

tmp title: MUSC source

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GEO-Example

Running head: *Geophysics* example

ABSTRACT

INTRODUCTION

Since the early developments of seismic imaging methods in the middle of 20th century, approaches and algorithms innovations are still proposed in current research projects. The improvements deal with both the qualitative imaging techniques like migration (e.g. Berkhout et al. (2012); Guofeng et al. (2013)), novel applications of quantitative imaging methods such as the first arrival tomography (e.g. Bohm et al. (2015)), or even more recent approaches like the Full Waveform Inversion (e.g. Perez Solano et al. (2014), see Virieux and Operto (2009) for a revue of this last decade). The refinements are proposed for different scales like near surface applications for civil engineering topics or more deeper investigation for example for oil prospection or crustal imaging at regional or global scales They are mostly validated by using synthetic data, for example with well known shared benchmark (like the Marmousi case). However, the synthetic data are generally computed using the same wave propagation modeling engine used in the inverse problem process. In other terms, the synthetic data are computed with some assumptions which are the same in the inverse problem, for example the approximation of acoustic propagation, a 2D space medium, or a 2D line source. This approach, called *inverse crime* (Wirgin, 2004) is particularly useful for validating an algorithm in its early development stage but does not take into account the artefacts that can be due to the assumptions of the direct problem. Some authors tackle this issue by providing 3D data which are inverted with a 2D approach or other restrictive assumptions (e.g). But also in this case, the approach does not allow to assess the efficiency of the method for real seismic data. Moreover, because no one knows precisely the Earth interior, it is difficult to evaluate the capacity of a method to recover physical parameters and structures from real seismic data which can lead sometimes to geological misinterpretation due to numerical artifacts (Morozov, 2004). Thus, it is necessary to add

a step for which imaging methods will be tested for experimental seismic measurements
25 obtained under controlled conditions.

The best way to satisfy this need is to use Physical Small Scale Modeling Methods (noted
PSM subsequently). *PSM* were used since several years to study the propagation of waves
in various media with several stage of complexity, from acoustic wave propagation in homo-
geneous media to elastic wave propagation in three-dimensional heterogeneous anisotropic
30 media (Rieber, 1936; Howes et al., 1953; Hiltermann, 1970; French, 1974; Bishop et al., 1985;
Pratt, 1999; Favretto-Cristini et al., 2013; Sarkar et al., 2003; Isaac and Lawton, 1999), and
allow to generate experimental seismic data under well-controlled conditions. In this way,
recent studies have been conducted to simulate multi-sources and multi-receivers through
piezzo-electric transducers (Wong et al., 2009). An alternative approach consists in using the
35 laser interferometry as the receiver system, as done in the MUSC Laboratory (Bretaudeau
et al., 2008, 2011, 2013), *Mesure Ultrasonore Sans Contact* in French, is one of them. This
technology, by avoiding the contact of the receivers on the model, allows to by-pass the
coupling issue of transducers that is difficult to model. In this way, the MUSC laboratory is
designed to simulate (1) wide-angle on-shore acquisitions modeling both body waves and sur-
40 face waves, (2) automatic multisource-multireceiver measurements with a high-productivity,
(3) high-precision source-receiver positioning and (4) high-precision recording of absolute
surface displacement without coupling effects.

Our objective here is to increase the potential of the MUSC system as a reliable tool for
generating experimental data which will be distributed in the scientific community. Thus,
45 we present two studies of experimental data in order to : 1) refine the comparison between
numerical and experimental data by taking into account the 3D/2D geometrical spreading
effects through an alternative way and 2) identify the reproducibility of the source impact

and, consequently, data repeatability. These approaches will complete the knowledge of the system and facilitate the achievement of massive multi-source and multi-receiver data
50 simulating subsurface seismic experimental campaigns.

To achieve some of these objectives, we used a seismic wave modeling code based on the Spectral Element Method (Komatitsch et al., 1998; Komatitsch and Tromp, 1999; Komatitsch et al., 2005; Festa and Vilotte, 2005). This method has several advantages compared to finite differences and finite elements, such as: (1) a weak formulation which can
55 naturally take into account the free surface, (2) an explicit scheme in time facilitating parallelization and reducing the computational cost, (3) a spatial discretization (mesh) convenient for the representation of complex environments and (4) high precision results and low numerical dispersion.

Thus, this article is organized as follow. In a first part, we present the MUSC laboratory
60 and the SEM code used for the studies. In a second part, we present two coupled studies of experimental data in order to: (1) refine the comparison between numerical and experimental data by taking into account the geometrical spreading effects between two-dimensional and three-dimensional data through an alternative way, and (2) identify the reproducibility of the source impact to validate the data reproducibility.

