

# CS 532: 3D Computer Vision

## 8<sup>th</sup> Set of Notes

Instructor: Philippos Mordohai

Webpage: [www.cs.stevens.edu/~mordohai](http://www.cs.stevens.edu/~mordohai)

E-mail: [Philippos.Mordohai@stevens.edu](mailto:Philippos.Mordohai@stevens.edu)

Office: Lieb 215

# FRIDAY

- Make up class for last week
- 3:30 in Altorfer 501

# Lecture Outline

- Large-scale Structure from Motion
  - Image collections
- Multi-view Stereo part I
- Sources:
  - Slides by R. Szeliski, S. Seitz, N. Snavely, D. Gallup, C. Hernandez, G. Vogiatzis, Y. Furukawa, M. Bleyer

# Structure from Motion from large Image Collections

- Given many images, how can we
  - a) figure out where they were all taken from?
  - b) build a 3D model of the scene?



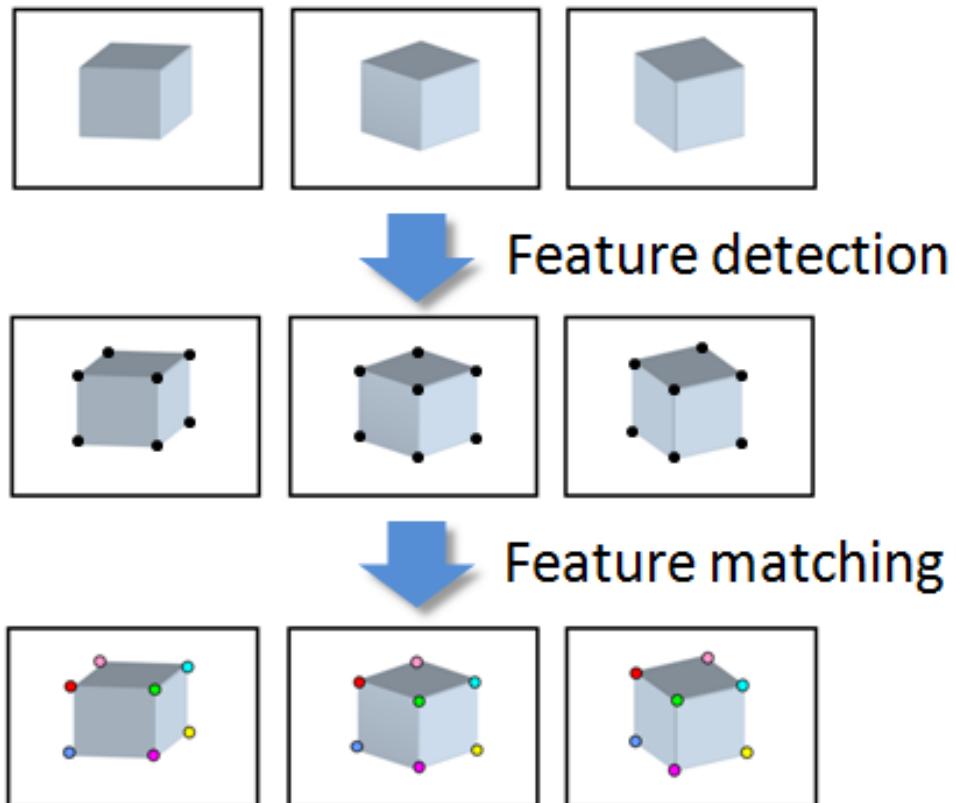
# Photo Tourism

## Photo Tourism Exploring photo collections in 3D

Noah Snavely   Steven M. Seitz   Richard Szeliski  
*University of Washington*                    *Microsoft Research*

