State

Language with Explicit References

Language wit Implicit References

Mutable Pai

Parameter Passing Part IV: State

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Explicit
References

Implicit References

Mutable Pair

- 1 State
- 2 Language with Explicit References
 - 3 Language with Implicit References
- 4 Mutable Pairs
- **5** Parameter Passing Variations

Language with Explicit References

Implicit
References

Mutable Pair

Parameter Passing

- Computations may also have effects
 - print
 - change a memory location
 - change a file

Language with Explicit References

Language wit Implicit References

Mutable Pair

- Computations may also have effects
 - print
 - change a memory location
 - change a file
- An effect is global: affects the entire computation

Language with Explicit References

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Mutable Pair

- · Computations may also have effects
 - print
 - change a memory location
 - change a file
- An effect is global: affects the entire computation
- We will now study assignment (aka mutation)

Language wir Explicit References

Language with Implicit References

Mutable Pair

Parameter Passing

- Assignment is about sharing values/information between unrelated parts of a computation
- CSAS 1115: telephone book, bank account

Language wit Explicit References

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Mutable Pair

- Assignment is about sharing values/information between unrelated parts of a computation
 - CSAS 1115: telephone book, bank account
 - Memory model
 - A finite map of locations to storable values (aka store or heap)
 - A place in memory where values can be stored

Language wit Explicit References

Language wit Implicit References

Mutable Pair

- Assignment is about sharing values/information between unrelated parts of a computation
- CSAS 1115: telephone book, bank account
- Memory model
 - A finite map of locations to storable values (aka store or heap)
 - A place in memory where values can be stored
- Implementation
 - Typically, storable values are the same as the expressed values
 - A data structure that represents a location is called a reference (aka pointer)

Language with Explicit References

Implicit
References

Mutable Pair

- Two ways to design a language with store
- Explicit references
- programmer allocates, dereferences, and mutates locations/memory

Language with Explicit References

Language wit Implicit References

Mutable Pair

- Two ways to design a language with store
- Explicit references
- programmer allocates, dereferences, and mutates locations/memory
- Implicit references
- language packages common patterns of allocation, dereferencing, and mutation

Mutable Pair

Parameter Passing

Language with Explicit References

- expval = int + bool + proc + ref(expval)
- denval = expval

Mutable Pair

Parameter Passing

Language with Explicit References

- expval = int + bool + proc + ref(expval)
- denval = expval
- 3 new ops needed:

newref allocates a new location and returns a reference to the new location

deref returns the content of a reference

setref changes the content of a referenced location

State

Language with Explicit References

Language wit Implicit References

Mutable Pair

Parameter Passing

Language with Explicit References

• Value?
let temp = newref(0)
in let x = newref(5)

Chaha

Language with Explicit References

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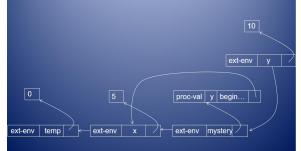
Mutable Pair

Parameter Passing

Language with Explicit References

• Value?

in (mystery newref(10))



State

Language with Explicit References

Language wit Implicit References

Mutable Pair

Parameter Passing

Language with Explicit References

```
let temp = newref(0)
    let x = newref(5)
         let mystery = proc (y)
                           begin
                              setref(temp, deref(x)));
                              setref(x, deref(y));
                              setref(y, deref(temp));
                              deref(x)
         end
    in (mystery newref(10))
                                                    ext-env
                                                v begin...
                                         proc-val
        ext-env
              temp
                        ext-env
                                         ext-env
                                                mystery
```

State

Language with Explicit References

Language wit Implicit References

Mutable Pair

Parameter Passing

Language with Explicit References

```
• let temp = newref(0)
      let x = newref(5)
       in let mystery = proc (y)
                              begin
                                setref(temp, deref(x)));
                                setref(x, deref(y));
                                setref(y, deref(temp));
                                deref(x)
           end
       in (mystery newref(10))
                                                      ext-env
                                           proc-val y begin...
                 temp
                           ext-env
                                           ext-env
                                                  mystery
          ext-env
```

Charle

Language with Explicit References

Language wit Implicit References

Mutable Pair:

Parameter Passing

Language with Explicit References

```
let temp = newref(0)
   let x = newref(5)
        let mystery = proc (y)
                           begin
                             setref(temp, deref(x)));
                             setref(x, deref(y));
                             setref(y, deref(temp));
                             deref(x)
         end
    in (mystery newref(10))
                                                  ext-env
                                               v begin...
       ext-env
              temp
                        ext-env
                                        ext-env
```

Returns: 10

Mutable Pair

Parameter Passing

Language with Explicit References

```
let x = newref(newref(10))
in begin
setref(deref(x), 20));
+(20, deref(deref(x)))
end
```

Language with Explicit References

Language wit Implicit References

Mutable Pair

Parameter Passing

Language with Explicit References

```
• let x = newref(newref(10))
  in begin
  setref(deref(x), 20));
   +(20, deref(deref(x)))
     end
```

Mutable Pai

Paramete Passing Variations

Language with Explicit References

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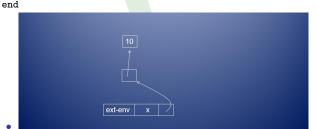


Mutable Pair

Parameter Passing

Language with Explicit References

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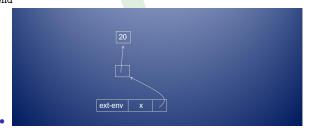


Mutable Pair

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Chaha

Language with Explicit References

Language with Implicit References

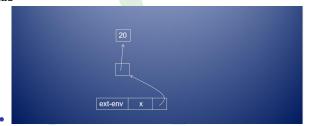
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Parameter Passing

Language with Explicit References

• Is this a valid program? If so, what does it evaluate to?

```
let x = newref(newref(10))
in begin
setref(deref(x), 20));
+(20, deref(deref(x)))
end
```



Returns 40

Language with Explicit References

Language wit Implicit References

Mutable Pair

Parameter Passing

Language with Explicit References

Expressed Values

```
(define-datatype expval expval?
  (num-val
    (value number?))
  (bool-val
    (boolean boolean?))
  (proc-val
    (proc proc?))
  (ref-val
    (ref reference?)))
```

Mutable Pair

Parameter Passing

Language with Explicit References

Expressed Values

```
(define-datatype expval expval?
    (num-val
     (value number?))
    (bool-val
     (boolean boolean?))
    (proc-val
     (proc proc?))
    (ref-val
     (ref reference?)))
• ;; expval --> ref throws error
  ;; Purpose: Extract ref from given expval
  (define (expval2ref v)
    (cases expval v
      (ref-val (ref) ref)
      (else (expval-extractor-error 'reference v))))
```

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Parameter Passing

Language with Explicit References

• To have effects values must be stored somewhere

Mutable Pai

Parameter Passing Variations

Language with Explicit References

- To have effects values must be stored somewhere
- σ ranges over the store (or heap)
- $[I=v]\sigma o$ the store σ extended with location I mapped to v

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Paramete Passing Variations

Language with Explicit References

- To have effects values must be stored somewhere
- σ ranges over the store (or heap)
- $[I=v]\sigma o$ the store σ extended with location I mapped to v
- · We shall think of the store as an argument to value-of
- (value-of exp1 ρ σ_0) = (val1, σ_1)
- σ_0 may or may not be the same as σ_1

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Parameter Passing

Language with Explicit References Specification

• (value-of (const-exp n) ρ σ) = ((numval n), σ)

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Parameter Passing

Language with Explicit References Specification

- (value-of (const-exp n) ρ σ) = ((numval n), σ)
- $\frac{(\textit{value-of exp1}\ \rho\ \sigma_0) = (\textit{val1},\ \sigma_1)\ \land\ (\textit{value-of exp2}\ \rho\ \sigma_1) = (\textit{val2},\ \sigma_2)}{(\textit{value-of (diff-exp exp1 exp2)}\ \rho\ \sigma_0) = ((\textit{num-val val1-val2})\ \sigma_2)}$

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Parameter Passing

Language with Explicit References Specification

- (value-of (const-exp n) ρ σ) = ((numval n), σ)
 - $\frac{(\textit{value-of exp1}\ \rho\ \sigma_0) = (\textit{val1},\ \sigma_1)\ \land\ (\textit{value-of exp2}\ \rho\ \sigma_1) = (\textit{val2},\ \sigma_2)}{(\textit{value-of (diff-exp exp1 exp2)}\ \rho\ \sigma_0) = ((\textit{num-val val1}-\textit{val2})\ \sigma_2)}$

```
\frac{(\textit{value-ofe1}\ \rho\ \sigma_0) = (\textit{v1},\sigma_1)}{(\textit{value-of}\ (\textit{if-exp}\ e1\ e2\ e3)}\ \rho\ \sigma_0) = \begin{cases} ((\textit{value-of}\ e2\ \rho\ \sigma_1),\sigma_2) & \text{if } (\exp\rightarrow\textit{val}\ \textit{v1}) = \#t\\ ((\textit{value-of}\ e3\ \rho\ \sigma_1),\sigma_2) & \text{otherwise} \end{cases}
```