METHODS

65 **Physical modeling: MUSC Bench**

The MUSC bench (Bretaudeau et al., 2008, 2011, 2013) is built to experimentally reproduce field seismic data with a great accuracy on small scale model. Figure 1 shows the bench and its components. MUSC is composed of a honeycomb tab and two arms which control

the source and the receiver position with a precision of 10 μm .

70 The receiving system of MUSC Laboratory is composed of a laser interferometer. The principle of this laser is based on a phase shift of the reflected laser signal due to the wave propagation in the material. A real-time calibration value enables a continuous conversion to a nanometric displacement. The focal diameter of the laser on the model surface is about several micrometers and allows a detection limit of 2.5 nm in the frequency range from 30
75 kHz to 20 MHz.

The seismic source is simulated by a piezoelectric transducer relied to a launching and synchronization system. This system provides more energy than a laser impulse source (Bretaudeau, 2010; Bretaudeau et al., 2011) and allows to choose the source in terms of waveform, *i.e.*, Gauss source, Ricker source, central frequency f_0 and time delay t_0 . The
80 source is generated by a waveform generator and is then amplified before transmitted to the small-scale-model. In the framework of seismic physical modeling, the source must be as closed as possible to a normal point source. Thus, the piezoelectric source is coupled with an adapter in order to reproduce the spatial energy repartition (limiting directivity) and conserving the waveform as shown in figure 3.

85 For the purpose of small scale modeling, the change of scale must keep the relationship between observables. For most of seismic imaging methods, the significant physical parameters are the compressional and shear waves velocities, V_P and V_S respectively, the density ρ and the quality factor Q . When scaling the model, many parameters can be modified: the distances, the time scale, the amplitudes of the signals, the viscoelastic properties, etc.
90 Hence, the predominant factor is the wavelength $\lambda = V/f$, where V is the wave velocity and f the frequency. Thus, physical and mechanical parameters are modified to preserve the

ratio $\lambda_{real} = \xi \lambda_{scale}$ where ξ is the scale ratio. It is therefore necessary to act directly on the time-frequency scales. Assuming the materials used to build the small scale model have the same mechanical properties (V_P , V_S , ρ) than the natural media, it is straightforward to
95 obtain the scale ratios for parameters involved in seismic experiment.

For near surface experiments, the scale ratio ξ is about 1000 which means that the central frequency f_0 of the source is few kHz (generally 100 kHz but can be more or less), distances are in mm (acquisition length around 50 mm typically) and time unit is ms .

Small-scale models are generally made of metal, thermoplastic or melted epoxy resin-based
100 materials (Bretaudeau et al., 2013, 2011, 2008). These materials allow to reproduce complex geometries and have a large panel of physical and mechanical properties. These materials have the advantages to have physical properties closed to natural soil materials. The models are generally over-sized to easily separate reflected waves on boundaries from the rest of the signal.

105 Numerical modeling: Spectral Element Method

Various numerical methods exist to resolve the equation of motion in arbitrary elastic media. The most widely used is the Finite-Differences (FD) method (Virieux, 1986; Levander, 1988; Robertsson et al., 1994; Pratt, 1990; Stekl and Pratt, 1998; Saenger and Bohlen, 2004) which estimates each derivative on a regular Cartesian grid using a Taylor development (Moczo
110 et al., 2004) of order n . FD is simple to implement but quickly shows some limitations: the Cartesian grid is defined by the minimum propagated wavelength (λ_{min}) in the full media and is unable to reproduce properly complex topography and interfaces. Moreover, Saenger et al. (2000) show that 60 points by wavelength (λ) are needed to model propagation of

Rayleigh wave in order $n = 2$ where only 15 points by λ are required to model propagation of
115 body waves which increases drastically the numerical cost in case of near-surface modeling
experiment. The Finite-Elements Method (FEM) is another popular method used for wave
propagation modeling (Lysmer and Drake, 1972; Seron et al., 1990; Hulbert and Hughes,
1990). FEM is based on a variational formulation of the equation of motion and gives a
continuous approximate solution in space using polynomial basis functions defined on each
120 node of each cell of the mesh. The natural boundary conditions of FEM is the free surface
and the triangular (in 2D) or tetraedric (in 3D) unstructured meshes are well adapted to
complex media and topography. However, low polynomial basis are inadequate with fine
spatial discretization and the required discretization to obtain precise and non-dispersive
solution in numerically costly.

125 Recently, the Spectral Element Method (SEM), widely used in fluid dynamics (Patera, 1984;
Korczak and Patera, 1986; Karniadakis, 1989), was adapted to seismic wave propagation
(Komatitsch et al., 1998; Komatitsch and Tromp, 1999; Komatitsch et al., 2005; Festa and
Vilotte, 2005).

The SEM is based upon a high-order piecewise polynomial approximation of the weak
130 formulation of the wave equation. It combines the accuracy of the pseudo-spectral method
with the flexibility of the finite-element method (Tromp et al., 2008).

