

## Task 1: Construct fixed-length and variable-length records

Imagine that we are working with the Room table from the university database that we used in [Lab 2](#). That table has the following schema:

```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

Consider the following tuple from that table:

```
('0123', 'PHO 206', 199)
```

1. If we use the fixed-length record format discussed in lecture, what would the record look like for this tuple?

## Task 1: Construct fixed-length and variable-length records

Imagine that we are working with the Room table from the university database that we used in [Lab 2](#). That table has the following schema:

```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

Consider the following tuple from that table:

```
('0123', 'PHO 206', 199)
```

1. If we use the fixed-length record format discussed in lecture, what would the record look like for this tuple?

0123	PHO 206#-----	199
------	---------------	-----

## Task 1: Construct fixed-length and variable-length records

Imagine that we are working with the Room table from the university database that we used in [Lab 2](#). That table has the following schema:

```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

Consider the following tuple from that table:

```
('0123', 'PHO 206', 199)
```

1. If we use the fixed-length record format discussed in lecture, what would the record look like for this tuple?

0123	PHO 206#-----	199
------	---------------	-----

**Do we need per-record metadata?**

## Task 1: Construct fixed-length and variable-length records

Imagine that we are working with the Room table from the university database that we used in [Lab 2](#). That table has the following schema:

```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

Consider the following tuple from that table:

```
('0123', 'PHO 206', 199)
```

1. If we use the fixed-length record format discussed in lecture, what would the record look like for this tuple?

0123	PHO 206#-----	199
------	---------------	-----

**Do we need metadata?**

No. Each field has the same length for every record.

# Task 1: Construct fixed-length and variable-length records

Imagine that we are working with the Room table from the university database that we used in [Lab 2](#). That table has the following schema:

```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

Consider the following tuple from that table:

```
('0123', 'PHO 206', 199)
```

2. What is the length in bytes of this record if we assume that:

- characters are one byte each
- integer data values are four bytes each.



Room(id CHAR(4), name VARCHAR(20), capacity INT)

0123	PHO 206#-----	199
------	---------------	-----

2. What is the length in bytes of this record if we assume that:

- characters are one byte each
- integer data values are four bytes each.

Room(id CHAR(4), name VARCHAR(20), capacity INT)

0123	PHO 206#-----	199
------	---------------	-----

2. What is the length in bytes of this record if we assume that:

- characters are one byte each
- integer data values are four bytes each.

$$\begin{array}{ccccccc} \text{len(id)} & + & \text{max\_len(name)} & + & \text{len(capacity)} & & \\ = & 4 & + & 20 & + & 4 & = 28 \end{array}$$

```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

```
('0123', 'PHO 206', 199)
```

3. Now assume that we are using the second type of variable-length record discussed in lecture, in which each record begins with a header of field offsets. What will the record look like for the above tuple? In addition to one-byte characters and four-byte integer *data* values, you should assume that we use **two-byte** integers for integer *metadata* like lengths and offsets.



```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

```
('0123', 'PH0 206', 199)
```

3. Now assume that we are using the second type of variable-length record discussed in lecture, in which each record begins with a header of field offsets. What will the record look like for the above tuple? In addition to one-byte characters and four-byte integer *data* values, you should assume that we use **two-byte** integers for integer *metadata* like lengths and offsets.

--	--	--	--

```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

```
('0123', 'PHO 206', 199)
```

3. Now assume that we are using the second type of variable-length record discussed in lecture, in which each record begins with a header of field offsets. What will the record look like for the above tuple? In addition to one-byte characters and four-byte integer *data* values, you should assume that we use **two-byte** integers for integer *metadata* like lengths and offsets.

--	--	--	--	--	--	--

```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

```
('0123', 'PHO 206', 199)
```

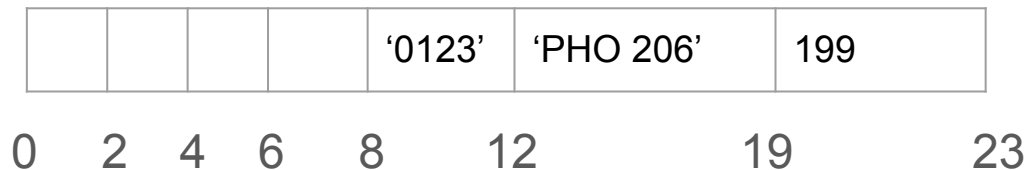
3. Now assume that we are using the second type of variable-length record discussed in lecture, in which each record begins with a header of field offsets. What will the record look like for the above tuple? In addition to one-byte characters and four-byte integer *data* values, you should assume that we use **two-byte** integers for integer *metadata* like lengths and offsets.

				'0123'	'PHO 206'	199
--	--	--	--	--------	-----------	-----

```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

```
('0123', 'PHO 206', 199)
```

3. Now assume that we are using the second type of variable-length record discussed in lecture, in which each record begins with a header of field offsets. What will the record look like for the above tuple? In addition to one-byte characters and four-byte integer *data* values, you should assume that we use **two-byte** integers for integer *metadata* like lengths and offsets.



```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

```
('0123', 'PHO 206', 199)
```

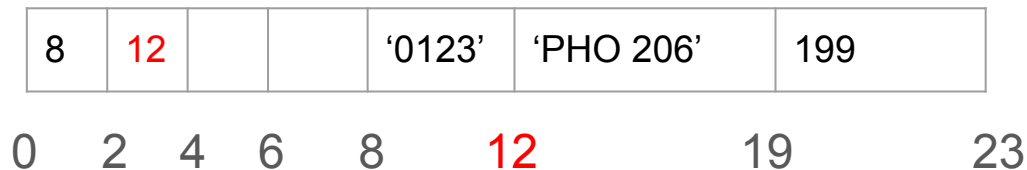
3. Now assume that we are using the second type of variable-length record discussed in lecture, in which each record begins with a header of field offsets. What will the record look like for the above tuple? In addition to one-byte characters and four-byte integer *data* values, you should assume that we use **two-byte** integers for integer *metadata* like lengths and offsets.



```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

```
('0123', 'PHO 206', 199)
```

3. Now assume that we are using the second type of variable-length record discussed in lecture, in which each record begins with a header of field offsets. What will the record look like for the above tuple? In addition to one-byte characters and four-byte integer *data* values, you should assume that we use **two-byte** integers for integer *metadata* like lengths and offsets.



```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

```
('0123', 'PHO 206', 199)
```

3. Now assume that we are using the second type of variable-length record discussed in lecture, in which each record begins with a header of field offsets. What will the record look like for the above tuple? In addition to one-byte characters and four-byte integer *data* values, you should assume that we use **two-byte** integers for integer *metadata* like lengths and offsets.

8	12	19		'0123'	'PHO 206'	199	
0	2	4	6	8	12	19	23

```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

```
('0123', 'PHO 206', 199)
```

3. Now assume that we are using the second type of variable-length record discussed in lecture, in which each record begins with a header of field offsets. What will the record look like for the above tuple? In addition to one-byte characters and four-byte integer *data* values, you should assume that we use **two-byte** integers for integer *metadata* like lengths and offsets.

8	12	19	23	'0123'	'PHO 206'	199
0	2	4	6	8	12	19
						23

Length of bytes? 23



```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

```
('0123', NULL, 199)
```

5. Now imagine that the room didn't have a name and we used a value of NULL to indicate this:

Room(id CHAR(4), name VARCHAR(20), capacity INT)

('0123', NULL, 199)

5. Now imagine that the room didn't have a name and we used a value of NULL to indicate this:

a.

8	-1	12	16	'0123'	199
---	----	----	----	--------	-----

b.

8	12	-1	16	'0123'	199
---	----	----	----	--------	-----

c.

8	-1	12	16	'0123'	NULL	199
---	----	----	----	--------	------	-----

d.

8	12	-1	16	'0123'	NULL	199
---	----	----	----	--------	------	-----

Room(id CHAR(4), name VARCHAR(20), capacity INT)

('0123', NULL, 199)

5. Now imagine that the room didn't have a name and we used a value of NULL to indicate this:

a.

8	-1	12	16	'0123'	199
---	----	----	----	--------	-----

b.

8	12	-1	16	'0123'	199
---	----	----	----	--------	-----

c.

8	-1	12	16	'0123'	NULL	199
---	----	----	----	--------	------	-----

d.

8	12	-1	16	'0123'	NULL	199
---	----	----	----	--------	------	-----

```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

```
('0123', NULL, 199)
```

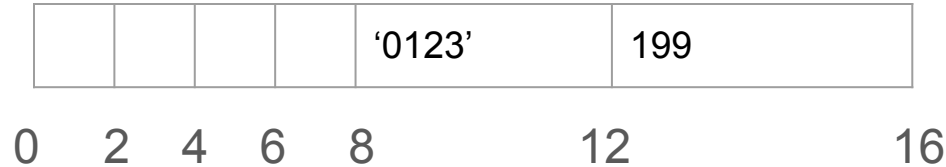
5. Now imagine that the room didn't have a name and we used a value of NULL to indicate this:

				'0123'	199
--	--	--	--	--------	-----

```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

