

Technical Aside

Viable prefix -- automaton

References:

- <https://stackoverflow.com/questions/4202181/explanation-about-viable-prefix>
- Lecture notes at http://www.cs.williams.edu/~tom/courses/434/outlines/lect14_2.html
- [Parsing theory vol II Book:](#)
Sippu, Seppo, and Eljas Soisalon-Soininen. *Parsing Theory: Volume II LR (k) and LL (k) Parsing*. Vol. 20. Springer Science & Business Media, 2013.

Right-sentential form

- A **right-sentential form** is a sentential form which can be reached by rightmost derivation,
 - which is another way to describe repeated expansion of only the rightmost non-terminal when proceeding from the start symbol.
 - This is a rightmost derivation, and all the forms in it are therefore right-sentential forms:

Example: right-sentential form

- For the following grammar, Terminals = { **NUMBER**, +, *, (,) }

```
expr -> expr + term | term
term -> term * factor | factor
factor -> NUMBER | ( expr )
```

- Each *right hand side* is a right-sentential form

```
expr -> expr + term
      -> expr + term * factor
      -> expr + term * NUMBER
      -> expr + factor * NUMBER
      -> expr + NUMBER * NUMBER
      -> expr + term + NUMBER * NUMBER
      -> expr + NUMBER + NUMBER * NUMBER
      -> term + NUMBER + NUMBER * NUMBER
      -> NUMBER + NUMBER + NUMBER * NUMBER
```

Last one is a right-most sentential form and a sentence.

Prefix of a sentential form

- A **prefix** of a sentential form (whether right or otherwise) is a sequence of input symbols that consists of zero or more leading symbols of that sentential form.
 - The empty sequence is trivially a prefix of every sentential form, and
 - the complete sequence of symbols making up a sentential form is also trivially a prefix of it.
- Can be generalized to prefix of a right-sentential form.

```
expr -> expr + term | term
term -> term * factor | factor
factor -> NUMBER | ( expr )
```

```
expr -> expr + term
      -> expr + term * factor
      -> expr + term * NUMBER
      -> expr + factor * NUMBER
      -> expr + NUMBER * NUMBER
      -> expr + term + NUMBER * NUMBER
      -> expr + NUMBER + NUMBER * NUMBER
      -> term + NUMBER + NUMBER * NUMBER
      -> NUMBER + NUMBER + NUMBER * NUMBER
```

- Some prefixes of right-sentential forms:

€

expr

expr + term

expr + term *

expr +

expr + term * factor

expr + term * NUMBER

expr + factor *

term + NUMBER +

NUMBER + NUMBER +

NUMBER + NUMBER + NUMBER *

```
expr -> expr + term | term
term -> term * factor | factor
factor -> NUMBER | ( expr )
```

```
expr -> term
      -> term * factor
      -> . .
```

- These are also prefixes of right-sentential forms:

```
term
```

```
term *
```

```
term * factor
```

Simple phrase

- A **simple phrase** is the expansion of a single non-terminal symbol that holds a place in a sentential form.
 - In the given example, **term * factor** is a simple phrase because it is an expansion of **term**.
 - **term**, **factor**, **NUMBER**, **term * factor**, **(expr)** are also simple phrases

```
expr -> expr + term | term
term -> term * factor | factor
factor -> NUMBER | ( expr )
```


The handle

- The **handle**: In a right-sentential form, it is a *simple phrase* that is included because of expansion of a non-terminal most recently.
 - In a rightmost derivation, the handle is easy to identify, since
 - it's the sequence of symbols that resulted from the most recently expanded non-terminal.
 - In LR parsing, **the handle** is the *simple phrase* that needs to be *reduced* at that point of parsing.

```
expr -> expr + term | term
term -> term * factor | factor
factor -> NUMBER | ( expr )
```

```
expr -> expr + term
      -> expr + term * factor
      -> expr + term * NUMBER
      -> expr + factor * NUMBER
      -> expr + NUMBER * NUMBER
      -> expr + term + NUMBER * NUMBER
      -> expr + NUMBER + NUMBER * NUMBER
      -> term + NUMBER + NUMBER * NUMBER
      -> NUMBER + NUMBER + NUMBER * NUMBER
```

```
expr -> expr + term
      -> expr + term * factor
      -> expr + term * NUMBER
      -> expr + factor * NUMBER
      -> expr + NUMBER * NUMBER
      -> expr + term + NUMBER * NUMBER
      -> expr + NUMBER + NUMBER * NUMBER
      -> term + NUMBER + NUMBER * NUMBER
      -> NUMBER + NUMBER + NUMBER * NUMBER
```

handle

Viable prefix

- A **viable prefix** of a right-sentential form is a prefix which does not extend beyond that form's handle –
 - in other words, that prefix which contains no reducible simple phrases, except possibly the handle (in this case, the prefix extends exactly to the end of the handle).

```

expr -> expr + term
      -> expr + term * factor
      -> expr + term * NUMBER
      -> expr + factor * NUMBER
      -> expr + NUMBER * NUMBER
      -> expr + term + NUMBER * NUMBER
      -> expr + NUMBER + NUMBER * NUMBER
      -> term + NUMBER + NUMBER * NUMBER
      -> NUMBER + NUMBER + NUMBER * NUMBER