In this method, the wave-field is represented in terms of high-degree Lagrange interpolants,
and integrals are computed based upon Gauss-Lobatto-Legendre (gll) quadrature. This
combination leading to a perfectly diagonal mass matrix leads in turn to a fully explicit
135 time scheme which lends itself very well to numerical simulations on parallel computers. It
is particularly well suited to handling complex geometries and interface matching conditions

(Cristini and Komatitsch, 2012).

As in FEM, all boundary of the domain are reflecting and the free surface is the natural condition. In order to simulate infinite or semi-infinite domain, SEM uses Perfect Match
140 Layers boundary conditions (Bérenger, 1994; Festa and Vilotte, 2005) but are not used here.

The typical element size that is required to generate an accurate mesh is of the order of λ , λ being the smallest wavelength of waves traveling in the model.

Models are meshed in 2D with quadrangles using the open-source software package GMSH (Geuzaine and Remacle, 2009).

RESULTS

145 From point-source to line-source response

In the framework of wave propagation modeling and waveform inversion, most of available algorithms are limited to the two-dimensional approximation especially for computational cost causes. Thus, line-source seismograms are required as observed data to be compared to synthetic seismograms or for inversion processes.

150 However, MUSC is designed to produce three-dimensional experimental seismograms from a piezoelectric source selected to be as closed as possible to a point source. Generally, the correction of the geometrical spreading is done by convolving each trace by $\sqrt{t^{-1}}$, where t is the travel-time, with or without offset conditioning. The correct phase can then be obtained using a source wavelet estimation method (Bretaudeau et al., 2011).

155 Recently, Forbriger et al. (2014) and Schafer et al. (2014) have developed, and successfully applied to synthetic seismograms, an hybrid method to convert the three-dimensional

geometrical spreading in two-dimensional spreading using both convolution tapering and offset dependent scaling of the waveform. However, these pre-processing methods are not perfect and can not be easily automated and the results are strongly conditioned by user's
160 experience and attempts.

Here, we take advantage of the experimental framework to explore an alternative approach specific to MUSC. Contrary to field experiments, it is possible to generate a pseudo-line-source finely sampled by multiple point-sources, perpendicular to the acquisition line.

Each point-source must be enough close each other so the resulting source being a line-
165 source in the sense of Huygens principle. To do that, we consider that the length of the line must be equal, at least, $L \geq 4\lambda_{max}$ and the sampling interval $ds \leq 10/\lambda_{min}$. Given the material's properties, we choose $L = 240 \text{ mm}$ and $ds = 0.5 \text{ mm}$ which leads to 481 point-source locations. The line of point-source is located at ?? mm distance. Four receiver positions have been selected: 90, 95, 100 and 105 mm offset from the source. The source
170 wavelet is a Ricker with a central frequency $f_0 = 100 \text{ kHz}$. Each receiver is perpendicular to and centered on the line-source. For each receiver position, the complete signal is stacked along source position to obtain an equivalent two-dimensional line-source response.

To evaluate the efficiency of the method, experimental line-source responses will be compared to point-source and equivalent line-source responses using the cross-correlation coefficient (**cc**) and the root mean square (**rms**) ratio. These values are presented in table
175 2. **cc_{init}** and **rms_{init}** correspond to direct evaluation whereas **cc_{final}** corresponds to the best **cc** obtained and **rms_{final}** is the corresponding **rms**.

Figures 7(a) show the comparison between experimental traces obtained using a point-source and a line-source for source-receiver offsets 50, 55, 60 and 65 mm respectively. It

180 is straightforward that these waveforms are not similar in terms of both phases ($\mathbf{cc}<0.75$) and amplitude ($\mathbf{rms}>0.4$). Even after amplitude fitting, point-source response to the line-response in term of phase ($\mathbf{cc}<0.8$), amplitudes do not match ($\mathbf{rms}>0.4$). These results confirm that using raw point-source responses in a two-dimensional inversion process or imaging method can be critical in terms of convergence and validity of the results since
185 these methods are built over phase and/or amplitude similarity.

Figures 7(b) show the comparison between experimental traces using a line-source and a point-source after geometrical spreading corrections (equivalent line-source response) for the same previous source-receiver offsets. The cross-correlation coefficient \mathbf{cc} for these waveforms are greater than 0.95 and $\mathbf{rms}<0.25$. These results denote that the experimental
190 line-source response is correct in terms of phase compared to an equivalent line-source response. However, \mathbf{rms} are quite great even if they are smaller than previously. This can be explained by small differences in terms of waveforms and phases which are critical in the final \mathbf{rms} results. Moreover, the *hybrid* method to obtain the equivalent line-source response from a point-source response needs accurate parametrization to obtain the best result which
195 is not necessarily in a good agreement with the attempt true line-source response.