```
('0123', NULL, 199)
```

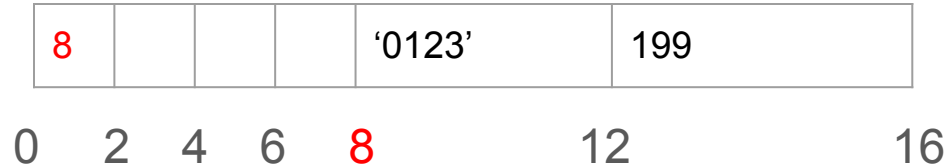
5. Now imagine that the room didn't have a name and we used a value of NULL to indicate this:



```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

```
('0123', NULL, 199)
```

5. Now imagine that the room didn't have a name and we used a value of NULL to indicate this:



```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

```
('0123', NULL, 199)
```

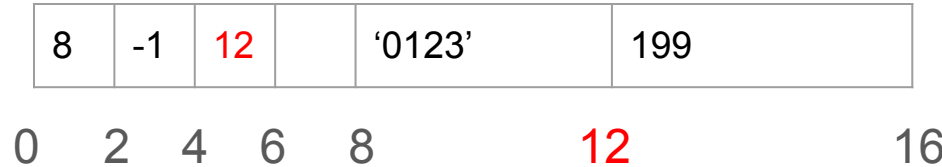
5. Now imagine that the room didn't have a name and we used a value of NULL to indicate this:

8	-1			'0123'	199	
0	2	4	6	8	12	16

```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

```
('0123', NULL, 199)
```

5. Now imagine that the room didn't have a name and we used a value of NULL to indicate this:



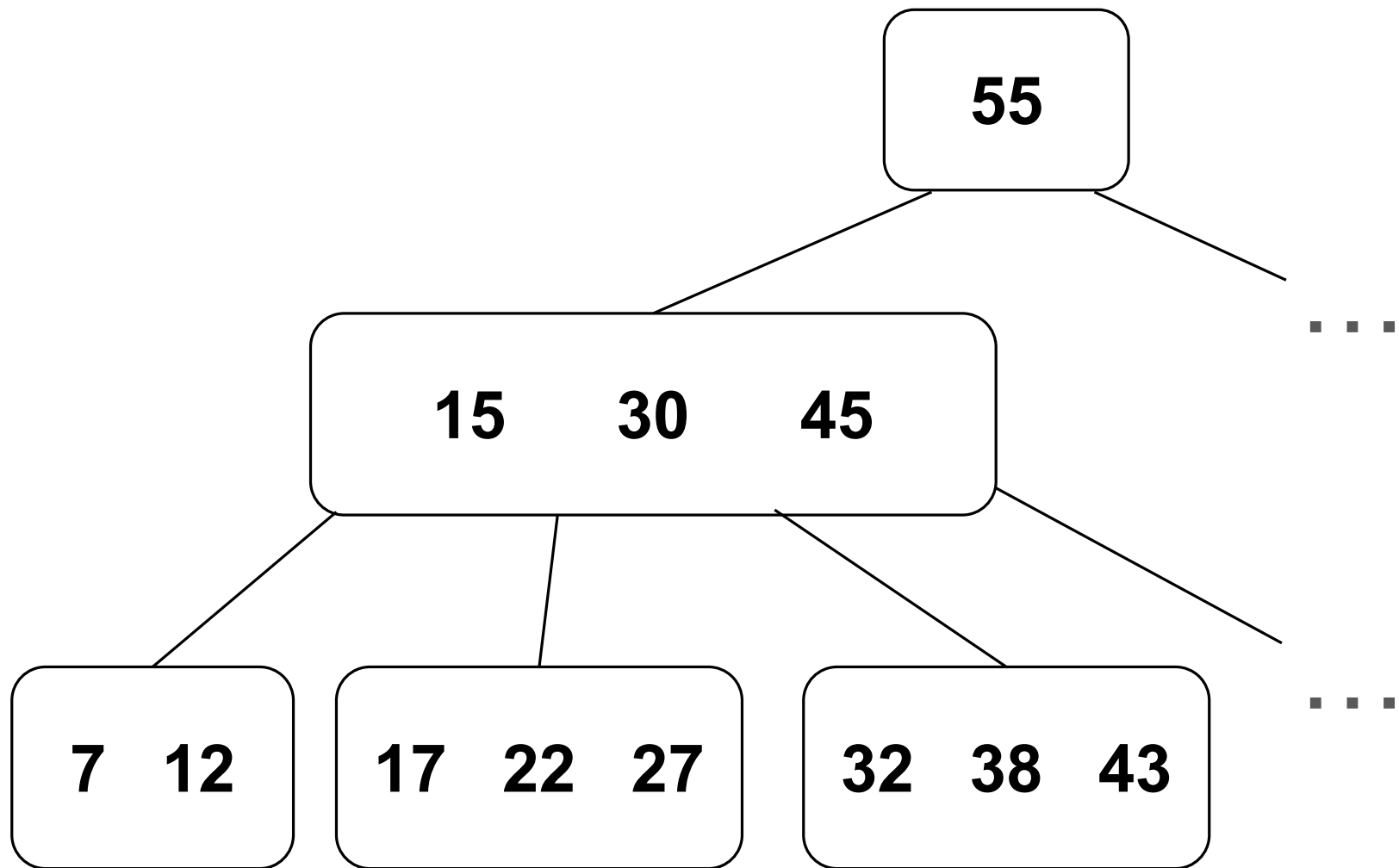


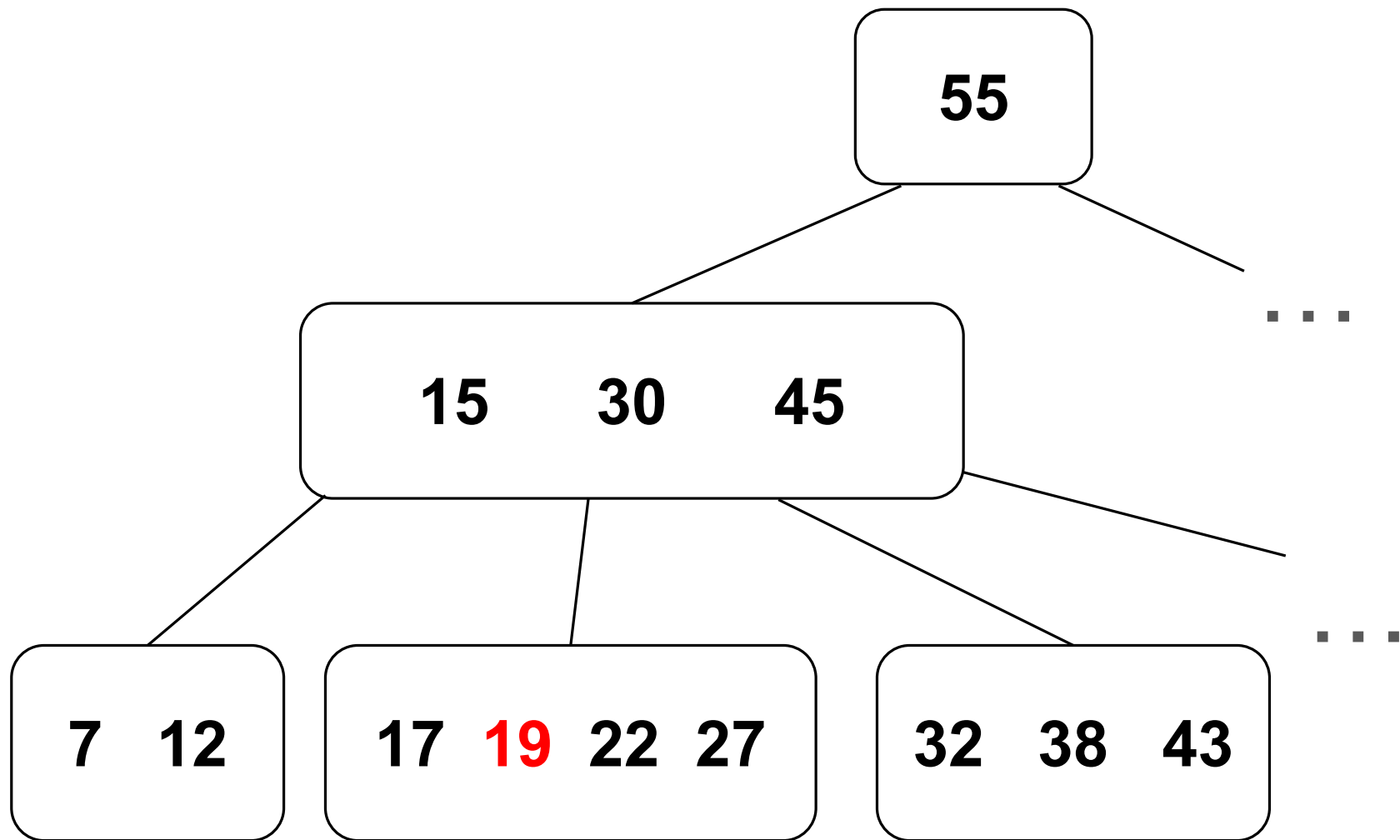
```
Room(id CHAR(4), name VARCHAR(20), capacity INT)
```

