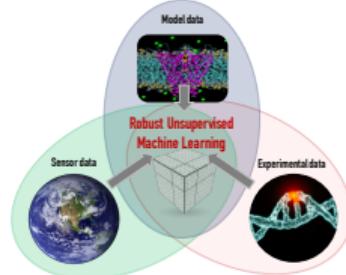


# Unsupervised Machine Learning Based on Tensor Factorization

Daniel O'Malley, Velimir V. Vesselinov (monty), Boian S. Alexandrov

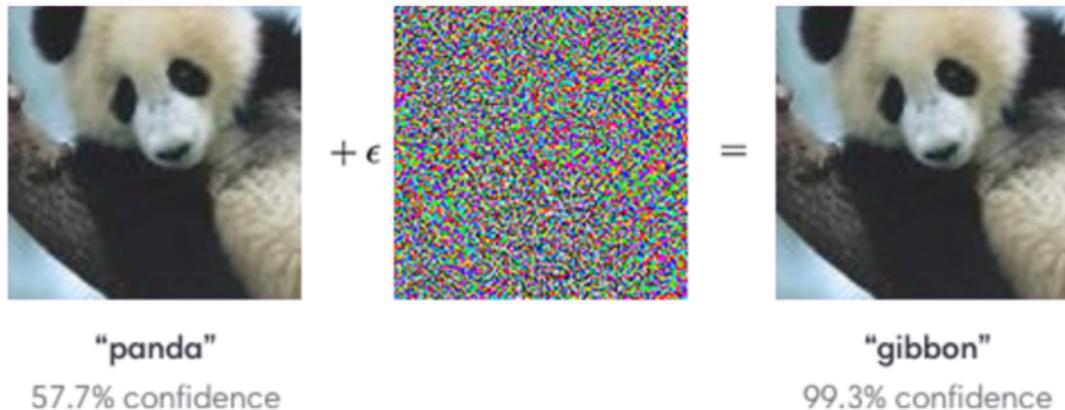
**Earth and Environmental Sciences Division — Theoretical Division**

Los Alamos National Laboratory, NM 87545, USA



- ▶ **Supervised** Machine Learning: requires prior categorization of the processed data (can introduce subjectivity)
- ▶ **Unsupervised** Machine Learning: discovers hidden features in the processed data without any prior information
- ▶ **Deep** Machine Learning: ... coupled supervised and unsupervised techniques

# Adversarial Examples



An adversarial input, overlaid on a typical image, can cause a classifier to miscategorize a panda as a gibbon.

- ▶ **Data analytics:**

- ▶ Feature extraction (**FE**)
- ▶ Blind source separation (**BSS**)
- ▶ Image recognition
- ▶ Detection of disruptions / anomalies
- ▶ Guide development of physics / reduced-order models representing the data

- ▶ **Analyses of model outputs:**

- ▶ Identify dominant processes (features) in the model outputs
- ▶ Guide development of reduced-order models

# Our Unsupervised Machine Learning Methodology

- ▶ We have developed a series of novel Unsupervised Machine Learning methods based on Nonnegative Factorization (Matrix and Tensor) + custom clustering
  - ▶ identify **the number of robust features** in the data
  - ▶ extract **robust features** representing the data
  - ▶ extracted features are parts of the data allowing for **intuitive** interpretations
- ▶ Selected publications:
  - ▶ Vesselinov, O'Malley, Alexandrov, Contaminant source identification using semi-supervised machine learning, Journal of Contaminant Hydrology, 10.1016/j.jconhyd.2017.11.002, 2017.
  - ▶ Alexandrov, Vesselinov, Blind source separation for groundwater level analysis based on nonnegative matrix factorization, Water Resources Research, 10.1002/2013WR015037, 2014.
- ▶ Machine Learning **Patent**:  
Alexandrov, Vesselinov, Alexandrov, Iliev, Stanev, Source Identification by **Nonnegative Matrix Factorization** Combined with Semi-Supervised Clustering, LANS Ref. No. S133364.000, KS Ref. No. 8472-97415-01, March 2018
- ▶ Machine Learning **Copyright Disclosure** :  
Alexandrov, Vesselinov, **Nonnegative Tensor Factorization**, November 2018

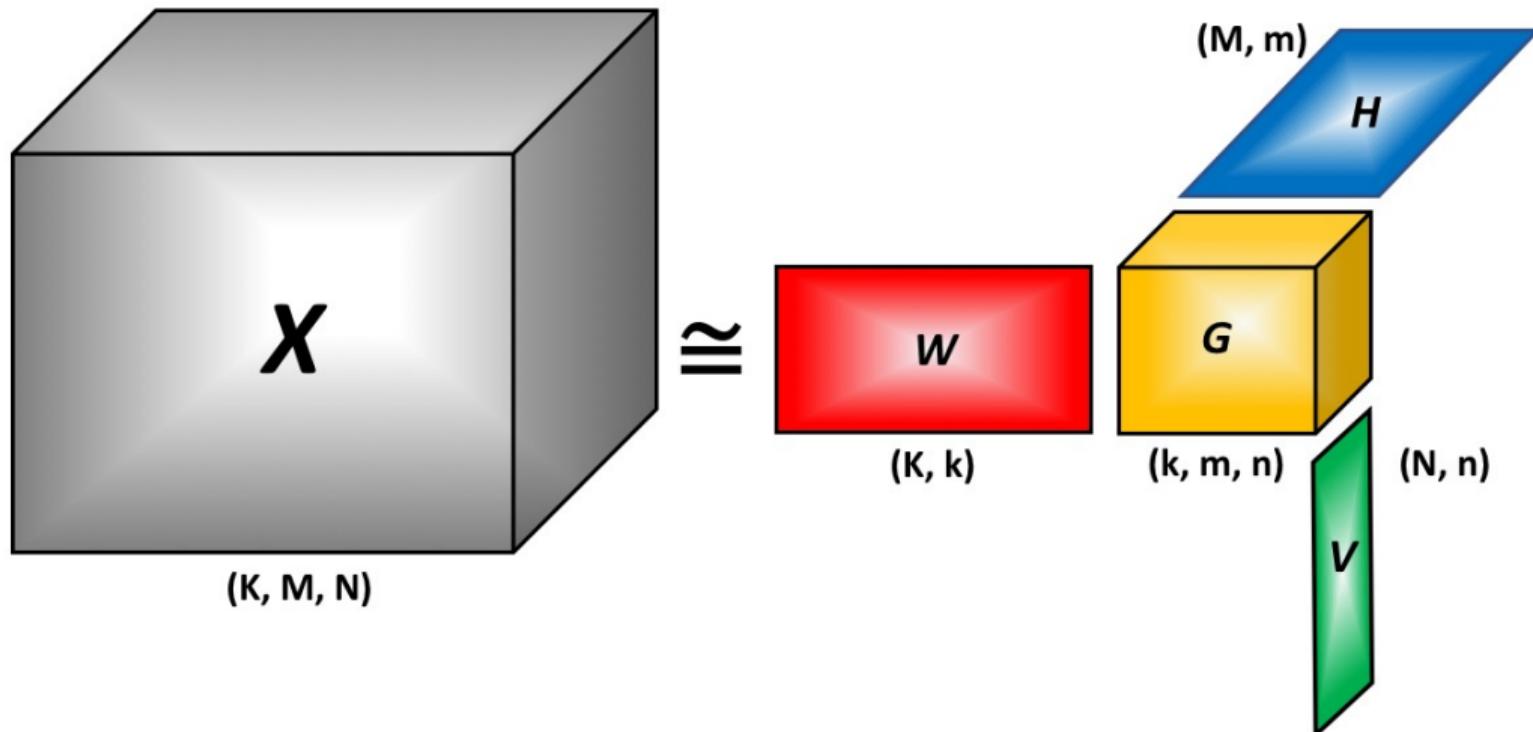
# Our Unsupervised Machine Learning Methodology Applications

- ▶ **NMF $k$** : matrix-based (two-dimensional) algorithms (well-tested; widely used)
  - ▶ Extract barometric and pumping effects in pressure data
  - ▶ Identify and predict processes for optimal control of the LANSCE particle accelerator
  - ▶ Characterize materials using X-ray
  - ▶ Analyze model predictions of molecular dynamics trajectories
  - ▶ Characterize influenza epidemics
  - ▶ Extract image features using Quantum Computing (**D-Wave**)
  - ▶ Identify cancer signatures in human genomes (**30+** papers in Nature/Science/Cell)
- ▶ **NTF $k$** : tensor-based (high-dimensional) algorithms (actively developed at the moment)
- ▶ Here, we present several **NTF $k$**  applications

## Matrix/Tensor Factorization (NTF) challenges

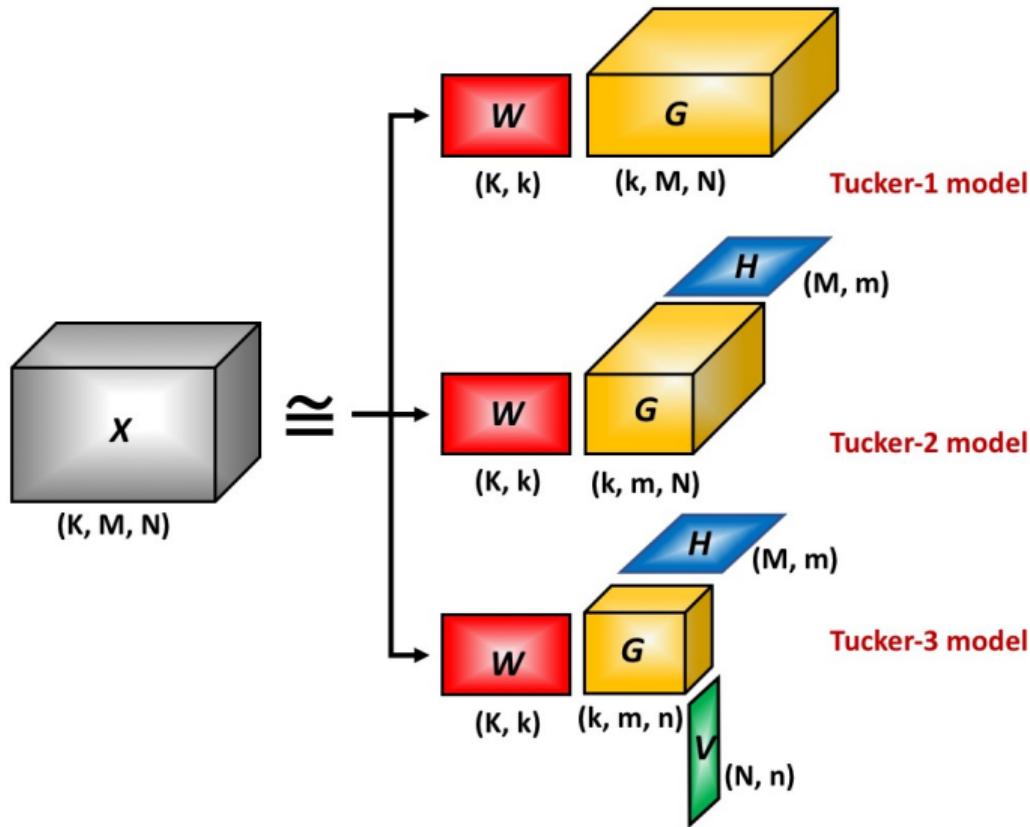
- ▶ identifying the number of unknown features (groundwater types) **K**  
(in **NMF $k$** , resolved using custom clustering based on the Frobenius norm and cluster Silhouettes; identification under **NTF $k$**  is much more challenging ...)
- ▶ solving the constraint optimization problem to estimate matrix/tensor elements
- ▶ dealing with large high-dimensional datasets (high-performance computing)
- ▶ ...

## Tucker-3 tensor factorization (3D case)

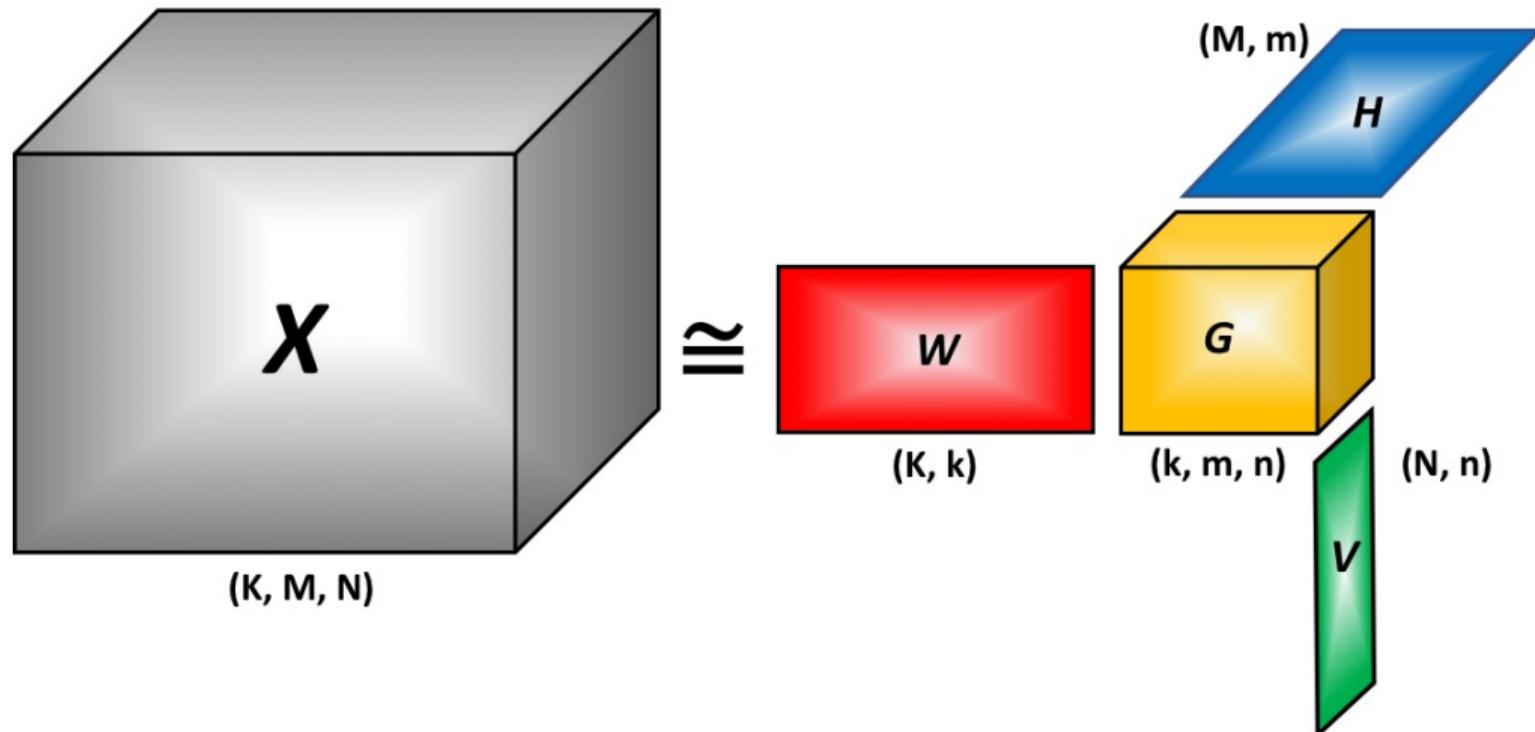


Factorizing all **3** dimensions ( $K \rightarrow k$ ,  $M \rightarrow m$ ,  $N \rightarrow n$ )

## Tucker tensor factorizations (3D case)

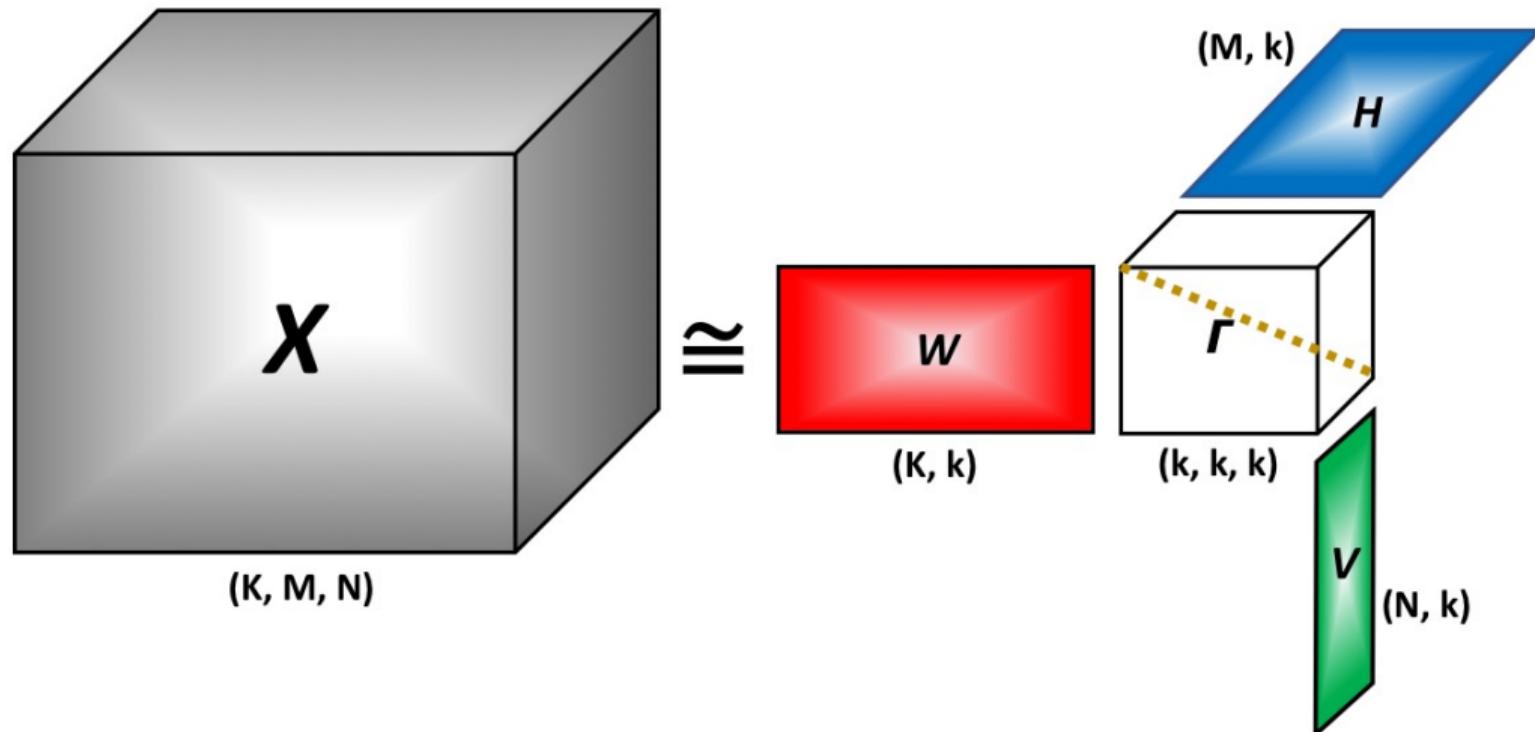


## Tucker-3 tensor factorization (3D case)



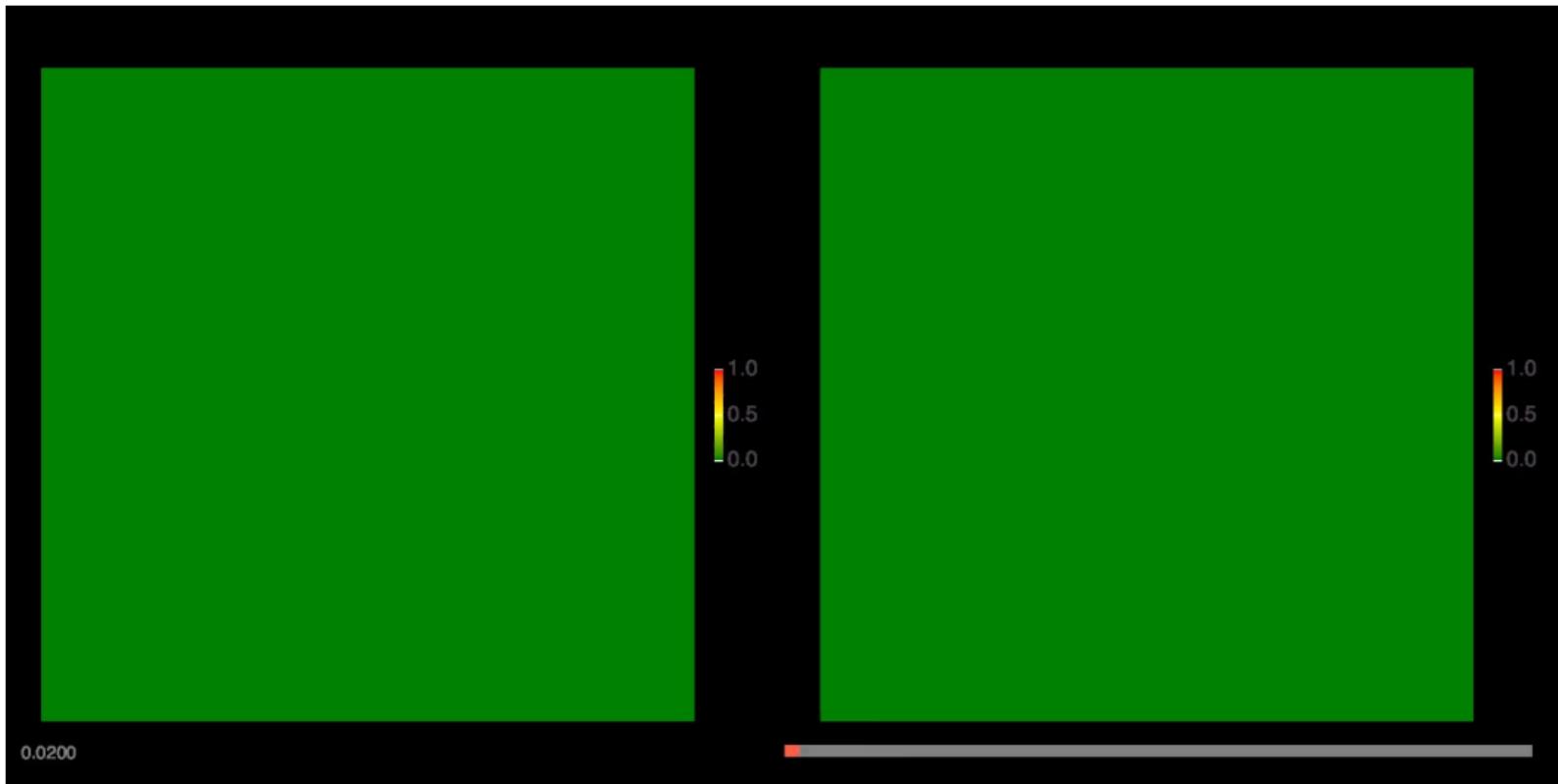
Factorizing all **3** dimensions ( $K \rightarrow k$ ,  $M \rightarrow m$ ,  $N \rightarrow n$ )

## Candecomp/Parafac (CP) tensor factorization (3D case)



Factorizing all **3** dimensions ( $K \rightarrow k$ ,  $M \rightarrow k$ ,  $N \rightarrow k$ )

## Tucker-3 tensor example



Factorizing all **3** dimensions ( $50 \rightarrow 6, 50 \rightarrow 44, 50 \rightarrow 48$ )

Machine Learning  
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NTF  
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Geochemistry  
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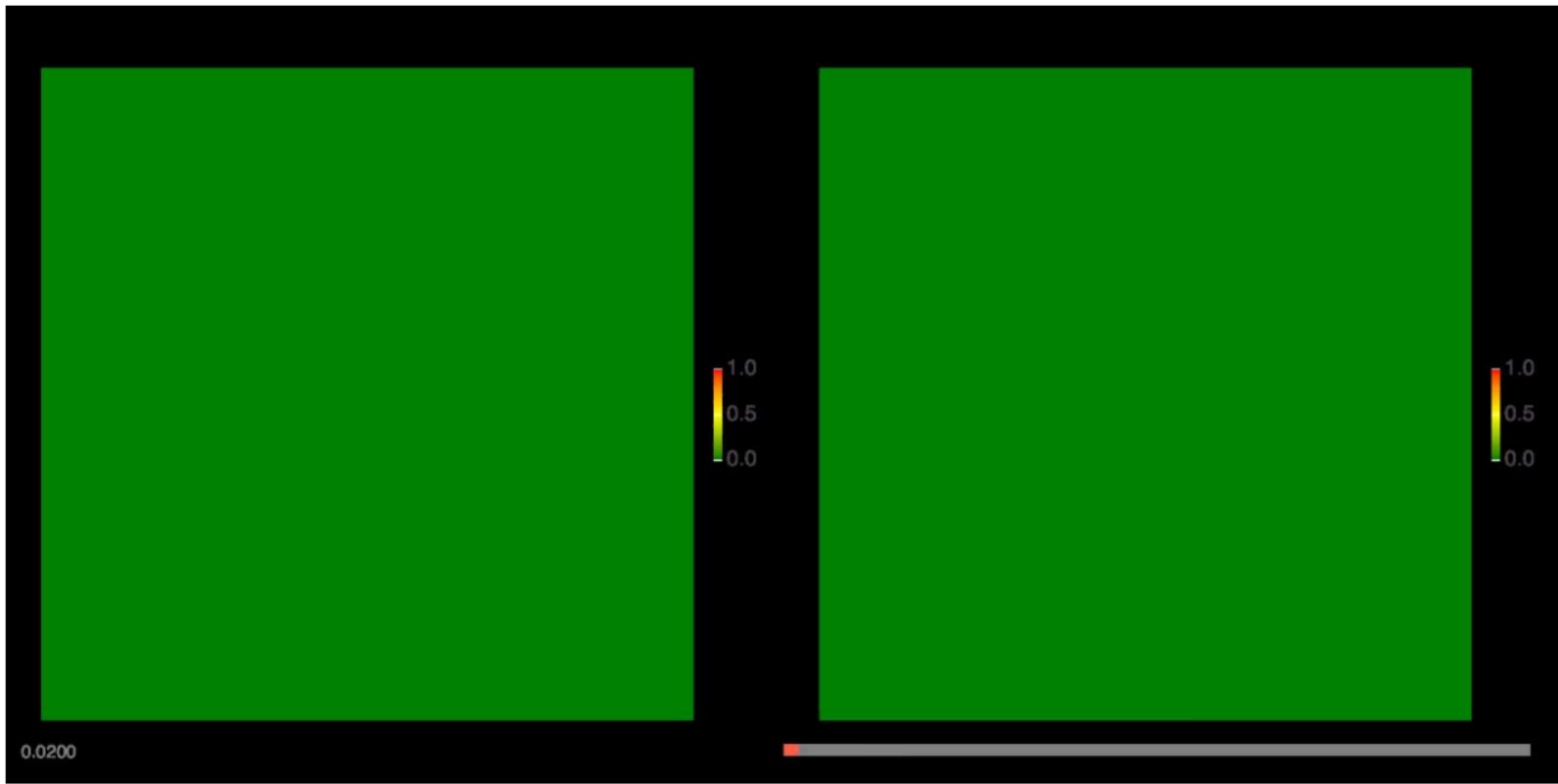
Fluid mixing  
○○○○

