- Height balance tree(AVL) Height  $N_h = N_{h-1} + N_{h-2} + 1$ , Is same as fibonacci So  $height = \log_{\phi} n$
- In a Red black tree, 1) Each node is either red or black 2) Every leaf (Null nodes) is black. 3) The root is black 4) No red node has a red parent or a red child 4) Paths from the root to any leaf all pass through the same number of black nodes (Constant black depth).
- RBT-Insertion (Always make new Insertion as Red)

If X's uncle is Red  $\rightarrow$  Make X's parent and uncle black and X's grandparent red.

If X's uncle is Black & and X is the right chil  $\rightarrow$ rotate the edge between X & its parent in opposite of X(yield Case 3) If X's uncle is Black and and X is the left child  $\rightarrow$  rotate the edge between X's parent and X's Grand parent in Opposite of X. Color X's parent black and its old grandparent red.

• Complexity Insertion - 1) Insert.O( $\log n$ ) + Color.O(1) + Fix Violation.( $O(\log n) \times (Recolor.O(1) + Rotation.O(1)) = O(2 \log n)$ 

```
int LCSubStr(char *X, char *Y, int m, int n) // Longest common substring
        int LCSuff[m+1][n+1];
        \begin{array}{lll} \text{int result} = 0;\\ \text{for (int } i = 0; \ i < = m; \ i + +) \end{array}
                for (int j=0; j \le n; j++)
                       else if (X[i-1] == Y[j-1])
                               \begin{array}{l} LCSuff[\,i\,][\,j\,] \,=\, LCSuff[\,i\,-1][\,j\,-1] \,+\, 1\,; \\ result \,=\, max(\,result\,\,,\,\, LCSuff[\,i\,][\,j\,]\,)\,; \end{array} 
                       else LCSuff[i][j] = 0;
         return result;
\text{def lcs}\left(X,\ Y,\ m,\ n\,\right)\colon\quad //\,\text{Longest common subsequence}
        \begin{array}{lll} \mbox{if } m =\!\!\! & 0 \mbox{ or } n =\!\!\! & 0 \colon \\ & \mbox{return } 0; \\ \mbox{elif } X[m-1] =\!\!\!\! & =\!\!\!\! & Y[n-1] \colon \\ \mbox{return } 1 + \log (X, \ Y, \ m-1, \ n-1); \end{array}
              return \max(lcs(X, Y, m, n-1), lcs(X, Y, m-1, n));
\# Returns the maximum value that can be put in a knapsack of capacity W def knapSack(W, wt, val, n): \#DP\ 0-1 KnapsackProblem. 
 K = \ [\ [0\ \text{for x in range}(W+1)] \ \text{for x in range}(n+1)]
         \begin{array}{l} 1-0 & 0 & w--0. \\ K[i][w] & = 0 \\ f & wt[i-1] <= w: \\ K[i][w] & = \max(val[i-1] + K[i-1][w-wt[i-1]], \quad K[i-1][w]) \end{array} 
                             K[i][w] = K[i-1][w]
        \mathtt{return}\ K\,[\,n\,]\,[W]
 \#val = [60\,,\,100\,,\,120] , wt = [10\,,\,20\,,\,30] , W = 50 ,n = len(val) \#print\ knapSack(W\ ,\ wt\ ,\ val\ ,\ n)
\begin{array}{c} \text{def minCoins(coins, m, V): } \\ \text{if (V == 0): \# base case} \\ \text{return 0} \end{array}
                                                   # Min Coin Change ,m is size of coins array
        res = sys.maxsize # Initialize result
        for i in range(0, m):   
# Try every coin that has smaller value than V if (coins[i] \leq V): sub_res = minCoins(coins, m, V-coins[i])
                       # Check for INT_MAX to avoid overflow and see if result can minimized
if (sub_res != sys.maxsize and sub_res + 1 < res):
    res = sub_res + 1</pre>
   \#print("Minimum coins required is", \minCoins([9, 6, 5, 1], len(coins), 11)) \# 2
```