



Next:

Wall following
PID control

Perception – Wall following

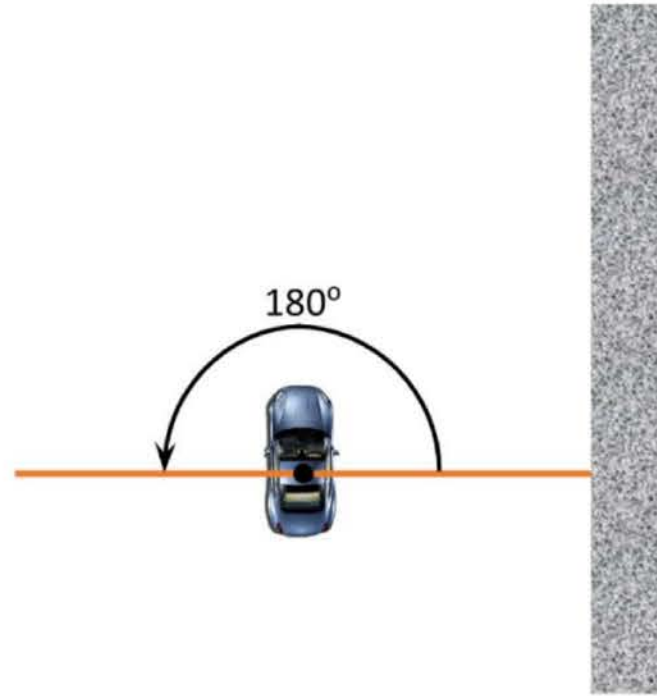
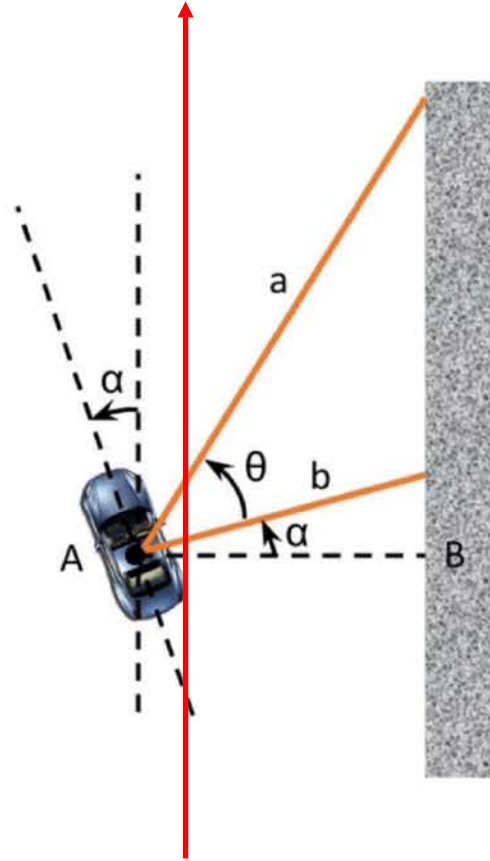


Figure 1: Lidar scan angles

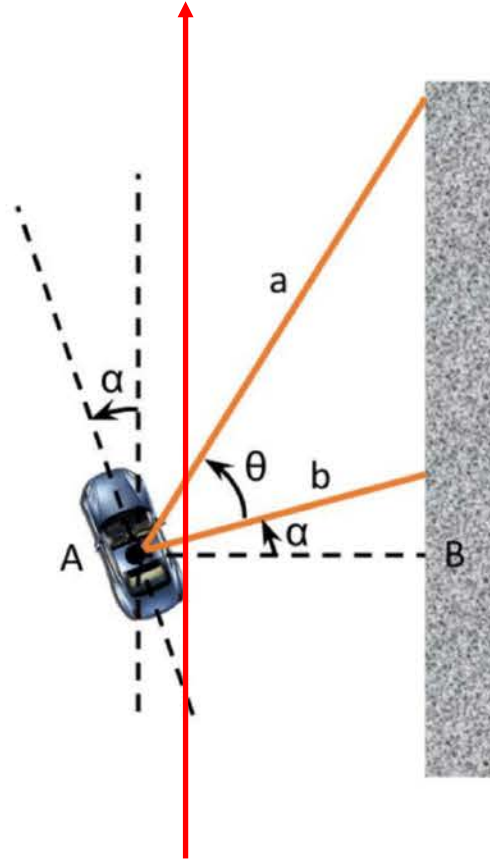
Pick two LIDAR rays facing right – One at 0° and one at θ°



$$\alpha = \tan^{-1}\left(\frac{a \cos(\theta) - b}{a \sin(\theta)}\right)$$

$$AB = b \cos(\alpha)$$

Pick two LIDAR rays facing right – One at 0° and one at θ°

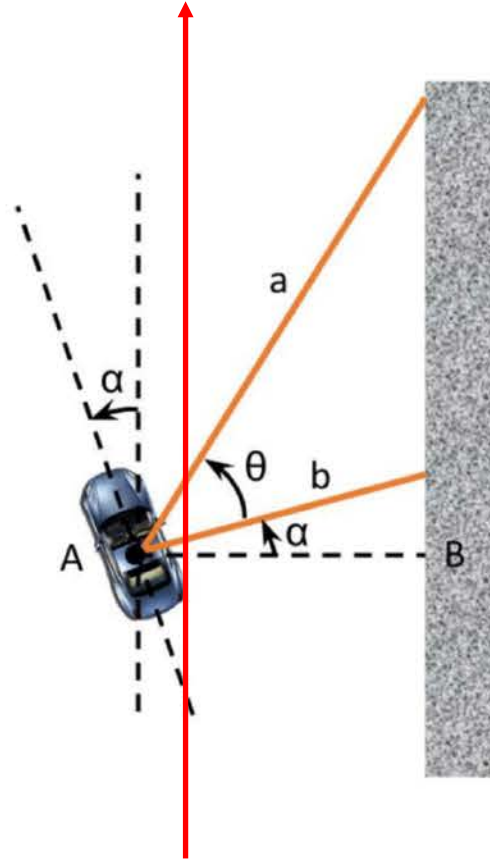


$$\alpha = \tan^{-1}\left(\frac{a \cos(\theta) - b}{a \sin(\theta)}\right)$$

$$AB = b \cos(\alpha)$$

Error = desired trajectory – AB ?