Polymers  
○

Climate  
○○○ ○○○○○○ ○○○○

Summary  
○○

## Tucker-3 tensor example



6 groups of swimmers (x); 44 lanes occupied (y); 48 time frames (first/last empty)

Machine Learning  
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NTF  
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Geochemistry  
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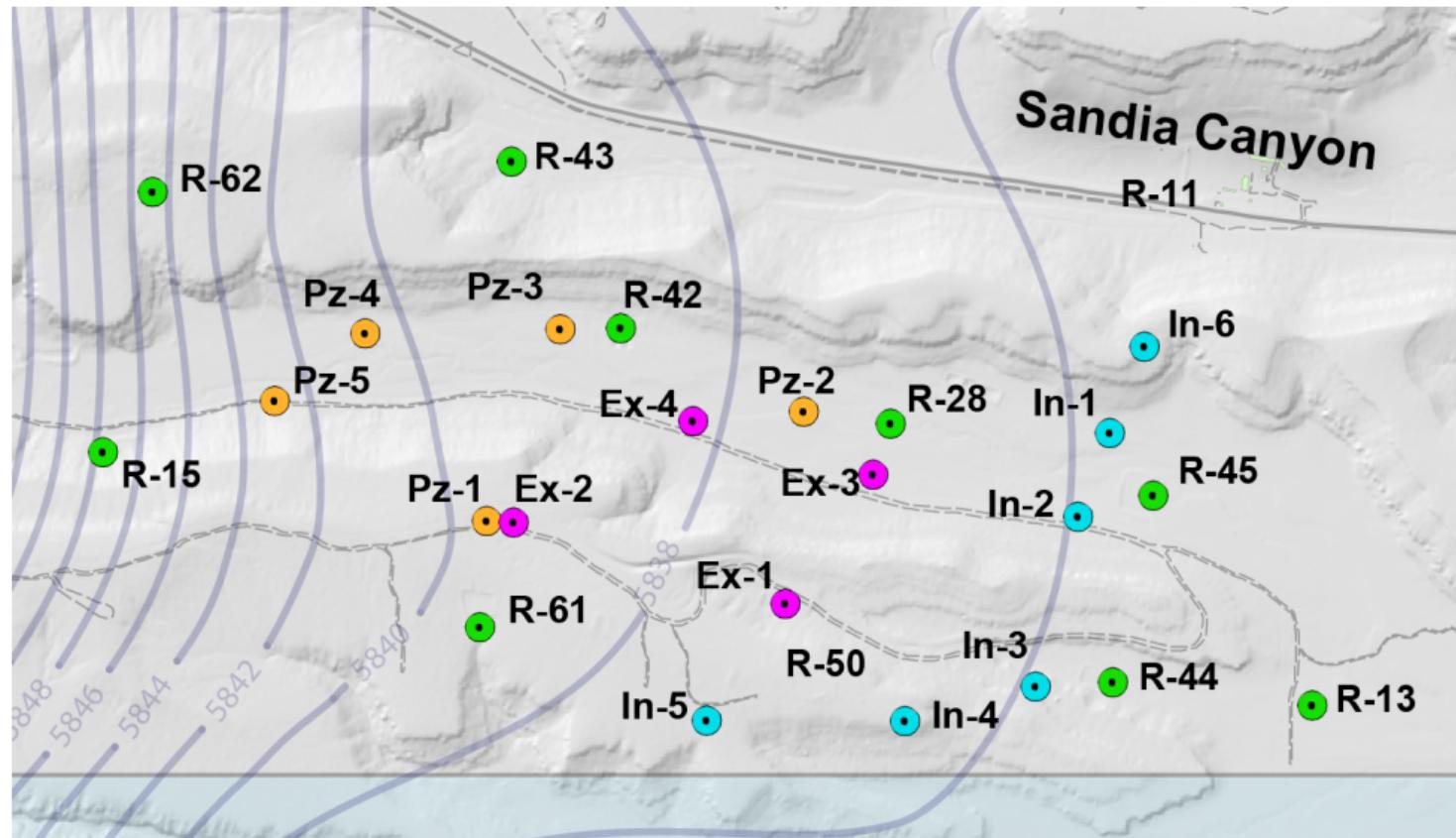
Fluid mixing  
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Polymers  
○

Climate  
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Summary  
○○

# LANL site



Machine Learning  
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NTF  
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Geochemistry  
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Fluid mixing  
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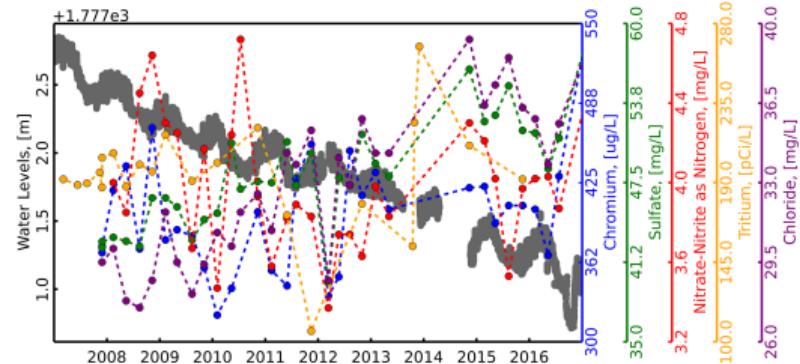
Polymers  
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Climate  
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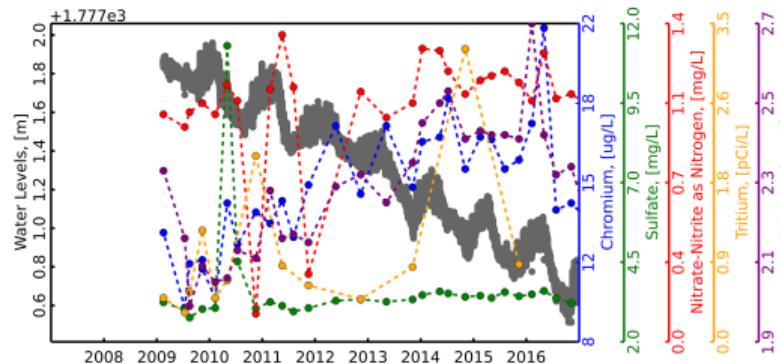
Summary  
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# LANL hydrogeochemical datasets

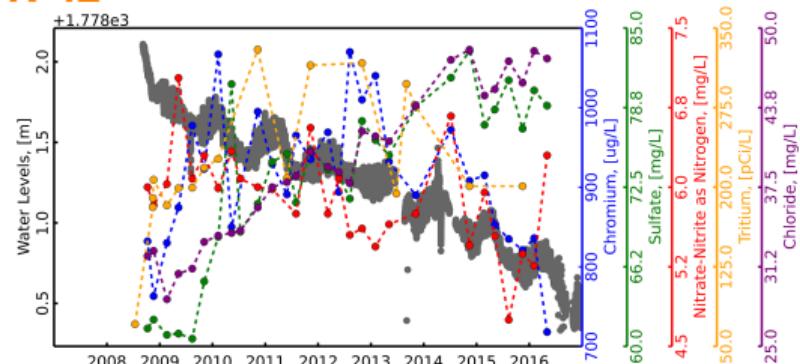
R-28



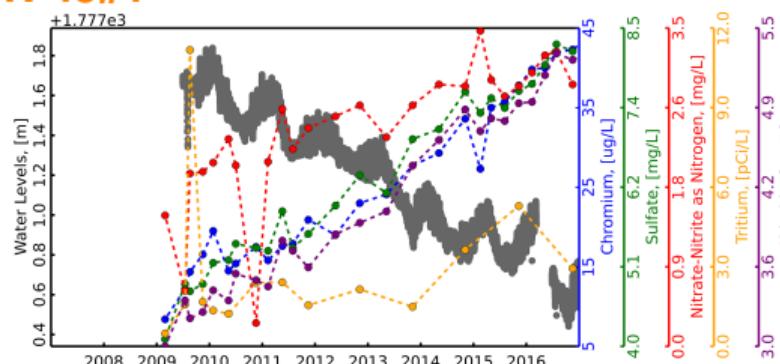
R-44#1



R-42



R-45#1



Machine Learning  
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NTF  
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Geochemistry  
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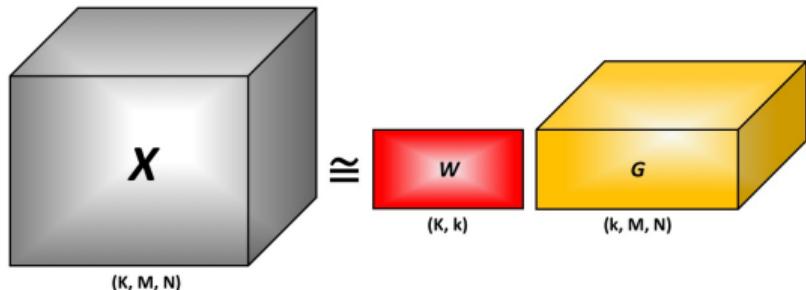
Fluid mixing  
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Polymers  
○

Climate  
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Summary  
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# Geochemistry: Nonnegative Tensor Factorization based on Tucker-1 decomposition



- ▶  $X$ : data tensor
- ▶  $W$ : source (groundwater type) matrix (**unknown**)
- ▶  $G$ : mixing tensor (**unknown**)

- ▶  $M$ : number of observation points (wells)
- ▶  $N$ : number of observation times (e.g., 2001, 2002, ..., 2017)
- ▶  $K$ : number of geochemical species observed (e.g.,  $Cr^{6+}$ ,  $SO_4^{2+}$ ,  $NO_3^-$ , etc.)
- ▶  $k$ : number of **unknown** groundwater types mixed at each well
- ▶ **Constraints:**

$$\text{all tensor/matrix elements } \geq 0$$
$$\sum_{i=1}^k G_{i,j,t} = 1 \quad \forall j, t$$

## Machine Learning analyses estimated 7 groundwater types

| Sources | $Cr$<br>( $\mu g/L$ ) | $Cl^-$<br>( $mg/L$ ) | $ClO_4$<br>( $\mu g/L$ ) | $^3H$<br>( $pCi/L$ ) | $NO_3$<br>( $mg/L$ ) | $Ca$<br>( $mg/L$ ) | $Mg$<br>( $mg/L$ ) | $SO_4$<br>( $mg/L$ ) |
|---------|-----------------------|----------------------|--------------------------|----------------------|----------------------|--------------------|--------------------|----------------------|
| S1      | 2970.00               | 63.00                | 0.00                     | 0.00                 | 14.00                | 73.00              | 25.00              | 170.00               |
| S5      | 21.00                 | 51.00                | 0.00                     | 950.00               | 2.40                 | 67.00              | 15.00              | 50.00                |
| S6      | 1.50                  | 64.00                | 0.00                     | 0.00                 | 2.80                 | 51.00              | 10.00              | 68.00                |
| S2      | 0.79                  | 0.35                 | 14.00                    | 0.00                 | 0.50                 | 5.30               | 1.70               | 0.60                 |
| S4      | 0.50                  | 0.14                 | 0.00                     | 0.00                 | 10.00                | 21.00              | 5.00               | 10.00                |
| S3 (B)  | 0.25                  | 3.60                 | 0.00                     | 0.00                 | 0.01                 | 41.00              | 11.00              | 0.06                 |
| S7 (B)  | 0.10                  | 0.03                 | 0.00                     | 0.00                 | 0.01                 | 0.40               | 0.80               | 0.90                 |

Machine Learning  
○○○

NTF  
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Geochemistry  
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Fluid mixing  
○○○○

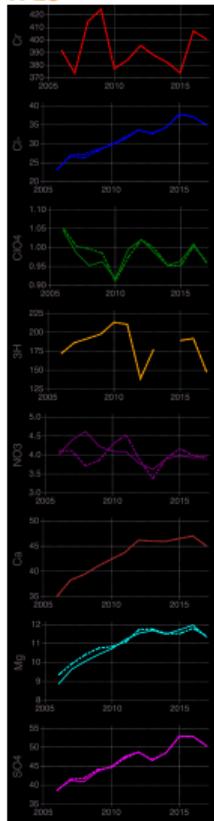
Polymers  
○

Climate  
○○○○ ○○○○○○ ○○○○

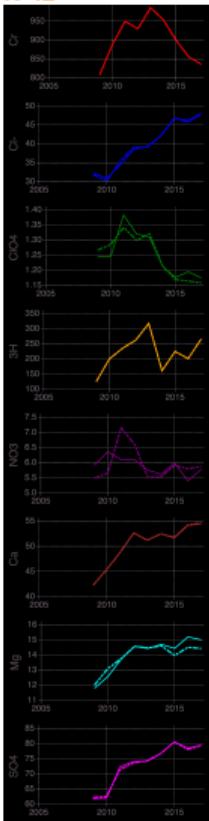
Summary  
○○

# NTF<sub>k</sub> estimated concentrations at various wells

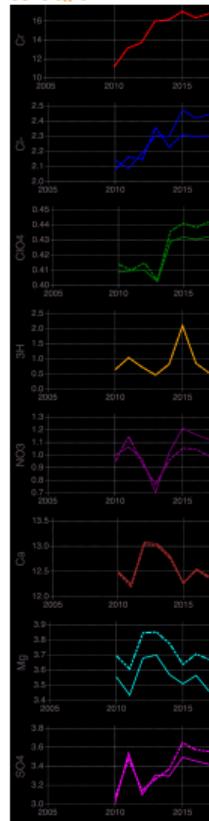
R-28



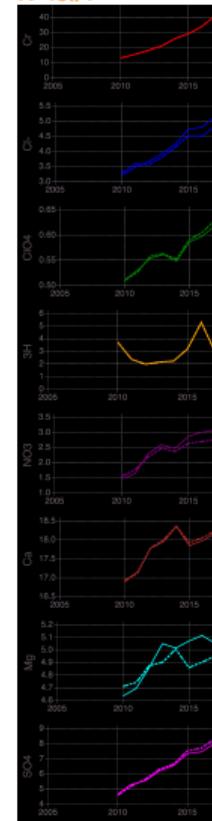
R-42



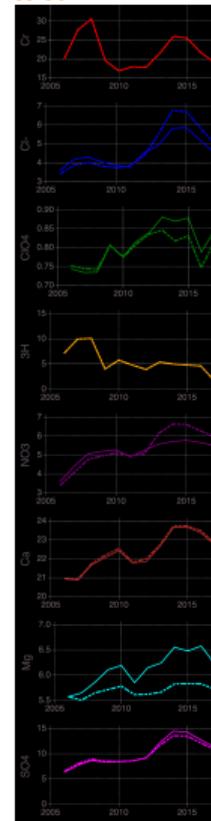
R-44#1



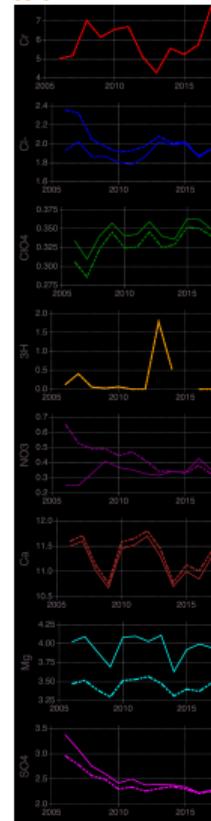
R-45#1



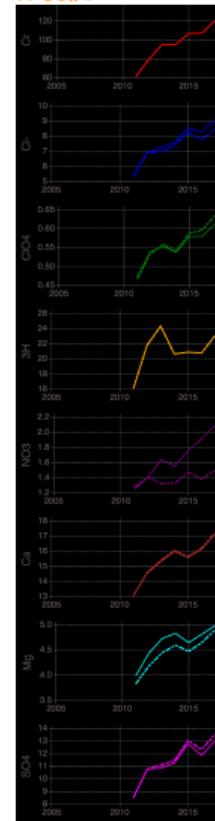
R-11



R-1



R-50#1



Machine Learning  
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NTF  
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Geochemistry  
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Fluid mixing  
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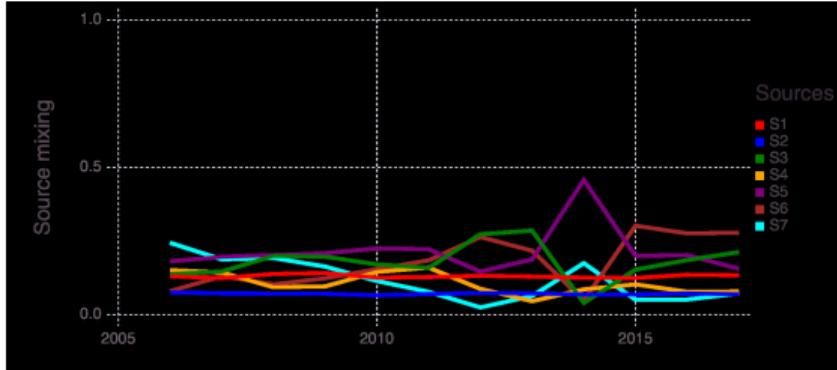
Polymers  
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Climate  
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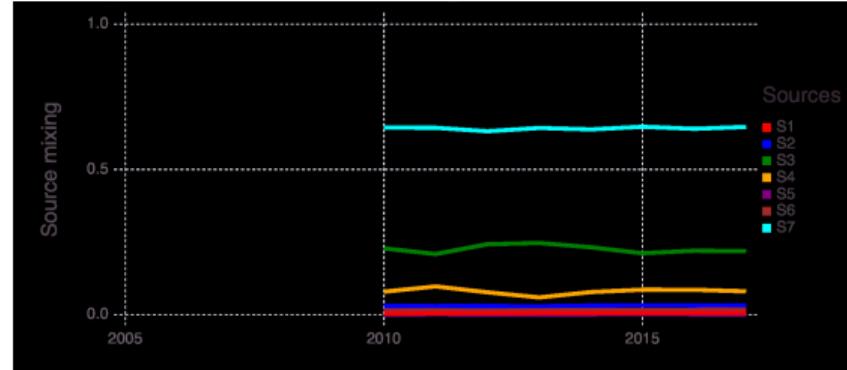
Summary  
○○

# NTF<sub>k</sub> estimated time-dependent mixing of 7 groundwater types at various wells

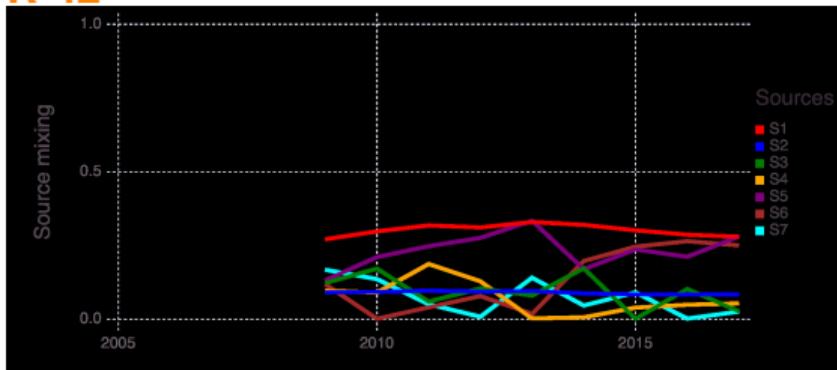
R-28



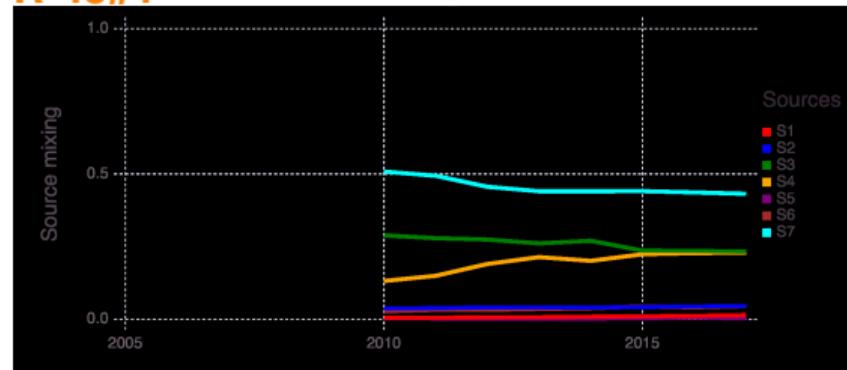
R-44#1



R-42



R-45#1



Machine Learning  
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NTF  
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Geochemistry  
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Fluid mixing  
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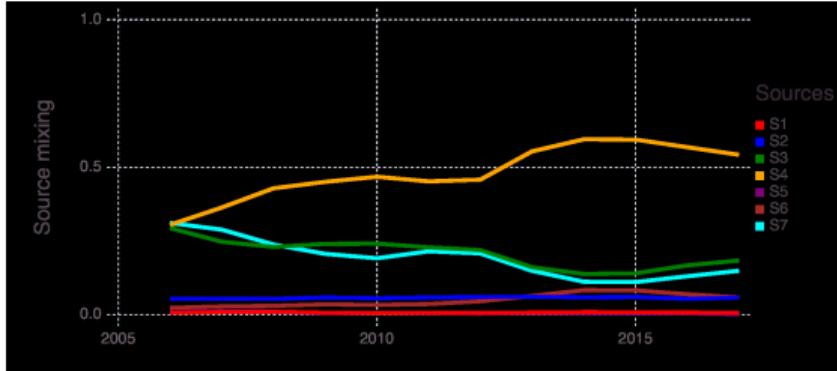
Polymers  
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Climate  
○○○○ ○○○○○○ ○○○○

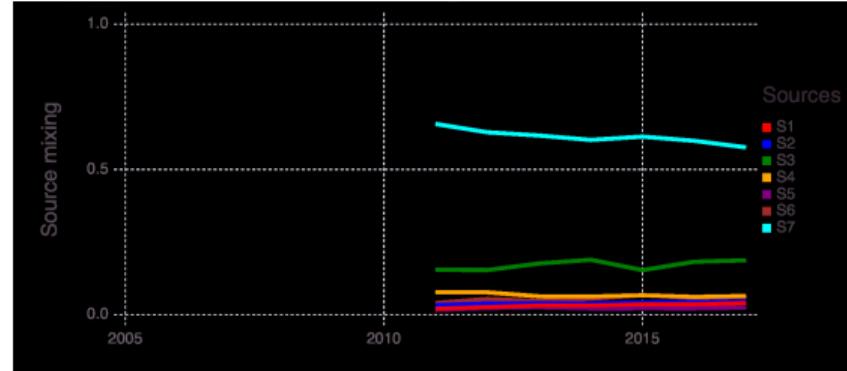
Summary  
○○

# NTF<sub>k</sub> estimated time-dependent mixing of 7 groundwater types at various wells

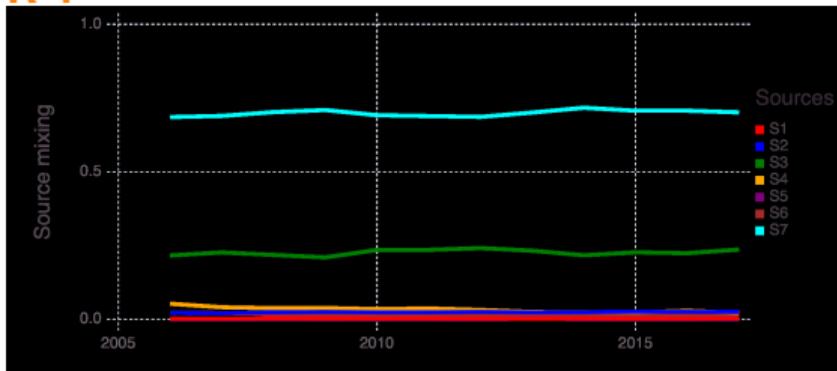
R-11



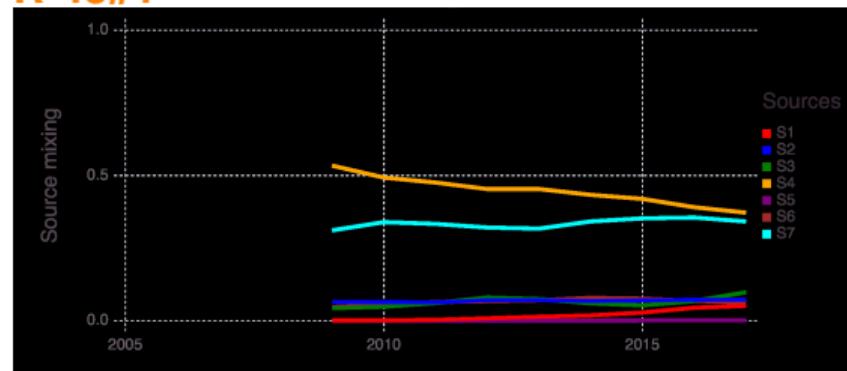
R-50#1



R-1



R-43#1



Machine Learning  
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NTF  
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Geochemistry  
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Fluid mixing  
○○○○

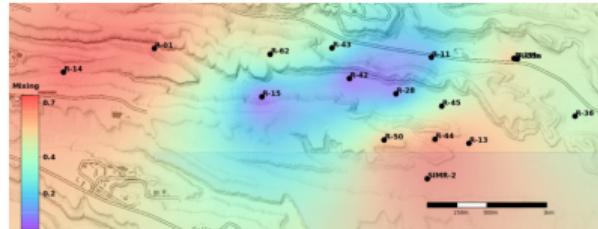
Polymers  
○

Climate  
○○○○ ○○○○○ ○○○○

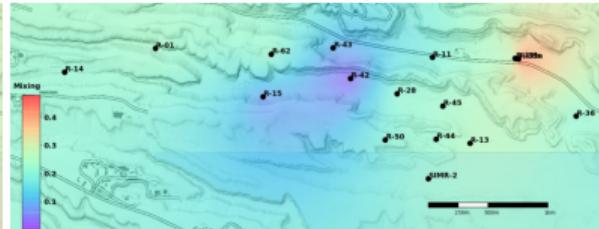
Summary  
○○

# NTF<sub>k</sub> identified sources (groundwater types) Jan-Dec 2016

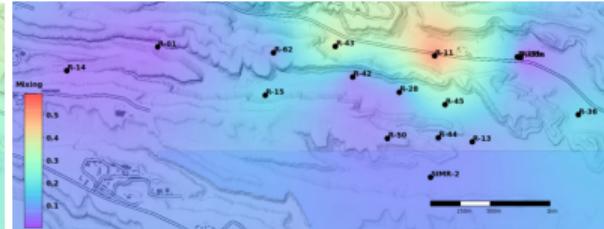
Source 7: (background)



