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CSC4202-5: DESIGN AND ANALYSIS OF ALGORITHMS

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## **Original Scenario: Landslide Risk Reduction in a Hilly Terrain**

### **Geographical Setting**

The scenario is set in a region characterized by steep slopes, hilly terrain, and unstable geological formations, making it prone to landslides. The region is home to several communities, with infrastructure such as roads, homes, and agricultural lands scattered throughout the area.

### **Type of Disaster**

The region faces the constant threat of landslides, which can be triggered by heavy rainfall, seismic activity, or human activities such as deforestation and construction. Landslides in this area can result in the sudden movement of rock, soil, and debris down slopes, causing extensive damage to infrastructure, homes, and natural habitats.

### **Damage Impact**

Landslides have the potential to cause significant damage, including the loss of life, displacement of communities, and disruption of transportation networks. They can also lead to the destruction of homes, agricultural lands, and natural ecosystems, further exacerbating the impact on local communities and the environment.

### **Importance of Automated Algorithm Design (AAD)**

AAD plays a crucial role in landslide risk reduction by optimizing landslide monitoring, early warning systems, land use planning and emergency response measures. It also plays a key role in the automated identification of evacuation routes in the event of a landslide. AAD can analyze geological data, rainfall patterns, terrain mapping, and land use changes to identify areas at risk and develop effective strategies for landslide mitigation, preparedness and evacuation.

### **Goal**

The goal of the scenario is to develop a comprehensive landslide risk reduction plan that minimizes the occurrence and impact of landslides, protects vulnerable populations, and ensures the sustainable development of the region. The plan should aim to enhance the resilience of the region to landslides and promote safe and sustainable development practices in hilly terrains. One of the important components of the landslide risk reduction plan is the

identification of the least risky evacuation paths for landslide victims, ensuring their safety during the emergency situations.

### **Expected Output**

The expected output of the scenario includes a path that identifies the least risky evacuation route, which is a critical component of the landslide risk reduction plans. The plan should be designed to efficiently determine optimal evacuation routes, enhancing the region's resilience to landslides and promote safe evacuation practices.

### **Explain why finding an optimal solution for this scenario is important.**

Finding the best way to reduce the risk of landslides in hilly areas is really important because for several reasons:

1. Save lives

Landslides can be very dangerous, especially in areas with dense populations and highways. Finding the best solution is crucial for predicting where landslides might occur and keeping everyone safe. Preventive measures such as early warning systems, slope stabilization, and land use planning can significantly reduce the risks associated with landslides. An optimal plan minimizes these risks by identifying vulnerable areas, implementing early warning systems, and ensuring communities are prepared to evacuate.

2. Minimizing Damage and Economic Loss

Landslides can destroy infrastructure, homes, and agricultural land, causing significant economic hardship. An optimal plan prioritizes cost-effective mitigation strategies like slope stabilization and land-use regulations, reducing the potential for damage during landslides.

3. Ensuring Sustainable Development

By finding the optimal solution, sustainable development practices can be promoted in hilly terrains. This includes identifying safe areas for construction, implementing land use regulations, and ensuring that infrastructure is resilient to landslides, and leading to sustainable development in the region.

#### 4. Enhancing Resilience

Developing an optimal solution enhances the region's resilience to landslides. This includes identifying and implementing measures to mitigate landslide risks, such as slope stabilization, early warning systems and effective evacuation routes, which can help communities recover quickly from landslides and reduce the impact of future events.

**Review the suitability of sorting, DAC, DP, greedy and graph algorithms as a solution paradigm for the chosen problem by stating their strengths and weaknesses.**

##### 1. Sorting Algorithm

Sorting algorithms excel at organizing and retrieving data, making them crucial for pre-processing landslide data like slope angles, soil types, and historical occurrences. This allows for faster analysis and prioritizes areas for mitigation based on risk levels. However, sorting has limitations. It doesn't consider the spatial relationships and dynamic factors that influence landslides. While valuable for initial data organization, sorting needs to be combined with other algorithms for a comprehensive solution. In essence, sorting lays the groundwork, but more sophisticated methods are needed to address the full complexity of landslide risk reduction.