SIGGRAPH 2006

# Input

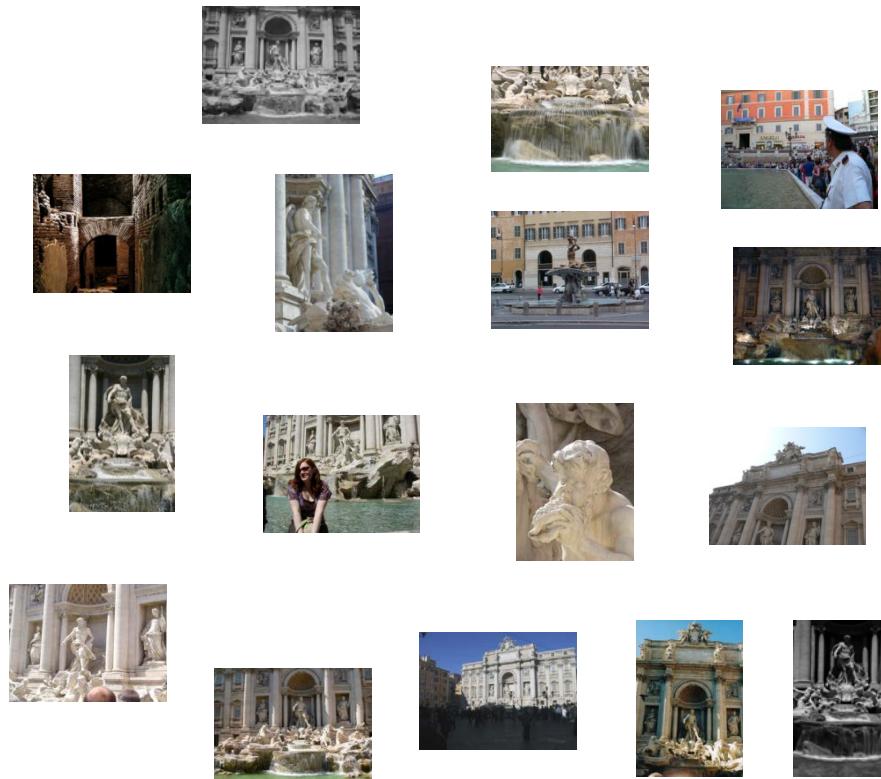


# First Step: How to Get Correspondences?

- Feature detection and matching

# Feature detection

Detect features using SIFT [Lowe, IJCV 2004] in all images

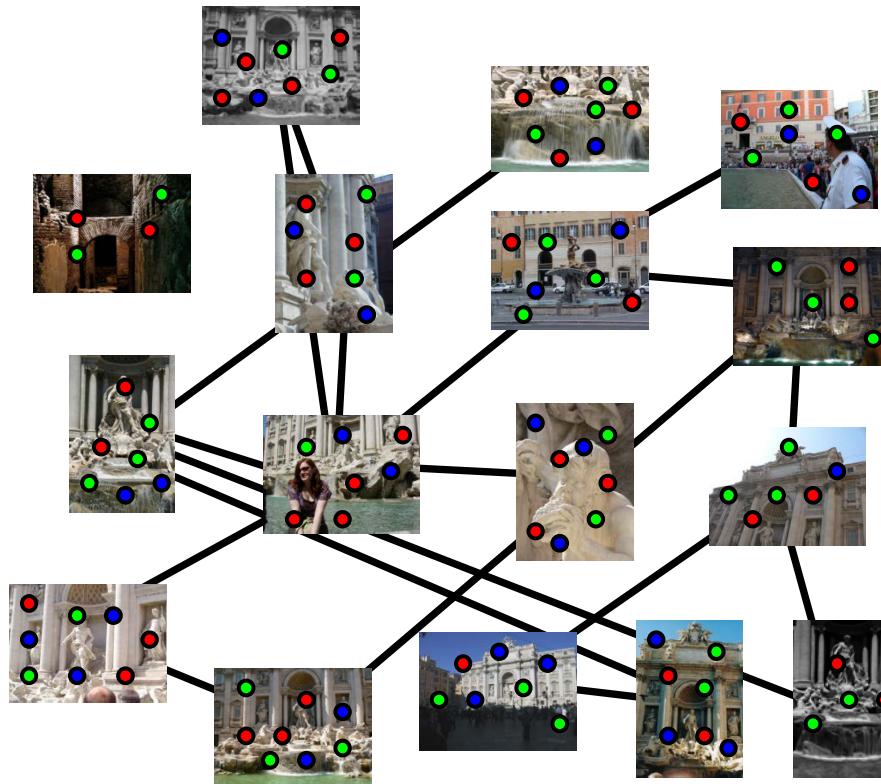


# Feature Detection



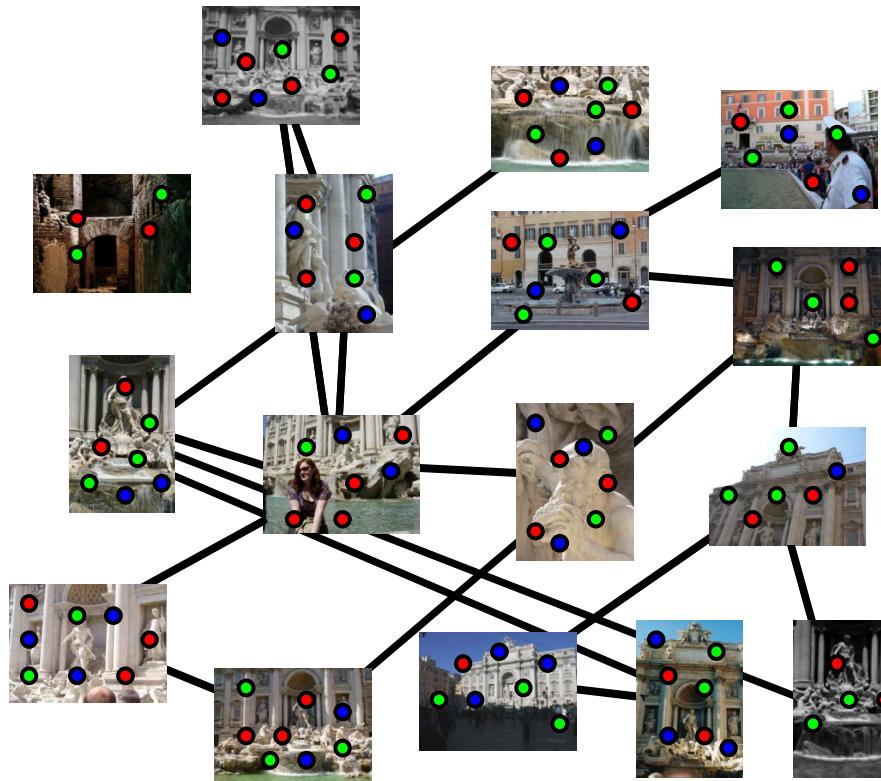
# Feature Matching

Match features between each pair of images

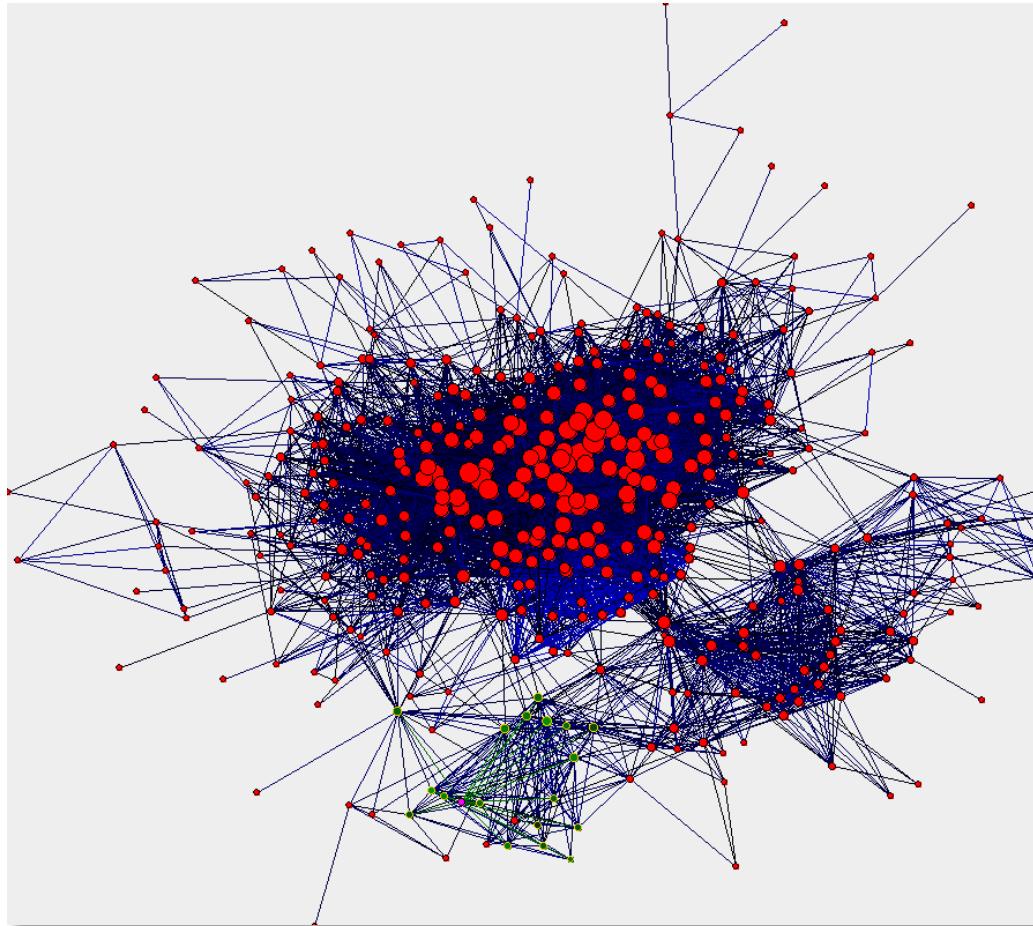


# Feature Matching

Refine matching using RANSAC to estimate fundamental matrix between each pair



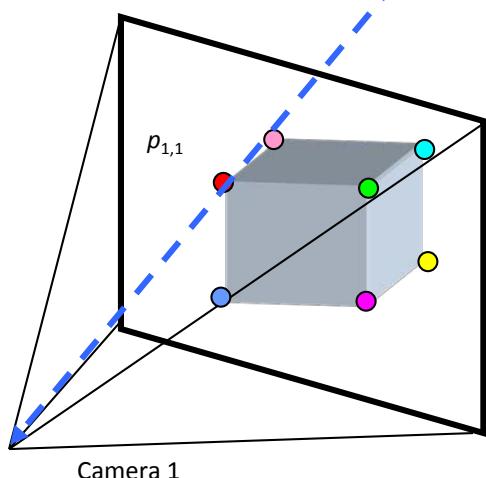
# Image Connectivity Graph



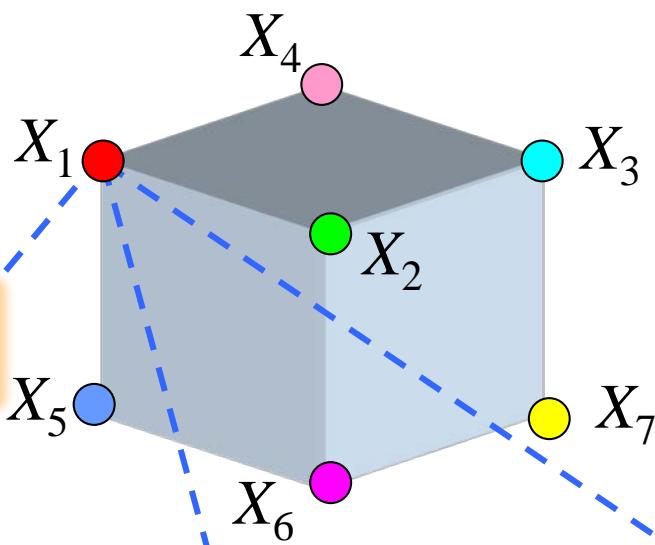
(graph layout produced using the Graphviz toolkit: <http://www.graphviz.org/>)

# Structure from motion

$$\Pi_1 X_1 \sim p_{11}$$

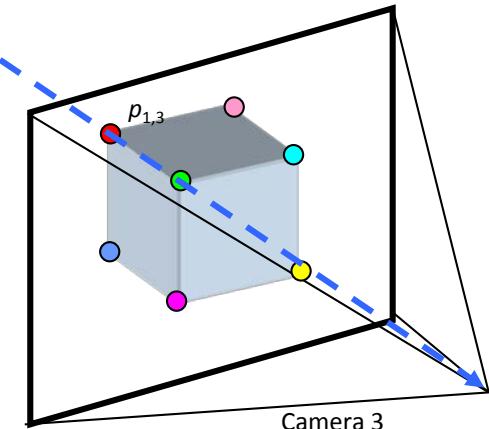


$$R_1, t_1$$



Camera 2

$$R_2, t_2$$



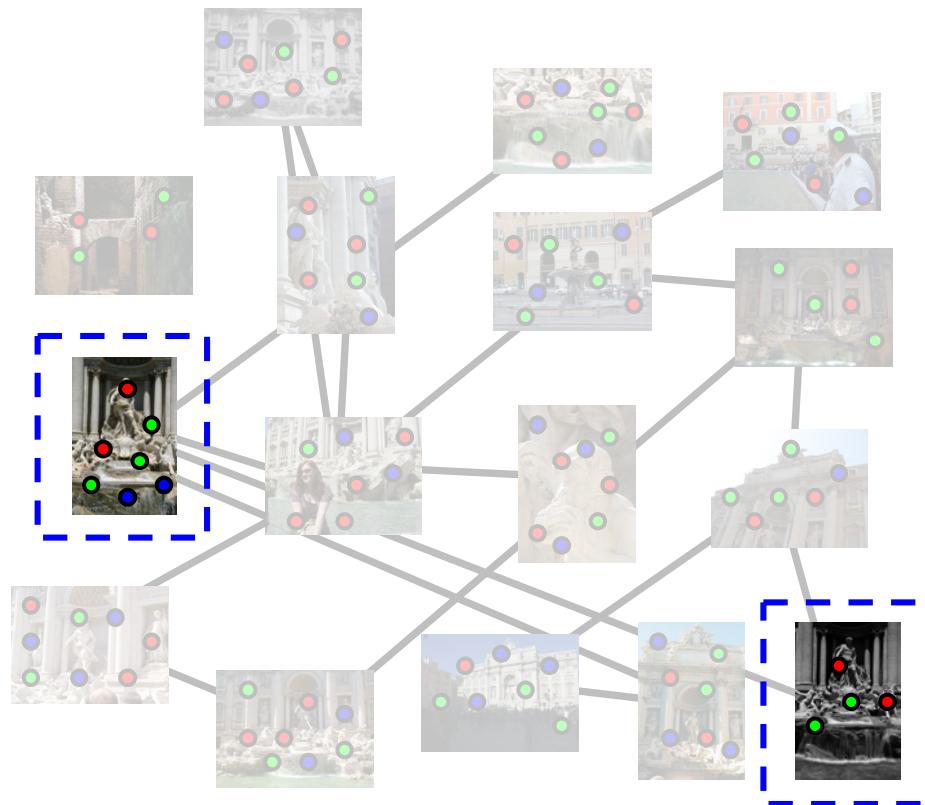
$$R_3, t_3$$

minimize  
 $g(\mathbf{R}, \mathbf{T}, \mathbf{X})$   
*non-linear least squares*

# Problem Size

- What are the variables?
- How many variables per camera?
- How many variables per point?
- Trevi Fountain collection
  - 466 input photos
  - + > 100,000 3D points
  - = very large optimization problem

