# Homework 2: Higher-Order Functions

hw02.zip (hw02.zip)

Due by 11:59pm on Thursday, September 12

#### Instructions

Download <u>hw02.zip</u> (<u>hw02.zip</u>). Inside the archive, you will find a file called <u>hw02.py</u> (<u>hw02.py</u>), along with a copy of the ok autograder.

**Submission:** When you are done, submit the assignment by uploading all code files you've edited to Gradescope. You may submit more than once before the deadline; only the final submission will be scored. Check that you have successfully submitted your code on Gradescope. See <u>Lab 0 (../../lab/lab00#task-c-submitting-the-assignment)</u> for more instructions on submitting assignments.

**Using Ok:** If you have any questions about using Ok, please refer to <u>this guide</u>. (../../articles/using-ok)

**Readings:** You might find the following references useful:

• <u>Section 1.6 (https://www.composingprograms.com/pages/16-higher-order-functions.html)</u>

**Grading:** Homework is graded based on correctness. Each incorrect problem will decrease the total score by one point. **This homework is out of 2 points.** 

## Required Questions

**Getting Started Videos** 

Several doctests refer to these functions:

https://cs61a.org/hw/hw02/

```
from operator import add, mul
square = lambda x: x * x

identity = lambda x: x

triple = lambda x: 3 * x

increment = lambda x: x + 1
```

### **Higher-Order Functions**

#### Q1: Product

Write a function called product that returns the product of the first n terms of a sequence. Specifically, product takes in an integer n and term, a single-argument function that determines a sequence. (That is, term(i) gives the i th term of the sequence.) product(n, term) should return term(1) \* ... \* term(n).

```
def product(n, term):
    """Return the product of the first n terms in a sequence.

n: a positive integer
    term: a function that takes one argument to produce the term

>>> product(3, identity) # 1 * 2 * 3
6
>>> product(5, identity) # 1 * 2 * 3 * 4 * 5
120
>>> product(3, square) # 1^2 * 2^2 * 3^2
36
>>> product(5, square) # 1^2 * 2^2 * 3^2 * 4^2 * 5^2
14400
>>> product(3, increment) # (1+1) * (2+1) * (3+1)
24
>>> product(3, triple) # 1*3 * 2*3 * 3*3
162
"""
"*** YOUR CODE HERE ***"
```

https://cs61a.org/hw/hw02/ 2/7

Use Ok to test your code:

#### Q2: Accumulate

Let's take a look at how product is an instance of a more general function called accumulate, which we would like to implement:

```
def accumulate(fuse, start, n, term):
    """Return the result of fusing together the first n terms in a sequence
    and start. The terms to be fused are term(1), term(2), ..., term(n).
    The function fuse is a two-argument commutative & associative function.

>>> accumulate(add, 0, 5, identity) # 0 + 1 + 2 + 3 + 4 + 5

15

>>> accumulate(add, 11, 5, identity) # 11 + 1 + 2 + 3 + 4 + 5

26

>>> accumulate(add, 11, 0, identity) # 11 (fuse is never used)

11

>>> accumulate(add, 11, 3, square) # 11 + 1^2 + 2^2 + 3^2

25

>>> accumulate(mul, 2, 3, square) # 2 * 1^2 * 2^2 * 3^2

72

>>> # 2 + (1^2 + 1) + (2^2 + 1) + (3^2 + 1)

>>> accumulate(lambda x, y: x + y + 1, 2, 3, square)

19

"**** YOUR CODE HERE ***"
```

accumulate has the following parameters:

- fuse: a two-argument function that specifies how the current term is fused with the previously accumulated terms
- start : value at which to start the accumulation
- n: a non-negative integer indicating the number of terms to fuse
- term: a single-argument function; term(i) is the i th term of the sequence

Implement accumulate, which fuses the first n terms of the sequence defined by term with the start value using the fuse function.