Pick two LIDAR rays facing right – One at 0° and one at θ°



$$\alpha = \tan^{-1}\left(\frac{a \cos(\theta) - b}{a \sin(\theta)}\right)$$

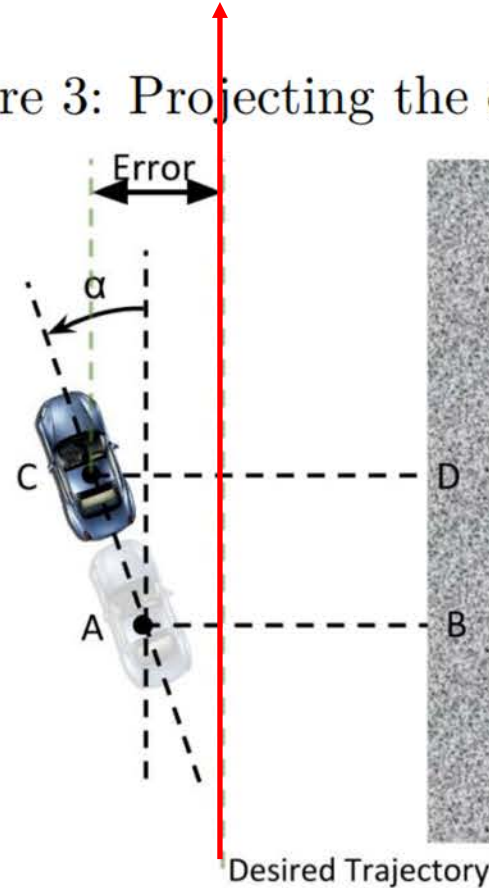
$$AB = b \cos(\alpha)$$

Error = desired trajectory – AB ?

Not quite

Account for the forward motion of the car

Figure 3: Projecting the car future in time



$$\alpha = \tan^{-1}\left(\frac{a \cos(\theta) - b}{a \sin(\theta)}\right)$$

$$AB = b \cos(\alpha)$$

$$CD = AB + AC \sin(\alpha)$$

$$\text{Error} = \text{desired trajectory} - CD$$

PID Steering Control

$$V_{\theta} = K_p \times e(t) + K_d \frac{de(t)}{dt}$$

$$V_{\theta} = K_p \times \text{error} + K_d \times \text{previous error} - \text{current error}$$

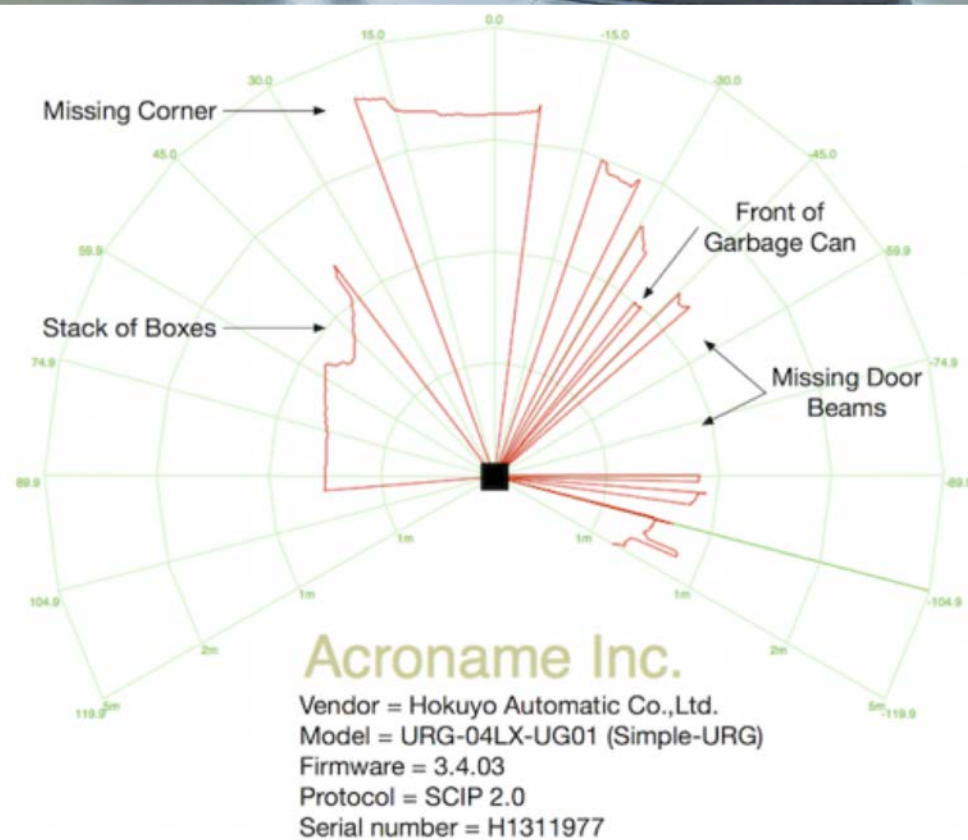
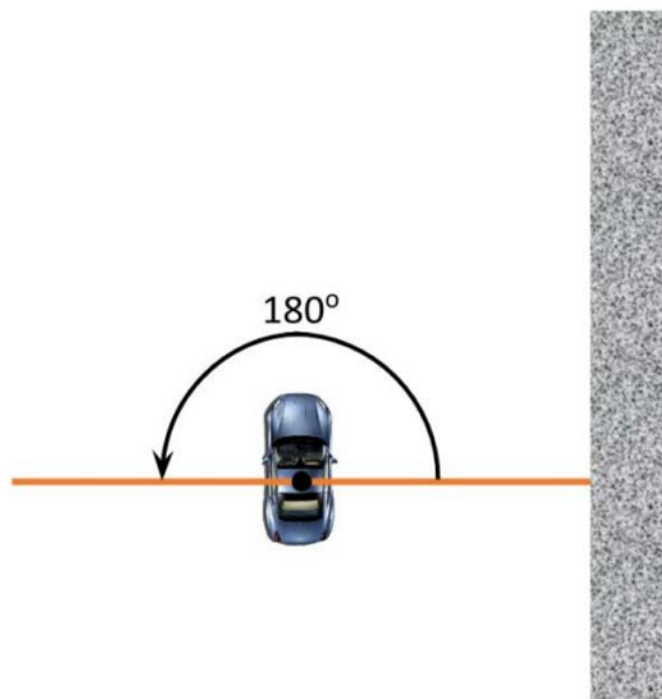
$$\text{steering angle} = \text{steering angle} - V_{\theta}$$