# Incremental Structure from Motion

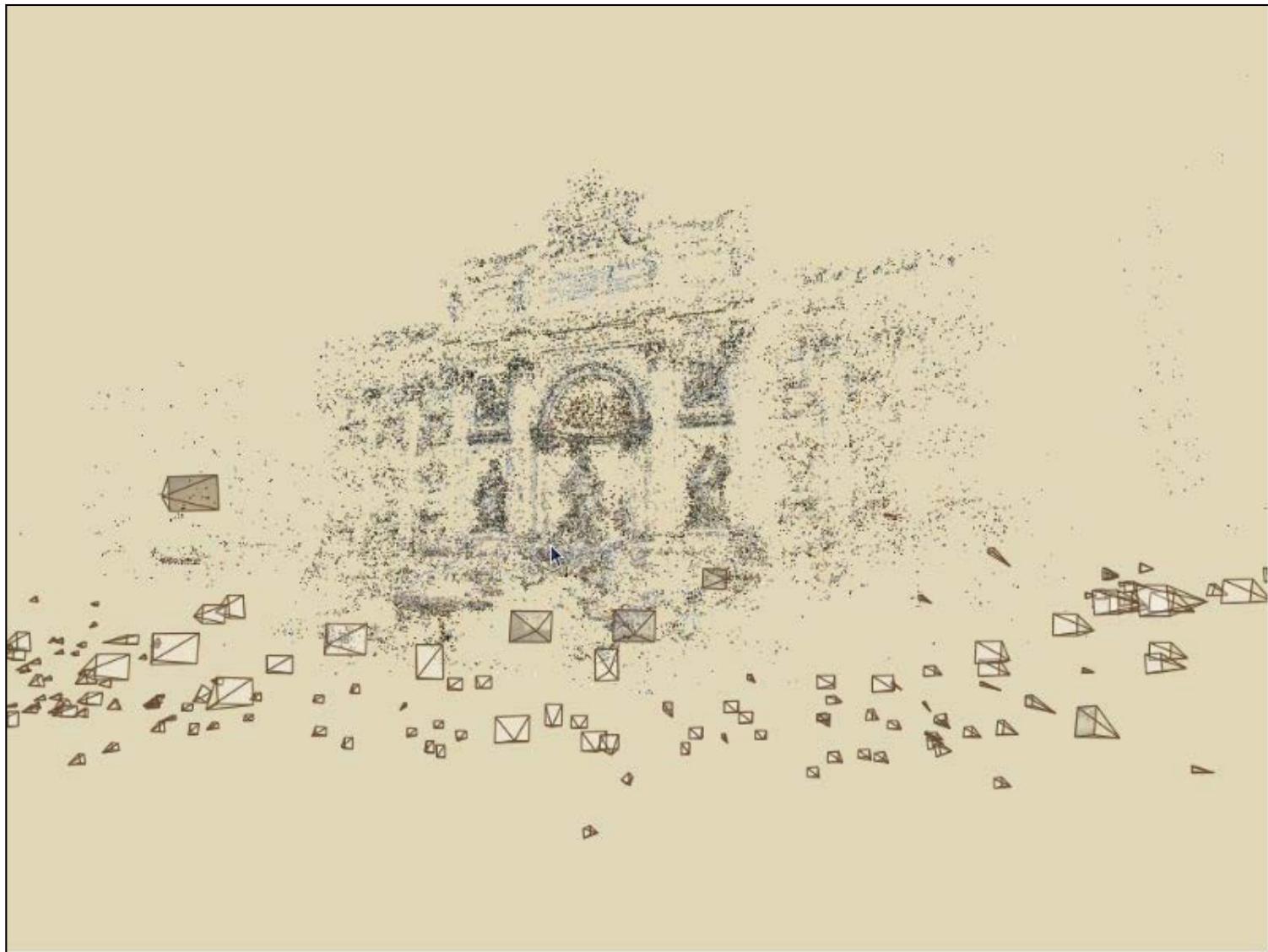


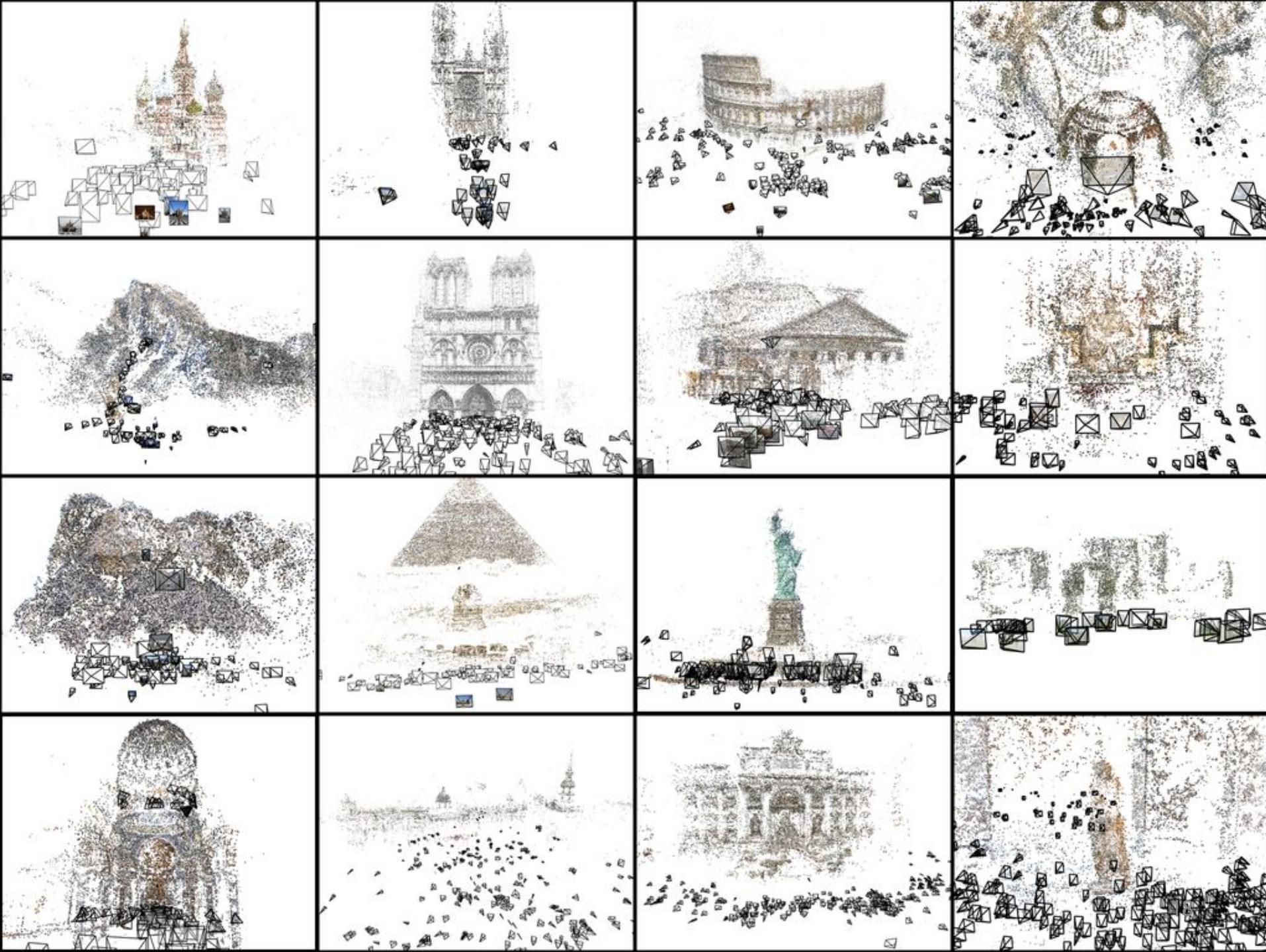
To help get good initializations for all of the parameters of the system, reconstruct the scene incrementally, starting from two photographs and the points they observe

# Incremental Structure from Motion



# Photo Explorer

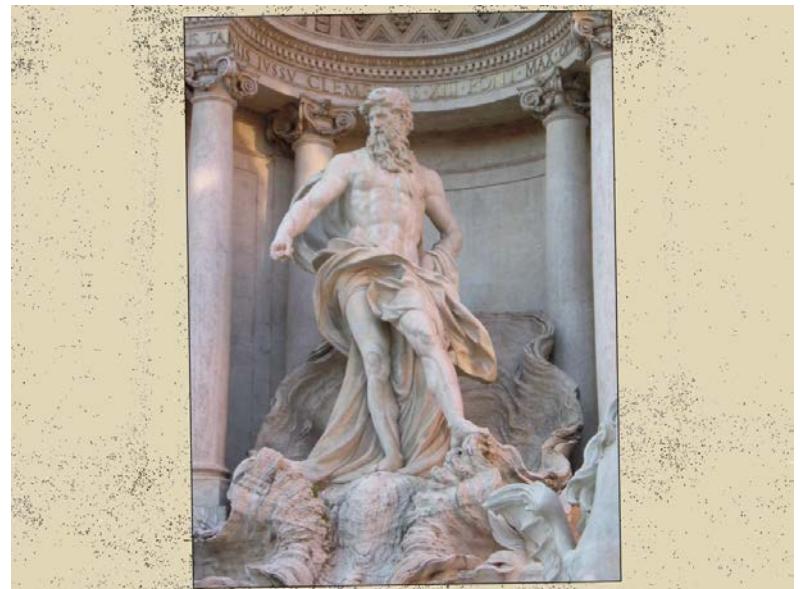
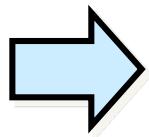




