**ABSTRACT**

LIU, LONGJU. Precise Optical Positioning Using an Inexpensive USB Microscope Camera.

(Under the direction of Dr. John F. Muth).

The availability of inexpensive Universal Serial Bus(USB) Charge Coupled Device(CCD) and Complementary Metal Oxide Semiconductor(CMOS) cameras with simple interfaces for image acquisition and image processing potentially allow other instruments to be constructed. This thesis describes using a USB digital microscope, consisting of a CCD camera with a high power adjustable lens, to investigate techniques to make inexpensive positioning systems with micron (1x 10-6 m) accuracy.

The first method uses the microscope to image an off-the-shelf micrometer scale and digitally process the image to obtain positions with accuracy comparable to commercial Mitutoyo digital micrometers based on linear variable transformers.

The second method images a digital paper with a coded pattern of closely spaced dots to determine an x-y position. The coding pattern is the one developed and described by the company patents of Anoto. The digital microscope was used to take an image of the dot pattern for positioning. The absolute coordinate of a 6×6 array of dots is determined by the spatial encoding. Image processing techniques are used to determine the relative position between the camera and the paper with the printed dot pattern. This method potentially allows absolute two-dimensional position to be obtained with micrometer accuracy.

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Precise Optical Positioning Using an Inexpensive USB Microscope Camera

by

Longju Liu

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North Carolina State University

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**DEDICATION**

To my parents

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**BIOGRAPHY**

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x

**CHAPTER 1 INTRODUCTION**

Determining the position of one object in relation to reference point is fundamental in many engineering tasks. This thesis describes the investigation of optical positioning methods using an inexpensive camera. These optical methods have the advantage of being precise and non-contact.

A common method of optical positioning uses optical encoders, which can convert mechanical movement into representative electric signals [1-3]. The signals are coded in a predetermined way that can be processed and decoded using a computer program. Optical encoders are especially useful when the movement of the object of interest is simple and clear, for example, to record how far a robot has moved forward or backward[4,11]. The details about several types of optical encoders are discussed in Chapter 2.

When the movement of the object of interest becomes unpredictable, or is in two or three dimensions, it is not always easy to tell the position using optical encoders. Usually, a number of different types of optical positioning sensors are used to form a complicate positioning system to provide the positional information accurately and precisely [5-7].

For the 2D case we can consider using mapping as an analogy, like the GPS (Global Positioning System) determination of latitude and longitude[8], I would like to be able to obtain coordinates for an optically flat surface. The idea is to encode positional information on a surface and then be able to read those positions optically.

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Instead of using multiple complicated and expensive sensors to ‘read’ the information, we utilize a microscopic digital camera [9] to ‘read’ the coordinate information. The most significant advantages include the ease of obtaining images and the dramatic drop in cost; the possibility of relatively high resolution and accuracy is maintained at the same time. On the other hand, computation power and storage space for images has been sharply increased to processing digital images.

Conventional Optical encoders are accurate and quick [1,2,10], but they are expensive due to the precision required during manufacturing[10]. They can also be limited functionally, for example, some encoders are only useful for obtaining relative position, and require measurement reinitialized if the reference position is lost[1,2]. The resolution of optical encoders is often limited to a couple of microns [12]. Considering a simple digital microscope composed of a lens and CCD or CMOS imaging chip, a magnification that covers a field of view of about 100 µm in a 1280 x 1024 pixel camera, results in about 0.2 µm per pixel, and suggests that sub-micron resolution could be obtained.

It is quite straightforward to think about patterning the surface of interest to convert it into a 2-D map. The method that we explore was invented by Anoto Group, known as Anoto Dot Pattern Technology [13]. It is found to work well in digital papers, where the absolute position of pattern is obtained by an electronic pen, which contains a camera that reads the encoded position of the dots [14,15].

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**CHAPTER 2 REVIEW OF PRECISE POSITIONING**

**METHODS**

There are several common methods for precise positioning. Each method has its own field of applications, where it has specific advantages and disadvantages. For example, one of the simplest precise positioning devices is a micrometer. It is very useful when the movement is in one dimension. Many translation stages are made that use a micrometer in order to provide accurate movement, are usually read by the human eye. Veriner micrometers using the English system are typically accurate to 10000th of an inch, or about 2.5 µm. Some metric vernier calipers can be read to an accuracy of about 1 µm [16].

Interferometers are another device that can be used for precise positioning, the Michelson Interferometer[17,37] for example. The movement of the object is related to the optical path difference of a split light of laser beam. The interference fringes observed in optical intensity change as the object moves; the bright constructive interference change to dark destructive interference as the optical path changes by one-half wavelength[37]. Changes in the length of one arm of the instrument can be counted using a photodiode as each intensity change represents an increment in motion of one-quarter of a wavelength. For more precise measurements one can measure the relative phase by monitoring the intensity within one fringe. With this type approach with appropriate control electronics allows sub-angstrom linear travel to be monitored.

Optical encoders are also very popular because of their ease of use, and these will be introduced in the following paragraphs. Optical encoders are usually electro-mechanical

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devices which convert the mechanical movement, or the position information of a mechanical unit, into representative electric signals by blocking and unblocking light, or by the reflection of light [1-3]. The common components of an optical encoder are a light source, a condenser lens, a scanning reticle, a patterned disk and photovoltaic cells [18].

There are several ways of classifying optical encoders, which depending on whether the mechanical movement is angular or linear, and are classified as rotary or linear optical encoders[18,19]. Each of these two types of optical encoders can be further sub-divided into two main types, known as absolute and incremental [1,2].

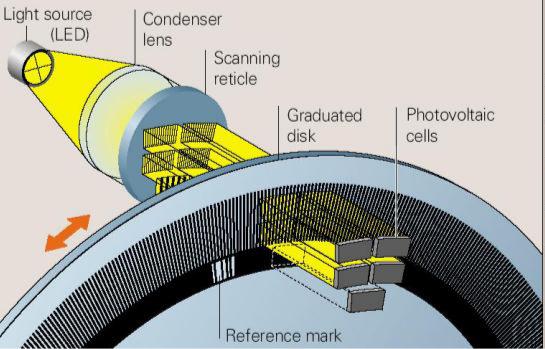
**2-1 Rotary optical encoders**

Rotary optical encoders are utilized to convert angular motion or position of a shaft. If a rotary encoder is designed to code the angular motion, it is called an incremental rotary encoder. The output of this type of encoder usually provides information which can be further processed into measured quantities, such as velocity, position, RPM and distance[1]. Another type of rotary encoder is the absolute rotary encoder, which provides an output of the current position of the shaft and is usually made an angle transducer[1]. Both of these two types are similar in construction and are made largely in the same manner[18,19]. The main differences lie in the pattern on the disk and the method of interpreting the code.

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**2-1-1 Incremental rotary encoder**

One typical incremental rotary encoder has the structure shown in Figure 2-1.

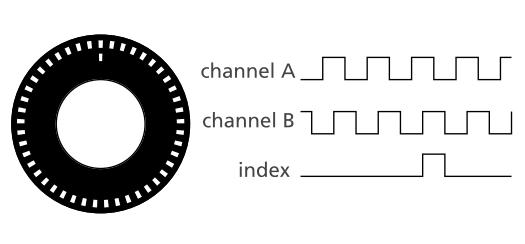


**Figure 2-1 The structure of an incremental rotary encoder[18]**

The pattern on the periphery of the disk of an incremental rotary encoder is made up with a single track of equally spaced transparent and opaque sectors. By counting the numbers of switching of the transparent and opaque sectors, the motion of disk is measured. The number of such switches that occur per revolution is defined as disk count of the incremental rotary encoder [1].

A transparent section as a reference mark is added to the inner side of the track in order to generate a signal that occurs once per revolution. This signal is used to indicate an absolute position as an index. There are two sensors used in a rotary encoder, which are labeled A and B respectively and shown in Figure 2-3. The outputs of sensor A and sensor B creates two signal trains called channel A and channel B, see Table 2-1 [1,2].

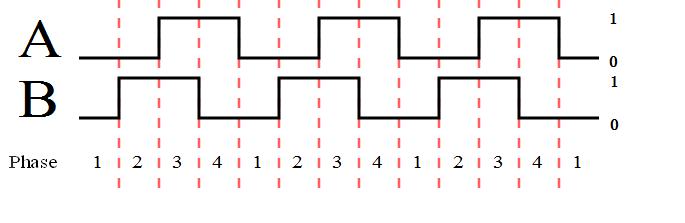
5



**Figure 2-2 Illustration of the disk[1]**

The sensor B is shifted a quarter of the pitch of a transparent/opaque section pair from the sensor A so that they are accurately 90 degrees out of phase. There are several reasons that two sensors are used, but the main one is that one output is incapable of determining the direction of rotation. With an additional output, the processing unit is then capable of telling which channel is leading the other one and the rotation direction is determined too [3].

For most encoders, the clockwise direction is defined as the signal of channel A becomes ‘1’ before that of channel B [3].



**Figure 2-3 The phase change of incremental encoder under clockwise rotation[3]**

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**Table 2-1 Phases of incremental rotary encoder[3]**

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Clockwise rotation | | | Counter-clockwise rotation | | |
|  |  |  |  |  |  |
| Phase | Ch A | Ch B | Phase | Ch A | Ch B |
|  |  |  |  |  |  |
| 1 | 0 | 0 | 1 | 1 | 0 |
|  |  |  |  |  |  |
| 2 | 0 | 1 | 2 | 1 | 1 |
|  |  |  |  |  |  |
| 3 | 1 | 1 | 3 | 0 | 1 |
|  |  |  |  |  |  |
| 4 | 1 | 0 | 4 | 0 | 0 |
|  |  |  |  |  |  |

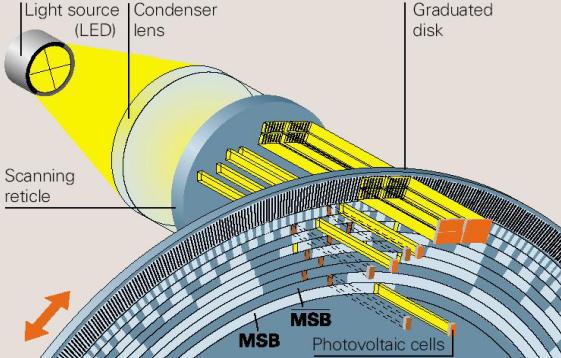
A third signal is generated by the reference mark every complete revolution, and makes it possible for an incremental rotary encoder to determine the angular position.

The incremental rotary encoders are not as accurate as absolute encoders, especially when the rotation speed is too high or too low. Because under these circumstance, misreading errors caused by missing counts or backward counts can easily occur. This would eventually result in a wrong output.

**2-1-2 Absolute rotary encoder**

A typical absolute rotary encoder has the structure shown in Figure 2-4.

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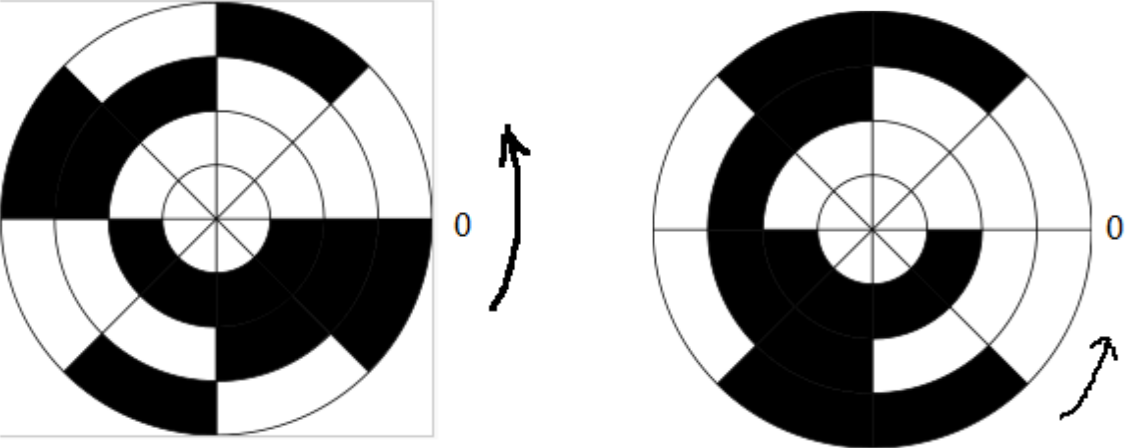


**Figure 2-4 The structure of an absolute rotary encoder[18]**

Figure 2-4 shows the most significant difference of an absolute rotary encoder and an incremental rotary encoder is that the periphery of the disk is uniquely patterned. The pattern converts the rotation of the shaft into a signal called Gray Code[20,42,43]. The reason that Standard Binary Encoding is not used is that determining the angle becomes impossible when the disk stops between two adjacent sectors. And in fact, the contacts cannot be produced to be perfectly aligned, makes the contacts switches from 1 to 0 or 0 to 1 at different times. If the order of switching is Contact 2, Contact 1 and Contact 3, and the starting sector is sector 1 reading (0, 0, 0), the sequence of the codes is shown as: (0,0,0) - >(0,1,0)->(1,1,0)->(1,1,1)->(0,0,1). The corresponding sequence of sectors, 1->3->7->8, is not acceptable since the next sector after sector 1 (0,0,0) should be sector 2 (0,0,1).

A comparison of the Standard Binary Encoding and the Gray Code is shown for a simple 3-contact absolute encoder in Table 2-2.

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**Figure 2-5 (a) A three-contact Standard Binary Encoded disk (b) A three-contact Gray Coded disk[35]**

**Table 2-2 Comparison of Standard Binary Code and Gray Code[35]**

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
|  | Standard Binary Encoding | | |  | Gray Code |  |  |
|  |  |  |  |  |  |  |  |
| Sector | Contact 1 | Contact 2 | Contact 3 | Contact 1 | Contact 2 | Contact 3 | Angle(°) |
|  |  |  |  |  |  |  |  |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0~45 |
|  |  |  |  |  |  |  |  |
| 2 | 0 | 0 | 1 | 0 | 0 | 1 | 45~ 90 |
|  |  |  |  |  |  |  |  |
| 3 | 0 | 1 | 0 | 0 | 1 | 1 | 90~135 |
|  |  |  |  |  |  |  |  |
| 4 | 0 | 1 | 1 | 0 | 1 | 0 | 135~180 |
|  |  |  |  |  |  |  |  |
| 5 | 1 | 0 | 0 | 1 | 1 | 0 | 180~225 |
|  |  |  |  |  |  |  |  |
| 6 | 1 | 0 | 1 | 1 | 1 | 1 | 225~270 |
|  |  |  |  |  |  |  |  |
| 7 | 1 | 1 | 0 | 1 | 0 | 1 | 270~315 |
|  |  |  |  |  |  |  |  |
| 8 | 1 | 1 | 1 | 1 | 0 | 0 | 315~360 |
|  |  |  |  |  |  |  |  |

The same problem is examined for the Gray Code. If the order of switching is Contact 2, Contact 1 and Contact 3, and the starting sector is sector 1 reading (0, 0, 0), the sequence of the codes is shown as: (0,0,0) ->(0,0,0)->(0,0,0)->(0,0,0)->(0,0,1). The corresponding

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sequence of sectors is 1->1->1->1->2. The change of sector is correct and stable, because there is only one contact that changes state when one sector changes to the next sector in Gray Code.

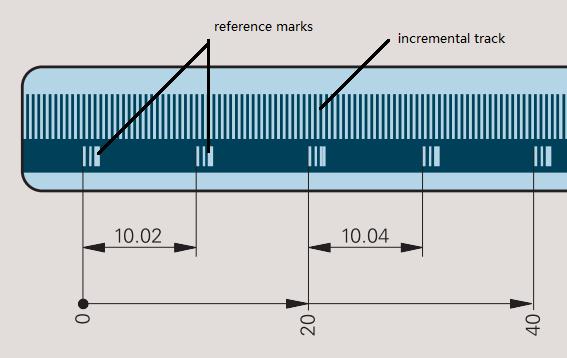
Actually the pattern on the disk of an absolute array can be rather complicated and divide the disk into many more parts instead of 23 = 8, and requires more contacts.

**2-2 Linear Optical Encoders**

Linear optical encoders are made to encode linear positions using optical techniques. Like rotary optical encoders, linear optical encoders are divided into two main types— incremental and absolute linear encoders [2,19]. The difference of between incremental linear optical encoders and absolute optical encoders is the reference for the graduations on the track [19].

