

You take the SAT and score 1100. The mean score for the SAT is ~~100~~ 1026 and the standard deviation is 209. How well did you score on the test compared to the average test taker.

Solution:-

Mean score of SAT = $\mu = 1026$

Standard deviation of SAT = $\sigma = 209$

$$\begin{aligned} \text{My } Z \text{ score} &= \frac{x - \mu}{\sigma} \\ &= \frac{1100 - 1026}{209} \\ &= \frac{74}{209} \\ &= 0.3541 \end{aligned}$$

$$\text{Probability}(Z) = \text{Probability}(0.3541) = 0.6368$$

$$\text{Average Test Taker } \text{Z} = \frac{1026 - 1026}{209} = 0$$

$$\text{Probability}(Z=0) = 0.5$$

Hence compared to average test taker, my score is 0.3541 standard deviation better than average test taker.

In terms of probability my score is $(0.6368 - 0.5) \times 100\%$
 $= 13.68\%$ better than average test taker