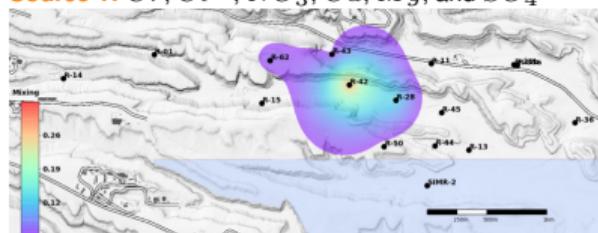
Source 3:  $Cl^-$ ,  $Ca$ ,  $Mg$  (background)



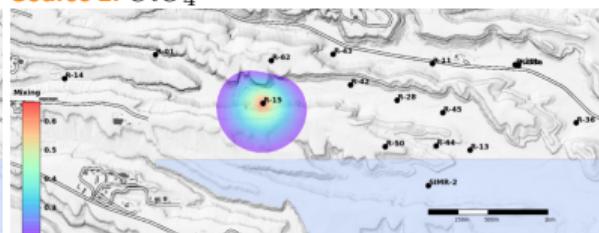
Source 4:  $NO_3$



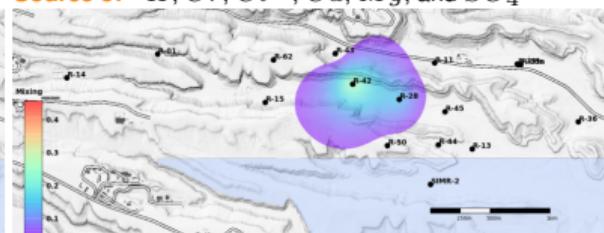
Source 1:  $Cr$ ,  $Cl^-$ ,  $NO_3$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



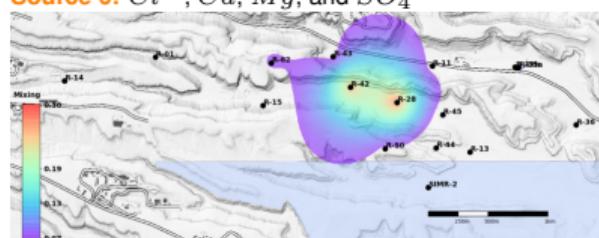
Source 2:  $ClO_4$



Source 5:  $^3H$ ,  $Cr$ ,  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

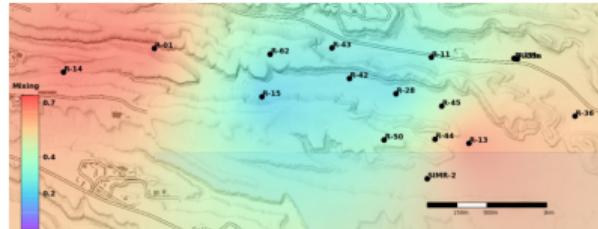


Source 6:  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

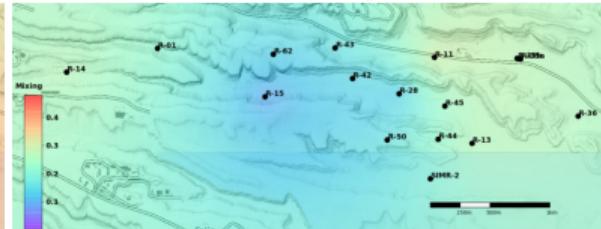


# NTF<sub>k</sub> identified sources (groundwater types) Jan-Dec 2005

Source 7: (background)



Source 3:  $Cl^-$ ,  $Ca$ ,  $Mg$  (background)



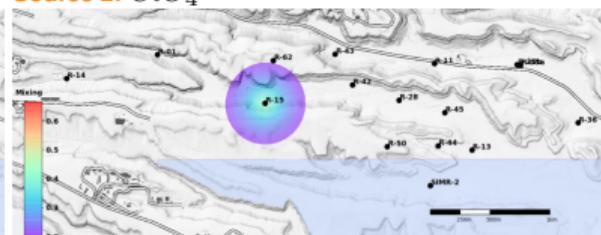
Source 4:  $NO_3$



Source 1:  $Cr$ ,  $Cl^-$ ,  $NO_3$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



Source 2:  $ClO_4$



Source 5:  $^3H$ ,  $Cr$ ,  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

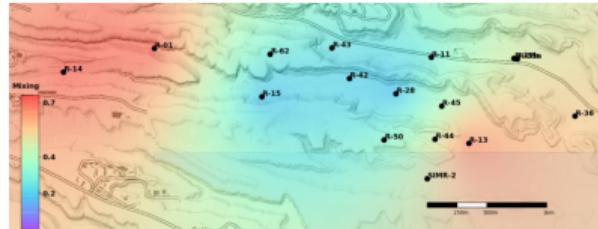


Source 6:  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

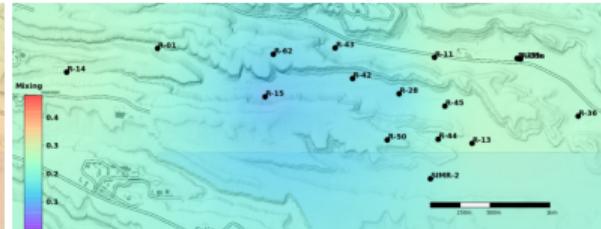


# NTF<sub>k</sub> identified sources (groundwater types) Jan-Dec 2006

Source 7: (background)



Source 3:  $Cl^-$ ,  $Ca$ ,  $Mg$  (background)



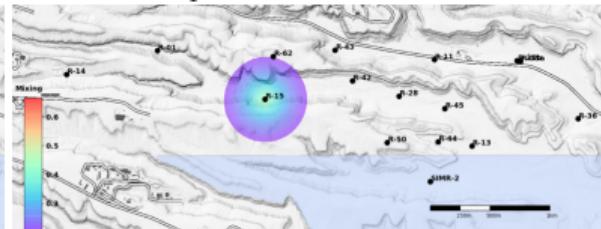
Source 4:  $NO_3$



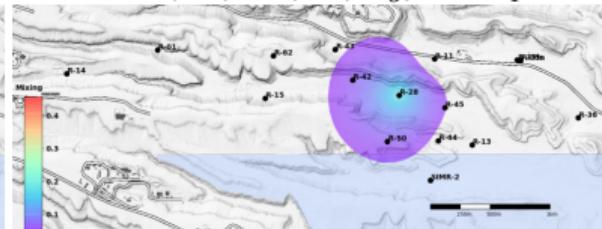
Source 1:  $Cr$ ,  $Cl^-$ ,  $NO_3$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



Source 2:  $ClO_4$



Source 5:  $^3H$ ,  $Cr$ ,  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

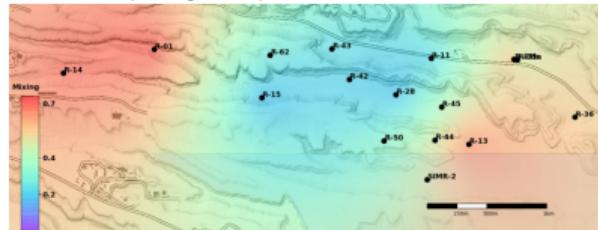


Source 6:  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

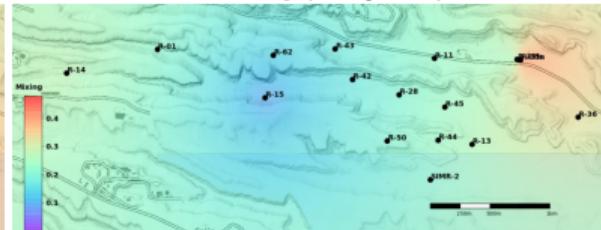


# NTF<sub>k</sub> identified sources (groundwater types) Jan-Dec 2007

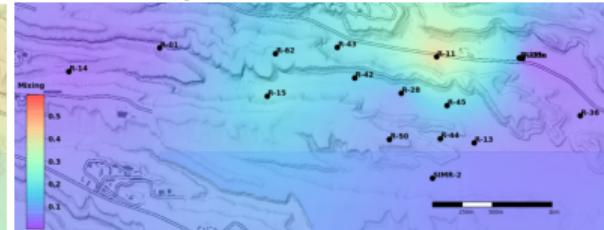
Source 7: (background)



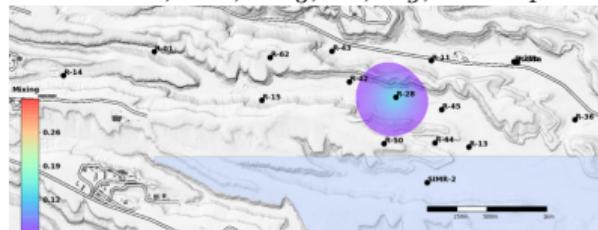
Source 3:  $Cl^-$ ,  $Ca$ ,  $Mg$  (background)



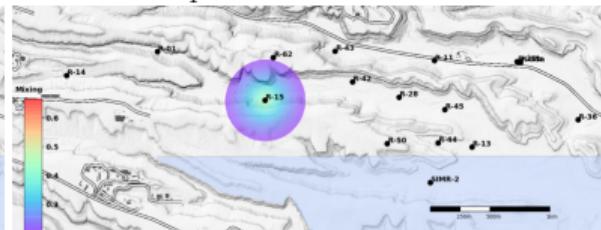
Source 4:  $NO_3$



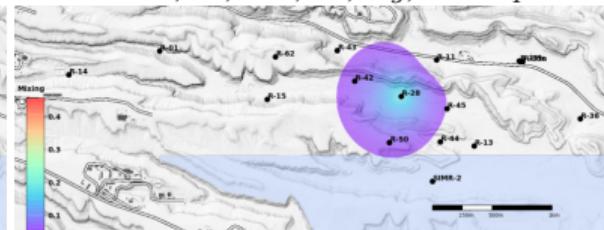
Source 1:  $Cr$ ,  $Cl^-$ ,  $NO_3$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



Source 2:  $ClO_4$



Source 5:  $^3H$ ,  $Cr$ ,  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

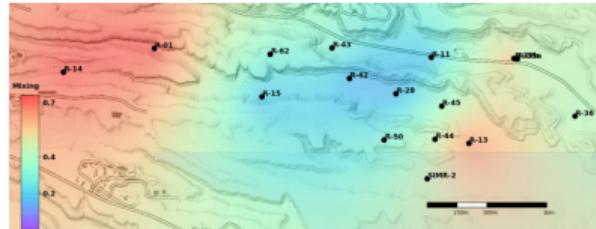


Source 6:  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

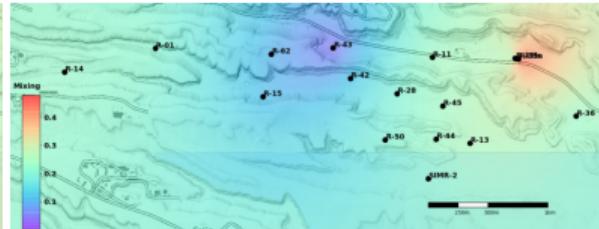


# NTF<sub>k</sub> identified sources (groundwater types) Jan-Dec 2008

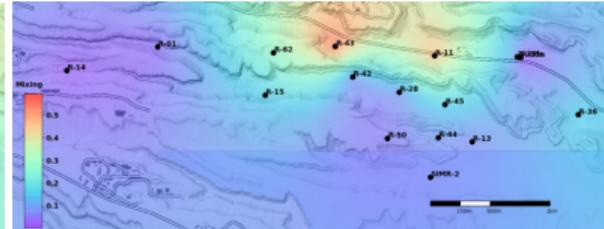
Source 7: (background)



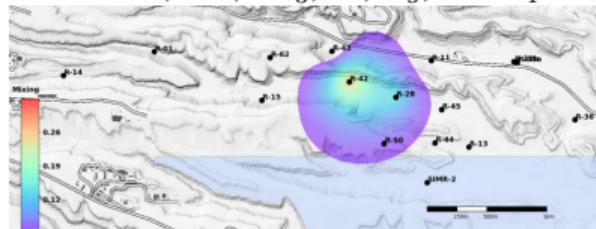
Source 3:  $Cl^-$ ,  $Ca$ ,  $Mg$  (background)



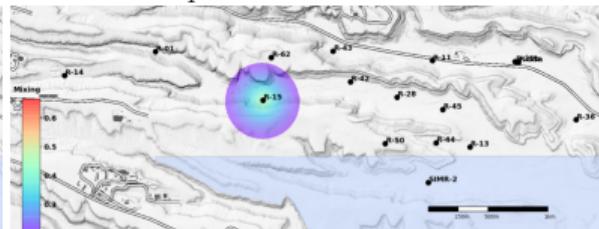
Source 4:  $NO_3$



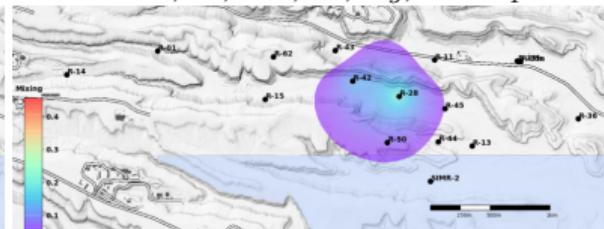
Source 1:  $Cr$ ,  $Cl^-$ ,  $NO_3$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



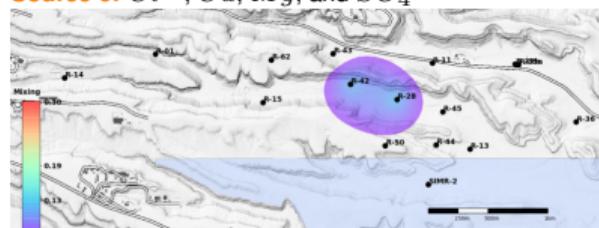
Source 2:  $ClO_4$



Source 5:  $^3H$ ,  $Cr$ ,  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

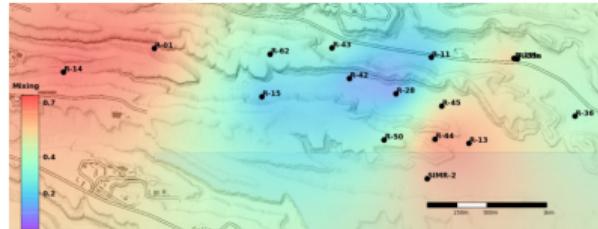


Source 6:  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

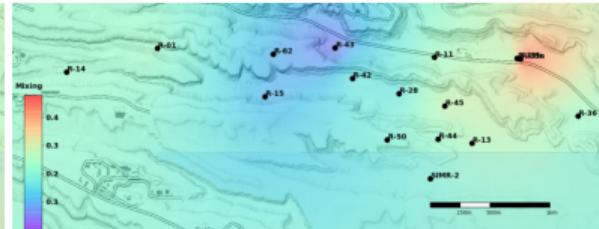


# NTF<sub>k</sub> identified sources (groundwater types) Jan-Dec 2009

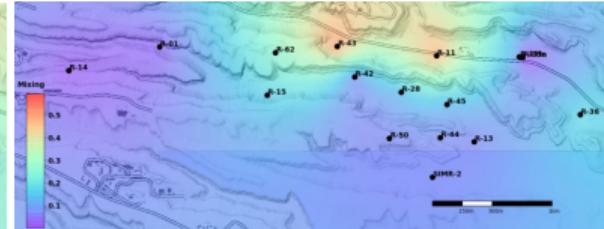
Source 7: (background)



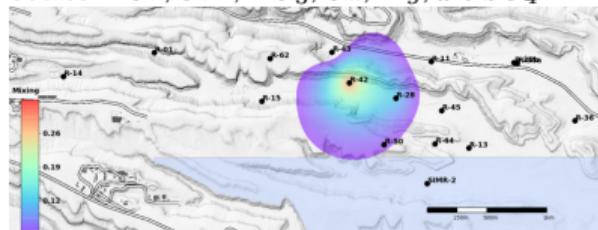
Source 3:  $Cl^-$ ,  $Ca$ ,  $Mg$  (background)



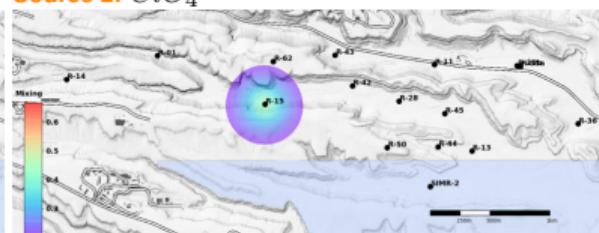
Source 4:  $NO_3$



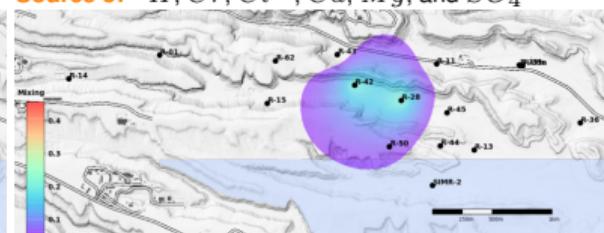
Source 1:  $Cr$ ,  $Cl^-$ ,  $NO_3$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



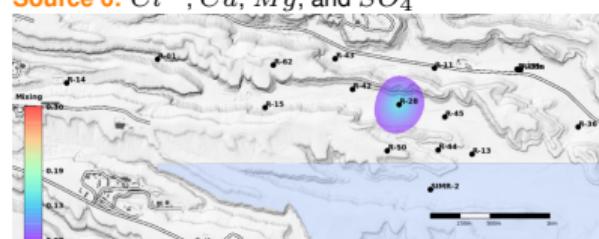
Source 2:  $ClO_4$



Source 5:  $^3H$ ,  $Cr$ ,  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

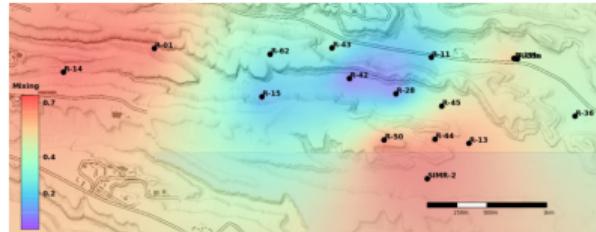


Source 6:  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

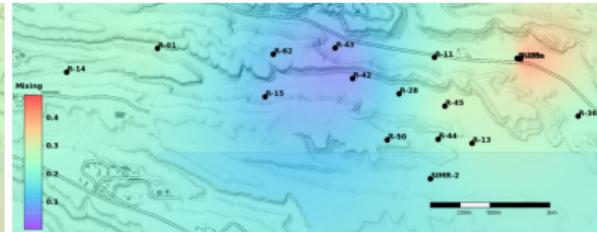


# NTF<sub>k</sub> identified sources (groundwater types) Jan-Dec 2010

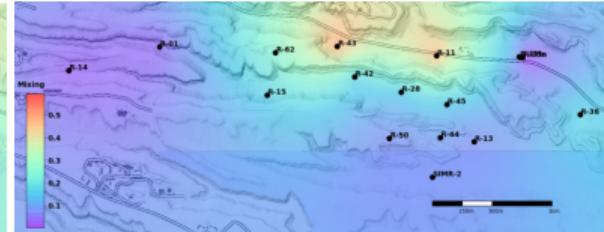
Source 7: (background)



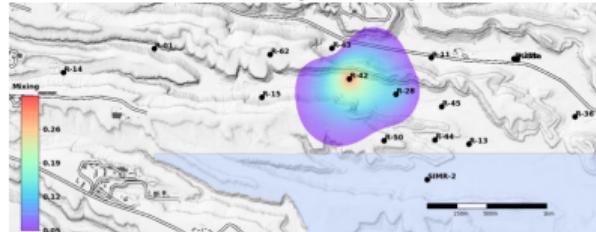
Source 3:  $Cl^-$ ,  $Ca$ ,  $Mg$  (background)



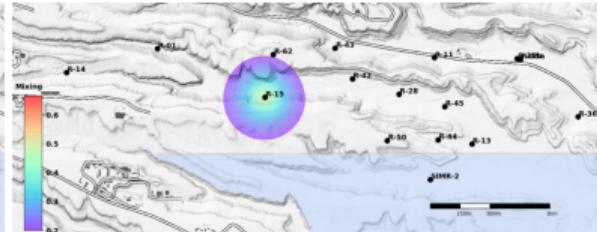
Source 4:  $NO_3$



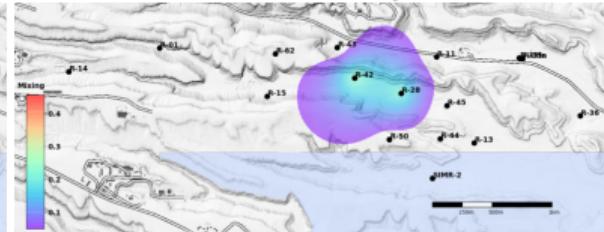
Source 1:  $Cr$ ,  $Cl^-$ ,  $NO_3$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



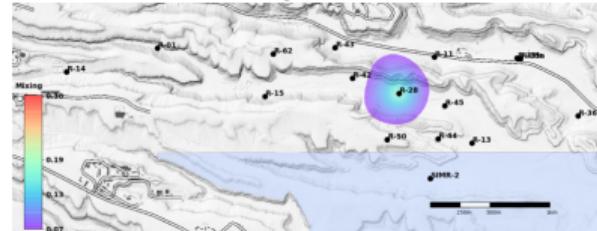
Source 2:  $ClO_4$



Source 5:  $^3H$ ,  $Cr$ ,  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

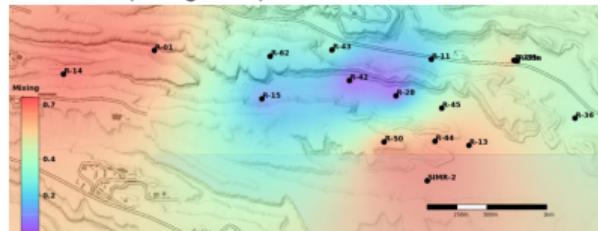


Source 6:  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



# NTF<sub>k</sub> identified sources (groundwater types) Jan-Dec 2011

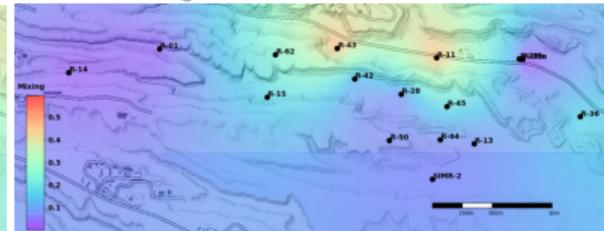
Source 7: (background)



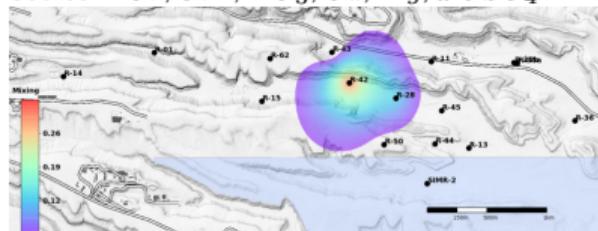
Source 3:  $Cl^-$ ,  $Ca$ ,  $Mg$  (background)



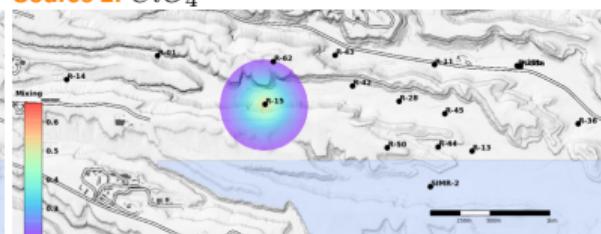
Source 4:  $NO_3$



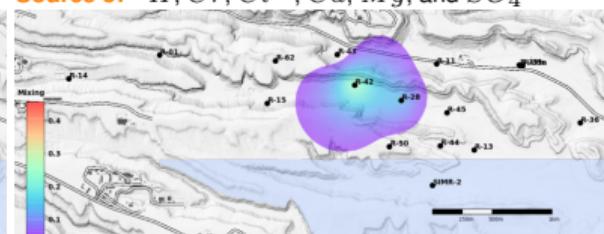
Source 1:  $Cr$ ,  $Cl^-$ ,  $NO_3$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



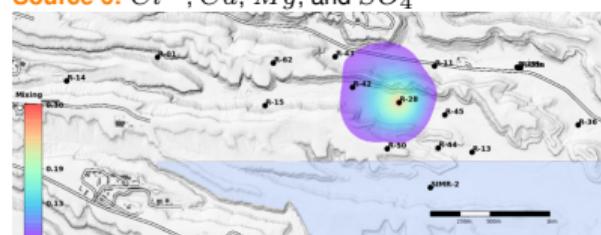
Source 2:  $ClO_4$



Source 5:  $^3H$ ,  $Cr$ ,  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

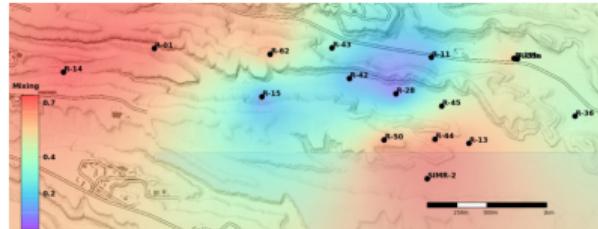


Source 6:  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

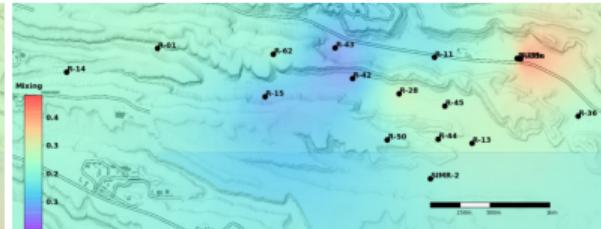


# NTF<sub>k</sub> identified sources (groundwater types) Jan-Dec 2012

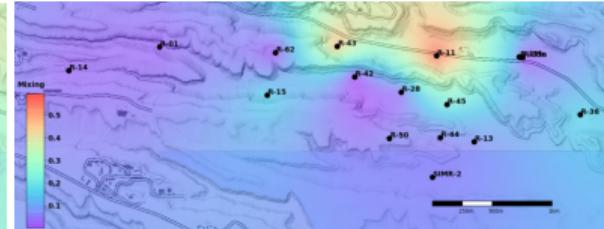
Source 7: (background)



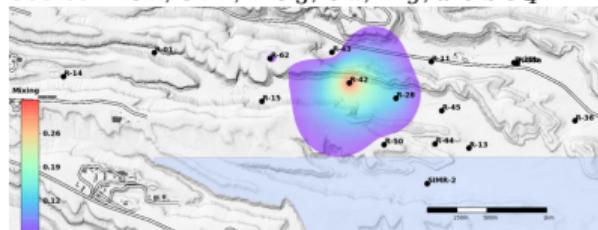
Source 3:  $Cl^-$ ,  $Ca$ ,  $Mg$  (background)