These results show that the line-source emulation on the MUSC laboratory is efficient and can produce data suitable for imaging methods such as 2D FWI.

Experimental source reproducibility

To assess the ability of MUSC to provide reproducible data, *i.e.* to evaluate the repro-
200 ducibility of the source impact, several physical modeling were performed on a homogeneous epoxy-resin block for which the seismic waves velocities and the intrinsic attenuation are

known : $V_P = 2300 \text{ m.s}^{-1}$, $V_S = 1030 \text{ m.s}^{-1}$, $\rho = 1300 \text{ kg.m}^{-3}$ and $Q = 30$.

Ten realizations have been acquired on this model with a similar geometry setup, i.e. 120 receivers positions with an increment equal to 1 mm and a minimum offset of 10 mm. The numerical wavelet sent to the piezoelectric transducer source is a Ricker signal with a central
205 frequency of 100 kHz. However, the source waveform is modified by the physical coupling effect of the transducer.

First, a mean receiver-gather was calculated from the ten realizations and each trace of each realization was compared to equivalent one from mean receiver-gather. Figure 8 shows the
210 central traces of each realization and `textbfcc` gives the correlation coefficient between each central trace with the central trace of the mean receiver-gather. The `cc` are always greater than 0.98 which demonstrate the high reproducibility of MUSC experiments. However, traces are not exactly the same which denotes a variability of the source from an experiment to another.

215 In a second step, a unique source wavelet is estimated using a linear source wavelet estimation method based on a stabilized deconvolution (Pratt, 1999). The source wavelet estimation takes into account the ten experiments together and allows to obtain a mean effective source suitable for each experiment. The resulting source wavelet is applied to the synthetic signals (figure 9). The corrected seismograms are in good agreement with the
220 experimental seismograms (correlation coefficients > 0.96) confirms the great efficiency of the wavelet source assessment process.

These last results, based on an average estimated source wavelet show that the effective impulse source emitted by the transducer in the MUSC measurement bench is stable enough to ensure a robust reproducibility of the source. Therefore, concerning the key issue of the

225 source knowledge, experimental data acquired in the MUSC laboratory can be efficiently
processed by imaging methods like Full Waveform Inversion (FWI) with only one estimation
step for all the multi-source and multi-receivers data.

To go further, we can imagine that the source correspond to the transducer-model coupling.
So, an other model containing F50 pure epoxy-resin at the source position should have the
230 same transmitted source wavelet....

Figure 10 shows the comparison between experiment data (black) and numerical data using
the previously estimated source (red)...

CONCLUSIONS

These two studies allow to refine the capacity of the physical modeling designed for seismic
experiments simulation by 1) completing the validation of the measurement through com-
235 parison of numerical and experimental data generated by a realistic 2D source line and 2)
assessing the reproductivity of the effective source emitted in a model. These improvements
allow to provide and distribute experimental reduced scale data to the scientific community
as benchmark datasets.

PLOTS

Equations

240 **Figures**

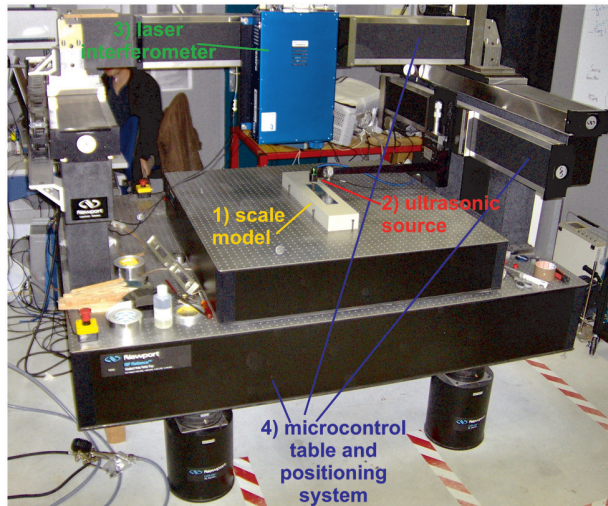


Figure 1: Photograph of the MUSC ultrasonic laboratory (from Bretaudeau et al. (2013)) with its four components: (1) a small-scale model of the underground, (2) an optical table with two automated arms moving above the model, (3) a laser interferometer recording ultrasonic wave propagation at the model surface, and (4) a piezoelectric ultrasonic source generating ultrasonic waves in the model.