```

```

expr -> expr + term | term
term -> term * factor | factor
factor -> NUMBER | ( expr )

```

- Some viable prefixes:

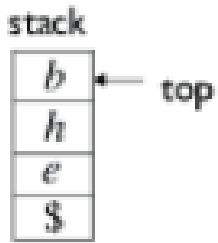
ϵ , expr, expr +, expr + tem, expr + tem *,
 term, NUMBER, term * NUMBER

expr -> term
 -> term * factor
 -> term * NUMBER

- Below are not viable prefixes:

expr + factor *, term +, term + NUMBER,
 NUMBER +, NUMBER + NUMBER

Viable prefix on stack makes you happy

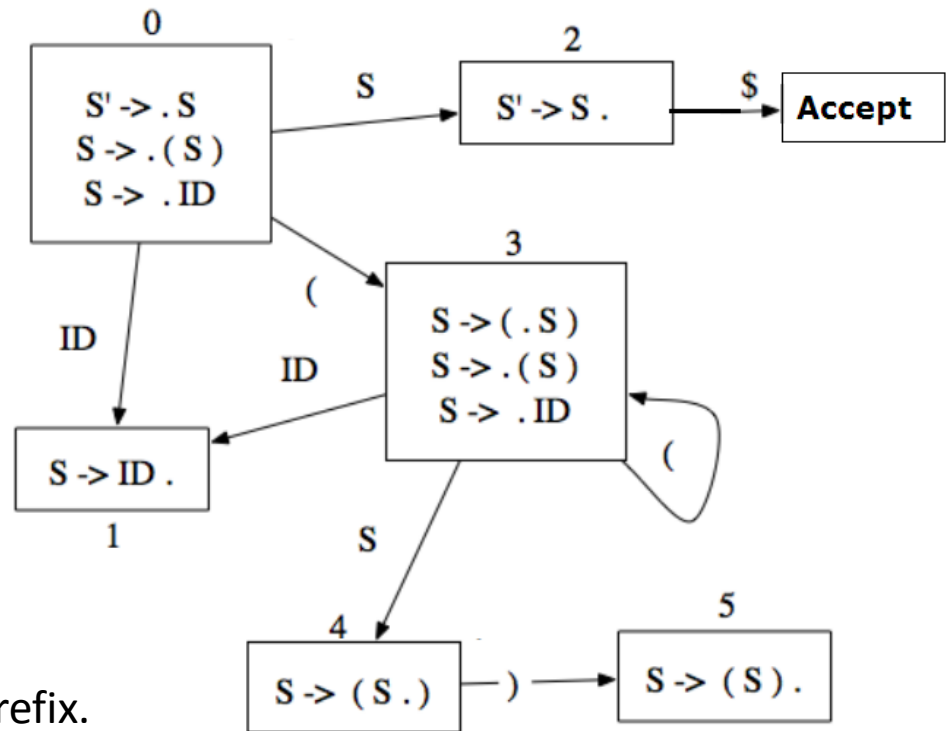


- From a shift-reduce parser's point of view, as long as you have a viable prefix on the stack, you can expect for a successful parse.
 - if handle appears on top of the stack, you will reduce.
 - Else you will shift the next token
 - if this makes the contents of stack in to a **non-viable prefix**, you will declare *fail*.

WHY VIABLE PREFIX?

- **The set of all viable prefixes of a context-free language is itself a regular language!**
- You can therefore build a finite automaton that recognizes the regular language of viable prefixes, and use it to determine when to shift and when to reduce.
- This combination of a stack and a finite state machine is essentially a push-down automaton, which is exactly the class of automaton needed to recognize a context-free language.

(0) $S \rightarrow (S)$
 (1) $S' \rightarrow S$
 (2) $S \rightarrow id$



By traversing the LR(0) automaton, the string you get is always a viable prefix.

Eg: Few viable prefixes:

(
 ((
 ((S
 (((id

Few non-viable prefixes:

id id
 ()
)

Stack containing a viable prefix

- Stack containing a viable prefix α says that
 - There is a sequence of tokens w , such that αw is a right-most sentential form.
 - That is, we can expect a successful parse.
 - So, if the stack, somehow contains a non-viable prefix, then immediately one can say that the parse is a failure (the given string is not in the language).
 - Then, why is that even when the input string is in that language, an LR parsing can fail?

Why different LR parsers?

- From one viable prefix, we go to the next viable prefix.
 - We do shift or we do reduce, for this.
 - With one action, the stack content with remaining tokens is a right-sentential form.
 - if you come to this stage, you can expect a successful parse.
 - But, with some other action, the stack with remaining tokens is not a right-sentential form.
 - if you come to this stage, you will fail.
 - The parsing technique, if is unable to decide which action to follow, it may choose a wrong choice and fail.
 - The weak the parser, this happens frequently.
 - The strong the parser, this happens less frequently.

We can go for stronger parsers (ultimately, wrong choices can be totally avoided), but these are costly (need to see more look-ahead, need to maintain more information).

Hierarchy of languages that can be parsed by various parsers