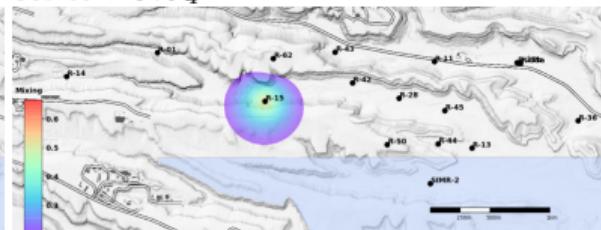
Source 4:  $NO_3$



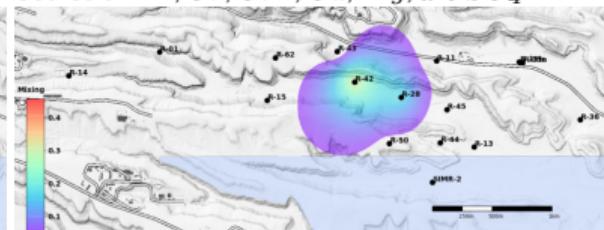
Source 1:  $Cr$ ,  $Cl^-$ ,  $NO_3$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



Source 2:  $ClO_4$



Source 5:  $^3H$ ,  $Cr$ ,  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

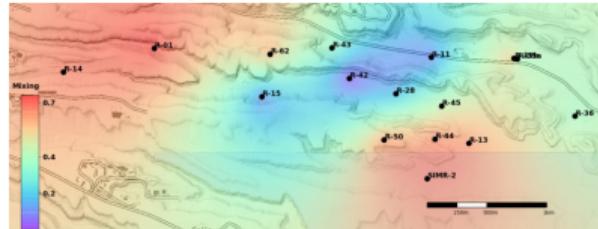


Source 6:  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

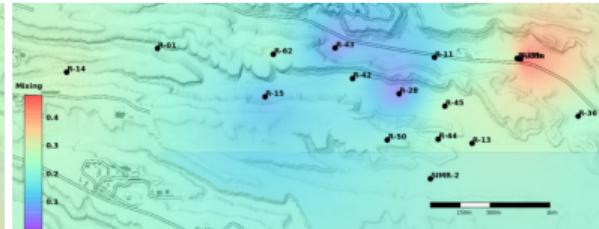


# NTF<sub>k</sub> identified sources (groundwater types) Jan-Dec 2013

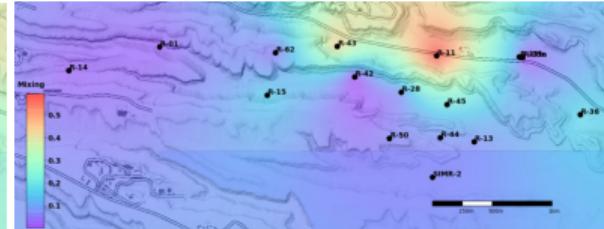
Source 7: (background)



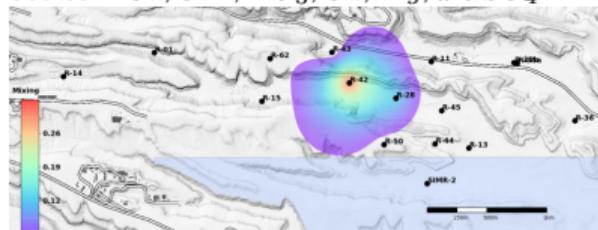
Source 3:  $Cl^-$ ,  $Ca$ ,  $Mg$  (background)



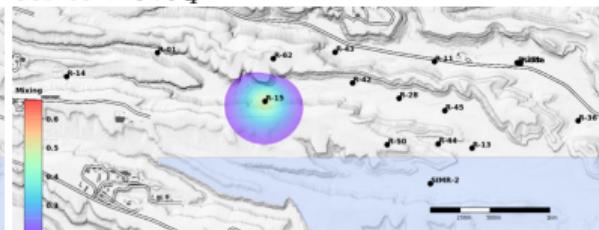
Source 4:  $NO_3$



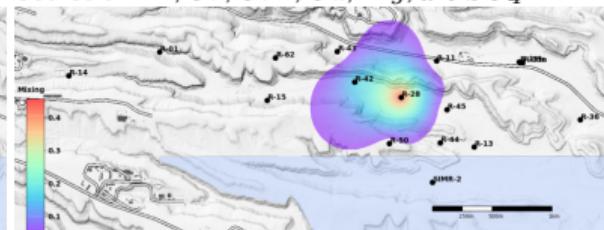
Source 1:  $Cr$ ,  $Cl^-$ ,  $NO_3$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



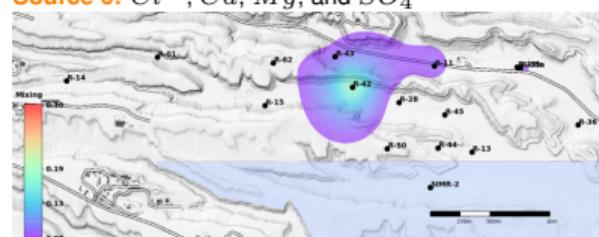
Source 2:  $ClO_4$



Source 5:  $^3H$ ,  $Cr$ ,  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

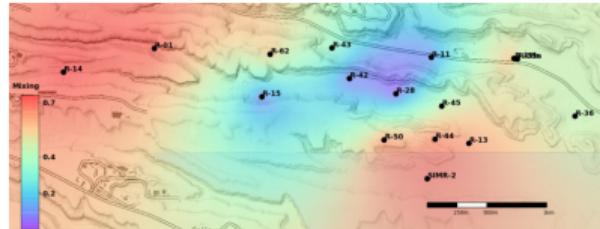


Source 6:  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

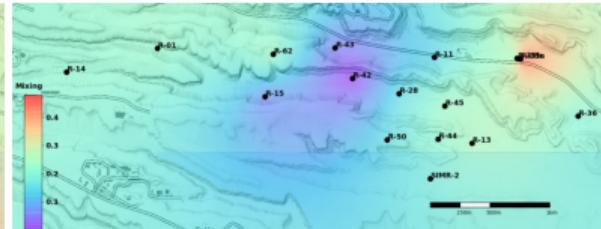


# NTF<sub>k</sub> identified sources (groundwater types) Jan-Dec 2014

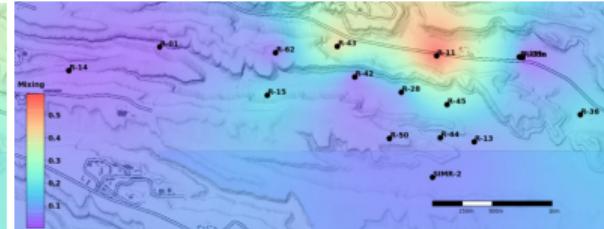
Source 7: (background)



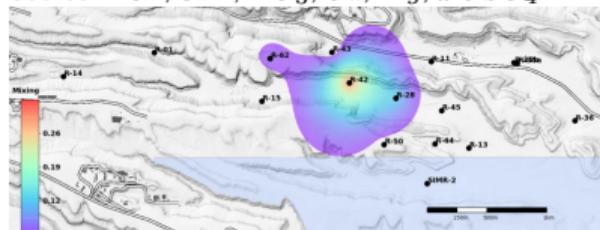
Source 3:  $Cl^-$ ,  $Ca$ ,  $Mg$  (background)



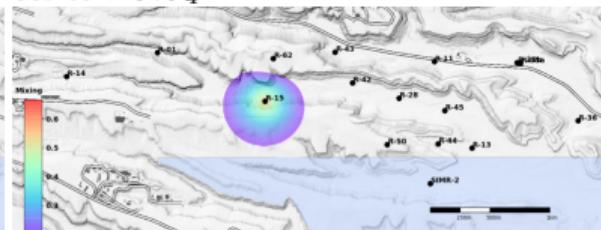
Source 4:  $NO_3$



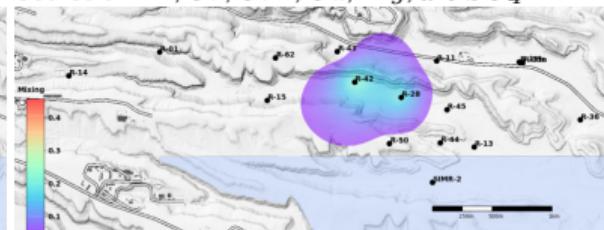
Source 1:  $Cr$ ,  $Cl^-$ ,  $NO_3$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



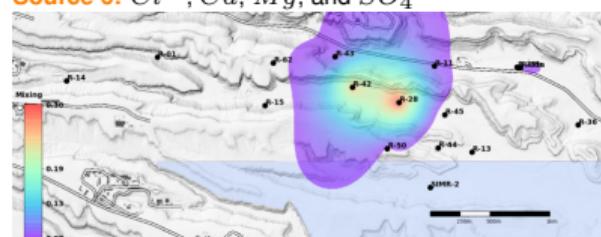
Source 2:  $ClO_4$



Source 5:  $^3H$ ,  $Cr$ ,  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

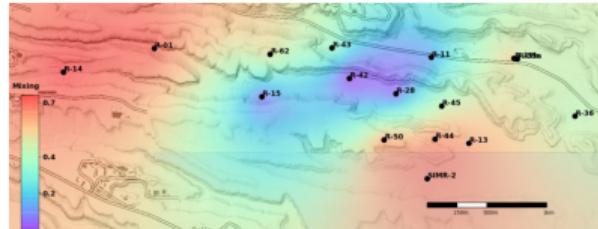


Source 6:  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

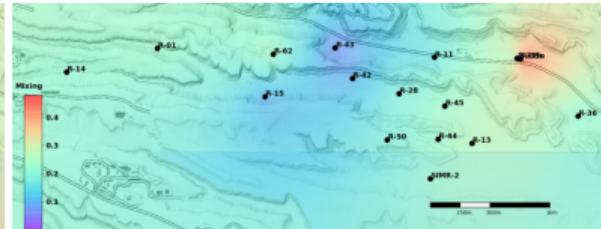


# NTF<sub>k</sub> identified sources (groundwater types) Jan-Dec 2015

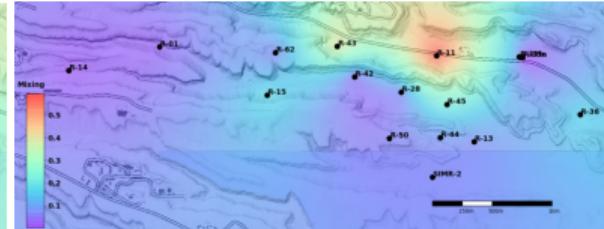
Source 7: (background)



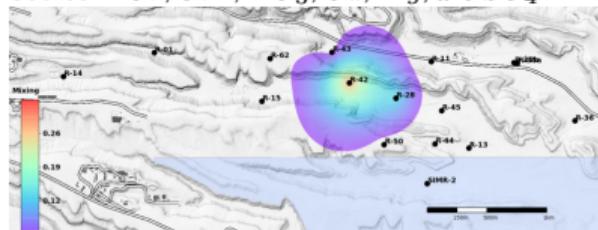
Source 3:  $Cl^-$ ,  $Ca$ ,  $Mg$  (background)



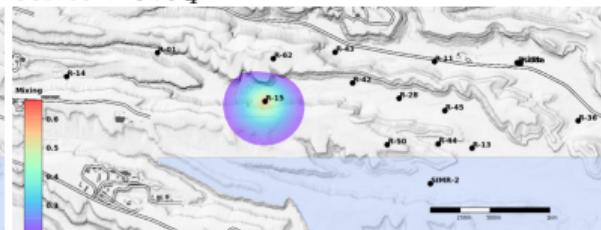
Source 4:  $NO_3$



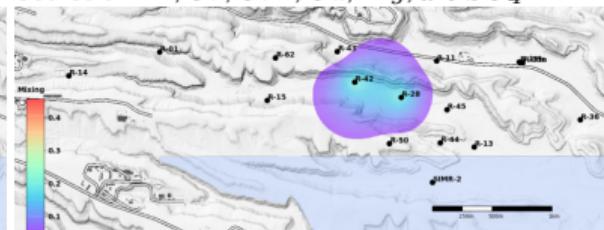
Source 1:  $Cr$ ,  $Cl^-$ ,  $NO_3$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



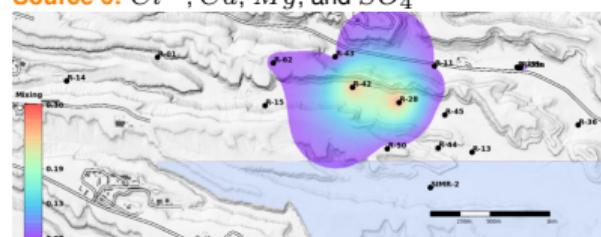
Source 2:  $ClO_4$



Source 5:  $^3H$ ,  $Cr$ ,  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

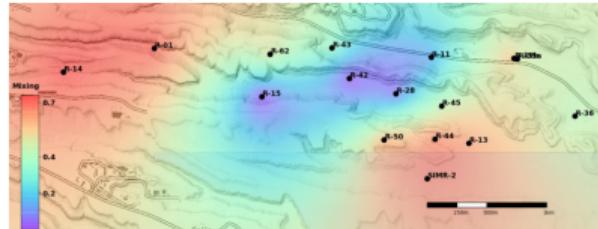


Source 6:  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$

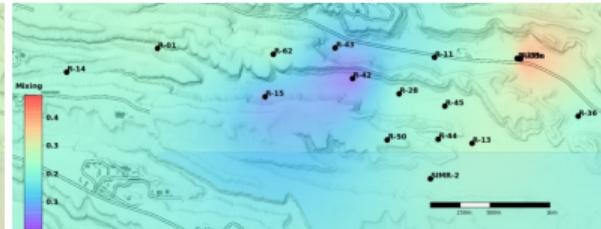


# NTF<sub>k</sub> identified sources (groundwater types) Jan-Dec 2016

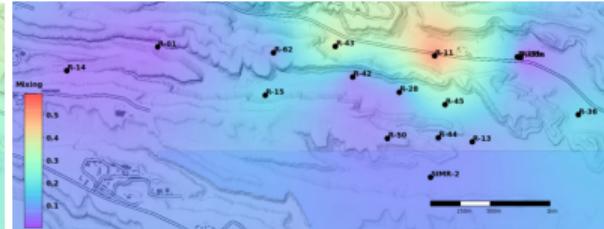
Source 7: (background)



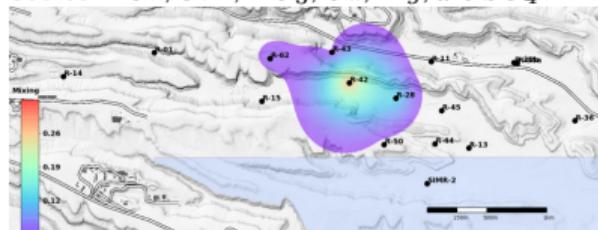
Source 3:  $Cl^-$ ,  $Ca$ ,  $Mg$  (background)



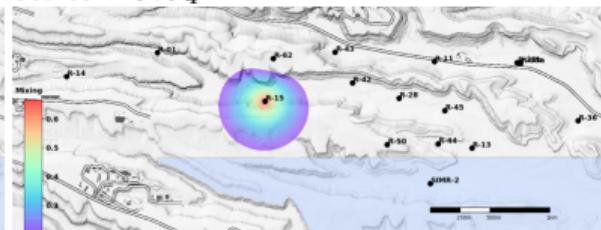
Source 4:  $NO_3$



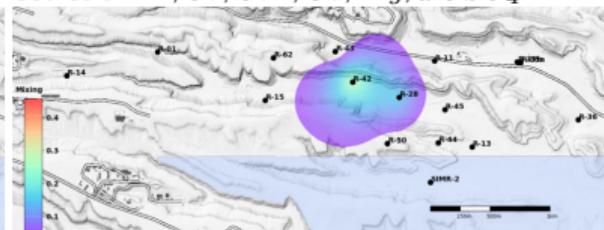
Source 1:  $Cr$ ,  $Cl^-$ ,  $NO_3$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



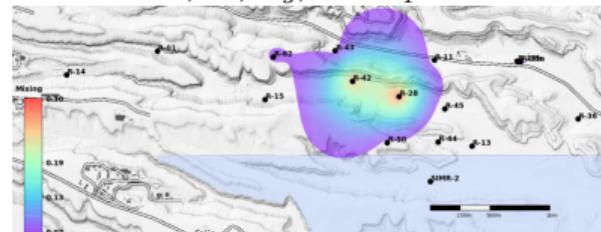
Source 2:  $ClO_4$



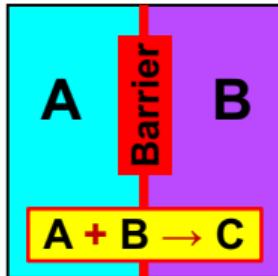
Source 5:  $^3H$ ,  $Cr$ ,  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



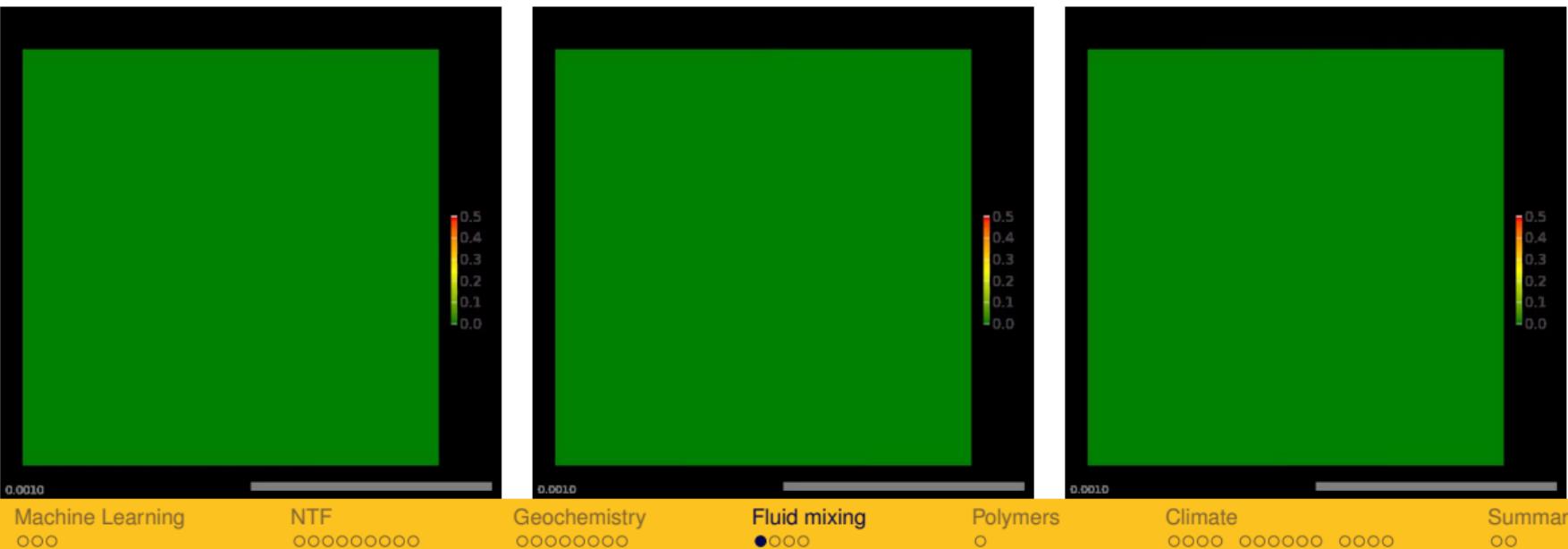
Source 6:  $Cl^-$ ,  $Ca$ ,  $Mg$ , and  $SO_4$



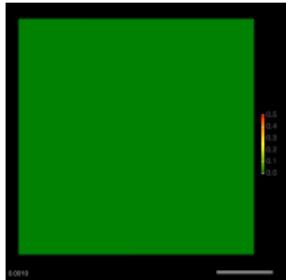
## Fluid mixing



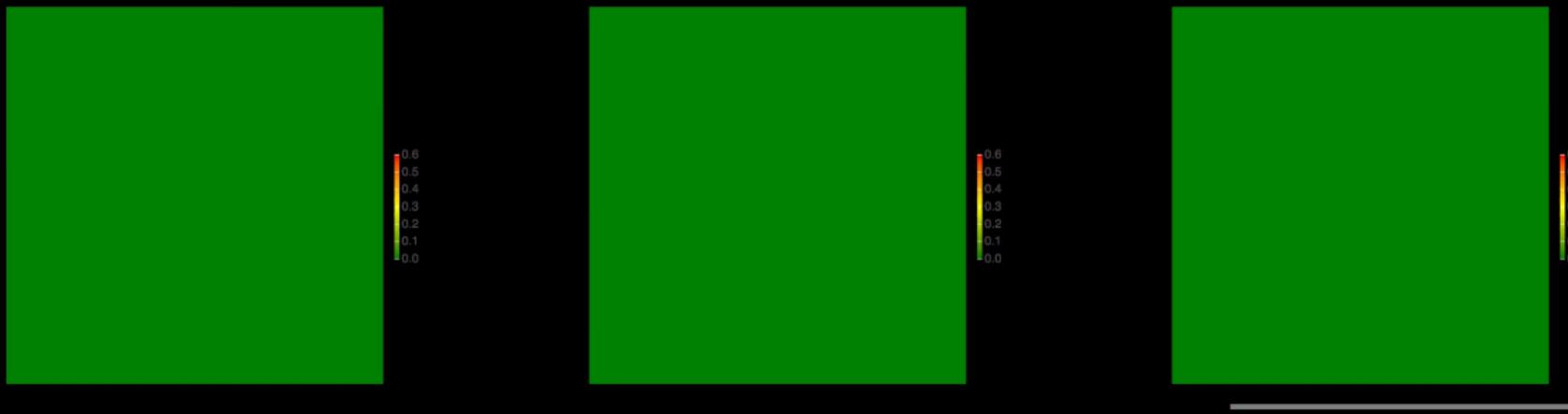
- ▶ We want to find how time/space behavior of  $C$  concentrations is controlled by the simulated physics processes
- ▶ > 2000 simulations of  $C$  concentrations in time/space for a series of model parameters impacting fluid mixing; 3 example predictions:



## NTF<sub>k</sub> results



- ▶ > 200 GB simulation data compressed to  $\approx 70$  MB (compression  $\approx 4 \times 10^{-4}$ )  
Here,  $(1000 \times 81 \times 81) \rightarrow (3 \times 12 \times 13)$
- ▶ NTF<sub>k</sub> processed all the data and extracted the dominant time/space features (**processes / vortices**)



### Advection

Machine Learning  
○○○

NTF  
○○○○○○○○○○

Geochemistry  
○○○○○○○○

### Dispersion

Fluid mixing  
○●○○

Polymers  
○

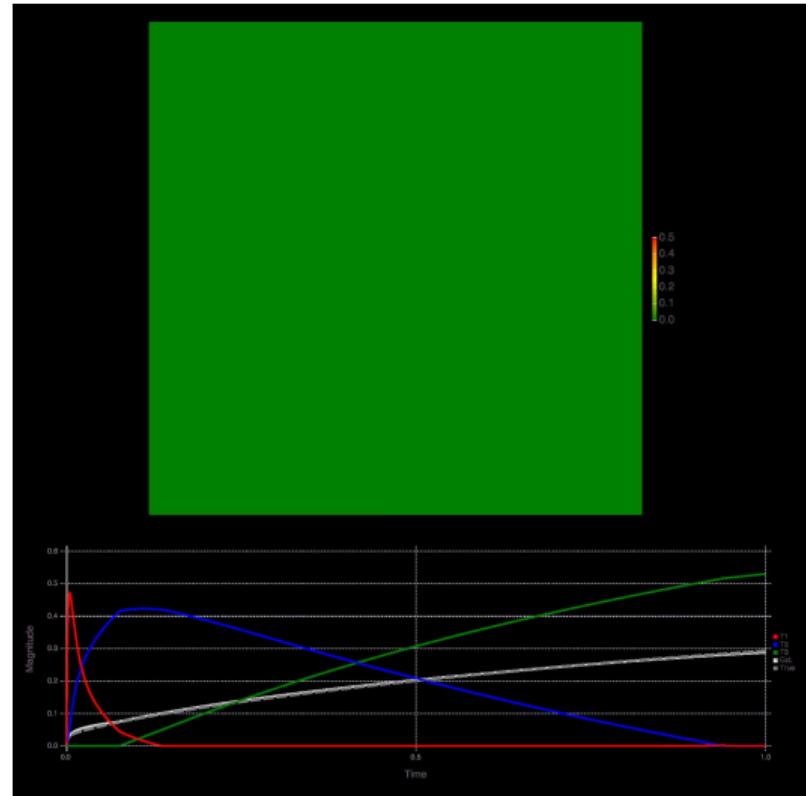
Climate  
○○○ ○○○○○ ○○○○

### Diffusion

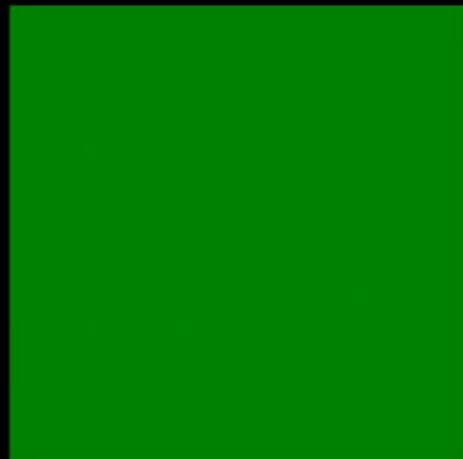
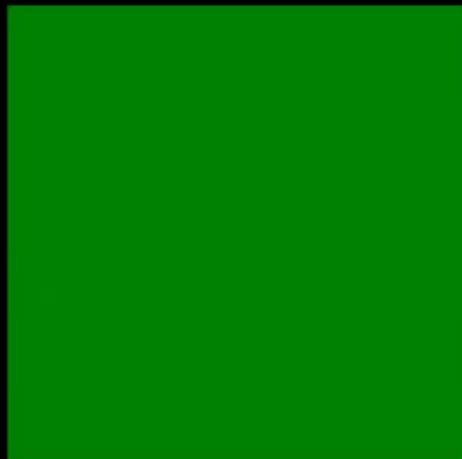
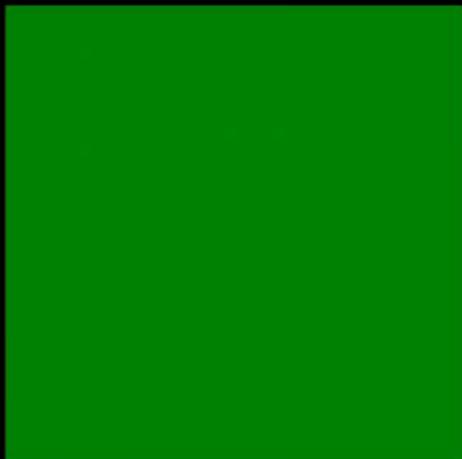
Summary  
○○