##### 2. Divide and Conquer (DAC) Algorithm

DAC excels at breaking down complex problems into smaller, independent subproblems. This makes it well-suited for dividing landslide risk assessment and mitigation planning into distinct regional analyses. Additionally, DAC's ability to leverage parallel processing allows for efficient concurrent risk assessments across multiple areas. However, a key limitation of DAC is its struggle with interconnected problems. Landslide risks are often interdependent, where actions in one region can affect neighboring areas. DAC might not effectively manage these complex dependencies, particularly those arising from factors like rainfall and vegetation. Therefore, for a comprehensive solution, DAC may need to be integrated with other methods that can better capture the interconnected nature of landslide risks.

##### 3. Dynamic Programming (DP) Algorithm

DP is highly effective for optimizing resource allocation in landslide prevention, taking into account factors like cost-effectiveness and impact. By efficiently handling overlapping subproblems through memoization, DP can identify repeated risk patterns and develop robust mitigation strategies. Nevertheless, DP can be computationally intensive, posing scalability challenges for large regions or complex terrains. DP excels at problems with overlapping subproblems. In landslide risk assessment, finding the least risky path from point A to point B might involve evaluating many smaller subpaths along the way. DP cleverly stores solutions to these subproblems, avoiding redundant calculations. This "remembering" aspect makes it a powerful tool for efficiently finding the single least risky path through the landslide terrain.

#### 4. Greedy Algorithm

Greedy algorithms offer a quick and straightforward approach to landslide mitigation. They excel at identifying high-risk areas rapidly, allowing for swift responses in emergency situations. This prioritization is crucial for taking immediate action in the face of potential landslides. However, there's a trade-off. Greedy algorithms prioritize local optima, meaning they choose the seemingly best option at each step without considering the overall picture. While this approach provides fast solutions, it might not lead to the absolute best outcome for long-term landslide risk reduction. In essence, greedy algorithms are valuable for quick identification of high-risk areas but may not be suitable for finding the globally optimal, least risky path across a broader region.

#### 5. Graph Algorithm

Graph algorithms play a crucial role in landslide emergency response by facilitating the modeling of transportation networks and evacuation routes. This allows for efficient planning and coordination with emergency services to ensure safe and swift evacuations during landslides. However, graph algorithms have limitations. Implementing them effectively requires detailed data on the terrain and careful consideration of the network's structure and properties. Additionally, the dynamic and spatially variable nature of landslide risks in certain regions can pose significant challenges. While graph algorithms excel at visualizing potential paths and analyzing associated risks, they might not be the most efficient way to find the absolute least

risky path directly, especially in complex situations. Their strength lies in providing a clear picture of the network, which is invaluable for emergency planning.

**Design the algorithm to solve the problem and explain the idea of your algorithm paradigm by emphasising which part needs recurrence and the function for the optimization.**

### **Dynamic Programming:**

Dynamic programming (DP) is a powerful technique for solving optimization problems and is well-suited for addressing the scenario of landslide risk reduction in a hilly terrain. Dynamic programming (DP) is a powerful technique for optimizing complex problems by breaking them down into smaller, more manageable subproblems. In the context of landslide risk reduction in hilly terrains, DP can be applied to various components such as monitoring, early warning systems, and evacuation planning. Each of these components represents a subproblem that contributes to the overall goal of minimizing landslide risks.

One key advantage of DP is its efficient use of resources. By storing intermediate results, DP avoids redundant calculations, making it a cost-effective approach for risk assessment and mitigation planning. This is particularly important in landslide risk reduction, where accurate and timely decision-making is critical.

Additionally, DP can handle multiple variables inherent in landslide risk reduction, such as geological data, rainfall patterns, and land use changes. It can analyze these variables to provide comprehensive solutions, such as determining the best allocation of land resources to minimize landslide risks.

Furthermore, DP is scalable and adaptable to different terrains and environmental conditions. It can be applied to various scales of risk reduction efforts, from small-scale localized plans to large-scale regional strategies. This flexibility makes DP a versatile approach for addressing landslide risks in diverse settings.

