

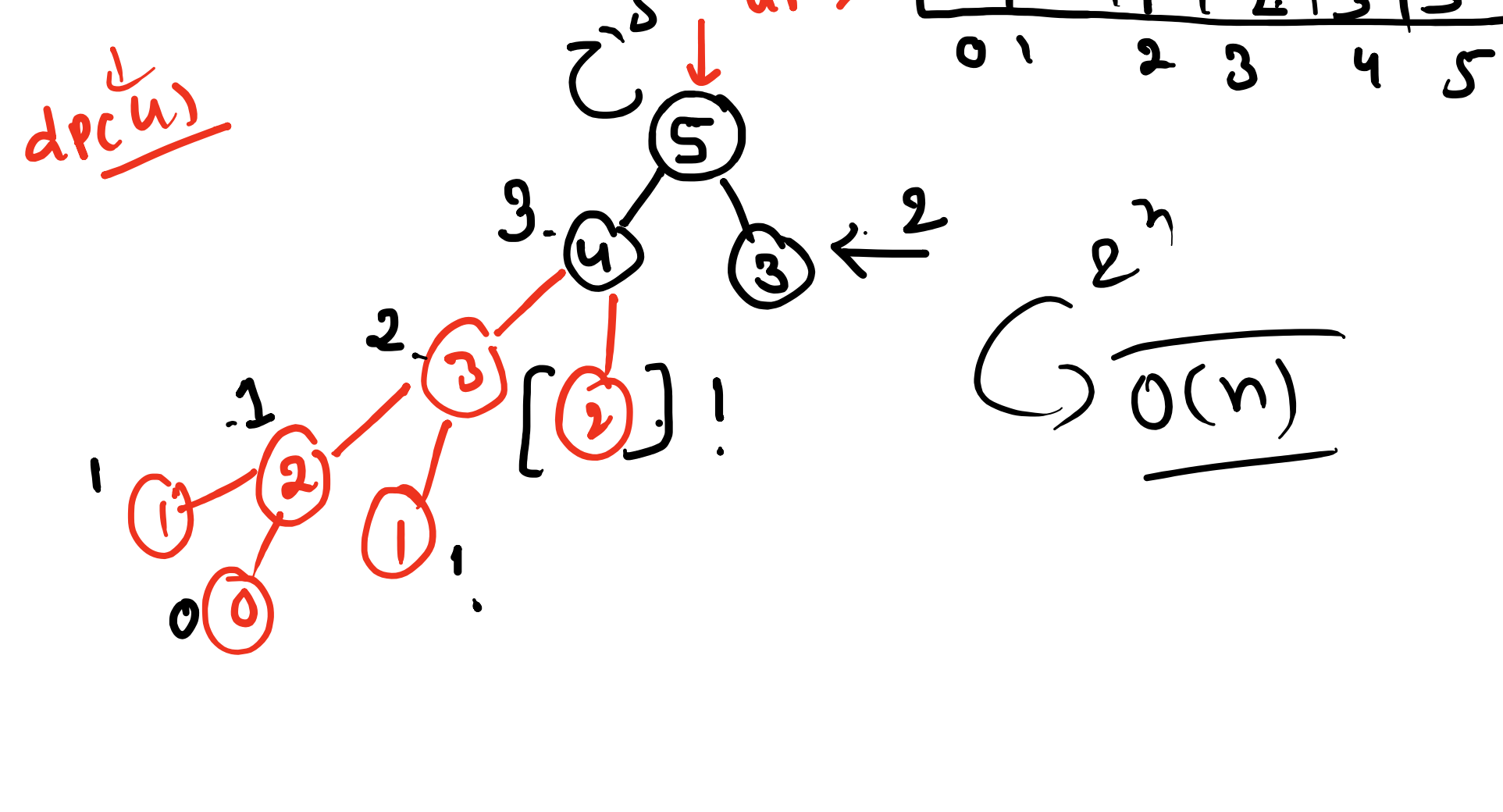
Dynamic programming

① Optimal substructure

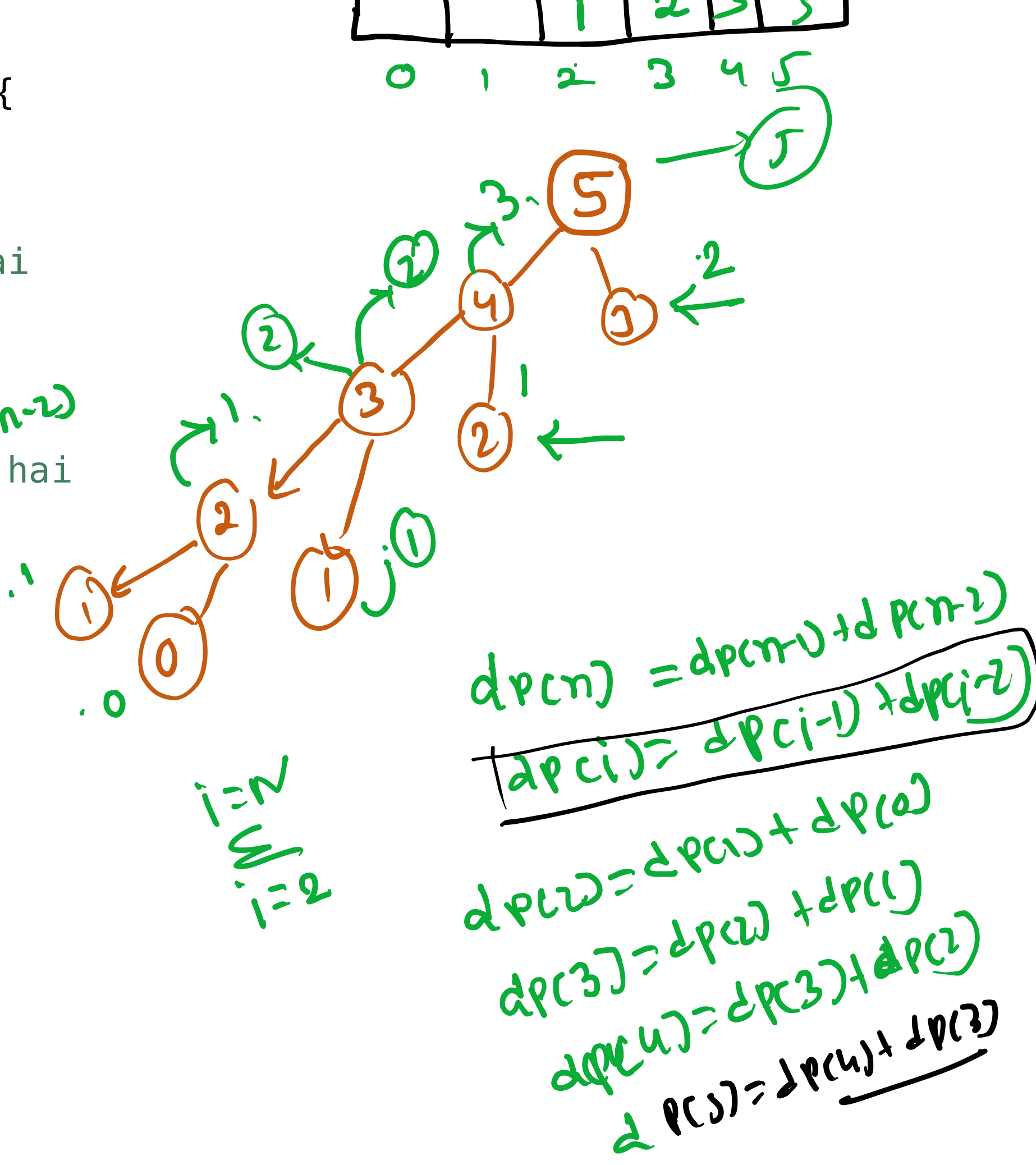
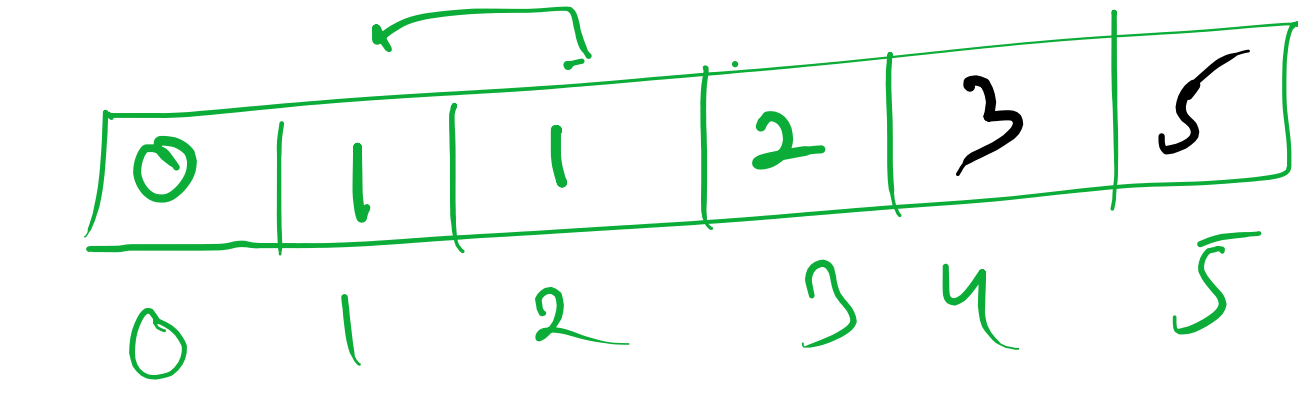
② Problem decomposition

- ① Top-down → Recursive
- ② Bottom-up → Iterative

```
public static int fib(int n) {
    if (n == 0 || n == 1) {
        return n;
    }
    int f1 = fib(n - 1);
    int f2 = fib(n - 2);
    return f1 + f2;
}
```