# NTF<sub>k</sub> results

- ▶ T1: Advection
- ▶ T2: Dispersion
- ▶ T3: Diffusion



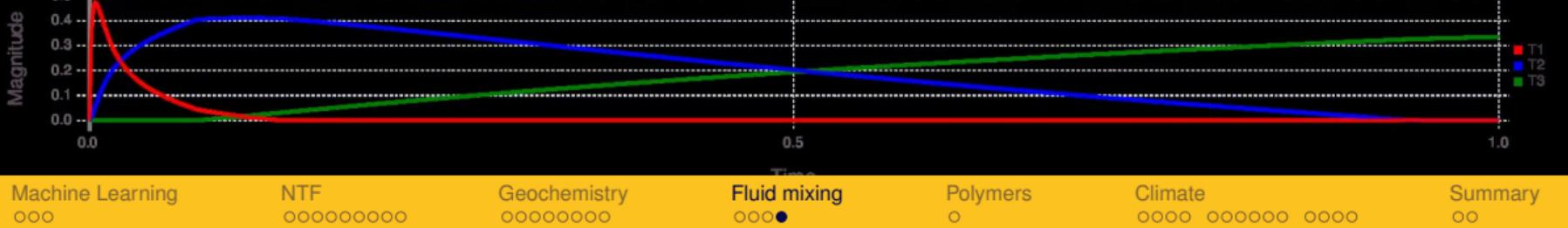
# NTF<sub>k</sub> results



0.6  
0.5  
0.4  
0.3  
0.2  
0.1  
0.0

T1  
T2  
T3

1.0



Machine Learning  
○○○

NTF  
○○○○○○○○○○

Geochemistry  
○○○○○○○○

Fluid mixing  
○○○●

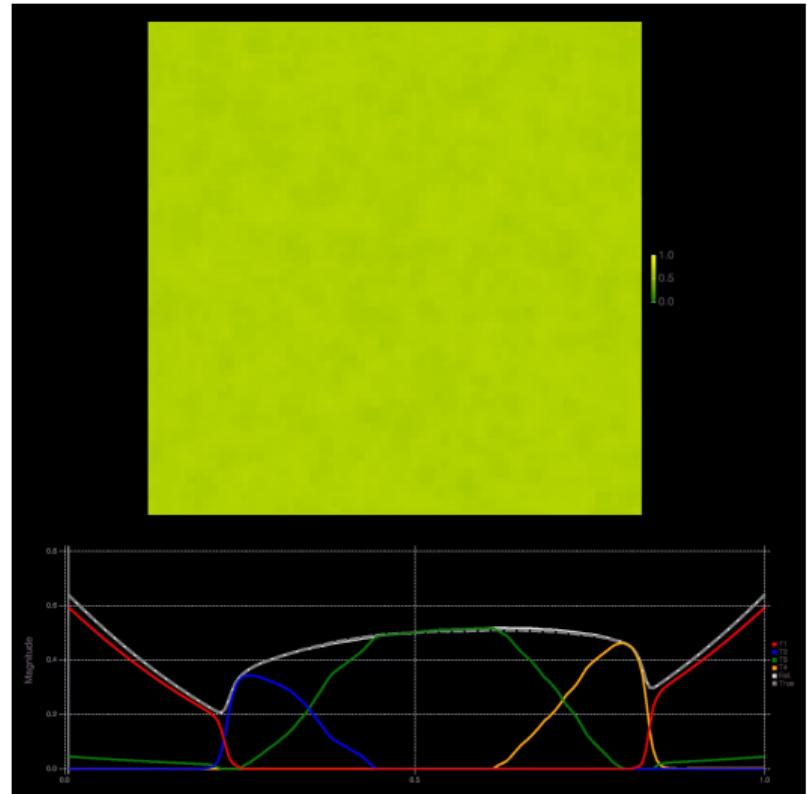
Polymers  
○

Climate  
○○○○ ○○○○○○ ○○○○

Summary  
○○

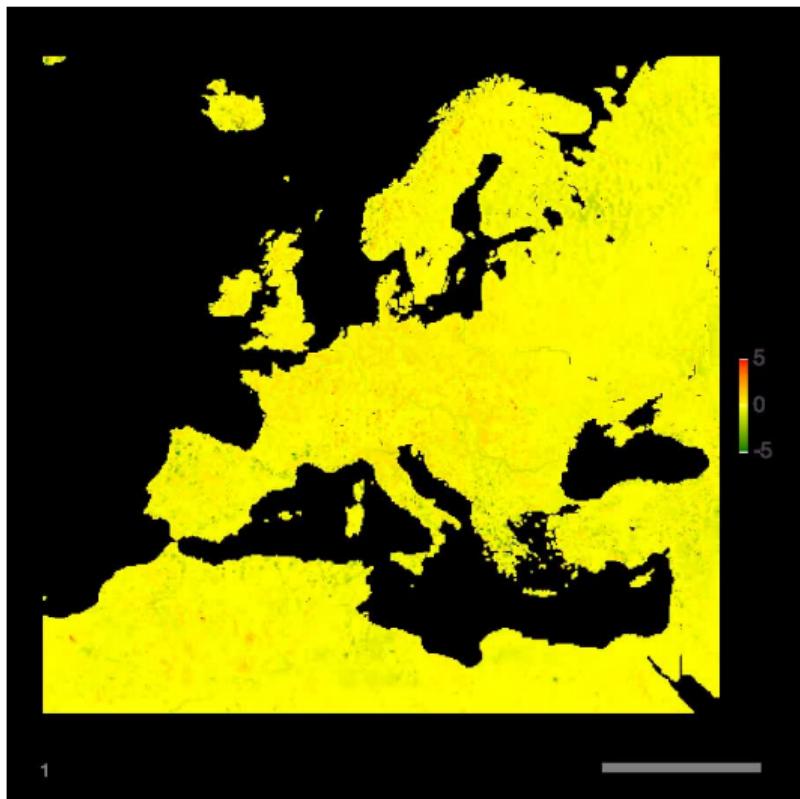
# Polymer-chain folding

- ▶ polymer transitions between different states
- ▶ **NTF<sub>k</sub>** extracts phase-transition stages
- ▶  $(201 \times 64 \times 64 \times 3) \rightarrow (5 \times 12 \times 12 \times 1)$

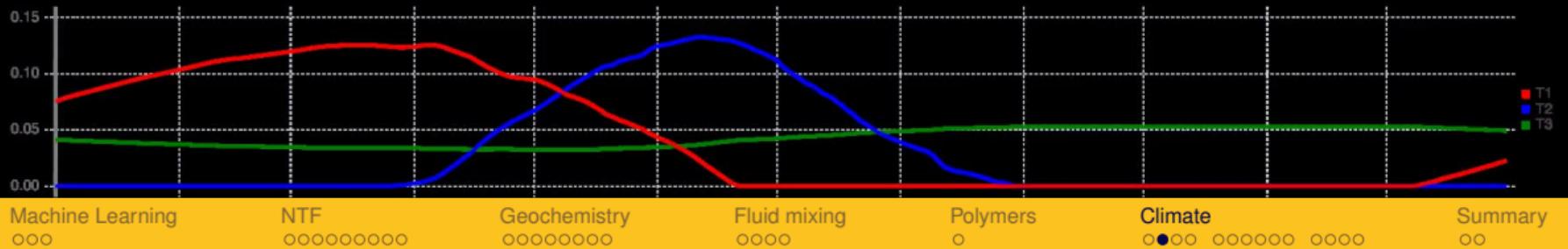


# Climate model of Europe: water-table fluctuations

- ▶ fluctuations in the water-table levels
- ▶ **NTF<sub>k</sub>** extracts seasonal changes and dominant infiltration signals
- ▶  $(424 \times 412 \times 365) \rightarrow (? \times ? \times ?)$

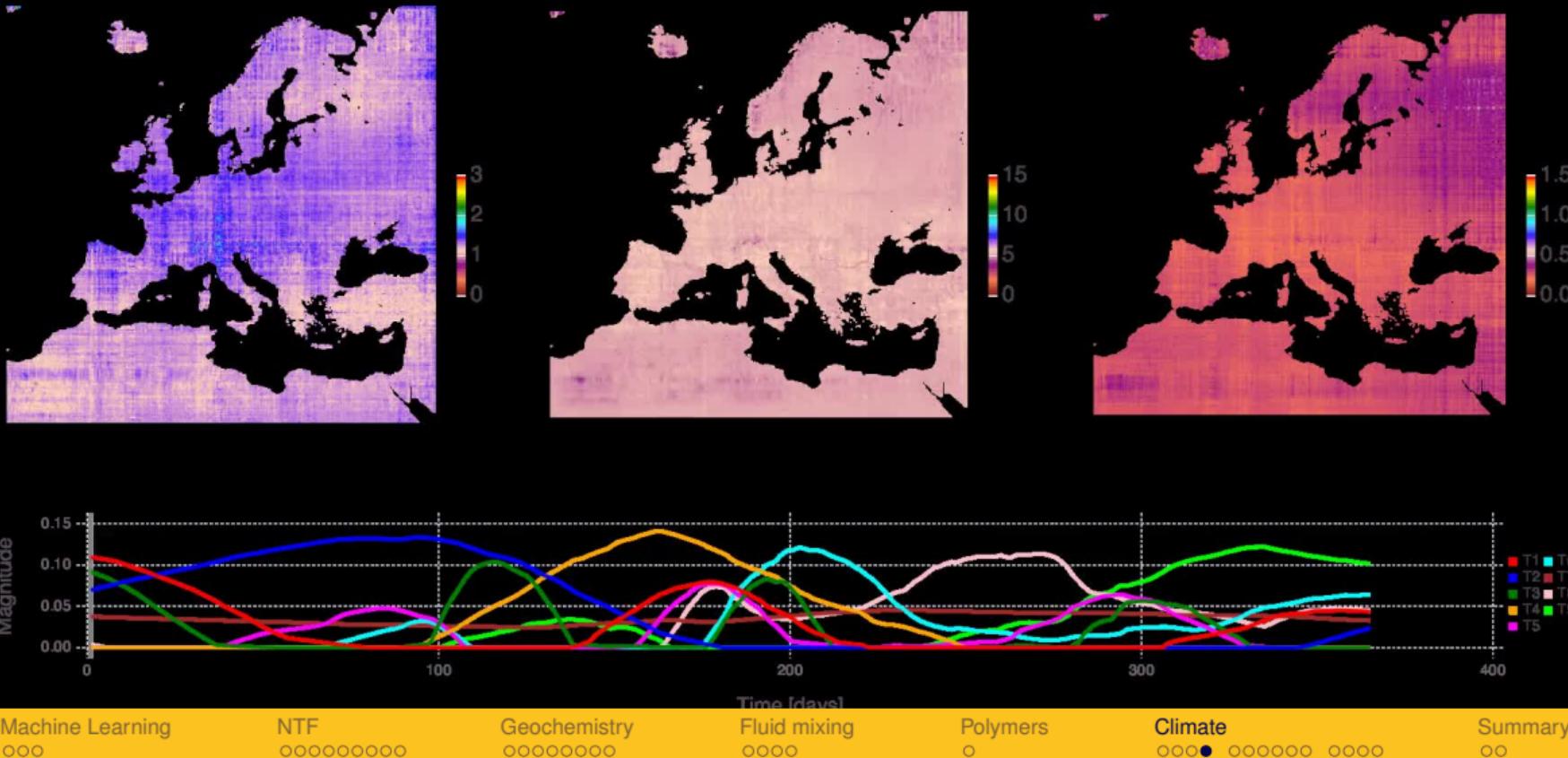


# Climate model of Europe: water-table fluctuations represented by 3 signals

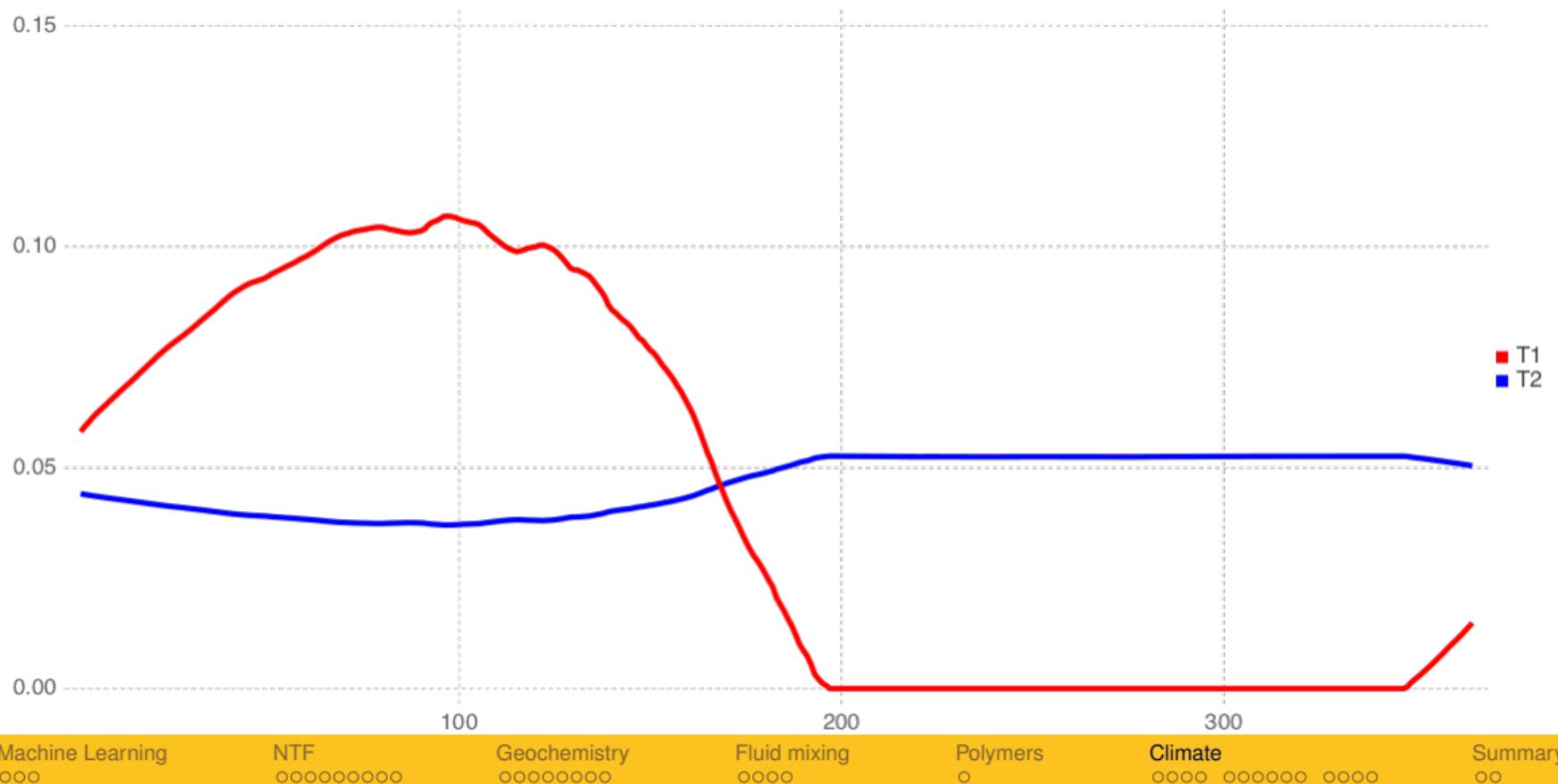




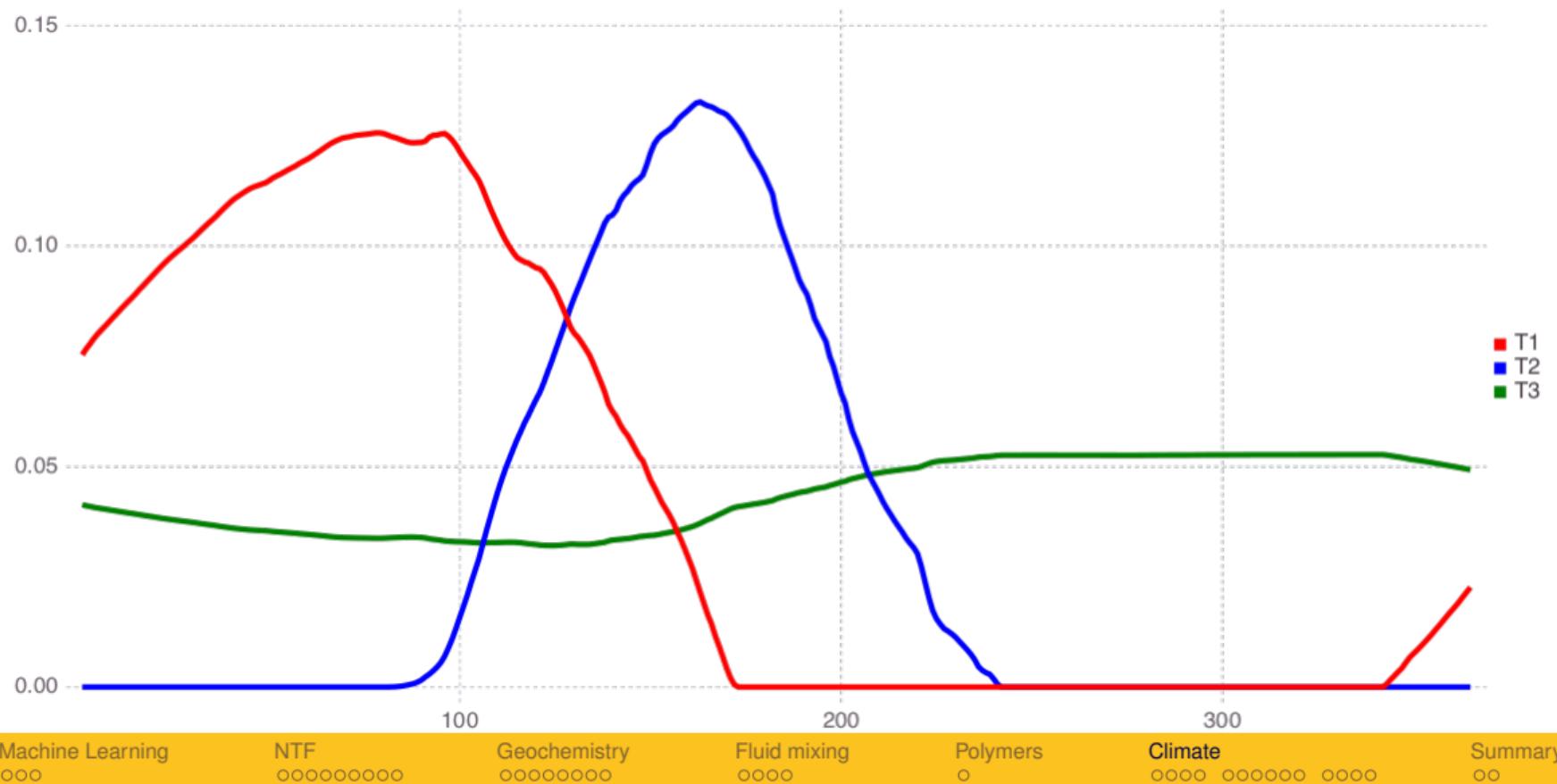
# Climate model of Europe: water-table fluctuations represented by 9 signals



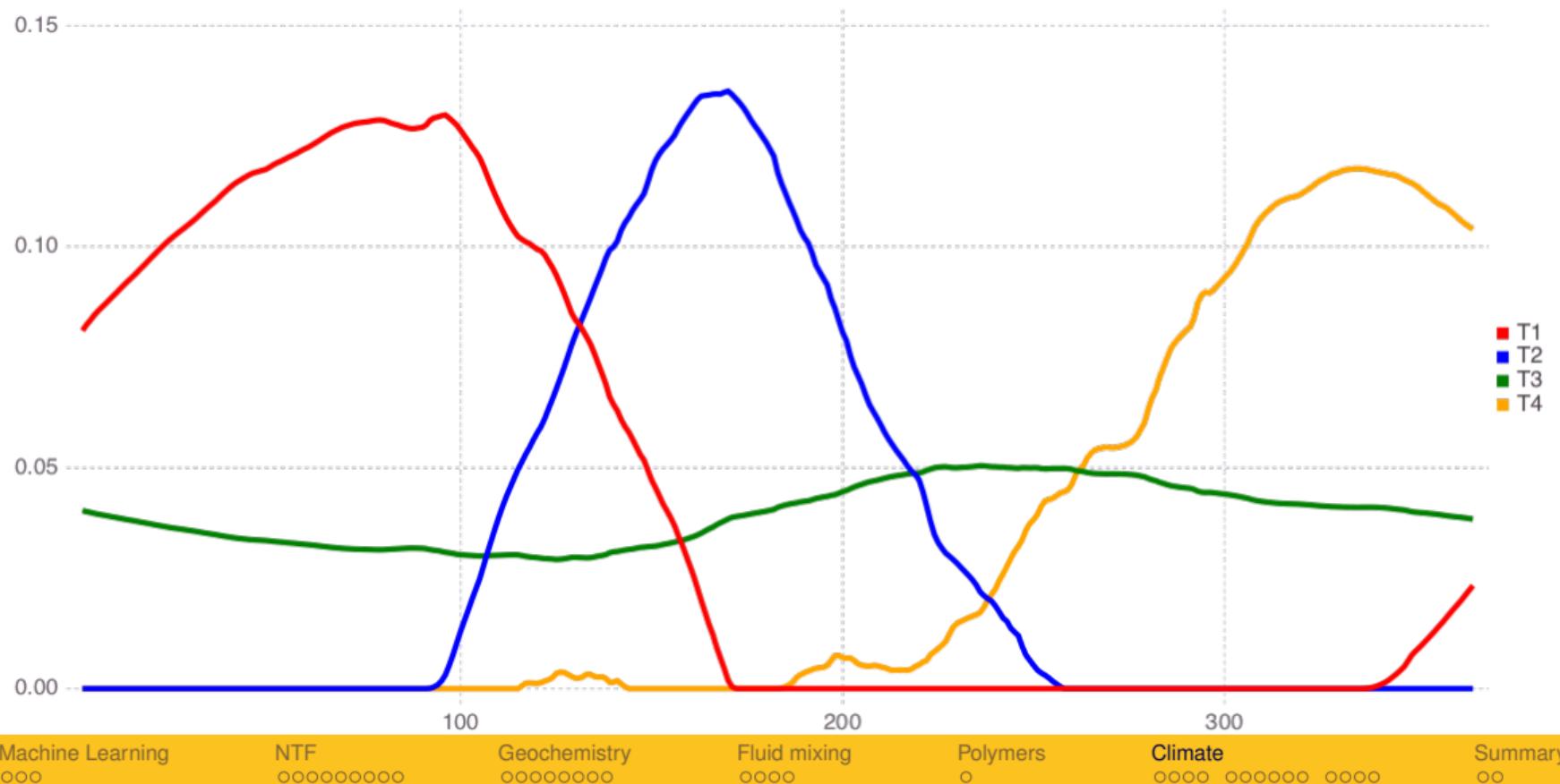
# Climate model of Europe: Water-table fluctuations represented by 2 signals



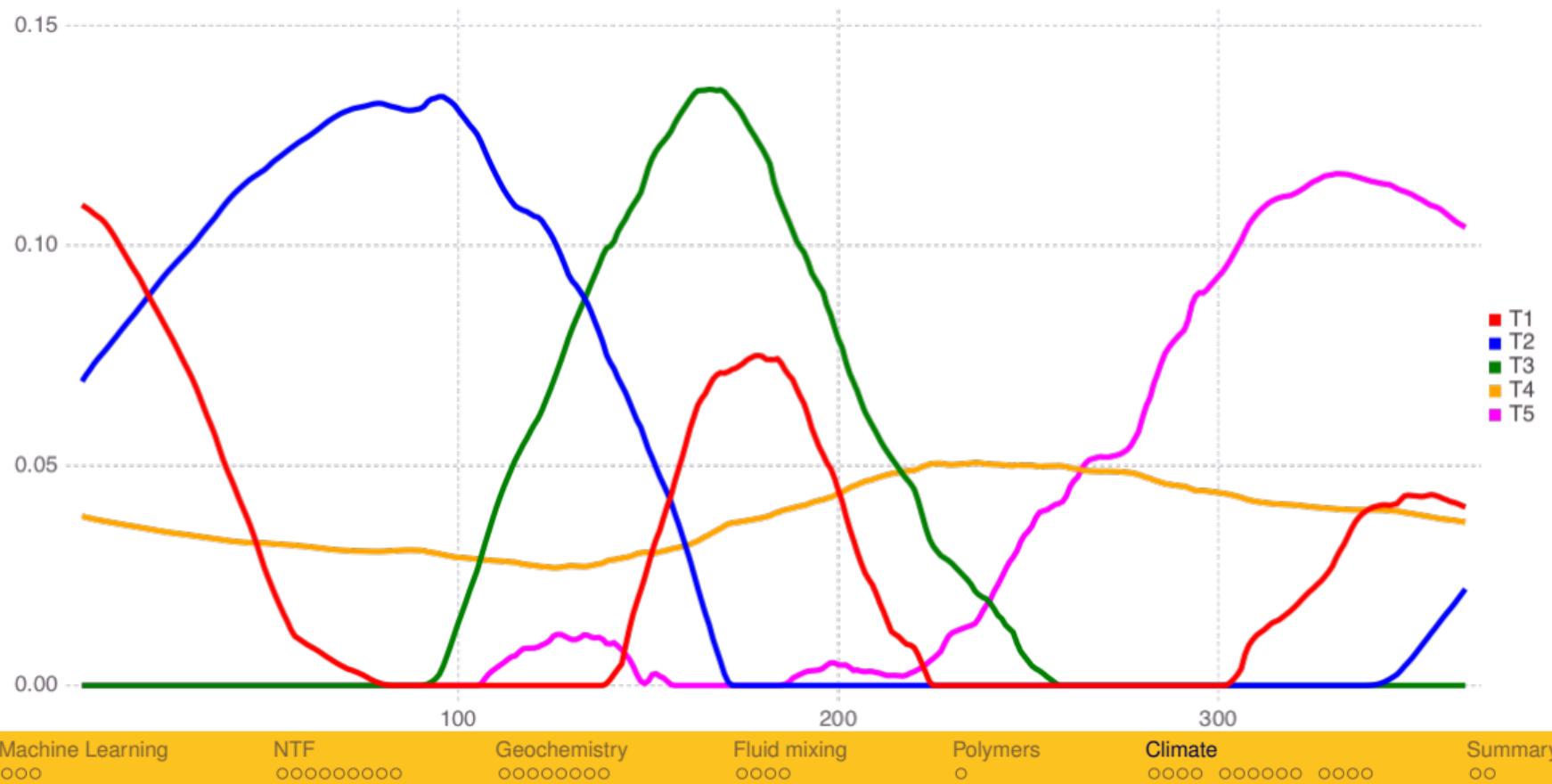
# Climate model of Europe: Water-table fluctuations represented by 3 signals