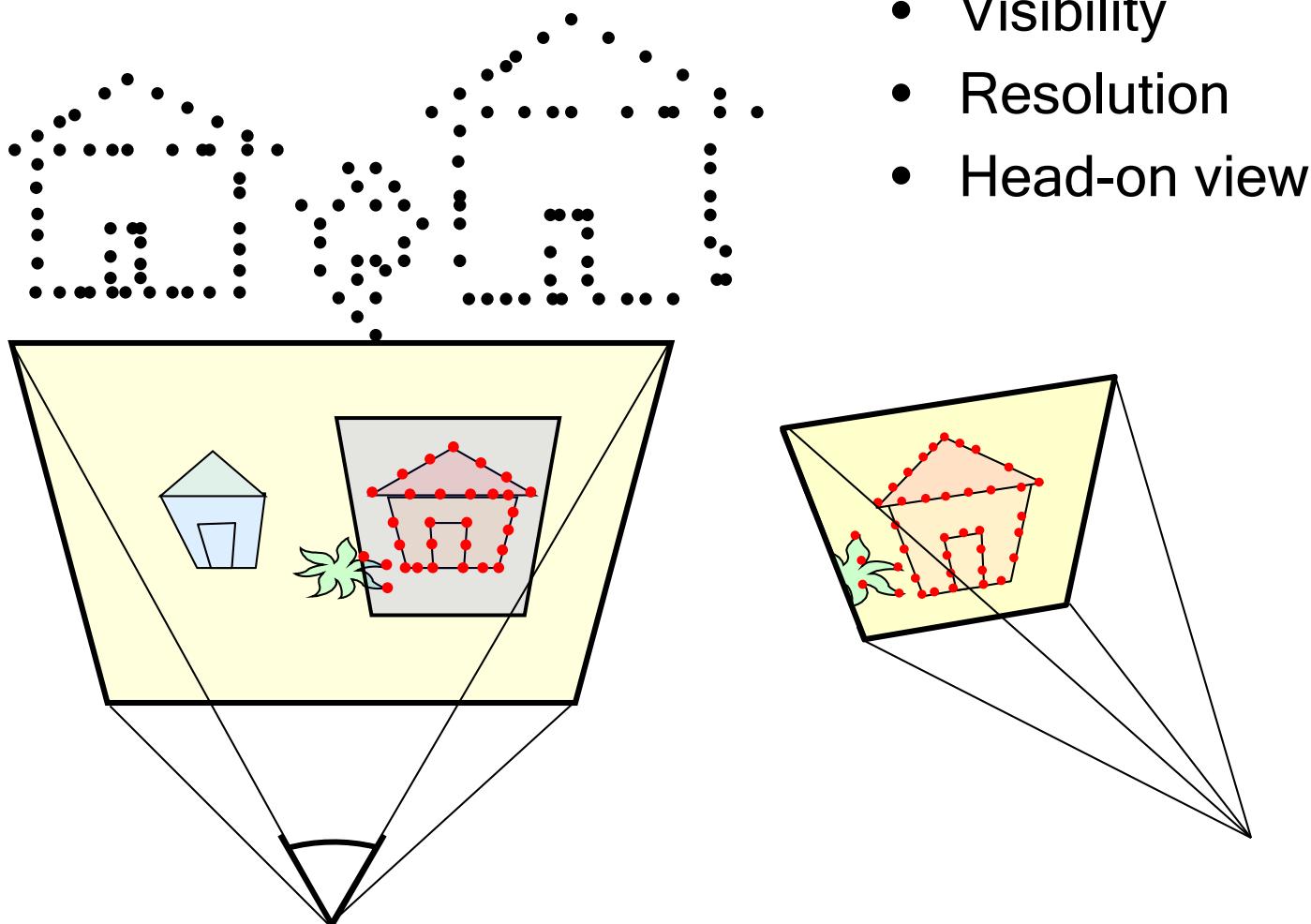
# Navigation Controls

- Free-flight navigation
- Object-based browsing
- Relation-based browsing
- Overhead map

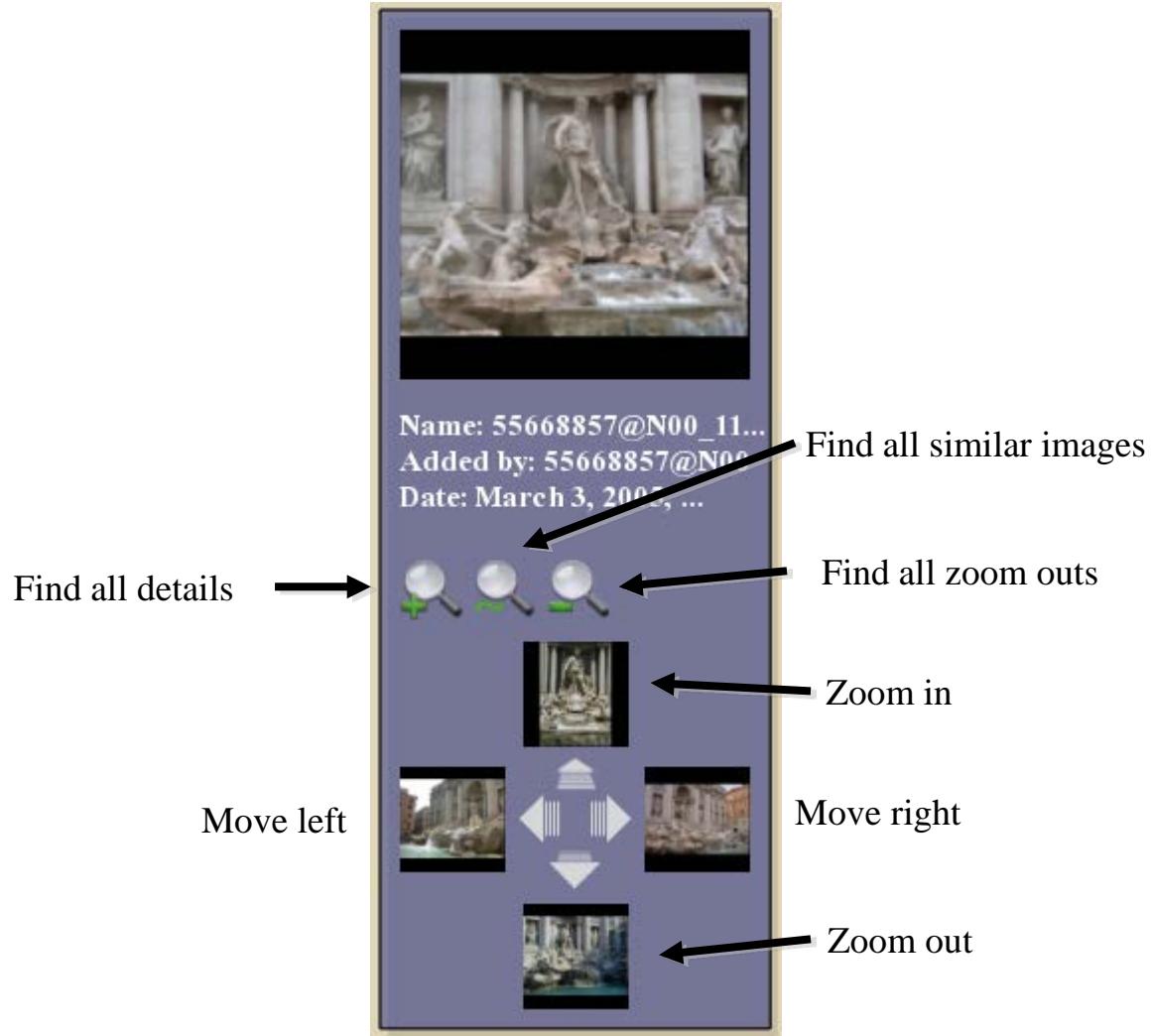
# Object-based Browsing



# Object-based browsing



# Relation-based Browsing



# Relation-based browsing

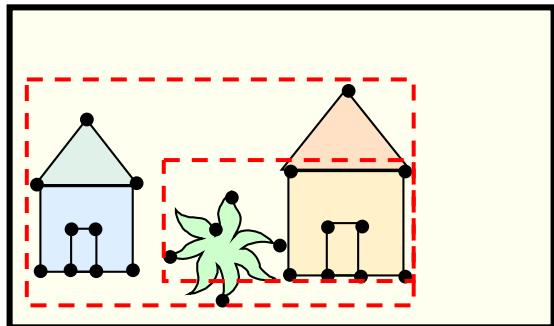


Image A

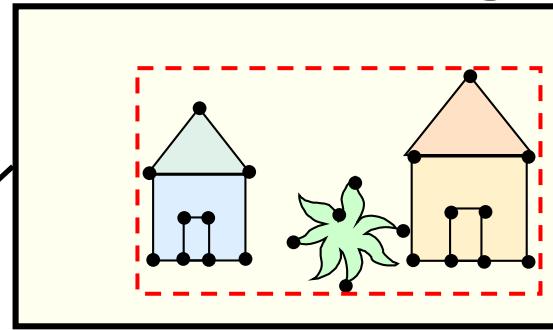


Image B

is to the  
left of

is detail of

is a zoom  
out of

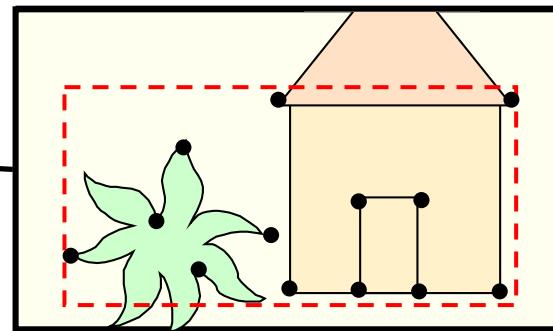


Image C

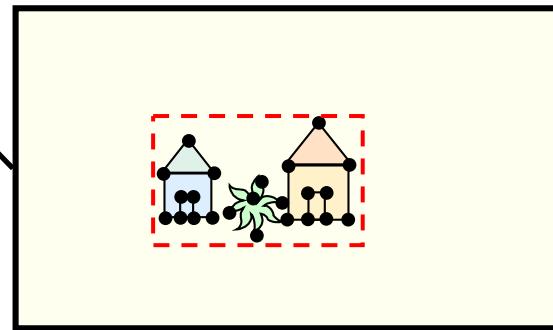
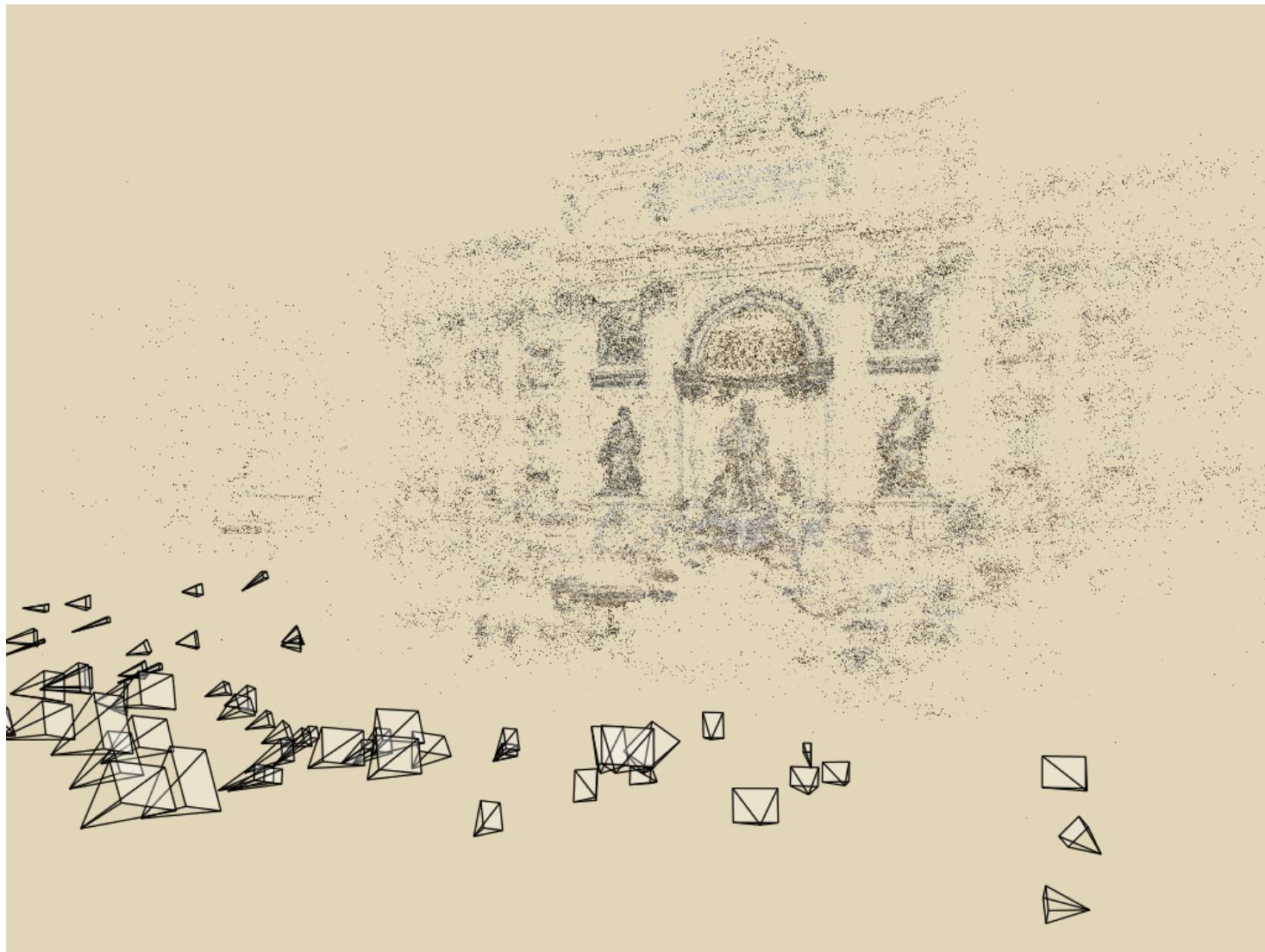