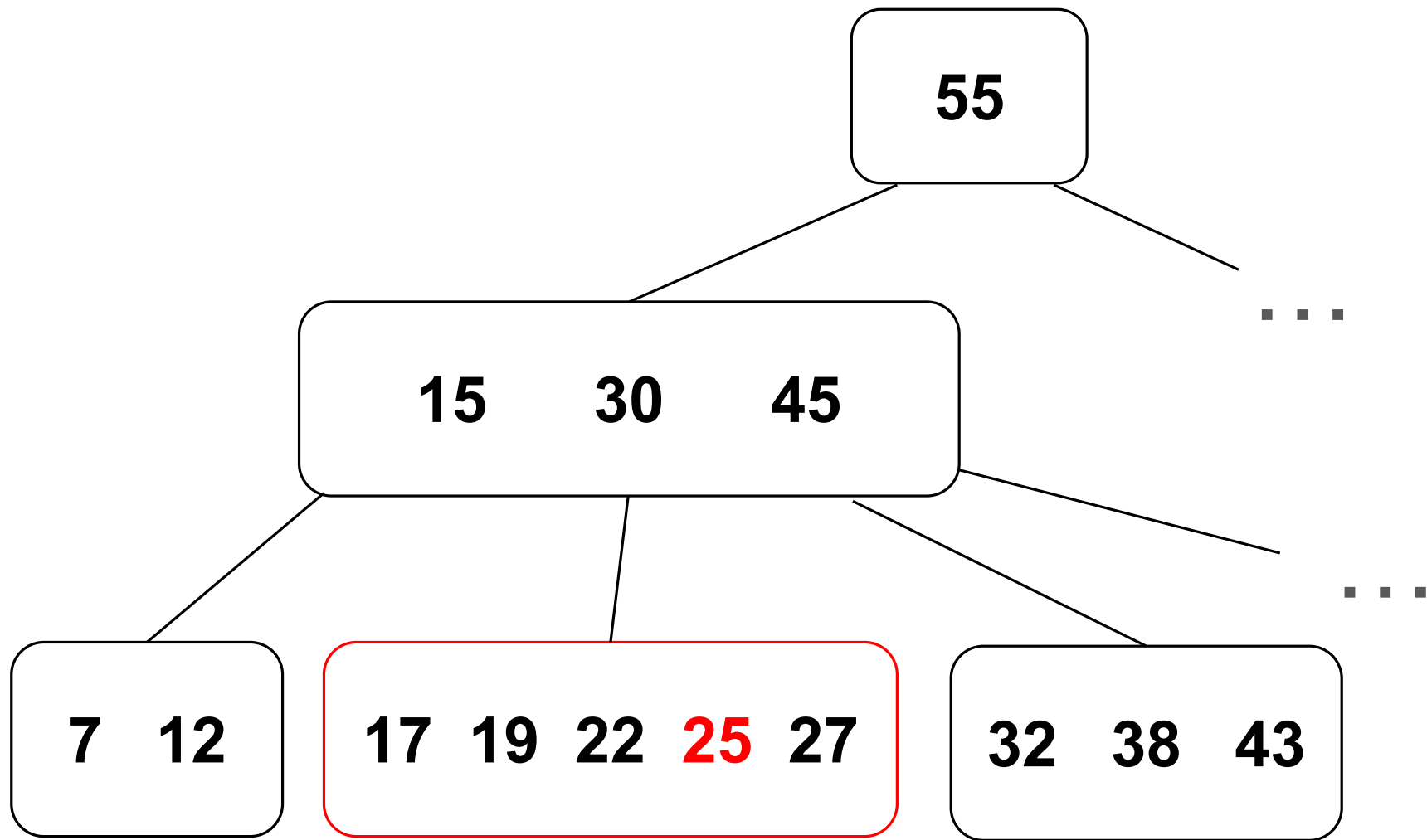
```
('0123', NULL, 199)
```

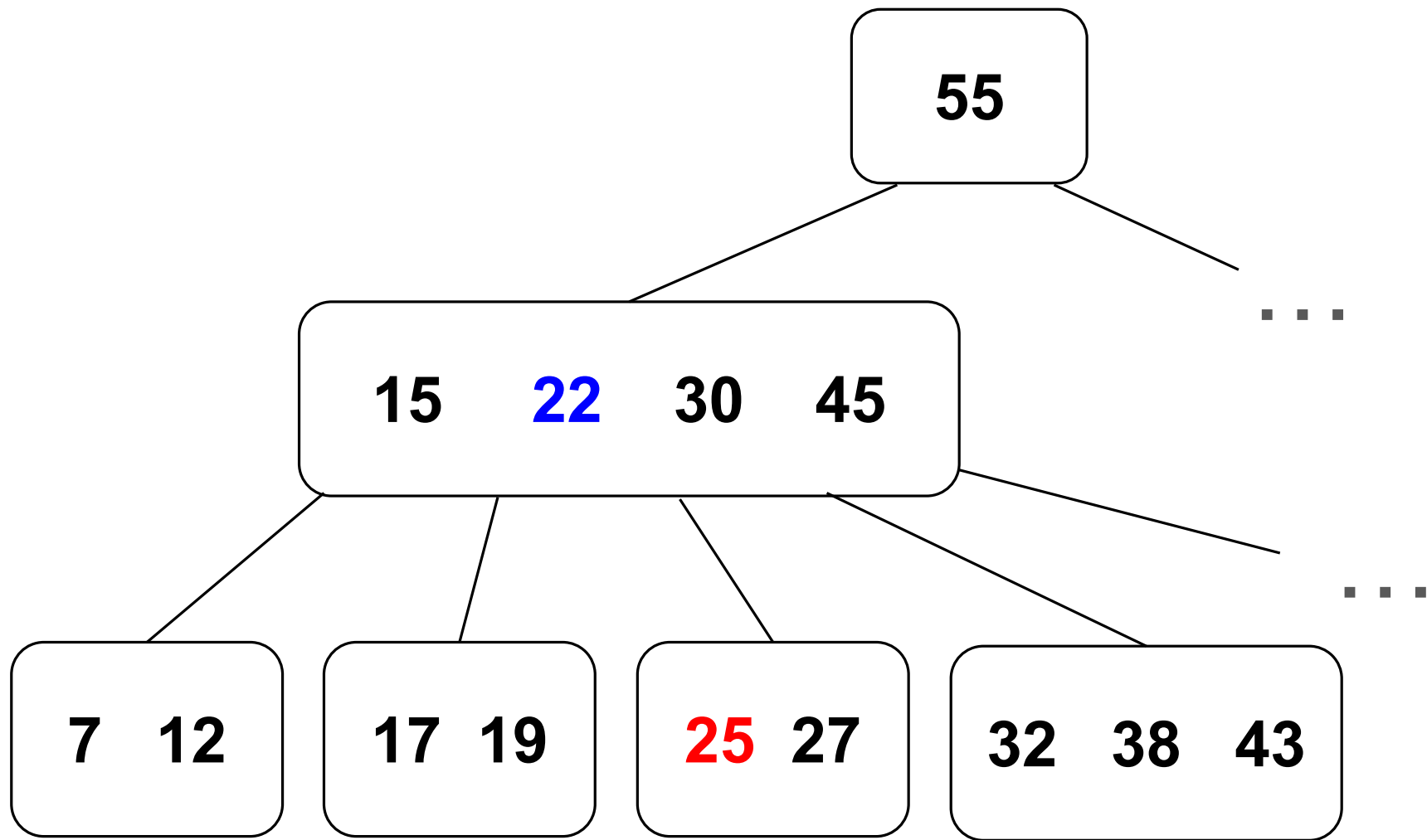
5. Now imagine that the room didn't have a name and we used a value of NULL to indicate this:

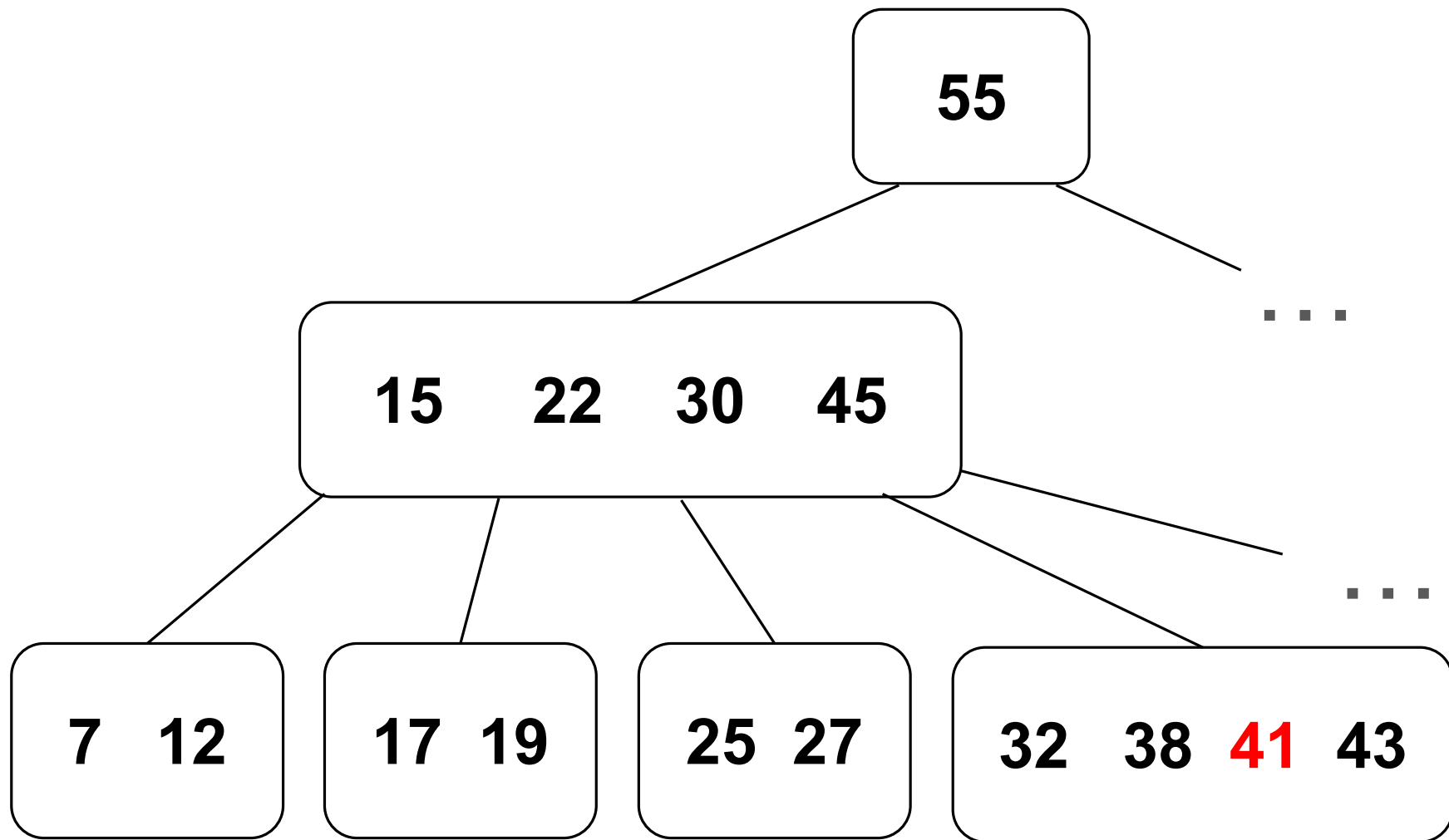
8	-1	12	16	'0123'	199	
0	2	4	6	8	12	16

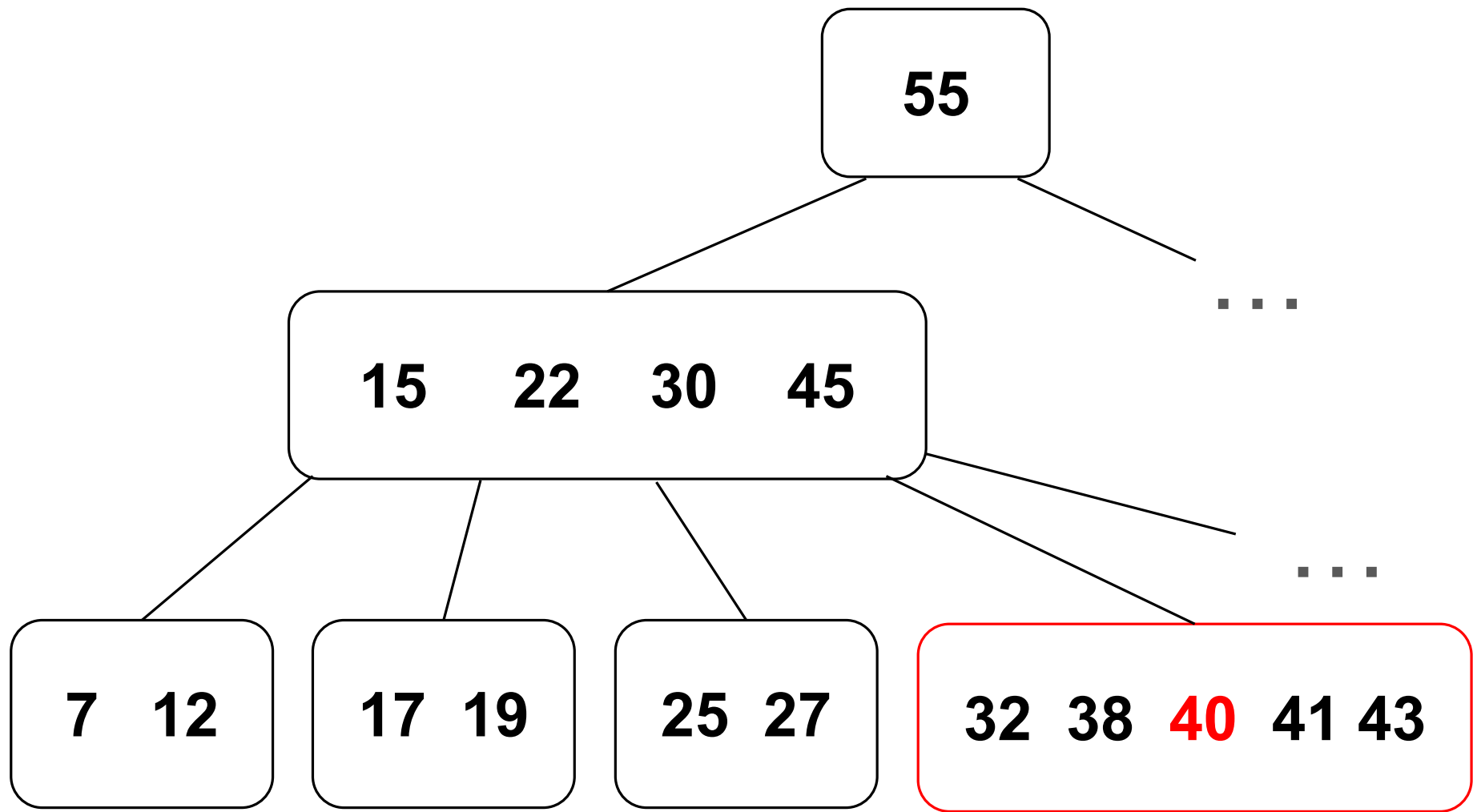


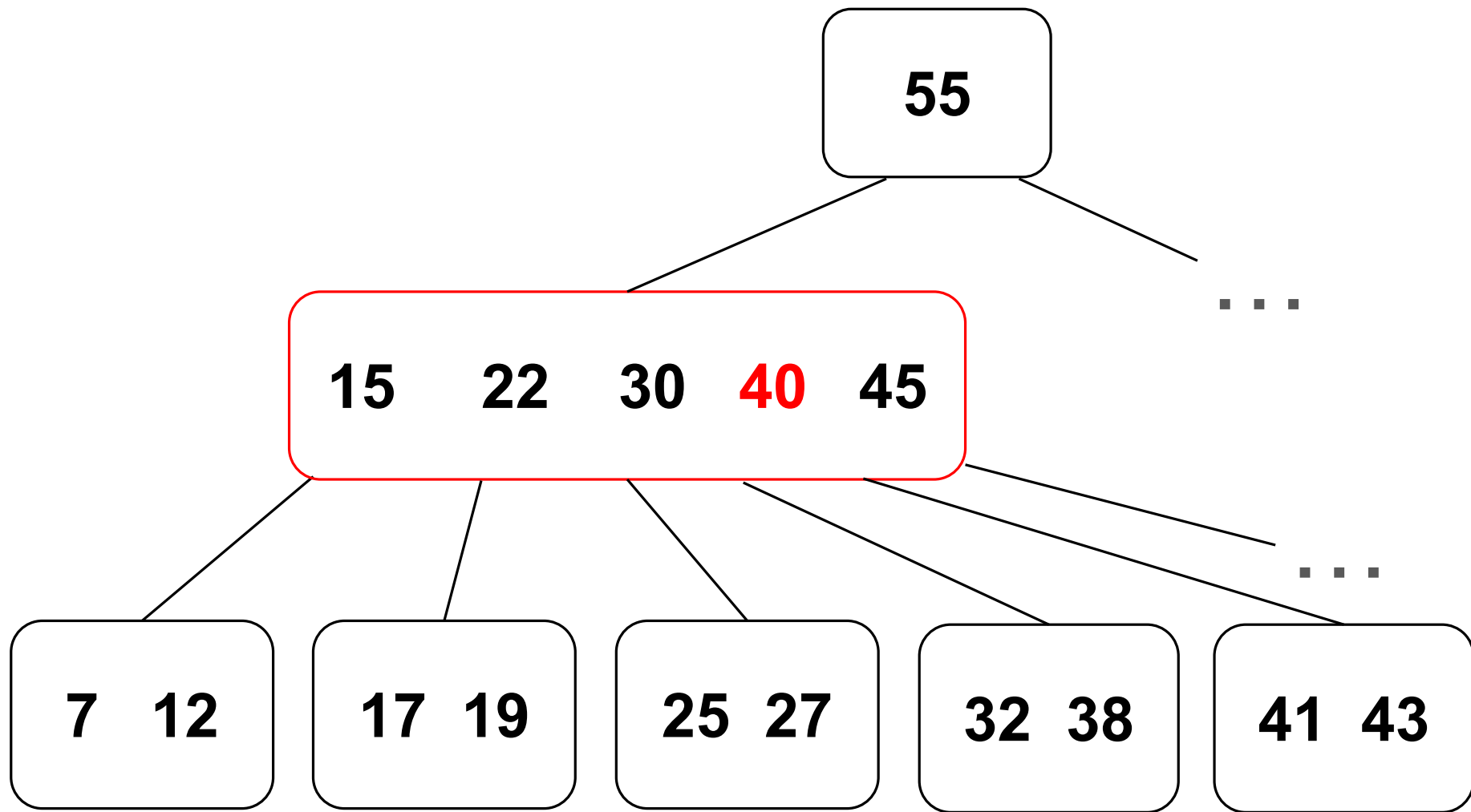




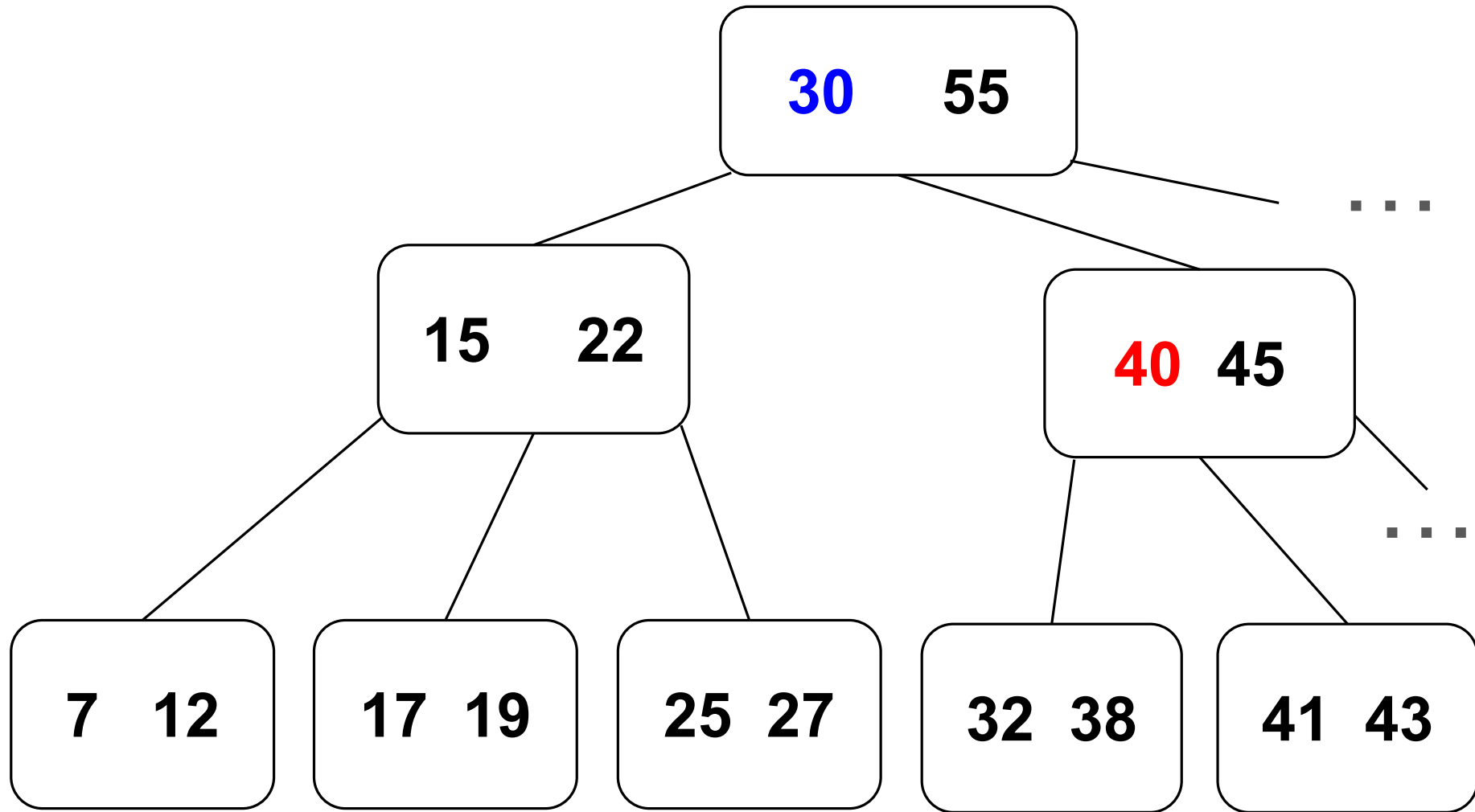