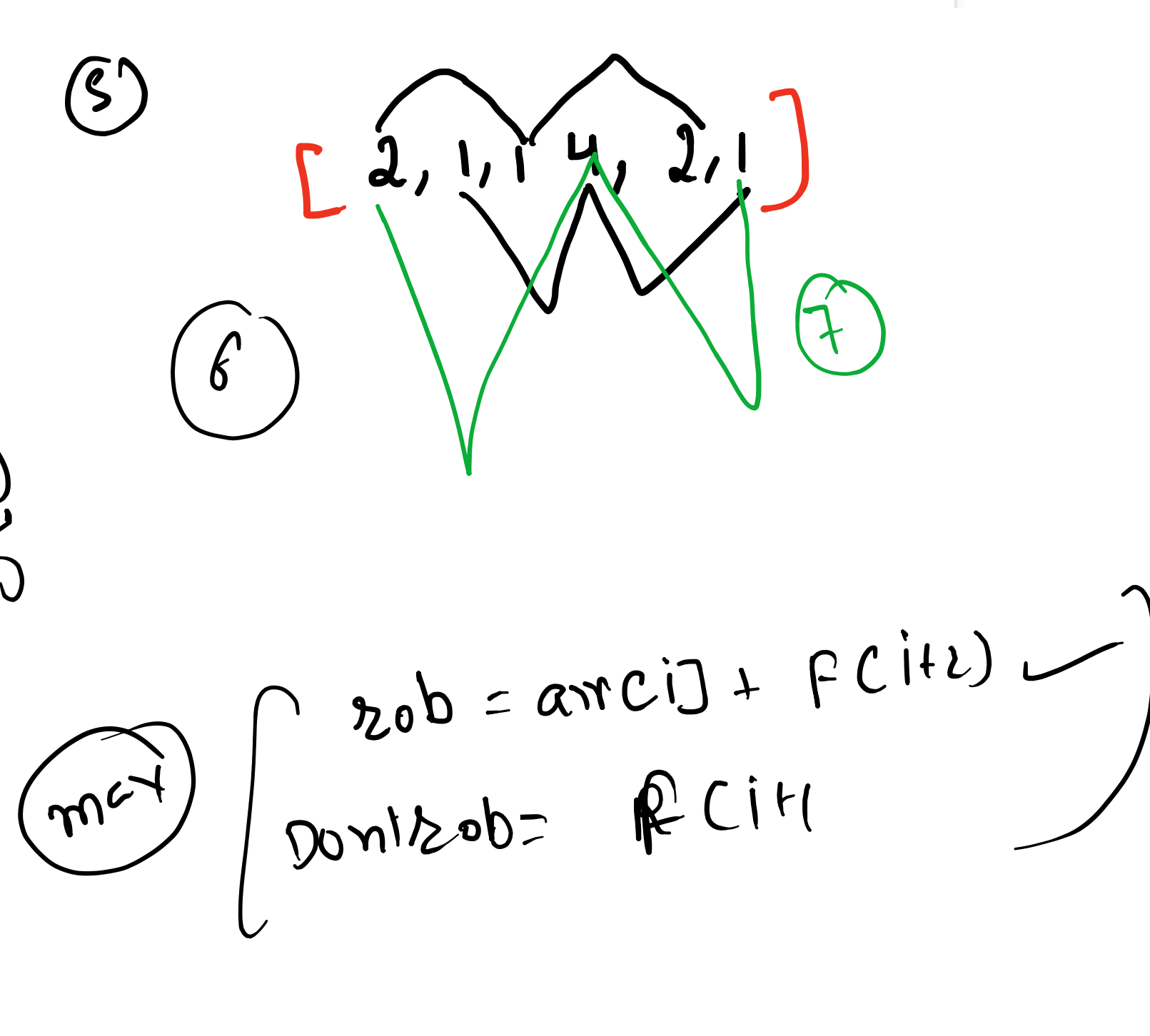
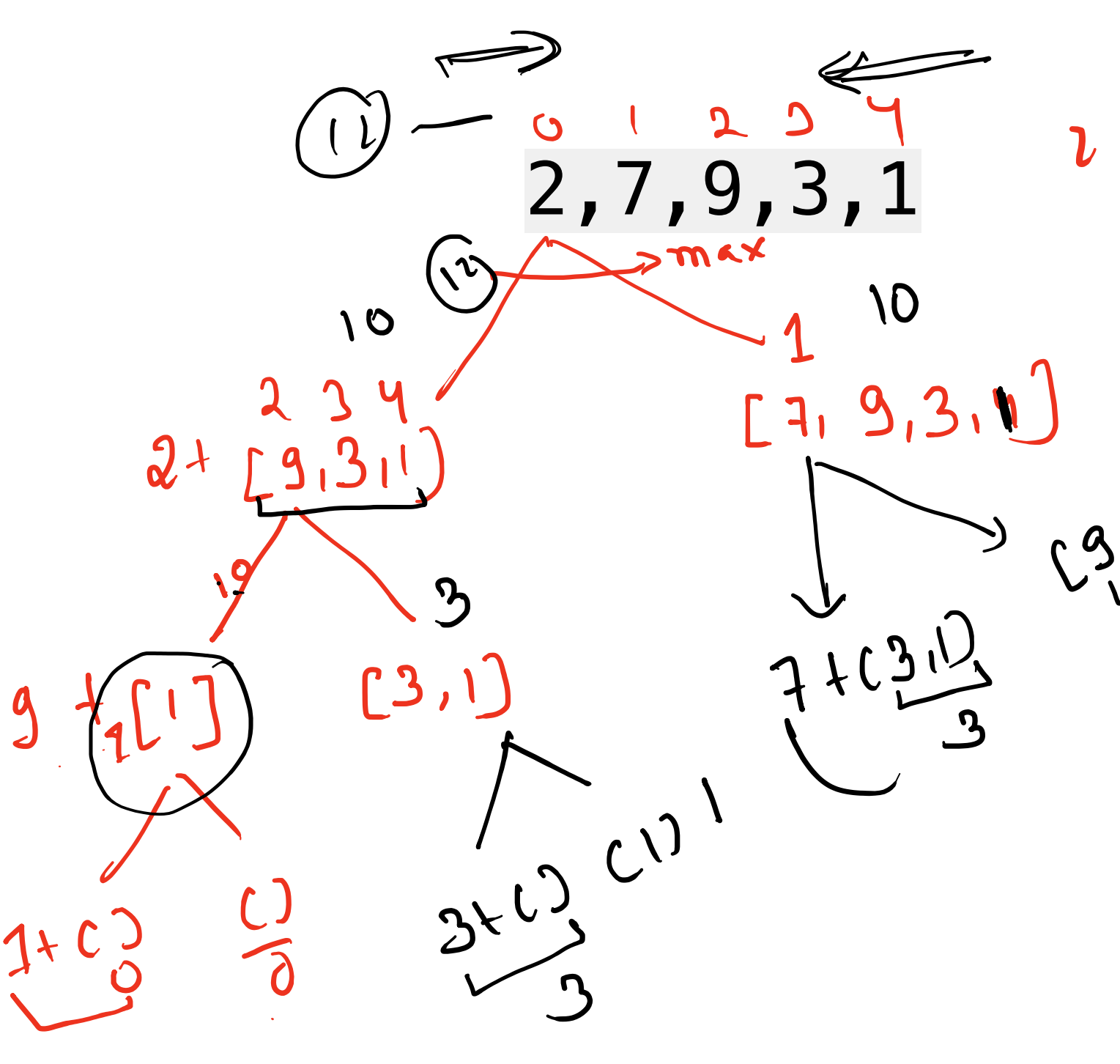


```
public static int fibTD(int n, int[] dp) {
    if (n == 0 || n == 1) {
        return n;
    }
    if (dp[n] != 0) { // dp apply kra hai
        return dp[n];
    }
    int f1 = fibTD(n - 1, dp);
    int f2 = fibTD(n - 2, dp);
    return dp[n] = f1 + f2; // yaad kra hai
}
```