Image D

# Rendering



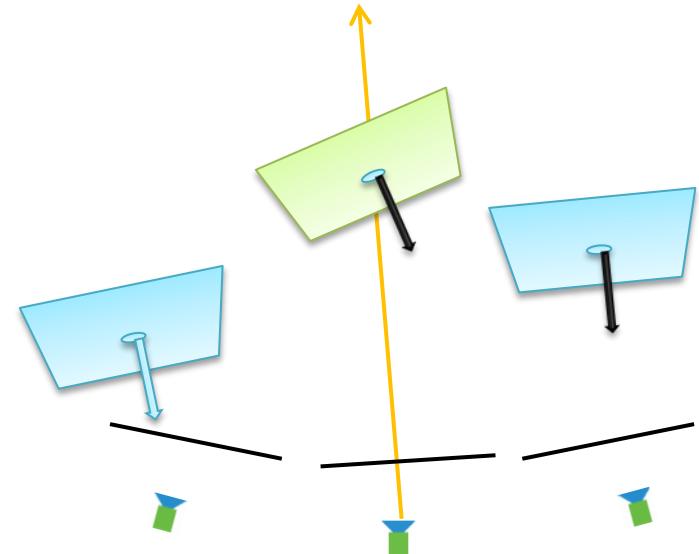
# Rendering



# Multi-View Stereo

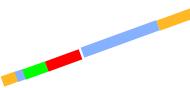
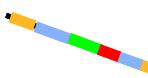
# Representations (coming soon)

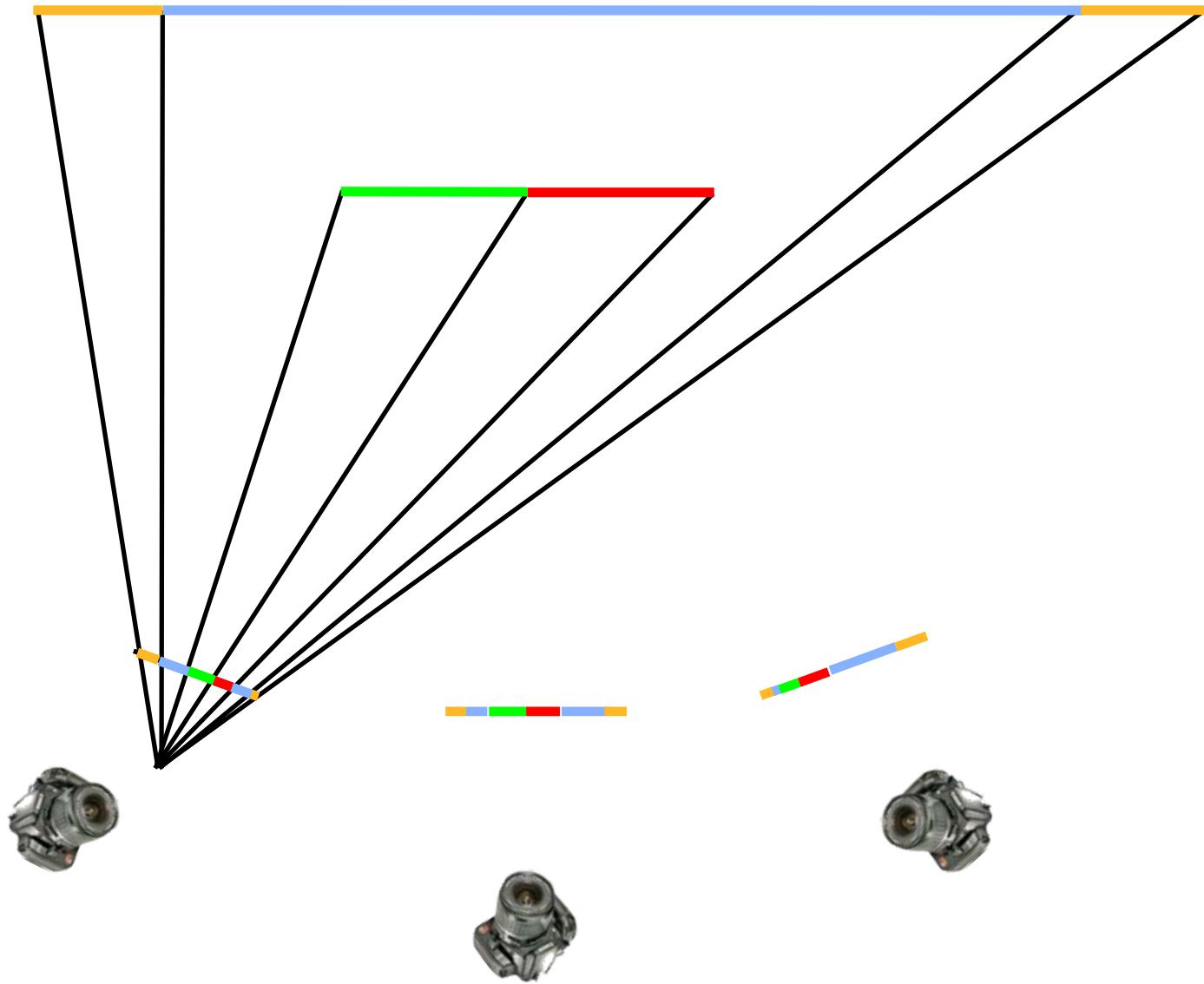
- Depth maps
- Point clouds
- Surface patches
- Level sets
- Voxels grids
- Meshes
- ...