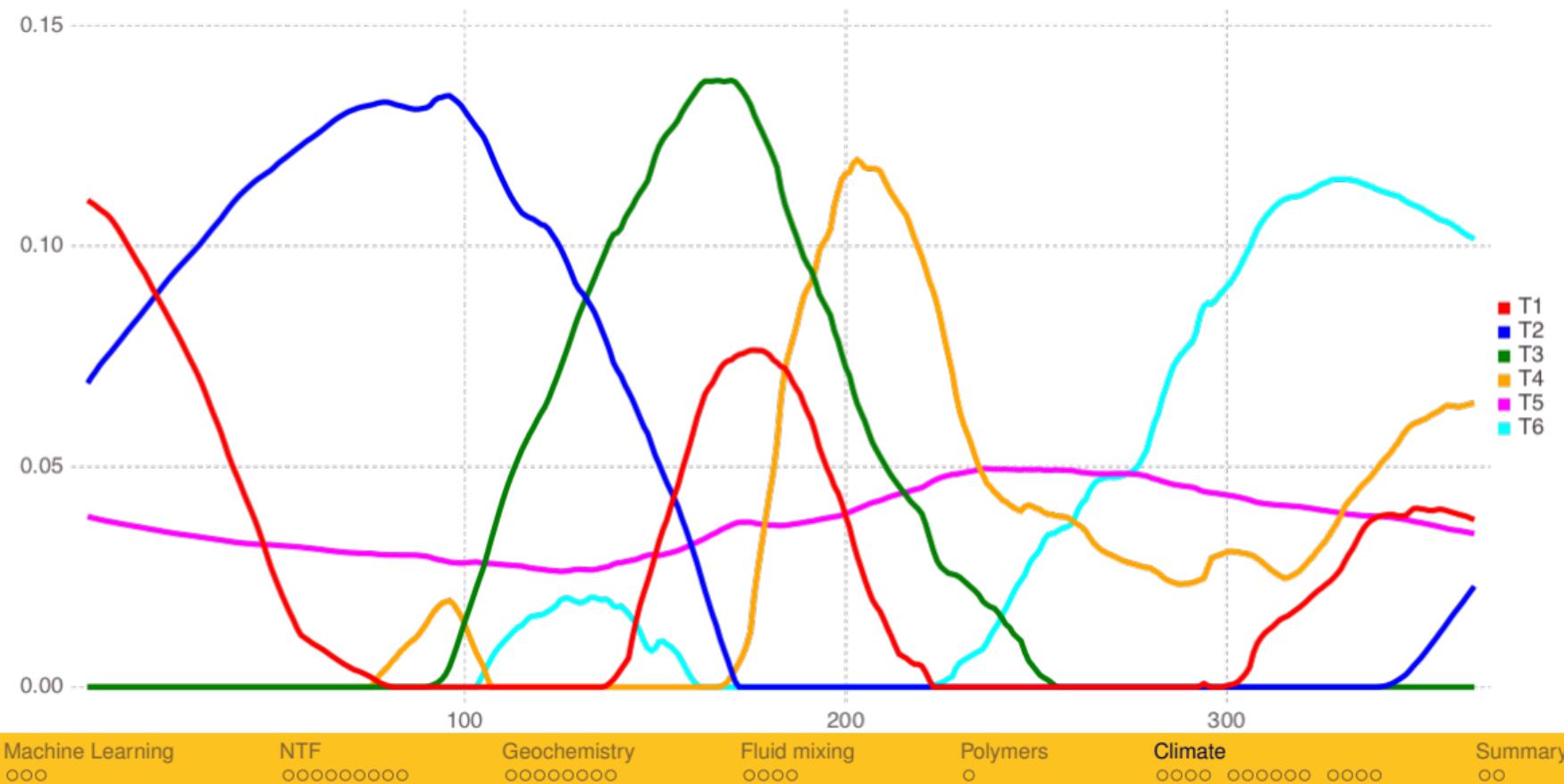
# Climate model of Europe: Water-table fluctuations represented by 4 signals



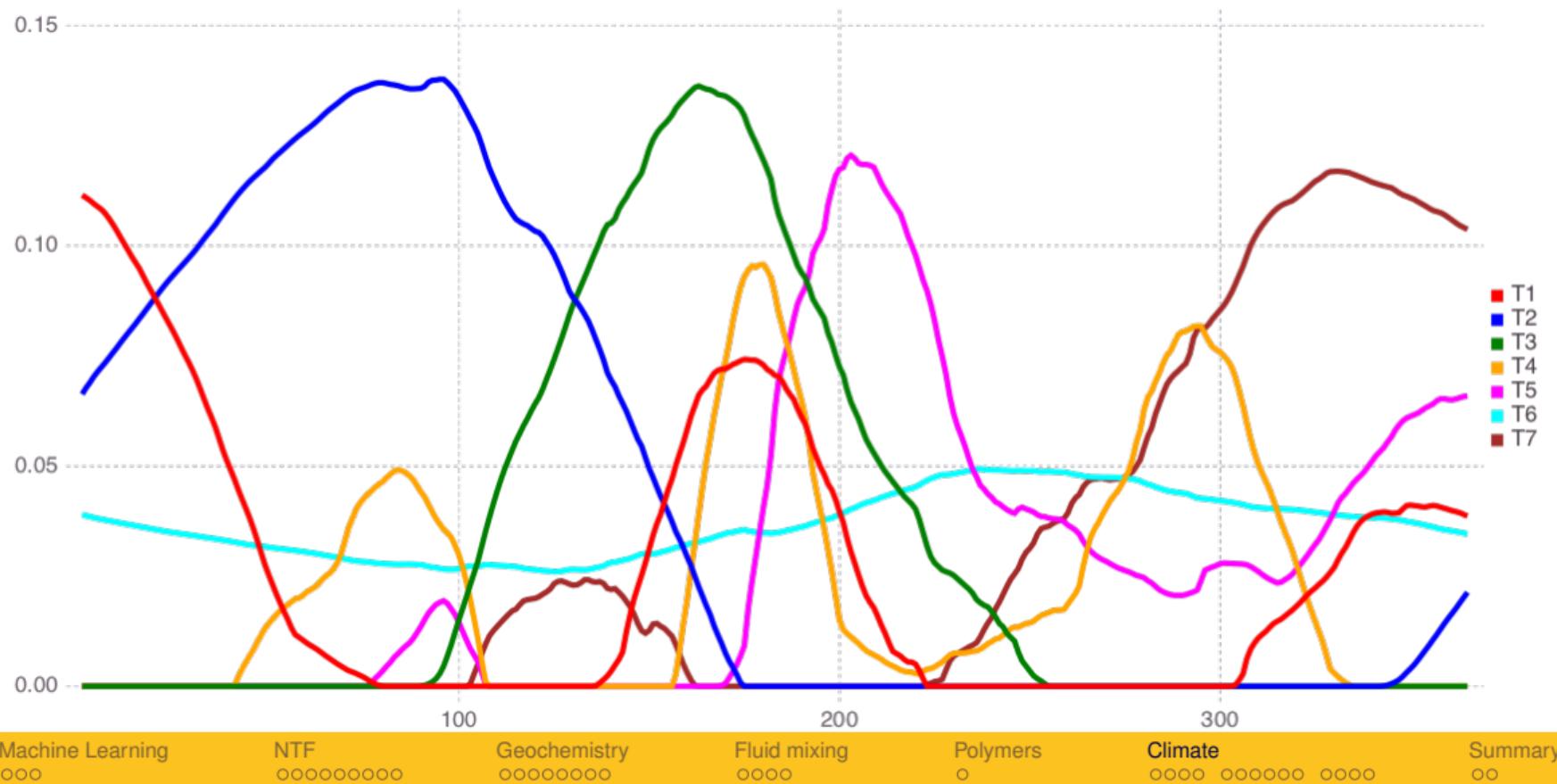
# Climate model of Europe: Water-table fluctuations represented by 5 signals



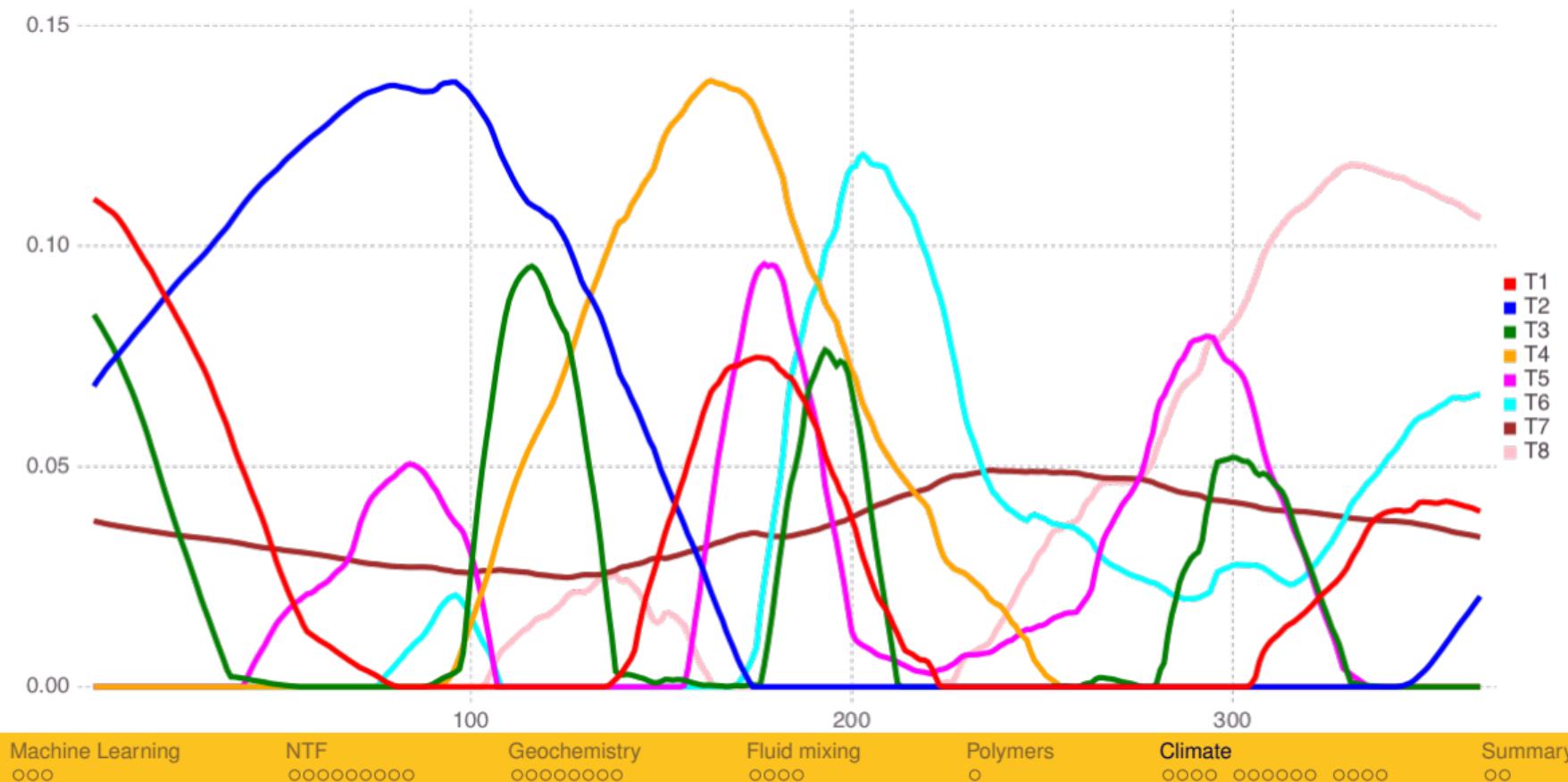
# Climate model of Europe: Water-table fluctuations represented by 6 signals



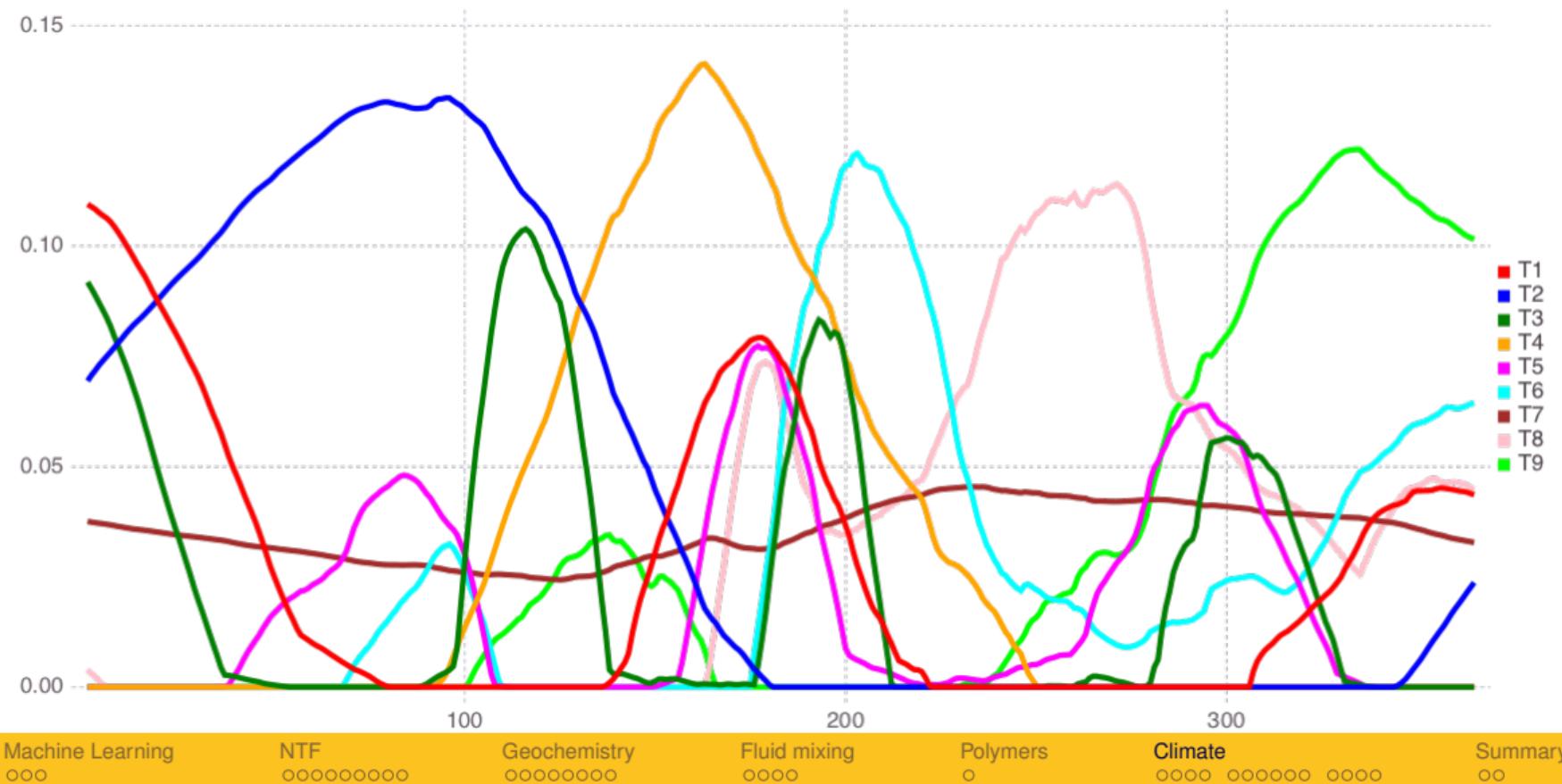
## Climate model of Europe: Water-table fluctuations represented by 7 signals



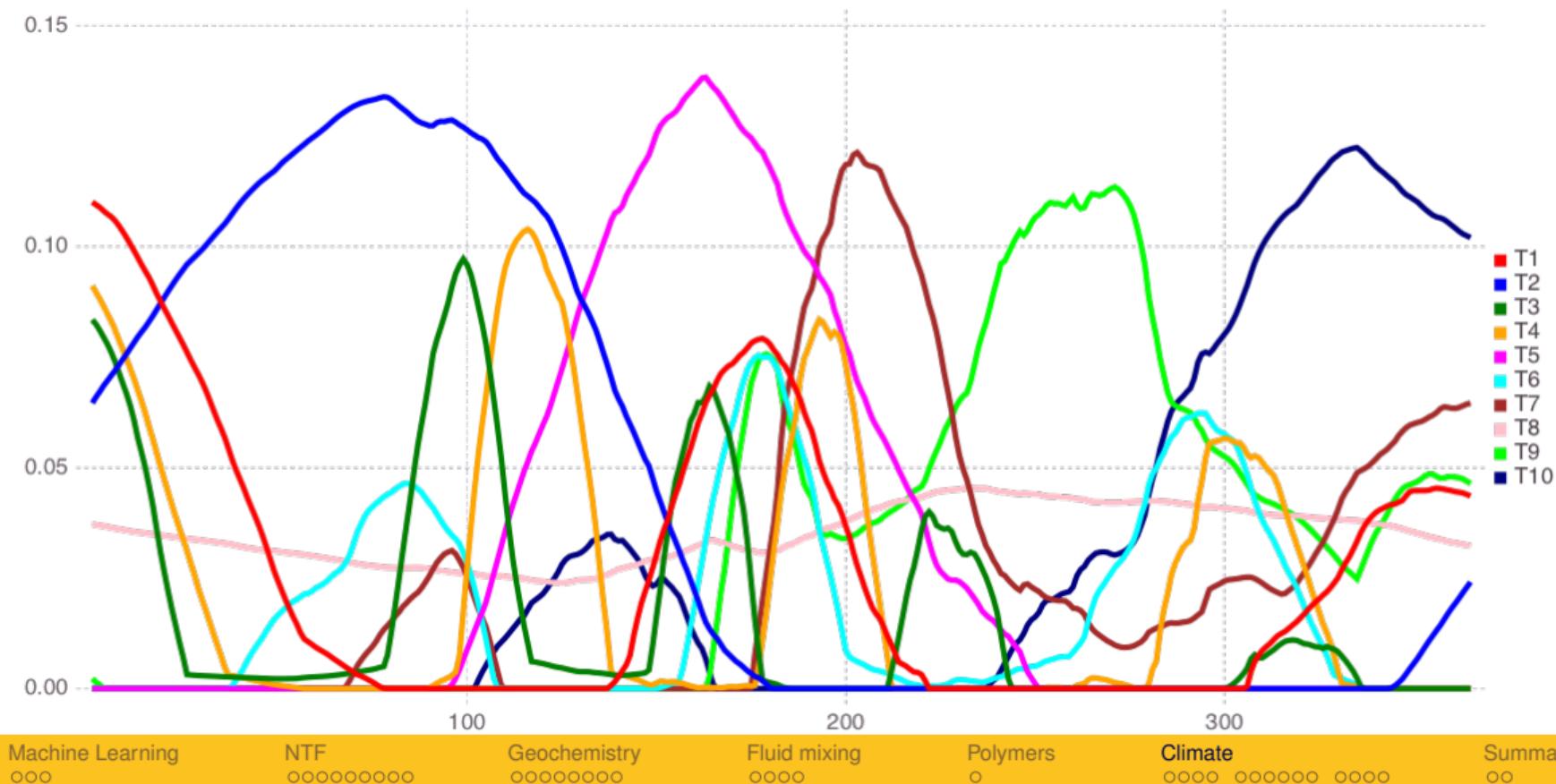
# Climate model of Europe: Water-table fluctuations represented by 8 signals



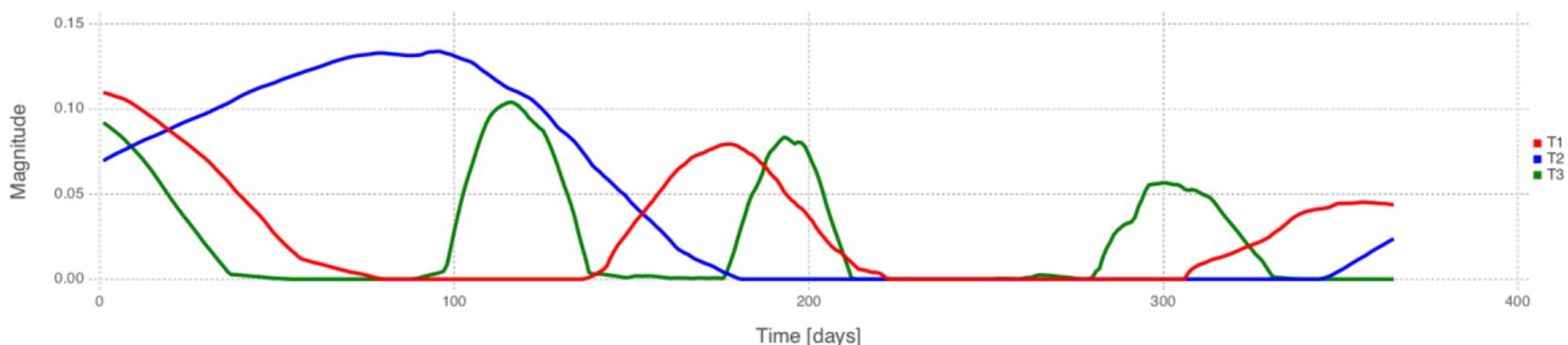
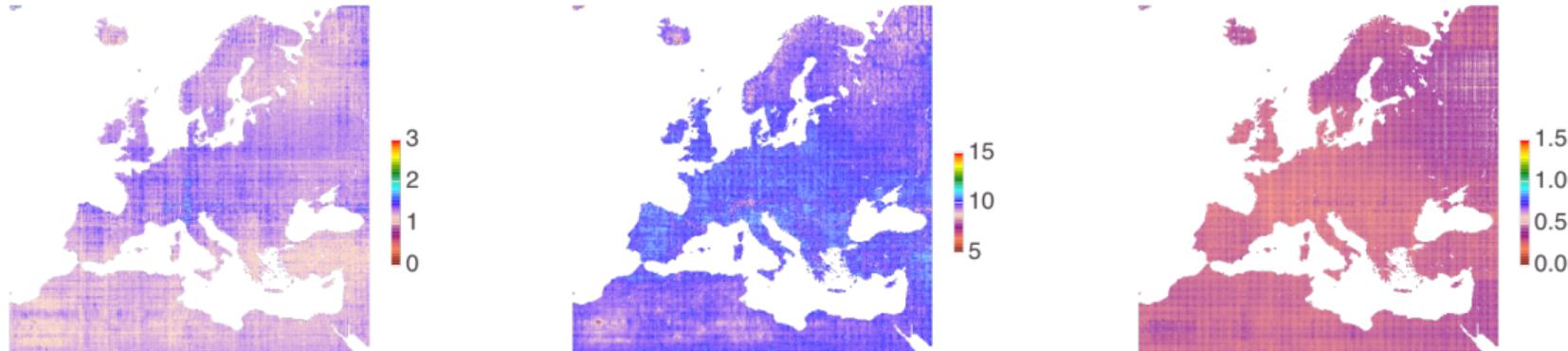
# Climate model of Europe: Water-table fluctuations represented by 9 signals



# Climate model of Europe: Water-table fluctuations represented by 10 signals



# Climate model of Europe: maximum water-table fluctuations for each signal (9)



Machine Learning  
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NTF  
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Geochemistry  
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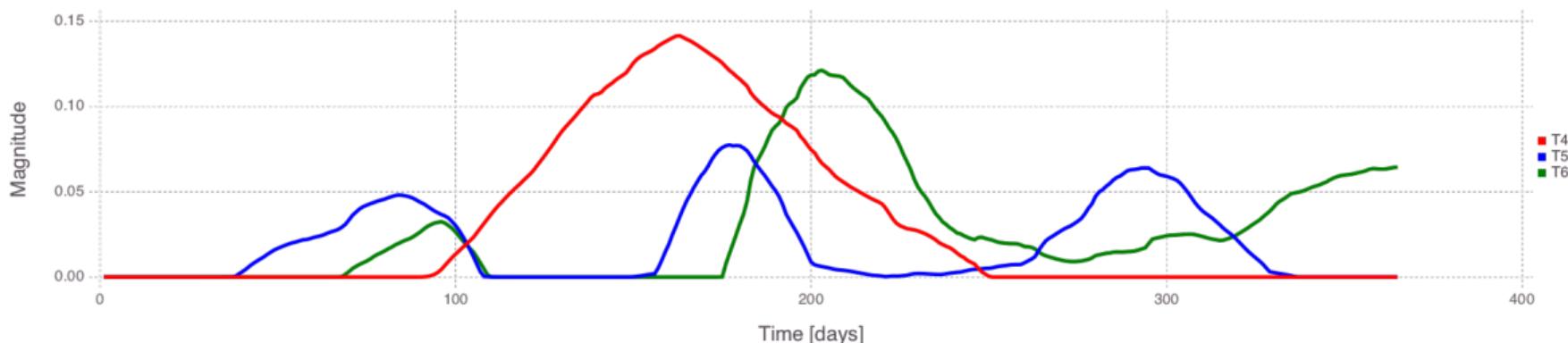
Fluid mixing  
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Polymers  
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Climate  
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Summary  
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# Climate model of Europe: maximum water-table fluctuations for each signal (9)



Machine Learning  
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NTF  
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Geochemistry  
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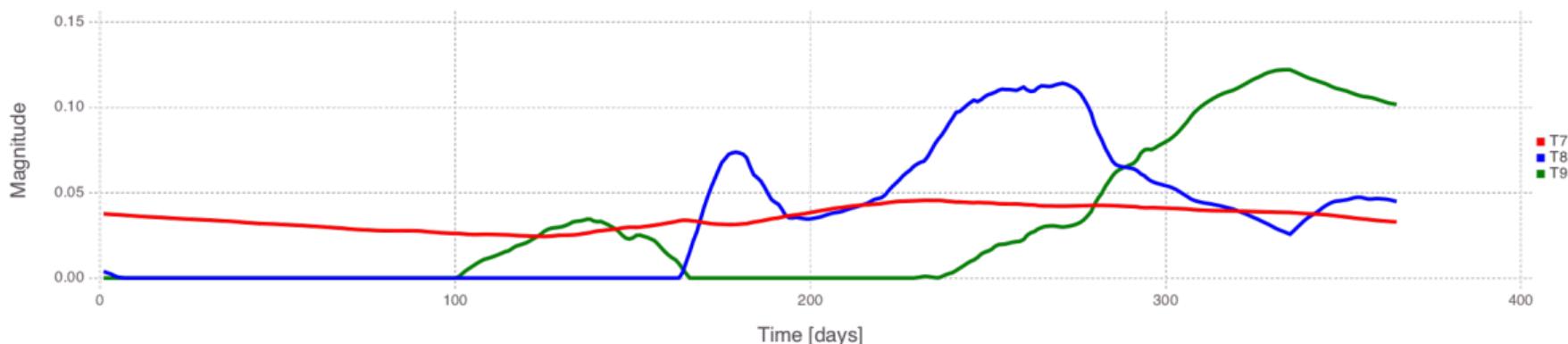
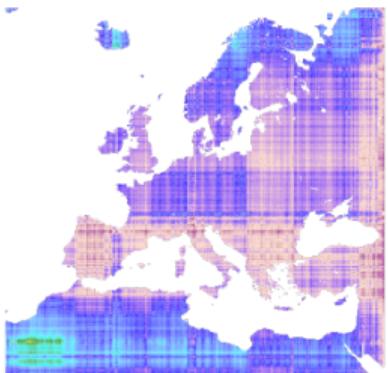
Fluid mixing  
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Polymers  
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Climate  
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Summary  
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# Climate model of Europe: maximum water-table fluctuations for each signal (9)



