Integrator Convergence with Piecewise-Constant Controls