

# Assignment 1

Monorina Mukhopadhyay, ID 260364335

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- Problem 2.

a The left side of the equation is:  $(X \implies Y) \vee (X \implies Z)$

$$\begin{aligned} &\equiv (\neg X \vee Y) \vee (\neg X \vee Z) && \text{Condition Identity} \\ &\equiv (\neg X \vee Y \vee \neg X) \vee (\neg X \vee Y \vee Z) && \text{Associative Property} \\ &\equiv (\neg X \vee Y) \vee (\neg X \vee Y \vee Z) && \text{Idempotent Identity} \\ &\equiv (\neg X \neg X \vee Y \vee Y) \vee (Z) && \text{Associative Identity} \\ &\equiv (\neg X \vee Y) \vee (Z) && \text{Idempotent Identity} \\ &\equiv \neg X \vee (Y \vee Z) && \text{Associative Identity} \\ &\equiv X \implies (Y \vee Z) && \text{Conditional Identity} \end{aligned}$$

b Starting from the left side again:  $(P \iff Q) \equiv (P \implies Q) \wedge (Q \implies P)$

$$\begin{aligned} &\equiv (P \implies Q) \wedge (\neg Q \vee P) && \text{Biconditional Identity} \\ &\equiv (P \implies Q) \wedge (\neg Q \vee P) && \text{Conditional Identity} \\ &\equiv (P \implies Q) \wedge (\neg(\neg P) \vee \neg Q) && \text{Commutative and Double Negative Properties} \\ &\equiv (P \implies Q) \wedge (\neg P \implies \neg Q) && \text{Conditional Identity} \end{aligned}$$

c Blah