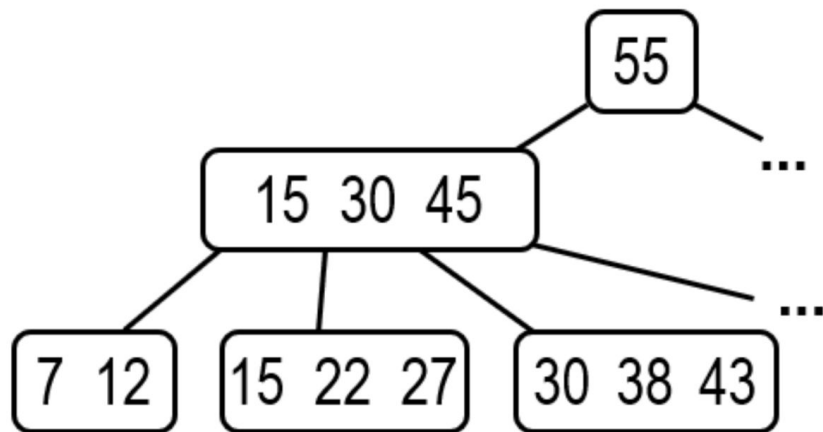






### Task 3: Perform insertions in a B+tree

Consider the following diagram, which shows a portion of a B+tree (note the + symbol!) of order 2:

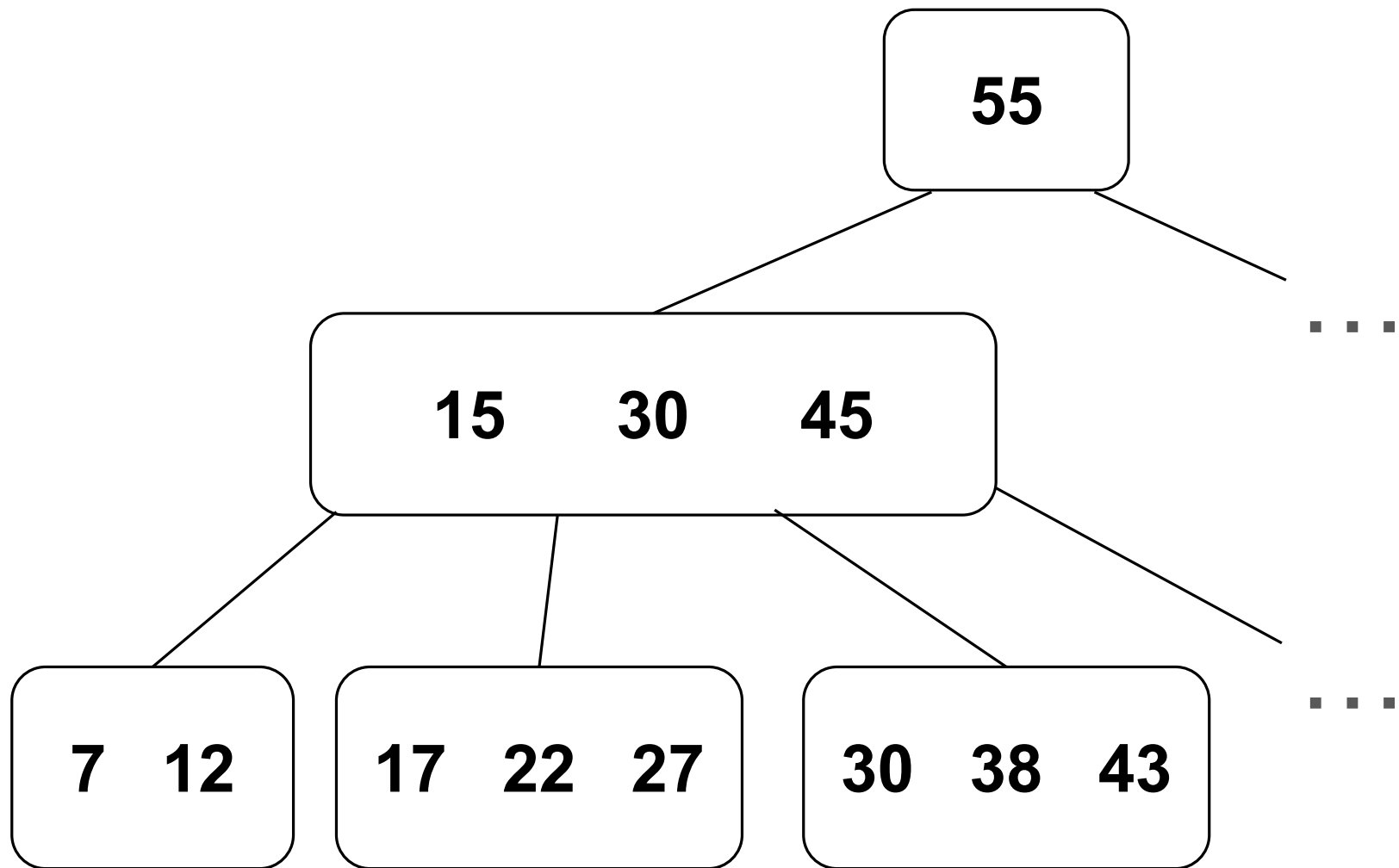


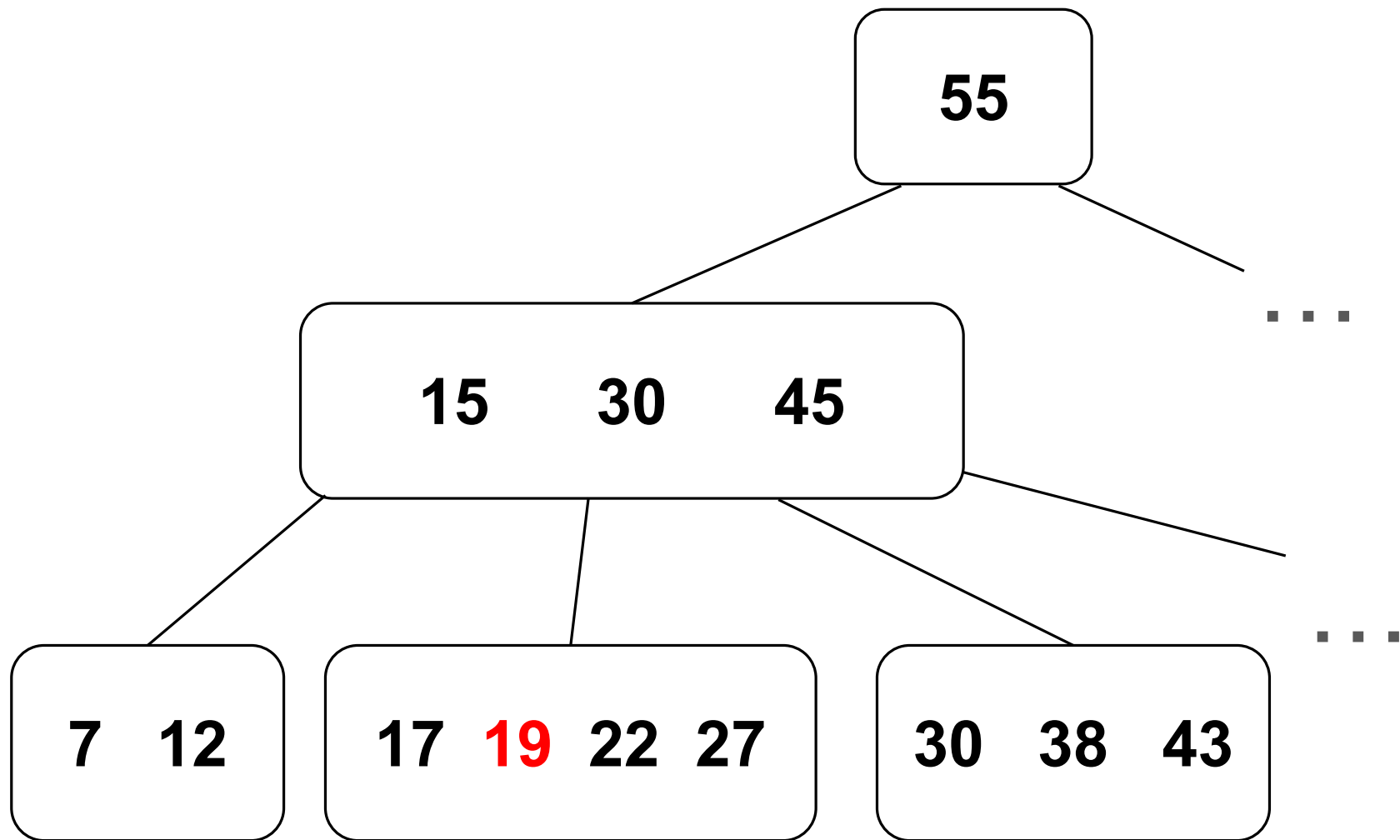
Note that this tree is similar to the initial tree in Task 2, but some keys are missing, and other keys appear in two places.

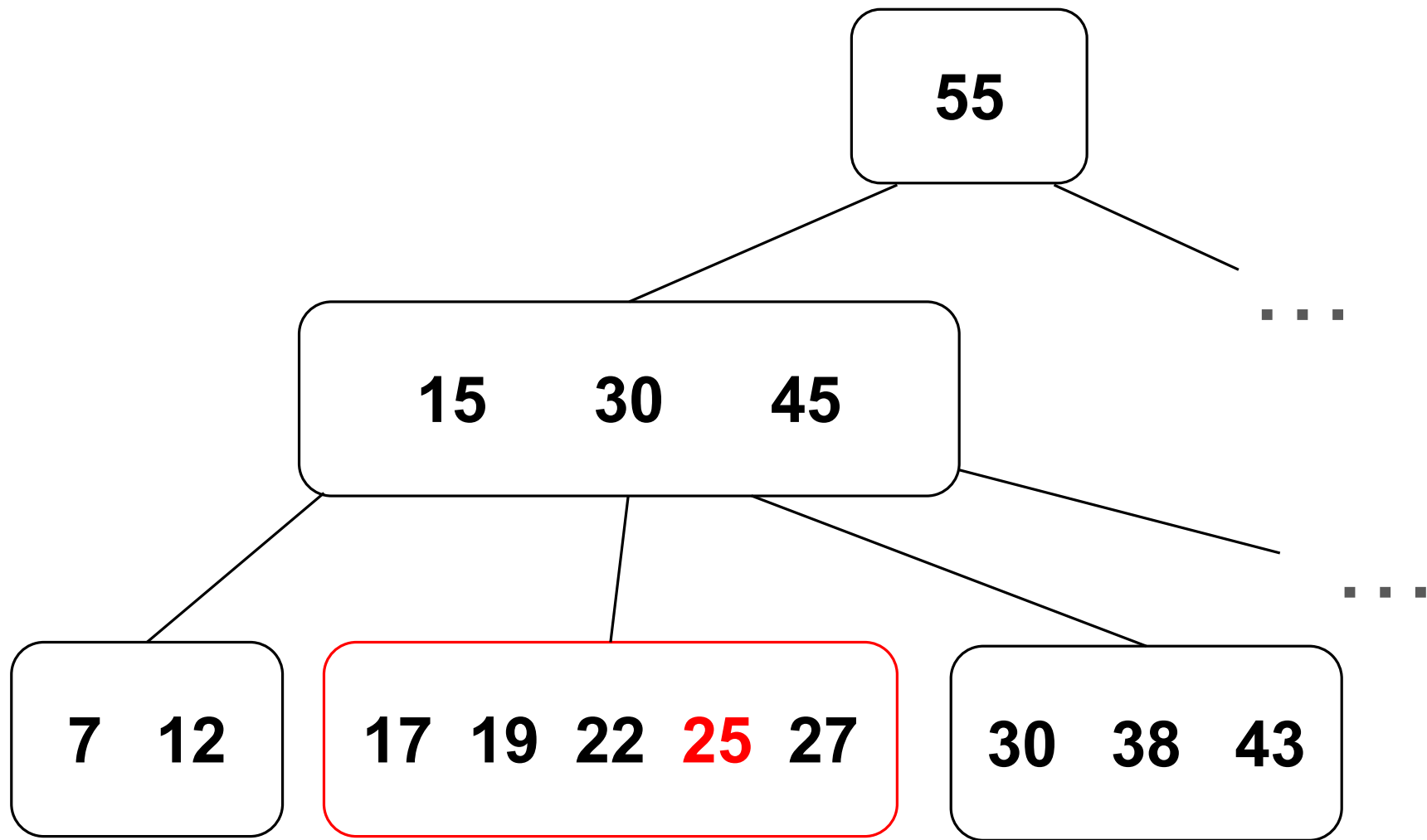
## 0. Why does it make sense that we have repeated keys?