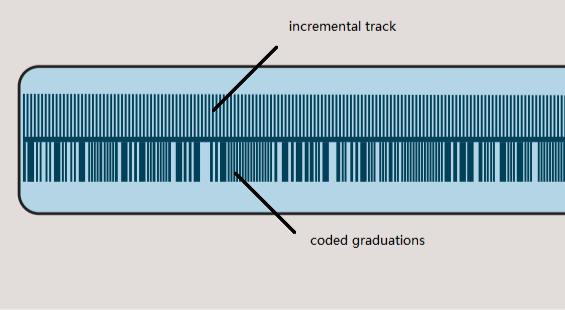
An incremental linear encoder usually has two tracks. The first track has graduations that are equally distributed, and the second track has a series of special coded graduations as reference marks. A schematic view is shown in Figure 2-6. With the help of the reference marks, it’s not difficult to determine the displacement and motion direction using incremental linear encoders.

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**Figure 2-6 A schematic view of the incremental linear encoder [19]**

Absolute linear encoders also have two tracks. One track has graduations that are distance-coded, and the other one is incremental with equally distributed graduations. A schematic view is shown in Figure 2-7.



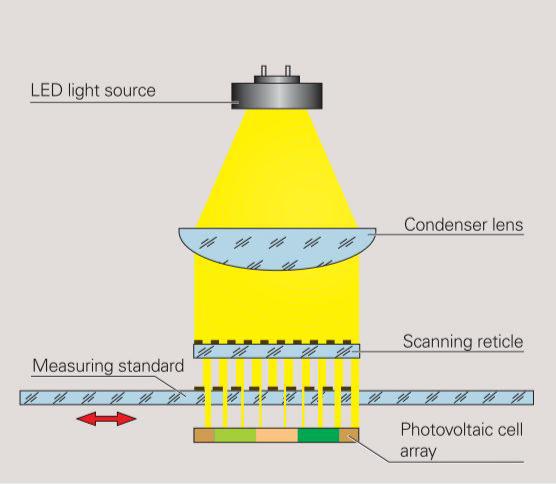
**Figure 2-7 A schematic view of the absolute linear [19]**

There are several approaches used to code the position using linear encoders. When the movement is relatively large, and the requirement for resolution is relatively low, image

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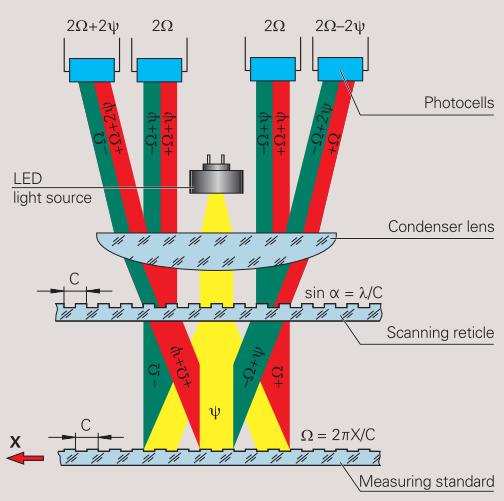
scanning is used [19]. A scanning reticle and a measuring standard scale are placed relative to each other. The scanning reticle is made of transparent materials that parallel light can passes through.

The incident light is modulated by the gaps of these two gratings when the measuring standard is moving. When the gaps are aligned, light is not blocked and can be detected by the photovoltaic cell array. The opposite case occurs when the gaps of one grating is blocked by the line of the other, and no light can pass measuring standard. The illustration is shown in Figure 2-8. On the occasions where the movement is relatively small or high resolution is needed, another method called interferential scanning should be applied. A schematic view is shown in Figure 2-9.



**Figure 2-8 Image scanning method [19]**

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**Figure 2-9 Interferential scanning method[19]**

When the light passes through the scanning reticle, it is diffracted into three beams with almost equal intensity with the order -1, 0,+1. These beams are diffracted again at the scales of the measuring standard and reflected back to the scanning reticle where interference occurs[19].

If relative motion occurs between the scanning reticle and the measuring standard, there will be phase shifts for the light with order +1 and -1. If the grating moves by one period, the shift of the “+1” light will be 2π in the positive direction while the shift of the “-1” light is 2π in the negative direction. Thus, one period change of the grating causes a change of 2 periods in the signal light.

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**2-3 Summary**

A review of four common optical encoders is presented in this chapter. The purpose is to investigate the features of these encoders and point out their advantages and disadvantages. This examination is to determine if they are suitable for the optical positioning using an ordinary camera.

Each of these optical encoders has favorable properties of high accuracy, high reliability and can code the position without direct contact [18,19]. However they are relatively complex and can require attachment of precision machined encoding strips and multiple detectors. They are also limited to measurement in one dimension and can’t freely code the position in higher dimensions.

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**CHAPTER 3 Obtain the Reading of the Micrometer with a**

**Microscopic Camera**

As an example of measuring linear motion we consider using a digital microscope with and off-the-shelf micrometer. The micrometer is widely used for precise measurement of small distance such as moving translation stages and optical components. The principle idea is that by using a digital camera higher accuracy can be obtained rather than reading by eye.



**Figure 3-1 The experimental arrangement (left) and the camera used (right)[21]**

The experimental arrangement is shown in Figure 3-1, and consists of a digital microscope and bracer to hold the microscope a translation stage with a digital micrometer. The camera is used to take pictures of the scales on the sleeve of the micrometer. The bracer and clamp is used to hold the camera and adjust its position. The translation stage is controlled by a micrometer. It is a Mitutoyo product, Digimatic Micrometer Heads - Series

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350 in this thesis[16]. When the thimble of the micrometer is being rotated, the translation stage will move along the same direction. To check the accuracy of our method, the micrometer is also equipped with a digital readout. This readout device uses a linear variable differential transformer with a custom chip that contains calibration data to measure the positions. The rated accuracy of the digital readout is 0.001 mm or 1 µm and are displayed on a small LCD screen [16].

The reading on the LCD screen provides a reference that we compare with our method. The important parameters of the micrometer in this thesis are shown below [16]:

1. Lead: 0.025 inch
2. Range: 1 inch
3. The number of the graduated markings on the thimble: 25, starting from ‘0’ to ‘24’.
4. The number of the major graduated markings on the sleeve: 11, starting from ‘0’ to ‘10’.
5. The number of the minor graduated markings on the sleeve: 20 above the axial line, and 40 sub-divisions below the axial line.

From the above parameters, it’s clear that if the thimble is screwed out by one turn, the axial movement of the micrometer will be 0.025 inch to the right. And the edge of the thimble will move from the central line of one minor graduation to that of an adjacent minor graduation. Meanwhile, the reading will change by 0.025/25 = 0.001 inch when the thimble

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is screwed out by one division on the thimble. If the graduation on the thimble that coincides with the axial line was graduation 0, then it would become graduation 1 after this operation. The reading of the micrometer is determined by how many divisions and sub-divisions are visible on the sleeve, and which graduation on the thimble coincides with the axial line or an estimated position when there is no such a graduation:

R = S \* 0.02495 + G\*0.0010.

Where R is Reading, S is the number of complete sub-divisions that can be seen on the sleeve and G is the estimated position on the thimble that coincides with the axial line.

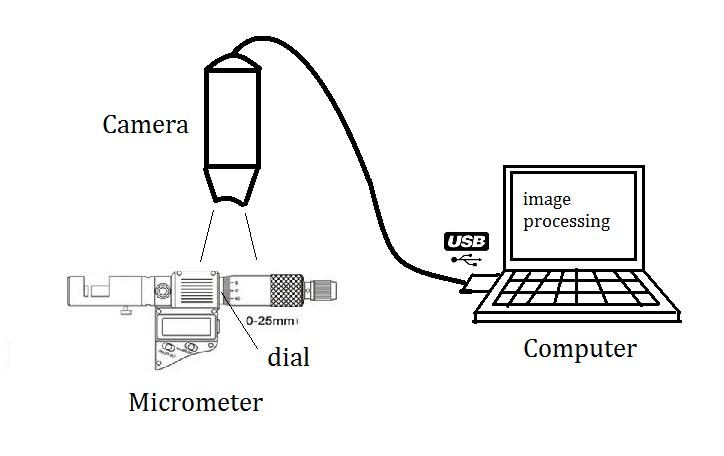


**Figure 3-2 Example of experimental image**

Thus in our experiments what we want to be able to do is accurately determine an estimate for the graduation. If we know that value to high accuracy we will have an accurate measurement of position. For example as shown in Figure 3-2, Graduation 0 and one sub-division are visible on the sleeve, Graduation 10 on the thimble is seen to coincide with the axial line, and thus R = 1\*0.025 +10\*0.001 = 0.035 inch.

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In general, the idea is to take a picture of the micrometer (Figure 3-3). Then digitize the image to identify the positions of the rotating horizontal lines, and compare the position of those lines with the horizontal reference line. Then using the knowledge of the spacing of the marks on the micrometer determines the position accurately.



**Figure 3-3 Obtaining the reading of a micrometer using a camera**

This was accomplished in two steps. First using the LCD readout of the micrometer a series of calibration images were taken for each turn of the thimble from graduation 0 to graduation 24. This establishes a bijection of the axial line and horizontal lines on the thimble. The program ran these 25 images as a batch file and then was used to form a table, where the ration of the distance between the axial line and the horizontal lines corresponds to the linear motion of the micrometer. This process is described in the section titled standard pictures. Using these images, we can then run an experiment where the relative spacing of the lines is

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expressed as a ratio. This can then be modified by a calibration factor using the series of calibration images that have been obtained.

**3-1 Obtaining standard pictures**

A number of images focused on the ROI are taken using the platform shown in Figure

3-1. There are several requirements when taking the images:

1. The images should be taken in the same surroundings with almost the same light source, the same shooting angle and the same distance from the lens;
2. The gray-scale of the images should be as even as possible. Avoid the situation that some parts of the images are too dark or too bright;
3. The images should contain mainly the scales of the micrometer. And the ROI should be made sure as clear as possible.

An example of the obtained images is shown in Figure 3-4.

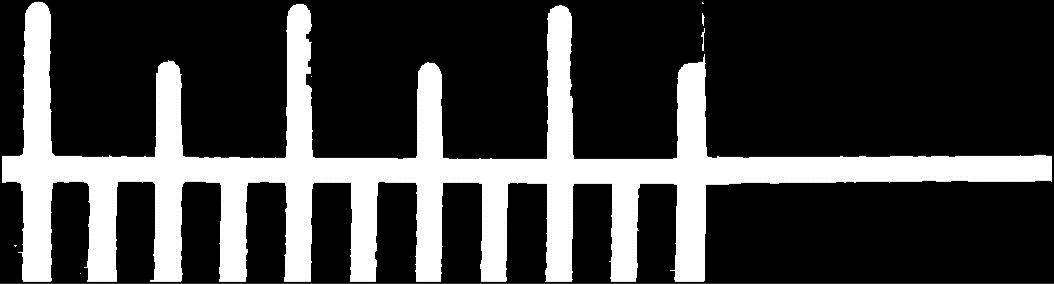
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**Figure 3-4 An example reference image of the ROI with a reading of 0.24995**

**3-2 Processing of the standard images**

The processing includes crop, incline correction, threshold, removing noise and converting the image from gray scale to black and white. As long as the images meet the requirements stated above, a batch file can complete the processing quickly for many images at a time. One example of the processed image is shown in Figure 3-4. Unnecessary part of the image has been cropped out. These reference images are then stored for future use.

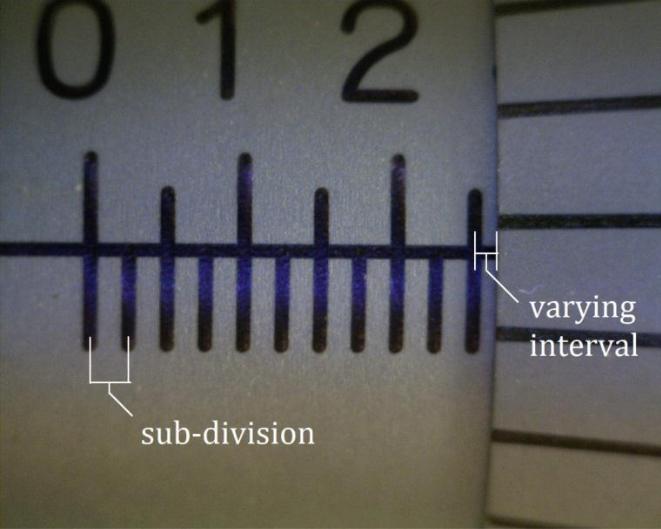


**Figure 3-5 A binary image of the processed image**

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**3-3 Calculation of the ratio**

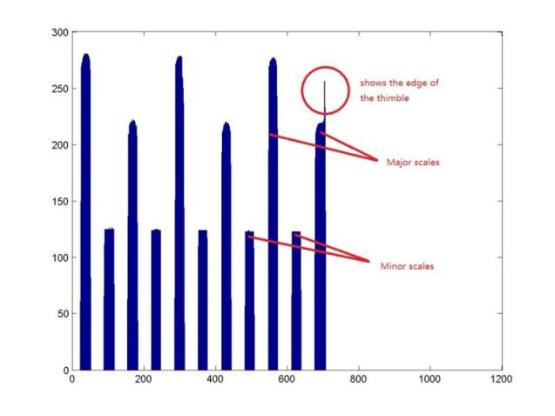
The special ratio refers to the ratio of the length of the last interval, which is not a complete sub-division and the average length of the complete sub-divisions. The lengths are obtained in pixels. (Figure 3-5)



**Figure 3-6 A illustration of the sub-division and the varying interval**

Continue taking Figure 3-4 as an example, a histogram of the distribution is shown in Figure 3-6. The peaks have shown the locations of the linear graduations on the sleeve. The thin small line shows the position of the edge of the thimble, which has overlapped with the right edge of the last graduation on the sleeve.

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**Figure 3-7 An intensity histogram of the reference image**

The locations of the linear graduations are shown in Table 3-1. p is the position in

pixels.

**Table 3-1 Locations of linear graduations of a reference image**

|  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| NO. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| p | 52 | 117 | 183 | 247 | 313 | 377 | 443 | 508 | 573 | 638 | 706 |
|  |  |  |  |  |  |  |  |  |  |  |  |

Use the value of the position of one graduation to subtract that of the former one, the lengths of the sub-divisions are obtained and shown in Table 3-2.

**Table 3-2 Lengths of the sub-divisions of a reference image**

|  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| NO. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|  |
|  |  |  |  |  |  |  |  |  |  |  |
| Length |  |  |  |  |  |  |  |  |  |  |
| (pixels) | 65 | 66 | 64 | 66 | 64 | 66 | 65 | 65 | 65 | 68 |
|  |  |  |  |  |  |  |  |  |  |  |

The average length of the former 9 sub-divisions is 65.11. The reason why the last sub-division has a larger length is due to the overlapping of the edges of the 11th graduation

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and the thimble. Therefore, the position of the last graduation in this image is not reliable. This problem is solved when images were taken for larger readings that the 11th graduation can be distinguished. It is found that the position of the 11th graduation should be 705 by comparison with other images. In this way the last graduation position are corrected for all other similar situations.

As a result, the length of the varying interval is about 1 pixel in this image. The ratio is defined as r,

The graduation on the thimble that coincides with the axial line is graduation 0. It is desirable that the ratio is calibrated to 0.00%. Same procedures are done for other 23 reference images and a bijection of the ratio and graduation is obtained and shown in Table 3-3.

