42
                                         1.00000
                                                      0
                                                                   0.0000000000
                   2 2008-01-12
                                   1.46
                                         1.00028
                                                      0
                                                                   0.0002799608
                                                                                        0
                                                                                                    2.799608e-04
                                                                                                                 0.0000000000
                     2008-01-19
                                         1.00055
                                                                   0.0005498488
                                                                                        0
                                   1.40
                                                                                                    2.698880e-04
                                                                                                                 0.0002799608
                     2008-01-26
                                   0.96
                                         1.00073
                                                      0
                                                                   0.0007297337
                                                                                        0
                                                                                                    1.798849e-04
                                                                                                                 0.0005498488
                     2008-02-02
                                   0.73
                                         1.00088
                                                                   0.0008796130
                                                                                        0
                                                                                                    1.498793e-04
                                                                                                                 0.0007297337
                     2008-02-09
                                   0.78
                                         1.00103
                                                                   0.0010294699
                                                                                        0
                                                                                                    1.498569e-04
                                                                                                                 0.0008796130
                     2008-02-16
                                         1.00125
                                                                   0.0012492194
                                                                                        0
                                                                                                    2.197495e-04
                                                                                                                 0.0010294699
                                   1.18
                   8 2008-02-23
                                   0.91
                                         1.00143
                                                      0
                                                                   0.0014289785
                                                                                        0
                                                                                                    1.797591e-04
                                                                                                                 0.0012492194
                   9 2008-03-01
                                   0.95
                                         1.00161
                                                      0
                                                                  0.0016087053
                                                                                        0
                                                                                                    1.797268e-04
                                                                                                                 0.0014289785
                     2008-03-08
                                   0.52
                                         1.00171
                                                                0 0.0017085396
                                                                                                    9.983428e-05
                                                                                                                 0.0016087053
```

## Lagging with panel data

```
statsbyweek = statsbyweek %>%
                     arrange(state, week) %>%
                     group_by(state) %>%
                     mutate(Dcases=cases-dplyr::lag(cases,1),
                                Ddeaths=deaths-dplyr::lag(deaths,1))
                                     † hoax † tweets † cases † deaths
                                                                          hoaxsh Dcases Ddeaths
                           ÷ week
                   state
                1 Alabama
                              2020-03-08
                                                      443
                                                                           0 0.22573363
                  Alabama
                                                                                               119
                                                                                                            0
                              2020-03-15
                                             13
                                                     2098
                                                               131
                                                                           0 0.61963775
                   Alabama
                                                                                               589
                                                                                                            4
                              2020-03-22
                                                     5824
                                                               720
                                                                              0.97870879
                   Alabama
                              2020-03-29
                                             10
                                                     4750
                                                              1632
                                                                          44
                                                                              0.21052632
                                                                                               912
                                                                                                            40
                                                                                              1630
                              2020-04-05
                                             16
                                                     4477
                                                              3262
                                                                          93
                                                                              0.35738218
                                                                                                            49
                5 Alabama
                6 Alabama
                              2020-04-12
                                              6
                                                     4180
                                                              4723
                                                                         151
                                                                              0.14354067
                                                                                              1461
                                                                                                            58
                              2020-04-19
                                                     3294
                                                              6213
                                                                         213
                                                                              0.21250759
                                                                                              1490
                                                                                                            62
                  Alabama
                              2020-04-26
                                                                              0.20533881
                                                                                              1398
                                                                                                            76