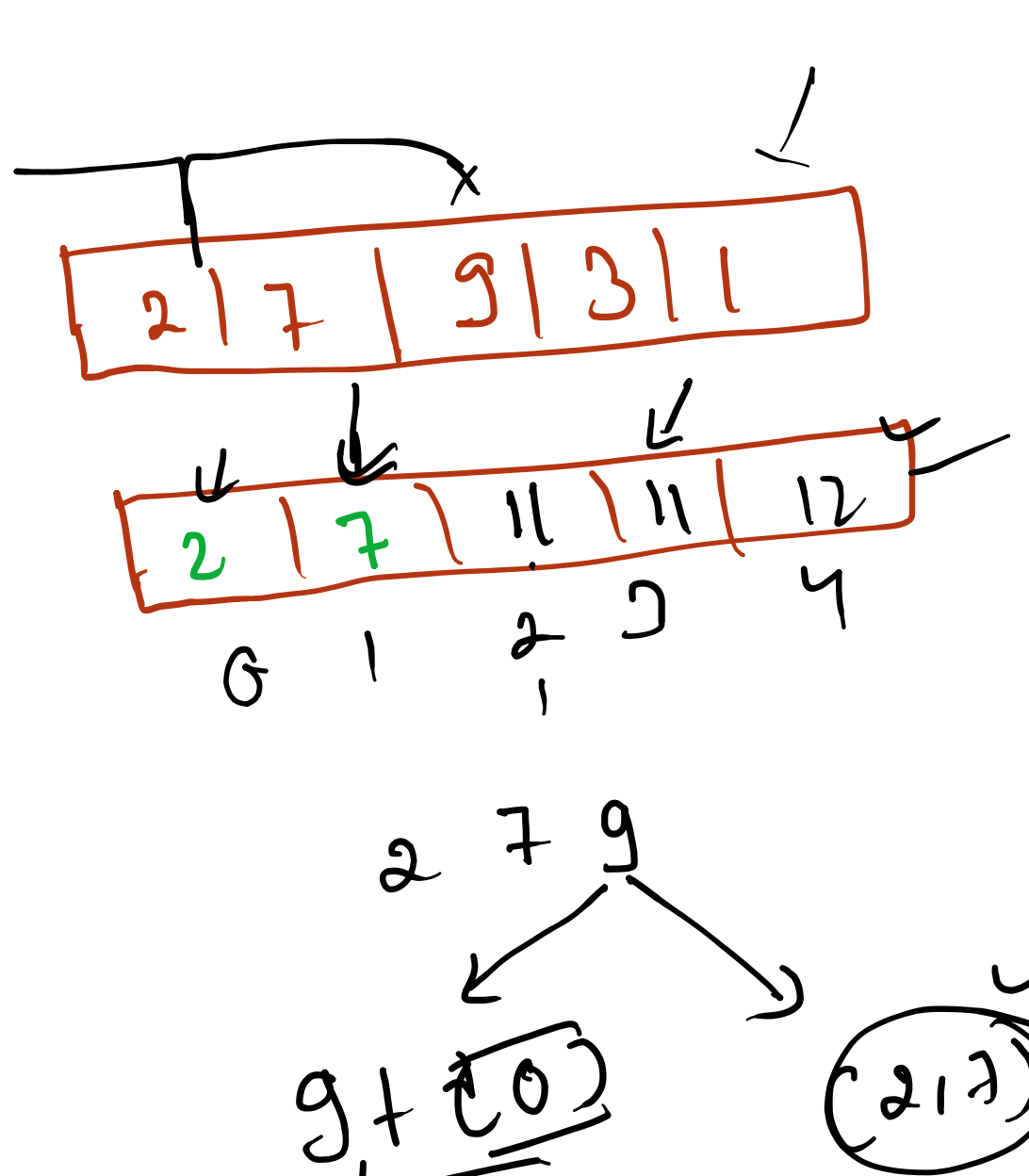
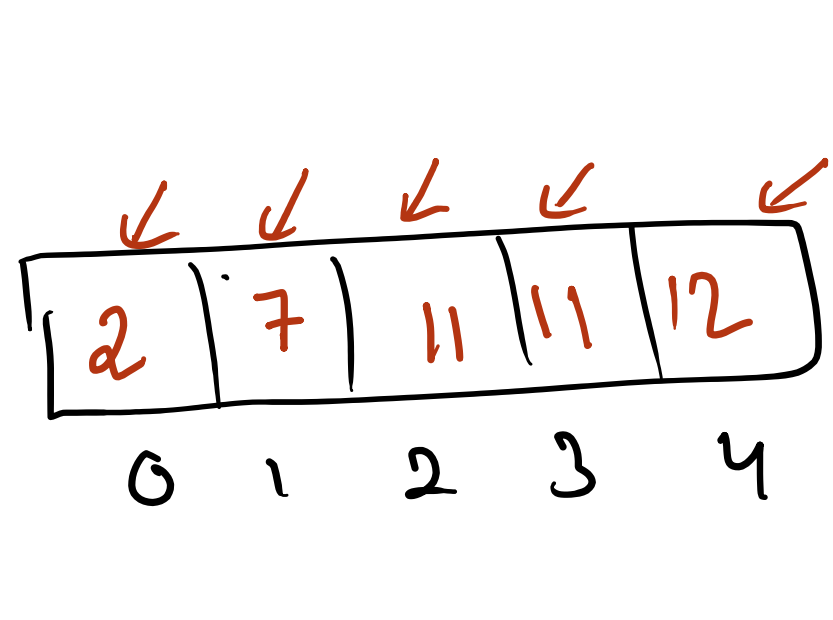