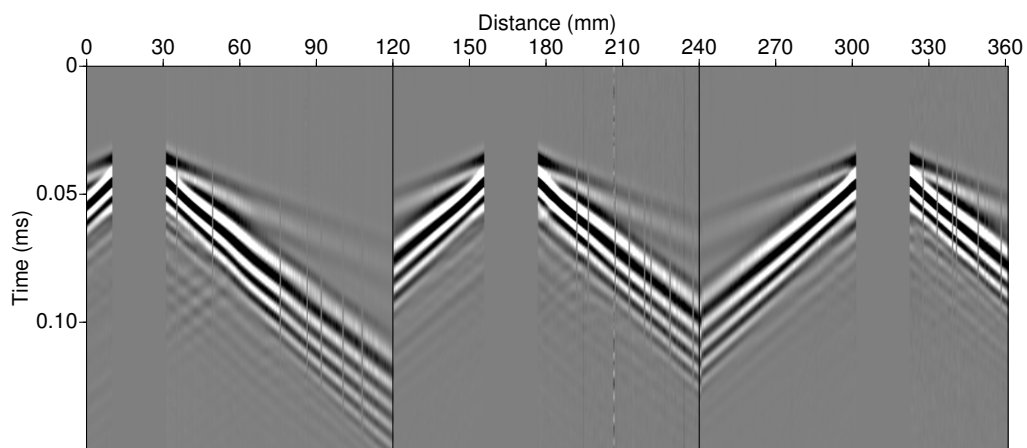


Figure 2: Example of multi-source multi-receiver record on the MUSC bench for a two-layer model (balt).

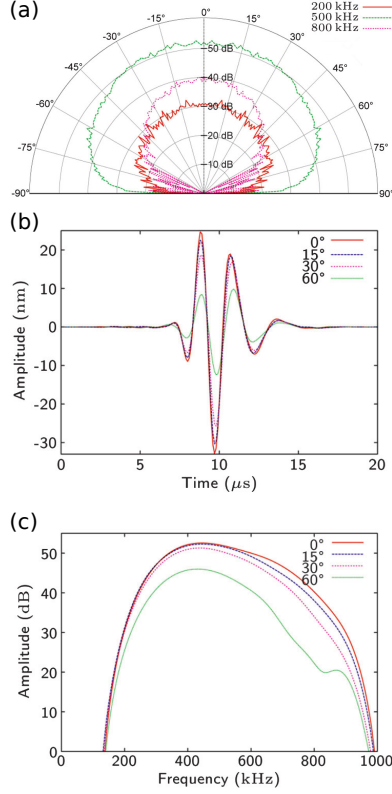


Figure 3: Validation of the piezoelectric source coupled with an adapter (Bretaudeau et al., 2011). (a) Directivity diagrams (dB) for the high-frequency source Panametrics® with conical polyurethane adapter: three frequencies normal particle displacement. (b) Temporal signals and (c) amplitude spectra for the high-frequency source Panametrics® with a conical polyurethane adapter in transmission through a PVC cylinder for various angles of incidence: 0, 15, 30, and 60 degrees normal particle displacement.

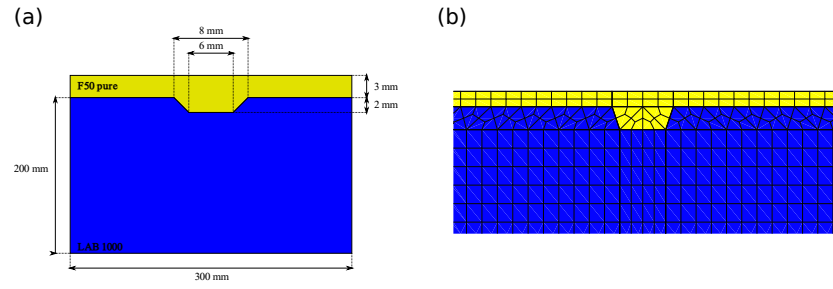


Figure 4: (a) Schematic representation of the so-called *BiAlt* model. (b) Zoom in the two-dimensional mesh designed for the numerical version of the *BiAlt* model.

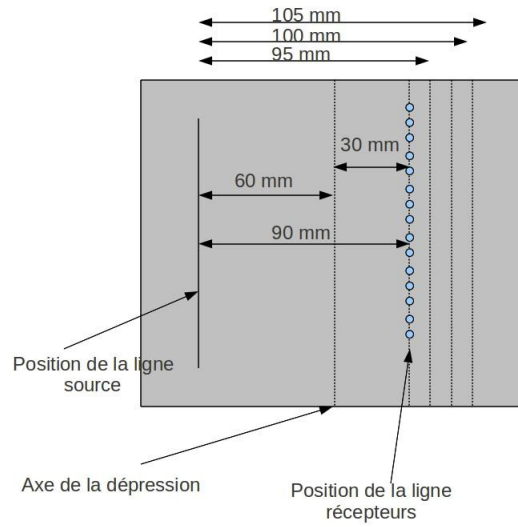


Figure 5: .