For example, the result of accumulate(add, 11, 3, square) is

https://cs61a.org/hw/hw02/ 3/7

```
add(11, add(square(1), add(square(2), square(3)))) =
11 + square(1) + square(2) + square(3) =
11 + 1 + 4 + 9 = 25
```

```
Assume that fuse is commutative, fuse(a, b) == fuse(b, a), and associative, fuse(fuse(a, b), c) == fuse(a, fuse(b, c)).
```

Then, implement summation (from lecture) and product as one-line calls to accumulate.

**Important:** Both summation\_using\_accumulate and product\_using\_accumulate should be implemented with a single line of code starting with return.

```
def summation_using_accumulate(n, term):
           """Returns the sum: term(1) + ... + term(n), using accumulate.
           >>> summation_using_accumulate(5, square) # square(1) + square(2) + ... + square(4) +
           55
           >>> summation_using_accumulate(5, triple) # triple(1) + triple(2) + ... + triple(4) +
           45
           >>> # This test checks that the body of the function is just a return statement.
           >>> import inspect, ast
           >>> [type(x).__name__ for x in ast.parse(inspect.getsource(summation_using_accumulate)
           ['Expr', 'Return']
           return ____
def product_using_accumulate(n, term):
           """Returns the product: term(1) * ... * term(n), using accumulate.
           >>> product_using_accumulate(4, square) # square(1) * square(2) * square(3) * square()
           576
           >>> product_using_accumulate(6, triple) # triple(1) * triple(2) * ... * triple(5) * triple(5) * triple(5) * triple(6, triple) # triple(1) * triple(1) * ... * triple(5) * triple(1) * triple(1) * ... * triple(2) * ... * triple(5) * triple(1) * ... * triple(1) * ... * triple(2) * ... * triple(3) * ... * triple(5) * triple(1) * ... * triple(1) * ... * triple(2) * ... * triple(3) * ... * triple(5) * ... * ... * triple(5) * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... * ... 
           524880
           >>> # This test checks that the body of the function is just a return statement.
           >>> import inspect, ast
           >>> [type(x).__name__ for x in ast.parse(inspect.getsource(product_using_accumulate)).
           ['Expr', 'Return']
           return ___
```

Use Ok to test your code:

https://cs61a.org/hw/hw02/ 4/7

```
python3 ok -q accumulate
python3 ok -q summation_using_accumulate
python3 ok -q product_using_accumulate
```

#### Q3: Make Repeater

Implement the function make\_repeater which takes a one-argument function f and a positive integer n. It returns a one-argument function, where make\_repeater(f, n)(x) returns the value of f(f(...f(x)...)) in which f is applied n times to x. For example, make\_repeater(square, 3)(5) squares 5 three times and returns 390625, just like square(square(5))).

```
def make_repeater(f, n):
    """Returns the function that computes the nth application of f.

>>> add_three = make_repeater(increment, 3)
    >>> add_three(5)
    8

>>> make_repeater(triple, 5)(1) # 3 * (3 * (3 * (3 * 1))))
    243

>>> make_repeater(square, 2)(5) # square(square(5))
625

>>> make_repeater(square, 3)(5) # square(square(square(5)))
390625
"""

"*** YOUR CODE HERE ***"
```

Use Ok to test your code:

```
python3 ok -q make_repeater
```

### **Check Your Score Locally**

You can locally check your score on each question of this assignment by running

```
python3 ok --score
```

This does NOT submit the assignment! When you are satisfied with your score, submit the assignment to Gradescope to receive credit for it.

https://cs61a.org/hw/hw02/ 5/7

## Submit Assignment

Submit this assignment by uploading any files you've edited **to the appropriate Gradescope assignment.** <u>Lab 00 (../../lab/lab00/#submit-with-gradescope)</u> has detailed instructions.

## [Optional] Exam Practice

Here are some related questions from past exams for you to try. These are optional. There is no way to submit them.

- 1. Fall 2019 MT1 Q3: You Again (https://cs61a.org/exam/fa19/mt1/61a-fa19-mt1.pdf#page=4) [Higher-Order Functions]
- 2. Fall 2021 MT1 Q1b: <u>tik (https://cs61a.org/exam/fa21/mt1/61a-fa21-mt1.pdf#page=4)</u> [Functions and Expressions]

https://cs61a.org/hw/hw02/

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