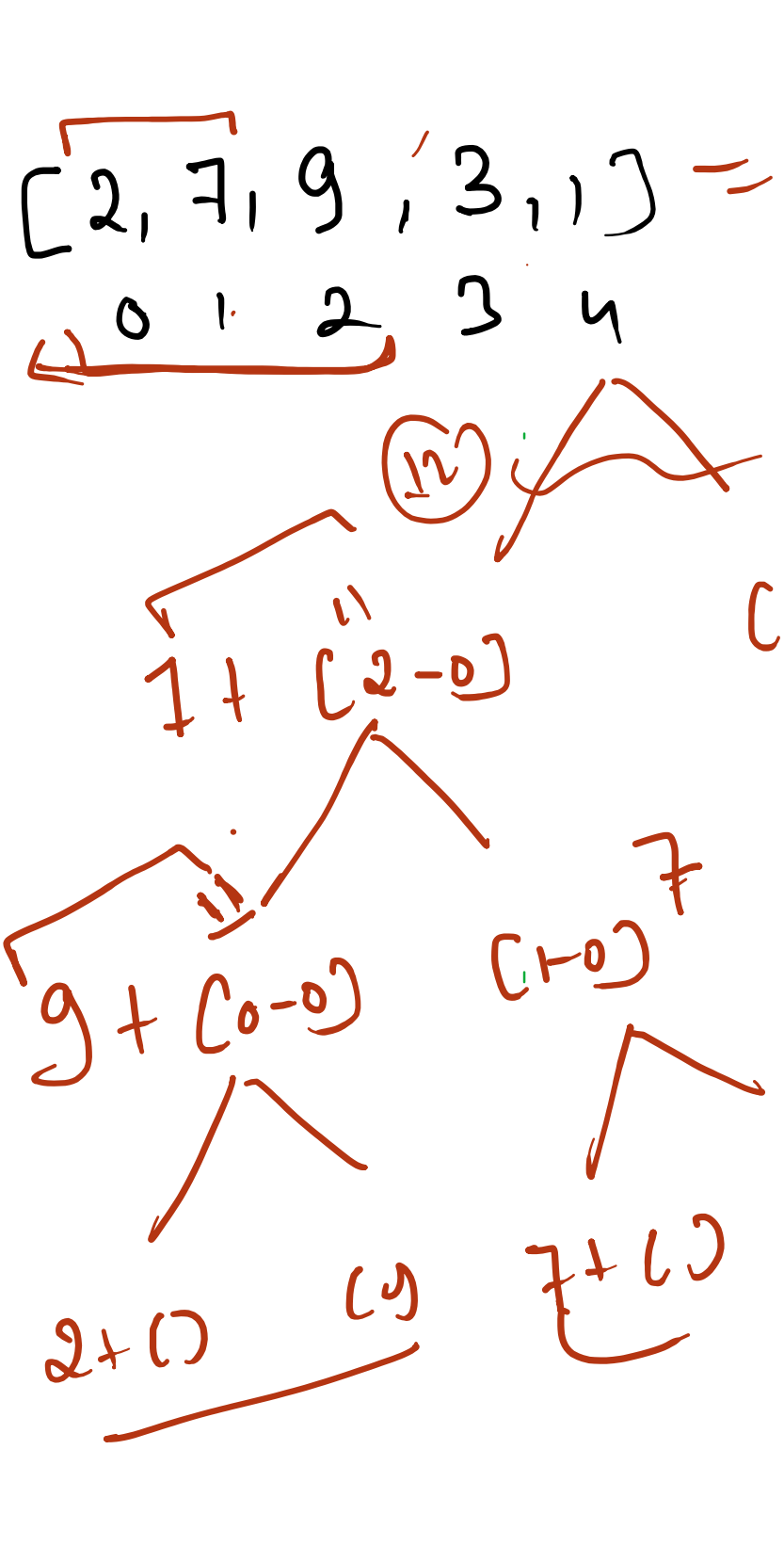
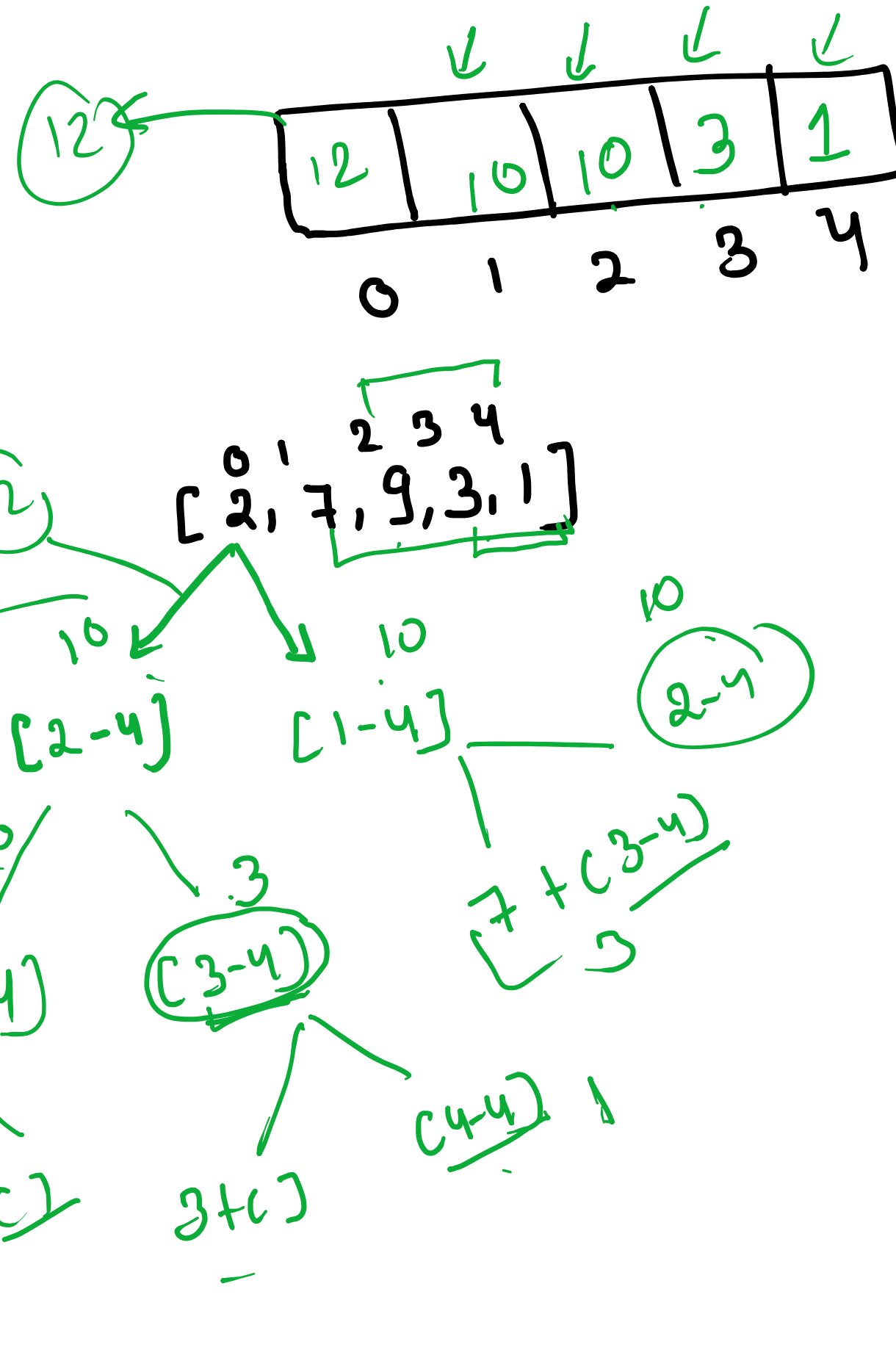