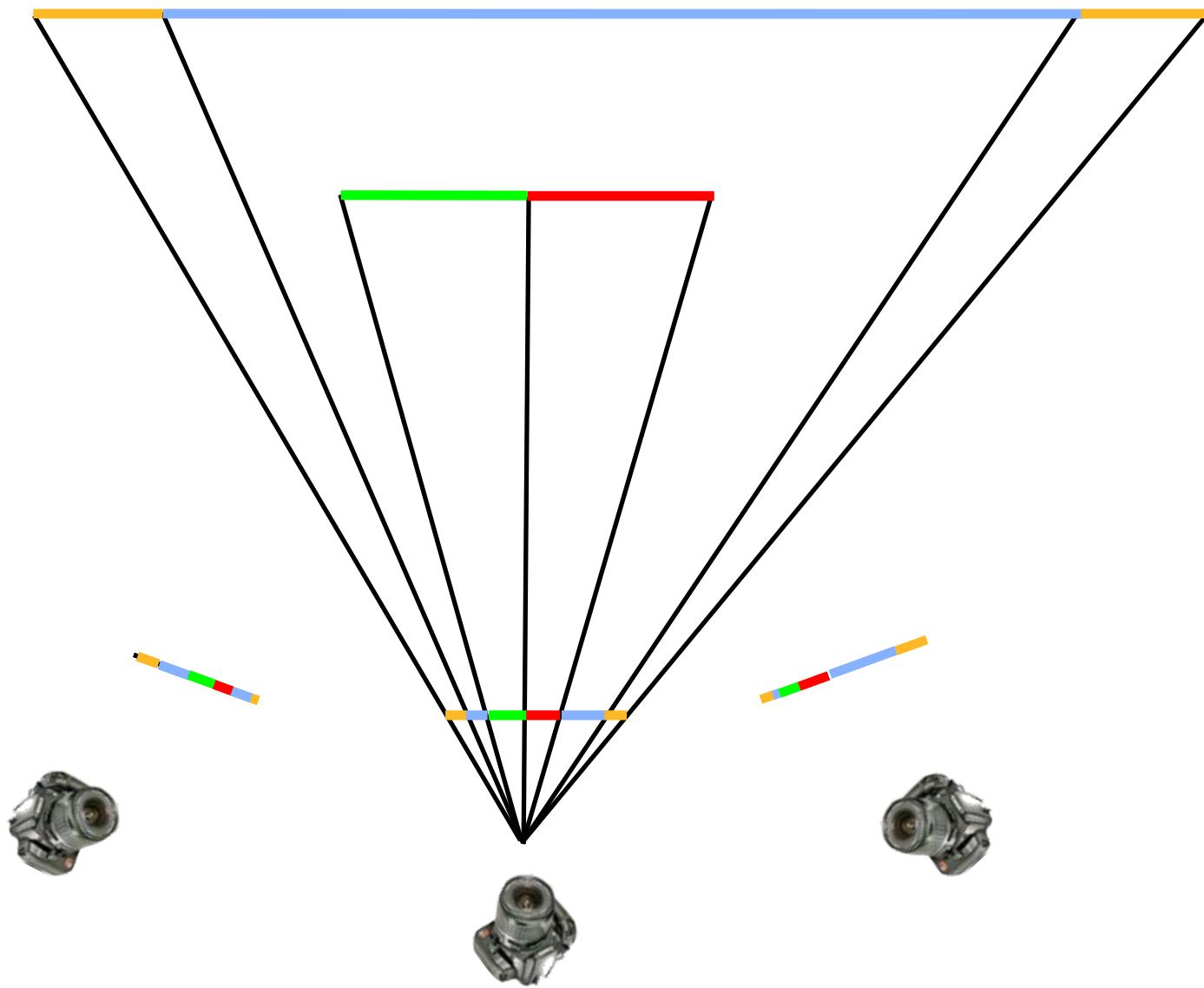


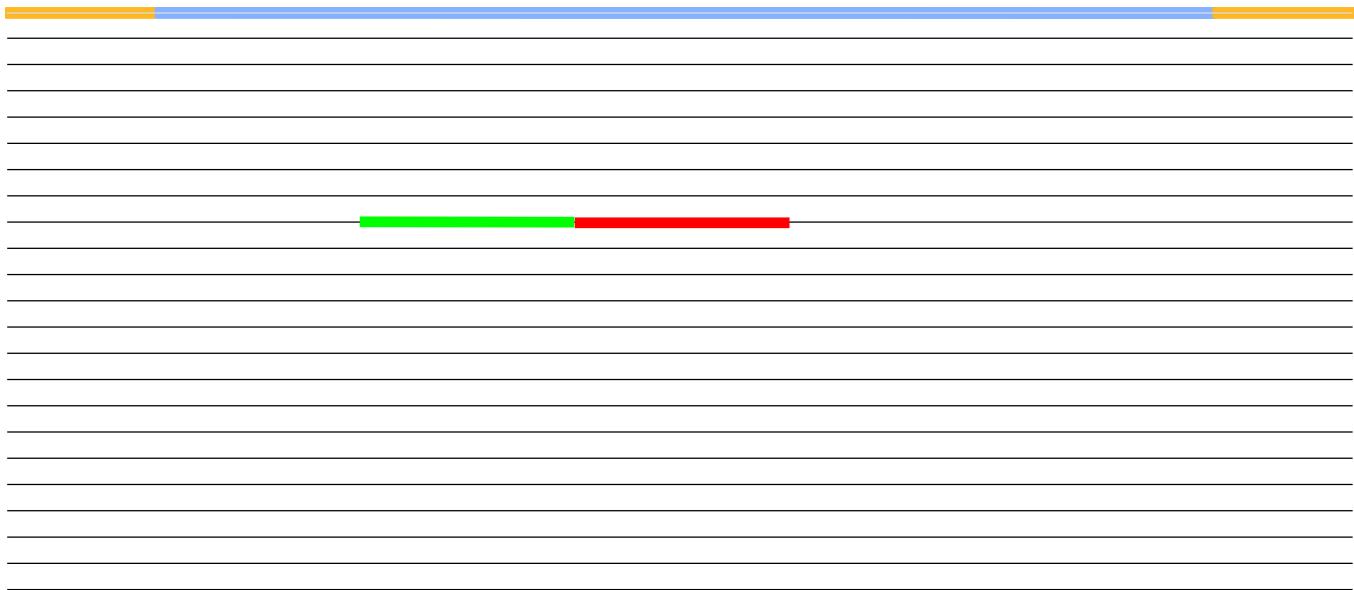
# Plane Sweeping Stereo

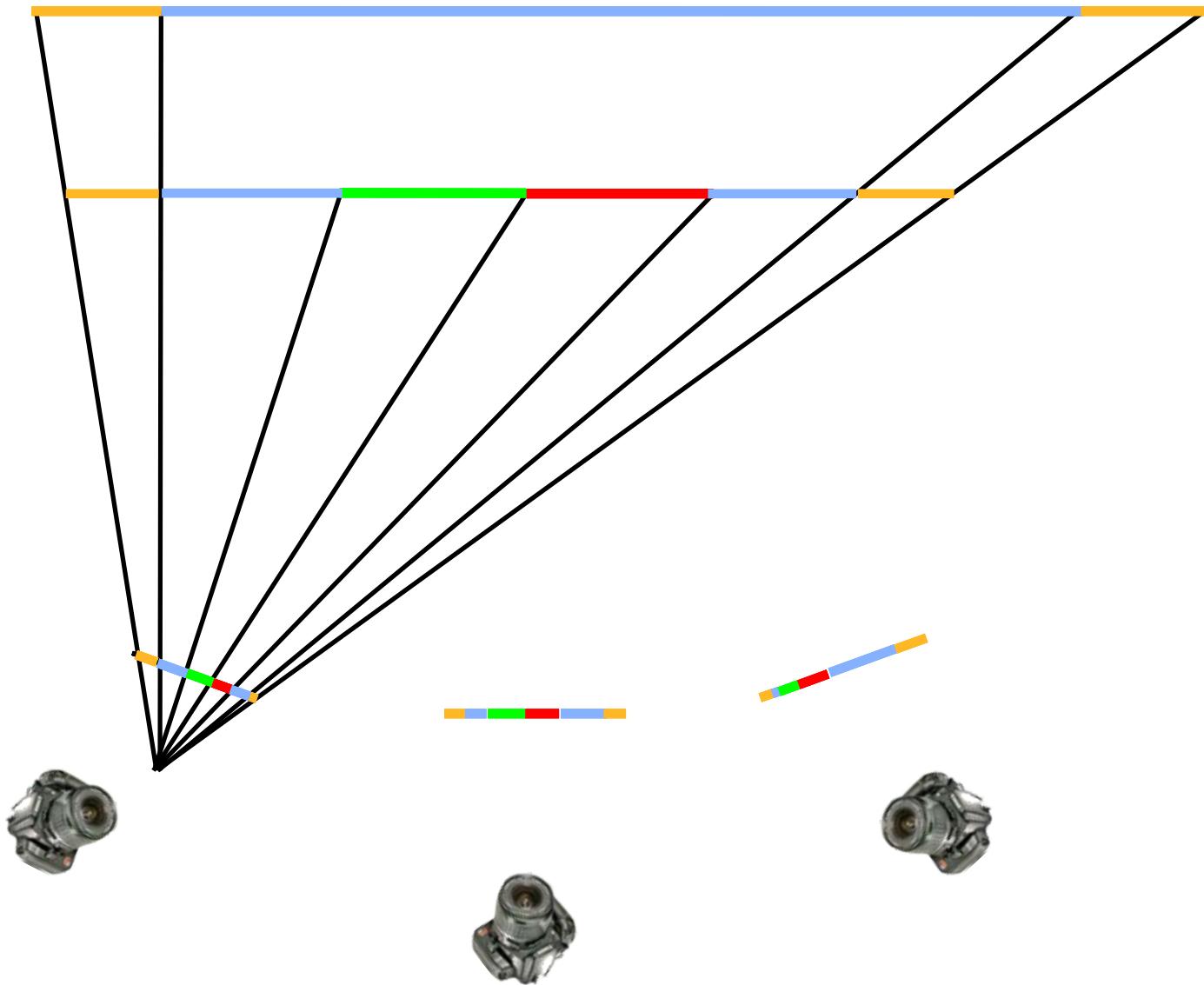
- True multi-view stereo
- Define family of planes that sweep depth range of interest
- For each pixel, generate and evaluate depth hypotheses by intersecting its ray with planes
  - Compute cost/score function to measure “photo-consistency”