Mutable Pair

Parameter Passing

Language with Explicit References Specification

```
• (value-of exp \rho \sigma_0) = (val1, \sigma_1) l \notin dom(\sigma_0)
(value-of (newref-exp exp) \rho \sigma_0)=((ref-val I), [I=val1]\sigma_1)
```

I is a new store location

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Parameter Passing

Language with Explicit References Specification

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(value-of exp \rho \sigma_0) = (val1, \sigma_1) l \notin dom(\sigma_0)
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```

- I is a new store location
- (value-of exp ρ σ_0) = (l, σ_1) (value-of (deref-exp exp) ρ σ_0) = ($\sigma_1(l)$, σ_1)

Implicit
References

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Parameter Passing Variations

Language with Explicit References Specification

- $\frac{(value-of\ exp\ \rho\ \sigma_0)=(val1,\ \sigma_1)\ l\notin dom(\sigma_0)}{(value-of\ (newref-exp\ exp)\ \rho\ \sigma_0)=((ref-val\ l),\ [l=val1]\sigma_1)}$
- I is a new store location
 - $\frac{(\textit{value-ofexp } \rho \ \sigma_0) = (\textit{I}, \ \sigma_1)}{(\textit{value-of } (\textit{deref-exp } \textit{exp}) \ \rho \ \sigma_0) = (\sigma_1(\textit{I}), \ \sigma_1)}$
- (value-of exp1 ρ σ_0) = (l, σ_1) \wedge (value-of exp2 ρ σ_1)=(val, σ_2) (value-of(setref-exp exp1 exp2) ρ σ_0) = (\varnothing , [l=val] σ_2)

Mutable Pair

Parameter Passing

Language with Explicit References Implementation

Grammar

Mutable Pair

Parameter Passing

Language with Explicit References

Implementation

- Design choice: the store is a global variable
- Design choice: Represent the store as a (listof expval)

Language with Explicit References

Language wit Implicit References

Mutable Pair

Parameter Passing

Language with Explicit References

- Design choice: the store is a global variable
- Design choice: Represent the store as a (listof expval)
 - ;; reference? : RacketVal --> Bool (define (reference? v) (and (integer? v) (>= v 0)))

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Parameter Passing

Language with Explicit References

- Design choice: the store is a global variable
- Design choice: Represent the store as a (listof expval)
- ;; reference? : RacketVal --> Bool (define (reference? v) (and (integer? v) (>= v 0)))
- ;; the-store: the current state of the store (define the-store 'uninitialized)

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Parameter Passing Variations

Language with Explicit References

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- ;; empty-store : --> store (define (empty-store) '())

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Parameter Passing Variations

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- ;; initialize-store! : --> store (define (initialize-store!) (set! the-store (empty-store)))

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Parameter Passing Variations

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- ;; empty-store : --> store (define (empty-store) '())
- ;; initialize-store! : --> store (define (initialize-store!) (set! the-store (empty-store)))
- ;; newref : expval --> ref
 (define (newref val)
 (let ((next-ref (length the-store)))
 (set! the-store (append the-store (list val)))
 next-ref))

Language with Explicit References

Language wit Implicit References

Mutable Pair

Parameter Passing Variations

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- Design choice: the store is a global variable
- Design choice: Represent the store as a (listof expval)
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- ;; newref : expval --> ref
 (define (newref val)
 (let ((next-ref (length the-store)))
 (set! the-store (append the-store (list val)))
 next-ref))
- ;; deref : ref --> expval (define (deref ref) (list-ref the-store ref))

Mutable Pair

Parameter Passing Variations

Language with Explicit References

```
    Design choice: the store is a global variable

    Design choice: Represent the store as a (listof expval)

:: reference? : RacketVal --> Bool
  (define (reference? v) (and (integer? v) (>= v 0)))
• :: the-store: the current state of the store
  (define the-store 'uninitialized)
• ;; empty-store : --> store
  (define (empty-store) '())
:: initialize-store! : --> store
  (define (initialize-store!) (set! the-store (empty-store)))
• ;; newref : expval --> ref
  (define (newref val)
    (let ((next-ref (length the-store)))
      (set! the-store (append the-store (list val)))
      next-ref))
• ;; deref : ref --> expval
  (define (deref ref) (list-ref the-store ref))
;; setref : ref expval --> expval
  (define (setref! ref new-expval)
    (set! the-store (append (take the-store ref)
                             (list new-expval)
                             (drop the-store (add1 ref)))))
```

Mutable Pair

Parameter Passing

Language with Explicit References Implementation

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Language with Explicit References

Language wit Implicit References

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Parameter Passing

Language with Explicit References

```
(define (value-of exp env)
  (cases expression exp
  (const-exp (num) (num-val num))
  (true-exp () (bool-val #t))
  (false-exp () (bool-val #f))
```

State

Language with Explicit References

Language wit Implicit References

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Parameter Passing

Language with Explicit References

```
(define (value-of exp env)
  (cases expression exp
   (const-exp (num) (num-val num))
   (true-exp () (bool-val #t))
   (false-exp () (bool-val #f))
   (var-exp (var) (apply-env env var))
```

Language with Explicit References

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Parameter Passing

Language with Explicit References

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Parameter Passing Variations

Language with Explicit References

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Language with Explicit References

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Parameter Passing

Language with Explicit References

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(define (value-of exp env)
  (cases expression exp
    (const-exp (num) (num-val num))
    (true-exp () (bool-val #t))
    (false-exp () (bool-val #f))
    (var-exp (var) (apply-env env var))
    (diff-exp (exp1 exp2)
              (let ((num1 (expval2num (value-of exp1 env)))
                    (num2 (expval2num (value-of exp2 env))))
                (num-val (- num1 num2))))
    (zero?-exp (exp1)
               (let ((val1 (expval2num (value-of exp1 env))))
                 (if (zero? val1)
                     (bool-val #t)
                     (bool-val #f))))
    (if-exp (exp1 exp2 exp3)
            (let ((val1 (value-of exp1 env)))
              (if (expval2bool val1)
                  (value-of exp2 env)
                  (value-of exp3 env))))
```

State

Language with Explicit References

Implicit
References

Mutable Pair

Parameter Passing Variations

Language with Explicit References

```
(define (value-of exp env)
  (cases expression exp
    (const-exp (num) (num-val num))
    (true-exp () (bool-val #t))
    (false-exp () (bool-val #f))
    (var-exp (var) (apply-env env var))
    (diff-exp (exp1 exp2)
              (let ((num1 (expval2num (value-of exp1 env)))
                    (num2 (expval2num (value-of exp2 env))))
                (num-val (- num1 num2))))
    (zero?-exp (exp1)
               (let ((val1 (expval2num (value-of exp1 env))))
                 (if (zero? val1)
                     (bool-val #t)
                     (bool-val #f))))
    (if-exp (exp1 exp2 exp3)
            (let ((val1 (value-of exp1 env)))
              (if (expval2bool val1)
                  (value-of exp2 env)
                  (value-of exp3 env))))
    (let-exp (vars exps body)
             (let [(vals (map (lambda (e) (value-of e env)) exps))]
               (value-of body
                          (foldr (lambda (var val acc)
                                   (extend-env var val acc))
                                 env
                                 vars
                                 vals))))
```

State

Language with Explicit References

Language wit Implicit References

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Parameter Passing

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Language wit Implicit References

Mutable Pair

Parameter Passing

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Parameter Passing Variations

Language with Explicit References

(define (value-of exp env)

State

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Parameter Passing Variations

Language with Explicit References

(define (value-of exp env)

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Parameter Passing Variations

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Language wit Implicit References

Mutable Pai

Parameter Passing Variations

```
    (define (value-of exp env)

     (cases expression exp
       (proc-exp (params body)
                 (proc-val (procedure params body (vector env))))
       (call-exp (rator rands)
                 (let [(proc (expval2proc (value-of rator env)))
                       (args (map (lambda (rand) (value-of rand env)) rands))]
                   (apply-procedure proc args)))
       (letrec-exp (names params bodies letrec-body)
                   (value-of letrec-body (mk-letrec-env names params bodies env)))
       (begin-exp (exp exps)
                  (foldl (lambda (e v) (value-of e env)) (value-of exp env) exps))
       (newref-exp (exp1)
                   (let ((v1 (value-of exp1 env)))
                     (ref-val (newref v1))))
       (deref-exp (exp1)
                  (let ((v1 (value-of exp1 env)))
                    (let ((ref1 (expval2ref v1)))
                    (deref ref1))))
```

State

Language with Explicit References

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Mutable Pair

Parameter Passing

