

- Linear regression assumptions (i) Additive assumption \rightarrow Effect of changes in a predictor X_j on the response Y is independent of other predictors. (Solution take intercept of two predictors) (ii) Linear assumption \rightarrow states that the change in the response Y due to change in X_j is constant, regardless of the value of X_j (iii) Error terms, $\epsilon_1, \epsilon_2, \dots, \epsilon_n$ are uncorrelated. (If we plot error terms there shouldn't be any pattern) (iv) Error terms have a constant variance (heteroscedasticity \rightarrow non-constant variances in the errors, makes funnel shape in residual plot. one possible solution is to transform the response Y using a concave function such as $\log Y$ or \sqrt{Y})
- $RSS(\text{ResidualSumOfSquares}) = (y_1 - \hat{\beta}_0 - \hat{\beta}_1 x_1)^2 + (y_2 - \hat{\beta}_0 - \hat{\beta}_1 x_2)^2 + \dots + (y_n - \hat{\beta}_0 - \hat{\beta}_1 x_n)^2$
- RSE (measure of the lack of fit of the model) $= \sqrt{\frac{1}{n-p-1} RSS} = \sqrt{\frac{1}{n-p-1} \sum_{i=1}^n (y_i - \hat{y}_i)^2}$
- $TSS(\text{TotalSumOfSquares}) = \sum_{i=1}^n (y_i - \bar{y})^2$, And $\dots R^2 = \frac{TSS - RSS}{TSS}$
- MeanSquaredError (values closer to zero are better) $= \frac{1}{n} \sum_{i=1}^n (y_i - \hat{f}(x))^2$, $\rightarrow \hat{f}(x_i)$ is the prediction that \hat{f} gives for the i^{th} observation
- Standard error $SE(\hat{\beta}_0)^2 = \sigma^2 \left[\frac{1}{n} + \frac{\bar{x}^2}{\sum_{i=1}^n (x_i - \bar{x})^2} \right]$ and $SE(\hat{\beta}_1)^2 = \frac{\sigma^2}{\sum_{i=1}^n (x_i - \bar{x})^2}$
- F-Statistics $= \frac{(TSS - RSS)/p}{RSS/(n-p-1)}$ \dots (p predictors, n observations. When n is large, F-statistic just above 1 might provide evidence against H_0 . If n is small a larger F-statistic is needed to reject H_0)
- If Null Hypothesis is correct $E\{TSS - RSS/p\} = \sigma^2$, If linear model assumptions are correct $E\{RSS/(n-p-1)\} = \sigma^2$, So when there is no relationship between the response and predictors, F-statistic ≈ 1
- $\text{Cor}(X, Y) = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2} \sqrt{\sum_{i=1}^n (y_i - \bar{y})^2}}$ \dots In multiple linear regression $\text{Cor}(Y, \hat{Y})^2 = R^2$
- multicollinearity \rightarrow Collinearity can exist between three or more variables even if no pair of variables has a particularly high correlation. Variance inflation factor (VIF) assess multi-collinearity. $VIF(\hat{\beta}_j) = \frac{1}{1 - R_{X_j|X_{-j}}^2}$. $VIF > 5 - 10$ Suggest strong collinearity.
- Degree of freedom = n - k - 1
- KNN $\rightarrow Pr(Y = j|X = x_0) = \frac{1}{K} \sum_{i \in N_0} I(y_i = j)$ (Given a +ve int K & observation x_0 , KNN classifier first identifies the K points that are closest to x_0 (represented by N_0), then estimates the conditional probability for class j as the fraction of points in N_0 whose response values equal j)
- KNN 2^{nd} form $\hat{f}(x_0) = \frac{1}{k} \sum_{x_i \in N_0} y_i$
- $SSR(\text{SumOfSquaredDueToRegression}) = \sum_{i=1}^n (\hat{y}_i - \bar{y})^2$, $SSE(\text{SumOfSquaredDueToError}) = \sum_{i=1}^n (y_i - \hat{y}_i)^2$, $SST = SSR + SSE = \sum_{i=1}^n (y_i - \bar{y})^2$ and $R^2 = \frac{SSR}{SST}$ = (Proportion of the variation of y being explained by the variation in x)
- HUNT \rightarrow (I) The initial tree contains a single node with class label that has majority of the outcome (II) If all the records in D_t belong to the same class y_t , then t is a leaf node labeled as y_t (III) Else partition the records into smaller subsets that yields highest Info gain $\Delta_{info} = I(\text{parent}) - \sum_{j=1}^k \frac{N(v_j)}{n} I(v_j)$. N is total records at parent Node, k is number of attributes, $N(v_j)$ is number of records associated with child node v_j . $I(.)$ = Impurity of a node $= - \sum_{i=0}^{c-1} p(i|t) \log_2 p(i|t)$ { \dots c is number of classes, $p(i|t)$ fraction of records having class i at a node t } . This algorithm is then recursively applied to each child node.
- GiniIndex $\rightarrow \sum_{i=0}^{c-1} p(i|t)^2$ { Can be used instead of entropy above } . Exam-Tan-P160-Sum-prob
- bagging $\rightarrow \hat{f}(x) = \frac{1}{B} \sum_{b=1}^B \hat{f}^{*b}(x)$ { B = bootstrapped training data sets. $\hat{f}^{*b}(x)$ = Prediction when model trained on b^{th} dataset, and finally average all the predictions }
- ConfusionMatrix $\rightarrow \text{Sensitivity} = \frac{\text{TruePositive}}{\text{TruePositive} + \text{FalseNegative}}$, $\text{Specificity} = \frac{\text{TrueNegative}}{\text{TrueNegative} + \text{FalsePositive}}$