

NegFeedback

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$A+B \rightleftharpoons C \rightarrow D$ (k_{1f} , k_{1r} , k_{3f}) $2B + C \rightleftharpoons E$ (k_{2f} , k_{2r}) $A + C \rightleftharpoons F$ (k_{4f} , k_{4r})

```
library(knitr)
knitr::opts_chunk$set(comment = NA, fig.width = 5, fig.height = 10, fig.align = "center")

library(deSolve)
```

```
##
## Attaching package: 'deSolve'

## The following object is masked from 'package:graphics':
##
##      matplot
```

```
library(ggplot2)
library(gridExtra)

tstart <- 0
tstop <- 10
tby <- 0.1
A0 <- 10^5
B0 <- 10^5
C0 <- 0 # want 10
D0 <- 0
E0 <- 0
#F0 <- 0
k1f <- .03 # adds C, subs A&B
k1r <- .03 # adds A&B, subs C
k2f <- 1.05 # adds E, subs B&C
k2r <- .4 # adds B&C
k3f <- .01 # adds D, subs C
k4f <- .08 # adds C, subs A&E
k4r <- .2 # adds A&E, subs C

negfeed <- function(t, init, parameters)
{
  with(as.list(c(init,parameters)),{
    dA <- k1r*C - k1f*A*B - 1.5*k4f*A^1.5*C + 1.5*k4r*F
    dB <- k1r*C - k1f*A*B - 1.5*k2f*B^1.5*C + 1.5*k2r*E
    dC <- k1f*A*B - k1r*C - k3f*C - k2f*B^1.5*C - k4f*A^1.5*C + k2r*E + k4r*F
    dD <- k3f*C
    dE <- k2f*B^1.5*C - k2r*E
    # dF <- k4f*A^1.5*C - k4r*F
    list(c(dA,dB,dC,dD,dE))
  })
}
```

```

}

times <- seq(tstart, tstop, by = tby)
init <- c(A=A0,B=B0,C=C0,D=D0,E=E0)

tmain <- paste("tby =",tby,"k1f =",k1f,"k1r =",k1r,"k2f =",k2f,"k2r =",k2r,"k3f =",k3f,
               "k4f =",k4f,"k4r =",k4r)
out <- ode(y=init,time=times,func=negfeed,parms=NULL)
out

```

| ## | time | A | B | C | D | E |
|-------|------|--------------|--------------|-------------|--------------|----------|
| ## 1 | 0.0 | 1.000000e+05 | 100000.00000 | 0.000000000 | 0.000000000 | 0.00 |
| ## 2 | 0.1 | 2.888113e+04 | 23.51359 | 0.08655643 | 0.0001931229 | 34061.37 |
| ## 3 | 0.2 | 2.189273e+04 | 29.72739 | 0.12577323 | 0.0002972342 | 32727.28 |
| ## 4 | 0.3 | 1.520182e+04 | 40.84760 | 0.20773917 | 0.0004583087 | 31447.50 |
| ## 5 | 0.4 | 8.853031e+03 | 65.45707 | 0.43859194 | 0.0007585005 | 30226.42 |
| ## 6 | 0.5 | 3.261116e+03 | 132.54507 | 1.49070855 | 0.0015823347 | 29129.05 |
| ## 7 | 0.6 | 5.907430e+02 | 168.40577 | 4.18202676 | 0.0043988494 | 28602.56 |
| ## 8 | 0.7 | 1.309970e+02 | 141.74434 | 6.31637067 | 0.0097093428 | 28527.08 |
| ## 9 | 0.8 | 4.249997e+01 | 124.74190 | 7.78037539 | 0.0168086812 | 28517.90 |
| ## 10 | 0.9 | 1.768461e+01 | 115.83439 | 8.71554649 | 0.0250933060 | 28517.14 |
| ## 11 | 1.0 | 8.630859e+00 | 110.98793 | 9.29521734 | 0.0341218148 | 28517.56 |
| ## 12 | 1.1 | 4.685909e+00 | 108.20703 | 9.65529299 | 0.0436111157 | 28518.02 |
| ## 13 | 1.2 | 2.742521e+00 | 106.53913 | 9.88201547 | 0.0533883284 | 28518.38 |