```
    (define (value-of exp env)

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                 (proc-val (procedure params body (vector env))))
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                       (args (map (lambda (rand) (value-of rand env)) rands))]
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       (letrec-exp (names params bodies letrec-body)
                   (value-of letrec-body (mk-letrec-env names params bodies env)))
       (begin-exp (exp exps)
                  (foldl (lambda (e v) (value-of e env)) (value-of exp env) exps))
       (newref-exp (exp1)
                   (let ((v1 (value-of exp1 env)))
                     (ref-val (newref v1))))
       (deref-exp (exp1)
                  (let ((v1 (value-of exp1 env)))
                    (let ((ref1 (expval2ref v1)))
                    (deref ref1))))
       (setref-exp (exp1 exp2)
                   (let ((ref (expval2ref (value-of exp1 env))))
                     (let ((v2 (value-of exp2 env)))
                       (begin
                         (setref! ref v2)
                         (num-val -1)))))))
```

Implicit
References

Mutable Pair

Parameter Passing

Language with Explicit References Homework

• 4.1, 4.2, 4.4, 4.8, 4.9

Stata

Language wit Explicit References

Language with Implicit References

Mutable Pai

Parameter Passing

- Most modern PLs package common patterns of allocation, dereferencing, and mutation
- Programmers do not need to worry about these operations

Mutable Pair

Parameter Passing Variations

- Most modern PLs package common patterns of allocation, dereferencing, and mutation
- Programmers do not need to worry about these operations
- Every variable denotes a reference
- References are no longer expressed values and exist only as bindings of vars

```
expval = int + bool + proc
denval = ref(expval)
```

Ctata

Language wit Explicit References

Language with Implicit References

Mutable Pair

Parameter Passing Variations

- Most modern PLs package common patterns of allocation, dereferencing, and mutation
- Programmers do not need to worry about these operations
- Every variable denotes a reference
- References are no longer expressed values and exist only as bindings of vars expval = int + bool + proc denval = ref(expval)
- Locations are created with each binding operation: procedure call, let, and letrec

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Parameter Passing Variations

- Most modern PLs package common patterns of allocation, dereferencing, and mutation
- Programmers do not need to worry about these operations
- Every variable denotes a reference
- References are no longer expressed values and exist only as bindings of vars expval = int + bool + proc denval = ref(expval)
- Locations are created with each binding operation: procedure call, let, and letrec
- What happens when the interpreter encounters a var-exp?
 - env look-up to find the location to which it's bound
 - look-up in the store to find the value at that location
 - two-level system for var-exps

Language with Implicit References

Mutable Pair

- The content of a location can be changed (or mutated)
- expression \rightarrow set identifier = expression
- the identifier is not an expression; not evaluated
- vars are mutable

Mutable Pair

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- ullet expression o set identifier = expression
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- Extend LETREC language and implement call-by-value semantics
- Values are passed to every function
- Formal parameters bound to locations of operand values
- It is the most common form of parameter passing

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- Why are chains of references not possible?

Mutable Pair

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- Extend LETREC language and implement call-by-value semantics
- Values are passed to every function
- Formal parameters bound to locations of operand values
- It is the most common form of parameter passing
- Why are chains of references not possible?
- Refs are not expressed values

Language with Explicit References

Language with Implicit References

Mutable Pair

Parameter Passing

Consider

let a = 3
in let p = proc (x) set x = 4
in begin (p a); a end

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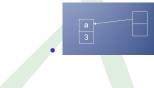
Language with Implicit References

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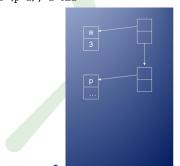
Explicit
References

Language with Implicit References

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Consider
let a = 3
in let p = proc (x) set x = 4
in begin (p a); a end
```



Charles

Explicit
References

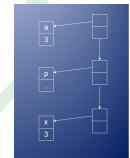
Language with Implicit References

Mutable Pair

Parameter Passing

```
• Consider
```

```
let a = 3
in let p = proc (x) set x = 4
  in begin (p a); a end
```



Mutable Pair

Parameter Passing Consider

let a = 3
in let p = proc (x) set x = 4
in begin (p a); a end



• Returns 3

State Specification

- (value-of (var-expv) ρ σ) = ($\sigma(\rho(v))$, σ)
- Get v's binding (a reference) and access store for v's expval
- The store is unchanged

Language with Implicit References

Mutable Pai

Parameter Passing Variations

State Specification

- (value-of (var-expv) ρ σ) = ($\sigma(\rho(v))$, σ)
- Get v's binding (a reference) and access store for v's expval
- The store is unchanged

- The location of v is changed to store val1
- The original value stored in $\sigma(v)$ is lost forever

Mutable Pair

Parameter Passing Variations

State Specification

- (value-of(var-expv) ρ σ) = ($\sigma(\rho(v))$, σ)
- Get v's binding (a reference) and access store for v's expval
- The store is unchanged

$$\frac{(\textit{value-of exp1 } \rho \ \sigma_0) = (\textit{val1}, \ \sigma_1)}{(\textit{value-of(set-exp } v \ exp1) \ \rho \ \sigma_0) = (\varnothing, \ [\sigma(v) = \textit{val1}]\sigma_1)}$$

- The location of v is changed to store val1
- The original value stored in $\sigma(v)$ is lost forever
- (apply-procedure (procedure v b ρ) val σ) = (value-of b [v = l] ρ [l = val] σ)
- The body is evaluated in a store where I contains the value of the parameter and an environment that binds the parameter to I

State

Explicit
References

Language with Implicit References

Mutable Pair

Parameter Passing Variations

State Specification

- (value-of(var-expv) $\rho \sigma$) = $(\sigma(\rho(v)), \sigma)$
- Get v's binding (a reference) and access store for v's expval
- The store is unchanged

$$\frac{(\textit{value-of exp1 } \rho \ \sigma_0) = (\textit{val1}, \ \sigma_1)}{(\textit{value-of(set-exp } v \ exp1) \ \rho \ \sigma_0) = (\varnothing, \ [\sigma(v) = \textit{val1}]\sigma_1)}$$

- The location of v is changed to store val1
- The original value stored in $\sigma(v)$ is lost forever
- (apply-procedure (procedure v b ρ) val σ) = (value-of b [v = l] ρ [l = val] σ)
- The body is evaluated in a store where I contains the value of the parameter and an environment that binds the parameter to I
- $\frac{(\textit{value-of exp1 } \rho \ \sigma) = (\textit{val}, \ \sigma_1)}{(\textit{value-of (let-exp var exp1 exp2)} \ \rho \ \sigma) = (\textit{value-of exp2 [var=l]} \rho \ [\textit{l=val}] \sigma_1)}$
- Evaluate the body of the let-exp in a store where I contains the value of the local variable and the local variable is bound to I

Language with Implicit References

Mutable Pair

Parameter Passing

State

- Evaluate all expressions using the given environment
- Evaluate ei using σ_i
- Apply the proc to the args using the store state after evaluating all expressions

Language with Implicit References

Mutable Pair

Parameter Passing Variations

- (value-of e0 ρ σ_0)=(ρ , σ_1) \wedge (value-of e1 ρ σ_1)=(ν 1, σ_2) \wedge (value-of e2 ρ σ_2)=(ν 2, σ_3) \wedge ... (value-of (call-exp e0 e1...en) ρ σ_0)=(apply-procedure ρ ν 1... ν n σ_{n+1})
- Evaluate all expressions using the given environment
- Evaluate ei using σ_i
- Apply the proc to the args using the store state after evaluating all expressions
- $\bullet \quad \frac{\rho_n = [n_1 = l_1 \dots n_n = l_n] \rho \ \land \ \rho 1 = (proc \text{-}val \ n_1 \ \rho_1 \ e_1 \ \rho_n) \ \land \dots \land \ pn = (proc \text{-}val \ n_n \ \rho_n \ e_n \ \rho_n)}{(v \text{-}o \ (letrec \text{-}exp \ n_1 \dots n_n \ p_1 \dots p_n \ e_1 \dots e_n \ e_{n+1}) \ \rho \ \sigma) = (v \text{-}o \ e_{n+1} \ \rho_n \ [l_1 = p1 \dots l_n = pn] \sigma)}$
- v-o = value-of
- All procs are allocated in the store