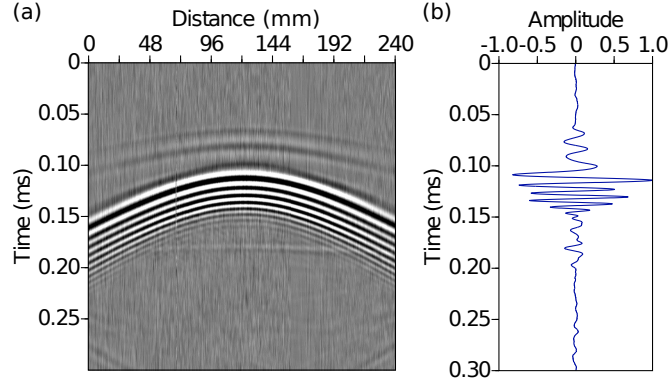


Figure 6: .

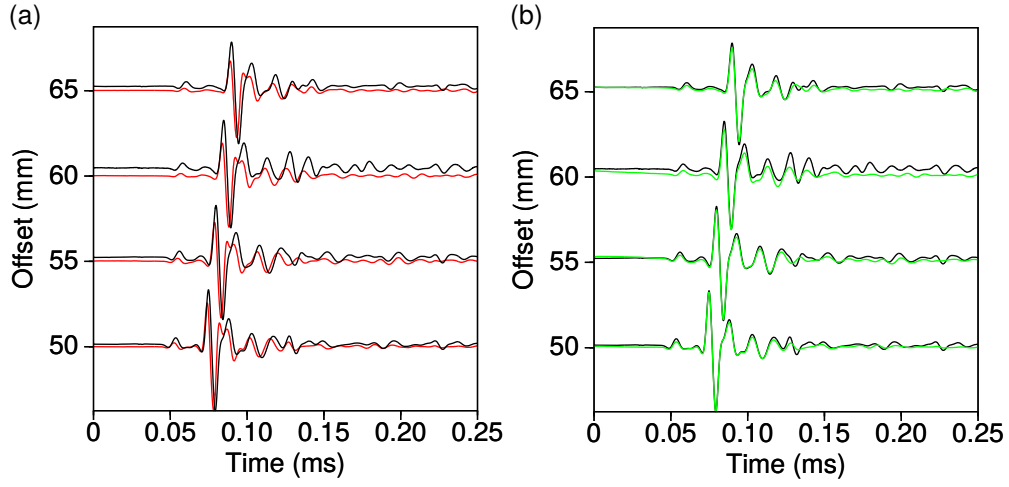


Figure 7: (a) Comparison between an experimental seismogram for a point-source (red) and for a line source (black), for 50, 55, 60 and 65 mm source-receiver offsets respectively. (b) Comparison between an experimental seismogram for a line-source (black), and a point-source response corrected from geometrical spreading (green) for same source-receiver offsets as (a). cc gives the correlation factor between line-source and point-source responses.