Machine Learning  
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NTF  
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Geochemistry  
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Fluid mixing  
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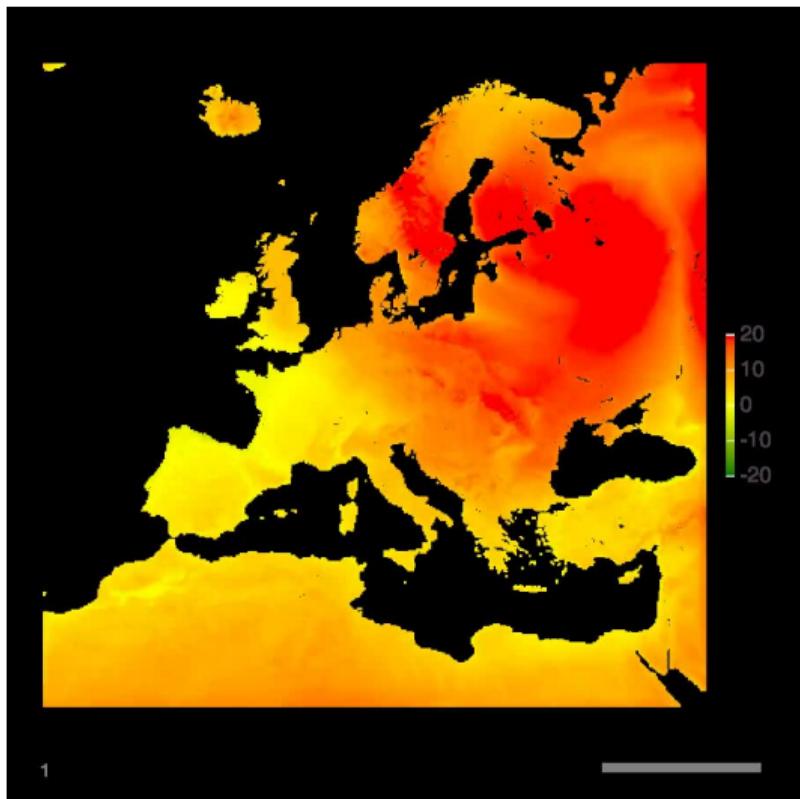
Polymers  
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Climate  
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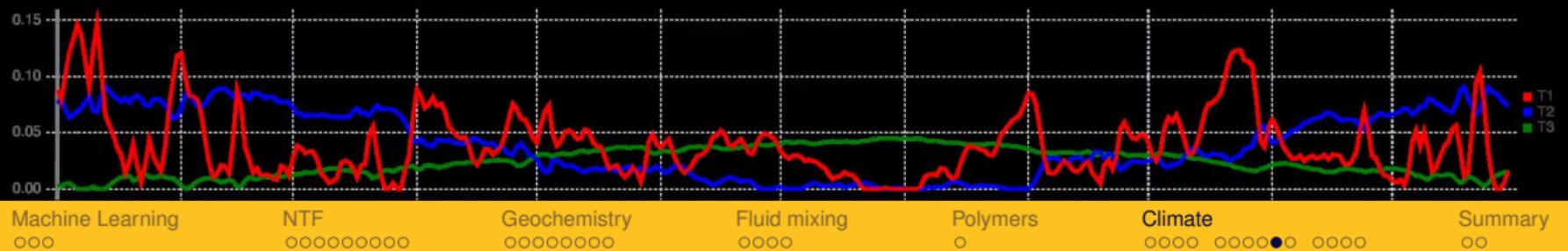
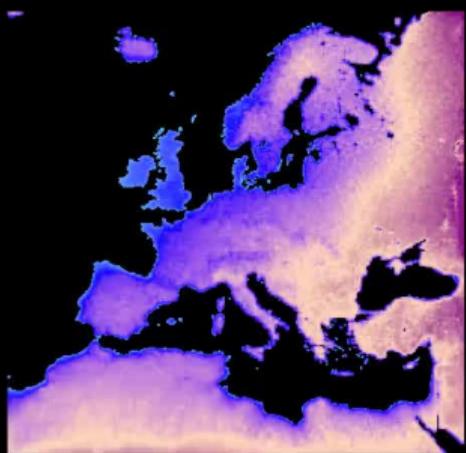
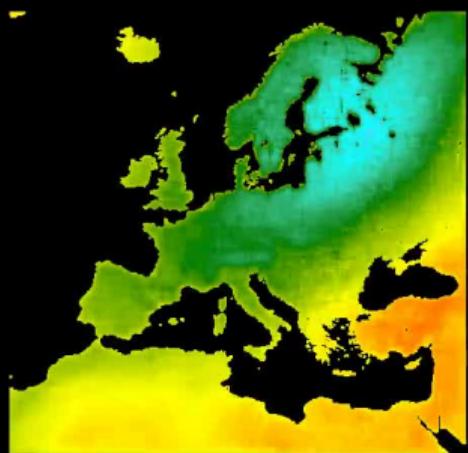
Summary  
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# Climate model of Europe: air-temperature fluctuations

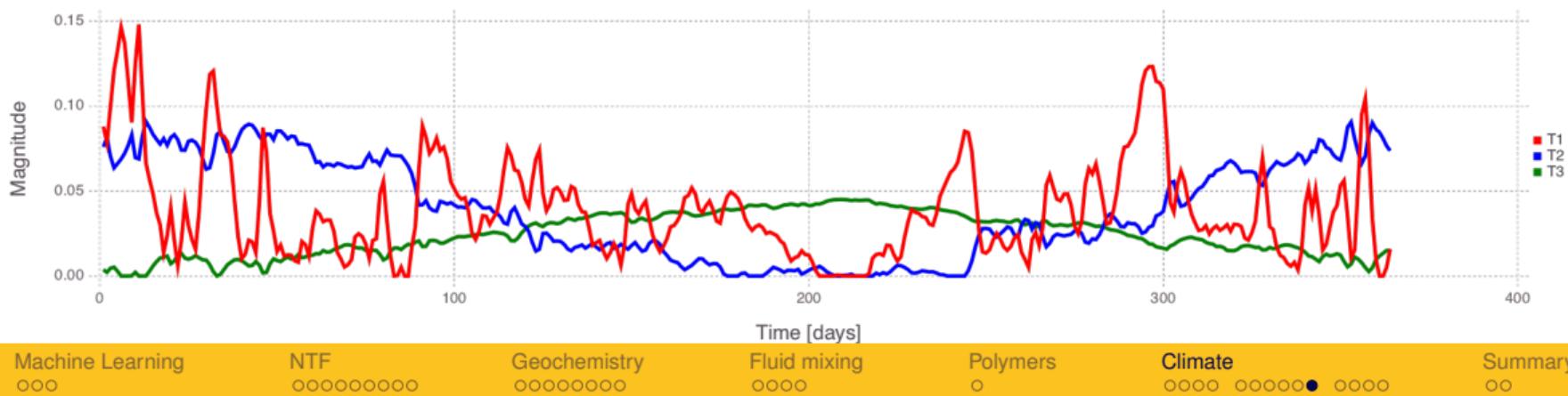
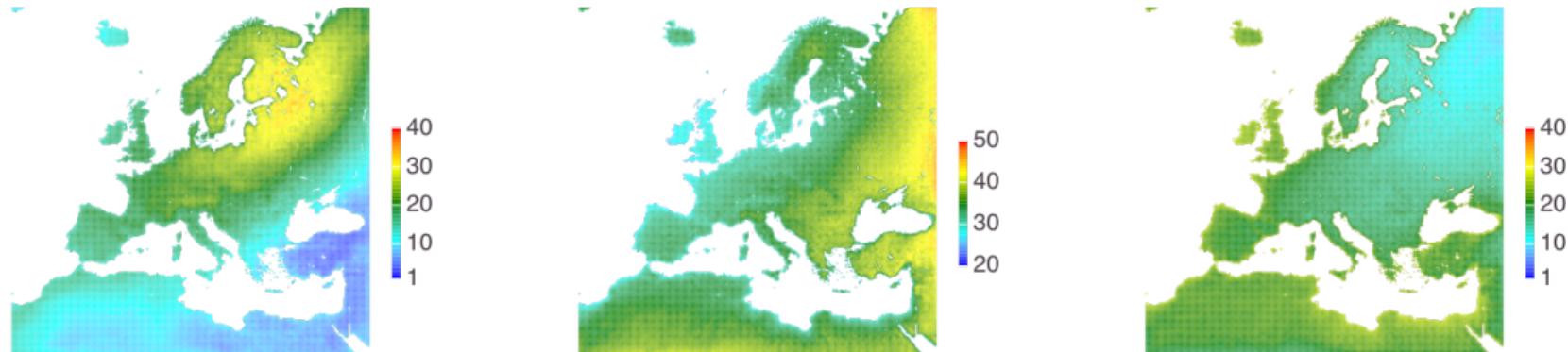
- ▶ fluctuations in the air temperature
- ▶  $(424 \times 412 \times 365) \rightarrow (? \times ? \times ?)$



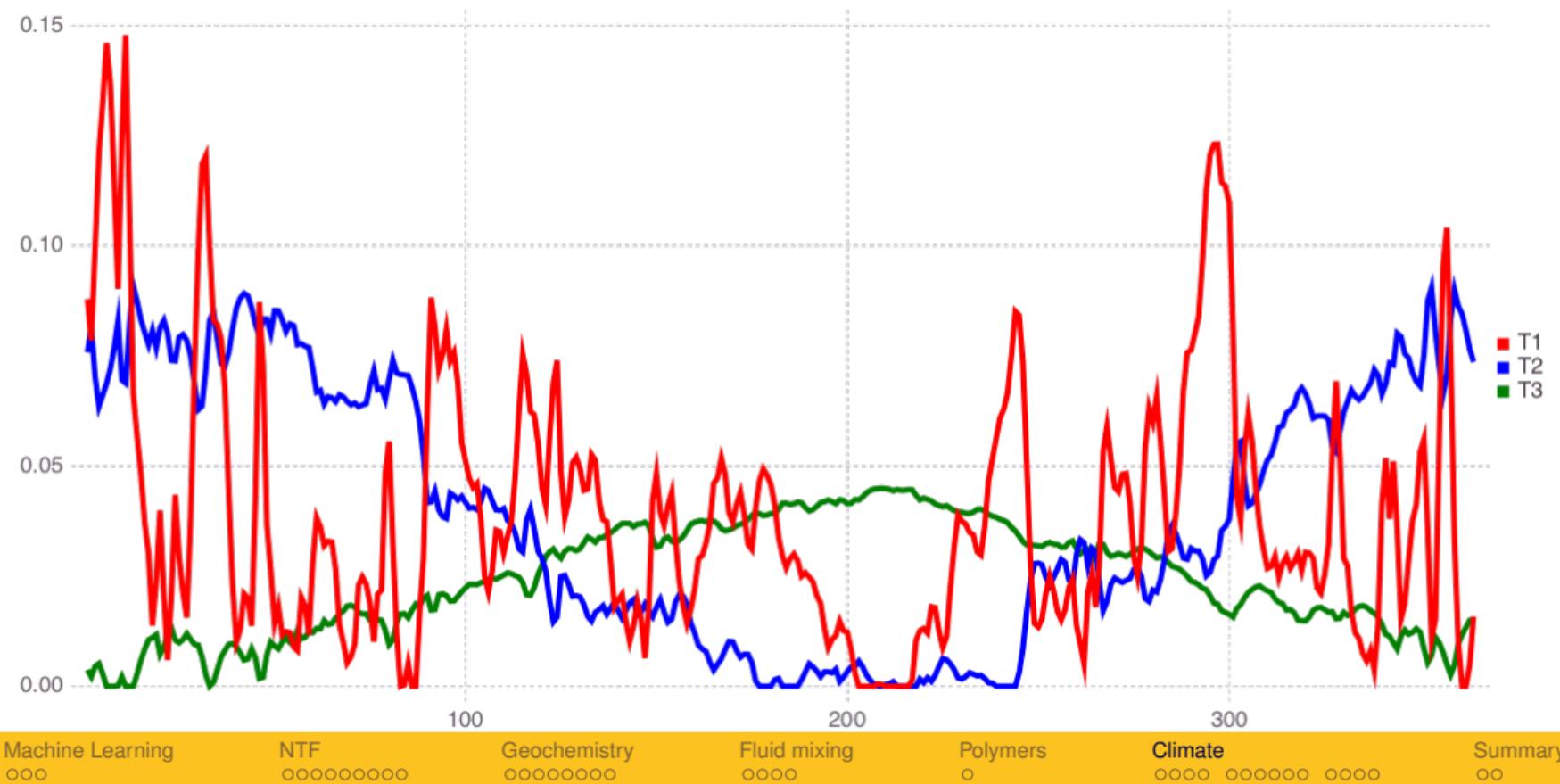
# Climate model of Europe: air temperature fluctuations represented by 3 signals



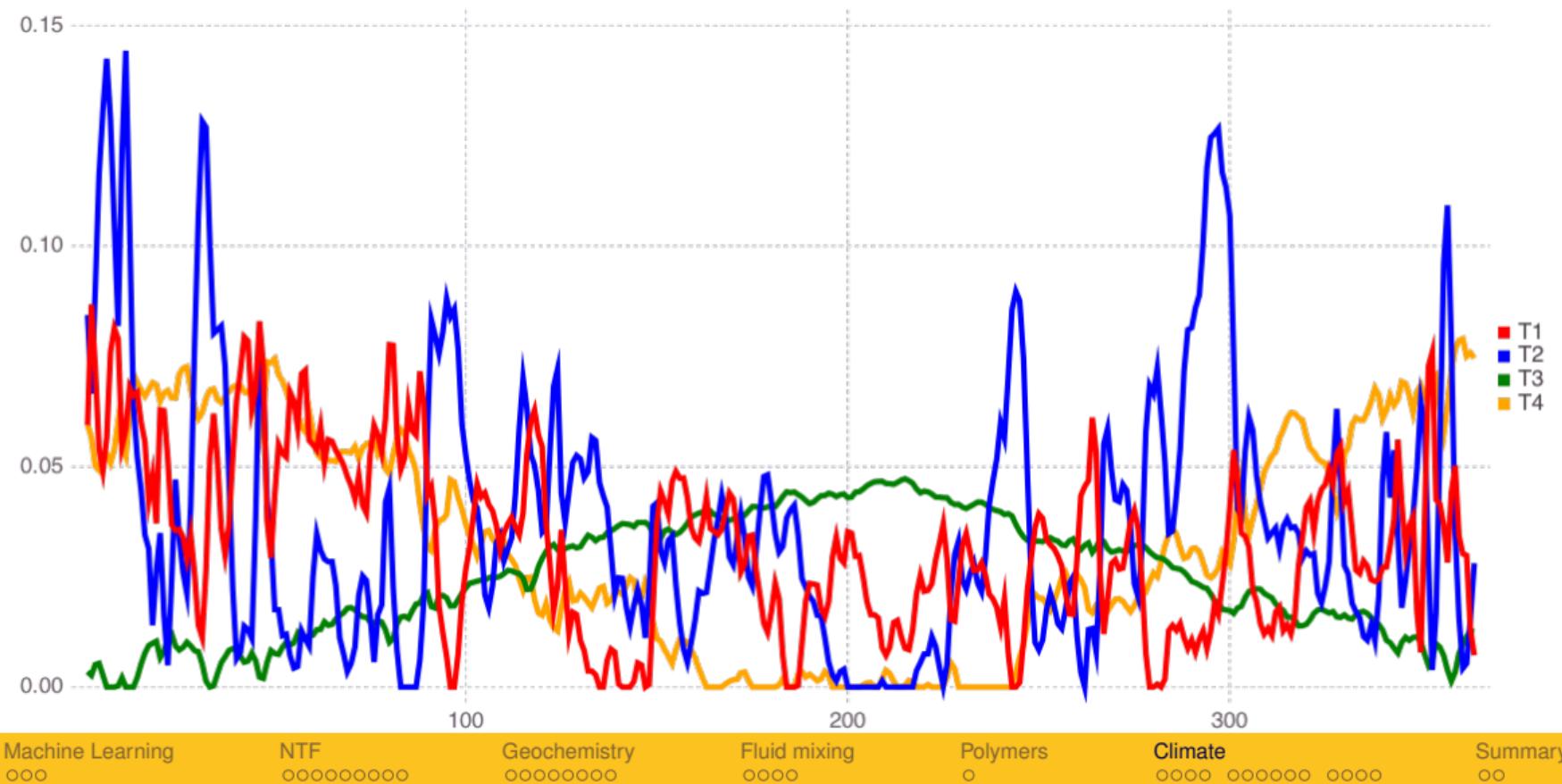
# Climate model of Europe: maximum air temperature fluctuations for each signal (3)



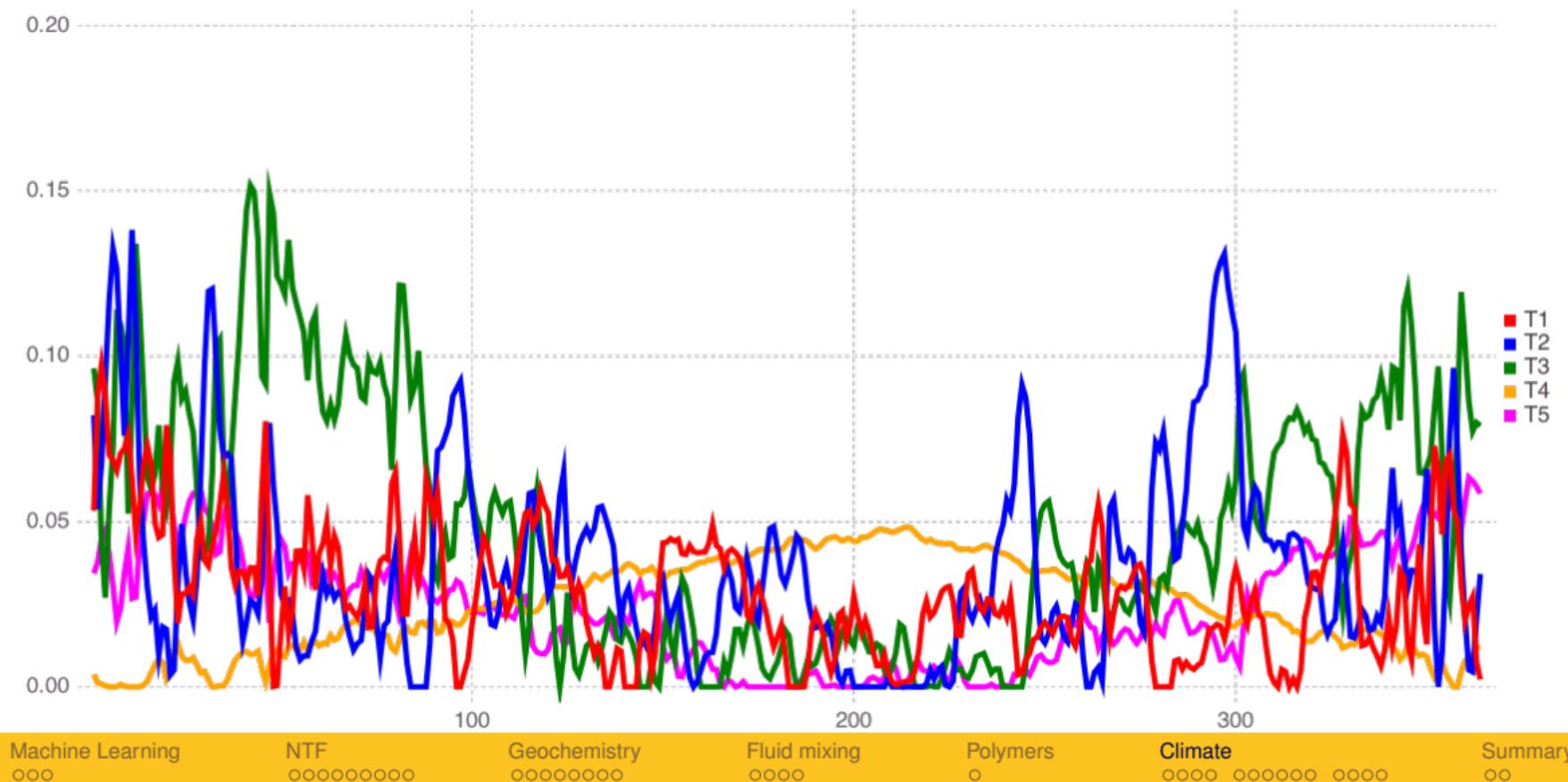
# Climate model of Europe: Air temperature fluctuations represented by 3 signals



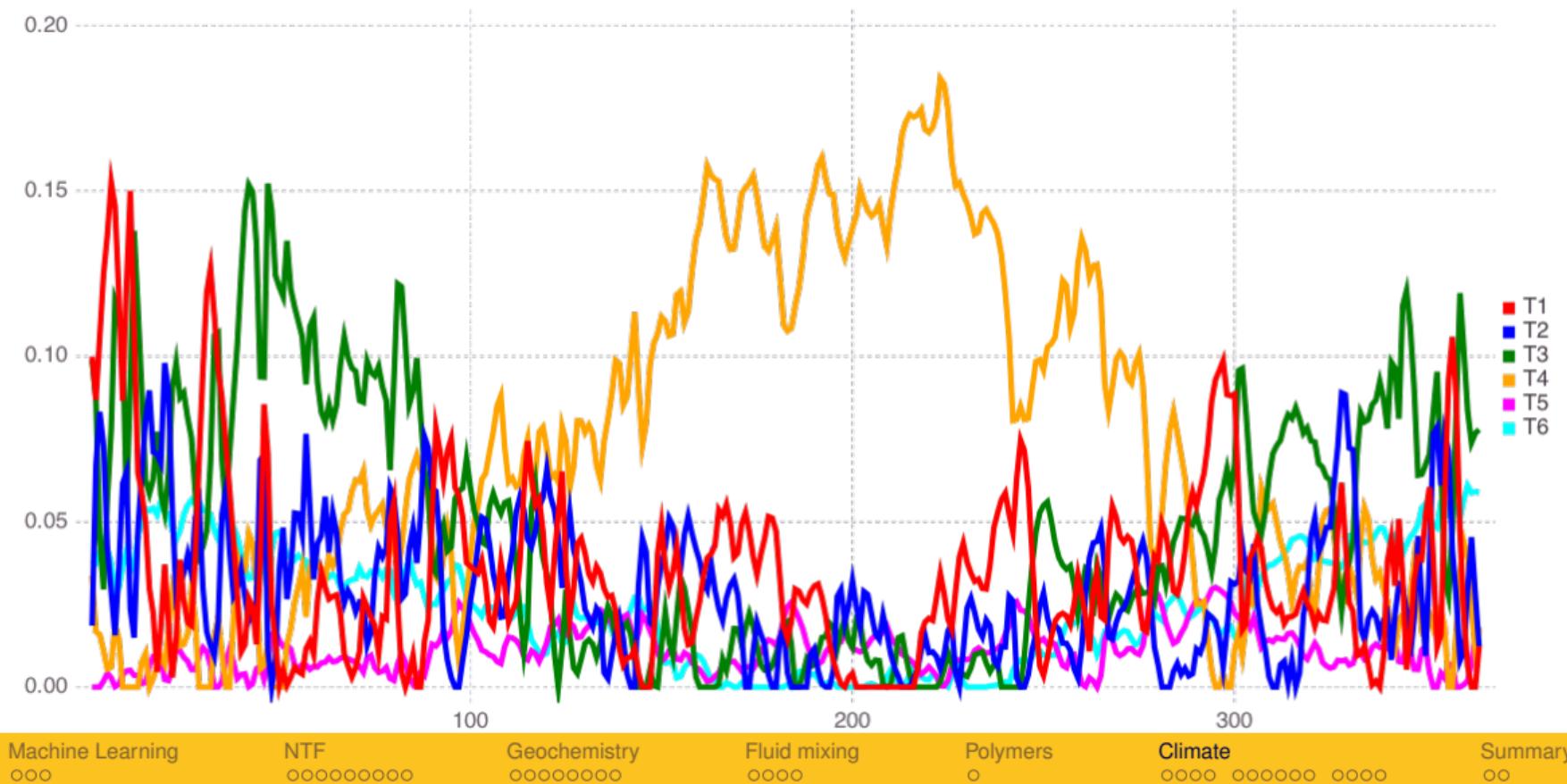
# Climate model of Europe: Air temperature fluctuations represented by 4 signals



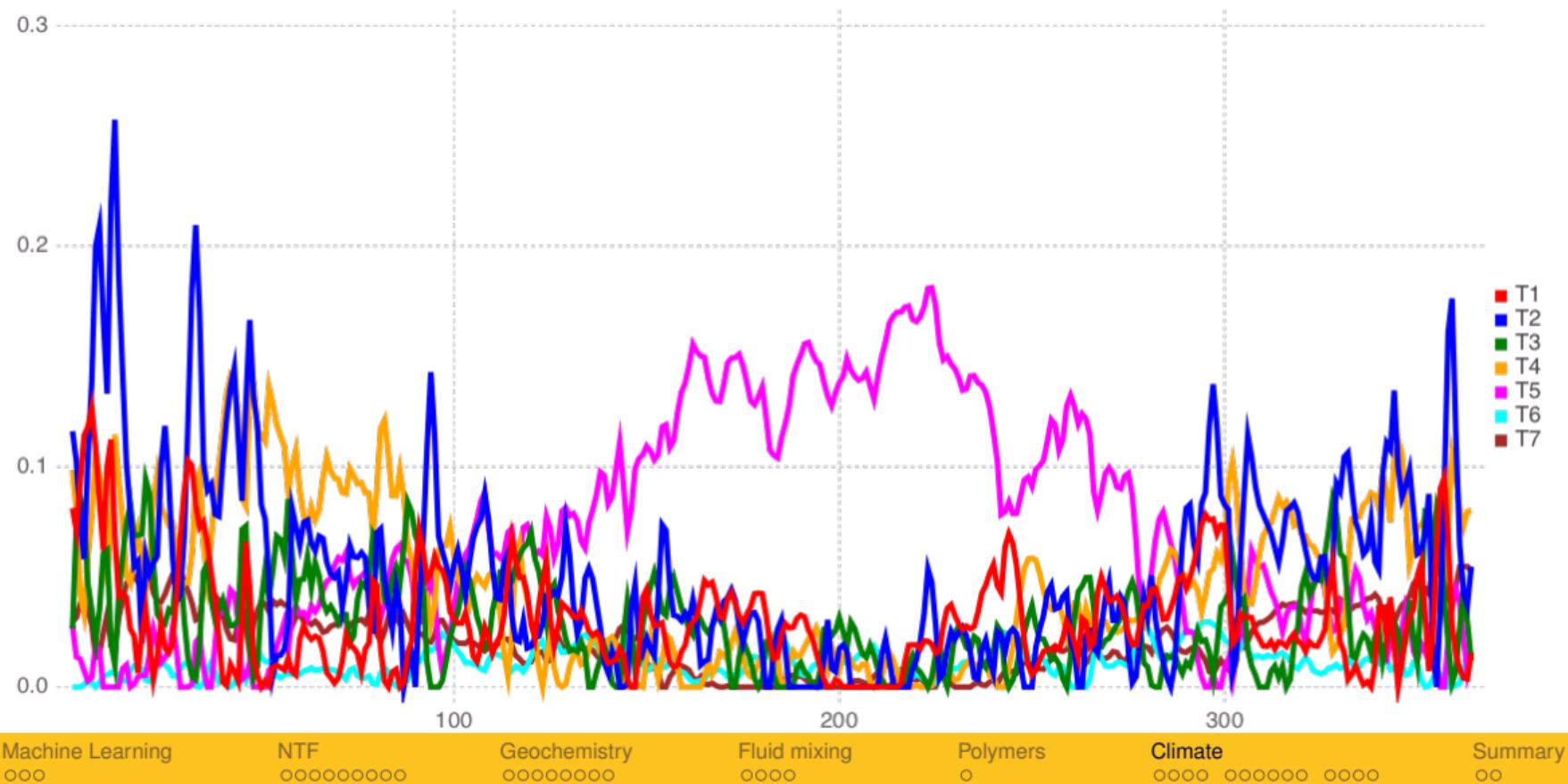
# Climate model of Europe: Air temperature fluctuations represented by 5 signals



