Fermat's Last Theorem

As we consider the Great Theorem of this chapter in our first reading, we'll also talk a bit more about one of the mathematicians we have mentioned a few times this semester: Pierre de Fermat. A little of Fermat's life story was mentioned in the first reading from Dunham in this chapter, as well as his famous "Last Theorem". Our second reading does a good job of explaining the basic ideas of the theorem and the history of its proof. Notice that Dunham's text was published before Wiles' proof! So, Dunham no longer correct that this is an unsolved problem in mathematics.

The article is still a little older than I'd like, however! Here is a bit more information to bring our story into the present.

- Since the article above was published pretty close to the publication of Wiles' proof, it ends with some uncertainty about the proof. That uncertainty has been removed - the proof has been reviewed and accepted.
- Wiles has since won a number of awards for his proof. Most recently, in 2016 he received the Abel Prize in Mathematics.
- Wiles' proof was essentially to verify a relevant case of the TaniyamaShimuraWeil conjecture. The full conjecture was proven in 2001, and is usually referred to as the "modularity theorem". The MathWorld article says a little more.
- Wiles originally gave the proof in about three lectures; now there are instances of entire courses being devoted to the matter. If you're interested in seeing more details for the proof, you can read a very short summary, a relatively short summary, or an entire textbook. You will likely need to have had a significant algebra course to understand much of the proof.
- The Wikipedia page for Fermat's Last Theorem is heavily referenced and also not a bad place to get general information about the theorem. (I know, I said you have to be careful with Wikipedia! Be sure to doublecheck the information in a non-open-source location.)

Author(s):

See Abel Prize at http://www.abelprize.no/

See MathWorld article http://mathworld.wolfram.com/

Taniyama-ShimuraConjecture.html

See a very short summary at https://www.math.wisc.edu/~boston/boston1.pdf See a relatively short summary at http://math.stanford.edu/~lekheng/flt/gouvea.pdf See an entire textbook at https://www.math.wisc.edu/~boston/869.pdf See Wikipedia page at https://en.wikipedia.org/wiki/Fermat's_Last_Theorem

Readings

First reading: Dunham, Chapter 7, pages 174 - 183 Second reading: Fermat's Last Theorem

Questions

Question 1 Into how many cases did Sophie Germain divide the problem? 2d given

Question 2 Where was Wiles working when he solved Fermat's Last Theorem?

Multiple Choice:

- (a) Stanford.
- (b) Princeton. ✓
- (c) Cambridge.
- (d) Oxford.

Question 3 What are the most important points from this reading?

Free Response:

See Fermat's Last Theorem at $http://www-history.mcs.st-andrews.ac.uk/HistTopics/Fermat's_last_theorem.html$