| ## 14 | 1.3 | 1.697909e+00 | 105.50517 | 10.02689586 | 0.0633480890 | 28518.63 |
| ## 15 | 1.4 | 1.099608e+00 | 104.84926 | 10.12059146 | 0.0734251885 | 28518.80 |
| ## 16 | 1.5 | 7.404024e-01 | 104.42713 | 10.18164599 | 0.0835784698 | 28518.91 |
| ## 17 | 1.6 | 5.169596e-01 | 104.15370 | 10.22150487 | 0.0937814610 | 28518.98 |
| ## 18 | 1.7 | 3.741706e-01 | 103.97696 | 10.24739829 | 0.1040168524 | 28519.03 |
| ## 19 | 1.8 | 2.810257e-01 | 103.86412 | 10.26397613 | 0.1142731700 | 28519.06 |
| ## 20 | 1.9 | 2.193037e-01 | 103.79407 | 10.27428031 | 0.1245427249 | 28519.07 |
| ## 21 | 2.0 | 1.779107e-01 | 103.75294 | 10.28032599 | 0.1348203194 | 28519.08 |
| ## 22 | 2.1 | 1.498996e-01 | 103.73150 | 10.28347159 | 0.1451024182 | 28519.08 |
| ## 23 | 2.2 | 1.308131e-01 | 103.72352 | 10.28462618 | 0.1553866035 | 28519.08 |
| ## 24 | 2.3 | 1.177402e-01 | 103.72479 | 10.28441447 | 0.1656712172 | 28519.07 |
| ## 25 | 2.4 | 1.087507e-01 | 103.73241 | 10.28326243 | 0.1759551196 | 28519.06 |
| ## 26 | 2.5 | 1.025498e-01 | 103.74443 | 10.28146250 | 0.1862375258 | 28519.06 |
| ## 27 | 2.6 | 9.826167e-02 | 103.75947 | 10.27921578 | 0.1965178954 | 28519.04 |
| ## 28 | 2.7 | 9.528863e-02 | 103.77661 | 10.27666634 | 0.2067958552 | 28519.03 |
| ## 29 | 2.8 | 9.322225e-02 | 103.79518 | 10.27389623 | 0.2170711489 | 28519.02 |
| ## 30 | 2.9 | 9.178142e-02 | 103.81475 | 10.27098485 | 0.2273435997 | 28519.01 |
| ## 31 | 3.0 | 9.077186e-02 | 103.83500 | 10.26797411 | 0.2376130858 | 28519.00 |
| ## 32 | 3.1 | 9.006019e-02 | 103.85572 | 10.26489565 | 0.2478795245 | 28518.99 |
| ## 33 | 3.2 | 8.955604e-02 | 103.87677 | 10.26177101 | 0.2581428606 | 28518.97 |
| ## 34 | 3.3 | 8.919529e-02 | 103.89803 | 10.25861546 | 0.2684030558 | 28518.96 |
| ## 35 | 3.4 | 8.893341e-02 | 103.91945 | 10.25543963 | 0.2786600846 | 28518.95 |
| ## 36 | 3.5 | 8.873997e-02 | 103.94097 | 10.25225078 | 0.2889139305 | 28518.94 |
| ## 37 | 3.6 | 8.859430e-02 | 103.96255 | 10.24905383 | 0.2991645834 | 28518.93 |
| ## 38 | 3.7 | 8.848156e-02 | 103.98418 | 10.24585233 | 0.3094120370 | 28518.91 |
| ## 39 | 3.8 | 8.839126e-02 | 104.00583 | 10.24264877 | 0.3196562878 | 28518.90 |
| ## 40 | 3.9 | 8.831649e-02 | 104.02749 | 10.23944476 | 0.3298973346 | 28518.89 |
| ## 41 | 4.0 | 8.825265e-02 | 104.04916 | 10.23624140 | 0.3401351776 | 28518.88 |
| ## 42 | 4.1 | 8.819650e-02 | 104.07084 | 10.23303978 | 0.3503698181 | 28518.86 |

| | | | | | | |
|-------|-----|--------------|-----------|-------------|--------------|----------|
| ## 43 | 4.2 | 8.814562e-02 | 104.09251 | 10.22983982 | 0.3606012578 | 28518.85 |