Language wit Explicit References

Language with Implicit References

Mutable Pai

Parameter Passing Variations

State

```
(expression
    ("begin" expression (arbno ";" expression) "end")
    begin-exp)
(expression ("set" identifier "=" expression) set-exp)
```

Implementation

Language wit Explicit

Language with Implicit References

Mutable Pair

Parameter Passing Variations

```
(expression
    ("begin" expression (arbno ";" expression) "end")
    begin-exp)
```

```
(expression ("set" identifier "=" expression) set-exp)
```

The store is the same as with Explicit Refs

Implementation

Language wit Explicit References

Language with Implicit References

Mutable Pair

Parameter Passing Variations

- The store is the same as with Explicit Refs
 - (define-datatype expval expval?
 (num-val
 (value number?))
 (bool-val
 (boolean boolean?))
 (proc-val
 (proc proc?)))
- Unlike Explicit Refs, no ref-val

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Implementation

Language wit Explicit References

Language with Implicit References

Mutable Pan

Parameter Passing Variations

```
(expression
        ("begin" expression (arbno ";" expression) "end")
       begin-exp)
  (expression ("set" identifier "=" expression) set-exp)

    The store is the same as with Explicit Refs

  (define-datatype expval expval?
    (num-val
      (value number?))
     (bool-val
      (boolean boolean?))
    (proc-val
      (proc proc?)))

    Unlike Explicit Refs, no ref-val

    Same as Explicit Refs

  (define (value-of-program pgm)
    (begin
       (initialize-store!)
       (cases program pgm
         (a-program (exp1)
```

(value-of exp1 (empty-env))))))

Implementation

```
Language wi
Explicit
References
```

Language with Implicit References

Mutable Pai

Parameter Passing Variations

```
(check-equal? (eval "if zero?(1) then 1 else 2")
               (num-val 2))
(check-equal? (eval "-(15, 10)")
               (num-val 5))
(check-equal?
  (eval "let x = 10 in if zero?(-(x, x)) then x else 2")
  (num-val 10))
(check-equal? (eval "let decr = proc (a) -(a, 1) in (decr 30)")
               (num-val 29))
(check-equal? (eval "( proc (g) (g 30) proc (y) -(y, 1))")
               (num-val 29))
(check-equal? (eval "let x = 200
                      in let f = proc(z) - (z, x)
                         in let x = 100
                            in let g = proc(z) - (z, x)
                               in -((f 1), (g 1))")
               (n_{11}m-val -100))
```

Language with Implicit References

Mutable Pairs

Parameter Passing Variations

State

```
(check-equal?
    (eval "let sum = proc (x) proc (y) -(x, -(0, y)) in ((sum 3) 4)")
    (num-val 7))
  (check-equal?
    (eval "let sum = proc (x) proc (y) -(x, -(0, y))
           in letrec sigma (n) = if zero?(n)
                                  then 0
                                  else ((sum n) (sigma -(n, 1)))
              in (sigma 5)")
    (num-val 15))
  (check-equal? (eval "letrec even(n) = if zero?(n)
                                         then zero?(n)
                                         else if zero?(-(n, 1))
                                              then zero?(n)
                                              else (even -(n, 2))
                       in (even 501)")
                (bool-val #f))
```

Language with Implicit References

State

```
• (check-equal? (eval "let a = 3
                        in let p = proc(x) set x = 4
                           in begin
                                (p a);
                              end")
                (num-val 3))
  (check-equal? (eval "let x = 0
                        in letrec f (x) = set x = +(x, 1)
                                  g(a) = set x = +(x, 2)
                           in begin
                                (f x);
                                (g x);
                                x
                              end")
                (num-val 2))
```

State

Language wit Explicit References

Language with Implicit References

Mutable Pair

Paramete Passing Variations

State

```
• (define (value-of exp env)
    (cases expression exp
      (const-exp (num) (num-val num))
      (true-exp () (bool-val #t))
      (false-exp () (bool-val #f))
      (var-exp (var) (deref (apply-env env var)))
      (diff-exp (exp1 exp2)
                 (let ((num1 (expval2num (value-of exp1 env)))
                       (num2 (expval2num (value-of exp2 env))))
                   (num-val (- num1 num2))))
      (zero?-exp (exp1)
                  (let ((val1 (expval2num (value-of exp1 env))))
                    (if (zero? val1)
                        (bool-val #t)
                        (bool-val #f))))
```

Ctata

Language wi Explicit References

Language with Implicit References

Mutable Pai

Parameter Passing Variations

State

```
(if-exp (exp1 exp2 exp3)
    (let ((val1 (value-of exp1 env)))
      (if (expval2bool val1)
          (value-of exp2 env)
          (value-of exp3 env))))
(let-exp (vars exps body)
         (let [(vals (map (lambda (e) (value-of e env)) exps))]
          (value-of body
                    (foldr (lambda (var val acc)
                            (extend-env var (newref val) acc))
                           env
                           vars
                           vals))))
(proc-exp (params body)
          (proc-val (procedure params body (vector env))))
(call-exp (rator rands)
          (let [(proc (expval2proc (value-of rator env)))
                (args (map (lambda (rand) (value-of rand env))
            (apply-procedure proc args)))
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```

Language with Implicit References

Mutable Pair

Parameter Passing

State

CLLL

Language wi Explicit References

Language with Implicit References

Mutable Pairs

Parameter Passing Variations

State

```
    (define (mk-letrec-env names params bodies env)

    (let* [(temp-proc-vals
             (map (lambda (p b)
                     (proc-val (procedure p b (vector (empty-env)))))
                   params
                   bodies))
           (new-env (foldl (lambda (name proc env)
                              (extend-env name
                                           (newref proc)
                                           env))
                            env
                            names
                            temp-proc-vals))]
      (begin
        (for-each (lambda (p)
                     (cases proc p
                       (procedure (p b ve)
                                   (vector-set! ve 0 new-env))))
                   (map (lambda (p) (expval2proc p))
                        temp-proc-vals))
        new-env)))
```

State

Language with Explicit References

Language with Implicit References

Mutable Pair

Paramete Passing Variations

State

Language with Explicit

Language wit Implicit References

Mutable Pairs

Parameter Passing • We will add mutable pairs to IMPLICIT-REFS



State

Language with Explicit

Language wit Implicit References

Mutable Pairs

Parameter Passing

- We will add mutable pairs to IMPLICIT-REFS
- expval = int + bool + proc + mutpair
- mutpair = ref(expval) x ref(expval)

State

Language w Explicit References

Language wir Implicit References

Mutable Pairs

Parameter Passing

- We will add mutable pairs to IMPLICIT-REFS
- expval = int + bool + proc + mutpair
- mutpair = ref(expval) x ref(expval)
- DenVal = ref(expval)

State

Language wi Explicit References

Language wit Implicit References

Mutable Pairs

Parameter Passing Variations

- We will add mutable pairs to IMPLICIT-REFS
- expval = int + bool + proc + mutpair
- mutpair = ref(expval) x ref(expval)
- DenVal = ref(expval)
- Specification
 - \rightarrow newpair: expval expval \rightarrow mutpair
 - \rightarrow left: mutpair \rightarrow expval
 - \rightarrow right: mutpair \rightarrow expval
 - ightarrow setleft: mutpair expval ightarrow
 - ightarrow setright: mutpair expval ightarrow

State

Language wit Explicit References

Language wit Implicit References

Mutable Pairs

Paramete Passing Variations

- We will add mutable pairs to IMPLICIT-REFS
- expval = int + bool + proc + mutpair
- mutpair = ref(expval) x ref(expval)
- DenVal = ref(expval)
- Specification
 - ightarrow newpair: expval expval ightarrow mutpair
 - \rightarrow left: mutpair \rightarrow expval
 - ightarrow right: mutpair ightarrow expval
 - \rightarrow setleft: mutpair expval $\rightarrow \varnothing$
 - \rightarrow setright: mutpair expval $\rightarrow \varnothing$
- (define-datatype expval expval?