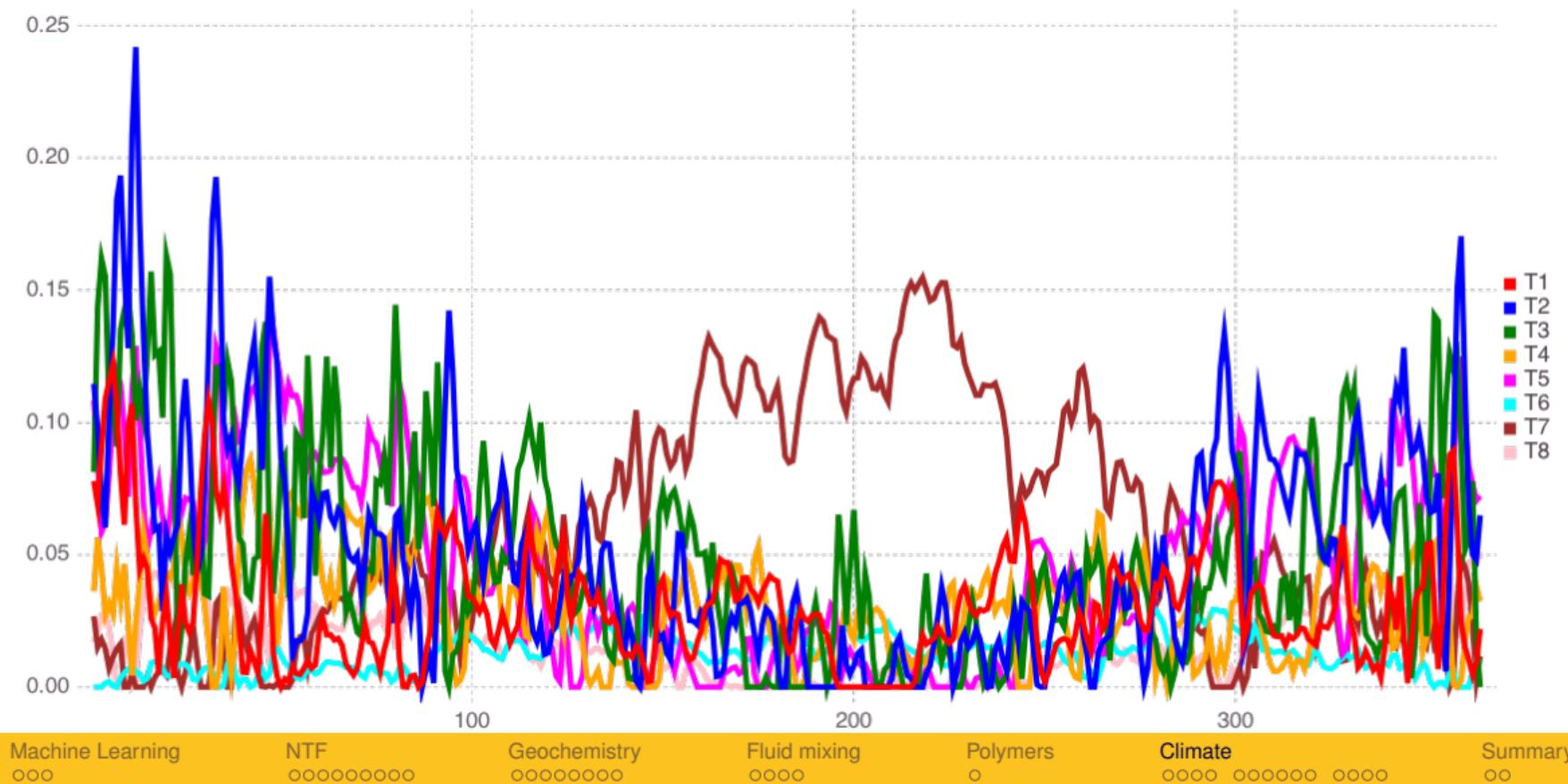
# Climate model of Europe: Air temperature fluctuations represented by 6 signals



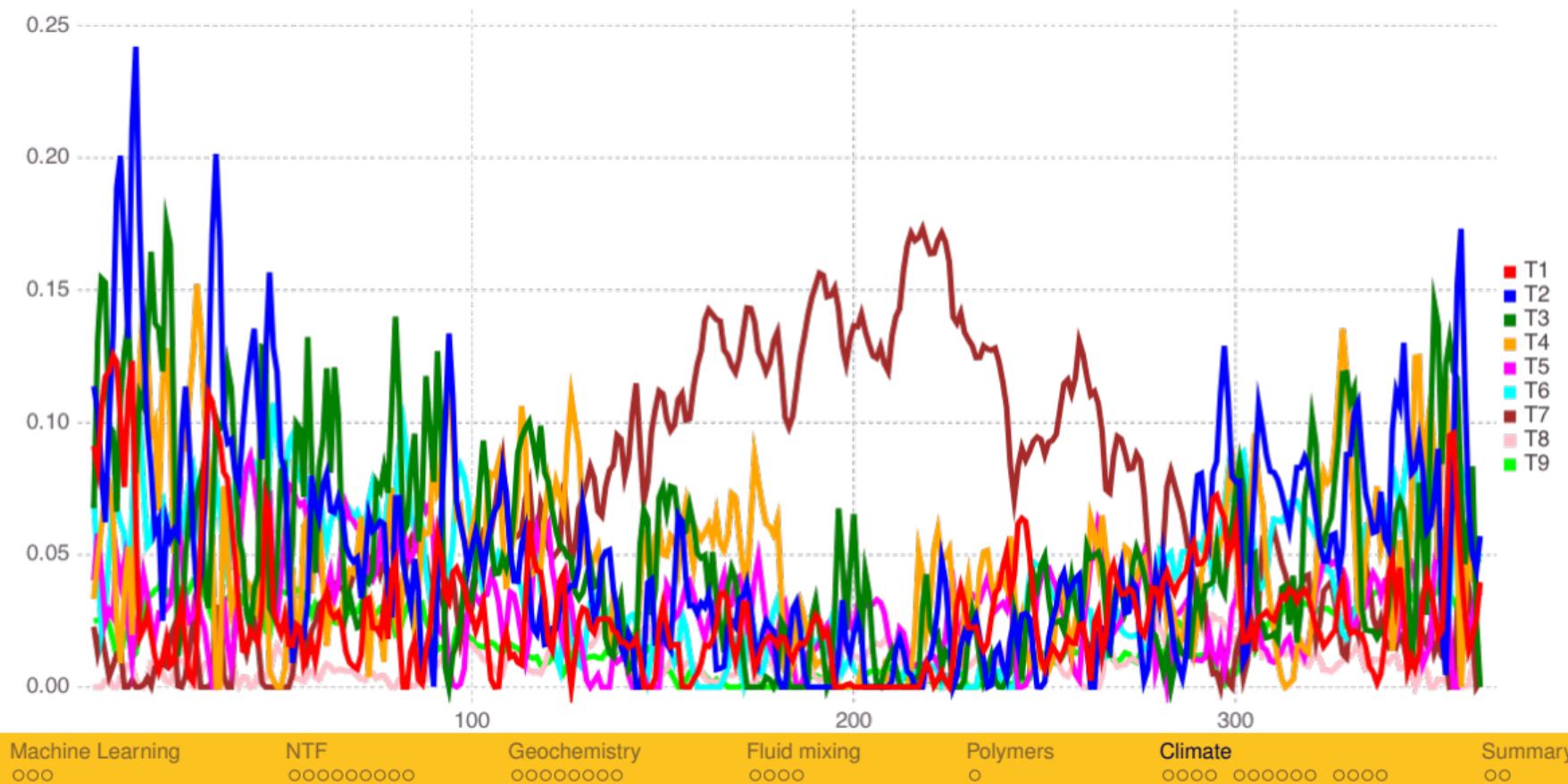
# Climate model of Europe: Air temperature fluctuations represented by 7 signals



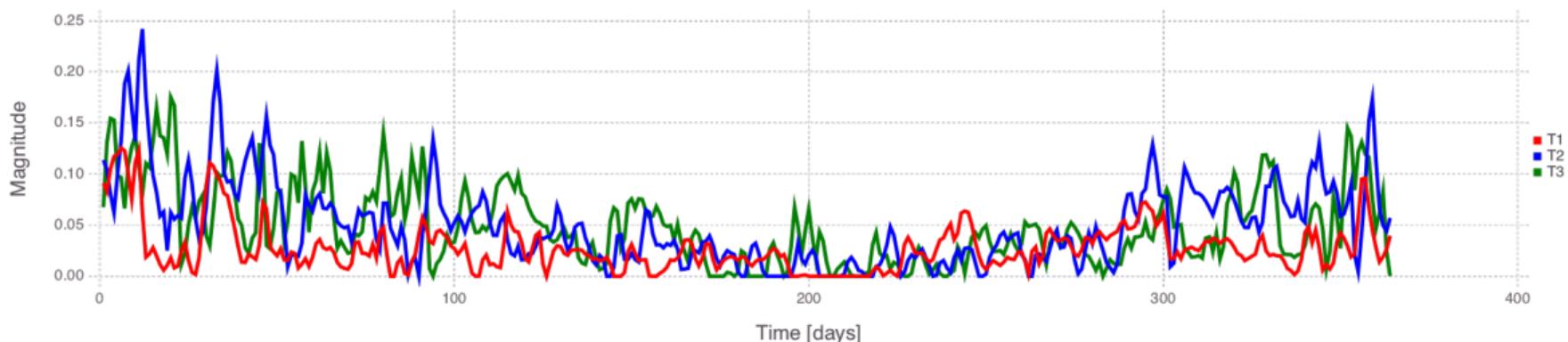
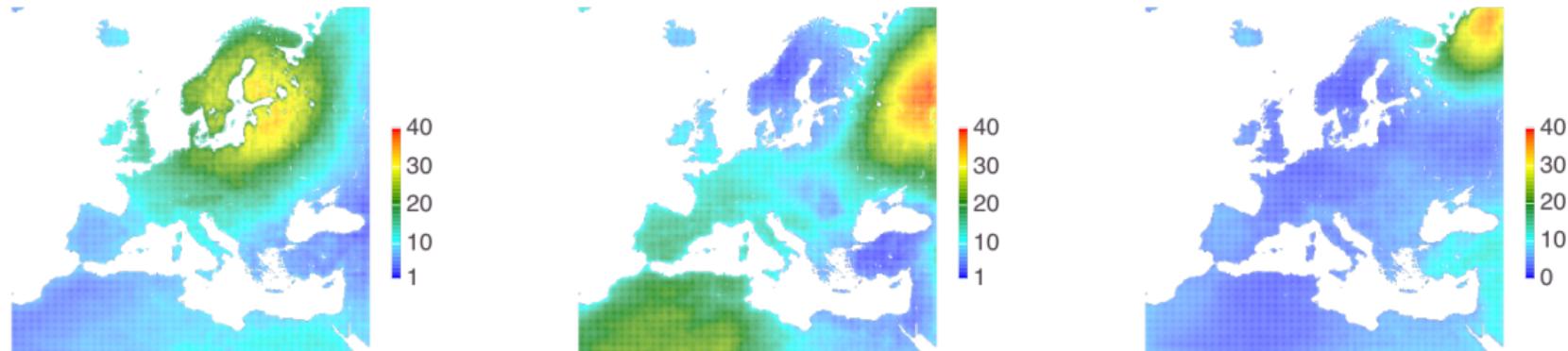
# Climate model of Europe: Air temperature fluctuations represented by 8 signals



# Climate model of Europe: Air temperature fluctuations represented by 9 signals



# Climate model of Europe: maximum air temperature fluctuations for each signal (9)



Machine Learning  
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NTF  
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Geochemistry  
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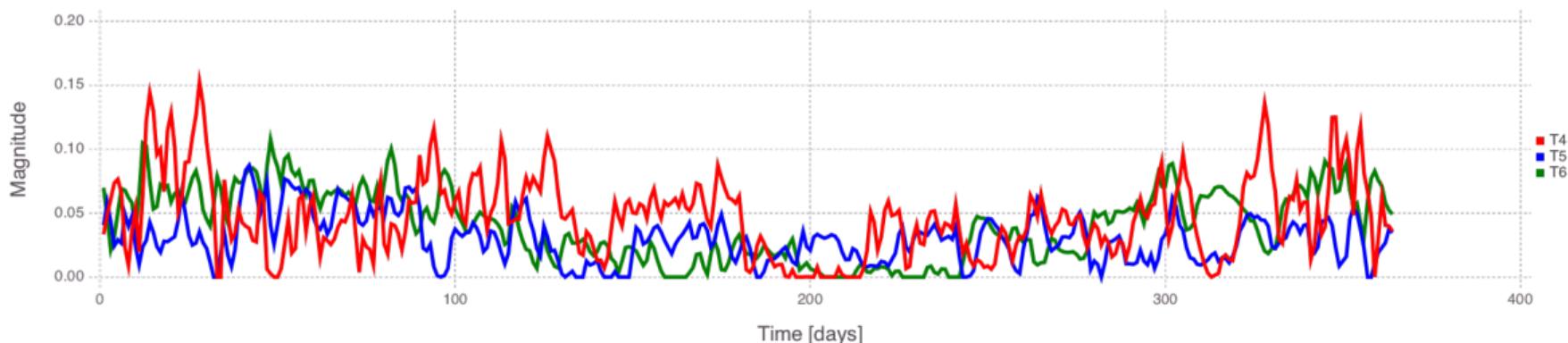
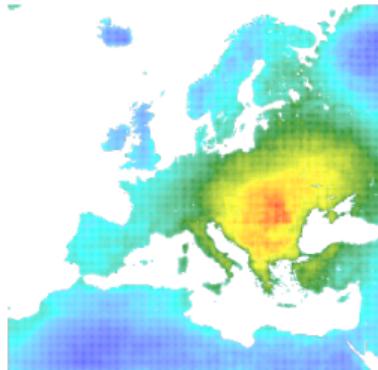
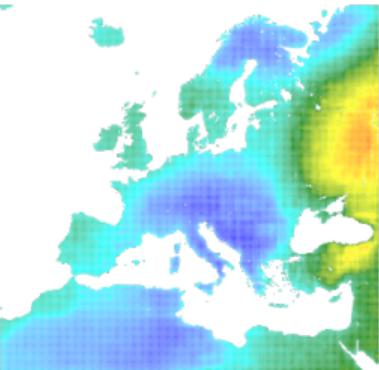
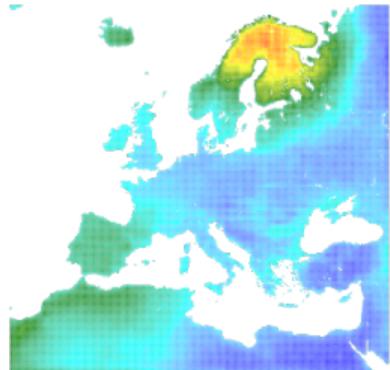
Fluid mixing  
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Polymers  
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Climate  
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Summary  
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# Climate model of Europe: maximum air temperature fluctuations for each signal (9)



Machine Learning  
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NTF  
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Geochemistry  
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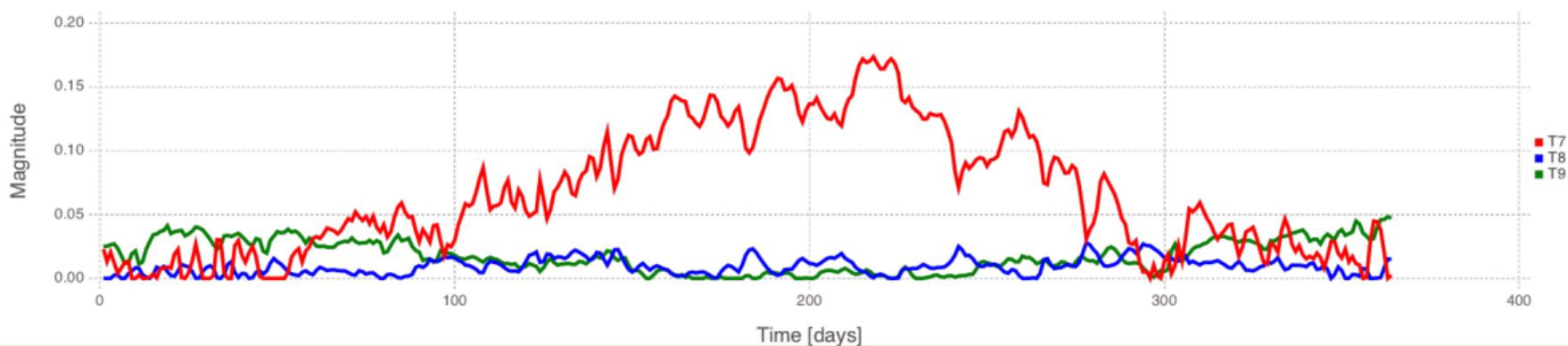
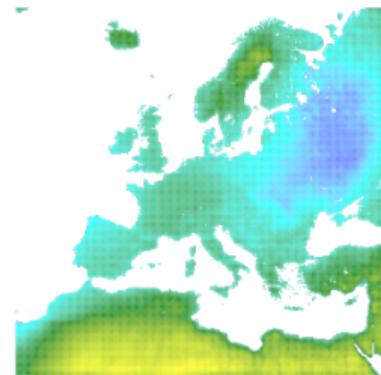
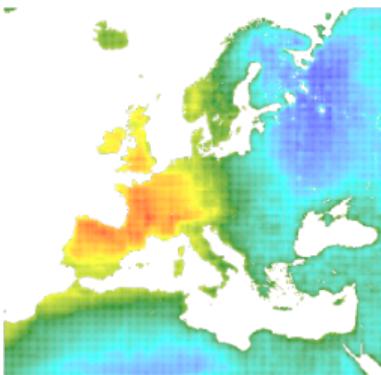
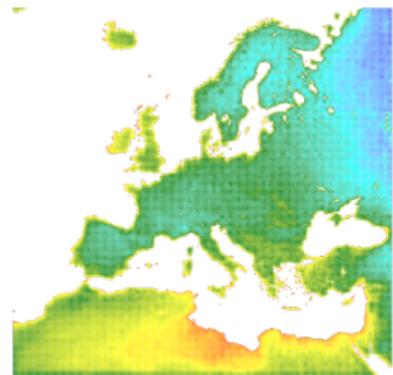
Fluid mixing  
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Polymers  
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Climate  
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Summary  
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# Climate model of Europe: maximum air temperature fluctuations for each signal (9)



Machine Learning  
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NTF  
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Geochemistry  
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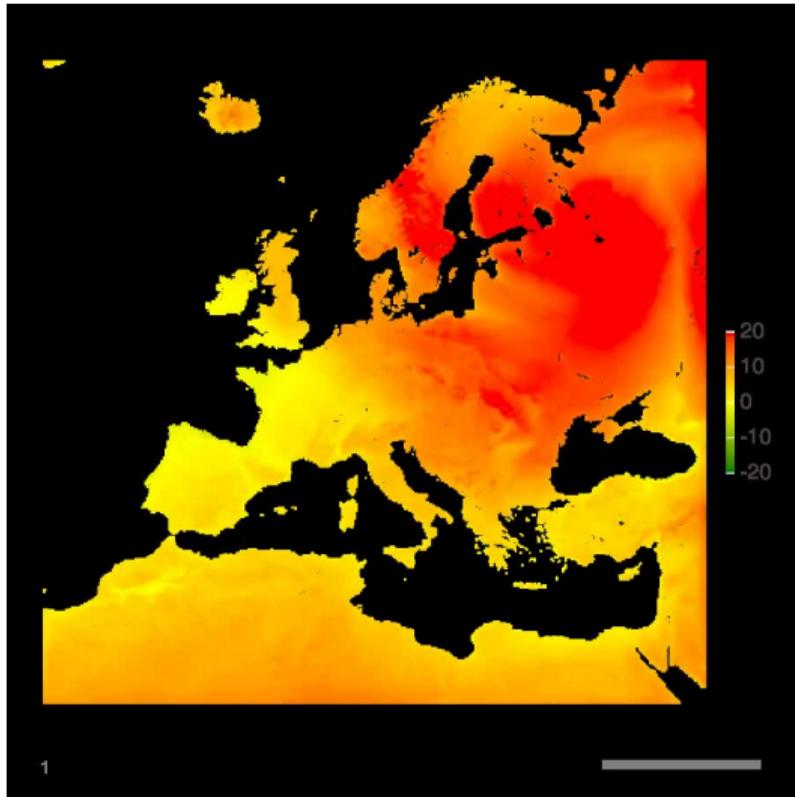
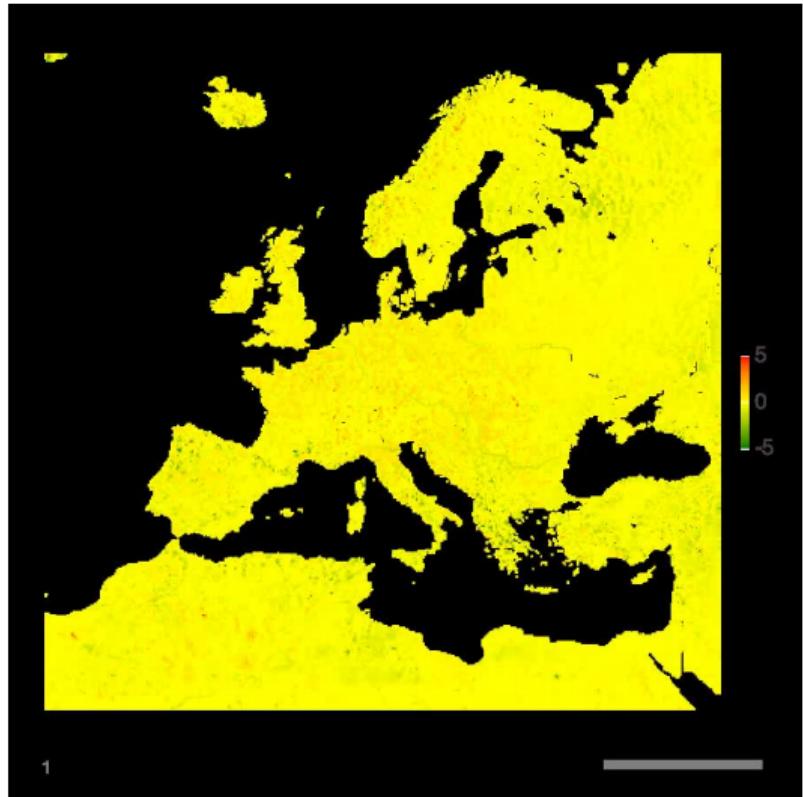
Fluid mixing  
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Polymers  
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Climate  
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Summary  
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# Climate model of Europe: water-table vs air-temperature fluctuations



Machine Learning  
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NTF  
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Geochemistry  
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Fluid mixing  
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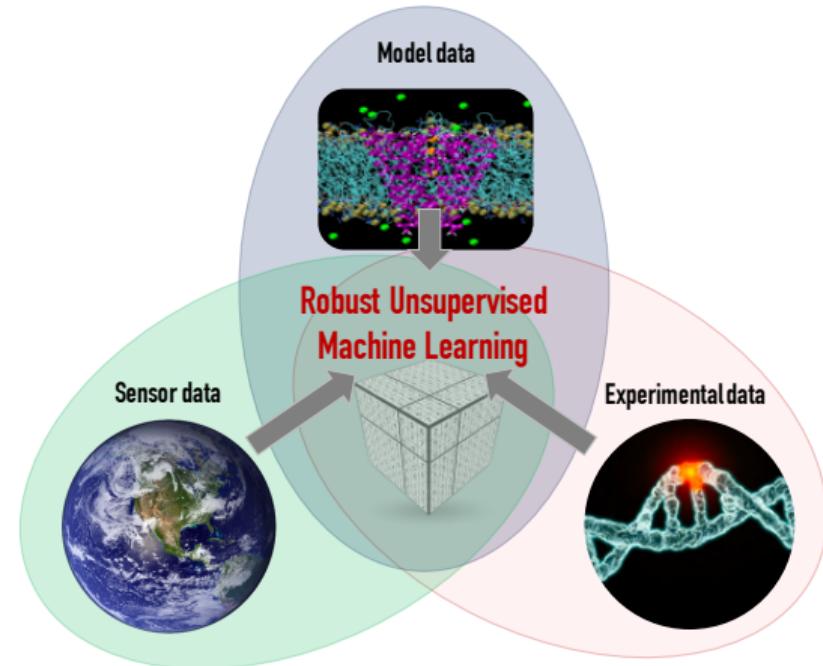
Polymers  
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Climate  
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Summary  
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## Summary

- ▶ We have developed a series of novel unsupervised ML methods based on Nonnegative Factorization (Matrices/Tensors)
- ▶ These ML methods have been used to solve various real-world problems
- ▶ Some of our ML analyses brought breakthrough discoveries (especially related to human cancer research)
- ▶ We have developed a series of ML computational tools for solving big-data problems using high-performance computing (HPC)



# Machine Learning (ML) Algorithms / Codes developed by our team

- ▶ NMF $k$  + ShiftNMF $k$  + GreenNMF $k$  (patent)
- ▶ NTF $k$
- ▶ NBMF: Quantum machine learning using **D-Wave**
- ▶ MADS: Model-Analyses & Decision Support  
**open-source, version-controlled, high-performance computational framework**  
<http://mads.lanl.gov>      <http://madsjulia.github.io/Mads.jl>



- ▶ Blind Source Separation examples:

[http://madsjulia.github.io/Mads.jl/Examples/blind\\_source\\_separation](http://madsjulia.github.io/Mads.jl/Examples/blind_source_separation)