You are a professional robber planning to rob houses along a street. Each house has a certain amount of money stashed, the only constraint stopping you from robbing each of them is that adjacent houses have security systems connected and it will automatically contact the police if two adjacent houses were broken into on the same night.

Given an integer array `nums` representing the amount of money of each house, return the maximum amount of money you can rob tonight **without alerting the police**.



```
public static int Robber(int[] arr, int i) {
    if (i >= arr.length) {
        return 0;
    }
    int rob = arr[i] + Robber(arr, i + 2);
    int Dont_rob = Robber(arr, i + 1);
    return Math.max(rob, Dont_rob);
}
```



$dp[i] = \max(dp[i-1], arr[i] + dp[i-2])$

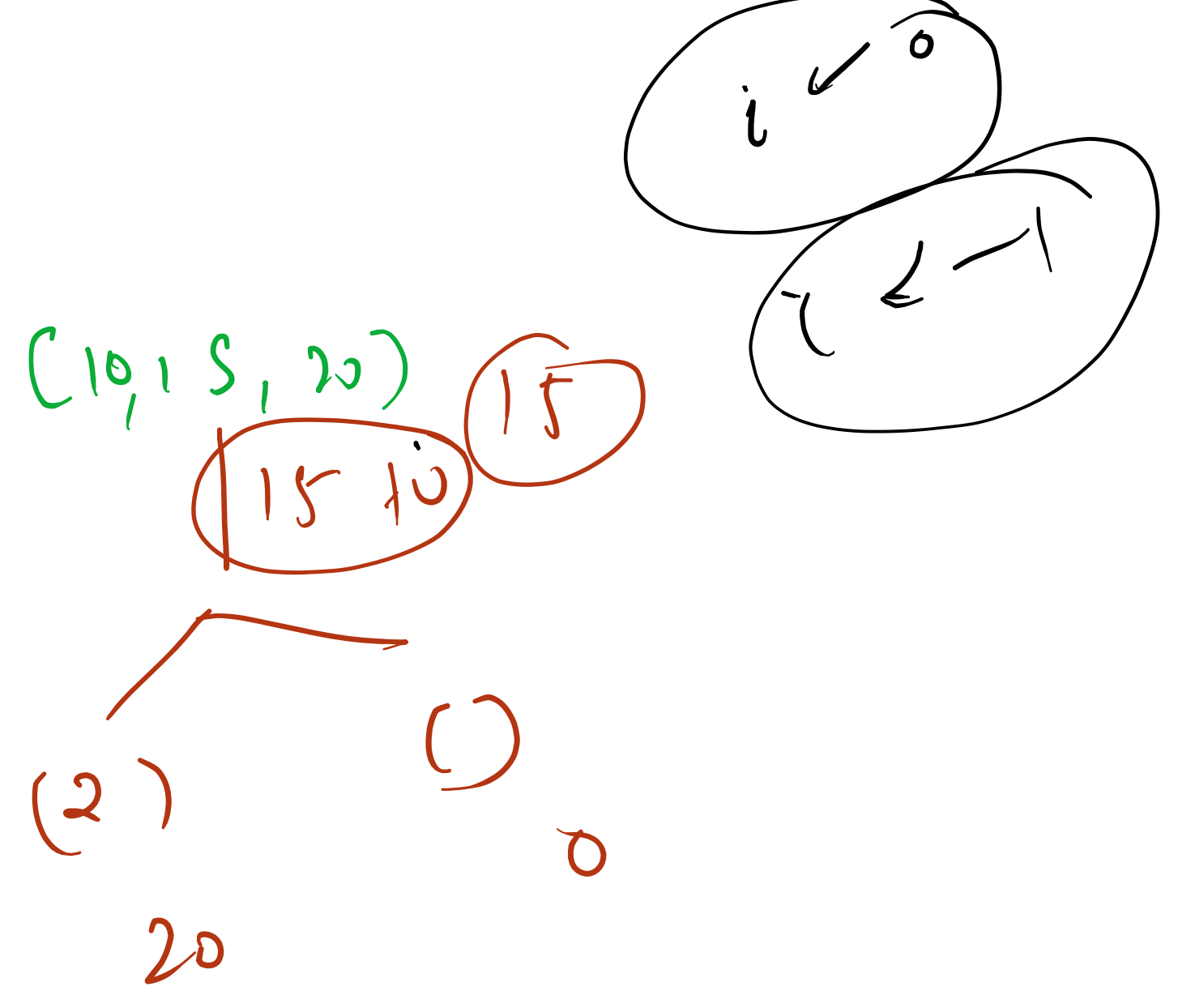
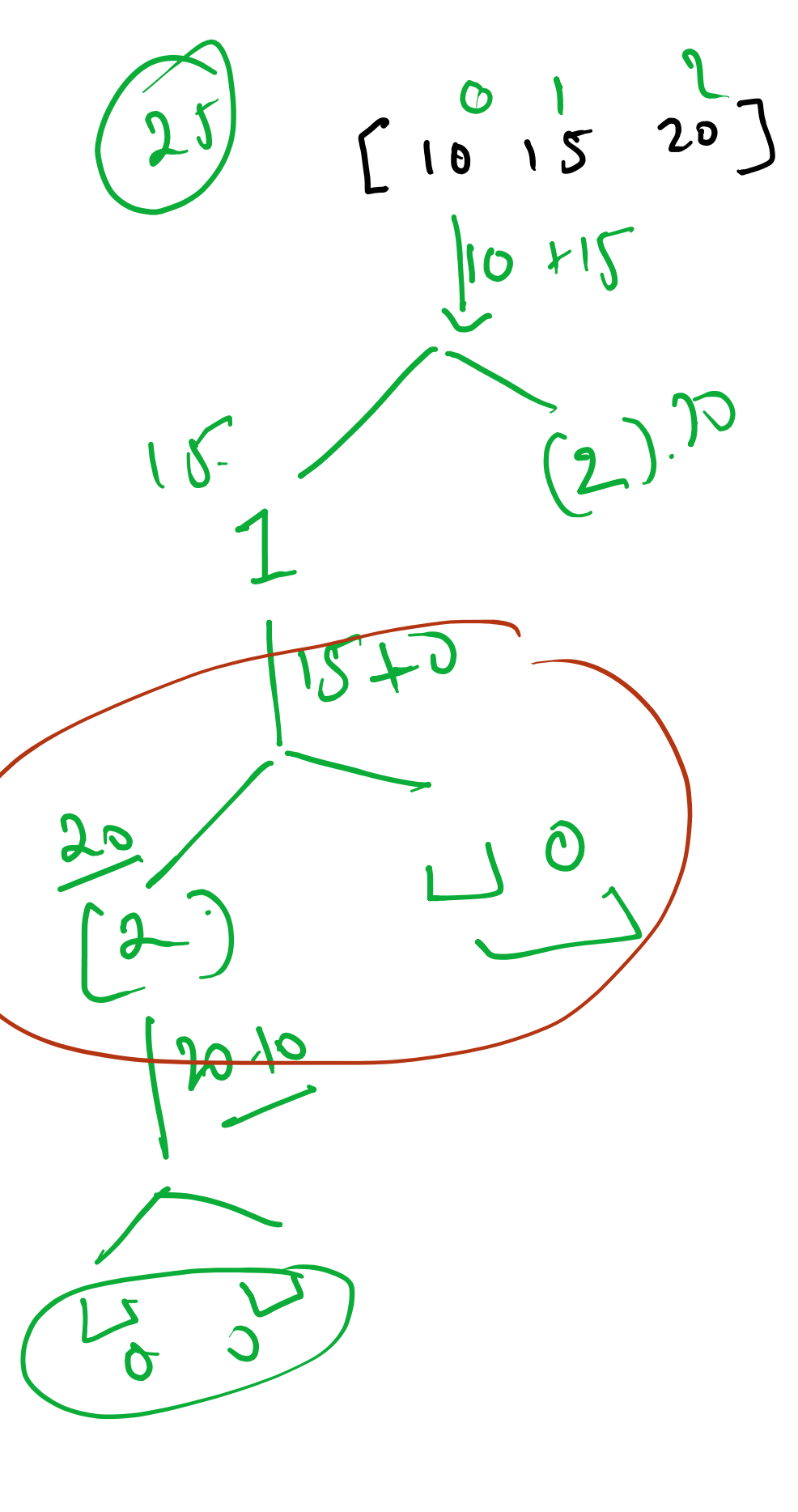
$dp[0] = 2$

