

STATS 506 HW 1

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STATS 506 Homework 1

Problem 1 - Abalone Data

a)

```
#a)
#Set directory and load data
setwd("C:/Users/moore/Desktop/School/Master/STATS 506/STATS-506-HW-1/abalone")

abalone <- read.csv("abalone.data")

#Rename columns
colnames(abalone)[1:9] <- c("Sex",
                           "Length",
                           "Diameter",
                           "Height",
                           "Whole weight",
                           "Shucked weight",
                           "Viscera weight",
                           "Shell weight",
                           "Rings")
```

b)

```
#b)
table(abalone$Sex)
```

```
      F      I      M
1307 1342 1527
```

There are 1,307 females, 1,526 males, and 1,342 infants.

c) #1

```
#c)

#1)
#Using covariance function between Rings and each weight
cov(abalone$Rings, abalone$`Whole weight`)
```

```
[1] 0.8549952
```

```
cov(abalone$Rings, abalone$`Shucked weight`)
```

```
[1] 0.3014396
```

```
cov(abalone$Rings, abalone$`Viscera weight`)
```

```
[1] 0.1781965
```

```
cov(abalone$Rings, abalone$`Shell weight`)
```

```
[1] 0.2818386
```

Whole weight has the greatest correlation with Rings, with a correlation of 0.855.

c) #2

```
#2)
cov(abalone$Sex == "F", abalone$`Whole weight`)
```

```
[1] 0.0681564
```

```
cov(abalone$Sex == "M", abalone$`Whole weight`)
```

```
[1] 0.05960039
```

```
cov(abalone$Sex == "I", abalone$`Whole weight`)
```

```
[1] -0.1277568
```

Being infant has the strongest correlation with Whole weight, with a correlation of -0.128. It is the greatest correlation in terms of magnitude, the correlation is more strongly negative than the others are positive.

c) #3

```
#3)
#Find the observation with the most Rings, and pulling the values for each weight
#from that observation
max_weights <- c(abalone[which.max(abalone$Rings),] ["Whole weight"],
                 abalone[which.max(abalone$Rings),] ["Shucked weight"],
                 abalone[which.max(abalone$Rings),] ["Viscera weight"],
                 abalone[which.max(abalone$Rings),] ["Shell weight"])

max_weights
```

```
$`Whole weight`
[1] 1.8075
```

```
$`Shucked weight`
[1] 0.7055
```

```
$`Viscera weight`
[1] 0.3215
```

```
$`Shell weight`
[1] 0.475
```

Whole weight is 1.8075, Shucked weight is 0.7055, Viscera weight is 0.3215, Shell weight is 0.475

c) #4

```
#4)
#Count the observations with a viscera weight greater than shell weight, and divide
#by the total number of observations
weight_prop <- sum(abalone$`Viscera weight` > abalone$`Shell weight`)/nrow(abalone)
weight_prop
```

```
[1] 0.0651341
```

Only ~6.5% of the observations have a Viscera weight larger than their Shell weight.

d)

```
#d)
#Pull out the different weight values by sex
cor_F <- c(cov(abalone$Sex == "F", abalone$`Whole weight`),
           cov(abalone$Sex == "F", abalone$`Shucked weight`),
           cov(abalone$Sex == "F", abalone$`Viscera weight`),
           cov(abalone$Sex == "F", abalone$`Shell weight`))

cor_M <- c(cov(abalone$Sex == "M", abalone$`Whole weight`),
           cov(abalone$Sex == "M", abalone$`Shucked weight`),
           cov(abalone$Sex == "M", abalone$`Viscera weight`),
           cov(abalone$Sex == "M", abalone$`Shell weight`))

cor_I <- c(cov(abalone$Sex == "I", abalone$`Whole weight`),
           cov(abalone$Sex == "I", abalone$`Shucked weight`),
           cov(abalone$Sex == "I", abalone$`Viscera weight`),
           cov(abalone$Sex == "I", abalone$`Shell weight`))

#Create the table with the weights split out by sex, and rename the rows and columns
#for easier reading
sex_weight_table <- rbind(cor_F, cor_M, cor_I)
colnames(sex_weight_table) <- c("Whole weight", "Shucked weight",
                               "Viscera weight", "Shell weight")
rownames(sex_weight_table) <- c("Female", "Male", "Infant")
sex_weight_table
```

	Whole weight	Shucked weight	Viscera weight	Shell weight
Female	0.06815640	0.02716934	0.01567647	0.01977180
Male	0.05960039	0.02694935	0.01280370	0.01580163
Infant	-0.12775680	-0.05411869	-0.02848017	-0.03557343

e)

```
#Create subsets of the data that only include the certain sex pairs so that we
#can run the t-tests for each pair: F and M, F and I, and M and I.
```

```
abalone_FM <- subset(abalone, abalone$Sex %in% c("F", "M"))
abalone_FI <- subset(abalone, abalone$Sex %in% c("F", "I"))
abalone_MI <- subset(abalone, abalone$Sex %in% c("M", "I"))
```

```
ttest_FM <- t.test(abalone_FM$Rings ~ abalone_FM$Sex)
ttest_FI <- t.test(abalone_FI$Rings ~ abalone_FI$Sex)
ttest_MI <- t.test(abalone_MI$Rings ~ abalone_MI$Sex)
```

```
ttest_FM
```

Welch Two Sample t-test

data: abalone_FM\$Rings by abalone_FM\$Sex

t = 3.69, df = 2741.8, p-value = 0.0002286

alternative hypothesis: true difference in means between group F and group M is not equal to

95 percent confidence interval:

0.1999174 0.6533201

sample estimates:

mean in group F mean in group M

11.12930 10.70269

```
ttest_FI
```

Welch Two Sample t-test

data: abalone_FI\$Rings by abalone_FI\$Sex

t = 29.477, df = 2508.9, p-value < 2.2e-16

alternative hypothesis: true difference in means between group F and group I is not equal to

```
95 percent confidence interval:
 3.023380 3.454304
sample estimates:
mean in group F mean in group I
 11.129304      7.890462
```

```
ttest_MI
```

Welch Two Sample t-test

```
data: abalone_MI$Rings by abalone_MI$Sex
t = -27.194, df = 2857.9, p-value < 2.2e-16
alternative hypothesis: true difference in means between group I and group M is not equal to 0
95 percent confidence interval:
 -3.014995 -2.609451
sample estimates:
mean in group I mean in group M
 7.890462      10.702685
```

The difference in rings between females and males was the smallest. Both females and males had significantly different numbers of rings from infants.

Problem 2 - Food Expenditure Data

a)

```
#Load data
setwd("C:/Users/moore/Desktop/School/Master/STATS 506/STATS-506-HW-1")

food <- read.csv("food_expenditure.csv")
```

b)

```
#Rename variables
colnames(food) <- c("ID",
                    "Age",
                    "Household Members",
```

```
"State",  
"Currency",  
"Total Expenditures",  
"Grocery Store Expenditures",  
"Dining Out Expenditures",  
"Misc Expenditures",  
"Dine Out Count",  
"Alcohol",  
"Assistance Program")
```

c)

```
#Count observations before currency restriction  
nrow(food)
```

```
[1] 262
```

```
#Restrict to only USD  
food_USD <- subset(food, food$Currency %in% c("USD"))  
  
#Recheck observation count  
nrow(food_USD)
```

```
[1] 230
```

Number of observations decreased by 32.

d-h)

```
#d) Remove under 18 since they probably don't have a great sense of home expenditures  
#usually, and also remove the couple of people who are apparently 150 since that seems  
#sort of unlikely  
  
food_clean <- subset(food_USD, food_USD$Age %in% c(18:100))  
  
#e) Remove the observations with a state of XX  
food_clean <- subset(food_clean, !food_clean$State %in% c("XX"))
```

```

#f) In total expenditures, there is an observation with "~350" rather than just 350.
#There are some negative values in the expenditure variables as well, and I'll remove
#them here but I'm not sure if it's great practice unless we're certain that they are
#the result of a data collection error.
food_clean$`Total Expenditures`[which(food_clean$`Total Expenditures` == "~350")] <- 350
food_clean <- subset(food_clean, food_clean$`Total Expenditures` > 0)
food_clean <- subset(food_clean, food_clean$`Grocery Store Expenditures` > 0)
food_clean <- subset(food_clean, food_clean$`Dining Out Expenditures` > 0)
food_clean <- subset(food_clean, food_clean$`Misc Expenditures` > 0)

#g) There are some entries in dine out count that seem excessive.
#Eating out 30 times in a week is crazy for example, so I'll remove observations with
#a count of 20 and over, but there are conceivably some people who would do it.
#I again don't necessarily think that removing outliers just because they're outliers
#is the best practice.

food_clean <- subset(food_clean, food_clean$`Dine Out Count` < 20)

#h)
nrow(food_clean)

```

```
[1] 116
```

Only 116 observations left after cleaning compared to an original 262.

Problem 3 - Collatz Conjecture

a)

```

#' Function to find the next value in the Collatz Conjecture sequence
#'
#' @param integer
#'
#' @returns the next number in the Collatz Conjecture sequence. Gives errors requesting
#' numeric and integer inputs if the user attempts a non numeric or negative.
#' Rounds floats to nearest integer value smaller than it.
#' @examples an input of 5 returns 16, of 16 returns 8 according to the rule
nextCollatz <- function(integer){
  #Check for numbers

```



```

if(is.numeric(integer)){
  #check for positive numbers
  if(integer > 0){
    #Check for evens
    if(round(integer) %% 2 == 0){
      next_int <- round(integer)/2
    }
    #Check for odds
    else if(round(integer) %% 2 != 0){
      next_int <- 3*round(integer) + 1
    }
    return(next_int)
  }
  else{
    return("Input must be positive")
  }
}
else{
  return("Input must be numeric")
}
}

#Test
nextCollatz(5)

```

[1] 16

```
nextCollatz(16)
```

[1] 8

b)

```

collatzSequence <- function(integer){
  seq <- c(integer)
  next_int <- nextCollatz(integer)
  while(next_int > 1){
    seq <- c(seq, next_int)
    next_int <- nextCollatz(next_int)
  }
}

```

```

    #Making sure it includes the final "1" to end the sequence
    if(next_int == 1){
      seq <- c(seq, next_int)
      break
    }
  }
  return(seq)
}

#Test
collatzSequence(5)

```

```
[1] 5 16 8 4 2 1
```

```
collatzSequence(19)
```

```
[1] 19 58 29 88 44 22 11 34 17 52 26 13 40 20 10 5 16 8 4 2 1
```

c)

```

collatzList <- c()

for(i in 100:500){
  collatzList <- c(collatzList, length(collatzSequence(i)))
}
names(collatzList) <- c(100:500)

collatzList[which(collatzList == max(collatzList))]

```

```
327
144
```

```
collatzList[which(collatzList == min(collatzList))]
```

```
128
8
```

327 gives the longest sequence with a length of 144, and 128 has the shortest sequence, with a length of 8.