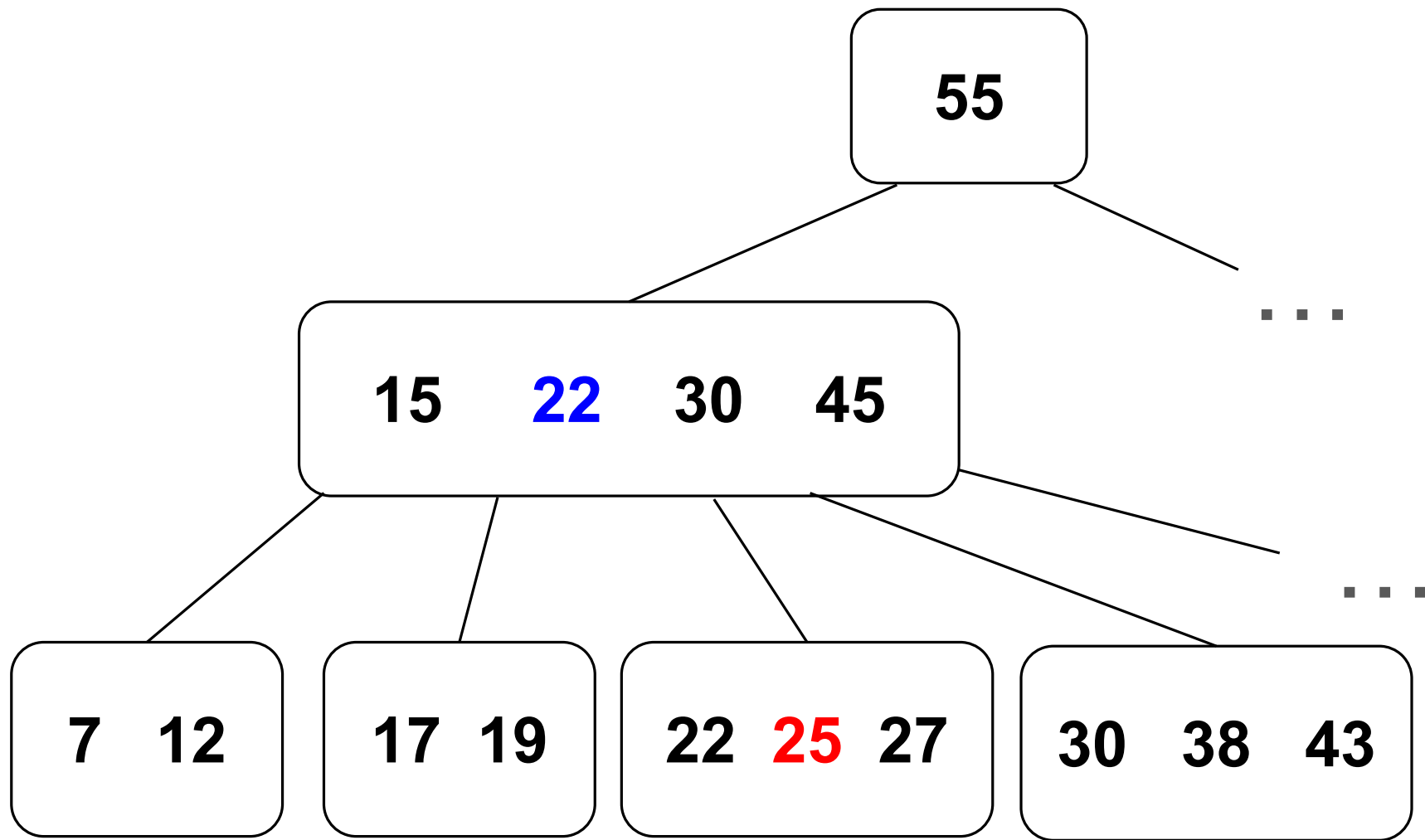
In a B+tree, the full key-value pairs are all stored in leaf nodes. The interior nodes only contain keys.

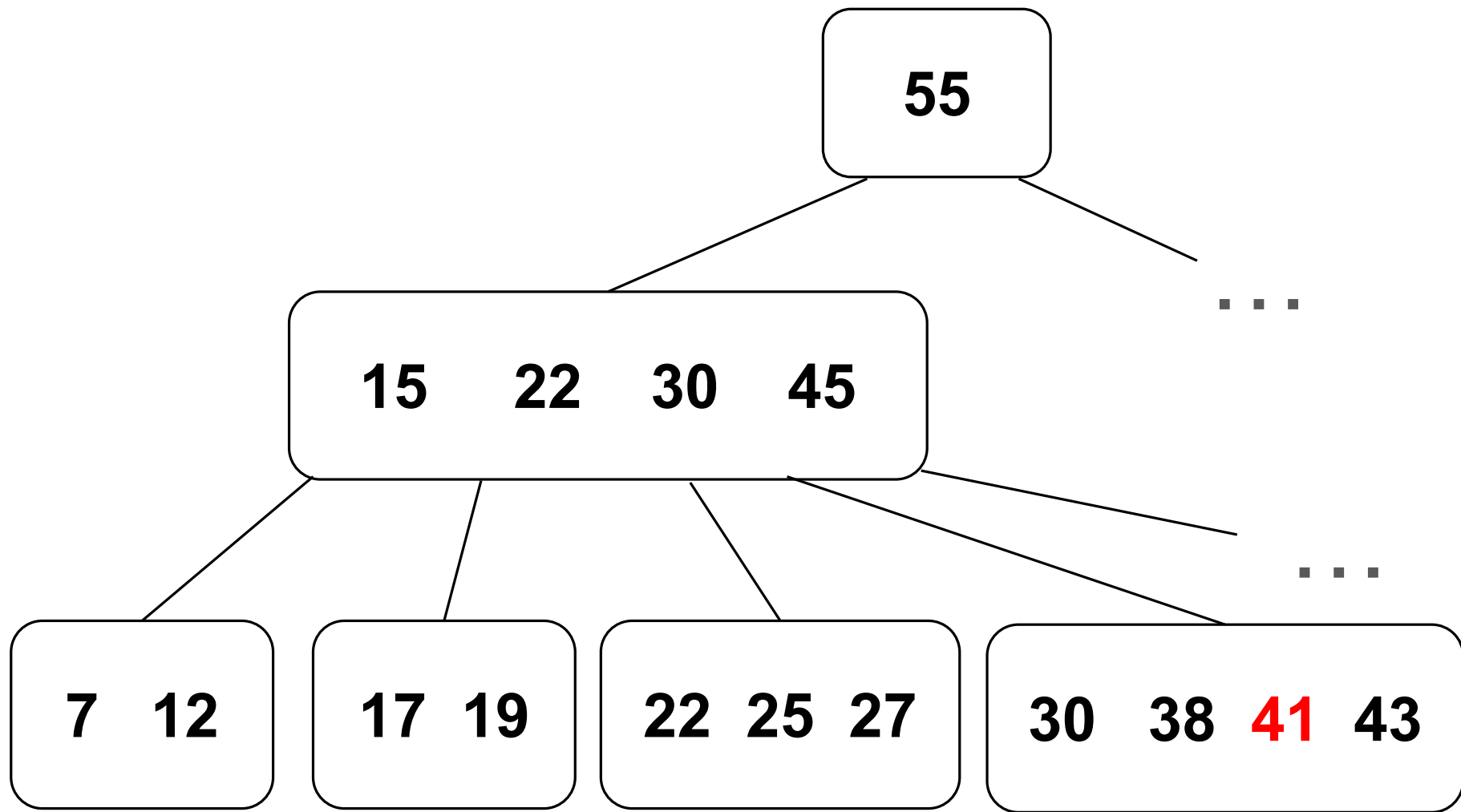
When a node is split, the middle key is sent up and inserted in the parent, but the corresponding key-value pair remains at the leaf level, in the new node that is created as part of the split.