$dp[1] = 7$

$dp[2] = 9$

$dp[3] = 3$

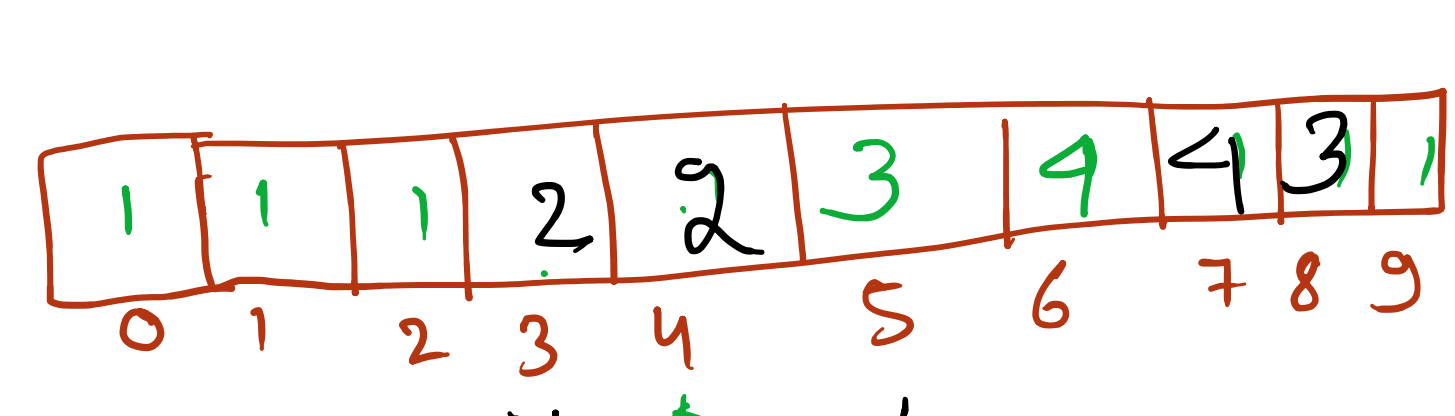
$dp[4] = 1$



Input: `nums = [10,9,2,5,3,7,101,18]`  
Output: 4  
Explanation: The longest increasing subsequence is `[2,3,7,101]`, therefore the length is 4.

10 101  
9 18  
9 101  
3 7 101  
5 7 101  
2 5 7 18  
2 5 7 101

5 4 3 2 1



10, 9, 2, 5, 3, 7, 101, 18, 6, 1

```
if (arr[j] < arr[i]) {
    int x = dp[j] + 1;
    dp[i] = Math.max(x, dp[i]);
}
```

