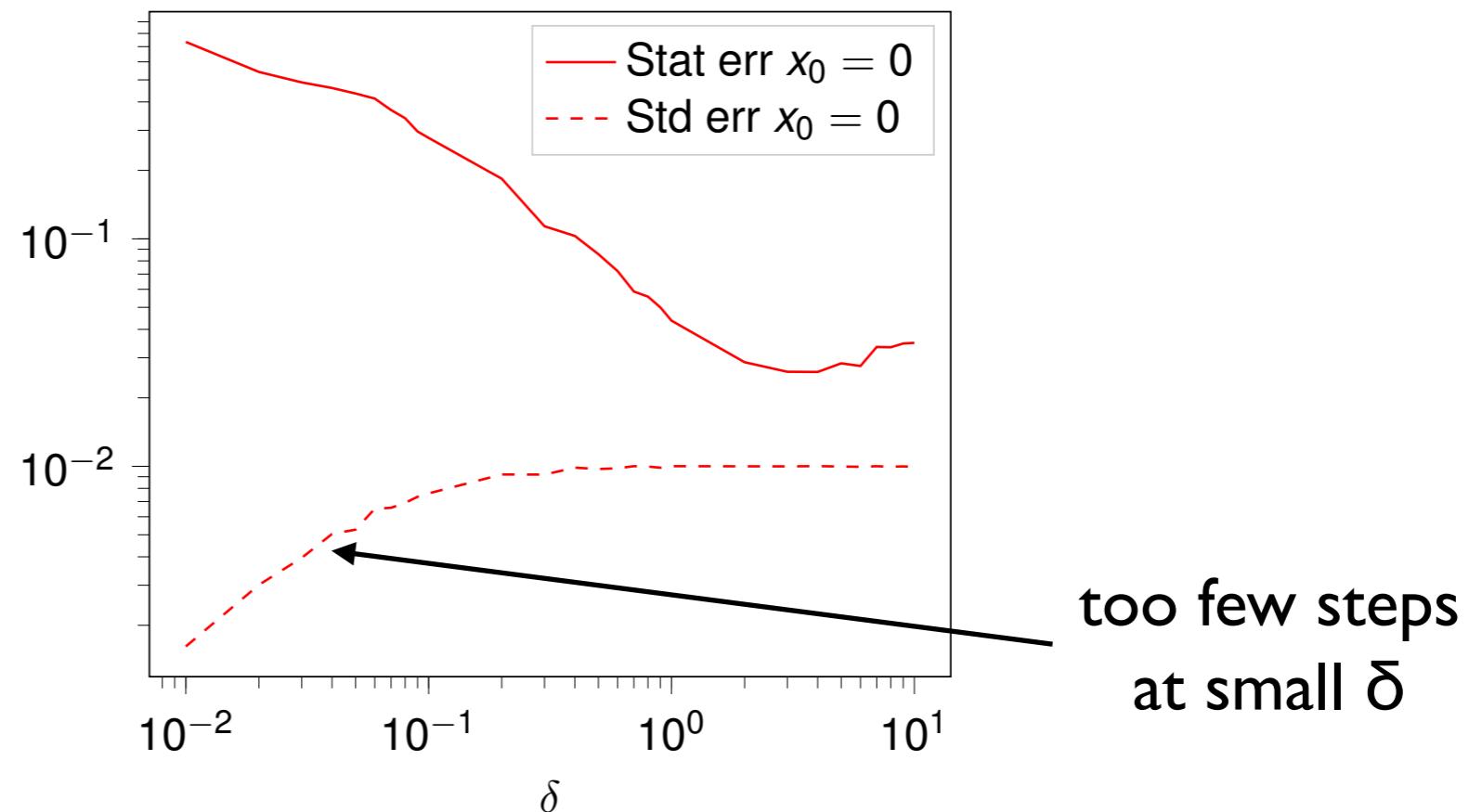


# MCMC exercise

## Calculation errors

- Statistical error:  $Staterr = \langle |\langle f \rangle_{sampled} - \langle f \rangle_{true}| \rangle_{runs}$
- Standard error:  $Stderr = \frac{\sigma}{\sqrt{N}} < Staterr$



