Problem 3. Experimental Analysis of Algorithms

Perform an experimental analysis of the three algorithms: *prefix_average1*, *prefix_average2*, and *prefix_average3*. Visualize their running times as a function of input size with a log-log scale chart.

```
1 def prefix_average1(S):
     """Return list such that, for all j, A[j] equals average of S[0], ..., S[j]."""
 2
     n = len(S)
 3
     A = [0] * n
                                       # create new list of n zeros
 4
 5
     for j in range(n):
        total = 0
                                       # begin computing S[0] + ... + S[j]
 6
7
        for i in range(j + 1):
          total += S[i]
 8
 9
        A[j] = total / (j+1)
                                       # record the average
10
      return A
   def prefix_average2(S):
1
     """ Return list such that, for all j, A[j] equals average of S[0], ..., S[j]."""
2
3
     n = len(S)
     A = [0] * n
                                         # create new list of n zeros
4
     for j in range(n):
5
       A[j] = sum(S[0:j+1]) / (j+1) # record the average
6
7
     return A
1
   def prefix_average3(S):
     """ Return list such that, for all j, A[j] equals average of S[0], ..., S[j]."""
2
3
     n = len(S)
     A = [0] * n
                                     # create new list of n zeros
4
                                     # compute prefix sum as S[0] + S[1] + ...
5
     total = 0
6
     for j in range(n):
7
       total += S[i]
                                    # update prefix sum to include S[j]
       A[j] = total / (j+1)
8
                                    # compute average based on current sum
9
     return A
```