Lab 2 Solutions [lab02.zip (lab02.zip)]

Solution Files

Topics

Consult this section if you need a refresher on the material for this lab. It's okay to skip directly to <u>the questions</u> and refer back here should you get stuck.

Required Questions

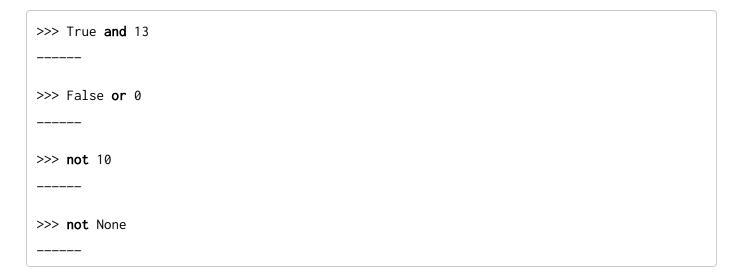
What Would Python Display?

Important: For all WWPD questions, type Function if you believe the answer is <function...>, Error if it errors, and Nothing if nothing is displayed.

Q1: WWPD: The Truth Will Prevail

Use Ok to test your knowledge with the following "What Would Python Display?" questions:

python3 ok -q short-circuit -u



```
>>> True and 1 / 0
-----
>>> True or 1 / 0
-----
>>> -1 and 1 > 0
-----
>>> -1 or 5
-----
>>> (1 + 1) and 1
-----
>>> print(3) or ""
```

```
>>> def f(x):
... if x == 0:
... return "zero"
... elif x > 0:
... return "positive"
... else:
... return ""
>>> 0 or f(1)
-----
>>> f(0) or f(-1)
------
>>> f(0) and f(-1)
```

Q2: WWPD: Higher-Order Functions

Use Ok to test your knowledge with the following "What Would Python Display?" questions:

python3 ok -q hof-wwpd -u

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```
>>> def cake():
... print('beets')
     def pie():
          print('sweets')
. . .
          return 'cake'
... return pie
>>> chocolate = cake()
>>> chocolate
>>> chocolate()
>>> more_chocolate, more_cake = chocolate(), cake
>>> more_chocolate
>>> def snake(x, y):
... if cake == more_cake:
           return chocolate
     else:
. . .
           return x + y
>>> snake(10, 20)
>>> snake(10, 20)()
>>> cake = 'cake'
>>> snake(10, 20)
```

Q3: WWPD: Lambda

Use Ok to test your knowledge with the following "What Would Python Display?"

```
questions:
                                                                                     QD
 python3 ok -q lambda -u
As a reminder, the following two lines of code will not display any output in the
interactive Python interpreter when executed:
 >>> x = None
 >>> x
 >>>
```

```
>>> lambda x: x # A lambda expression with one parameter x
>>> a = lambda x: x \# Assigning the lambda function to the name a
>>> a(5)
>>> (lambda: 3)() # Using a lambda expression as an operator in a call exp.
>>> b = lambda x, y: lambda: x + y # Lambdas can return other lambdas!
>>> c = b(8, 4)
>>> c
>>> c()
>>> d = lambda f: f(4) \# They can have functions as arguments as well.
>>> def square(x):
        return x * x
>>> d(square)
```

Coding Practice

Q4: Composite Identity Function

Write a function that takes in two single-argument functions, f and g, and returns another **function** that has a single parameter x. The returned function should return True if f(g(x)) is equal to g(f(x)) and False otherwise. You can assume the output of g(x) is a valid input for f and vice versa.

```
def composite_identity(f, g):
    Return a function with one parameter x that returns True if f(g(x)) is
    equal to g(f(x)). You can assume the result of g(x) is a valid input for f
    and vice versa.
   >>> add one = lambda x: x + 1
                                        # adds one to x
   >>> square = lambda x: x**2
                                        # squares x [returns x^2]
   >>> b1 = composite_identity(square, add_one)
   >>> b1(0)
                                         \# (0 + 1) ** 2 == 0 ** 2 + 1
   True
                                         # (4 + 1) ** 2 != 4 ** 2 + 1
   >>> b1(4)
   False
    return lambda x: f(g(x)) == g(f(x))
   # Alternate solution:
    def h(x):
        return f(g(x)) == g(f(x))
    return h
```

We must create a function to take x using lambda or def, then compare the two quantities. Use Ok to test your code:

Q5: Count Cond

Consider the following implementations of count_fives and count_primes which use the sum_digits and is_prime functions from earlier assignments:

```
def count_fives(n):
    """Return the number of values i from 1 to n (including n)
    where sum_digits(n * i) is 5.
    >>> count_fives(10) # Among 10, 20, 30, ..., 100, only 50 (10 * 5) has digit sum 5
   >>> count_fives(50) # 50 (50 * 1), 500 (50 * 10), 1400 (50 * 28), 2300 (50 * 46)
    11 11 11
    i = 1
    count = 0
    while i <= n:</pre>
        if sum_digits(n * i) == 5:
            count += 1
        i += 1
    return count
def count_primes(n):
    """Return the number of prime numbers up to and including n.
   >>> count_primes(6)
                         # 2, 3, 5
   >>> count_primes(13) # 2, 3, 5, 7, 11, 13
    6
    11 11 11
    i = 1
    count = 0
    while i <= n:</pre>
        if is_prime(i):
            count += 1
        i += 1
    return count
```

The implementations look quite similar! Generalize this logic by writing a function count_cond, which takes in a two-argument predicate function condition(n, i). count_cond returns a one-argument function that takes in n, which counts all the numbers from 1 to n that satisfy condition when called.

Note: When we say condition is a predicate function, we mean that it is a function that will return True or False.

```
def sum_digits(y):
    """Return the sum of the digits of non-negative integer y."""
   while y > 0:
       total, y = total + y % 10, y // 10
    return total
def is_prime(n):
    """Return whether positive integer n is prime."""
   if n == 1:
       return False
   k = 2
   while k < n:</pre>
       if n % k == 0:
           return False
       k += 1
    return True
def count_cond(condition):
    """Returns a function with one parameter N that counts all the numbers from
    1 to N that satisfy the two-argument predicate function Condition, where
    the first argument for Condition is N and the second argument is the
    number from 1 to N.
   >>> count_fives = count_cond(lambda n, i: sum_digits(n * i) == 5)
   >>> count_fives(10) # 50 (10 * 5)
   >>> count_fives(50) # 50 (50 * 1), 500 (50 * 10), 1400 (50 * 28), 2300 (50 * 46)
   >>> is_i_prime = lambda n, i: is_prime(i) # need to pass 2-argument function into cour
   >>> count_primes = count_cond(is_i_prime)
   >>> count_primes(2)
                          # 2
    1
   >>> count_primes(3)
                        # 2, 3
   >>> count_primes(4)
                         # 2, 3
   >>> count_primes(5) # 2, 3, 5
   >>> count_primes(20)  # 2, 3, 5, 7, 11, 13, 17, 19
    def counter(n):
       i = 1
```

```
count = 0
while i <= n:
    if condition(n, i):
        count += 1
    i += 1
return count</pre>
```

One question that might be nice to ask is: in what ways is the logic for count_fives and count_primes similar, and in what ways are they different?

The answer to the first question can tell us the logic that we want to include in our count_cond function, while the answer to the second question can tell us where in count_cond we want to be able to have the difference in behavior observed between count_fives and count_primes.

It'll be helpful to also keep in mind that we want <code>count_cond</code> to return a function that, when an argument <code>n</code> is passed in, will behave similarly to <code>count_fives</code> or <code>count_primes</code>. In other words, <code>count_cond</code> is a higher order function that returns a function, that then <code>contains</code> the <code>logic common to both <code>count_fives</code> and <code>count_primes</code>.</code>

Use Ok to test your code:

```
python3 ok -q count_cond
```

Check Your Score Locally

You can locally check your score on each question of this assignment by running

```
python3 ok --score
```

This does NOT submit the assignment! When you are satisfied with your score, submit the assignment to Gradescope to receive credit for it.

Submit Assignment

If you are in a regular section of CS 61A, fill out this <u>lab attendance and feedback form</u> (https://forms.gle/dHxj8gttNWRY6Ptm9). (If you are in the mega section, you don't need to fill out the form.)

Then, submit this assignment by uploading any files you've edited **to the appropriate Gradescope assignment.** Lab 00 (../lab00/#submit-with-gradescope) has detailed instructions.

Environment Diagram Practice

There is no Gradescope submission for this component.

However, we still encourage you to do this problem on paper to develop familiarity with Environment Diagrams, which might appear in an alternate form on the exam. To check your work, you can try putting the code into PythonTutor.

Q6: HOF Diagram Practice

Draw the environment diagram that results from executing the code below on paper or a whiteboard. Use <u>tutor.cs61a.org</u> (<u>https://tutor.cs61a.org</u>) to check your work.