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**Table 3-3 G and corresponding ratio of reference images**

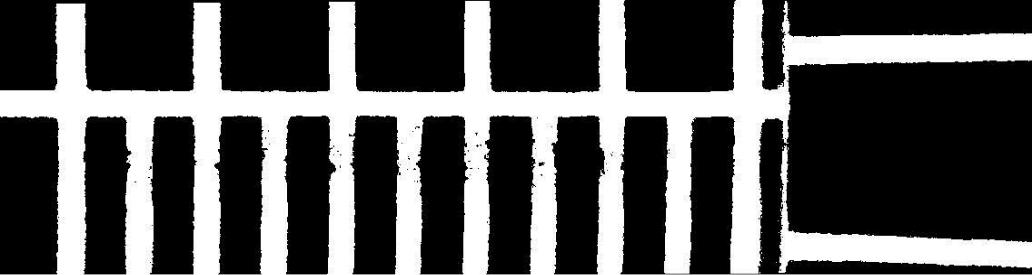
|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Original | Original | Improved | Improved |  | Ideal |
| length | ratio | length | ratio | G | ratio'' |
|  |  |  |  |  |  |
| 1 | 1.53% | 0 | 0.00% | 0 | 0.00% |
|  |  |  |  |  |  |
| 4 | 6.13% | 3 | 4.59% | 1 | 4.00% |
|  |  |  |  |  |  |
| 6 | 9.19% | 5 | 7.66% | 2 | 8.00% |
|  |  |  |  |  |  |
| 8 | 12.25% | 7 | 10.72% | 3 | 12.00% |
|  |  |  |  |  |  |
| 11 | 16.85% | 10 | 15.31% | 4 | 16.00% |
|  |  |  |  |  |  |
| 14 | 21.47% | 13 | 19.94% | 5 | 20.00% |
|  |  |  |  |  |  |
| 15 | 22.94% | 14 | 21.41% | 6 | 24.00% |
|  |  |  |  |  |  |
| 18 | 27.57% | 17 | 26.03% | 7 | 28.00% |
|  |  |  |  |  |  |
| 21 | 32.21% | 20 | 30.67% | 8 | 32.00% |
|  |  |  |  |  |  |
| 23 | 35.28% | 22 | 33.74% | 9 | 36.00% |
|  |  |  |  |  |  |
| 27 | 41.41% | 26 | 39.88% | 10 | 40.00% |
|  |  |  |  |  |  |
| 31 | 47.55% | 30 | 46.01% | 11 | 44.00% |
|  |  |  |  |  |  |
| 33 | 50.69% | 32 | 49.16% | 12 | 48.00% |
|  |  |  |  |  |  |
| 35 | 53.68% | 34 | 52.15% | 13 | 52.00% |
|  |  |  |  |  |  |
| 38 | 58.37% | 37 | 56.84% | 14 | 56.00% |
|  |  |  |  |  |  |
| 40 | 61.44% | 39 | 59.91% | 15 | 60.00% |
|  |  |  |  |  |  |
| 43 | 65.95% | 42 | 64.42% | 16 | 64.00% |
|  |  |  |  |  |  |
| 46 | 70.66% | 45 | 69.12% | 17 | 68.00% |
|  |  |  |  |  |  |
| 48 | 73.62% | 47 | 72.09% | 18 | 72.00% |
|  |  |  |  |  |  |
| 51 | 78.22% | 50 | 76.69% | 19 | 76.00% |
|  |  |  |  |  |  |
| 54 | 82.95% | 53 | 81.41% | 20 | 80.00% |
|  |  |  |  |  |  |
| 57 | 87.56% | 56 | 86.02% | 21 | 84.00% |
|  |  |  |  |  |  |
| 60 | 92.17% | 59 | 90.63% | 22 | 88.00% |
|  |  |  |  |  |  |
| 64 | 98.16% | 63 | 96.63% | 23 | 92.00% |
|  |  |  |  |  |  |
| 66 | 101.38% | 65 | 99.85% | 24 | 96.00% |
|  |  |  |  |  |  |

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The original length and original ratio stands for the interval length and the ratio that obtained from the last step directly. And it’s not so accurate and useful as can be seen in the last row of Table 3-4 that the ratio exceeds 100% when graduation 24 coincide with the axial line. We assume that there is a system error and therefore a calibration is needed. The result is the improved length and improved ratio. They are obtained by subtracting 1 pixel from the original length. G is the number of the graduation that coincides with the axial line. The ideal ratio is obtained by dividing G by 25.

The next step is to obtain the reading of an unknown experiment image by interpolating its ratio *r* into Table 3-3.

One processed example image is shown as Figure 3-8.



**Figure 3-8 A processed example image**

The locations of the graduations and the length of the sub-divisions are obtained and shown in Table 3-4.

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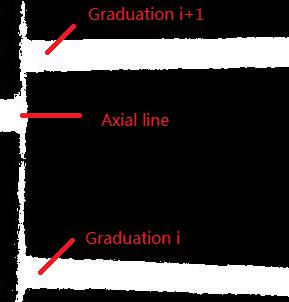
**Table 3-4 The locations of the graduations and the length of the sub-divisions of the experimental image**

|  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| NO. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 11.X |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| p | 96 | 169 | 244 | 317 | 392 | 465 | 541 | 614 | 689 | 762 | 840 | \*870 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| Length | 73 | 75 | 73 | 75 | 73 | 76 | 73 | 75 | 73 | 78 | \*\*30 | -- |
|  |  |  |  |  |  |  |  |  |  |  |  |  |

* The position of the edge of the thimble
* The length of the varying interval.

The average length of the sub-divisions is 74.4, and the improved ratio is roughly

By looking up Table 3-3, G of this image is found to be between 9 and 10. The exactly position is calculated another way. The right part of the image is extracted and shown as Figure 3-8.

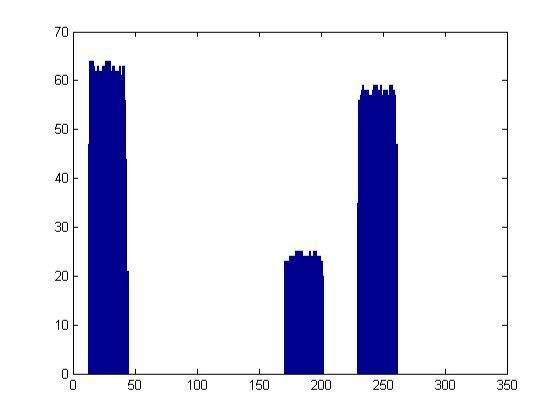


**Figure 3-9 The right part used to calculate the position of the axial line**

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*i* = 9 in Figure 3-8. As long as the exact position where the axial line coincides withthe edge of the thimble is obtained, the G for this image can be determined precisely.

Therefore, another intensity histogram is made and shown in Figure 3-9.



**Figure 3-10 The histogram of the right part of the experiment image**

The three peaks represent the positions of Graduation 9, the axial line and Graduation 10 respectively.

**Table 3-5 Calculation of the precise location of the rotary graduations**

|  |  |  |  |
| --- | --- | --- | --- |
|  | Left edge position | Right edge | Mean Value |
|  | (pixel) | position (pixel) | (pixel) |
|  |  |  |  |
| Graduation 9 | 13 | 44 | 28.5 |
|  |  |  |  |
| Axial line | 171 | 202 | 186.5 |
|  |  |  |  |
| Graduation 10 | 230 | 261 | 245.5 |
|  |  |  |  |

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The ratio of the distance between Graduation 9 and Axial line and the distance between Graduation 9 and Graduation 10, which is defined as , is found to be:

The final value of the reading is expected to be:

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  |  | . | | |
| The reading on the LCD screen is | |  |  | . Take this reading as the |
| reference, the error is | |  |  |  |
|  |  |  |  | . |
|  |  |  |

It is in good agreement with the digital readout, and demonstrates the principle that high accuracy can be obtained using image processing methods.

Potentially this type of measurement could be integrated into a small package and image processing algorithms could be incorporated on a specialized chip.

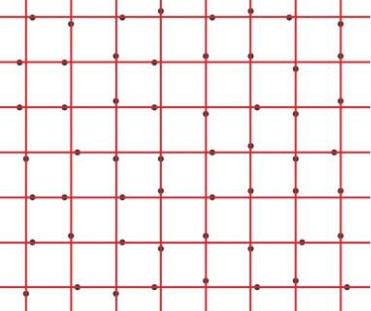
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**Глава 4 Anoto Dot Pattern Technology**

**4-1 Введение**

Anoto Dot Pattern Technology была изобретена и разработана Anoto AB Group для использования с их цифровым пером для электронных бумажных приложений. Эта технология позволяет создать абсолютную систему координат для оцифровки рукописного текста и изображений путем печати на бумаге специального точечного шаблона. [13] Таким образом, когда кто-то пишет на цифровой бумаге, ручка записывает координаты, которые затем передаются на компьютер или смартфон [14][15].

Система Anoto хорошо развита и коммерциализирована. Описанная информация об их технологии извлечена из общедоступной информации на их веб-сайте и о патентах. У них также есть комплект для разработки программного обеспечения, позволяющий сторонним разработчикам использовать их перо. Однако это доступ к информации на высоком уровне. В этой части диссертации будет продемонстрирован собственный метод декодирования точечного шаблона для получения координат, а затем изложено исследование возможности использования этой информации для получения точной информации о местоположении.

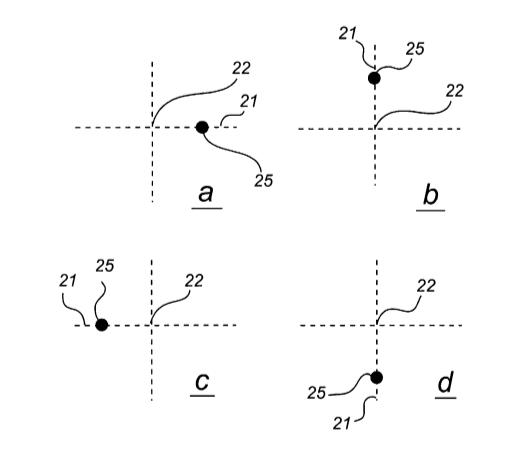


**Рисунок 4-1 Иллюстрация Anoto Dot Pattern (с виртуальными растровыми линиями)**

**4-2 Принципы работы**

Этот раздел суммирует методы, описанные Anoto в их патентах, и предназначен для того, чтобы предоставить читателю достаточно ссылок для понимания кода MATLAB в Приложении B.

Точечный шаблон, имеющий форму сетки с шагом 0,3 мм, состоит из множества маленьких черных точек. Сетка называется растром в Anoto Patents [13,22]. Растровые линии невидимы как для человеческого глаза, так и для оптического считывателя. Вместо того, чтобы располагаться точно на пересечении растровых линий (называемых «номинальной позицией»), каждая маленькая точка слегка смещается вблизи пересечения в одном из четырех направлений: вверх, вниз, влево и вправо. Все четыре вида расположения точек показаны на рис 4-2.



**Рисунок 4-2 Четыре вида расположения точек в шаблоне Anoto Dot Pattern[13]**

Каждый вариант расположения точек кодирует возможную комбинацию битов. Таким образом 4 возможные позиции позволяют закодировать два бита информации в каждом элементе. Последовательность из таких точек в блоке образуют координаты x и y, причем в каждой точке один бит используется для кодирования координаты x, а второй для координаты y. Пара из X‑бита и Y‑бита назначается для каждого типа (направления) смещения, как показано в таблице 4-1.

**Таблица 4-1 Преобразование между направлением смещения и кодовой парой [13]**

|  |  |  |
| --- | --- | --- |
| Направление смещения | x бит | y бит |
|  |  |  |
| Влево | 1 | 0 |
|  |  |  |
| Вправо | 0 | 1 |
|  |  |  |
| Вверх | 0 | 0 |
|  |  |  |
| Вниз | 1 | 1 |
|  |  |  |

Таким образом, координаты x и y могут считываться одновременно и независимо, если имеется фрагмент шаблона, содержащий массив точек больше определенного размера. Блок 8x8 с закодированными координатами, показан на рисунке 4-3.



**Рисунок 4-3 Пример блока 8×8 для шаблона Anoto Dot Pattern [13,23]**

Чтобы идентифицировать положение, необходим, по крайней мере, фрагмент точечного рисунка, содержащий 6 × 6 точек [24]. Но в Anoto Dot Pattern блоки по 8×8 [13], где добавлены по одной точке для поворота и для исправления ошибок. Одним из наиболее важных свойств шаблона является то, что массив, образованный любыми точками 8×8, появляется только один раз по всей поверхности, что позволяет идентифицировать уникальные позиции.

Причина, по которой шаблон обладает вышеуказанным свойством, состоит в том, что код, в который он закодирован, разработан с использованием специальной последовательности De Bruijin [25, 42, 47]. Эта последовательность чисел является циклической, и длина последовательности специально предназначена для того, чтобы любая частичная последовательность определенной длины, взятая из основной последовательности, встречалась только один раз. В патентах Anoto [13] специально разработанная квази-последовательность De Bruijin [25] называется main number sequence (MNS) и имеет в общей сложности 63 числа и представлена ниже:

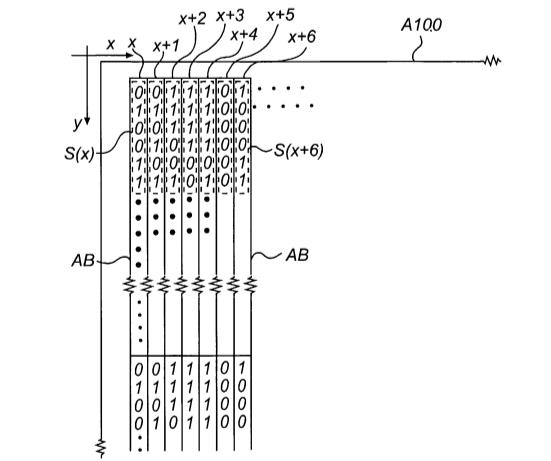
0, 0, 0, 0, 0, **0, 1, 0, 0, 1, 1**, 1, 1, 1, 0, 1, 0, 0, 1, 0, 0, 0, 0, 1, 1, 1, 0, 1, 1, 1, 0, 0, 1, 0, 1, 0,

1, 0, 0, 0, 1, 0, 1, 1, 0, 1, 1, 0, 0, 1, 1, 0, 1, 0, 1, 1, 1, 1, 0, 0, 0, 1, 1.

Любая частичная последовательность длиной 8 имеет значение позиции от 0 до 62. Например, последовательность «0, 0, 0, 0, 0, 0, 1, 0» имеет значение позиции «0», а «0, 0, 0, 0, 0, 1, 0, 0, 1», сдвинутая вправо, имеет значение позиции «1».

Последовательность главных чисел сдвигается вверх и вниз в столбцах, а влево и вправо в строках на разные номера и повторяется, когда она подходит к концу. Следовательно, соседние два столбца или две строки имеют постоянную разность чисел. Например, что касается направления x, если столбец k содержит последовательность основных чисел, сдвинутую на число строк l, а столбец k + 1 содержит последовательность основных чисел, сдвинутую на количество строк m, разность этих двух столбцов будет равна (lm) по модулю 63. Разностные числа между столбцами и строками образуют другую важную последовательность, называемую первичной разностной последовательностью (PDS). Как можно легко заметить, хотя каждый столбец и каждая строка начинаются с идентичного MNS, смещенного на разные номера, PDS не изменяется от строки к строке для направления x и от столбца к столбцу для направления y.

Массив 8 × 8 этого типа точечного шаблона имеет восемь столбцов и восемь строк, которые могут быть закодированы в восемь вертикальных частичных последовательностей, и восемь горизонтальных частичных последовательностей с каждой частичной последовательностью имеет длину восемь. Каждая частичная последовательность затем имеет соответствующий номер позиции для направления x и направления y отдельно. Кроме того, два частичных PDS длиной 7 для направлений x и y также могут быть получены отдельно.



**Figure 4-4 How the vertical partial sequences is coded in x direction[13]**

Положение частичного PDS в целом PDS является одним из ключевых элементов информации, который сообщает нам о координатах. Хотя разностные числа получают с помощью разностей по модулю 63 и, следовательно, все они находятся в диапазоне от 0 до 62, могут использоваться только значения со значениями от 5 до 58, то есть 54 = 2 \* 33 числа. Если из [5, 58] найдено разностное число, значит, произошла ошибка.

На практике первичная разностная последовательность дополнительно преобразуется в так называемые вторичные разностные числовые последовательности (SDS) для целей расчета, обнаружения ошибок и исправления ошибок [17]. Для любой разности число d принадлежит [5, 58], биекция может быть установлена с использованием правил, описанных ниже, где a1, a2 и a4 имеют значения от 0 до 2, а a3 имеет значения от 0 до 1.

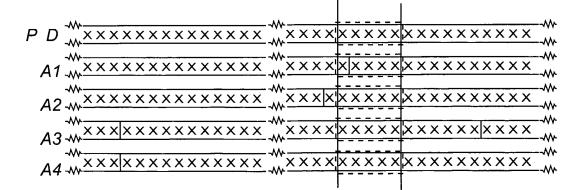
d = 5 + a1 + 3 \* a2 + 3^2 \* a3 + 2 \* 3^2 \* a4;

Например, если d = 35, то

d = 5 + 0 + 3 + 9 + 18 =

= 5 + 0 (a1) + 3 \* 1 (a2) + 3^2 \* 1 (a3) + 2 \* 3^2 \* (a4).