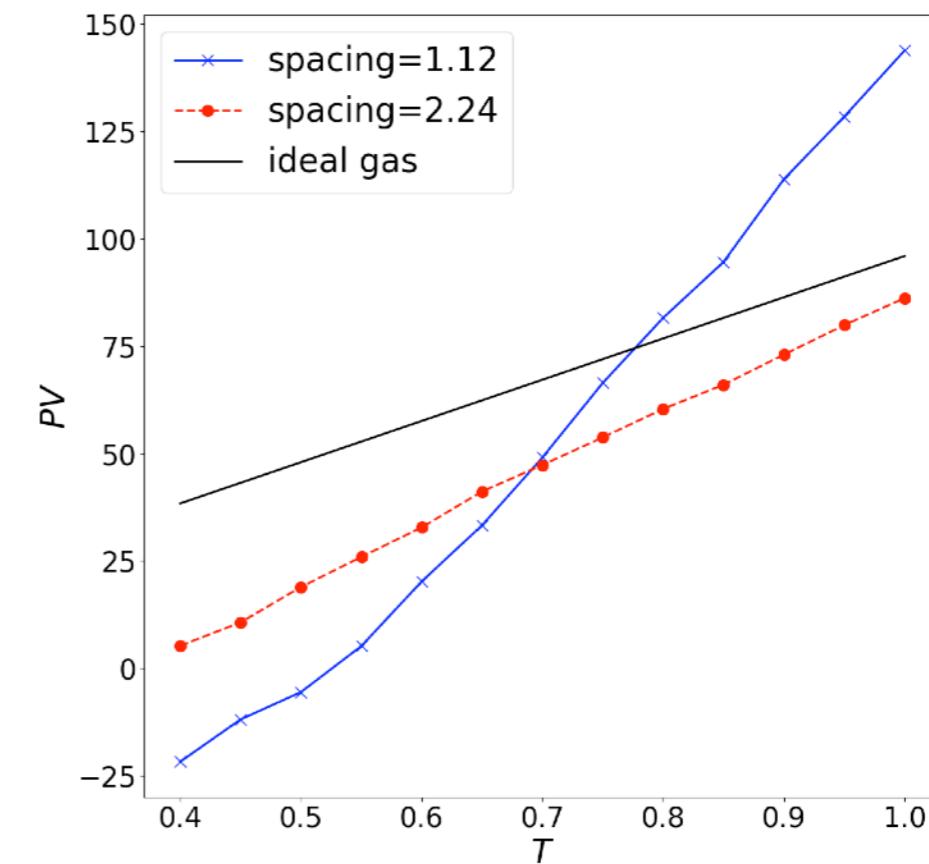
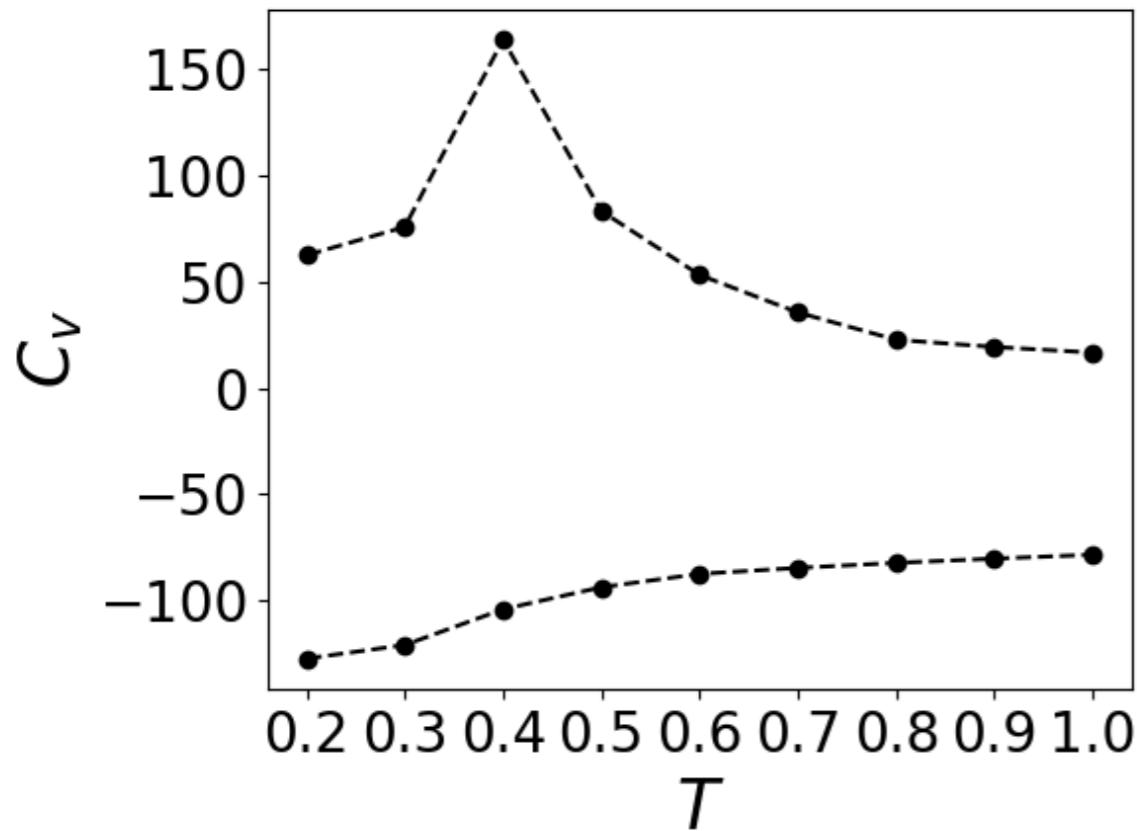
**Figure:** Average statistical error on 200 runs compared with average standard error as a function of  $\delta$  with 10000 samples, a warming time of 100 steps and  $x_0 = 0$

# MD exercise

- Conclusions:
  - A very narrow range of time steps with visible energy drift before things explode
  - In the microcanonical ensemble to total energy ( $E_{\text{pot}} + E_{\text{kin}}$ ) sets the accessible energy
  - The results depend very much on the initial  $E_{\text{pot}}$ , so on the initial coordinates
  - Sampled confirmations, heat capacity and pressure point to a phase transition

# MD observables

Bug in pressure code:  $E_{\text{kin}}$  missing,  
corrected PV result:



Low  $T$ : attraction dominates:  $P$  negative,  $P < P_{\text{ideal}}$   
High  $T$ :  $E_{\text{kin}}$  dominates:  $P$  positive,  
repulsion/exclude volume makes  $P > P_{\text{ideal}}$