#### Air Cargo Problem 1 Chart 1.1

| SEARCH FUNCTION                           |  | EXPANSIONS  | GOAL<br>TESTS | NEW<br>NODES | TIME seconds | PLAN<br>LENGTH |
|---|--|---|---------------|--------------|--------------|----------------|
| Non-<br>Heuristic                         | BFS:<br>Breadth First                  | 43  | 56            | 180          | 0.02         | 6              |
|   | BFT:<br>Breadth First<br>Tree          | 1458  | 1459          | 5960         | 0.82         | 6              |
|   | DFG:<br>Depth First<br>Graph           | 21  | 22            | 84           | 0.01         | 20             |
|   | DL:<br>Depth Limited                   | 101   | 271           | 414          | 0.08         | 6              |
|   | UC:<br>Uniform cost                    | 55  | 57            | 224          | 0.03         | 6              |
|   | RBFG:<br>Recursive Best<br>First Graph | 4229  | 4230          | 17023        | 2.43         | 6              |
|   | GBFG:<br>Greedy Best<br>First Graph    | 7   | 9             | 28           | 0.006        | 6              |
|   | A *                                    | 55  | 57            | 224          | 0.53         | 6              |
| Heuristic                                 | A*IP:<br>A * Ignore<br>Preconditions   | 41  | 43            | 170          | 0.03         | 6              |
|   | A*LS:<br>A * Level Sum                 | 11  | 13            | 50           | 0.48         | 6              |
| Optimal Plan Length: 6 Optimal Plan: GBFG |  | Load(C1, P1, SFO) Fly(P1, SFO, JFK) Load(C2, P2, JFK) Fly(P2, JFK, SFO) Unload(C1, P1, JFK) Unload(C2, P2, SFO) |               |              |              |                |
| Search Space Size: 2 <sup>12</sup>        |  |   |               |              |              |                |

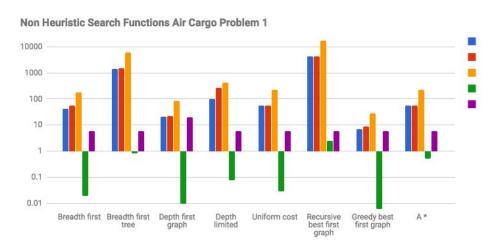


Chart 1.2

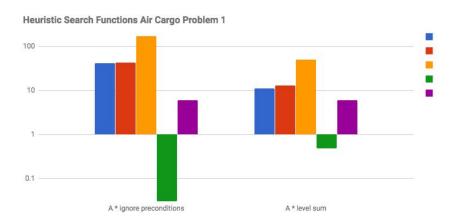


Chart 1.3

#### **Problem 1 Analysis**

This is the smallest problem of all three to be analyzed with a state space of 2<sup>12</sup>. Non-Heuristic DFG performed the fastest but had the highest plan length. GBFG had the least expansions, goal tests, new nodes and shortest plan length. DFS is not optimal with the highest plan length because it goes the deepest before considering frontier nodes. UC found the optimal plan but is slower and continues searching even after finding the optimal plan to expand the next node with the lowest cost. The heuristic search functions did not perform the best for this small problem.

#### Air Cargo Problem 2 Chart 2.1

| SEARCH FUNCTION   |  | EXPANSIONS  | GOAL<br>TESTS | NEW<br>NODES | TIME seconds | PLAN<br>LENGTH |
|---|--|---|---------------|--------------|--------------|----------------|
| Non-<br>Heuristic   | BFS:<br>Breadth First                  | 3343  | 4609          | 30509        | 12.44        | 9              |
|   | BFT:<br>Breadth First<br>Tree          | too long to compute on my mac osx   |               |              |              |                |
|   | DFG:<br>Depth First<br>Graph           | 624   | 625           | 5602         | 3.15         | 619            |
|   | DL:<br>Depth Limited                   | too long to compute on my mac osx   |               |              |              |                |
|   | UC:<br>Uniform cost                    | 4849  | 4851          | 44001        | 10.83        | 9              |
|   | RBFG:<br>Recursive Best<br>First Graph | too long to compute on my mac osx   |               |              |              |                |
|   | GBFG:<br>Greedy Best<br>First Graph    | 990   | 992           | 8910         | 28.73        | 17             |
|   | A *                                    | 4849  | 4851          | 44001        | 10.59        | 9              |
| Heuristic   | A*IP:<br>A * Ignore<br>Preconditions   | 1443  | 1445          | 13234        | 3.71         | 9              |
|   | A*LS:<br>A * Level Sum                 | 85  | 87            | 831          | 44.75        | 9              |
| Optimal Plan Length: 9  Optimal Plan: BFS  Search Space Size: 2 <sup>27</sup> |  | Load(C3, P3, ATL) Fly(P3, ATL, SFO) Unload(C3, P3, SFO) Load(C1, P1, SFO) Fly(P1, SFO, JFK) Unload(C1, P1, JFK) Load(C2, P2, JFK) Fly(P2, JFK, SFO) Unload(C2, P2, SFO) |               |              |              |                |

# Non Heuristic Search Functions Air Cargo Problem 2 10000 1000 Breadth first Depth first graph Uniform cost Greedy best first graph A\*

Chart 2.2

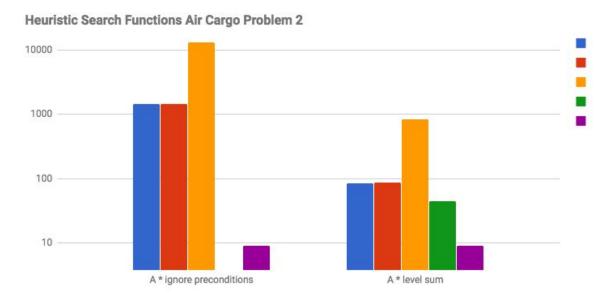


Chart 2.3

#### Problem 2 Analysis

The state space for this problem is 2<sup>27</sup>. A\*LS provided optimal plan, least number of expansions, goal tests and new nodes; but required the most time to compute. BFS was the best performer with the optimal plan of 9. DFG was fast but did not find an optimal plan.