Таким образом, d = 35 в представлении (a1, a2, a3, a4) равно (0, 1, 1, 1). Таким образом, первичная разностная последовательность преобразуется в четыре вторичные разностные последовательности, как показано в таблице 4-5.



**Figure 4-5 Conversion between primary difference number sequence and four secondary difference number sequences[13]**

Если найдены номера позиций частичных вторичных разностных последовательностей во всех вторичных разностных последовательностях, то номер позиции частичного PDS может быть рассчитан с использованием китайской теоремы об остатках [44]. Поэтому четыре последовательности вторичных разностных чисел A1‑A4 вводятся, как показано ниже [13].

A1=[0,0,0,0,0,1,0,0,0,0,2,0,1,0,0,1,0,1,0,0,2,0,0,0,1,1,0,0,0,1,2,0,0,1,0,2,0,0,2,0,2,0,1,1,0,

1,0,1,1,0,2,0,1,2,0,1,0,1,2,0,2,1,0,0,1,1,1,0,1,1,1,1,0,2,1,0,1,0,2,1,1,0,0,1,2,1,0,1,1,2,0,0,0,

2,1,0,2,0,2,1,1,1,0,0,2,1,2,0,1,1,1,2,0,2,0,0,1,1,2,1,0,0,0,2,2,0,1,0,2,2,0,0,1,2,2,0,2,02,2,1,

0,1,2,1,2,1,0,2,1,2,1,1,0,2,2,1,2,1,2,0,2,2,0,2,2,2,0,1,1,2,2,1,1,0,1,2,2,2,2,1,2,0,0,2,2,1,1,2,

1,2,2,1,0,2,2,2,2,2,0,2,1,2,2,2,1,1,1,2,1,1,2,0,1,2,2,1,2,2,0,1,2,1,1,1,1,2,2,2,0,0,2,1,1,2,2]

A2= [0,0,0,0,0,1,0,0,0,0,2,0,1,0,0,1,0,1,0,1,1,0,0,0,1,1,1,1,0,0,1,1,0,1,0,0,2,0,0,0,1,2,0,1,0,1,2,

1,0,0,0,2,1,1,1,0,1,1,1,0,2,1,0,0,1,2,1,2,1,0,1,0,2,0,1,1,0,2,0,0,1,0,2,1,2,0,0,0,2,2,0,0,1,1,2,

0,2,0,0,2,2,2,1,0,1,2,2,0,0,2,1,2,2,1,1,1,1,1,2,0,0,1,2,2,1,2,0,1,1,1,2,1,1,2,0,1,2,1,1,1,2,2,0,

2,2,0,1,1,2,2,2,2,1,2,1,2,2,0,1,2,2,2,0,2,0,2,1,1,2,2,1,0,2,2,0,2,1,0,2,1,1,0,2,2,2,2,0,1,0,2,2,

1,2,2,2,1,1,2,1,2,0,2,2,2]

A3 = [0,0,0,0,0,1,0,0,1,1,0,0,0,1,1,1,1,0,0,1,0,1,0,1,1,0,1,1,1,0,1]

A4=[0,0,0,0,0,1,0,2,0,0,0,0,2,0,0,2,0,1,0,0,0,1,1,2,0,0,0,1,2,0,0,2,1,0,0,0,2,1,1,2,0,1,0,1,0,

0,1,2,1,0,0,1,0,0,2,2,0,0,0,2,2,1,0,2,0,1,1,0,0,1,1,1,0,1,0,1,1,0,1,2,0,1,1,1,1,0,0,2,0,2,0,1,2,

0,2,2,0,1,0,2,1,0,1,2,1,1,0,1,1,1,2,2,0,0,1,0,1,2,2,2,0,0,2,2,2,0,1,2,1,2,0,2,0,0,1,2,2,0,1,1,2,

1,0,2,1,1,0,2,0,2,1,2,0,0,1,1,0,2,1,2,1,0,1,0,2,2,0,2,1,0,2,2,1,1,1,2,0,2,1,1,1,0,2,2,2,2,0,2,0,

2,2,1,2,1,1,1,1,2,1,2,1,2,2,2,1,0,0,2,1,2,2,1,0,1,1,2,2,1,1,2,1,2,2,2,2,1,2,0,1,2,2,1,2,2,0,2,2,

2,1,1]

Они имеют длину 236, 233, 31 и 241 соответственно. Длины выбираются относительно взаимно простыми, поэтому наименьшее общее кратное из четырех последовательностей будет произведением их длин. Тогда соответствующие места p1, p2, p3 и p4 частичной последовательности длины 5 в этих четырех вторичных разностных последовательностях могут быть определены с использованием того же метода определения места P частичной последовательности в первичной разностной последовательности, который был указан выше. И они имеют отношение, перечисленное ниже:

P ≡ p1 (mod 236)

P ≡ p2 (mod 233)

P ≡ p3 (mod 31)

P ≡ p4 (mod 241)

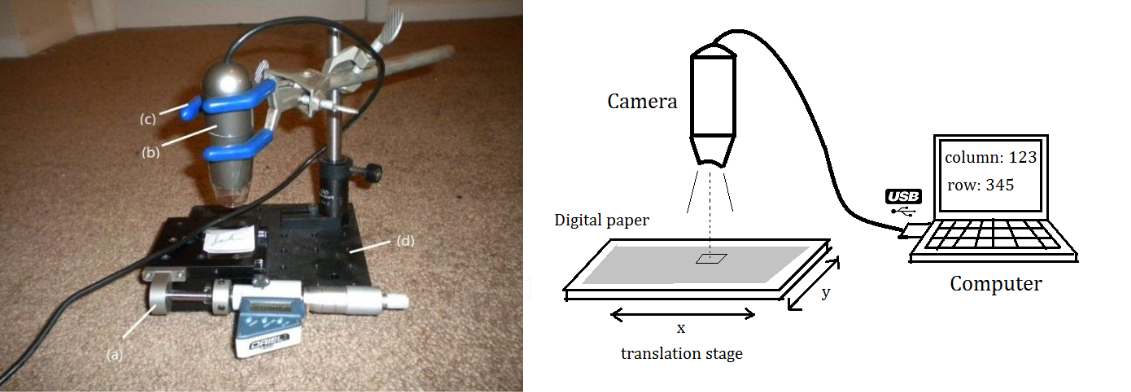
Где 236, 233, 31, 241 - длины вторичных разностных последовательностей. В результате P можно рассчитать с помощью китайской теоремы об остатках [26]. Фактически, нет необходимости вычислять номер позиции P частичного PDS, поскольку мы знаем, что четыре номера позиций p1, p2, p3, p4 частичного SDS определяют P, а затем определяют координаты x или y. Существует также биекция между (p1x, p2x, p3x, p4x) и x, а также (p1y, p2y, p3y, p4y) и y, где x, y - координаты в направлениях x и y. Здесь x обозначает x-й столбец, y обозначает y-й ряд, который дает нам информацию напрямую. Это именно то, что мы используем в этом тезисе.

Другой фактор, который важен в позиционировании Anoto, называется «Section» [13]. Поскольку существует 63 различных номера места для первичной разностной последовательности, существует 63 возможных значения, которые могут начинать самую первую координату x и первую координату y соответственно. Это в сумме 63 \* 63 = 3969 различных «версий» точечного рисунка [13]. И какие два числа начинаются с первого столбца и первой строки, называются номерами секций для направления x и номерами секций для направления y соответственно. Это полезно, когда вы управляете множеством частей поверхности с огромным количеством областей в сумме. Поскольку поверхность, используемая в этом тезисе, намного меньше, нет проблем с управлением различными «сечениями» поверхности. Поэтому нет необходимости рассчитывать номер раздела. На самом деле, они представлены в качестве известного параметра в экспериментах, изложенных в главе 5.

**CHAPTER 5 DESIGN OF AN OPTICAL POSITIONING**

**SYSTEM**

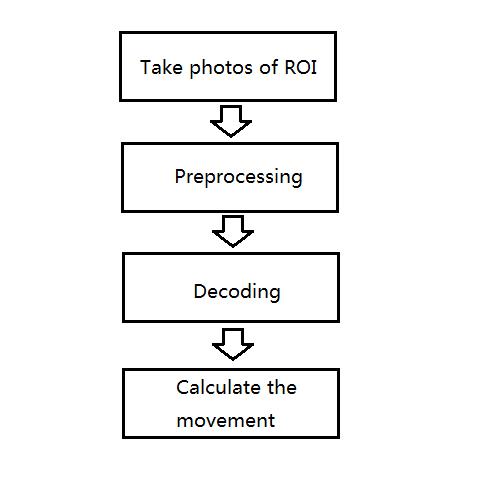
The design of the optical positioning system consists of the design of a hardware system and a software system. The hardware system contains four devices as shown in Figure 5-1: (a) a translation stage with a micrometer; (b) a Dino Microtouch Camera with an USB connector[21]; (c) a camera bracer; (d) a pedestal.



**Figure 5-1 The hardware of the optical positioning system**

The software system is a program developed using Matlab scripts to process images and make calculations. The entire process of the experiment is schematically shown in the flow chart in Figure 5-2.

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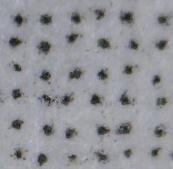


**Figure 5-2 Flowchart of the experiment**

The Anoto Dot Pattern that we use in this thesis comes from a test paper of their products. We used a Canon Laser jet printer with a high resolution of 1200 dpi to print the dot pattern on to several pieces ordinary paper.

**5-1 Image Preparation**

An enlarged partial image of the paper with printed dot patterns is shown in Figure 5-3.



**Figure 5-3 Partial image showing the printed 6×6 array at 200X magnification**

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The number of dots contained in the array in Figure 5-2 is the minimum for enough information to identify a position when it is being decoded. But a typical image taken by the camera could have much more dots as shown in Figure 5-4. Those black curves are written pen strokes. It can be seen that grid spacing of the dot pattern is a little smaller than the width of the pen strokes and the raster lines are not actually printed on the paper.



**Figure 5-4 A typical image taken by the camera at 60X magnification**

**5-2 Preprocessing**

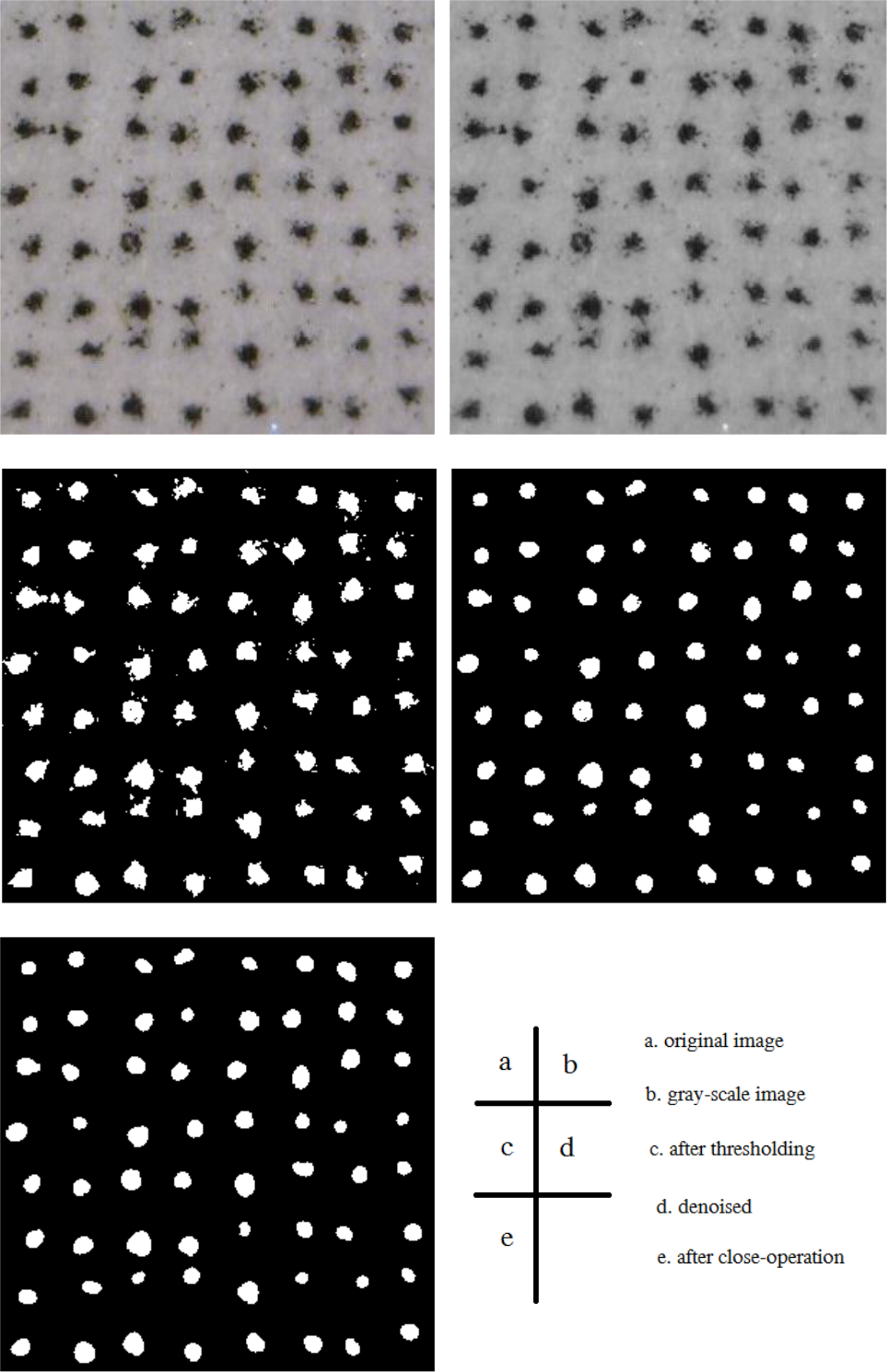
After the image is taken, the next step is to preprocess it to prepare it for decoding process. The preprocessing section consists of conversion into gray-scale image, thresholding, removing noise and converting to a black and white image. These processes can be done manually to get the best image quality for decoding with a relatively large time cost and human-attention, or automatically using a series of batch scripts with a much smaller time cost which can be applied to many images at a time. Which method to use is mainly

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determined by the printing quality of the original image. One set of the Figures showing

these four processes is shown in Figure 5-5.

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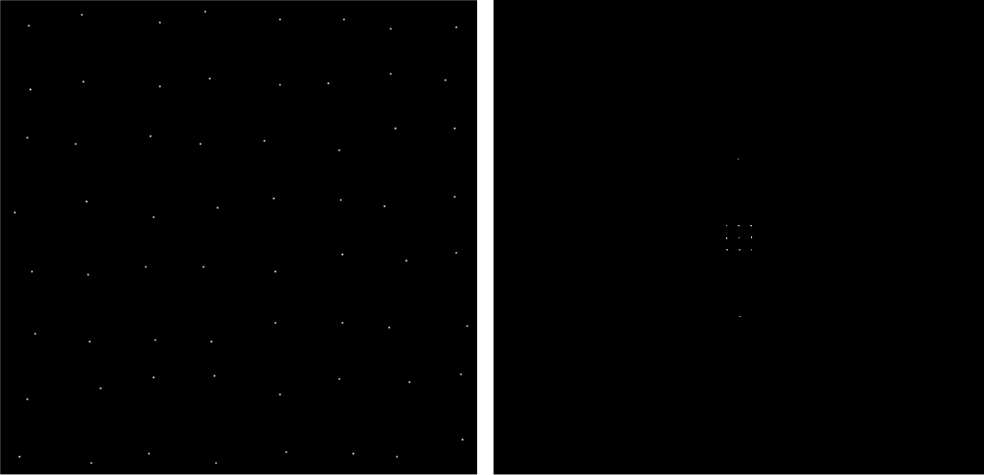


**Figure 5-5 The preprocess steps**

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**5-3 Decoding**

The image shown as Figure 5-6 (e) is ready for decoding. Firstly, Each blob in the preprocessed image is identified using Matlab scripts[27,28]. Then the blobs will be replaced with their own centroids, or the center of gravity. The coordinates of these centroids are obtained in pixels. Using these coordinates, a new image containing dots of only one pixel is obtained as shown in Figure 5-6 (a).



