Competitive Programming Note

# Contents

T	使用场京	T
2	Segment Tree	2
3	Binary Indexed Tree	3
4	Sparse Table	4
5	莫隊	5
6	$\mathbf{D}\mathbf{S}\mathbf{U}$	6
7	PBDS & ROPE	7
8	拓樸排序	8
9	Floyd	9
10	Dijkstra	10
11	Bellman-Ford	11
<b>12</b>	Prime	<b>12</b>
13	Kruskal	13
14	Tarjan	14
15	<b>Kosaraju</b> 15.1 2-SAT	15 15
16	Eulerian Path	16
17	<b>占</b> 包	17

### 1 使用場景

• 區間修改、區間查詢:線段樹+懶人標記

• 區間修改、單點查詢:BIT+差分、線段樹+懶人標記

• 單點修改、區間查詢:線段樹、BIT

• 區間修改、沒有查詢:差分

• 區間查詢、沒有修改:前綴和、稀疏表

#### 2 Segment Tree

```
\#define lc id * 2 + 1
\#define rc id * 2 + 2
#define M ((L + R) \gg 1)
struct Nodes {
    Info info;
    Tag tag;
\} seg[N * 4];
void push(int L, int R, int id) {
    if (R > L + 1) {
        seg[lc].tag... seg[id].tag;
        seg[rc].tag... seg[id].tag;
                                      // Update the info from tag
    seg[id].info = ... seg[id].tag;
                                       // clear seg[id].tag
    seg[id].tag = NULL;
void pull(int L, int R, int id) {
    push(L, M, lc), push(M, R, rc);
    // Update the info of id from lc and rc
    seg[id].info = seg[lc].info... seg[rc].info;
void modify(int 1, int r, Tag tag, int L = 0, int R = n, int id = 0) {
    push (id);
    if (1 == L && r == R) {
        seg[id].tag = tag;
    } else {
        if (1 >= M)
            modify(1, r, tag, M, R, rc);
         else if (r = < M)
            modify(1, r, tag, L, M, lc);
         else
             modify(1, M, tag, L, M, 1c), modify(M, r, tag, M, R, rc);
         pull(id);
    }
Info query (int l, int r, int L = 0, int R = n, int id = 0) {
    push(id);
    if (1 = L \&\& r = R) return id.info;
    if (1 >= M) return query (1, r, M, R, rc);
    if (r <= M) return query(l, r, lc);</pre>
    // calculate answer from lc and rc
    return query(1, M, L, M, lc)... query(M, r, M, R, rc);
}
```

### 3 Binary Indexed Tree

```
struct BIT {
    vector < int > bit;
    int n;

BIT(int _n) {
        n = _n;
        bit.resize(n + 1);
    }

    void modify(int pos, int val) {
        for (; pos <= n; pos += pos & (-pos)) bit[pos] += val;
    }

    int query(int pos) {
        int ans = 0;
        for (; pos > 0; pos -= pos & (-pos)) ans += bit[pos];
        return ans;
    }
};
```

# 4 Sparse Table

### 5 莫隊

- 可以離線處理(沒有修改)
- 區間眾數、區間最大連續和、區間某個數字的數量

```
Range Pairing Query
int n, q, s;
struct qu {
    int l, r, id;
    bool operator < (const qu &B) const {
        if (1 / s != B.1 / s) return 1 < B.1;
        return (1 / s \& 1) ? r < B.r : r > B.r;
    }
};
signed main() {
    cin >> n;
    vector < int > arr(n + 1);
    for (int i = 1; i \le n; i++) cin >> arr[i];
    s = sqrt(n);
    cin >> q;
    vector < qu > qus(q);
    for (int i = 0; i < q; i++)
        cin >> qus[i].l >> qus[i].r, qus[i].id=i;
    sort(qus.begin(), qus.end());
    int l = 1, r = 1, p = 0;
    set < pair < int, int >> ans;
    vector < int > cur(n + 1);
    cur[arr[1]] = 1;
    for (qu i : qus) {
        while (i.r > r) {
             r++;
             if (cur[arr[r]] & 1) p++;
             cur [arr [r]]++;
        while (i.l > l) {
             cur [ arr [ 1]] --;
             if (cur[arr[1]] & 1) p--;
             1++;
        \mathbf{while} (i.r < r)  {
             cur [ arr [ r ]] --;
             if (cur[arr[r]] & 1) p--;
             r --;
        while (i.l < l)
             1--:
             if (cur[arr[1]] & 1) p++;
             cur[arr[1]]++;
        ans.insert(\{i.id, p\});
    for (auto i : ans) cout << i.second << '\n';
    return 0;
}
```