| ## 44 | 4.3 | 8.809832e-02 | 104.11417 | 10.22664249 | 0.3708294987 | 28518.84 |
| ## 45 | 4.4 | 8.805354e-02 | 104.13583 | 10.22344776 | 0.3810545436 | 28518.83 |
| ## 46 | 4.5 | 8.801055e-02 | 104.15748 | 10.22025586 | 0.3912763952 | 28518.81 |
| ## 47 | 4.6 | 8.796884e-02 | 104.17912 | 10.21706692 | 0.4014950563 | 28518.80 |
| ## 48 | 4.7 | 8.792799e-02 | 104.20076 | 10.21388103 | 0.4117105301 | 28518.79 |
| ## 49 | 4.8 | 8.788775e-02 | 104.22238 | 10.21069823 | 0.4219228194 | 28518.78 |
| ## 50 | 4.9 | 8.784794e-02 | 104.24399 | 10.20751857 | 0.4321319276 | 28518.77 |
| ## 51 | 5.0 | 8.780845e-02 | 104.26559 | 10.20434207 | 0.4423378576 | 28518.75 |
| ## 52 | 5.1 | 8.776920e-02 | 104.28719 | 10.20116874 | 0.4525406128 | 28518.74 |
| ## 53 | 5.2 | 8.773012e-02 | 104.30877 | 10.19799859 | 0.4627401962 | 28518.73 |
| ## 54 | 5.3 | 8.769117e-02 | 104.33034 | 10.19483162 | 0.4729366110 | 28518.72 |
| ## 55 | 5.4 | 8.765233e-02 | 104.35190 | 10.19166784 | 0.4831298605 | 28518.70 |
| ## 56 | 5.5 | 8.761357e-02 | 104.37345 | 10.18850725 | 0.4933199478 | 28518.69 |
| ## 57 | 5.6 | 8.757488e-02 | 104.39499 | 10.18534983 | 0.5035068760 | 28518.68 |
| ## 58 | 5.7 | 8.753625e-02 | 104.41652 | 10.18219560 | 0.5136906485 | 28518.67 |
| ## 59 | 5.8 | 8.749768e-02 | 104.43804 | 10.17904454 | 0.5238712683 | 28518.65 |
| ## 60 | 5.9 | 8.745915e-02 | 104.45954 | 10.17589666 | 0.5340487386 | 28518.64 |
| ## 61 | 6.0 | 8.742067e-02 | 104.48104 | 10.17275193 | 0.5442230627 | 28518.63 |
| ## 62 | 6.1 | 8.738224e-02 | 104.50253 | 10.16961037 | 0.5543942436 | 28518.62 |
| ## 63 | 6.2 | 8.734385e-02 | 104.52400 | 10.16647197 | 0.5645622845 | 28518.61 |
| ## 64 | 6.3 | 8.730550e-02 | 104.54547 | 10.16333672 | 0.5747271886 | 28518.59 |
| ## 65 | 6.4 | 8.726719e-02 | 104.56692 | 10.16020461 | 0.5848889590 | 28518.58 |
| ## 66 | 6.5 | 8.722893e-02 | 104.58837 | 10.15707564 | 0.5950475988 | 28518.57 |
| ## 67 | 6.6 | 8.719070e-02 | 104.60980 | 10.15394980 | 0.6052031113 | 28518.56 |
| ## 68 | 6.7 | 8.715251e-02 | 104.63123 | 10.15082710 | 0.6153554995 | 28518.54 |
| ## 69 | 6.8 | 8.711437e-02 | 104.65264 | 10.14770752 | 0.6255047665 | 28518.53 |
| ## 70 | 6.9 | 8.707626e-02 | 104.67404 | 10.14459106 | 0.6356509155 | 28518.52 |
| ## 71 | 7.0 | 8.703819e-02 | 104.69543 | 10.14147771 | 0.6457939497 | 28518.51 |
| ## 72 | 7.1 | 8.700016e-02 | 104.71682 | 10.13836746 | 0.6559338720 | 28518.50 |
| ## 73 | 7.2 | 8.696217e-02 | 104.73819 | 10.13526032 | 0.6660706856 | 28518.48 |
| ## 74 | 7.3 | 8.692422e-02 | 104.75955 | 10.13215628 | 0.6762043937 | 28518.47 |
| ## 75 | 7.4 | 8.688630e-02 | 104.78090 | 10.12905533 | 0.6863349992 | 28518.46 |