**(a)** **(b)**

**Figure 5-6 An example image of one-pixel dots and its FFT**

Figure 5-6 (b) is a binary image of the Fast Fourier Transform of Figure 5-6 (a). It is thresholded to filter out unnecessary information but the small grid which is made up of nine dots in the middle. The relative position of the nine dots tells us if a rotation correction is needed for the original image[29]. This step is essential to make sure the decoding process goes on smoothly, reducing the chance of occurrences of errors. If the original image is tilted,

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the 9-dot grid will look like a parallelogram other than a rectangular. The value of the angle used to correct the rotation can be calculated by using the slopes of the sides of the parallelogram. Then the original image could be rotated back to balance the tilt.

Next, the centroids of the blobs in the image are divided into columns and rows. If there are M×N blobs in the image, the coordinates of the centroids are recorded into two M×N matrices, one for the x-coordinates and the other for the y-coordinates.

As for the x-coordinates, from the relative positions inside a same column, the dots could be divided into 3 kinds: left (L), medium (M), and right (R), depending on which direction the dot is offset in x dimension. If the number of dots is relatively large, there is a big chance that all three kinds of the dots can be found in a single column. But if the number of dots is relatively small, for example only 6~10 dots per column, there is a good chance that only two kinds of the dots (L and M, or M and R) can be found in a column. Sometimes extreme situation happens that only one kind of the dots is found in a single column. Fortunately, the three situations can be easily identified by comparing the width of each column to the mean value of themselves.

In our embodiment, if the width of the column is larger than 2/3 of the mean value, we know the column contains all three kinds of dots. If the width is smaller than 1/3 of the mean value, then the column has probably only one kind of dots. And if the width of the column is between 1/3 and 2/3 of the mean value, then the column should have 2 kinds of dots.

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It is easy to find out in which direction the dots are offset for the first kind of column. Since all we need to do is further divide the dots in the column into three kinds. The smallest 1/3 is the left ones, the medium 1/3 the medium ones, the largest 1/3 the right ones.

Things get more complicate when it comes to the latter two kinds of columns. The solution we give is to take the other coordinates into account based on the property that Anoto Dot Pattern has. We know that there are in total four directions the dots can be displaced in, two in x dimension, the other two in y dimension. And we assign a direction indicator as list in the table below:

**Table 5-1 Conversion between offset direction and offset indicators**

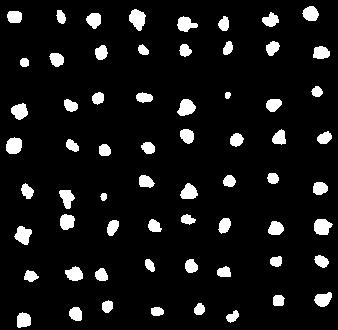
|  |  |  |
| --- | --- | --- |
| Offset direction | Indicator in x | Indicator in y |
|  | dimension | dimension |
|  |  |  |
| Left | -1 | 0 |
|  |  |  |
| Right | 1 | 0 |
|  |  |  |
| Up | 0 | 1 |
|  |  |  |
| Down | 0 | -1 |
|  |  |  |

As can be seen in Table 5-1, one of the two indicators must be 0, but they cannot be 0 simultaneously. This property is useful that once we cannot determine the offset direction of the dot in one dimension, we can search in another dimension. Usually the problem will be solved.

Once the offset direction of each dot is determined, it is important to make sure it’s correct. Since the quality of the printing or image can be low and the image can be distorted. The dots obtained through above procedures might not be located exactly where it should be.

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After the error-correction section, we can decode the dot patterns into codes both in x and y direction as shown in Table 4-1. And then we can utilize the x codes and y codes, following the directions stated in Chapter 4 to determine the coordinates of columns and rows. An example of the process is given below. A preprocessed binary image is shown in Figure 5-7.



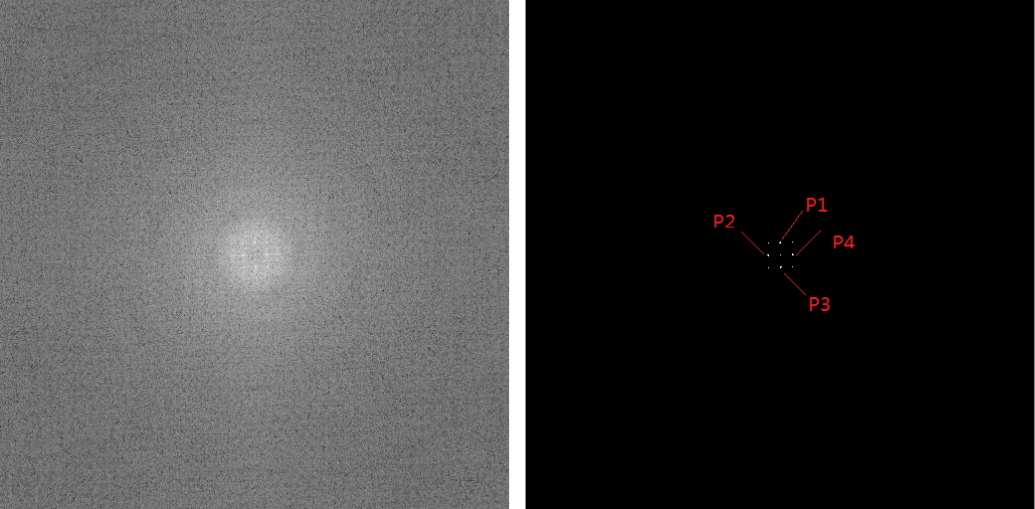
**Figure 5-7 A preprocessed image ready for decoding (60X)**

The first thing we need to do is to check if the dot pattern contained in this image is inclined. If it is not, then the virtual raster lines should be parallel to the coordinate axis. And this is what we desire. Otherwise, we must find out how much it is inclined and rotate the image to the opposite direction to cancel the effect. Of course, sometimes it is not easy to judge whether the image is inclined and needs rotation-correction by human eye, since the incline angle maybe relatively small. But we can make use of the Fourier Transform, usually

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the Fast Fourier Transform of the image and solve this problem in Frequency Domain. The FFT of Figure 5-7 is shown in Figure 5-8 (a) below.

Before the use is made of it, a threshold is made to filter out unnecessary information. This process needs to be done manually to make sure all the information, except the nine dots in the middle of the image, is filtered. These nine dots form a small parallelogram. The angle made by the sides of the parallelogram and the horizontal and vertical directions tells if the virtual raster lines are parallel to the coordinate axis.



**Figure 5-8 Using FFT of the one-pixel dots image to correct the incline**

Since the 9-dot parallelogram is made up of 4 smaller parallelograms, we can look into the smaller parallelograms for simplicity. According to the geometry relations of these dots, the calculations are made as follows:

1. Locate the center dot, and its coordinate is obtained as Pc (257.00, 257.00).

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1. Find the four nearest dots to the center dot in all the quadrants. It is done by

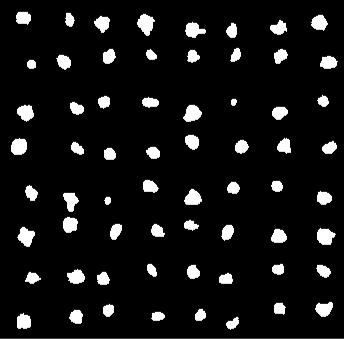
searching the dot that has the smallest Euclidean distance to the center dot in all the four quadrants. And they are P1(257.33, 269.33), P2(244.67, 257.33), P3(256.67, 244.67) and P4(269.33, 256.67).

1. Determine the four slopes of the straight lines P1Pc, P2Pc, P3Pc and P4Pc. The result is shown in Table 4-2

**Table 5-2 Calculation of the incline angle**

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | *P*1*P*c | *P*2*P*c | *P*3*P*c | *P*4*P*c |
|  |  |  |  |  |
| Slope | 0.9996 | 0.0270 | 0.9996 | 0.0270 |
|  |  |  |  |  |
| Angle | 88.45º | 1.55º | 88.45º | 1.55º |
|  |  |  |  |  |

Analyze the angles in Table 5-2, and it is found that the dot pattern is 1.55 degree inclined. Rotate the original image -1.55 degree to for rotation-correction. The corrected image is shown as Figure 5-9.



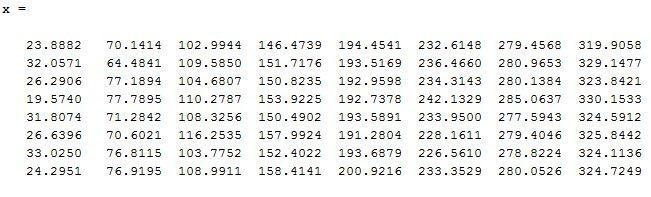
**Figure 5-9 The incline-corrected image**

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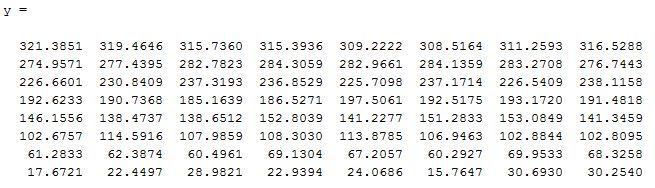
Then the x, y coordinates of the centroids are obtained and shown in the Table 5-3:

**Table 5-3 x, y coordinates (in pixels) of the centroids (a) the x coordinates (b) the y coordinates**

(a) the x coordinates



(b) the y coordinates



Use the first column as an example. The minimum value of x coordinates is 19.5740, and the maximum value of x coordinates is 33.0250. Thus the difference of these two is ∆1 = 33.0250-19.5740 = 13.4510. We can calculate the difference of maximum and minimum for every column. The result is shown in Table 5-4.

**Table 5-4 Differences of maximum and minimum of each column**

|  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Column | ∆1 | ∆2 | ∆3 | ∆4 | ∆5 | ∆6 | ∆7 | ∆8 |
|  |  |  |  |  |  |  |  |  |
| Difference | 13.4510 | 13.3054 | 13.2591 | 11.9402 | 9.6412 | 15.5719 | 7.4694 | 10.2475 |
|  |  |  |  |  |  |  |  |  |

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Therefore, the maximum difference is 15.5719.

1/3 of the maximum difference: 5.1906

2/3 of the maximum difference: 10.3813

The columns that have a difference larger than 10.3813 (Column Class A): Column 1, Column 2, Column 3, Column 4 and Column 6

The columns that have a difference between 5.1906 and 10.3813 (Column Class B):

Column 5, Column 7 and Column8.

As for the Columns in Class A, there are three kinds of dots (considering only in x direction, so the dots that offset upwards and downwards count as one ‘medium’ kind). Again, take the first Column as an example, divide the spacing between the dot with the minimum x coordinate and the dot with the maximum x coordinate into three intervals of equal length in x direction: [19.5740, 24.0577), [24.0577, 28.5414) and [ 28.5414, 33.0250] . Assign offset indicator ‘-1’ to the dots whose x coordinate falls in the first interval (left ones), ‘0’ to the dots whose x coordinate falls in the second interval (medium ones), and ‘1’ to the dots whose x coordinate falls in the last interval.

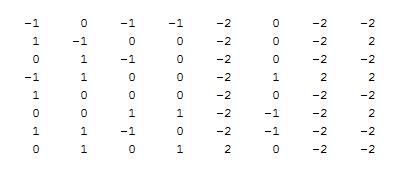
As for the Columns in Class B, there are only two possible combinations of offset directions for the dots--the left ones and the medium ones, or the medium ones and the right ones. In this situation, we can first divide the spacing between the dot with the minimum x coordinate and the dot with the maximum x coordinate into two intervals of equal length. Take the fifth column of the array for example, the intervals are [191.2804, 196.1010) and

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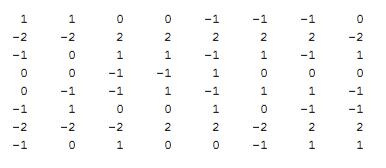
[196.1010, 200.9216]. Assign offset indicator ‘-2’ to the dots whose x coordinate falls in the first interval and offset indicator ‘2’ to the dots whose x coordinate falls in the second interval. And the offset direction indicators are then obtained and shown in Table 5-5.

**Table 5-5 Unmatched Offset direction indicators in x, y directions (a) in the x direction and (b) in the y direction**

(a) in the x direction



(b) in the y direction



The offset indicator ‘-2’and ‘2’ are only temporary. They do not tell the actual offset direction of the dots, but just indicate the position relation inside a column. In order to find out the actual offset direction, we need to account for the offset indicator in y direction, which has been shown in Table 5- 5 (b). It can be easily found that the common feature of the columns with ‘2’ and ‘-2’ is that there is no ‘0’ in that column.

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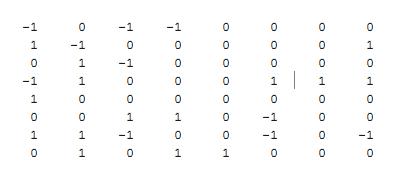
Now focus on the offset indicator of column 2 in y direction. They are -1, 2, -1, 1, -1, 1, 2, 0. Together with those in x direction, they are made into pairs as (-2,-1), (-2,2), (-2,-1), (-2,1), (-2, -1), (-2,1), (-2, 2), (2,0). We know that the offset indicators in x and y direction should not be 0 simultaneously, but at least one of them must be 0. Thus, the factor pairs are improved to (0,-1), (-2, 2), (0,-1), (0,1), (0,-1), (0,1), (-2, 2), (2, 0). Then we get an inference that in the second column, the offset indicator ‘-2’ is actually ‘0’, and therefore the offset indicator ‘2’ should be ‘1’.

Besides, notice that the last pair is (2,0), Because ‘2’ indicates that the dot is in the relatively right half of the dots distribution and its counterpart in y direction is already ‘0’, it must be ‘1’. This is consistent with the above inference. Finally, the offset indicator for the fifth column in x direction should be: 0, 0, 0, 0, 0, 0, 0, 1. Similar process are done for the other two columns. The updated results of all the columns are shown in Table 5-6 (a). The process for the y direction is similar and the results are shown in Table 5- 6(b). The whole process is like a Sudoku problem but is much easier.

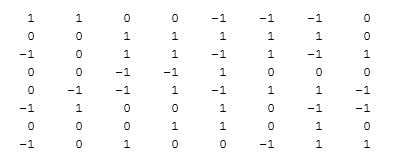
52

**Table 5-6 Offset direction indicators after first correction (a) in the x direction and (b) in the y direction**

(a) in the x direction



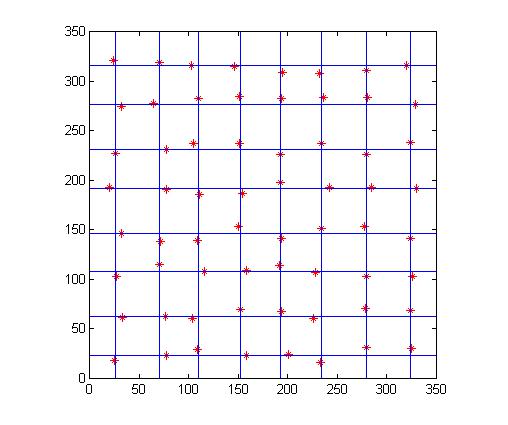
(b) in y direction



However, the offset indicators are not finally verified. As can be seen in Table 5-6(a) and (b), the indicator pairs at {1,1},{3,3} and {1,8} are (-1,1), (-1,1) and (0, 0) respectively ({*L*,*M*} means the *Lth* row and the *Mth* column). These indicator pairs cannot create correct x-code and y-code. The solution in this thesis is to reconstruct the virtual raster lines [23].

Once the offset indicators are obtained for both x and y directions, it becomes easy to establish the virtual raster lines. The dot pattern with raster lines are shown in Figure 5-10.

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**Figure 5-10 The dot pattern with reconstructed visible raster lines**

Since the raster lines are obtained through the positions of the dots, which may have been distorted during processing, the raster lines may not equally spaced. However, with the aid of the raster lines, the offset directions of each dot become even clear. And this is a complementary method to make sure offset indicator is correctly obtained. Take the indicator pair at {1,1} for example.

The distance between the dot and the raster line in the x direction:

Dx = 23.8882 - 25.7418 = -1.8536;

The distance between the dot and the raster line in the y direction:

Dy = 321.3851 – 315.8861 = 5.4990;

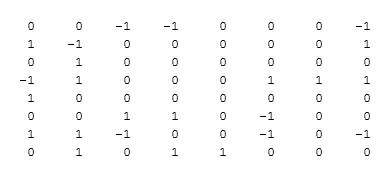
54

And for the absolute value, abs(Dy) >abs(Dx).

