

Math 181A HW9

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Problem 19-1. In Finance, a return is the change in price of an asset, investment, or project over time, which may be represented in terms of price change or percentage change. We define discrete return and continuous return based on different application. The discrete return, which is the division between the change from yesterday's price to today's price and yesterday's price, will be used in this problem. If we denote S_t as the price at day t , then the discrete return at day t is $r_t = \frac{S_t - S_{t-1}}{S_{t-1}}$. Construct a 90% bootstrap confidence interval of the discrete return based on the APPLE stock price data from 01/01/2023 - 05/23/2023.

Problem 7.5.7 Start with the fact that $(n-1)S^2/\sigma^2$ has a chi square distribution with $n-1$ df (if the Y_i 's are normally distributed) and derive the confidence interval formulas given in Theorem 7.5.1:

- (a) a $100(1-\alpha)\%$ confidence interval for σ^2 is the set of values

$$\left(\frac{(n-1)s^2}{\chi_{1-\alpha/2, n-1}^2}, \frac{(n-1)s^2}{\chi_{\alpha/2, n-1}^2} \right)$$

- (b) a $100(1-\alpha)\%$ confidence interval for σ is the set of values

$$\left(\sqrt{\frac{(n-1)s^2}{\chi_{1-\alpha/2, n-1}^2}}, \sqrt{\frac{(n-1)s^2}{\chi_{\alpha/2, n-1}^2}} \right)$$

Problem 7.5.12

- (a) Use the asymptotic normality of chi square random variables (see Question 7.3.6) to derive large-sample confidence interval formulas for σ and σ^2 .
- (b) Use your answer to part (a) to construct an approximate 95% confidence interval for the standard deviation of estimated potassium-argon ages based on the nineteen y_i 's in Table 7.5.1. How does this

confidence interval compare with the one in Case Study 7.5.1: (20.5 million years, 40.0 million years)?

<i>Specimen</i>	<i>Estimated Age (millions of years)</i>
1	249
2	254
3	243
4	268
5	253
6	269
7	287
8	241
9	273
10	306
11	303
12	280
13	260
14	256
15	278
16	344
17	304
18	283
19	310