#### Air Cargo Problem 3 Chart 3.1

| SEARCH FUNCTION                                     |  | EXPANSIONS                        | GOAL<br>TESTS   | NEW<br>NODES | TIME seconds | PLAN<br>LENGTH |
|---|--|-----------------------------------|---|--------------|--------------|----------------|
| Non-<br>Heuristic                                   | BFS:<br>Breadth First                  | 14663                             | 18098   | 128631       | 92.98        | 12             |
|   | BFT:<br>Breadth First<br>Tree          | too long to compute on my mac osx |   |              |              |                |
|   | DFG:<br>Depth First<br>Graph           | 408                               | 409   | 3364         | 1.59         | 392            |
|   | DL:<br>Depth Limited                   | too long to compute on my mac osx |   |              |              |                |
|   | UC:<br>Uniform cost                    | 18235                             | 18237   | 159716       | 45.43        | 12             |
|   | RBFG:<br>Recursive Best<br>First Graph | too long to compute on my mac osx |   |              |              |                |
|   | GBFG:<br>Greedy Best<br>First Graph    | 5462                              | 5464  | 48176        | 13.84        | 21             |
|   | A *                                    | 18235                             | 18237   | 159716       | 46.16        | 12             |
| Heuristic   | A*IP:<br>A* Ignore<br>Preconditions    | 4945                              | 4947  | 43991        | 14.25        | 12             |
|   | A*LS:<br>A * Level Sum                 | 318                               | 320   | 2934         | 231.18       | 12             |
| Optimal Plan Length: 12                             |  |                                   | Load(C1, P1, SFO)<br>Load(C2, P2, JFK)  |              |              |                |
| Optimal Plan: A* Search Space Size: 2 <sup>33</sup> |  | ·IP                               | Fly(P2, JFK, ORD)<br>Load(C4, P2, ORD)<br>Fly(P1, SFO, ATL)   |              |              |                |
|   |  | 2                                 | Load(C3, P1, ATL) Fly(P1, ATL, JFK) Unload(C1, P1, JFK) Unload(C3, P1, JFK) Fly(P2, ORD, SFO) Unload(C2, P2, SFO) Unload(C4, P2, SFO) |              |              |                |

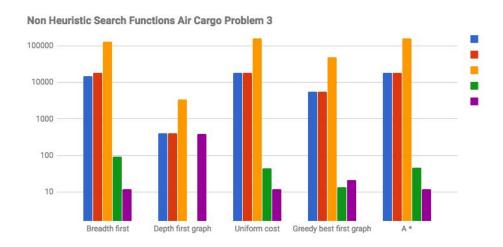


Chart 3.2



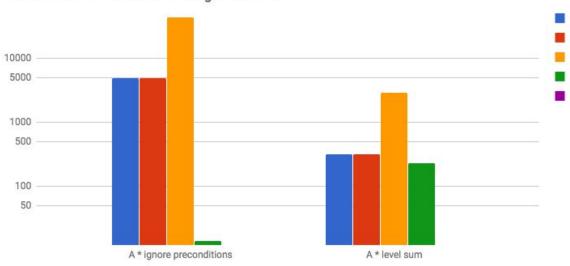


Chart 3.3

#### **Problem 3 Analysis**

State space is  $2^{32}$ , the optimal plan is up to 12 and the time in seconds to run the search is longer than the previous two problems. This is the first of our three problems to have a heuristic search as the best option; A \* ignore precondition (A\*IP).

A\*IP provided the optimal plan of 12 and performed better than the rest of the heuristic and non-heuristic functions. It was much faster than A \* level sum (A\*LS). The calculation time of A\*LS was much higher, even though it had less node expansions.

#### Conclusion

Breadth first search (BFS) was the most optimal non-heuristic search function with less expansions and faster computing time for our smallest problem with search state space of  $2^{12}$ , while the heuristic search functions (A\*IP and A\*LS) were not.

The heuristic functions had less expansions with better results for our larger problems with a search state space of  $2^{27}$  and  $2^{32}$ .

It appears that between the three algorithm choices of BFS, A\*IP and A\*LS we can get the best results and find the optimal plan with the following assumptions:

| State Search Space | Best Algorithm Choice            | Worse Algorithm Choice |  |  |
|--------------------|----------------------------------|------------------------|--|--|
| 212                | BFS<br>Breadth first search      | RBFG, BFT, DFG         |  |  |
| 227                | A*IP<br>A * Ignore Preconditions | RBFG, BFT, DL, DFG     |  |  |
| 2 <sup>32</sup>    | A*LS<br>A * Level Sum            | RBFG, DL, BFT, DFG     |  |  |

#### **REFERENCES**

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