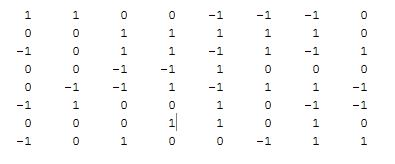
Thus the offset direction is determined to be in the y direction. The indicator is assigned ‘1’ with the sign determined by the sign of Dy. Therefore, the indicator pairs at {1,1} has been corrected from (-1,1) to (0,1).

**Table 5-7 Final offset direction indicators (a) in the x direction and (b) in the y direction**

**(a) in the x direction**

****

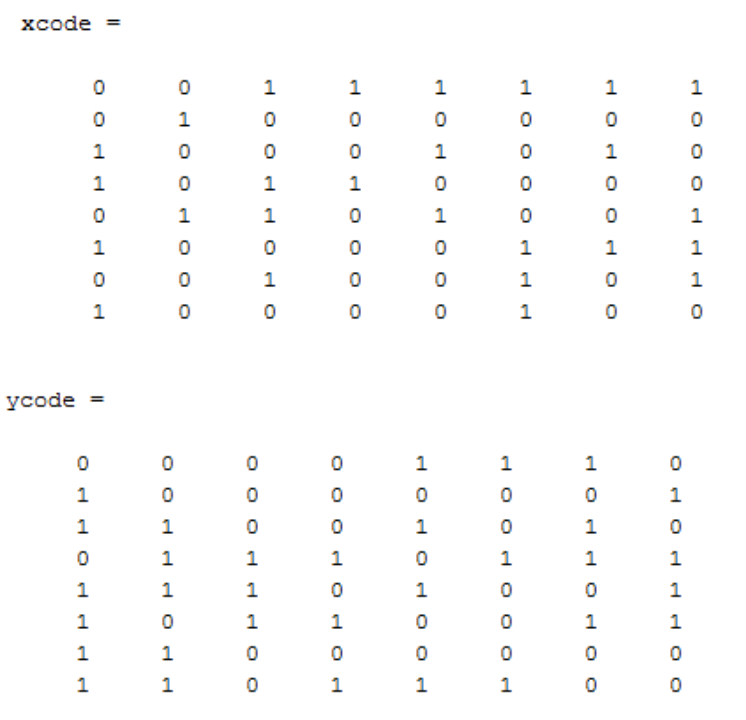
**(b) in the y direction**

****

The x, y codes then are obtained by converting the indicator pairs through the bijection shown in Table 4-1. The results are shown in Table 5-9:

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**Table 5-8 Corresponding x, y codes**

****

Then we can decode in two dimensions respectively.

For the x direction, from Table 5-5(a), six vertical partial sequences are obtained as follows: 00110101, 01001000, 10011010, 10010000, 10101000, 10000111, 10100100 and 10001110. The corresponding places of these partial sequences in the main number sequences are

47, 14, 46, 15, 32, 18, 13, 57.

The primary difference sequence is further obtained as

30, 32, 32, 17, 49, 58, 44.

The secondary difference sequences are obtained using Table 5-9:

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**Table 5-9 An example of converting primary difference number sequence into secondary difference number sequences**

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
| d | 30 | 32 | 32 | 17 | 49 | 58 | 44 |
|  |  |  |  |  |  |  |  |
| a1 | 1 | 0 | 0 | 0 | 2 | 2 | 0 |
|  |  |  |  |  |  |  |  |
| a2 | 2 | 0 | 0 | 1 | 2 | 2 | 1 |
|  |  |  |  |  |  |  |  |
| a3 | 0 | 1 | 1 | 1 | 0 | 1 | 0 |
|  |  |  |  |  |  |  |  |
| a4 | 1 | 1 | 1 | 0 | 2 | 2 | 2 |
|  |  |  |  |  |  |  |  |

The four partial sequences of length 5 are ‘10002’ for A1, ‘20012’ for A2, ‘01110 ’for A3, ‘11102’ for A4. The corresponding place numbers are listed below:

p1 = 119

p2 = 147

p3 = 25

p4 = 178

As long as the section number in x direction is known, or the four such numbers for the first 8×8 array of the dot pattern are obtained, we can assign a column coordinate.

For the first 8×8 array, p1 to p4 are obtained as

p1= 32

p2= 57

p3= 12

p4= 96

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Since the p1 to p4 get larger by one consecutively when the region of interest is moved one column right, an infinite table can be established like below:

**Table 5-10 The relation between column number and the four place numbers**

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
|  | Column 1 | Column 2 | Column 3 | … | Column x | … |
|  |  |  |  |  |  |  |
| p1 | 32 | 33 | 34 | … | 119 | … |
|  |  |  |  |  |  |  |
| p2 | 57 | 58 | 59 | … | 147 | … |
|  |  |  |  |  |  |  |
| p3 | 12 | 13 | 14 | … | 25 | … |
|  |  |  |  |  |  |  |
| p4 | 96 | 97 | 98 | … | 178 | … |
|  |  |  |  |  |  |  |

The ranges of p1, p2, p3 and p4 are 0 to 235, 0 to 232, 0 to 30 and 0 to 240 respectively. Identical combinations of p1, p2, p3 and p4 occur every l1×l2×l3×l4 = 236×

233×31×241 = 410815348 columns. That is 410815348×0.3 mm = 123244604.4 mm =123.2 km, which is much larger than the dimension of test papers used in this thesis.

By looking up the Table 5-10, which is established using Matlab, the column corresponding to (119, 147, 25, 178) is found to be column 324, which means that the first column of the 8×8 array is column 324 of the whole surface. So the last column of the 8×8 array is column 331.

A similar process is made for the y direction. Instead of using vertical partial sequences in Table 5-5, horizontal partial sequences are used. They are 00001110, 1000001, 11001010, 01110111, 11101001, 10110011, 11000000 and 11011100. The place numbers in

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secondary difference sequences are (50, 87, 11, 207). And the place numbers for the first row of the dot pattern are (224, 19, 4, 155), then a similar table to Table 5-10 is obtained for the y direction, shown as Table 5-11.

**Table 5-11 The relation between row number and the four place numbers**

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | p1 | p2 | p3 | p4 |
|  |  |  |  |  |
| Row 1 | 224 | 19 | 4 | 155 |
|  |  |  |  |  |
| Row 2 | 225 | 20 | 5 | 156 |
|  |  |  |  |  |
| Row 3 | 226 | 21 | 6 | 157 |
|  |  |  |  |  |
| … | … | … | … | … |
|  |  |  |  |  |
| Row y | 50 | 87 | 11 | 207 |
|  |  |  |  |  |
| … | … | … | … | … |
|  |  |  |  |  |

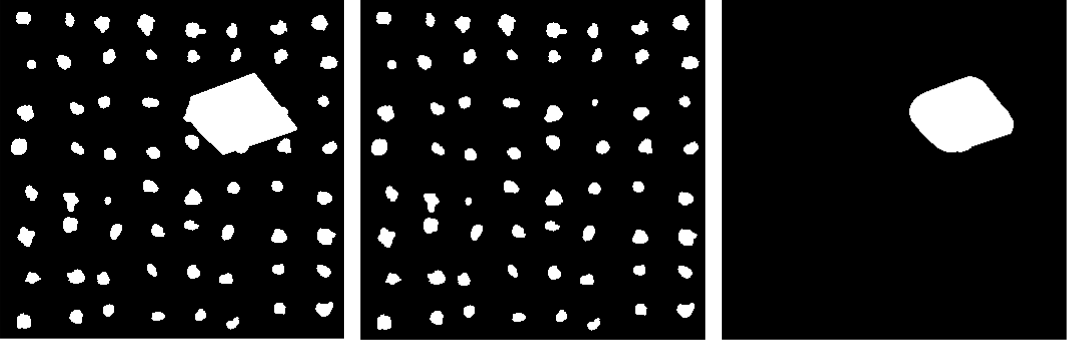
By looking up the Table 5-11, the row coordinate corresponding to (50, 87, 11, 207) is Row 535. Thus the rows that are included in the 8×8 array of interest are Row 535 to Row 542. The decoding is complete and successful.

**5-4 Calculate the movement distance**

With any 6×6 array or 8×8 array of the dot pattern being successfully decoded, we can quickly get the accurate position information of the object that we’re interested in on the digitized surface just by taking pictures of the region of interest [30,31]. If we record the position information of an object at a first position and that of the object at a second position, then the distance that the object translated from the first position to the second one.

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As an example we can consider the case of when the position information of the background dot array is known. This is shown in Figure 5-11. This can be a little impractical since it assumes that the image is taken before and after the object is on the page, but it shows in principle how the method can be used. However, in the case of a pen where the dots are reflective in the infrared, and the ink from the pen is transparent to the infrared, this method should work. In both cases- as an extension of this- is if the field of view is wide enough and as long as one 8×8 can be used to obtain the absolute coordinate position, that information can be used to extrapolate information about the occluded dots. This information can be used to subtract dots from the image.



(a) (b) (c)

**Figure 5-11 (a) the preprocessed image of the region of interest, with the object (the circle) at its starting position (b) the known dot pattern of the background, which will provide the position of the region (c) extracted from (a), which is a binary image of the object with the position relation unchanged from (a). 60× magnification.**

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Since we already know the position of the 8×8 array in the whole dot pattern, what we need to do is to locate the object in the array. This can be simplified to locate the centroid of the object in the array. This is done as below.

1. Get the coordinate in pixels of the centroid of the object in the image. In this example

it’s *P*o(238.7545, 224.2730).

1. Compare the coordinate of the dot *P*o with the raster lines. And it can be found that the dot is located between the 6th column and 7th column, 3rd row and 4th row.
2. Add a decimal part to the dot’s location to indicate its precise coordinate in columns

and rows.

The coordinate of the 6th column is x = 234.1396;

The coordinate of the 7th column is x = 279.4906;

The coordinate of the 3rd row is y = 230.8409.

The coordinate of the 4th row is y = 192.1063.

Object\_Column = (238.7545 – 234.1396)/ (279.4906-238.7545) +6 = 6.1018;

Object\_Row = (224.2730-230.8469)/(192.1063-230.8469) +3 = 3.1696.

1. The column and row coordinates of the centroid in the dot pattern are obtained as: C = 6.1018 + 324 -1 =329.1018;

R = 3.1696 +535 -1 = 537.1696.

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The same process can be done when the object has moved to its finishing position. And we can then get another coordinate of its centroid, the coordinate at the finishing position. If the value is (923.2411, 345.5511), then using basic knowledge of vector and Euclidean geometry, we can calculate the distance the object moved as:

√

This is based on the spacing of the grid in x direction and that of y direction are equal, which of course is not really necessary. Then as we know beforehand, the spacing of the grid in both directions is 0.3 mm, thus Distance 624.27×0.3 mm = 187.3 mm.

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**CHAPTER 6 CONCLUSION AND FUTURE WORK**

**6-1 Summary of the work**

The purpose of this thesis is to design a platform using an inexpensive camera for optical position measurements. In order to realize the positioning function, several common optical encoders were considered, and a method for reading a micrometer was implemented. The Anoto Dot Pattern was investigated because of its advantages, such as those listed below:

1. Two-dimensional measurement- Anoto Dot Pattern is actually a special 2-D

“barcode” that can code a large area and make optical measurements on a plane surface possible.

1. Ease of sample analysis. A laser printer with a resolution higher than 600 dpi is sufficient for the job. The pattern can be printed to any surfaces that are printable.
2. Inexpensive instrument. Images taken by an inexpensive camera are sufficient for processing at useful resolution.

The printed dots are irregular in shape, which leads to errors in centroid position in pixels of the dots. However, each raster line has several dots, so error in raster lines is potentially less than that of an individual dot. The spacing of raster lines is also known, which can be used to potentially improve the accuracy. For a lower magnification image, there are more dots in the field of view that give a higher accuracy, but they also bring a larger number of microns/pixel (about 6.7 µm/pixel at 60X magnification). For a higher

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magnification image, since there are fewer dots in the field of view, the ability to do statistics determine absolute accuracy is lost, but relative accuracy within an 8×8 dot array can be high with a smaller number of microns/pixel( about 2.1 µm/pixel at 200X magnification). One possible significant improvement to obtain higher accuracy would be printing of nice circular uniform sized dots. But this also requires a better device with higher printer quality.

**6-2 Future Directions**

The measurement platform built in this thesis can register the positions of a region of interest accurately (to at least one hundredth millimeter) with the help of Anoto Dot Pattern. By comparison of the position information of a starting position and that of a finishing position, a displacement can also be measured accurately. Since the measurement is non-contact and can detect tiny displacements, it is very appropriate to apply this optical measurement to situations where the sample is small and a non-contact measurement is required.

Future work will implement the system and calibrate it against a standard to obtain a better appreciation of the limit of accuracy that can be obtained. Once the dot pattern is decoded, and the raster patterns are obtained, one has both the absolute position reference and grid, which is a position that is relative to the coordinates system of the camera. While the grid is not equally spaced, which may be due to problems induced during the printing process, or distortions in the image due to the acquisition process, one has considerable information that potentially can be extracted to determine the relative position. Since

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typically the field of view contains many dots, (and one knows the intended relative positions and sizes) one can also obtain statistics about the mean spacing and size of the dots which also provide dimensional reference. Presently, with the above method, the variation observed in the spacing of the raster lines is approximately 20 µm. Thus presently, one can obtain the relative position of the paper with the camera to about 20 µm. Taking the above statistical processes into consideration, or by having carefully printed high fidelity patterns prepared, one can reasonably expect micron or even sub-micron positional accuracy.

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**APPPENDIX**

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**Appendix A Matlab scripts used in Chapter 3**

This part contains matlab scripts used in Chapter 3.

Document 1

* File name: BATPROCESS.m
* BATPROCESS batch processes the binary images stored in a folder, dir\_name,
* plotting intensity histogram to find the locations of the graduations on a sleeve.
* Then save the data into an excel file for establishing Table 3-3.
* Input: dir\_name – location of the source images.
* dir\_name2 – location of the output images and excel file.
* Output: xSpacing.xlsx – file contain the spacing information of each

% reference image.

% name.jpg – intensity histogram of each reference image.

clc;clear all;

dir\_name = uigetdir('E:\EsoneruzA\Desktop\','Choose Source Folder'); if isequal(dir\_name,0)

disp('invalid')

else

tarFiles = dir(dir\_name);

end

dir\_name2 = uigetdir('E:\EsoneruzA\Desktop\','Choose Destination Folder');

filename = 'xSpacing.xlsx';

ffn = fullfile(dir\_name2, filename);

px = zeros(numel(tarFiles)-2,20);

[rpx, cpx] = size(px);

xSpacing = zeros(rpx,cpx-1);

for k = 3:numel(tarFiles)

BW = imread(fullfile(dir\_name,tarFiles(k).name)); [r,c] = size(BW);

* The name of the image file is specially named by its reading on the LCD screen.
* This is very convenient when labeling each histogram.

[~, name, ~] = fileparts(tarFiles(k).name);

BW =BW>100;

[n,~] = hist(BW);

n = n(10,:);

for i= 1:c

if n(i)<40||(n(i)<75 && i>820) % Filter out unnecessary parts n(i) = 0;

end

end

j = 0;

for i = 1:c-1 % Locate the position of peaks if n(i)~=0 && n(i+1)==0

px(k-2,j+1) = i;

j = j+1;

end

end

for i = 1:rpx

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for j =1:cpx-1

if px(i,j+1)~=0

xSpacing(i,j) = px(i,j+1)-px(i,j); % Calculate the values of spacings

end

end

end

histo = bar(n);

str = ['0.' name];

num1 = str2double(str);

saveas(histo, [dir\_name2,'\',name,'.jpg']); % Save histograms as jpeg images.

end

xlswrite(ffn, xSpacing ,'sheet1', 'A1'); % Save data into an excel document.