```
n = 7

def f(x):
    n = 8
    return x + 1

def g(x):
    n = 9
    def h():
        return x + 1
    return h

def f(f, x):
    return f(x + n)

f = f(g, n)
g = (lambda y: y())(f)
```

Optional Questions

These questions are optional. If you don't complete them, you will still receive credit for this assignment. They are great practice, so do them anyway!

Q7: Multiple

Write a function that takes in two numbers and returns the smallest number that is a multiple of both.

```
def multiple(a, b):
    """Return the smallest number n that is a multiple of both a and b.

>>> multiple(3, 4)
    12
    >>> multiple(14, 21)
    42
    """
    n = 1
    while True:
        if n % a == 0 and n % b == 0:
            return n
        n += 1
```

Use Ok to test your code:

```
python3 ok -q multiple
```

Q8: I Heard You Liked Functions...

Define a function cycle that takes in three functions f1, f2, and f3, as arguments. cycle will return another function g that should take in an integer argument n and return another function h. That final function h should take in an argument x and cycle through applying

f1, f2, and f3 to x, depending on what n was. Here's what the final function h should do to x for a few values of n:

- n = 0, return x
- n = 1, apply f1 to x, or return f1(x)
- n = 2, apply f1 to x and then f2 to the result of that, or return f2(f1(x))
- n = 3, apply f1 to x, f2 to the result of applying f1, and then f3 to the result of applying f2, or f3(f2(f1(x)))
- n = 4, start the cycle again applying f1, then f2, then f3, then f1 again, or f1(f3(f2(f1(x))))
- And so forth.

Hint: most of the work goes inside the most nested function.

```
def cycle(f1, f2, f3):
    """Returns a function that is itself a higher-order function.
   >>> def add1(x):
            return x + 1
   >>> def times2(x):
           return x * 2
    . . .
   >>> def add3(x):
           return x + 3
   >>> my_cycle = cycle(add1, times2, add3)
   >>> identity = my_cycle(0)
   >>> identity(5)
   >>> add_one_then_double = my_cycle(2)
   >>> add_one_then_double(1)
   >>> do_all_functions = my_cycle(3)
   >>> do_all_functions(2)
   >>> do_more_than_a_cycle = my_cycle(4)
   >>> do_more_than_a_cycle(2)
   10
   >>> do_two_cycles = my_cycle(6)
   >>> do_two_cycles(1)
   19
    11 11 11
   def g(n):
        def h(x):
            i = 0
            while i < n:
                if i % 3 == 0:
                    x = f1(x)
                elif i % 3 == 1:
                    x = f2(x)
                else:
                    x = f3(x)
                i += 1
            return x
        return h
    return g
   # Alternative recursive solution
    def g(n):
        def h(x):
            if n == 0:
```

```
return x
    return cycle(f2, f3, f1)(n - 1)(f1(x))
    return h
return g
```

There are three main pieces of information we need in order to calculate the value that we want to return.

- 1. The three functions that we will be cycling through, so f1, f2, f3.
- 2. The number of function applications we need, namely n. When n is 0, we want our function to behave like the identity function (i.e. return the input without applying any of our three functions to it).
- 3. The input that we start off with, namely x.

The functions are the parameters passed into cycle. We want the return value of cycle to be a function ret_fn that takes in n and outputs another function ret. ret is a function that takes in x and then will cyclically apply the three passed in functions to the input until we have reached n applications. Thus, most of the logic will go inside of ret.

Solution:

To figure out which function we should next use in our cycle, we can use the mod operation via %, and loop through the function applications until we have made exactly n function applications to our original input x.

Use Ok to test your code:

python3 ok -q cycle