### **Recurrence Relation and Optimization Function:**

Recurrence Relation: Defines how the solution to a larger problem is built from the solutions to smaller subproblems.

Optimization Function: Ensures that the best (optimal) solution is selected by comparing the outcomes of different choices.

### **Algorithm Design:**

#### **1. Terrain Data Collection**

To effectively address landslide risk reduction, it is crucial to start with comprehensive terrain data collection. This process involves gathering detailed information about the terrain, including elevation, slope, and geological characteristics. Elevation data helps in understanding the height variations across the terrain, while slope data indicates the steepness, which is a critical factor in landslide susceptibility. Geological information provides insights into the soil composition and stability, which are essential for accurate risk assessment. Once collected, this data needs to be preprocessed to create a grid representation of the terrain. In this grid, each cell corresponds to a specific location and contains a value representing the risk level associated with that location. This preprocessing step ensures that the terrain data is structured in a format suitable for further analysis and calculations.

#### **2. Minimum Risk Path Calculation**

With the terrain data represented in a grid, the next step is to calculate the minimum risk path from the top-left corner to the bottom-right corner of the grid. This path represents the safest route across the terrain, minimizing the risk of encountering hazardous conditions. To achieve this, dynamic programming is employed. The approach involves initializing a 2D array (dp array) that will store the minimum risk value at each cell in the grid. Initially, this array is filled with maximum possible values, except for the starting cell (top-left corner), which is set to its own risk value. The dynamic programming algorithm then iterates through the grid. For each cell, it updates the minimum risk value based on the risk values of the neighbouring cells (top and left). Specifically, the risk at each cell is updated to the minimum of its current risk and the sum of its own risk and the minimum risk of the neighbouring cells. This process



continues until all cells are processed, ensuring that the dp array contains the minimum risk values for all paths leading to each cell.

### 3. Output the Minimum Risk Path

After completing the dynamic programming calculation, the final step is to determine and output the minimum risk path value. This value represents the least risky path from the top-left corner to the bottom-right corner of the terrain grid. By accessing the value at the bottom-right cell of the dp array, we obtain the minimum risk required to traverse the entire terrain. This information is crucial for decision-making and planning, as it provides a quantifiable measure of the safest route through the terrain. The output can be used to inform various applications, such as designing infrastructure, planning evacuation routes, and implementing risk mitigation measures. By providing a clear and concise output of the minimum risk path, stakeholders can make informed decisions to enhance safety and reduce the impact of landslides.

The Algorithm Paradigm:

#### Problem Breakdown:

Dynamic programming (DP) is an algorithmic paradigm that solves complex problems by breaking them down into simpler subproblems and storing the results of these subproblems to avoid redundant calculations.

#### Recurrence Relation:

In dynamic programming, a recurrence relation defines how the solution to a problem can be constructed from solutions to smaller subproblems. For this problem, the recurrence relation is based on the minimum risk path to reach each cell in the grid.

The recurrence relation for the minimum risk at cell (i, j) can be expressed as:

$$dp[i][j] = terrain[i][j] + \min(dp[i-1][j], dp[i][j-1])$$

This means that the minimum risk to reach cell (i, j) is the risk of the current cell  $terrain[i][j]$  plus the minimum of the risks from the top cell (i-1, j) and the left cell (i, j-1).

### **Function for Optimization:**

The optimization function in the context of solving the minimum risk path problem minimizes the risk by considering the minimum risk from the possible previous cells. This function ensures that each cell in the dp array contains the minimum risk required to reach that cell from the start. In the context of the algorithm for finding the minimum risk path, the optimization function is the minimum risk path itself. This path is the one that minimizes the risk of landslides when traversing from the start to a given cell. By calculating this path using dynamic programming, each cell in the grid is ensured to be part of the path that offers the lowest risk of encountering hazardous conditions.