Document 2

* Script: Rigtpart.m
* Purpose: process the right part of an experimental image to obtain the exact
* ratio, ratio2\_exp, of the distances A and B.
* A is the distance between the point on the thimble which coincides with the axial
* line to the lower graduation.
* B is the distance between the lower graduation and the higher graduation.
* Input: ‘\*\*\*\*\*.jpg’ – the experimental image.
* Output: ratio2\_exp -- the ratio as describe above.

clc;clear all;

BW = imread('25973.jpg'); % A typical experimental image [r,c] = size(BW);

BW =BW>100;

[n,~] = hist(BW);

n = n(10,:);

* Filter out unnecessary parts for i= 1:c

if n(i)<20 n(i) = 0;

end

end

* Locate the ranges of lower graduation, higher graduation and the axial line. py=zeros(2,3);

j = 0;

for i = 1:c-1

if n(i)~=0 && n(i+1)==0 py(2,j+1) = i;

j = j+1;

end

end

j = 0;

for i = 1:c-1

if n(i)==0 && n(i+1)~=0

py(1,j+1) = i+1;

j = j+1;

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end

end

* Find the means for lower graduation, higher graduation and the axial line.
* Use the means to represent the positions of each line.
* Calculate the ratio using the means.

pymean = mean(py);

ratio2\_exp = (pymean(2)-pymean(1))/(pymean(3)-pymean(1));

* Plot the intensity histogram histo = bar(n)

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**Appendix B Matlab scripts used in Chapter 5**

This part contains matlab scripts used in Chapter 5.

Document 1

* Title: CENTROIDS.m
* CENTROIDS is the main script.
* It calls a number of functions to do incline-correction reconstruct the virtual
* raster lines and decoding.
* clean up the work space

clc; clear all;

disp('Running centroids.m...'); % Message sent to command window.

[FileName,PathName] = uigetfile({'\*.bmp;\*.tif;\*.jpg;\*.gif;\*.png','Images

(\*.bmp,\*.tif,\*.jpg,\*.gif,\*.png)';

'\*.bmp', 'BMP Image(\*.bmp)'; ...

'\*.tif','Tiff Image(\*.tif)'; ...

'\*.jpg','JPEG Image (\*.jpg)'; ...

'\*.gif','GIF (\*.gif)'; ...

'\*.png','PNG (\*.png)'; ...

'\*.\*', 'All Files (\*.\*)'}, ...

'Select an Image');

if isequal(FileName,0)

disp('User selected Cancel')

else

FullFileName = fullfile(PathName, FileName); end

OI = imread(FullFileName);

OI = flipud(OI);

figure

%imshow(OI);

[numofBlobs, centroids] = GetCentroids(OI);

%}

* Since centroids is a N×2 array, it's not easy and instinct to utilize
* its data, we set two new N×N arrays x and y to store x-coordinates and
* y-coordinates of the centroids separately.

N = sqrt(numofBlobs);

xt = zeros(N);

yt = zeros(N);

for n=1:N

for m=1:N

xt(m,n) = centroids(m+(n-1)\*N,1);

yt(m,n) = centroids(m+(n-1)\*N,2);

end

end

[temp,index]=sort(yt,'descend');

% create y matrix

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y = temp;

* + create x matrix x = zeros(N); for m=1:N

for n=1:N x(n,m)=xt(index(n,m),m);

end

end

* obtain the offset indicators recX and recY
* obtain the spacing in x and y directions [recX,recY,xSpace,ySpace] = dotDirec(x,y);

[averx,avery,~,~] = Gridestab(recX,recY,x,y);

for i = 1:N

for j = 1:N

if abs(recX(j,i))+abs(recY(j,i))~=1

if abs(x(j,i)-averx(i))>abs(y(j,i)-avery(j)); recY(j,i) = 0;

recX(j,i) = sign(x(j,i)-averx(i));

else

recY(j,i) = sign(y(j,i)-avery(j));

recX(j,i) = 0;

end

end

end

end

MarkVal\_x = zeros(N);

MarkVal\_y = zeros(N);

* calculate the mark value for i=1:N^2

if recX(i) == -1 && recY(i) == 0 MarkVal\_x(i) = 3;

elseif recX(i) == 1 && recY(i) == 0 MarkVal\_x(i) = 1;

elseif recX(i) == 0 && recY(i) == -1 MarkVal\_y(i) = 4;

elseif recX(i) == 0 && recY(i) == 1 MarkVal\_y(i) = 2;

else

end

end

MarkVal = MarkVal\_x +MarkVal\_y;

* using mark value to determine x, y codes. xcode = zeros(N); ycode = zeros(N);

for j =1:N for i = 1:N

switch MarkVal(j,i)

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case 1

xcode(j,i)=0;

ycode(j,i)=1;

case 2

xcode(j,i)=0;

ycode(j,i)=0;

case 3

xcode(j,i)=1;

ycode(j,i)=0;

case 4

xcode(j,i)=1;

ycode(j,i)=1;

otherwise

* when error occurs xcode(j,i)=3; ycode(j,i)=3;

end

end

end

* find the pixel coordinates of the centroid of the object [objectX,objectY] = getcent

objectR = 0; objectC = 0;

for i = 1:N-1

if objectX >= averx(i) && objectX <=averx(i+1)

objectC = i + (objectX-averx(i))/(averx(i+1)-averx(i));

end

end

for j = 1:N-1

if objectY <= avery(j) && objectY >=avery(j+1)

objectR = j + (objectY-avery(j))/(avery(j+1)-avery(j));

end

end

* establish the code book as a reference for decoding BitSeq = enCod(0,6);

PaSeq\_1SDS = enCod(1,5); PaSeq\_2SDS = enCod(2,5); PaSeq\_3SDS = enCod(3,5); PaSeq\_4SDS = enCod(4,5);

* decoding..
* obtain the PDS

[PVy,PDSy] = deCody(ycode, BitSeq, 6);

[PVx,PDSx] = deCodx(xcode, BitSeq, 6);

* convert PDS into SDS in x direction [a1x,a2x,a3x,a4x] = PDScoeff(PDSx);
* obtain the place numbers in SDS in x direction [p1x,~] = deCodx(a1x,PaSeq\_1SDS ,5);

[p2x,~] = deCodx(a2x,PaSeq\_2SDS ,5);

[p3x,~] = deCodx(a3x,PaSeq\_3SDS ,5);

[p4x,~] = deCodx(a4x,PaSeq\_4SDS ,5);

* convert PDS into SDS in y direction [a1y,a2y,a3y,a4y] = PDScoeff(PDSy);

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% obtain the place numbers in SDS in y direction

[p1y,~] = deCody(a1y,PaSeq\_1SDS ,5);

[p2y,~] = deCody(a2y,PaSeq\_2SDS ,5);

[p3y,~] = deCody(a3y,PaSeq\_3SDS ,5);

[p4y,~] = deCody(a4y,PaSeq\_4SDS ,5);

* obtain the place numbers in PDS if needed %Px = Place\_PDS(xcode,1);

%Py = Place\_PDS(ycode,2);

* obtain the place numbers of the ROI

Bx = [p1x(1,1),p2x(1,1),p3x(1,1),p4x(1,1)];

By = [p1y(1,1),p2y(1,1),p3y(1,1),p4y(1,1)];

* the place numbers of the first column and the first row
* provided as a reference when establish Table 5-10 and Table 5-11 Ax = [32,57,12,96];

Ay = [224,19,4,155];

* + obtain the coordinates in columns and rows of the ROI.

X = DetCor(Ax,Bx);

Y = DetCor(Ay,By);

* obtain the coordinates in columns and rows of the object. objectC = X + objectC -1;

objectR = Y + objectR -1; Coordinate = [objectC,objectR]

Document 2

* Title: GetCentroids.m
* [numofBlobs, centroids] = GetCentroids(OI) uses binary image information
* contained in OI to determine the number of blobs, numofBlobs in the original
* image, locate the coordinates (pixels) of the centroids of each blob and save
* them in a array called centroids.

function [numofBlobs, centroids] = GetCentroids(OI)

% Maximize the figure window.

set(gcf, 'Position', get(0, 'ScreenSize'));

% Thresholding the image

thres = 100; % Set a threshold value for binarize the image

% BW = OI < thres; % Store the obtained binary image into an array 'BW'

BW = OI > thres;

* Find the coordinates of centroids of each blob
* Calculate all properties of the binary image blobMeasurements = regionprops(BW, 'centroid');
* Put the coordinates into an array 'centorids' centroids = cat(1, blobMeasurements.Centroid);
* Plot the centroids on the binary image

%imagesc(BW); colormap(gray(256)); title('Centroids of each blob'); axis square; imshow(BW)

[~,numofBlobs] = bwlabel(BW,8);

%hold on

plot(centroids(:,1), centroids(:,2),'.');axis square %hold off

Document 3

% Title: enCod.m

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* BitSeq = enCod(NumSeq,n) establishes a code book for decoding.
* NumSeq-- an integer number that has values 0~4. Indicate the
* kind of the number sequence used.
* 0- main number sequence.
* 1~4- secondary number sequence set A1, A2, A3, A4.
* n— has the value 5, 6 or 8. n=5 indicates encoding SDS, n=6 or 8
* indicate encoding PDS using 6×6 array or 8×8 array.
* BitSeq— the output.

function BitSeq = enCod(NumSeq,n)

switch NumSeq

case 0

NS =

[0,0,0,0,0,0,1,0,0,1,1,1,1,1,0,1,0,0,1,0,0,0,0,1,1,1,0,1,1,1,0,0,1,0,1,0,1,0,0,0,1,

0,1,1,0,1,1,0,0,1,1,0,1,0,1,1,1,1,0,0,0,1,1];

case 4

NS =

[0,0,0,0,0,1,0,2,0,0,0,0,2,0,0,2,0,1,0,0,0,1,1,2,0,0,0,1,2,0,0,2,1,0,0,0,2,1,1,2,0,

1,0,1,0,0,1,2,1,0,0,1,0,0,2,2,0,0,0,2,2,1,0,2,0,1,1,0,0,1,1,1,0,1,0,1,1,0,1,2,0,1,1

,1,1,0,0,2,0,2,0,1,2,0,2,2,0,1,0,2,1,0,1,2,1,1,0,1,1,1,2,2,0,0,1,0,1,2,2,2,0,0,2,2,

2,0,1,2,1,2,0,2,0,0,1,2,2,0,1,1,2,1,0,2,1,1,0,2,0,2,1,2,0,0,1,1,0,2,1,2,1,0,1,0,2,2

,0,2,1,0,2,2,1,1,1,2,0,2,1,1,1,0,2,2,2,2,0,2,0,2,2,1,2,1,1,1,1,2,1,2,1,2,2,2,1,0,0,

2,1,2,2,1,0,1,1,2,2,1,1,2,1,2,2,2,2,1,2,0,1,2,2,1,2,2,0,2,2,2,1,1]; case 2

NS =

[0,0,0,0,0,1,0,0,0,0,2,0,1,0,0,1,0,1,0,1,1,0,0,0,1,1,1,1,0,0,1,1,0,1,0,0,2,0,0,0,1,

2,0,1,0,1,2,1,0,0,0,2,1,1,1,0,1,1,1,0,2,1,0,0,1,2,1,2,1,0,1,0,2,0,1,1,0,2,0,0,1,0,2

,1,2,0,0,0,2,2,0,0,1,1,2,0,2,0,0,2,0,2,0,1,2,0,0,2,2,1,1,0,0,2,1,0,1,1,2,1,0,2,0,2,

2,1,0,0,2,2,2,1,0,1,2,2,0,0,2,1,2,2,1,1,1,1,1,2,0,0,1,2,2,1,2,0,1,1,1,2,1,1,2,0,1,2

,1,1,1,2,2,0,2,2,0,1,1,2,2,2,2,1,2,1,2,2,0,1,2,2,2,0,2,0,2,1,1,2,2,1,0,2,2,0,2,1,0,

2,1,1,0,2,2,2,2,0,1,0,2,2,1,2,2,2,1,1,2,1,2,0,2,2,2];

case 3

NS = [0,0,0,0,0,1,0,0,1,1,0,0,0,1,1,1,1,0,0,1,0,1,0,1,1,0,1,1,1,0,1]; case 1

NS =

[0,0,0,0,0,1,0,0,0,0,2,0,1,0,0,1,0,1,0,0,2,0,0,0,1,1,0,0,0,1,2,0,0,1,0,2,0,0,2,0,2,

0,1,1,0,1,0,1,1,0,2,0,1,2,0,1,0,1,2,0,2,1,0,0,1,1,1,0,1,1,1,1,0,2,1,0,1,0,2,1,1,0,0

,1,2,1,0,1,1,2,0,0,0,2,1,0,2,0,2,1,1,1,0,0,2,1,2,0,1,1,1,2,0,2,0,0,1,1,2,1,0,0,0,2,

2,0,1,0,2,2,0,0,1,2,2,0,2,0,2,2,1,0,1,2,1,2,1,0,2,1,2,1,1,0,2,2,1,2,1,2,0,2,2,0,2,2

,2,0,1,1,2,2,1,1,0,1,2,2,2,2,1,2,0,0,2,2,1,1,2,1,2,2,1,0,2,2,2,2,2,0,2,1,2,2,2,1,1,

1,2,1,1,2,0,1,2,2,1,2,2,0,1,2,1,1,1,1,2,2,2,0,0,2,1,1,2,2];

end

SL = length(NS);

bitseq = zeros(SL,n);

BitSeq = zeros(SL,n);

for i = 1:SL

for j = 1:n

if i+j-1 <= SL

bitseq(i,j) = NS(i+j-1);

else

bitseq(i,j) = NS(i+j-1-SL);

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end

end

end

BitSeq = cellstr(int2str(bitseq));

Document 4

* Title: deCodx.m
* [PosVal,DS] = deCodx(code, BitSeq, n)decodes the code in the x direction
* n— has the value 5, 6 or 8. n=5 indicates encoding SDS, n=6 or 8
* indicate encoding PDS using 6×6 array or 8×8 array.

function [PosVal,DS] = deCodx(code, BitSeq, n)

[r\_code,c\_code] = size(code);

switch n

case 8

r\_codeT = floor(r\_code/n); % number of vertical bit sequences of x-code. c\_codeT = c\_code;

bla = blanks(c\_codeT\*(n+2\*(n-1)));

bla = zeros(r\_codeT,length(bla));

case 6

r\_codeT = floor(r\_code/n); % number of vertical bit sequences of x-code. c\_codeT = c\_code;

bla = blanks(c\_codeT\*(n+2\*(n-1)));

bla = zeros(r\_codeT,length(bla)); % build a temporary array to contain the

codes.

case 5

c\_codeT = floor(c\_code/n);

r\_codeT = r\_code;

bla = blanks(c\_codeT\*(n+2\*(n-1)));

bla = zeros(r\_codeT,length(bla));

otherwise

disp('n must be 5 or 6 or 8')

end

PosVal = zeros(r\_codeT,c\_codeT);

DS = zeros(r\_codeT,c\_codeT-1); %Primary Difference Sequence

switch n

case 8

for i = 1: r\_codeT

code8 = char(int2str(code(1+(i-1)\*n:i\*n,:)')); [r8,c8] = size(code8);

for j = 1:r8

bla(i, 1+(j-1)\*c8:j\*c8) = code8(j,:);

end

end

case 6

for i = 1: r\_codeT

code6 = char(int2str(code(1+(i-1)\*n:i\*n,:)')); [r6,c6] = size(code6);

for j = 1:r6

bla(i, 1+(j-1)\*c6:j\*c6) = code6(j,:);

end

end

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case 5

for i = 1: r\_codeT

code5 = char(int2str(code(:,1+(i-1)\*n:i\*n)));

[~,c5] = size(code5);

bla(:,1+(i-1)\*c5:i\*c5) = code5;

end

end

bla = char(bla);

for i = 1:r\_codeT

for j = 1:c\_codeT

for k = 1:length(BitSeq)

if isequal(bla(i,1+(j-1)\*n+2\*(n-1)\*(j-1):j\*n+2\*(n-1)\*j),BitSeq{k})

PosVal(i,j) = k-1;

end

end

end

end

switch n

case 6

for i = 1:r\_codeT

for j = 1:c\_codeT-1

DS(i,j) = mod((PosVal(i,j+1)-PosVal(i,j)),63);

end

end

case 8

for i = 1:r\_codeT

for j = 1:c\_codeT-1

DS(i,j) = mod((PosVal(i,j+1)-PosVal(i,j)),63);

end

end

otherwise

DS = [];

end

Document 5

* Title: deCody.m
* [PosVal,DS] = deCody(code, BitSeq, n)decodes the code in the y direction
* n— has the value 5, 6 or 8. n=5 indicates encoding SDS, n=6 or 8
* indicate encoding PDS using 6×6 array or 8×8 array.

function [PosVal,DS] = deCody(code, BitSeq, n)

[r\_code,c\_code] = size(code);

switch n

case 8

c\_codeT = floor(c\_code/n); % number of vertical bit sequences of x-code. r\_codeT = r\_code;

bla = blanks(c\_codeT\*(n+2\*(n-1)));