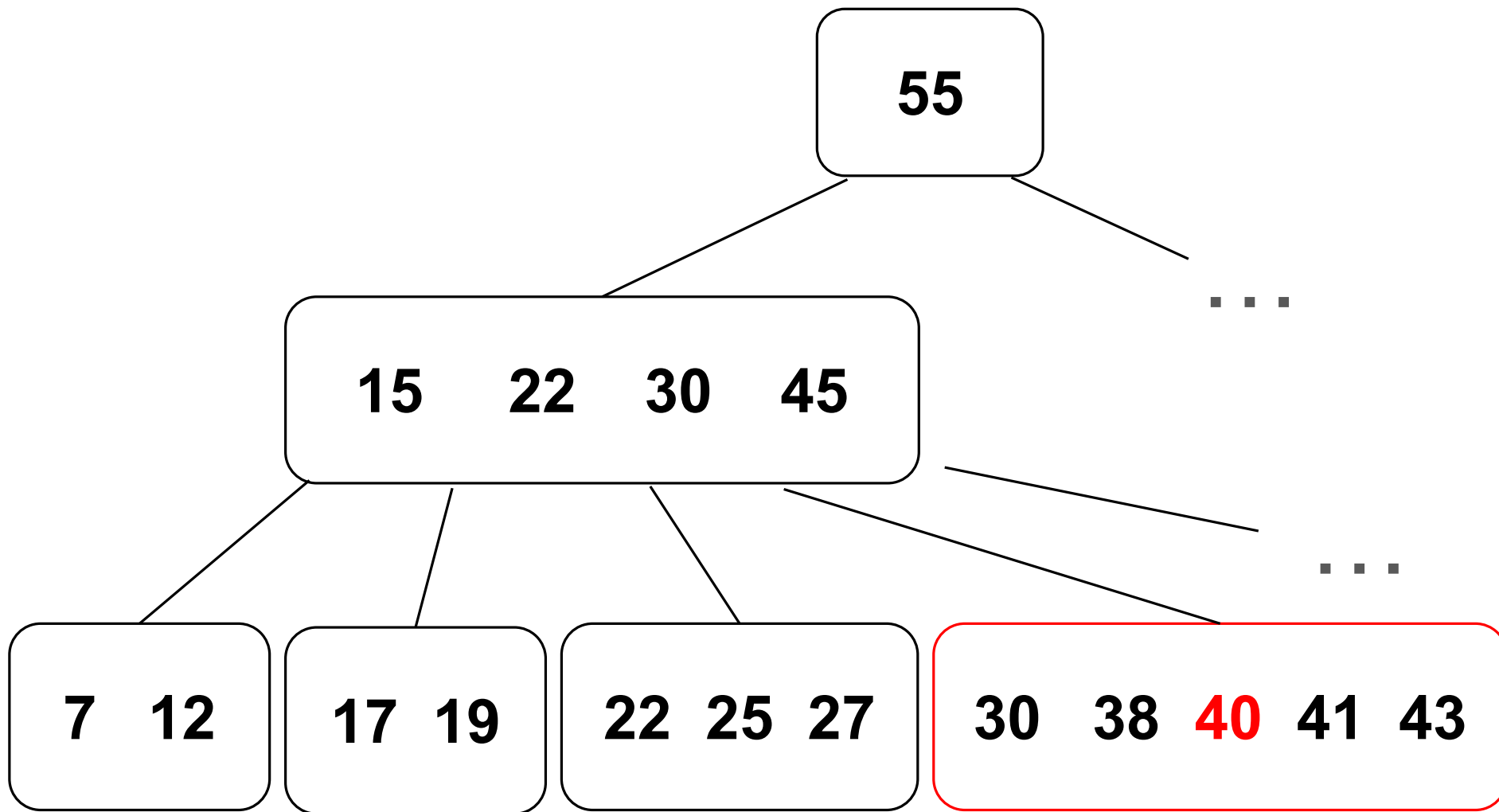














**55**

```
graph TD; 55[55] --- L1[15 22 30 40 45]; 55 --- L1_ellipsis[...]; L1 --- L2_1[7 12]; L1 --- L2_2[17 19]; L1 --- L2_3[22 25 27]; L1 --- L2_4[30 38]; L1 --- L2_5[40 41 43]; L1 --- L1_ellipsis[...];
```

**15 22 30 40 45**

...

...

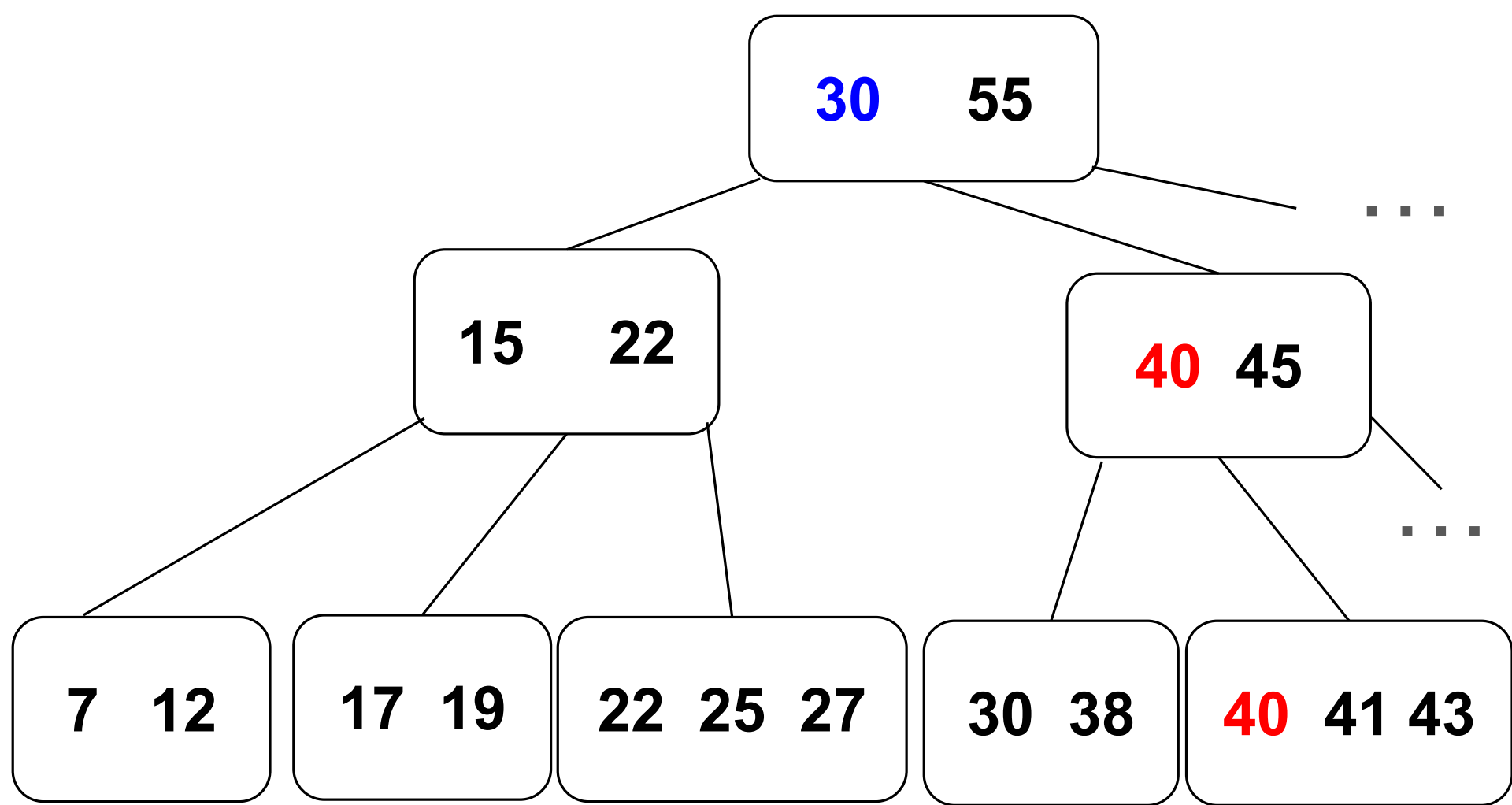
**7 12**

**17 19**

**22 25 27**

**30 38**

**40 41 43**



$$h(k) = k \% 10$$

- We grow the table whenever the number of items ( $f$ ) becomes more than twice the number of buckets ( $n$ ).

0 [1000, 972]

1 [713]

1. an item (i.e., a key-value pair) whose key is 12

$$h(k) = k \% 10$$

- We grow the table whenever the number of items ( $f$ ) becomes more than twice the number of buckets ( $n$ ).

0 [1000, 972]

1 [713]

1. an item (i.e., a key-value pair) whose key is 12

$h(12) = 2 = 0010$ . The rightmost bit is 0, so add 12 to 0.

0 [1000, 972, 12]

1 [713]

$$h(k) = k \% 10$$

- We grow the table whenever the number of items ( $f$ ) becomes more than twice the number of buckets ( $n$ ).

0 [1000, 972]

1 [713]

1. an item (i.e., a key-value pair) whose key is 12

$h(12) = 2 = 0010$ . The rightmost bit is 0, so add 12 to 0.

0 [1000, 972, 12]

1 [713]

$f = 4, n = 2$

Add bucket when

$f > 2n$

$f > 4$

\*Add bucket on  
next insert

0 [1000, 972, 12]  
1 [713]

**Insert 436**

0 [1000, 972, 12]  
1 [713]

**Insert 436**

**436 % 10 = 6 = 0110**

0 [1000, 972, 12, 436]  
1 [713]

0 [1000, 972, 12]  
1 [713]

## Insert 436

$$436 \% 10 = 6 = 011\underline{0}$$

0 [1000, 972, 12, 436]  
1 [713]

$f > 2n$ , add bucket



```
0 [1000, 972, 12]
1 [713]
```

## Insert 436

**436 % 10 = 6 = 0110**

```
0 [1000, 972, 12, 436]
1 [713]
```

$f > 2n$ , add bucket

```
00 [1000, 972, 12, 436]
01 [713]
10 []
```

0 [1000, 972, 12]  
1 [713]

## Insert 436

$$436 \% 10 = 6 = 011\underline{0}$$

0 [1000, 972, 12, 436]  
1 [713]

$f > 2n$ , add bucket

00 [1000, 972, 12, 436]  
01 [713]  
10 []

rehash!



00 [1000, 972, 12, 436]  
01 [713]  
10 []



00 [1000] (because 1000 hashes to 0000, or 00)  
01 [713] (we don't need to look at the contents of this bucket at all)  
10 [972, 12, 436] (972 and 12 hash to 0010; 436 hashes to 0110 or 10)

00 [1000]

01 [713]

10 [972, 12, 436]

insert 113

00 [1000]

01 [713]

10 [972, 12, 436]

insert 113

$113 \% 10 = 3$

3 = 0011

00 [1000]

01 [713, 113]

10 [972, 12, 436]

00 [1000]  
01 [713, 113]  
10 [972, 12, 436]       $\xrightarrow{\text{insert 116}}$       00 [1000]  
01 [713, 113]  
10 [972, 12, 436, 116]

$\xrightarrow{\text{Split}}$       00 [1000]  
01 [713, 113]  
10 [972, 12, 436, 116]       $\xrightarrow{\text{rehash}}$   
11 []

00 [1000] (we don't need to look at the contents of this bucket at all)  
01 [] (nothing remains after rehashing!)  
10 [972, 12, 436, 116] (we don't need to look at the contents of this bucket at all)  
11 [713, 113] (they both hash to 0011 or 11)