Pseudocode:

1. Start
2. Initialize rows and cols from terrain dimensions
3. Create a 2D array dp for dynamic programming
4. Initialize dp with maximum values
5. Set dp[0][0] as the starting point of the terrain grid
6. Iterate through each cell of the terrain grid
  - Update dp[i][j] with the minimum risk to reach the current cell
7. Return dp[rows-1][cols-1] as the minimum risk path
8. End

### **PSEUDOCODE :**

Algorithm MinimizeLandslideRisk

Input: 2D array terrain representing the terrain grid with risk levels

Output: Minimum risk to reach the bottom-right corner

1. Define the Terrain Grid:

Let terrain be a 2D array of size rows x cols

2. Initialise the DP Table:

Create a 2D array dp of the same size as terrain

For i from 0 to rows-1

For j from 0 to cols-1

dp[i][j] = Infinity // Initialize all cells with a large value

3. Base Case:

dp[0][0] = terrain[0][0]

4. Recurrence Relation:

For i from 0 to rows-1

For j from 0 to cols-1

If i > 0

dp[i][j] = min(dp[i][j], dp[i-1][j] + terrain[i][j])

If j > 0

dp[i][j] = min(dp[i][j], dp[i][j-1] + terrain[i][j])

5. Boundary Conditions:

For i = 0 and j = 0

Continue // Already handled in base case

6. Final Solution:

Return dp[rows-1][cols-1]

End Algorithm

**Define the algorithm specification.**

The dynamic programming algorithm specification involves several key components that ensure efficient and optimal problem-solving. The first step is to break down a complex problem into smaller, manageable subproblems. This decomposition is

crucial because it allows the algorithm to focus on solving each subproblem independently, which is essential for efficient computation.

**Problem Statement:**

Given a hilly terrain characterized by steep slopes and unstable geological formations, develop an algorithm to find the least risky evacuation path for landslide victims. The goal is to minimize the risk of casualties and damage to infrastructure during a landslide event.

**Input:**

- A 2D array `terrain` representing the terrain, where `terrain[i][j]` represents the risk value at cell  $(i, j)$  of the terrain.
- The terrain is a grid of size  $n \times m$ , where  $n$  is the number of rows and  $m$  is the number of columns.
- The risk value at each cell represents the likelihood of a landslide occurring at that location, with higher values indicating higher risk.

**Output:**

- The minimum risk path from the top-left corner of the terrain to the bottom-right corner, representing the least risky evacuation path for landslide victims.
- The total risk value along the minimum risk path.

**Constraints:**

- The terrain grid is non-empty, with  $n > 0$  and  $m > 0$ .
- Each cell in the terrain grid contains a non-negative integer representing the risk value, i.e.,  $0 \leq \text{terrain}[i][j] \leq 100$ .

**Dynamic Programming Approach:**

- **Initialization:** Create a 2D array `dp` of size  $n \times m$  to store the minimum risk at each cell. Initialize all values in `dp` to `Integer.MAX_VALUE` except for `dp[0][0]`, which is initialized to `terrain[0][0]`.

- **Recurrence Relation:** For each cell  $(i, j)$  in the terrain grid, update  $dp[i][j]$  with the minimum risk value to reach that cell from the top-left corner. The minimum risk value to reach cell  $(i, j)$  is the minimum of the risks from the cell above  $(i-1, j)$  and the cell to the left  $(i, j-1)$ , plus the risk value at cell  $(i, j)$ . This can be expressed as:  $dp[i][j] = \min(dp[i-1][j], dp[i][j-1]) + \text{terrain}[i][j]$
- **Optimal Substructure:** The minimum risk path to reach cell  $(i, j)$  depends on the minimum risk paths to reach the cells  $(i-1, j)$  and  $(i, j-1)$ .
- **Final Result:** The minimum risk path to reach the bottom-right corner  $(n-1, m-1)$  is stored in  $dp[n-1][m-1]$ . Return this value as the total risk along the minimum risk path.

**Time Complexity:** The time complexity of the dynamic programming approach is  $O(nm)$ , where  $n$  is the number of rows and  $m$  is the number of columns in the terrain grid. This is because we iterate through each cell of the terrain grid once to calculate the minimum risk path.