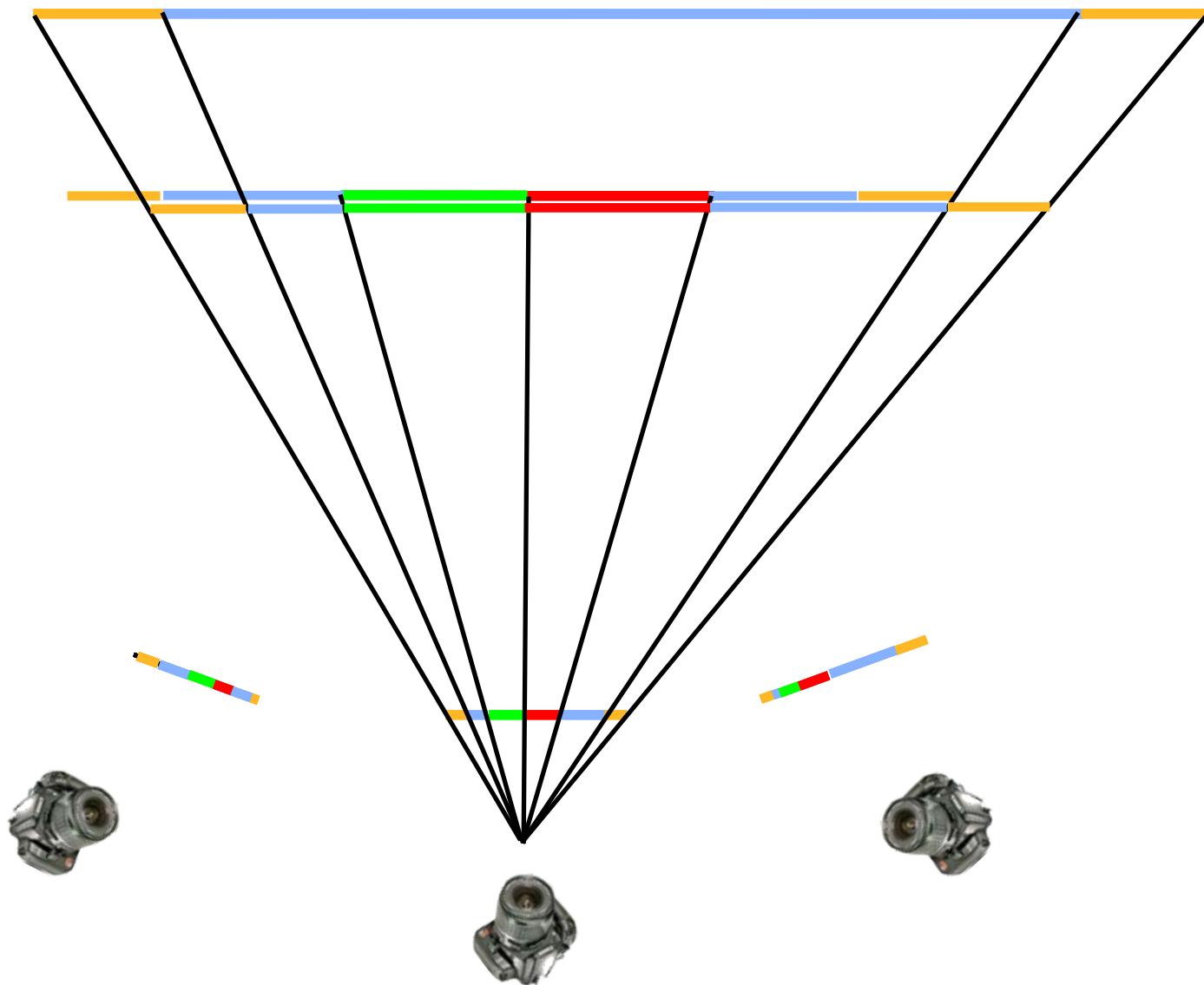


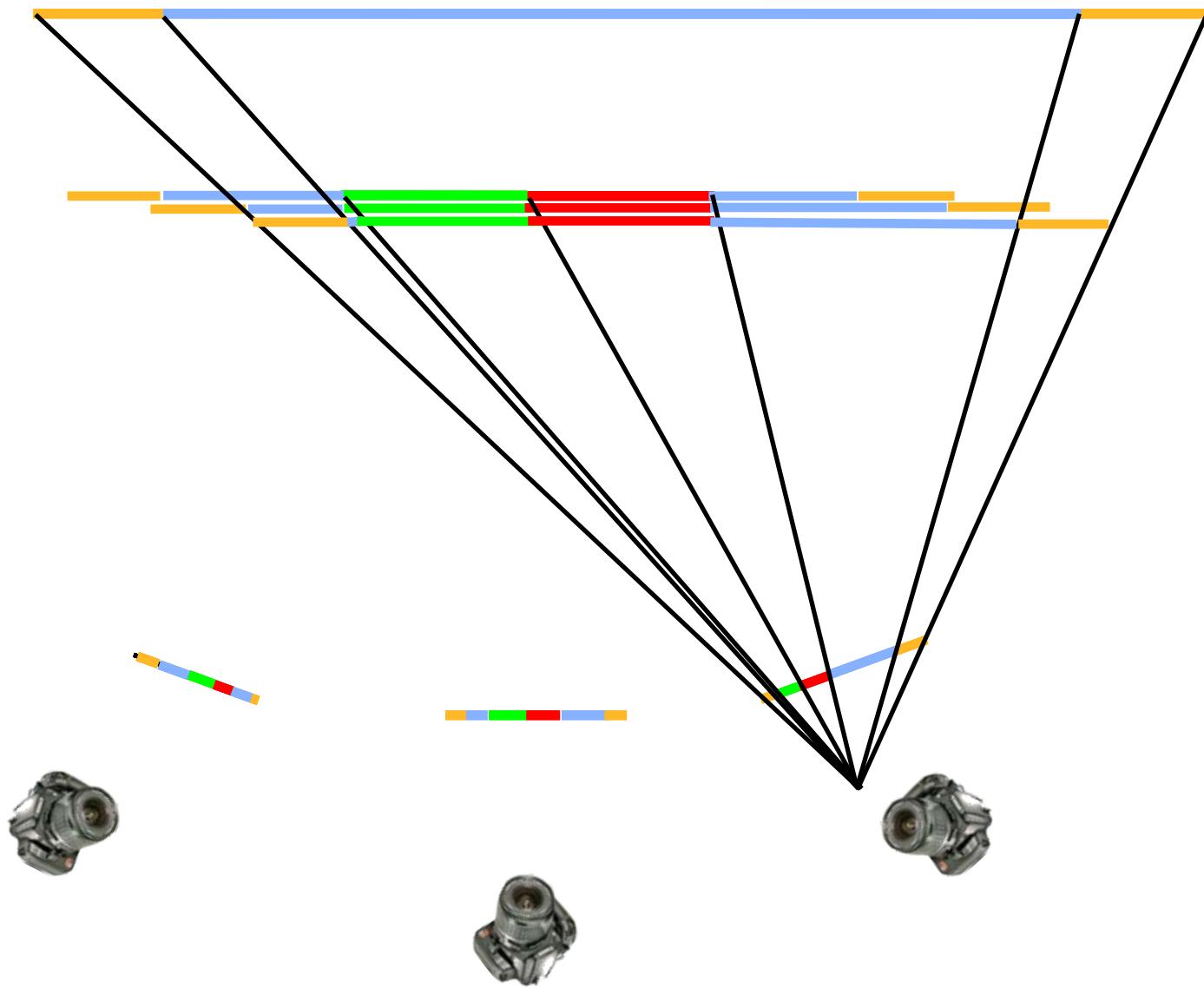


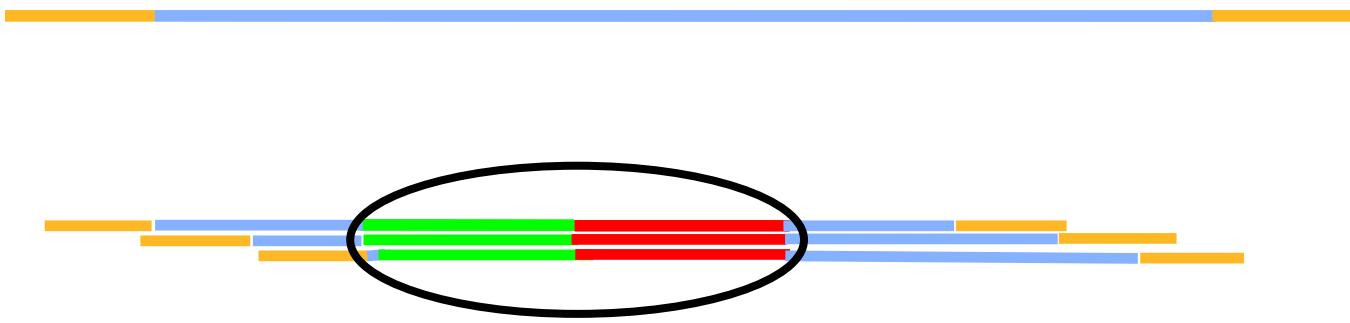


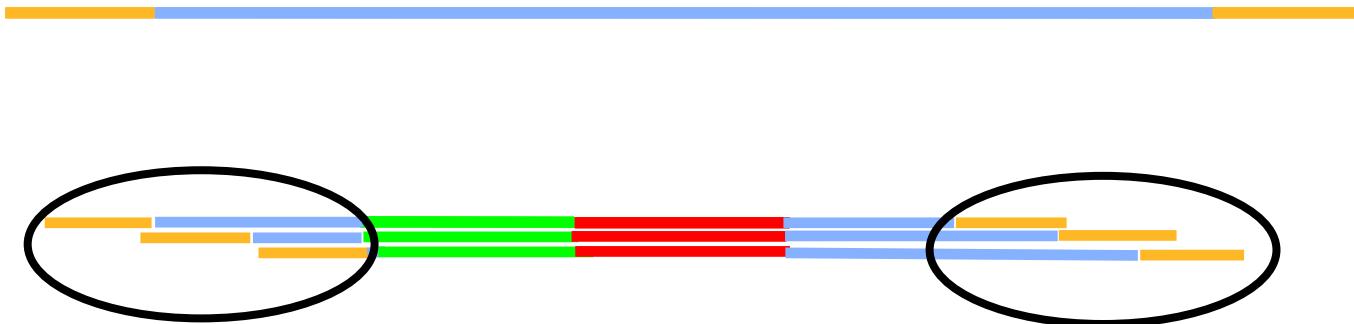


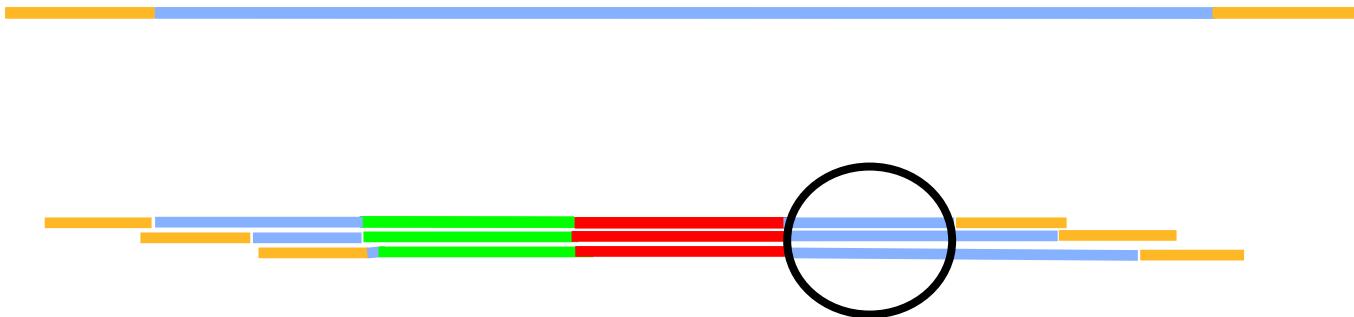






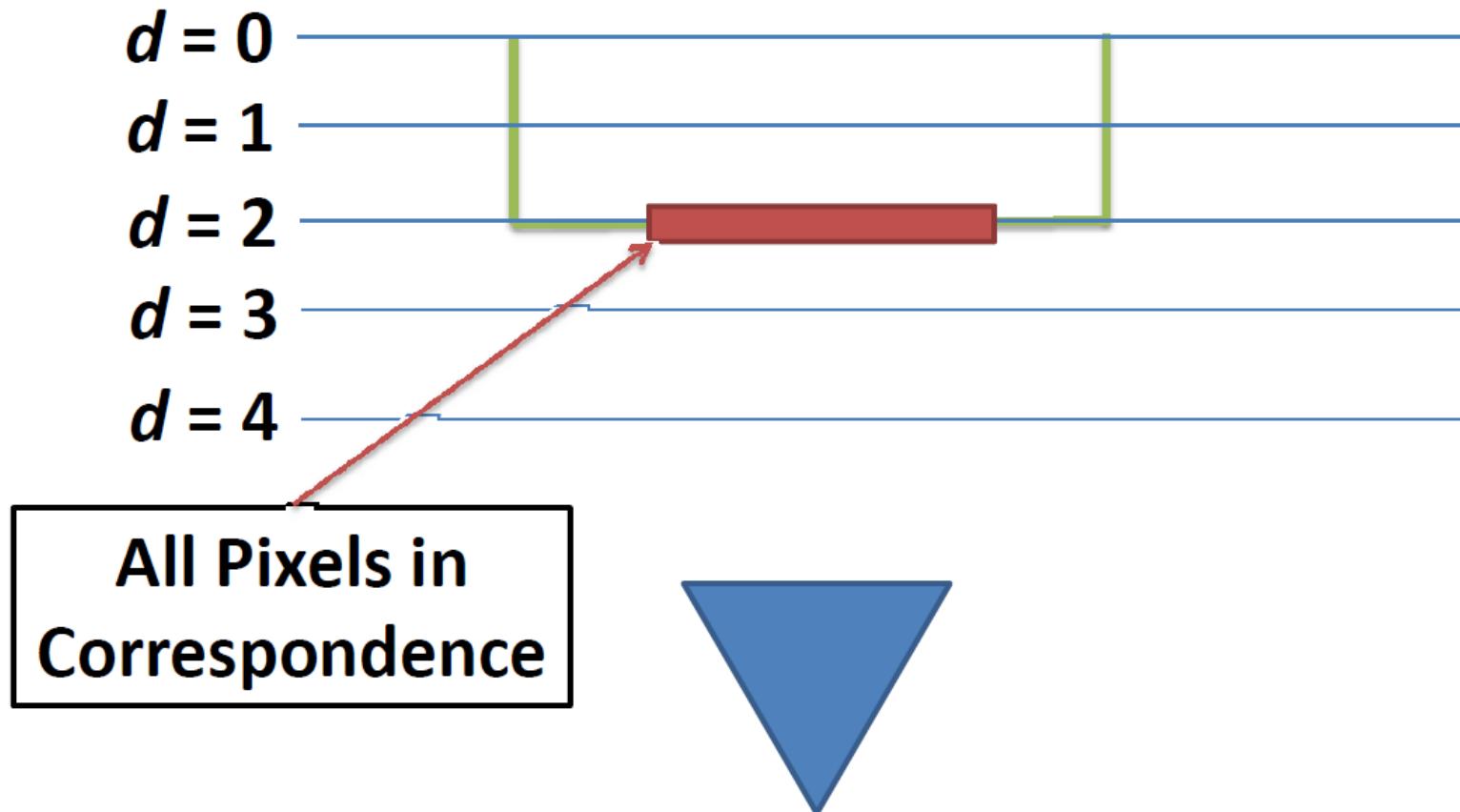






# Limitation of Plane Sweeping

- Assumes that all surfaces are planes which are fronto-parallel to the camera



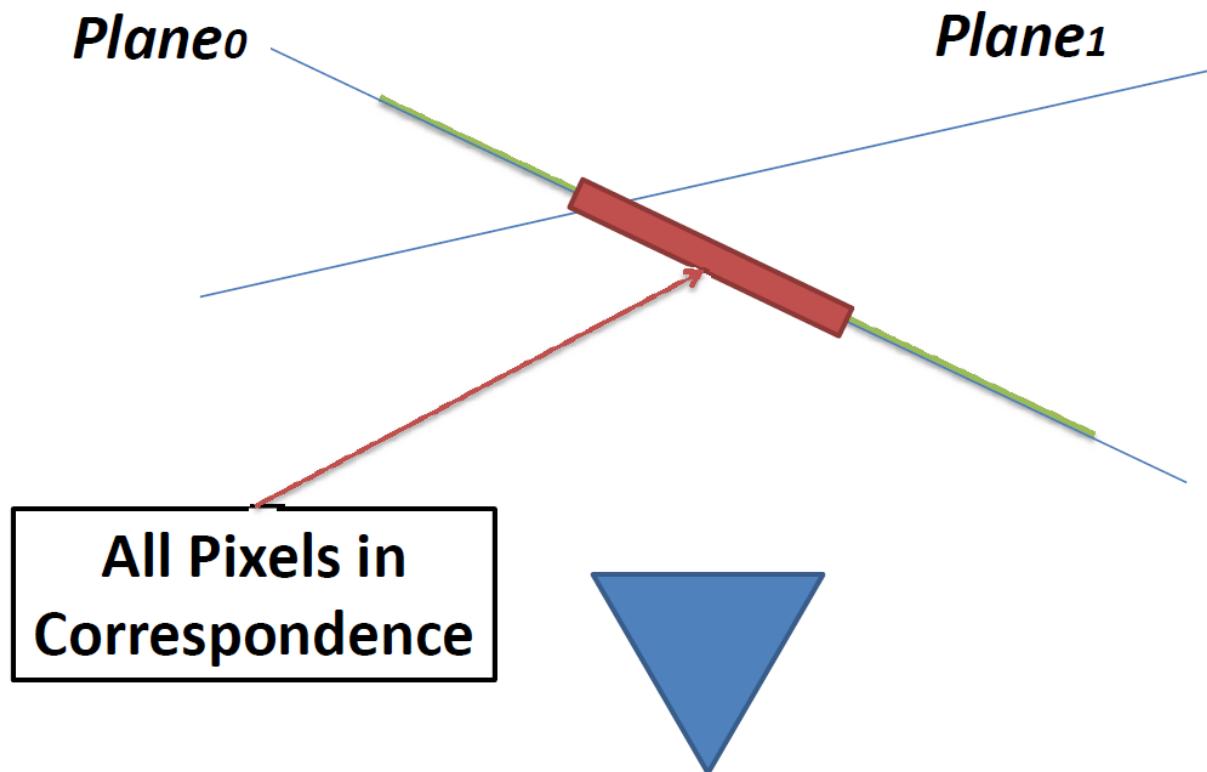
# Limitation of Plane Sweeping

- Cannot handle slanted planes