```
(num-val
  (value number?))
(bool-val
  (boolean boolean?))
(proc-val
  (proc proc?))
(mutpair-val ;; new for mutable pairs
   (p mutpair?)))
```

State

Language w Explicit References

Language wit Implicit References

Mutable Pairs

Parameter Passing Variations

Grammar

- \rightarrow (expression ("newpair" "(" expression "," expression ")") newpair-exp)
- \rightarrow (expression ("left" "(" expression ")") left-exp)
- ightarrow (expression ("setleft" expression "=" expression) setleft-exp)
- → (expression ("right" "(" expression ")") right-exp)
- → (expression ("setright" expression "=" expression) setright-exp)

State

Explicit
References

Language wit Implicit References

Mutable Pairs

Parameter Passing • Let's trace

```
(eval "let p = newpair(4, 5)
    in begin
        setleft p = 15;
        setright p = 15;
        -(left(p), right(p))
        end")
```

State

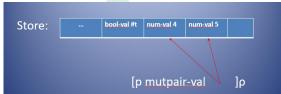
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Mutable Pairs

Parameter Passing · Let's trace

```
(eval "let p = newpair(4, 5)
    in begin
        setleft p = 15;
        setright p = 15;
        -(left(p), right(p))
        end")
```



Stata

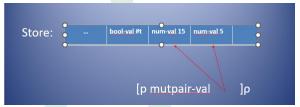
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Mutable Pairs

Parameter Passing · Let's trace

```
(eval "let p = newpair(4, 5)
    in begin
        setleft p = 15;
        setright p = 15;
        -(left(p), right(p))
        end")
```



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Language wi Explicit References

Language wit Implicit References

Mutable Pairs

Parameter Passing Let's trace

```
(eval "let p = newpair(4, 5)
    in begin
        setleft p = 15;
        setright p = 15;
        -(left(p), right(p))
        end")
```



• Returns (num-val 0)

Chaha

Language with Explicit
References

Language wit Implicit References

Mutable Pairs

Parameter Passing • How can we represent a mutable pair?



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References

Language wit Implicit References

Mutable Pairs

Parameter Passing

- How can we represent a mutable pair?
- (define-datatype mutpair mutpair? (a-pair (left-loc reference?) (right-loc reference?)))
- Is this a good implementation choice?

State

Language wit Explicit References

Implicit
References

Mutable Pairs

Parameter Passing Variations

- How can we represent a mutable pair?
- (define-datatype mutpair mutpair? (a-pair (left-loc reference?) (right-loc reference?)))
- Is this a good implementation choice?
- Does not take into account everything we know about mutable pairs
 - ightarrow The two locations are independently assignable
 - $\rightarrow \ \mathsf{Not} \ \mathsf{independently} \ \mathsf{allocated}$

State

Language wit Explicit References

Implicit
References

Mutable Pairs

Parameter Passing Variations • How can we represent a mutable pair?

```
• (define-datatype mutpair mutpair?
(a-pair (left-loc reference?)
(right-loc reference?)))
```

- Is this a good implementation choice?
- Does not take into account everything we know about mutable pairs
 - ightarrow The two locations are independently assignable
 - → Not independently allocated
- Consider newpair(4, 5) and σ

$$\sigma = (\ldots)$$
 $\sigma = (\ldots 4)$

$$\sigma$$
 = (... 4 5)

State

Language wit Explicit References

Implicit
References

Mutable Pairs

Parameter Passing Variations • How can we represent a mutable pair?

```
• (define-datatype mutpair mutpair?
(a-pair (left-loc reference?)
(right-loc reference?)))
```

- Is this a good implementation choice?
- Does not take into account everything we know about mutable pairs
 - ightarrow The two locations are independently assignable
 - ightarrow Not independently allocated
- Consider newpair(4, 5) and σ

$$\sigma = (...)
\sigma = (... 4)
\sigma = (... 4 5)$$

• If the left is in position p in σ , where is the right?

State

Language wit Explicit References

Language wit Implicit References

Mutable Pairs

Parameter Passing Variations • How can we represent a mutable pair?

```
• (define-datatype mutpair mutpair?
(a-pair (left-loc reference?)
(right-loc reference?)))
```

- Is this a good implementation choice?
- Does not take into account everything we know about mutable pairs
 - ightarrow The two locations are independently assignable
 - ightarrow Not independently allocated
- Consider newpair(4, 5) and σ

$$\sigma = (...)
\sigma = (... 4)
\sigma = (... 4 5)$$

- If the left is in position p in σ , where is the right?
- What does this tell you?

State

Language wit Explicit References

Language wit Implicit References

Mutable Pairs

Parameter Passing Variations • How can we represent a mutable pair?

```
• (define-datatype mutpair mutpair?
(a-pair (left-loc reference?)
(right-loc reference?)))
```

- Is this a good implementation choice?
- Does not take into account everything we know about mutable pairs
 - ightarrow The two locations are independently assignable
 - → Not independently allocated
- Consider newpair(4, 5) and σ

$$\sigma = (...)
\sigma = (... 4)
\sigma = (... 4 5)$$

- If the left is in position p in σ , where is the right?
- What does this tell you?
- We can implement mutable pairs using a single reference

Part IV: State

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Language wit Explicit References

Language wir Implicit References

Mutable Pairs

Parameter Passing

Part IV: State

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Mutable Pairs

Parameter Passing

```
• ;; expval --> reference throws error
(define (expval->mutpair v)
  (cases expval v
        (mutpair-val (ref) ref)
        (else (expval-extractor-error 'mutable-pair v))))
```

```
• ;; mutpair? : X -> Boolean (define (mutpair? v) (reference? v))
```

State

Language wir Explicit References

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References

Mutable Pairs

Parameter Passing Variations

```
;; expval --> reference throws error
(define (expval->mutpair v)
   (cases expval v
        (mutpair-val (ref) ref)
        (else (expval-extractor-error 'mutable-pair v))))
;; mutpair? : X -> Boolean
(define (mutpair? v) (reference? v))
;; make-pair : expval expval -> mutpair
```

(define (make-pair val1 val2)
 (let ((ref1 (newref val1)))

ref1)))

(let ((ref2 (newref val2)))

State

Language wit Explicit References

Language wit Implicit References

Mutable Pairs

Parameter Passing Variations

```
• ;; expval --> reference throws error
  (define (expval->mutpair v)
    (cases expval v
      (mutpair-val (ref) ref)
      (else (expval-extractor-error 'mutable-pair v))))
• ;; mutpair? : X -> Boolean
  (define (mutpair? v) (reference? v))
;; make-pair : expval expval -> mutpair
  (define (make-pair val1 val2)
    (let ((ref1 (newref val1)))
      (let ((ref2 (newref val2)))
        ref1)))
;; left : mutpair -> expval
  (define (left p) (deref p))
  ;; right : mutpair -> expval
  (define (right p) (deref (+ 1 p)))
```

State

Language wit Explicit References

Language wit Implicit References

Mutable Pairs

Parameter Passing Variations

```
• ;; expval --> reference throws error
  (define (expval->mutpair v)
    (cases expval v
      (mutpair-val (ref) ref)
      (else (expval-extractor-error 'mutable-pair v))))
• ;; mutpair? : X -> Boolean
  (define (mutpair? v) (reference? v))
;; make-pair : expval expval -> mutpair
  (define (make-pair val1 val2)
    (let ((ref1 (newref val1)))
      (let ((ref2 (newref val2)))
        ref1)))
• ;; left : mutpair -> expval
  (define (left p) (deref p))
  ;; right : mutpair -> expval
  (define (right p) (deref (+ 1 p)))
• ;; setleft : mutpair expval -> Unspecified
  (define (setleft p val) (setref! p val))
  ;; setright : mutpair expval -> Unspecified
  (define (setright p val) (setref! (+ 1 p) val))
```

State

Language with Explicit References

Language wit Implicit References

Mutable Pairs

Parameter Passing Variations

```
(check-equal? (eval "let p = newpair(4, 5)
                     in left(p)")
              (num-val 4))
(check-equal? (eval "let p = newpair(4, 5)
                     in right(p)")
              (num-val 5))
(check-equal? (eval "let p = newpair(4, 5)
                     in begin
                          setleft p = 15;
                          setright p = 15;
                          -(left(p), right(p))
                        end")
              (num-val 0))
```

Part IV: State

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Language wi Implicit References

Mutable Pairs

Parameter Passing

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Language wit Implicit References

Mutable Pairs

Paramete Passing

```
    (define (value-of exp env)

    (cases expression exp
      (newpair-exp (exp1 exp2)
        (let ((v1 (value-of exp1 env))
              (v2 (value-of exp2 env)))
          (mutpair-val (make-pair v1 v2))))
      (left-exp (exp1)
        (let ((v1 (value-of exp1 env)))
          (let ((p1 (expval->mutpair v1)))
            (left p1))))
      (right-exp (exp1)
        (let ((v1 (value-of exp1 env)))
          (let ((p1 (expval->mutpair v1)))
            (right p1))))
```