Develop a program Java language.

```
1 package algo;
2 import java.util.Arrays;
3
4 public class LandslideRiskReduction {
5
6     // Function to find the minimum risk path
7     public static int findMinRisk(int[][] terrain) {
8         int rows = terrain.length;
9         int cols = terrain[0].length;
10
11         // Create a dp array to store the minimum risk at each cell
12         int[][] dp = new int[rows][cols];
13
14         // Initialize the dp array with maximum possible values
15         for (int[] row : dp) {
16             Arrays.fill(row, Integer.MAX_VALUE);
17         }
18
19         // Start from the top-left corner
20         dp[0][0] = terrain[0][0];
21
22         // Fill the dp array with the minimum risk values
23         for (int i = 0; i < rows; i++) {
24             for (int j = 0; j < cols; j++) {
25                 if (i > 0) {
26                     dp[i][j] = Math.min(dp[i][j], dp[i-1][j] + terrain[i][j]);
27                 }
28                 if (j > 0) {
29                     dp[i][j] = Math.min(dp[i][j], dp[i][j-1] + terrain[i][j]);
30                 }
31             }
32         }
33
34         // Return the minimum risk to reach the bottom-right corner
35         return dp[rows-1][cols-1];
36     }
37
38     public static void main(String[] args) {
39         // Example terrain grid
40         int[][] terrain = {
41             {1, 3, 1},
42             {1, 5, 1},
43             {4, 2, 1}
44         };
45
46         // Find and print the minimum risk
47         int minRisk = findMinRisk(terrain);
48         System.out.println("The minimum risk path has a risk of: " + minRisk);
49     }
50 }
51
```

package algo;

import java.util.Arrays;

public class LandslideRiskReduction {

// Function to find the minimum risk path

public static int findMinRisk(int[][] terrain) {

## 1. Class and Method Declaration

- **Package Declaration:** package algo; specifies that this class belongs to the algo package.

- **Import Statement:** `import java.util.Arrays;` is used to import the Arrays class, which provides utility methods for array operations.
- **Class Declaration:** `public class LandslideRiskReduction` declares the class.
- **Method Declaration:** `public static int findMinRisk(int[][] terrain)` is a static method that takes a 2D array terrain representing the risk values of the terrain grid and returns an integer representing the minimum risk path.

```
int rows = terrain.length;
int cols = terrain[0].length;
```

## 2. Initialization

- **Rows and Columns:** rows and cols store the number of rows and columns in the terrain grid.

```
int[][] dp = new int[rows][cols];
```

```
// Initialize the dp array with maximum possible values
for (int[] row : dp) {
    Arrays.fill(row, Integer.MAX_VALUE);
}
```

```
// Start from the top-left corner
dp[0][0] = terrain[0][0];
```

## 3. Create and Initialize DP Array

- **DP Array:** `int[][] dp = new int[rows][cols];` creates a 2D array dp to store the minimum risk at each cell.
- **Initialization:** The for loop initializes all cells in dp with `Integer.MAX_VALUE` to represent an initially infinite risk.
- **Starting Point:** `dp[0][0] = terrain[0][0];` initializes the top-left cell with the risk value from the terrain grid.

```
for (int i = 0; i < rows; i++) {
    for (int j = 0; j < cols; j++) {
        if (i == 0 && j == 0) continue; // Skip the start cell
```

```
        // Check from top cell
        if (i > 0) {
            dp[i][j] = Math.min(dp[i][j], dp[i-1][j] + terrain[i][j]);
        }
    }
}
```

```

        // Check from left cell
        if (j > 0) {
            dp[i][j] = Math.min(dp[i][j], dp[i][j-1] + terrain[i][j]);
        }
    }
}

```

#### 4. Fill DP Array

- **Nested Loop:** Two nested loops iterate through each cell in the terrain grid.
- **Skip Start Cell:** if (i == 0 && j == 0) continue; skips the top-left cell as it is already initialized.
- **From Top Cell:** if (i > 0) checks if the current cell is not in the first row, and updates the minimum risk from the cell directly above it.
- **From Left Cell:** if (j > 0) checks if the current cell is not in the first column, and updates the minimum risk from the cell directly to the left.

```

// Return the minimum risk to reach the bottom-right corner
return dp[rows-1][cols-1];
}