Field of View

← Assumption

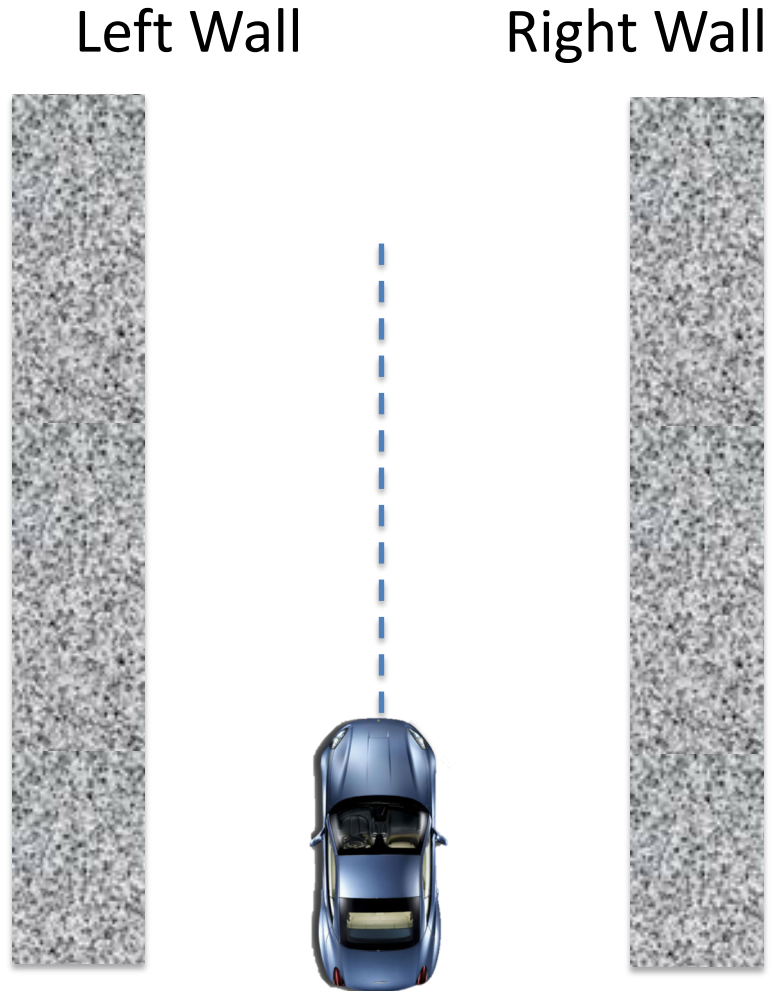
Reality →



Control

Proportional, Integral, Derivative control

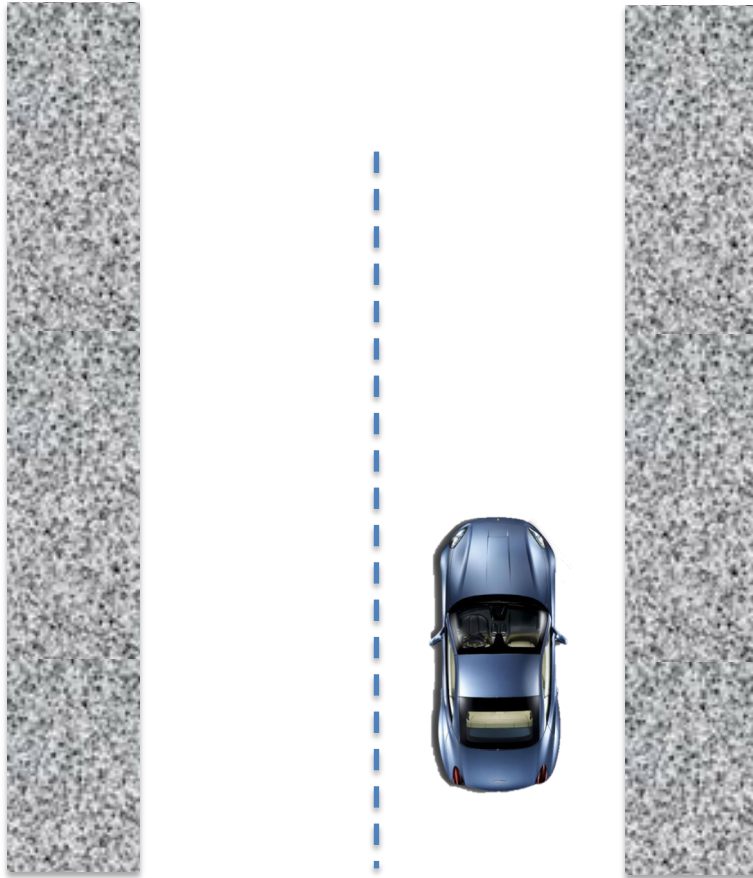
PID control: objectives



Control objective:

- 1) keep the car driving along the centerline,
- 2) parallel to the walls.