```
• (define (value-of exp env)
Part IV: State
                     (cases expression exp
 Marco T
  Morazán
                       (newpair-exp (exp1 exp2)
                         (let ((v1 (value-of exp1 env))
                                (v2 (value-of exp2 env)))
                           (mutpair-val (make-pair v1 v2))))
                       (left-exp (exp1)
                         (let ((v1 (value-of exp1 env)))
                           (let ((p1 (expval->mutpair v1)))
                              (left p1))))
Mutable Pairs
                       (right-exp (exp1)
                         (let ((v1 (value-of exp1 env)))
                           (let ((p1 (expval->mutpair v1)))
                              (right p1))))
                       (setleft-exp (exp1 exp2)
                         (let ((v1 (value-of exp1 env))
                                (v2 (value-of exp2 env)))
                           (let ((p (expval->mutpair v1)))
                              (begin (setleft p v2)
                                     (num-val 82))))) :: this is a don't care value.
                       (setright-exp (exp1 exp2)
                         (let ((v1 (value-of exp1 env))
                                (v2 (value-of exp2 env)))
                           (let ((p (expval->mutpair v1)))
                              (begin (setright p v2)
                                     (num-val 83)))));; this is a don't care value.
```

Part IV: State

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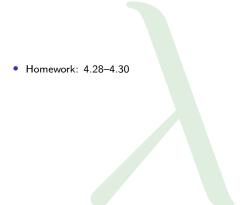
State

Language with Explicit
References

Language wit Implicit References

Mutable Pairs

Parameter Passing



State

Language with Explicit References

Language wit Implicit References

Mutable Pairs

Parameter Passing Variations

Parameter Passing Variations

- In call-by-value semantics the callee is isolated from the caller
- Assignments by the callee to its parameters can not be seen by the caller

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- In call-by-value semantics the callee is isolated from the caller
- Assignments by the callee to its parameters can not be seen by the caller
- Sometimes it is desirable to pass in variables expecting the callee to make assignments to them
- This can be done by passing references to the callee instead of actual values
- This is known as call-by-reference

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations Call by Reference

- In call-by-value semantics the callee is isolated from the caller
- Assignments by the callee to its parameters can not be seen by the caller
- Sometimes it is desirable to pass in variables expecting the callee to make assignments to them
- This can be done by passing references to the callee instead of actual values
- This is known as call-by-reference
- If an operand is a variable, then a reference to the variable's location is passed
- The formal parameter is bound to this location

Mutable Pair

Parameter Passing Variations

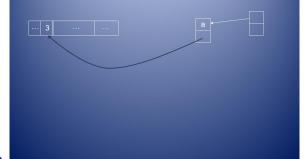
Parameter Passing Variations Call by Reference

- In call-by-value semantics the callee is isolated from the caller
- Assignments by the callee to its parameters can not be seen by the caller
- Sometimes it is desirable to pass in variables expecting the callee to make assignments to them
- This can be done by passing references to the callee instead of actual values
- This is known as call-by-reference
- If an operand is a variable, then a reference to the variable's location is passed
- The formal parameter is bound to this location
- If the operand is some other type of expression, then the formal parameter is bound to a new location containing the value of the operand
- Just like in call-by-value

Mutable Pair

Parameter Passing Variations

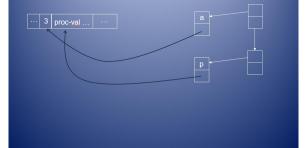
Parameter Passing Variations



Mutable Pair

Parameter Passing Variations

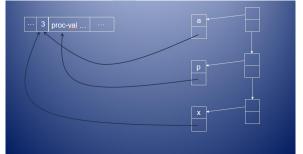
Parameter Passing Variations



Mutable Pair

Parameter Passing Variations

Parameter Passing Variations



Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

Call by Reference

```
let a = 3
p = proc(x) set x = 4
in begin
    (p a);
    a
   end
               proc-val ... ···
```

Returns 4

Mutable Pai

Parameter Passing Variations

Parameter Passing Variations

- Why use call-by-reference?
 - → Return multiple values (by making assignments to parameters)
 - → Implementation of common operations

c. .

Explicit
References

Language wit Implicit References

Mutable Pairs

Parameter Passing Variations

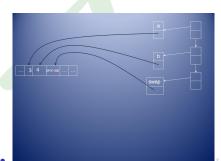
Parameter Passing Variations

Call by Reference

Call-by-Value

end

```
let a = 3
    b = 4
    swap = proc (x, y)
    let temp = x
    in begin
        set x = y
        set y = temp
    end
in begin
    swap(a b)
    -(a, b)
```



Mutable Pair

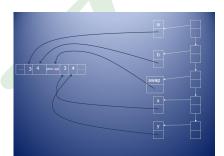
Parameter Passing Variations

Parameter Passing Variations

Call by Reference

Call-by-Value

```
let a = 3
   b = 4
   swap = proc (x, y)
      let temp = x
      in begin
        set x = y
        set y = temp
   end
in begin
   swap(a b)
   -(a, b)
   end
```



Charles

Explicit
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Language wit Implicit References

Mutable Pairs

Parameter Passing Variations

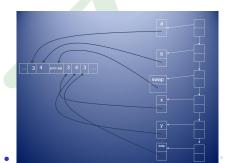
Parameter Passing Variations

Call by Reference

Call-by-Value

end

```
let a = 3
    b = 4
    swap = proc (x, y)
    let temp = x
    in begin
        set x = y
        set y = temp
    end
in begin
    swap(a b)
    -(a, b)
```



Cara

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References

Language wit Implicit References

Mutable Pairs

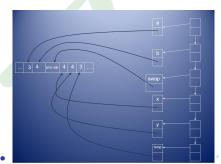
Parameter Passing Variations

Parameter Passing Variations

Call by Reference

Call-by-Value

```
let a = 3
  b = 4
  swap = proc (x, y)
    let temp = x
    in begin
        set x = y
        set y = temp
    end
in begin
    swap(a b)
    -(a, b)
  end
```



Charles

Explicit
References

Language with Implicit

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

Call by Reference

Call-by-Value

end

```
let a = 3
   b = 4
   swap = proc (x, y)
    let temp = x
   in begin
        set x = y
        set y = temp
   end
in begin
   swap(a b)
   -(a, b)
```

Returns -1



Language wit Implicit

Mutable Pairs

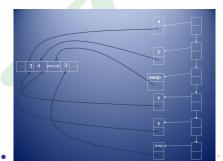
Parameter Passing Variations

Parameter Passing Variations

Call by Reference

Call-by-Reference

```
let a = 3
    b = 4
    swap = proc (x, y)
        let temp = x
        in begin
        set x = y
        set y = temp
    end
in begin
    swap(a b)
    -(a, b)
end
```



Explicit
References

Language wit Implicit References

Mutable Pairs

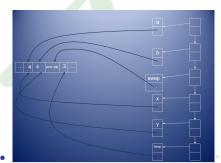
Parameter Passing Variations

Parameter Passing Variations

Call by Reference

Call-by-Reference

```
let a = 3
  b = 4
  swap = proc (x, y)
  let temp = x
  in begin
      set x = y
      set y = temp
  end
in begin
  swap(a b)
  -(a, b)
  end
```



Language with Implicit References

Mutable Pairs

Parameter Passing Variations

Parameter Passing Variations

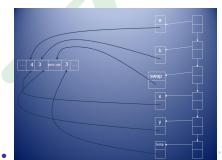
Call by Reference

Call-by-Reference

end

```
let a = 3
   b = 4
   swap = proc (x, y)
     let temp = x
     in begin
        set x = y
        set y = temp
   end
in begin
     swap(a b)
   -(a, b)
```

Returns 1



Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- Only change is for when new references are created:
 - ightarrow call-by-value: a new reference is created for every operand evaluated
 - ightarrow call-by-reference: a new reference is created for evaluation of an operand other than a variable
- Under call-by-reference we need a new location for some operands and not for others

Ctata

Language wit Explicit References

Language wit Implicit References

Mutable Pain

Parameter Passing Variations

Parameter Passing Variations

```
Part IV: State
```

c. .

Explicit
References

Language wit

Mutable Daim

Parameter Passing Variations

Parameter Passing Variations

;; apply-procedure : proc (listof expval) -> expval

```
(define (apply-procedure f vals)
    (cases proc f
      (procedure (params body envv)
        (let [(saved-env (vector-ref envv 0))]
          (value-of body
            (foldr (lambda (binding acc)
                     (extend-env (car binding)
                                 (newref (cadr binding))
                                 acc))
                   saved-env
                   (map (lambda (p v) (list p v)) params vals))))))
  Can't always allocate an argument in the store
• ;; apply-procedure : proc (listof ref) -> expval
  (define (apply-procedure f vals)
   (cases proc f
    (procedure (params body envv)
     (let [(saved-env (vector-ref envv 0))]
      (value-of body
               (foldr (lambda (binding acc)
                       (extend-env (car binding) (cadr binding) acc))
                       saved-env
                       (map (lambda (p v) (list p v)) params vals))))
  Decision made in the evaluation of a call-ern
```

State

Language wit Explicit References

Language with Implicit References

Mutable Pairs

Parameter Passing Variations

Parameter Passing Variations

Call by Reference

In value-of