| ## 76 | 7.5 | 8.684843e-02 | 104.80224 | 10.12595747 | 0.6964625054 | 28518.45 |
| ## 77 | 7.6 | 8.681059e-02 | 104.82357 | 10.12286269 | 0.7065869152 | 28518.43 |
| ## 78 | 7.7 | 8.677279e-02 | 104.84489 | 10.11977098 | 0.7167082317 | 28518.42 |
| ## 79 | 7.8 | 8.673503e-02 | 104.86620 | 10.11668234 | 0.7268264581 | 28518.41 |
| ## 80 | 7.9 | 8.669731e-02 | 104.88749 | 10.11359677 | 0.7369415974 | 28518.40 |
| ## 81 | 8.0 | 8.665963e-02 | 104.90878 | 10.11051426 | 0.7470536527 | 28518.39 |
| ## 82 | 8.1 | 8.662199e-02 | 104.93006 | 10.10743480 | 0.7571626270 | 28518.37 |
| ## 83 | 8.2 | 8.658438e-02 | 104.95133 | 10.10435839 | 0.7672685233 | 28518.36 |
| ## 84 | 8.3 | 8.654682e-02 | 104.97259 | 10.10128503 | 0.7773713448 | 28518.35 |
| ## 85 | 8.4 | 8.650929e-02 | 104.99383 | 10.09821471 | 0.7874710944 | 28518.34 |
| ## 86 | 8.5 | 8.647180e-02 | 105.01507 | 10.09514742 | 0.7975677752 | 28518.33 |
| ## 87 | 8.6 | 8.643434e-02 | 105.03630 | 10.09208316 | 0.8076613902 | 28518.31 |
| ## 88 | 8.7 | 8.639693e-02 | 105.05751 | 10.08902192 | 0.8177519425 | 28518.30 |
| ## 89 | 8.8 | 8.635955e-02 | 105.07872 | 10.08596370 | 0.8278394351 | 28518.29 |
| ## 90 | 8.9 | 8.632221e-02 | 105.09991 | 10.08290849 | 0.8379238709 | 28518.28 |
| ## 91 | 9.0 | 8.628491e-02 | 105.12110 | 10.07985629 | 0.8480052531 | 28518.27 |
| ## 92 | 9.1 | 8.624765e-02 | 105.14228 | 10.07680710 | 0.8580835845 | 28518.25 |
| ## 93 | 9.2 | 8.621042e-02 | 105.16344 | 10.07376090 | 0.8681588683 | 28518.24 |
| ## 94 | 9.3 | 8.617323e-02 | 105.18460 | 10.07071770 | 0.8782311073 | 28518.23 |
| ## 95 | 9.4 | 8.613608e-02 | 105.20574 | 10.06767748 | 0.8883003046 | 28518.22 |
| ## 96 | 9.5 | 8.609897e-02 | 105.22688 | 10.06464024 | 0.8983664632 | 28518.20 |

```
## 97  9.6 8.606189e-02    105.24800 10.06160599 0.9084295861 28518.19
## 98  9.7 8.602485e-02    105.26912 10.05857470 0.9184896762 28518.18
## 99  9.8 8.598785e-02    105.29022 10.05554638 0.9285467365 28518.17
## 100 9.9 8.595088e-02    105.31132 10.05252103 0.9386007700 28518.16
## 101 10.0 8.591396e-02    105.33240 10.04949863 0.9486517795 28518.14
```

```
#axis(2, at = seq(0,100000,by=10000))
#pch=21 WAS working at one point with type="p"
#lines(out[,1],out[,7], type = "l", col="pink")

plot(out[,1],out[,2], type = "l", col="purple", ylim=c(0,40000),main = tmain)
lines(out[,1],out[,3], type = "l", col="green")
lines(out[,1],out[,4], type = "p", pch=21, col="red")
lines(out[,1],out[,5], type = "l", col="black")
lines(out[,1],out[,6], type = "l", col="blue")
```

$\gamma = 0.1$ $k1f = 0.03$ $k1r = 0.03$ $k2f = 1.05$ $k2r = 0.4$ $k3f = 0.01$ $k4f = 0.08$ $k4r = 0.08$