# 6 DSU

#### 7 PBDS & ROPE

```
#include <bits/extc++.h>
using namespace __gnu_pbds;
using namespace std;
template <class T>
using Tree =
     tree <\!\!T, null\_type \;, less <\!\!T\!\!>, rb\_tree\_tag \;, tree\_order\_statistics\_node\_update >\!\!;
template <class T>
using multiTree =
     tree<T, null_type, less_equal<T>, rb_tree_tag, tree_order_statistics_node_update>;
int main() {
    Tree<int> tr;
     tr.insert(1), tr.insert(8), tr.insert(3);
     // an iterator of the (k+1)th smallest element
     cout \ll *tr.find_by\_order(1) \ll '\n';
     // the number of elements are less than ktyl,
     cout \ll tr.order_of_key(6) \ll 'n';
     tr.erase(8);
     return 0;
#include <bits/extc++.h>
\mathbf{using} \ \mathbf{namespace} \ \_\_\mathtt{gnu\_cxx} \ ;
using namespace std;
int main() {
    rope < int > r, a, b;
                       // {10}
    b += 10;
                       // {2}
    r += 2;
                      // {2, 3}
// {2, 3, 2, 3, 10}
    r += 3;
    \mathbf{a} = \mathbf{r} + \mathbf{r} + \mathbf{b};
     for (int i : a) cout << i << '.';
     cout << '\n';
    b += a.substr(2, 3); // get 3 elements from a_2
     for (int i : b) cout << i << ', ';
    cout << \ `\n';
                           // {3}
    r.pop_back();
                           // empty
// {1}
    r.pop_front();
    r.push_back(1);
                           // {10, 1}
    r.push_front(10);
                           // replace r_1 to 100
    r.replace(1, 100);
                           // erase 1 element from 0
    r.erase(0, 1);
                           // insert 7 at r_-0
    r.insert(0, 7);
    for (int i : r) cout << i << '.';
}
```

# 8 拓樸排序

# 9 Floyd

# 10 Dijkstra

# 11 Bellman-Ford

# 12 Prime

# 13 Kruskal

# 14 Tarjan

### 15 Kosaraju

```
int id = 0;
int n, m;
vi g[100005], rg[100005], ord;
int idx[100005];
bool vis [100005], rvis [100005];
void dfs(int rt){
      if(vis[rt]) return;
       vis[rt] = 1;
      \quad \quad \mathbf{for} \left( \, \mathbf{int} \quad \mathbf{i} \quad : \quad \mathbf{g} \left[ \, \mathbf{rt} \, \right] \, \right) \quad \mathrm{dfs} \left( \, \mathbf{i} \, \right);
      ord.eb(rt);
}
void rdfs(int rt){
      if(rvis[rt]) return;
      rvis[rt] = 1;
      for(int i : rg[rt]) rdfs(i);
      idx[rt] = id;
}
signed main() {
      ios;
      cin >> n >> m;
      \operatorname{rep}\left(\,i\,\,,\,\,1\,,\,\,m\right)\ \left\{\,\,
             int a, b;
             cin >> a >> b;
             g[a].eb(b);
             rg[b].eb(a);
      rep(i, 1, n) dfs(i);
      reverse (all (ord));
      \mathbf{for}\left(\mathbf{int}\ \mathbf{i}\ :\ \mathrm{ord}\right)\ \mathbf{if}\left(!\,\mathrm{rvis}\left[\,\mathbf{i}\,\right]\right)\ \mathbf{id}++,\mathrm{rdfs}\left(\,\mathbf{i}\,\right);
      cout << id << '\n';
      rep(i, 1, n) cout << idx[i] << '.';
      return 0;
15.1
          2-SAT
     Each pair (a_i \vee b_i) generates two edges: \neg a_i \rightarrow b_i and \neg b_i \rightarrow a_i
   1. find SCC of G (use kosaraju can find topological ordering at the same time)
   2. for all x:
            if(x and \neg x in the same SCC) return IMPOSSIBLE
   3. for all x:
            if
(topological ordering \neg x > x) set x to true
            else set x to false
```

#### 16 Eulerian Path

```
int n, m, odd=1, ed=1, cnt_odd = 0;
int deg[100005];
vi g[100005], ans;
bool vis [100005];
map<pii, bool> evis;
void dfs(int rt){
    vis[rt] = 1;
    while (!g[rt].empty()) {
        int cur = g[rt].back();
        g[rt].pob();
        if (evis[{rt, cur}]) continue;
        evis[{rt, cur}] = 1, evis[{cur, rt}] = 1, dfs(cur);
        ans.eb(rt);
    }
}
signed main() {
    ios;
    cin >> n >> m;
    si cg;
    rep(i, 1, m){
        int a, b;
        cin >> a >> b;
        g[a].eb(b), g[b].eb(a);
        deg[a]++, deg[b]++;
        cg.insert(a), cg.insert(b);
    }
    rep(i, 1, n) if (deg[i]\&1) ed = odd, odd = i, cnt\_odd++;
    if(cnt_odd!=0) {
        cout << "IMPOSSIBLE\n";</pre>
        return 0;
    dfs (odd);
    for(int i : cg) if(!vis[i]) {
        cout <<"IMPOSSIBLE\n";
        return 0;
    reverse (all (ans));
    for(int i : ans) cout << i << '.';</pre>
    cout \ll ed \ll '\n';
    return 0;
}
```

17 凸包