```
apply-procedure must be called with a (listof ref)
```

Ctata

Language wit Explicit References

Language with Implicit References

Mutable Pairs

Parameter Passing Variations

Parameter Passing Variations

Call by Reference

apply-procedure must be called with a (listof ref)

(call-exp (rator rands) (let [(proc (expval2proc (value-of rator env)))

value-of-rand returns a reference

State

Language wit Explicit References

Language witl Implicit References

Mutable Pairs

Parameter Passing Variations

Parameter Passing Variations

```
    In value-of

  (call-exp (rator rands)
    (let [(proc (expval2proc (value-of rator env)))
          (args (map (lambda (rand) (value-of rand env)) rands))]
      (apply-procedure proc args)))
  apply-procedure must be called with a (listof ref)
• (call-exp (rator rands)
    (let [(proc (expval2proc (value-of rator env)))
          (args (map (lambda (rand) (value-of-rand rand env)) rands))
      (apply-procedure proc args)))
  value-of-rand returns a reference
• ;; value-of-rand : expression environment -> Ref
  ;; Purpose: For a var-exp return existing reference.
              Otherwise, return reference to a new cell.
  (define (value-of-rand exp env)
    (cases expression exp
      (var-exp (var) (apply-env env var))
      (else (newref (value-of exp env)))))
```

Cana

Language wi Explicit References

Language wit Implicit References

Mutable Pain

Parameter Passing Variations

Parameter Passing Variations

```
(check-equal? (eval "let a = 3
                     in let p = proc(x) set x = 4
                        in begin (p a); a end")
              (num-val 4))
(check-equal? (eval "let x = 0
                     in letrec f (x) = set x = +(x, 1)
                                g(a) = set x = +(x, 2)
                        in begin (f x);
                                  (g x);
                                  х
                           end")
              (num-val 3))
(check-equal?
 (eval "let swap = proc (a)
                    proc (b)
                      let t = a
                      in begin set a = b; set b = t
        in let a = 33
           in let b = 44
              in begin ((swap a) b);
                       -(a, b)
                 end")
 (num-val 11))
```

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- Call-by-value and call-by-reference are eager
- Always find the value of each operand

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- Call-by-value and call-by-reference are eager
- Always find the value of each operand
- Lazy evaluation
- Operands not evaluated until needed
- ullet Never needed ightarrow never evaluated

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- Call-by-value and call-by-reference are eager
- Always find the value of each operand
- Lazy evaluation
- Operands not evaluated until needed
- Never needed \rightarrow never evaluated
- Is this useful?

State

Explicit
References

Language with Implicit References

Mutable Pair:

Parameter Passing Variations

Parameter Passing Variations

- letrec compute-ints-from-n (n) = (compute-ints-from-n +(n, 1))
 in let f = proc (k) 42
 in (f (compute-ints-from-n 100))
- What should this program return?

State

Language wit Explicit References

Language with Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- letrec compute-ints-from-n (n) = (compute-ints-from-n +(n, 1))
 in let f = proc (k) 42
 in (f (compute-ints-from-n 100))
- What should this program return?
- It should return 42, but does not. Why?

State

Language wit Explicit References

Language with Implicit References

Mutable Pairs

Parameter Passing Variations

Parameter Passing Variations

- letrec compute-ints-from-n (n) = (compute-ints-from-n +(n, 1))
 in let f = proc (k) 42
 in (f (compute-ints-from-n 100))
- What should this program return?
- It should return 42, but does not. Why?
- Under lazy evaluation this program returns 42

Ctata

Language wit Explicit References

Language with Implicit References

Mutable Pain

Parameter Passing Variations

Parameter Passing Variations

Lazy Evaluation: Call by Name

```
• letrec compute-ints-from-n (n) = (compute-ints-from-n +(n, 1))
in let f = proc (k) 42
in (f (compute-ints-from-n 100))
```

- What should this program return?
- It should return 42, but does not. Why?
- Under lazy evaluation this program returns 42
- #lang eopl
 (require rackunit "../eopl-extras.rkt")

(check-equal?

(first-n-natnums 15)

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

```
#lang eopl
  (require rackunit "../eopl-extras.rkt")
  :: natnum --> natnum
  ;; Purpose: Return the kth Fibonacci number
  (define (fib k)
    (if (< k 2)
        (+ (fib (- k 1)) (fib (- k 2)))))
  (define (the-fibs n) (stream-cons (fib n) (the-fibs (+ n 1))))
  (define fibs (the-fibs 0))
  (define (nth-fib n) (stream-ref fibs n))
  (check-equal? (nth-fib 5) 8)
  (check-equal?
                 (nth-fib 10) 89)
```

Mutable Pai

Parameter Passing Variations

Parameter Passing Variations

```
#lang eopl
  (require rackunit "../eopl-extras.rkt")
  :: natnum --> natnum
  ;; Purpose: Return the kth Fibonacci number
  (define (fib k)
    (if (< k 2))
        (+ (fib (- k 1)) (fib (- k 2)))))
  (define (the-fibs n) (stream-cons (fib n) (the-fibs (+ n 1))))
  (define fibs (the-fibs 0))
  (define (nth-fib n) (stream-ref fibs n))
  (check-equal? (nth-fib 5) 8)
  (check-equal? (nth-fib 10) 89)
• (define the-doubles (stream-map (\lambda (n) (* 2 n)) natnums))
  (check-equal? (stream-ref the-doubles 10) 20)
  (check-equal? (stream-ref the-doubles 1287) 2574)
```

Mutable Pai

Parameter Passing Variations

Parameter Passing Variations

Lazy Evaluation: Call by Name

An operand is not evaluated until needed

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- An operand is not evaluated until needed
- A bound var is associated with unevaluated expression (frozen)

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- An operand is not evaluated until needed
- A bound var is associated with unevaluated expression (frozen)
- When the value of the bound var is needed, then the expression is evaluated (thawed)

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- An operand is not evaluated until needed
- A bound var is associated with unevaluated expression (frozen)
- When the value of the bound var is needed, then the expression is evaluated (thawed)
- What does this require?

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- An operand is not evaluated until needed
- A bound var is associated with unevaluated expression (frozen)
- When the value of the bound var is needed, then the expression is evaluated (thawed)
- What does this require?
- The env that exists when the expr is frozen

State

Language with Explicit References

Language with Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- An operand is not evaluated until needed
- A bound var is associated with unevaluated expression (frozen)
- When the value of the bound var is needed, then the expression is evaluated (thawed)
- What does this require?
- The env that exists when the expr is frozen
- (define-datatype thunk thunk? (a-thunk (exp1 expression?)
 (env environment?))
- The expr in a thunk is evaluated when a proc needs the value of bound var

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- Language
 - $\rightarrow \ \text{let remains eager}$
 - ightarrow lazy evaluation of arguments
 - \rightarrow effects

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- Language
 - \rightarrow let remains eager
 - ightarrow lazy evaluation of arguments
 - → effects
- Values
 - \rightarrow expval = int + bool + proc
 - \rightarrow denval = ref(expval + thunk)

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- Language
 - \rightarrow let remains eager
 - ightarrow lazy evaluation of arguments
 - \rightarrow effects
- Values
 - \rightarrow expval = int + bool + proc
 - \rightarrow denval = ref(expval + thunk)
- New allocations policy
 - → var: pass its denotation (which is a reference; same as call-by-reference)
 - → not var: pass a ref to a new location storing a thunk for the unevaluated arg

Canada

Language with Explicit

Language wit Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

```
• ;; value-of-rand : expression environment -> Ref
;; Purpose: if the expression is a var-exp, then return the reference; otherwise, return a thunk for the given expression.