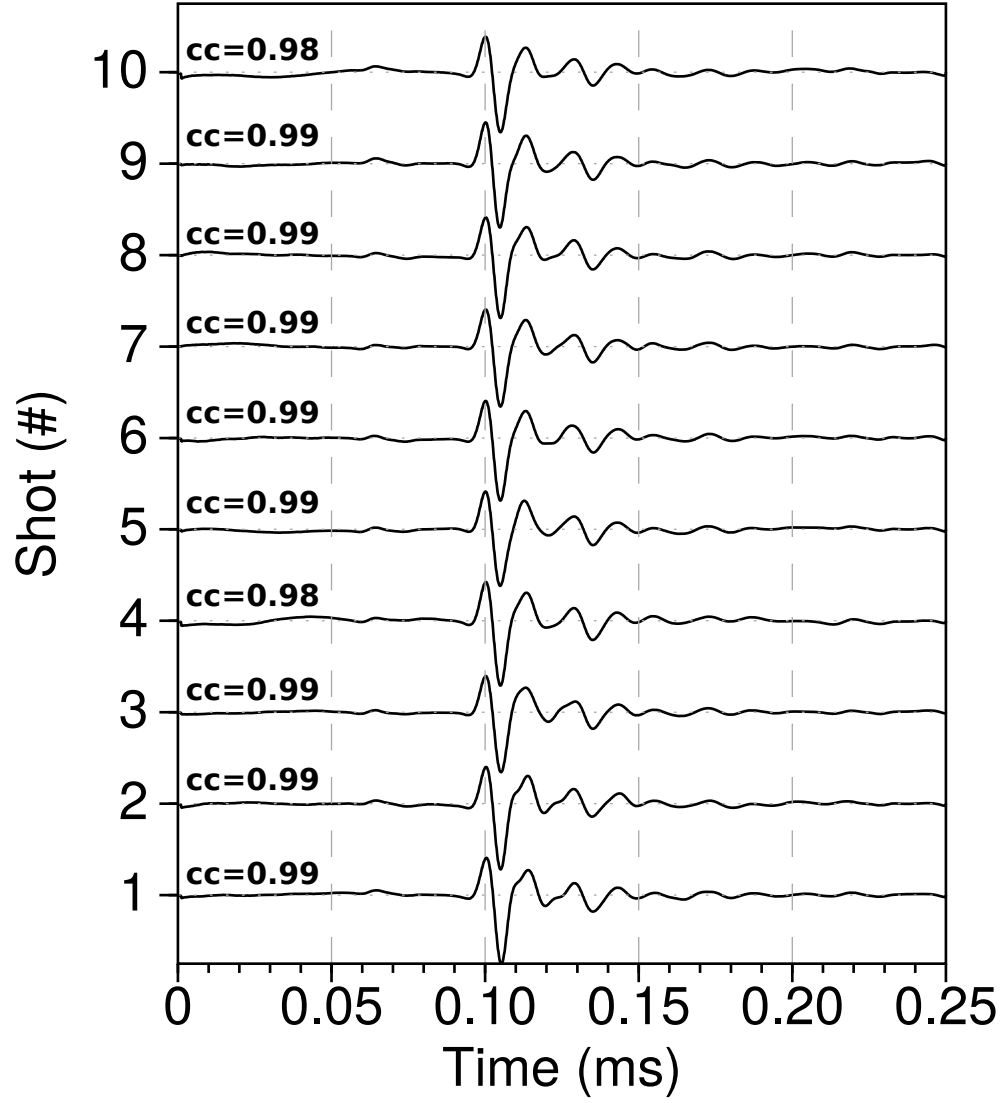


Figure 8: Central trace for each of the ten analogic experiment. **cc** gives the correlation factor of each central trace with respect to a mean trace.

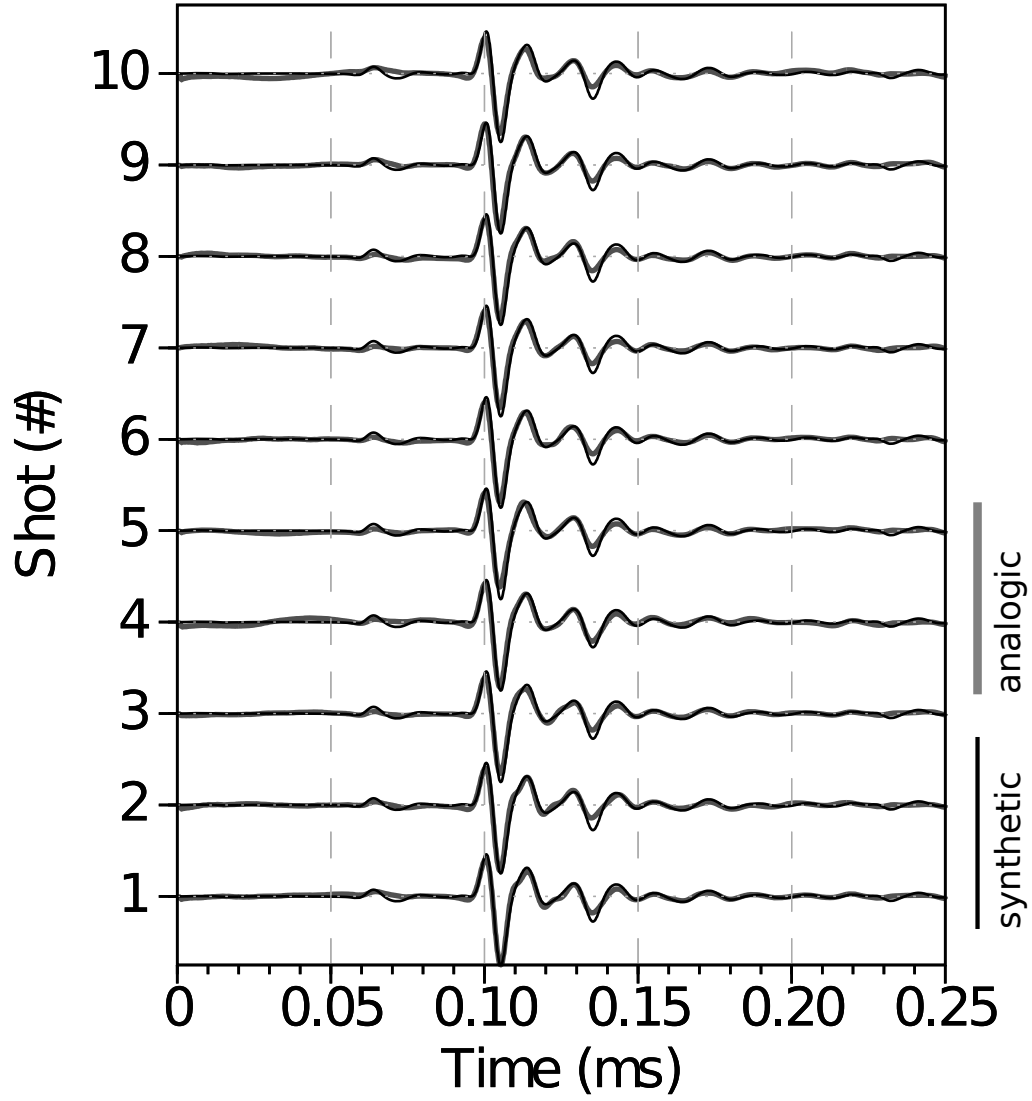


Figure 9: Comparison between analogic central traces (grey) and numerical traces corrected from the estimated effective source (black) for each experiment. **cc** gives the correlation coefficient.

