BIRLA INSTITUTE OF TECHNOLOGY & SCIENCE -PILANI, K K BIRLA GOA CAMPUS

Second Semester 2024–2025

Course Handout

Date: 07.01.2025

Course No.: PHY F243

Course Title: Mathematical Methods of Physics

Instructor: Chandradew Sharma

Course Description:

This course will cover some of the mathematical techniques that are routinely used to understand most of the topics in undergraduate physics. It is essential that the students practice problems relevant to the topics covered in the class. It is assumed that students are familiar with the concepts covered in mathematics courses and the previous physics courses.

Text Books:

T1. Mathematical Methods for Physicists, Arfken, and Weber, Elsevier

Reference Books:

- R1. Mathematical Physics: A Modern Introduction to Its Foundations by Sadri Hassani
- R2. Methods of Mathematical Physics: Courant and Hilbert
- **R3.** Mathematical Methods in the Physical Sciences. Mary L Boas.

Evaluation Scheme:

| Sr. No. | Evaluation Component | Duration Weightage Date & time (%) | Nature |
|---------|-------------------------------------|-------------------------------------------|----------------|
| 1 | Midsem | (30%) 3/3/25 (Mon, 9:30-11:00 am) | Closed Book |
| 2 | Comprehensive Exam | (40%) 1/5/25 (FN) | Closed Book |
| 3 | 4 Quizzes (best 3 out of 4) | (21%) (29/1/25,28/2/25, 19/3/25, 21/4/25) | Open Book |
| 4 | Presentation | (3%) (23/4/25, 25/4/25 and 28/4/25) | Open Book |
| 5 | Attendance (lecture + tutorial) | (6%) 1-20 0% | |

| | 20-29 30-39 | 1% 3% | |
|--|----------------|----------|--|
| | 40 or more | 6% | |

General Information: References for the specific topics will be announced in class.

Course Plan: (C306, Lecture: M, W, F 12-12:50 pm (5), Tutorial M 8-8:50 am (1))

| No. of | Topics | References |
|-----------|--------------------------------------------------------------------|------------|
| Lectures | | |
| + | | |
| Tutorials | | |
| 1-6 | Vector Space: Vector Spaces, Linearly Independence, | T1 Chap 5 |
| | Orthogonalization, Linear Operators, Eigenvalues, Eigenvectors, | |
| | Linear Transformations, Diagonalization, | |
| 7-13 | Complex Analysis: Argand Plane, Branch Points, Cauchy-Riemann | T1 Chap 11 |
| | Theorem, Integral Theorem, Laurent Expansion, Singularities, | |
| | Residue Theorem, Conformal Mapping, Methods of Steepest | |
| | Descent, etc | |
| 14-19 | Ordinary Differential Equation (ODE): Singular Points, Series | T1 Chap 7 |
| | Solution (Frobenius's method), Linear Independence of Solutions, | & 8 |
| | Sturm-Liouville Theory, Nonlinear differential Equation, IVP, BVP | |
| 20-25 | Special Functions: Bessel Functions, Legendre Functions, | T1 Chap |
| | Spherical Harmonics, Hermite Functions, Laguerre Functions | 11, 12, 13 |
| 26-32 | Integral Transform: Laplace Transform, Fourier Transform | T1 Chap |
| | | 14, 15 |
| 33-42 | Green Functions: Nonhomogenous Equations, Eigenfunction | T1 Chap 8, |
| | Expansion, Integral Equation, IVP, BVP | 9, 16 |
| 43-56 | Partial Differential Equation (PDE): Classification, Separation of | Lecture |
| | Variables, Spectral Methods, Pseudo Spectral Methods, Converting | Notes |
| | PDE into system of coupled ODE, Laplace Equation, Poisson | |
| | Equation, Wave Equation, Heat Equation, IVP, BVP | |
| | | |

Quiz/Assignment Information: Instructions for the quizzes will be announced in class.

Consultation Hours: TBA

Notices: Quanta.

Make-up Policy: Consideration of make-up will be made as and when necessary

Chandradew Sharma **Instructor-in-charge**