```

#### 5. Return Result

```

public static void main(String[] args) {
    // Example terrain grid
    int[][] terrain = {
        {1, 3, 1},
        {1, 5, 1},
        {4, 2, 1}
    };

    // Find and print the minimum risk
    int minRisk = findMinRisk(terrain);
    System.out.println("The minimum risk path has a risk of: " + minRisk);
}

```

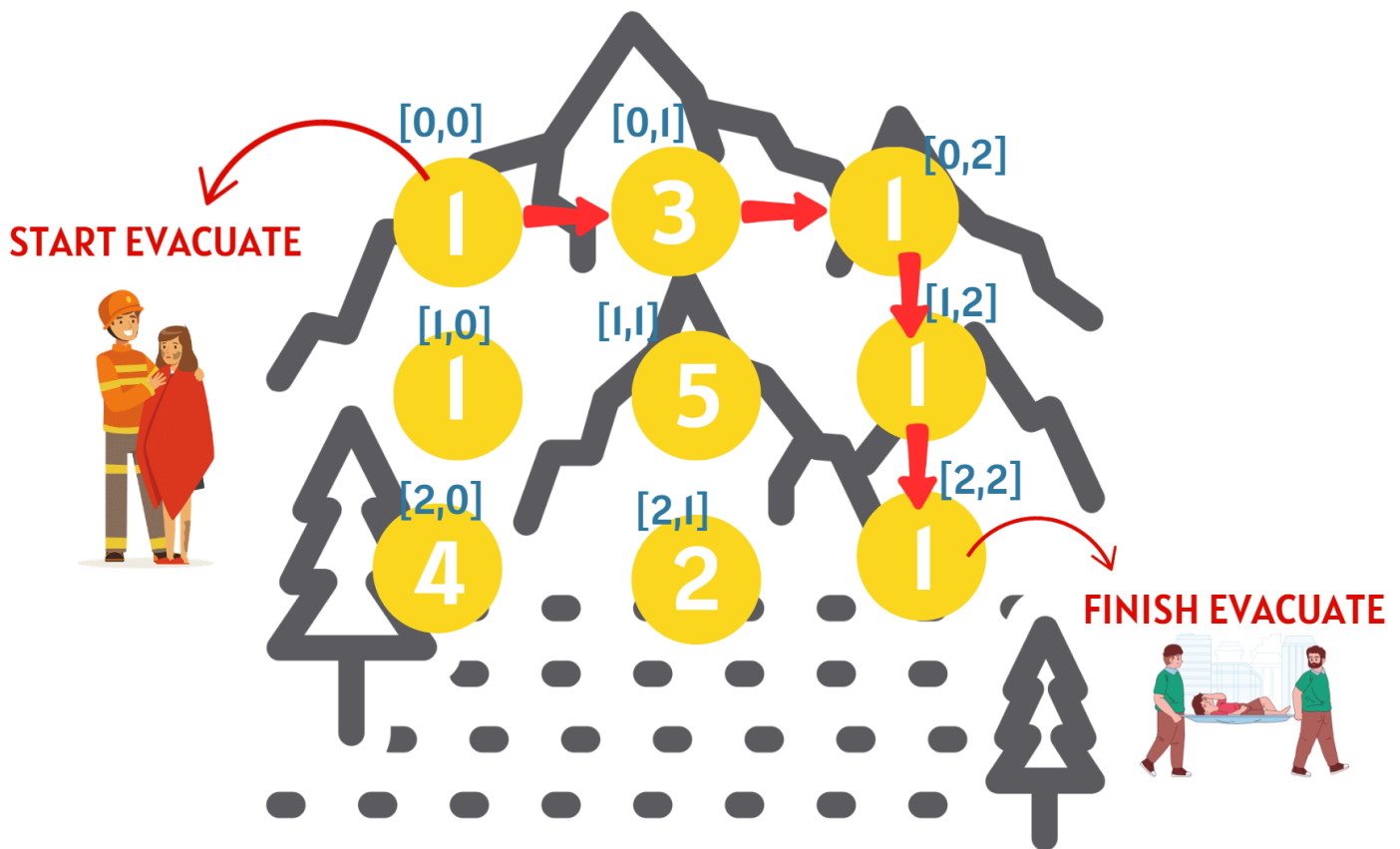
- **Main Method:** public static void main(String[] args) is the entry point of the program.
- **Example Grid:** int[][] terrain = {...}; defines an example terrain grid.
- **Find Minimum Risk:** int minRisk = findMinRisk(terrain); calls the findMinRisk method with the example grid.