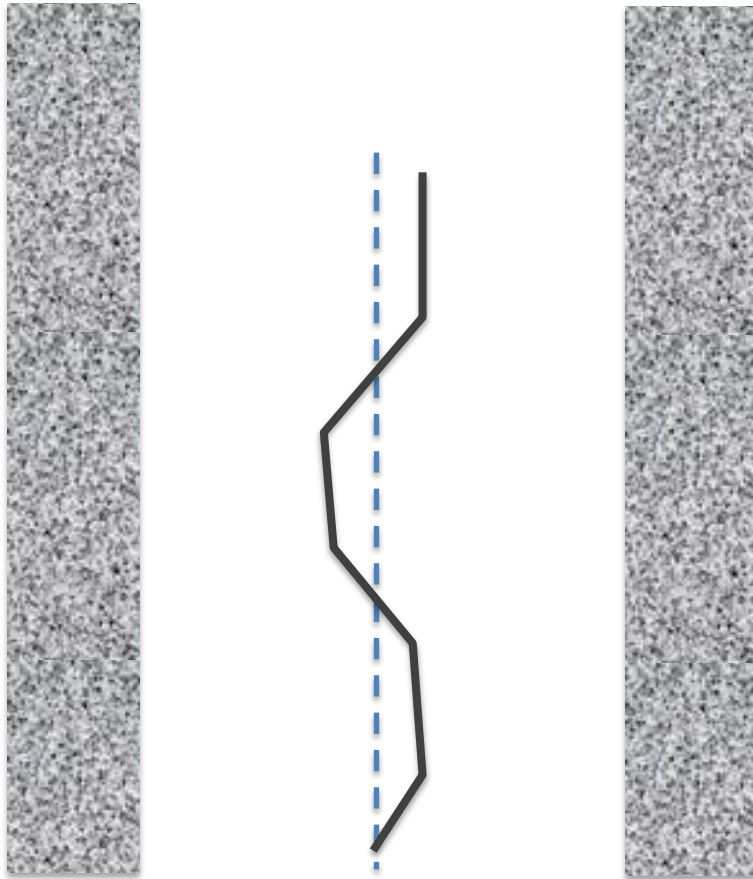
PID control: objectives



Control objective:

- ~~1) keep the car driving along the centerline,~~
- 2) parallel to the walls.

PID control: objectives

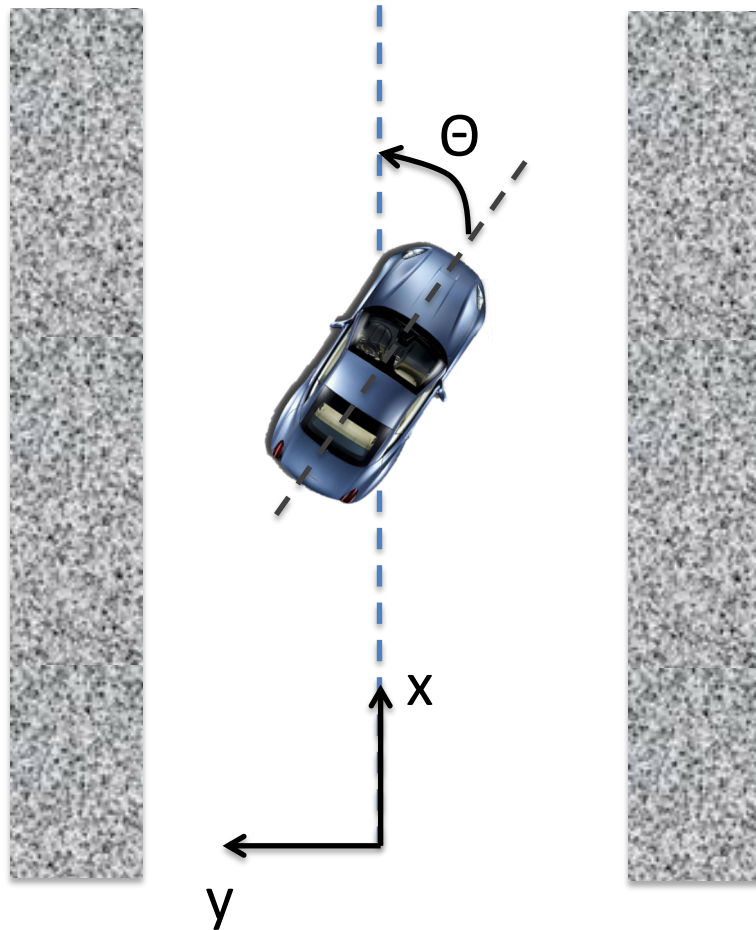


Control objective:

1) keep the car driving (roughly) along the centerline,

~~2) parallel to the walls.~~

PID control: control objectives



Control objective:

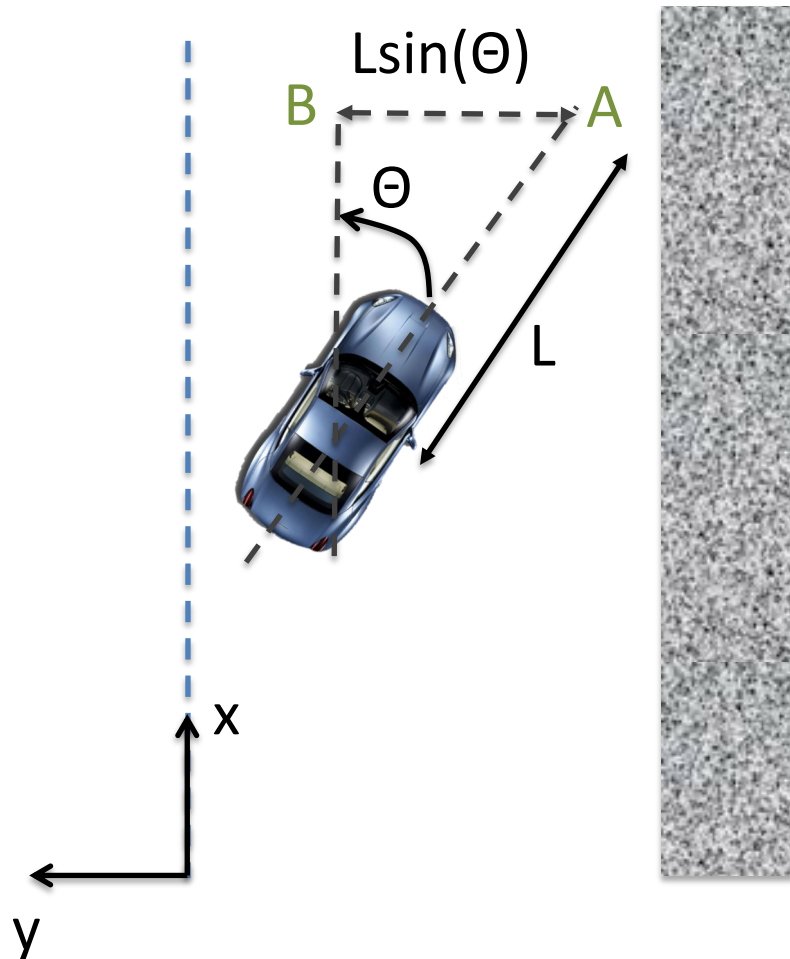
1) keep the car driving along the centerline,

$$y = 0$$

2) parallel to the walls.

$$\Theta = 0$$

PID control: control objectives



Control objective:

1) keep the car driving along the centerline,

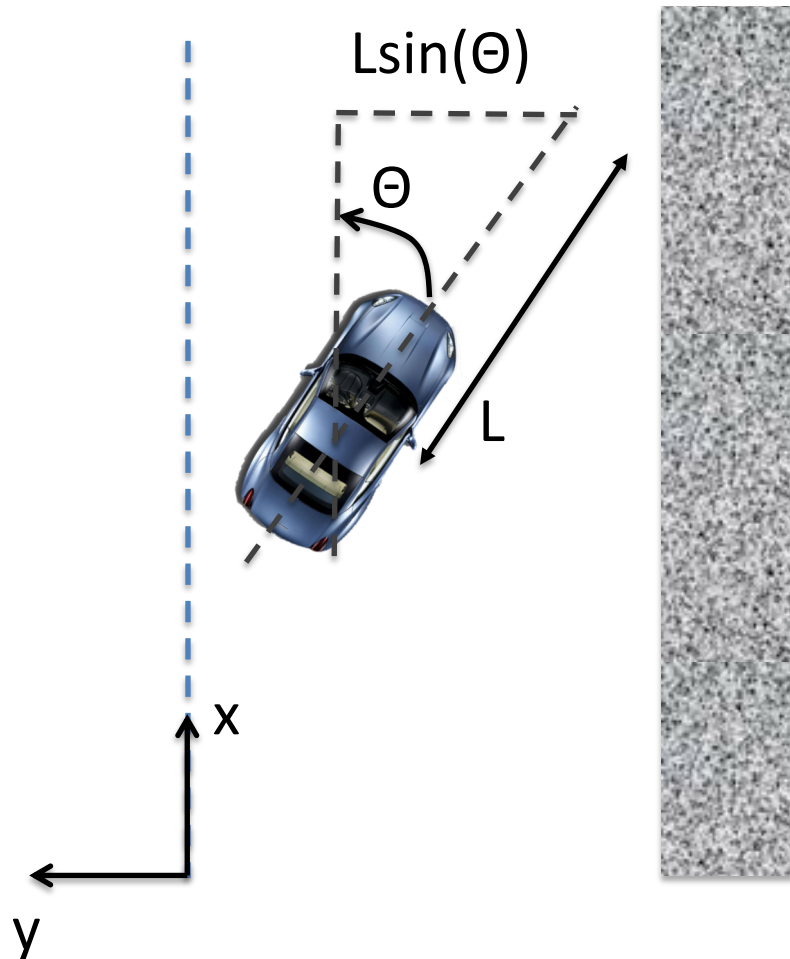
$$y = 0$$

2) After driving L meters, it is still on the centerline:

Horizontal distance after driving L meters

$$L\sin(\Theta) = 0$$

PID control: control inputs



Control input:
Steering angle Θ

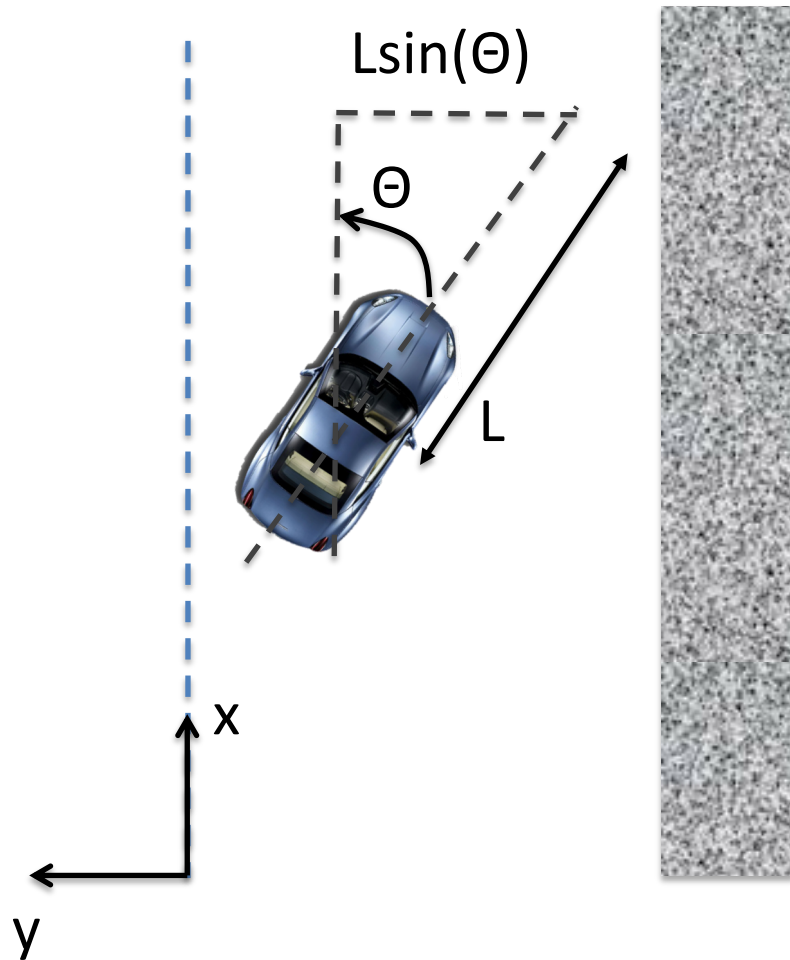
We will hold the velocity constant.

How do we control the steering angle
to keep

$$y = 0, L\sin(\Theta) = 0$$

as much as possible?