(define (value-of-rand exp env)

(cases expression exp

(var-exp (var) (apply-env env var))

(else

(newref (a-thunk exp env))))) ← not a var-exp create thunk
```

Ctata

Language with Explicit References

Language wit Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

Lazy Evaluation: Call by Name

• How do you evaluate a var-expr?

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- How do you evaluate a var-expr?
- $\frac{w = deref(\rho(v))}{(value-of (var-expv) \rho) = if (expval? w) then w else (value-of-thunk w)}$

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- How do you evaluate a var-expr?
- $\frac{w = deref(\rho(v))}{(value-of (var-expv) \rho) = if (expval? w) then w else (value-of-thunk w)}$
- change to value-of

```
(var-exp (var)
  (let ((ref1 (apply-env env var)))
    (let ((w (deref ref1)))
        (if (expval? w)
        w
  (value-of-thunk w))))
```

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- Evaluating a thunk

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

Lazy Evaluation: Call by Name

Consider

```
let g = let counter = 10
            in proc (d) *(2, counter)
in (proc (x) +(x, x) (g 0))
```

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

Lazy Evaluation: Call by Name

Consider

• x is the thunk for (g 0)

Parameter Passing

Variations

Parameter Passing Variations

Lazy Evaluation: Call by Name

Consider

```
let g = let counter = 10
            in proc (d) *(2, counter)
in (proc (x) + (x, x) (g 0))
```

- x is the thunk for (g 0)
- the first x forces the evaluation of the thunk \rightarrow 20

Passing

Parameter Variations

Parameter Passing Variations

Lazy Evaluation: Call by Name

Consider

```
let g = let counter = 10
            in proc (d) *(2, counter)
in (proc (x) + (x, x) (g 0))
```

- x is the thunk for (g 0)
- the first x forces the evaluation of the thunk $\rightarrow 20$
- the second x forces the evaluation of the thunk → 20
- returns 40

Mutable Pai

Parameter Passing Variations

Parameter Passing Variations

Lazy Evaluation: Call by Need

Evaluating the same thunk seems wasteful

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- Evaluating the same thunk seems wasteful
- Solution: Evaluate it once and mutate it for its value

Language wit Implicit

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- Evaluating the same thunk seems wasteful
- Solution: Evaluate it once and mutate it for its value
- Change in value-of

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

```
• let g = let counter = 10
in proc (d) *(2, counter)
in (proc (x) +(x, x) (g 0))
```

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

Lazy Evaluation: Call by Need

• x is the thunk for (g 0)

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- x is the thunk for (g 0)
- the first x forces the evaluation of the thunk to 20
- mutates x to 20

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- x is the thunk for (g 0)
- the first x forces the evaluation of the thunk to 20
- mutates x to 20
- the second x (simply) returns its value of 20
- returns 40

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Explicit
References

Language wit Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

Lazy Evaluation: Call by Need

 In the absence of side-effects, call-by-name and call-by-need always yield the same answer

State

Explicit
References

Language wit Implicit References

Mutable Pai

Parameter Passing Variations

Parameter Passing Variations

- In the absence of side-effects, call-by-name and call-by-need always yield the same answer
- In the presence of side-effects, it is easy to distinguish them

State

Language wit Explicit References

Language wit Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- In the absence of side-effects, call-by-name and call-by-need always yield the same answer
- In the presence of side-effects, it is easy to distinguish them

```
let g = let count = 0
    in proc (d)
    begin
        set count = -(count, -1);
        count
    end
in (proc (x) +(x, x) (g 0) )
```

State

Language with Explicit References

Language with Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- In the absence of side-effects, call-by-name and call-by-need always yield the same answer
- In the presence of side-effects, it is easy to distinguish them

- g returns the number of times it is called
- Thunk for (g 0) is passed as the argument to the function in the body of the let

State

Language with Explicit References

Language witl Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- In the absence of side-effects, call-by-name and call-by-need always yield the same answer
- In the presence of side-effects, it is easy to distinguish them

- g returns the number of times it is called
- Thunk for (g 0) is passed as the argument to the function in the body of the let
- call-by-name

State

Language with Explicit References

Language with Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- In the absence of side-effects, call-by-name and call-by-need always yield the same answer
- In the presence of side-effects, it is easy to distinguish them

- g returns the number of times it is called
- Thunk for (g 0) is passed as the argument to the function in the body of the let
- call-by-name
- the first reference to x: sets count to 1 & returns 1 as the value of (g 0)

State

Language with Explicit References

Language witl Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- In the absence of side-effects, call-by-name and call-by-need always yield the same answer
- In the presence of side-effects, it is easy to distinguish them

- g returns the number of times it is called
- Thunk for (g 0) is passed as the argument to the function in the body of the let
- call-by-name
- the first reference to x: sets count to 1 & returns 1 as the value of (g 0)
- the second reference to x: sets count to 2 & returns 2 as the value of (g 0)

State

Language with Explicit References

Language witl Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- In the absence of side-effects, call-by-name and call-by-need always yield the same answer
- In the presence of side-effects, it is easy to distinguish them

- g returns the number of times it is called
- Thunk for (g 0) is passed as the argument to the function in the body of the let
- call-by-name
- the first reference to x: sets count to 1 & returns 1 as the value of (g 0)
- the second reference to x: sets count to 2 & returns 2 as the value of (g 0)
- +(1, 2) = 3

State

Language with Explicit References

Language wit Implicit References

Mutable Pail

Parameter Passing Variations

Parameter Passing Variations

- In the absence of side-effects, call-by-name and call-by-need always yield the same answer
- In the presence of side-effects, it is easy to distinguish them

- g returns the number of times it is called
- Thunk for (g 0) is passed as the argument to the function in the body of the let
- call-by-name
- the first reference to x: sets count to 1 & returns 1 as the value of (g 0)
- the second reference to x: sets count to 2 & returns 2 as the value of (g 0)
- +(1, 2) = 3
- call-by-need

State

Language with Explicit References

Language wit Implicit References

Mutable Pan

Parameter Passing Variations

Parameter Passing Variations

- In the absence of side-effects, call-by-name and call-by-need always yield the same answer
- In the presence of side-effects, it is easy to distinguish them

- g returns the number of times it is called
- Thunk for (g 0) is passed as the argument to the function in the body of the let
- call-by-name
- the first reference to x: sets count to 1 & returns 1 as the value of (g 0)
- the second reference to x: sets count to 2 & returns 2 as the value of (g 0)
- +(1, 2) = 3
- call-by-need
- the first reference to x forces: sets count to 1, returns 1 as the value of (g
 0), and stores 1 as the value of (g
 0)

State

Language with Explicit References

Language wit Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- In the absence of side-effects, call-by-name and call-by-need always yield the same answer
- In the presence of side-effects, it is easy to distinguish them

- g returns the number of times it is called
- Thunk for (g 0) is passed as the argument to the function in the body of the let
- call-by-name
- the first reference to x: sets count to 1 & returns 1 as the value of (g 0)
- the second reference to x: sets count to 2 & returns 2 as the value of (g 0)
- +(1, 2) = 3
- call-by-need
- the first reference to x forces: sets count to 1, returns 1 as the value of (g
 0), and stores 1 as the value of (g
 0)
- second reference to x: returns the stored 1

Part IV: State

Marco T Morazán

Parameter Passing Variations

Parameter Passing Variations

- In the absence of side-effects, call-by-name and call-by-need always yield the same answer
- In the presence of side-effects, it is easy to distinguish them

```
• let g = let count = 0
          in proc (d)
           begin
                  set count = -(count, -1);
                  count
         end
  in (proc (x) + (x, x) (g 0))
```

- g returns the number of times it is called
- Thunk for (g 0) is passed as the argument to the function in the body of the let
- call-by-name
- the first reference to x: sets count to 1 & returns 1 as the value of (g 0)
- the second reference to x: sets count to 2 & returns 2 as the value of (g 0)
- +(1, 2) = 3
- call-by-need
- the first reference to x forces: sets count to 1, returns 1 as the value of (g 0), and stores 1 as the value of (g 0)
- second reference to x: returns the stored 1
- +(1, 1) = 2



Mutable Pair

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- The effect of a procedure call is modeled by:
 - ightarrow Replacing the call with the body of the procedure
 - $\rightarrow\,$ Every reference to a parameter in the body is replaced by the corresponding operand
 - ightarrow This evaluation strategy is the basis of the lambda calculus and is known as eta-reduction

Implicit
References

Mutable Pair

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- Lazy evaluation: in the absence of side-effects allows for a simple way to reason about programs
- The effect of a procedure call is modeled by:
 - \rightarrow Replacing the call with the body of the procedure
 - ightarrow Every reference to a parameter in the body is replaced by the corresponding operand
 - ightarrow This evaluation strategy is the basis of the lambda calculus and is known as eta-reduction
- β -reduction: $\lambda(x.e)x0 \rightarrow e\{x0/x\}$

```
\lambda(x.+(x, *(2, x)) - (5, -10))

\rightarrow +(-(5, -10) *(2, -(5, -10)))

\rightarrow +(15, *(2, -(5, -10)))

\rightarrow +(15, *(2, 15))

\rightarrow +(15, 30)

\rightarrow 45
```

Mutable Pairs

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- You do not have to think operationally: you can reason equationally about your programs.—S. Doaitse Swierstra
- I prefer call by value to call by name because it is more predictable.—Mitchell Wand
- Popular with pure functional languages (i.e. with no side-effects) and rarely found elsewhere
- Haskell and Clean
- C# (deferred execution)

Mutable Pair

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• HOMEWORK: 4.31, 4.32, 4.39, 4.40, 4.42