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bla = zeros(r\_codeT,length(bla)); % build a temporary array to contain the

codes.

case 6

c\_codeT = floor(c\_code/n); % number of vertical bit sequences of x-code. r\_codeT = r\_code;

bla = blanks(c\_codeT\*(n+2\*(n-1)));

bla = zeros(r\_codeT,length(bla)); % build a temporary array to contain the

codes.

case 5

r\_codeT = floor(r\_code/n);

c\_codeT = c\_code;

bla = blanks(c\_codeT\*(n+2\*(n-1)));

bla = zeros(r\_codeT,length(bla));

otherwise

disp('n must be 5 or 6.')

end

PosVal = zeros(r\_codeT,c\_codeT);

DS = zeros(r\_codeT-1,c\_codeT); %Primary Difference Sequence

switch n

case 8

for i = 1: c\_codeT

code8 = char(int2str(code(:,1+(i-1)\*n:i\*n))); [~,c8] = size(code8);

bla(:,1+(i-1)\*c8:i\*c8) = code8;

end

case 6

for i = 1: c\_codeT

code6 = char(int2str(code(:,1+(i-1)\*n:i\*n))); [~,c6] = size(code6);

bla(:,1+(i-1)\*c6:i\*c6) = code6;

end

case 5

for i = 1: r\_codeT

code5 = char(int2str(code(1+(i-1)\*n:i\*n,:)')); [r5,c5] = size(code5);

for j = 1:r5

bla(i, 1+(j-1)\*c5:j\*c5) = code5(j,:);

end

end

end

bla = char(bla);

for i = 1:r\_codeT

for j = 1:c\_codeT

for k = 1:length(BitSeq)

if isequal(bla(i,1+(j-1)\*n+2\*(n-1)\*(j-1):j\*n+2\*(n-1)\*j),BitSeq{k})

PosVal(i,j) = k-1;

end

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end

end

end

switch n

case 8

for i = 1:r\_codeT-1

for j = 1:c\_codeT

DS(i,j) = mod((PosVal(i+1,j)-PosVal(i,j)),63); %DS(i,j) = mod(abs((PosVal(i,j+1)-PosVal(i,j))),63);

end

end

case 6

for i = 1:r\_codeT-1

for j = 1:c\_codeT

DS(i,j) = mod((PosVal(i+1,j)-PosVal(i,j)),63); %DS(i,j) = mod(abs((PosVal(i,j+1)-PosVal(i,j))),63);

end

end

otherwise

DS = [];

end

Document 6

* Title: PDScoeff.m
* [a1,a2,a3,a4] = PDScoeff(PDS) converts the primary difference sequence PDS into
* sequences a1, a2, a3 and a4.

function [a1,a2,a3,a4] = PDScoeff(PDS)

[r,c] = size(PDS);

a1= zeros(r,c);a2= zeros(r,c);a3= zeros(r,c);a4= zeros(r,c);

for i = 1:r

for j = 1:c

if PDS(i,j)>=5 && PDS(i,j)<= 58%PDS(i,j)>=5 && PDS(i,j)<= 58 if PDS(i,j)>=41 % 5+2\*18

a4(i,j) = 2;

elseif PDS(i,j)>=23 % 5+1\*18

a4(i,j) = 1;

else

a4(i,j) = 0;

end

PDS(i,j) = PDS(i,j) - a4(i,j)\*18 -5;

if PDS(i,j)>= 9 % 1\*9

a3(i,j) = 1;

else

a3(i,j) = 0;

end

PDS(i,j) = PDS(i,j)-a3(i,j)\*9;

if PDS(i,j) >= 6 % 2\*3

a2(i,j) = 2;

elseif PDS(i,j) >= 3 %1\*3

a2(i,j) = 1;

else

a2(i,j) = 0;

end

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PDS(i,j)= PDS(i,j)-a2(i,j)\*3;

a1(i,j) = PDS(i,j);

else % which means the element of PDS does not belong to [5,58] a1(i,j) = 8;

a2(i,j) = 8;

a3(i,j) = 8;

a4(i,j) = 8;

end

end

end

Document 7

* Title: DetCor.m
* X = DetCor(A,B) determines the coordinates of the dots in columns and rows.
* A = (p1r,p2r,p3r,p4r) is the reference unique 4-number combination.
* B = (p1,p2,p3,p4) is the 4-number combination of the interested region. function X = DetCor(A,B)

a = zeros(4,1000);

* establish a table for i = 1:1000

a(1,i) = mod(A(1)+i-1,236); a(2,i) = mod(A(2)+i-1,233); a(3,i) = mod(A(3)+i-1,31); a(4,i) = mod(A(4)+i-1,241);

end

% output the result.

flag = 0;

for i=1:1000

if a(4,i) == B(4) && a(3,i)== B(3) && a(2,i) == B(2) && a(1,i) == B(1) X = i;

flag =1;

end

end

if flag == 0

disp('no match found')

X=0;

end

Document 8

* Title: getcent.m
* [X,Y] = getcent find the centroid coordinates in pixels for the object. function [X,Y] = getcent

clc; clear all;

disp('Running program, please wait...'); % Message sent to command window.

[FileName,PathName] = uigetfile({'\*.bmp;\*.tif;\*.jpg;\*.gif;\*.png','Images

(\*.bmp,\*.tif,\*.jpg,\*.gif,\*.png)';

'\*.bmp', 'BMP Image(\*.bmp)'; ...

'\*.tif','Tiff Image(\*.tif)'; ...

'\*.jpg','JPEG Image (\*.jpg)'; ...

'\*.gif','GIF (\*.gif)'; ...

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'\*.png','PNG (\*.png)'; ...

'\*.\*', 'All Files (\*.\*)'}, ...

'Select an Image');

if isequal(FileName,0)

disp('User selected Cancel')

else

FullFileName = fullfile(PathName, FileName); end

OI3 = imread(FullFileName);

OI3 = flipud(OI3);

figure

[numofBlobs, centroids] = GetCentroids(OI3);

N = sqrt(numofBlobs);

xt = zeros(N);

yt = zeros(N);

for n=1:N

for m=1:N

xt(m,n) = centroids(m+(n-1)\*N,1);

yt(m,n) = centroids(m+(n-1)\*N,2);

end

end

[temp,index]=sort(yt,'descend');

* create y matrix y = temp;
* create x matrix x = zeros(N); for m=1:N

for n=1:N x(n,m)=xt(index(n,m),m);

end

end

X = x;

Y = y;

Document 9

* Title: dotDirec.m
* [recX,recY,xSpace,ySpace] = dotDirec(x,y) analyzes the x-coordinates and
* y-coordinates of the centroids and assign offset direction indicators recX and
* recY to each dot. xSpace and ySpace are two arrays used to record the spacings
* of the columns and rows respectively.

function [recX,recY,xSpace,ySpace] = dotDirec(x,y)

[N,M] = size(x);

recX = zeros([N,M]);

recY = recX;

xSpace = zeros(1,M);

ySpace = zeros(N,1);

xt1 = zeros(1,M);

xt2 = zeros(1,M);

yt1 = zeros(N,1);

yt2 = zeros(N,1);

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for i = 1:M

xt1(i) = min(x(:,i));

xt2(i) = max(x(:,i));

xSpace(i) = xt2(i)-xt1(i);

end

for i = 1:M

for j = 1:N

x\_m1 = abs((x(j,i)/xt1(i))-1);

x\_m2 = abs((x(j,i)/xt2(i))-1);

x\_mm = min([x\_m1,x\_m2]);

if xSpace(i)> 2/3\* max(xSpace)

xt3 = (xt2(i)-xt1(i))/3+xt1(i);

xt4 = 2\*(xt2(i)-xt1(i))/3+xt1(i);

if x(j,i)>=xt1(i) && x(j,i)< xt3

recX(j,i) = -1;

elseif x(j,i)>=xt3 && x(j,i)< xt4

recX(j,i) = 0;

elseif x(j,i)>=xt4 && x(j,i)<= xt2(i)

recX(j,i) = 1;

else

switch x\_mm

case x\_m1

recX(j,i)=-1;

case x\_m2

recX(j,i)=1;

end

end

elseif xSpace(i)< 1/3\* max(xSpace)

recX(j,i) = 3;

else

xt5 = 0.5\*(xt1(i)+xt2(i));

if x(j,i)>=xt1(i) && x(j,i) < xt5

recX(j,i) = -2;

elseif x(j,i)>=xt5 && x(j,i) < xt2(i)

recX(j,i) = 2;

else

switch x\_mm

case x\_m1

recX(j,i)=-2;

case x\_m2

recX(j,i)=2;

end

end

end

end

end

for j = 1:N

yt1(j) = min(y(j,:));

yt2(j) = max(y(j,:));

ySpace(j) = yt2(j)-yt1(j);

end

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for j = 1:N

for i = 1:M

y\_m1 = abs((y(j,i)/yt1(j))-1);

y\_m2 = abs((y(j,i)/yt2(j))-1);

y\_mm = min([y\_m1,y\_m2]);

if ySpace(j)> 2/3\* max(ySpace)

yt3 = (yt2(j)-yt1(j))/3+yt1(j);

yt4 = 2\*(yt2(j)-yt1(j))/3+yt1(j);

if y(j,i)>=yt1(j) && y(j,i)< yt3

recY(j,i) = -1;

elseif y(j,i)>=yt3 && y(j,i)< yt4

recY(j,i) = 0;

elseif y(j,i)>=yt4 && y(j,i)<= yt2(j)

recY(j,i) = 1;

else

switch y\_mm

case y\_m1

recY(j,i)=-1;

case y\_m2

recY(j,i)=1;

end

end

elseif ySpace(i)< 1/3\* max(ySpace)

recY(j,i) = 3;

else

yt5 = 0.5\*(yt1(j)+yt2(j));

if y(j,i)>=yt1(j) && y(j,i) < yt5

recY(j,i) = -2;

elseif y(j,i)>=yt5 && x(j,i) < yt2(j)

recY(j,i) = 2;

else

switch y\_mm

case y\_m1

recY(j,i)=-2;

case y\_m2

recY(j,i)=2;

end

end

end

end

end

xismatched = zeros(N,M);

wrongcolumn = zeros(1,M);

x\_replace = 225;

k = 1;

for i = 1:M

if isempty(find(recX(:,i) ==0))

wrongcolumn(k)= i;

k = k+1;

end

end

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for i = 1:M

if wrongcolumn(i) ~=0

t = wrongcolumn(i);

for j = 1:N

if (recY(j,t)== -1) || (recY(j,t) == 1)

x\_replace = recX(j,t);

xismatched(j,t) = 1;

else

xismatched(j,t) = 0;

end

if recX(j,t) == x\_replace

recX(j,t) = 0;

elseif recX(j,t)>0

recX(j,t) = 1;

else

recX(j,t) = -1;

end

end

end

end

yismatched = zeros(N,M);

wrongrow = zeros(N,1);

y\_replace = 225;

l = 1;

for j = 1:N

if isempty(find(recY(j,:) ==0))

wrongrow(l)= j;

l = l+1;

end

end

for j = 1:N

if wrongrow(j) ~=0

s = wrongrow(j);

for i = 1:M

if (recX(s,i)== -1) || (recX(s,i) == 1)

y\_replace = recY(s,i);

yismatched(s,i) = 1;

else

yismatched(s,i) = 0;

end

if recY(s,i) == y\_replace

recY(s,i) = 0;

elseif recY(s,i)>0

recY(s,i) = 1;

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else

recY(s,i) = -1;

end

end

end

end

Document 10

* Title: Gridestab.m
* [averx,avery,~,~] = Gridestab(recX,recY,x,y)reconstructs the virtual raster lines
* and returns the coordinates averx and avery of the raster lines.

function [averx,avery,deltax,deltay] = Gridestab(recX,recY,x,y)

plot(x(:,:),y(:,:),'r\*');axis square

hh=axis;

[M,N] = size(x);

averx = zeros(1,M);

deltax = zeros(1,M-1);

hold on;

for i = 1:M

count = 0;

sum = 0;

for j = 1:N

if recX(j,i) == 0

sum = sum + x(j,i);

count = count+1;

end

end

averx(i) = sum/count;

plot([averx(i),averx(i)],[hh(3),hh(4)],'b');axis square

end

for i = 1:M-1

deltax(i) = averx(i+1)-averx(i);

end

avery = zeros(1,N);

deltay = zeros(1,N-1);

for j = 1:N

count = 0;

sum = 0;

for i = 1:M

if recY(j,i) == 0

sum = sum + y(j,i);

count = count+1;

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end

end

avery(j) = sum/count;

plot([hh(1),hh(2)],[avery(j),avery(j)],'b');axis square

end

for j = 1:N-1

deltay(j) = avery(j+1)-avery(j);

end

hold off

Document 11

* Title: RotateCorrect.m
* Purpose: Do incline-correction. clc;

clear all;

[FileName,PathName] = uigetfile({'\*.bmp;\*.tif;\*.jpg;\*.gif;\*.png','Images (\*.bmp,\*.tif,\*.jpg,\*.gif,\*.png)';

'\*.bmp', 'BMP Image(\*.bmp)'; ...

'\*.tif','Tiff Image(\*.tif)'; ...

'\*.jpg','JPEG Image (\*.jpg)'; ...

'\*.gif','GIF (\*.gif)'; ...

'\*.png','PNG (\*.png)'; ...

'\*.\*', 'All Files (\*.\*)'}, ...

'Select an Image');

if isequal(FileName,0)

disp('User selected Cancel')

else

FullFileName = fullfile(PathName, FileName); end

OI = imread(FullFileName);

imshow(OI);

[numofBlobs, centroids] = GetCentroids(OI);

xy = [centroids(round(numofBlobs/2),1), centroids(round(numofBlobs/2),2)]; P = FindPoint(centroids,xy);

alphaSum = 0;

for i=1:4

temp = P{i}-xy;

d = sqrt(temp(1)^2+temp(2)^2);

if temp(1)/d ~=0 && temp(2)/d ~=0

if mod(i,2)==0

asin(abs(temp(2))/d)

alpha = asin(abs(temp(2))/d);

else

asin(abs(temp(2))/d)

alpha = pi/2-asin(abs(temp(2))/d);

end

alphaSum = alphaSum + alpha;

else

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alphaSum = 0;

end

end

alphaM = 0.25\*alphaSum\*180/pi;

sprintf('the rotated angle is: %.2f degrees',alphaM)

[FileName,PathName] = uigetfile({'\*.bmp;\*.tif;\*.jpg;\*.gif;\*.png','Images

(\*.bmp,\*.tif,\*.jpg,\*.gif,\*.png)';

'\*.bmp', 'BMP Image(\*.bmp)'; ...

'\*.tif','Tiff Image(\*.tif)'; ...

'\*.jpg','JPEG Image (\*.jpg)'; ...

'\*.gif','GIF (\*.gif)'; ...

'\*.png','PNG (\*.png)'; ...

'\*.\*', 'All Files (\*.\*)'}, ...

'Select an Image');

if isequal(FileName,0)

disp('User selected Cancel')

else

FullFileName = fullfile(PathName, FileName); end

OI2 = imread(FullFileName);

RI = imrotate(OI2,-alphaM);

figure

imshow(RI);

Document 12[28]

* Title: FindPoint.m
* This function is not written by the author of this thesis. It is found on a
* Matlab learner’s forum on the internet.
* Point = FindPoint(xy0, xy)Find nearest points of one given point in 4 quadrants. function Point = FindPoint(xy0, xy)

Point = cell(1,4);

x = xy0(:,1) - xy(1); y = xy0(:,2) - xy(2);

* 1st quadrant

id1 = (x>0 & y>=0);

Point{1} = subfun(id1,x,y,xy0);

% 2nd quadrant

id2 = (x<=0 & y>0);

Point{2} = subfun(id2,x,y,xy0);

% 3rd quadrant

id3 = (x<0 & y<=0);

Point{3} = subfun(id3,x,y,xy0);

% 4th quadrant

id4 = (x>=0 & y<0);

Point{4} = subfun(id4,x,y,xy0);

function xyPoint = subfun(id,x,y,xy0) % find the nearest point xyPoint = [];

x1 = x(id);

if ~isempty(x1)

y1 = y(id);

distance = x1.^2 + y1.^2;

xy0\_1 = xy0(id,:);

xyPoint = xy0\_1(find(distance == min(distance)),:);

end

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