- **Print Result:** `System.out.println("The minimum risk path has a risk of: " + minRisk);` prints the minimum risk path.

### The Output :

```
Console ×
<terminated> LandslideRiskReduction [Java Application] C:\Users\moonnn\p2\pool\plugins\org.eclipse.justj.openjdk.hotspot.jre.full.win32.x86_64
The minimum risk path has a risk of: 7
```



Based on the illustration above, the least risky path = 7 is represented in grid format. We can calculate the total number of paths from the top-left corner (0,0) to the bottom-right corner (2,2) in a 3x3 grid where movement is only allowed to the right or down, we can use a combinatorial approach. In addition to the paths shown above, there are several other ways to evacuate victims. The total number of paths is given by the binomial coefficient:

$$\binom{4}{2} = \frac{4!}{2!2!} = 6$$

Here is the detailed calculation:

$$\frac{4!}{2!2!} = \frac{4 \times 3 \times 2 \times 1}{(2 \times 1) \times (2 \times 1)} = \frac{24}{4} = 6$$

Below are the paths represented in a grid format to visualize how they traverse the grid, making it easier to understand. This format is similar to the diagram shown above.

1. 1 -> 3 -> 1

```

      |
1    5 -> 1
      |
4    2 -> 1

```

2. 1 -> 3 1

```

      |  |
1 -> 5 -> 1
      |
4    2 -> 1

```

3. 1 -> 3 1

```

      |  |
1 -> 5  1
      |  |
4 -> 2 -> 1

```

4. 1 3 -> 1

```

      |  |

```

1 -> 5 -> 1

|

4 2 -> 1

5. 1 3 1

| |

1 -> 5 1

| |

4 -> 2 -> 1

6. 1 3 1

| |

1 5 1

| |

4 -> 2 -> 1

Each path corresponds to a unique combination of right and down moves from the start to the destination:

1. (0,0) -> (0,1) -> (0,2) -> (1,2) -> (2,2)

2. (0,0) -> (0,1) -> (1,1) -> (1,2) -> (2,2)

3. (0,0) -> (0,1) -> (1,1) -> (2,1) -> (2,2)

4. (0,0) -> (1,0) -> (1,1) -> (1,2) -> (2,2)

5. (0,0) -> (1,0) -> (1,1) -> (2,1) -> (2,2)

6. (0,0) -> (1,0) -> (2,0) -> (2,1) -> (2,2)

Therefore, with the 3x3 grid, there are 6 paths the emergency response team can evacuate landslide victims and the least risky path is the path (1) with risk value 7.

**Provide an analysis of the algorithm's correctness as well as time complexity (best, average and worst time) by using asymptotic notation.**

### Algorithm's Correctness Analysis

The algorithm implements a dynamic programming approach to find the minimum risk path in a 2D grid.

1. Initialization

The `dp` array is initialized to store the minimum risk at each cell. The initial cell `dp[0][0]` is set to the risk value of the starting cell `terrain[0][0]`, ensuring the starting point is correctly represented.

2. Filling the DP Array

The algorithm iterates over each cell in the grid and updates the `dp` array with the minimum risk value by considering the minimum risk from the top cell (`i-1, j`) and the left cell (`i, j-1`). This ensures that each cell in the `dp` array holds the minimum risk required to reach that cell.

3. Final Value

The value in `dp[rows-1][cols-1]` represents the minimum risk to reach the bottom-right corner of the grid from the top-left corner, which is the desired output.