PID control: error term

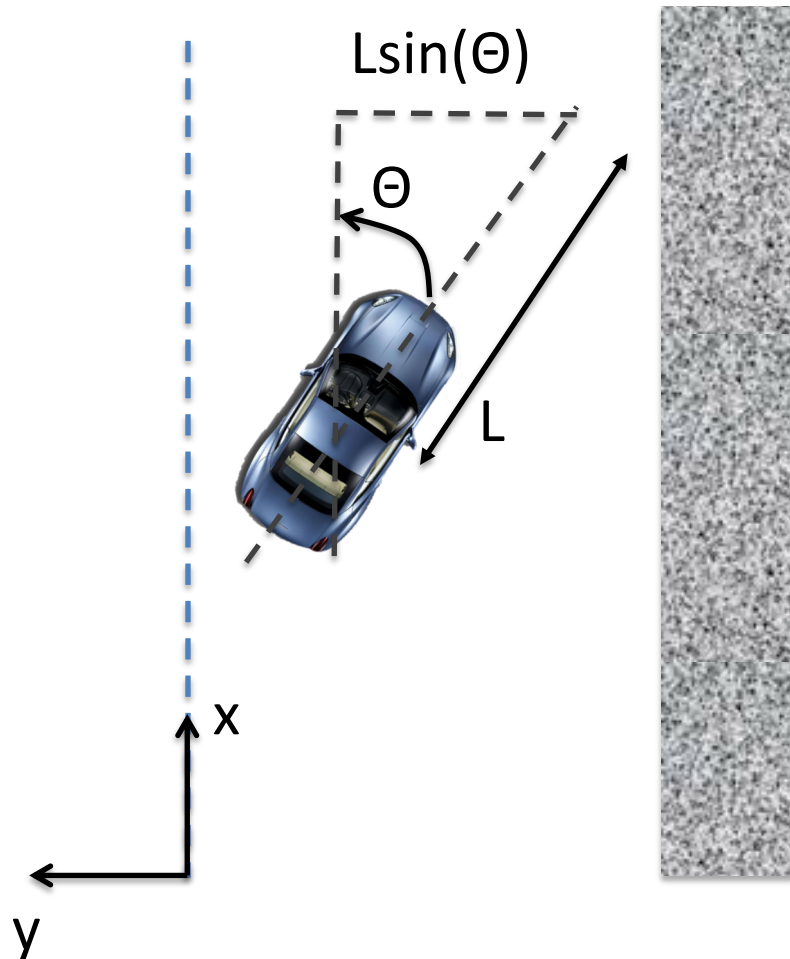


Want both y and $L\sin(\Theta)$ to be zero

→ Error term $e(t) = -(y + L\sin(\Theta))$

We'll see why we added a minus sign

PID control: computing input



When $y > 0$, car is to the left of centerline

→ Want to steer right: $\Theta < 0$

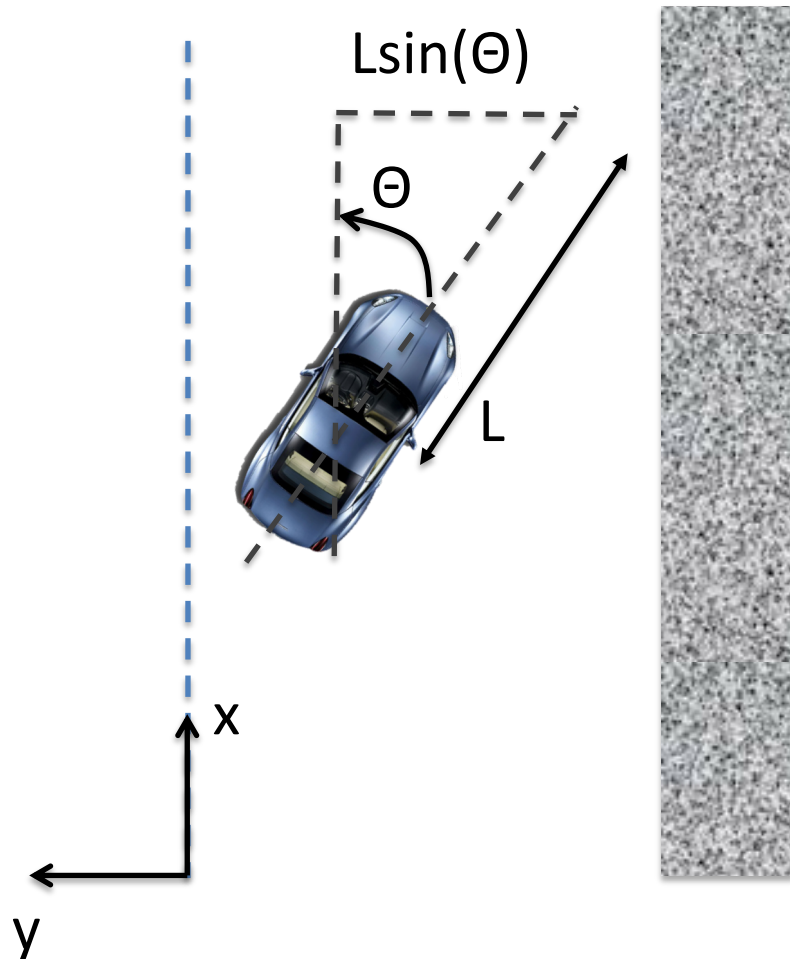
When $L \sin(\Theta) > 0$, we will be to the left of centerline in L meters

→ so want to steer right: $\Theta < 0$

Set *desired* angle to be

$$\Theta_d = K_p (-y - L \sin(\Theta))$$

PID control: computing input



When $y < 0$, car is to the right of centerline

→ Want to steer left

→ Want $\Theta > 0$

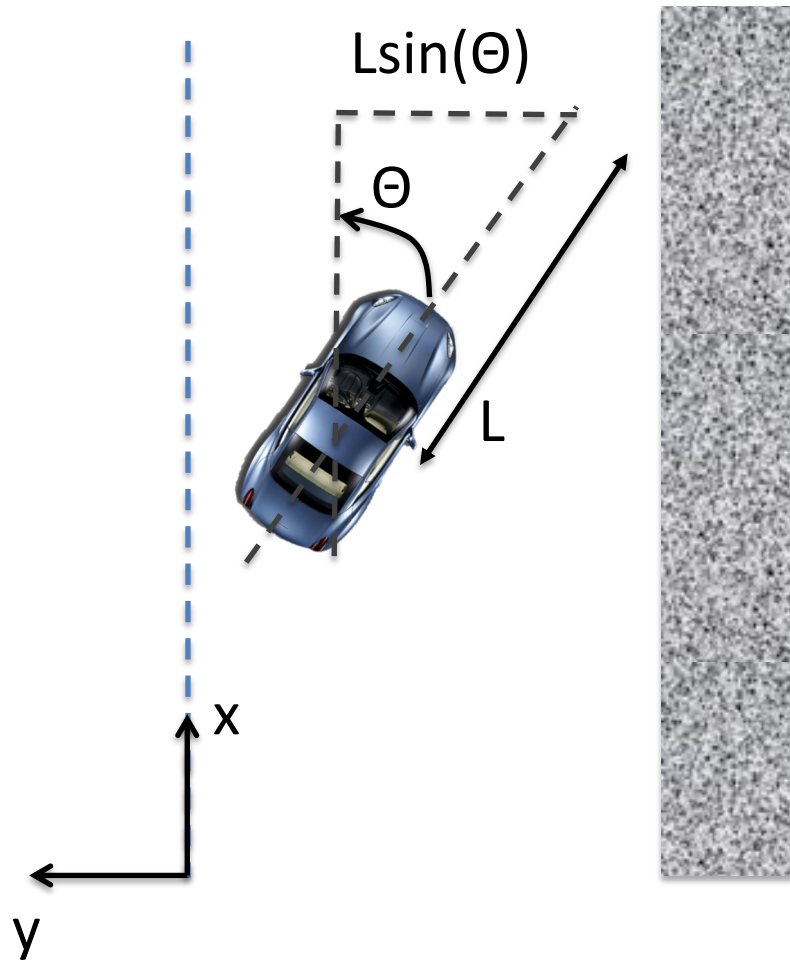
When $L \sin(\Theta) < 0$, we will be to the right of centerline in L meters, so want to steer left