                                                     2435
                                                              7611
                                                                         289
                  Alabama
                              2020-05-03
                                             20
                                                      593
                                                              9668
                                                                              3.37268128
                                                                                              2057
                                                                                                           101
                9 Alabama
                                                                         390
                              2020-05-10
                                                             11674
                                                                              4.89510490
                                                                                              2006
                                                                                                            95
               10 Alabama
                                                      429
                                                                         485
               11 Alabama
                              2020-05-17
                                                      816
                                                             14149
                                                                         549
                                                                              0.61274510
                                                                                              2475
                                                                                                            64
               12 Alabama
                                              3
                                                             17359
                                                                         618 0.58252427
                                                                                              3210
                                                                                                            69
                              2020-05-24
                                                      515
               29 Alabama
                                                           151591
                                                                                                       69
                             2020-09-20
                                                                      2506
                                                                           0.00000000
                                                                                           7427
                                                     280
               30 Alaska
                             2020-03-08
                                                     59
                                                                           1.69491525
                                                                                           NA
                                                                                                        0
               31 Alaska
                             2020-03-15
                                                                                            20
                                                     300
                                                                            1.66666667
               32 Alaska
                             2020-03-22
                                                    776
                                                             102
                                                                           0.12886598
                                                                                            81
                                                                                            67
               33 Alaska
                             2020-03-29
                                            38
                                                    863
                                                             169
                                                                        3 4.40324450
                                                                                                        3
               34 Alaska
                             2020-04-05
                                                     993
                                                             255
                                                                           0.70493454
                                                                                            86
               35 Alaska
                             2020-04-12
                                                                                            57
                                                    805
                                                             312
                                                                        7 0.86956522
                                                                                                        0
               36 Alaska
                             2020-04-19
                                                    842
                                                             337
                                                                                            25
                                                                        7 0.71258907
                                                                                                        0
               37 Alaska
                             2020-04-26
                                                     741
                                                             363
                                                                           0.40485830
                                                                                            26
               38 Alaska
                             2020-05-03
                                                     105
                                                             377
                                                                        8 0.95238095
                                                                                            14
               39 Alaska
                             2020-05-10
                                                     109
                                                             392
                                                                        8 2.75229358
                                                                                            15
                                                                                                        0
```

## Summary

- Time series can be easy
- But you need to worry about how stationary your series is
- If the series clearly grows or shrinks continuously definitely include a time trend
- However, even if it doesn't grow (or shrink) the series might contain a unit root
- If that's the case a time trend is not enough
- Use the Dickey Fuller Test to make sure you are dealing with a stationary series
- If not take first difference and check Dickey Fuller again
- Reliable causal estimators you can only get from a stationary series.
- If you have panel data you can control for specific time effects (and cross sectional unit effects)



# **Extra Slides**



#### Other considerations

```
lm(Dlnindex~cases+lockshare+t,df) %>% summary()
##
## Call:
## lm(formula = Dlnindex ~ cases + lockshare + t, data = df)
##
## Residuals:
                            Median
         Min
                     10
                                           30
                                                     Max
## -9.141e-04 -1.092e-04 2.947e-05 1.456e-04 1.104e-03
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 1.209e-04 2.266e-05
                                      5.335 1.31e-07 ***
               5.646e-04 7.334e-05 7.698 5.00e-14 ***
## cases
              -2.772e-05 1.205e-06 -23.014 < 2e-16 ***
## lockshare
               6.278e-07 6.152e-08 10.205 < 2e-16 ***
## t
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.0002847 on 666 degrees of freedom
    (1 observation deleted due to missingness)
## Multiple R-squared: 0.6578, Adjusted R-squared: 0.6562
## F-statistic: 426.7 on 3 and 666 DF, p-value: < 2.2e-16
```

- lockshare=percentage of population in lockdown
- If 100% of US population go into lockdown GDP goes down by -0.2772% (seems low..more research needed)

## More lags AR(2)?

$$Y_t = \beta_0 + \beta_1 Y_{t-1} + \beta_2 Y_{t-2} + u_t.$$

Stationarity now requires

$$\beta_1 + \beta_2 < 1$$

while

$$\beta_1 + \beta_2 = 1$$

$$Y_t - Y_{t-1} = \beta_0 + (\beta_1 + \beta_2 - 1)Y_{t-1} - \beta_2(Y_{t-1} - Y_{t-2}) + \epsilon_t$$

We can test this again using the coefficient on  $Y_{t-1}$ 

## More lags and trend?

$$Y_t - Y_{t-1} = \beta_0 + (\beta_1 + \beta_2 - 1)Y_{t-1} - \beta_2(Y_{t-1} - Y_{t-2}) + \rho t + \epsilon_t$$

## Further reading

- On time fixed effects: <u>Hanck et al Chapter 10.4</u>
- Unit roots: <u>Hanck et al Chapter 14.7</u>