The algorithm correctly computes the minimum risk path by ensuring that at each step, the minimum cumulative risk is propagated through the grid. The correctness is maintained by the principle of dynamic programming, where the optimal solution to the problem is built from the optimal solutions to its subproblems. The algorithm ensures that the minimum risk path is found, which is crucial for safe evacuation during a landslide. This directly aligns with the goal of minimizing the impact of landslides by finding the safest routes for evacuation. By calculating the cumulative risk at each cell, the algorithm effectively maps out the risk landscape, helping to identify the safest paths in a landslide-prone area.

### Time Complexity Analysis

The time complexity of the algorithm can be analyzed as follows:

1. Initialization

Initializing the `dp` array takes  $O(\text{rows} * \text{cols})$  time since we need to fill the entire array with `Integer.MAX_VALUE`.

## 2. Filling the DP Array

The nested loops iterate over each cell in the grid. Each cell is visited once, and updating the `dp` array takes constant time  $O(1)$  per cell. Therefore, the time complexity for filling the `dp` array is  $O(\text{rows} * \text{cols})$ .

Since both the initialization and the main computation steps have the same time complexity, the overall time complexity of the algorithm is  **$O(\text{rows} * \text{cols})$** . With a time complexity of  $O(\text{rows} * \text{cols})$ , the algorithm efficiently handles large terrains, ensuring that evacuation paths can be computed quickly even in real-time scenarios. This is critical in emergency situations where rapid decision-making is necessary.

### Best Case, Average Case, and Worst Case Analysis

As each cell in the grid represents a terrain segment with an associated risk value, for this algorithm, the time complexity remains the same across all cases because the algorithm processes each cell in the grid exactly once regardless of the input values.

#### - Best Case

The best case occurs when the terrain values are such that the minimum risk path is straightforward, either going directly right or down, but the algorithm still needs to compute the risk values for all cells. Time complexity is  **$O(\text{rows} * \text{cols})$** . Example terrain grid:

```
int[ ][ ] terrain = {  
    {1, 1, 1},  
    {1, 1, 1},  
    {1, 1, 1}  
};
```

#### - Average Case

For an average terrain configuration, the algorithm processes each cell once. If the terrain grid has varying risk values, neither extremely high nor extremely low, the algorithm needs to explore various paths to find the one with the least cumulative risk by processing each cell exactly once. Time complexity is  **$O(\text{rows} * \text{cols})$** . Example terrain grid:

```
int[ ][ ] terrain = {
    {1, 3, 1},
    {1, 5, 1},
    {4, 2, 1}
};
```

#### - Worst Case

Even in the worst-case scenario, where the risk values are high and require maximum computation, the algorithm still processes each cell once to find the minimum cumulative risk. Time complexity is **O(rows \* cols)**. Example of terrain grid:

```
int[ ][ ] terrain = {
    {5, 8, 9},
    {7, 10, 6},
    {12, 11, 4}
};
```

### Space Complexity Analysis

The space complexity of the algorithm is dominated by the space required for the `dp` array, which is **O(rows \* cols)**. This space is used to store the minimum risk values for each cell in the grid.

The `dp` array is a two-dimensional array that stores the minimum risk values for each cell in the grid. It has dimensions `rows` x `cols`, where `rows` is the number of rows in the grid and `cols` is the number of columns. Each cell in the `dp` array corresponds to a cell in the terrain grid, and it stores the minimum cumulative risk value to reach that cell from the starting point `(0, 0)`. Since the `dp` array stores a value for each cell in the grid, its total size is proportional to the number of cells in the grid, which is `rows` x `cols`.

In the context of finding the evacuation path with the least risk in a terrain grid prone to landslides, the space complexity analysis is crucial for understanding the algorithm's memory requirements. The `dp` array's space complexity directly relates to the grid size and determines the amount of memory needed to store the minimum risk values for each cell. As the algorithm processes each cell in the grid and computes the minimum risk path, the `dp` array's space usage grows with the grid size. This space is essential for the algorithm to store intermediate results and ensure that the optimal evacuation path can be traced back from the destination cell to the starting point.

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- <https://github.com/monot08/CSC4202>