→ Want $\Theta > 0$

Consistent with previous requirement:

$$\Theta_d = K_p (-y - L \sin(\Theta))$$

PID control: Proportional control

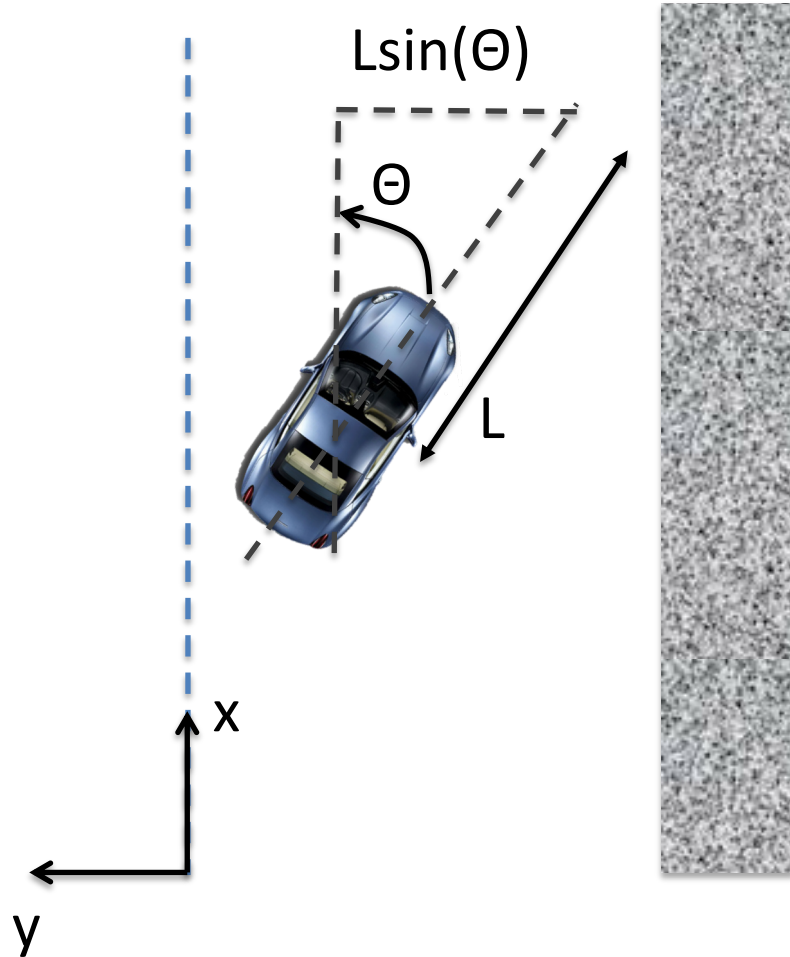


$$\Theta_d = C K_p (-y - L \sin(\Theta)) = C K_p e(t)$$

This is **P**roportional control.

The extra C constant is for scaling distances to angles.

PID control: Derivative control

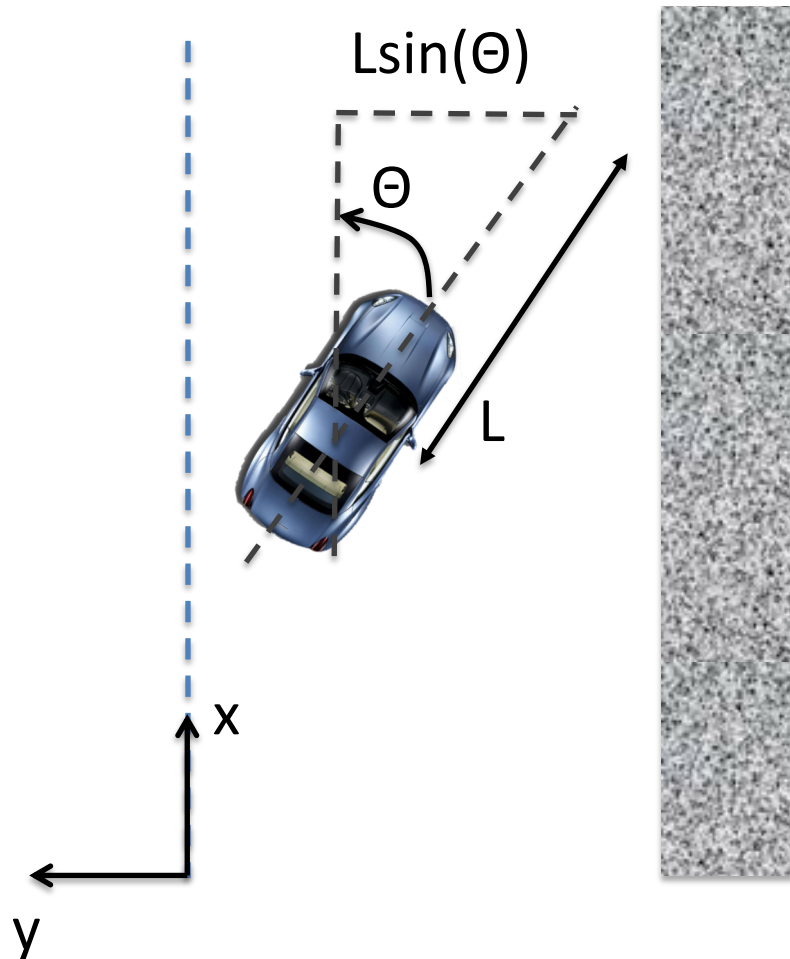


If error term is increasing quickly, we might want the controller to react quickly

→ Apply a *derivative gain*:

$$\Theta = K_p e(t) + K_d \frac{de(t)}{dt}$$

PID control: Integral control



Integral control is proportional to the *cumulative* error

$$\Theta = K_p e(t) + K_i E(t) + K_d \frac{de(t)}{dt}$$

Where $E(t)$ is the integral of the error up to time t (from a chosen reference time)

PID control: tuning the gains

- Default set of gains, determined empirically to work well for this car.
 - $K_p = 14$
 - $K_i = 0$
 - $K_d = 0.09$

PID control: tuning the gains

- Reduce $K_p \rightarrow$ less responsive to error magnitude
 - $K_p = 5$
 - $K_i = 0$
 - $K_d = 0.09$

PID control: tuning the gains

- Include $K_i \rightarrow$ overly sensitive to accumulating error \rightarrow over-correction
 - $K_p = 14$
 - $K_i = 2$
 - $K_d = 0.09$