

A Circle Packing Algorithm

Final Project of the Advanced AlgorithmII

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 - What is Circle Packing?
- 2 Input/Output data of Circle Packing Algorithm
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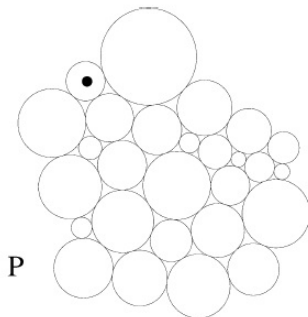
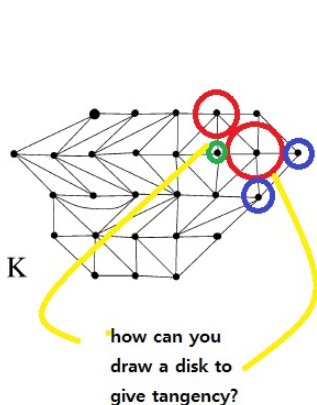
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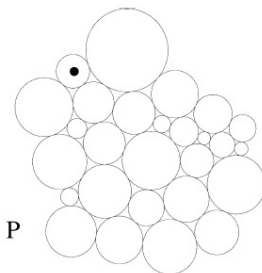
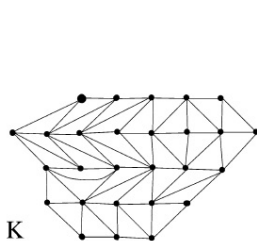
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Given a complex K , consists of vertices and the information of the connection between two vertices,



we are looking for a configuration P of circles realizing a pattern of 

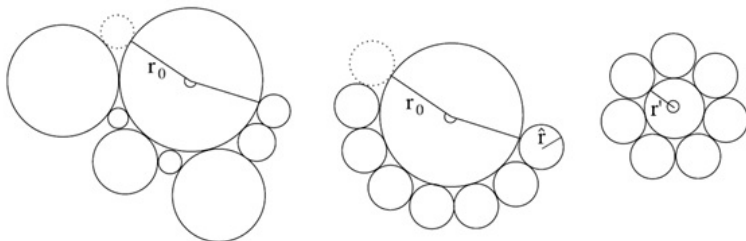
Input and Output data



- Input data are set of vertices and the connection information between two vertices(not triangles) and the appropriate boundary conditions.
- Output data are radii of the corresponding circle packing for K .

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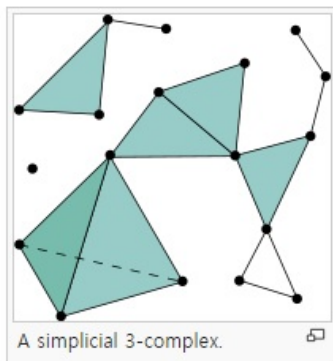
The Process of the Uniform Neighbor Model Algorithm

Step1. Given a value for r (radius of a center disk), determine \hat{r} so that $\hat{\theta}(r; \hat{r}) = \theta(r; r_j)$.

Step2. Solve for a new value for r (call it u) so that $\hat{\theta}(u; \hat{r}) = A(r)$.

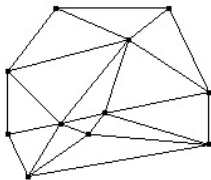
Some restrictions

We restrict to the case in which K is a finite triangulation of a closed topological disc, so we have a finite number of vertices, edges and faces.

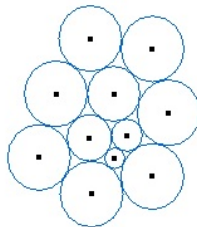


Test results of some complexes

Test results



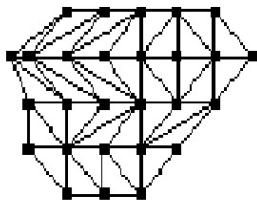
K



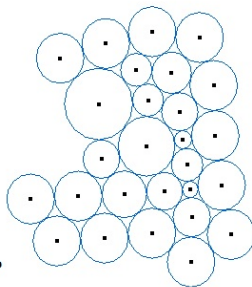
P

With boundary radii, $r_{boundary}=16$

Test results



K

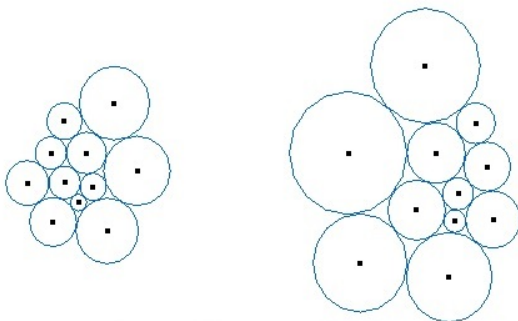


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With boundary radii, $r_{boundary}=16$

Test results

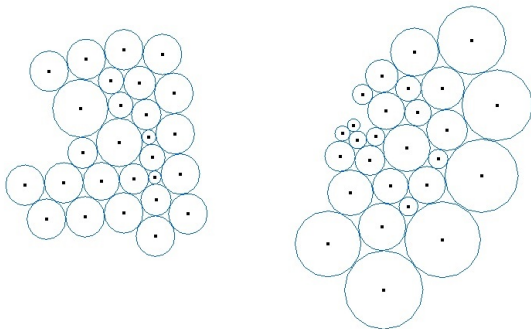
The boundary conditions are needed to give a unique circle packing.



Without the boundary conditions, there can be many possible circle packings

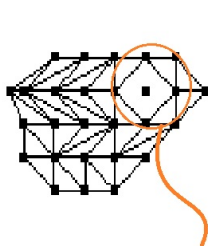
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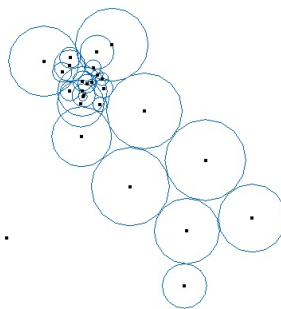


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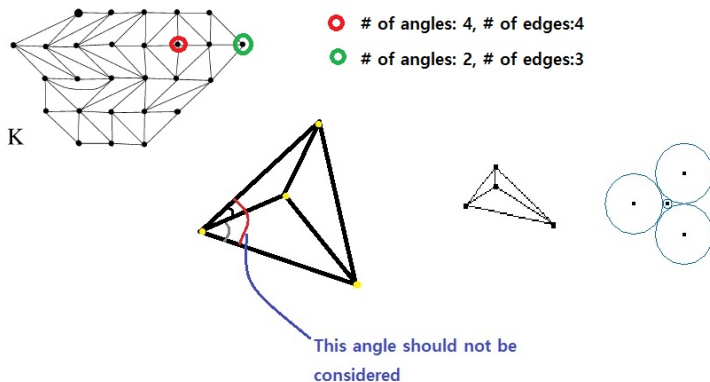


Because of this, it is not a closed topological disc



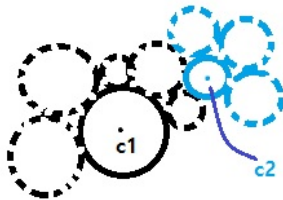
Things to consider

To discern whether the vertex is interior or boundary, I used the information of the sign of the normal vector.



Things to consider

To locate circles in certain order, in this implementation I used the angle information with vectors between x-axis. and I also used two directions to located circles.



Locating Circles in certain order should be considered with angle

Thank you



C.Collins, K. Stephenson A circle packing algorithm, J. Comp. Geom. **25** (2003), 233-256.