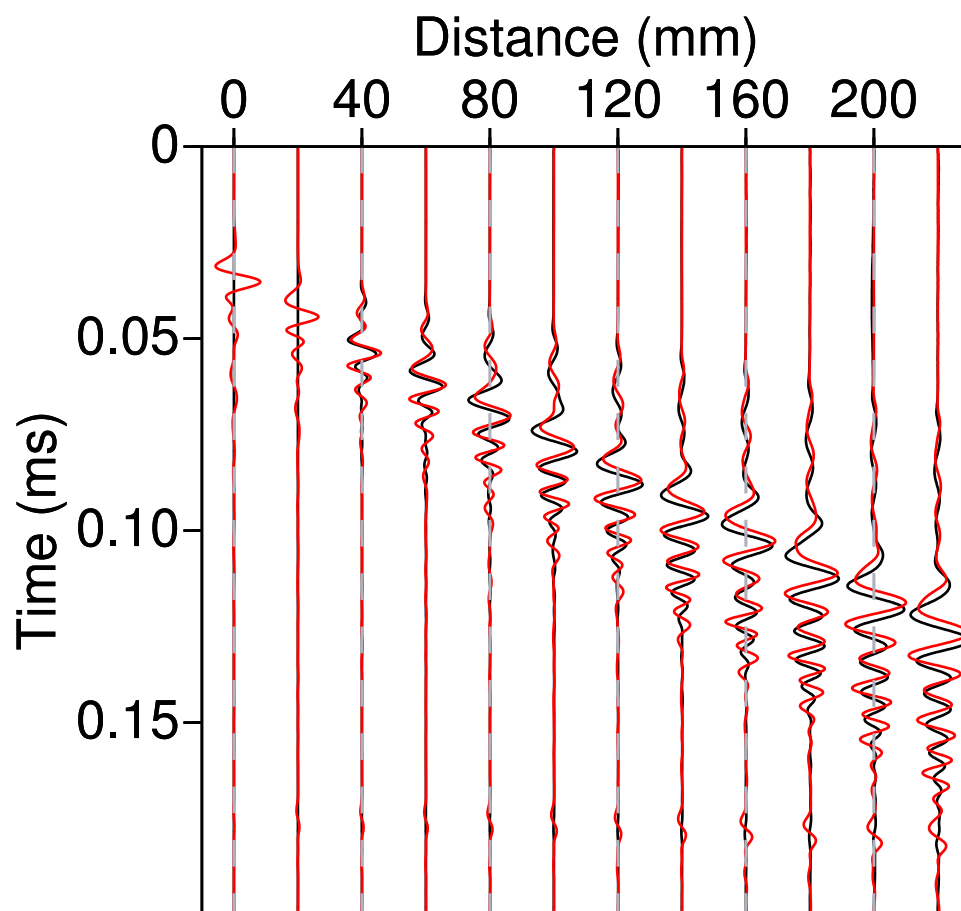


Figure 10: .

Tables

material	V_P (m/s)	V_S (m/s)	V_R (m/s)	ρ (kg/m ³)	Q
Aluminium	5630	3225	–	2700	–
F50 pure	2300	1030	965	1300	30
F50 200%	2820	1425	1328	1766	–
F50 240%	2968	1496	1388	1822	–
LAB1000	2850	1400	1310	1500	75

Table 1: Physical properties of some materials used to build small scale models. V_P , V_S and V_R are the P-wave velocity, S-wave and the Rayleigh wave velocity, respectively. ρ is the density and Q is the quality factor.

	90 mm	95 mm	100 mm	105 mm
$cc1_{init}$	0.702	0.725	0.728	0.728
$rms1_{init}$	0.794	0.760	0.762	0.774
$cc1_{final}$	0.940	0.953	0.951	0.949
$rms1_{final}$	0.358	0.317	0.325	0.343
$cc2_{init}$	0.954	0.987	0.988	0.988
$rms2_{init}$	0.304	0.162	0.155	0.154
$cc2_{final}$	—	—	—	—
$rms2_{final}$	—	—	—	—

Table 2: .

ACKNOWLEDGMENTS

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