# Multi-way Plane Sweeping

- Solutions:
  - Detect planes in the scene and sweep parallel to them
  - Or, sweep in a few directions which are often sufficient



# Depth Map Fusion

- Fuse depth maps to improve accuracy and minimize violations of visibility constraints

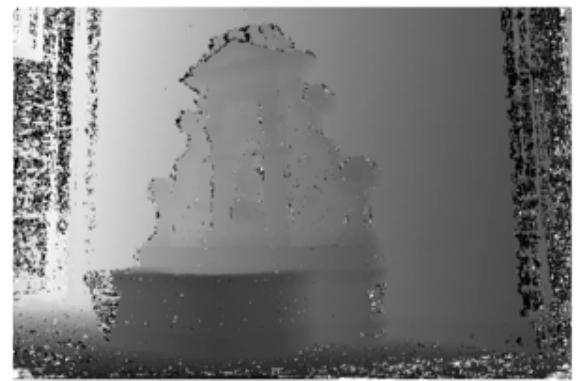
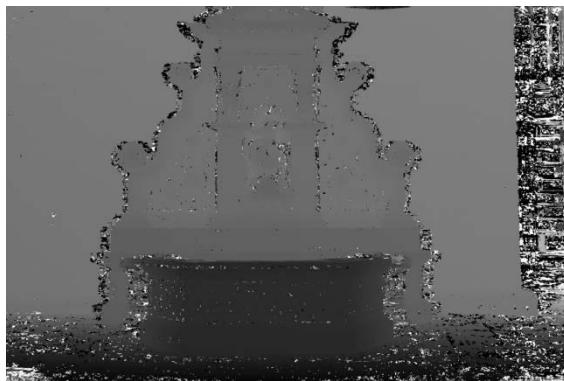
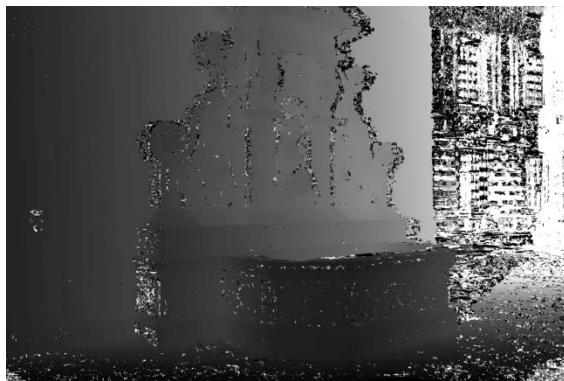
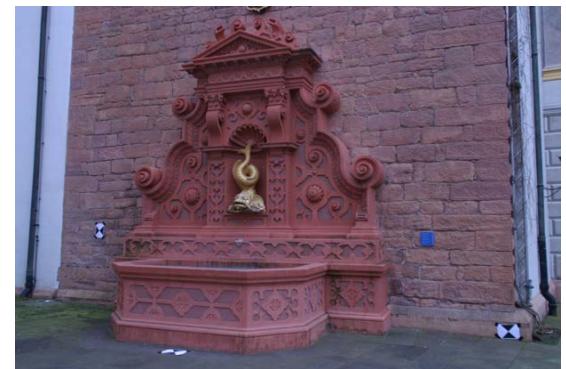
# Depth Map Fusion

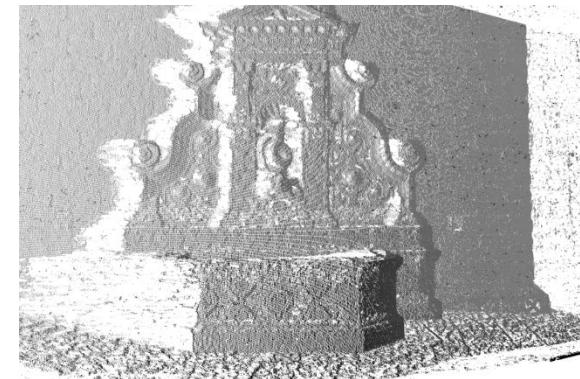
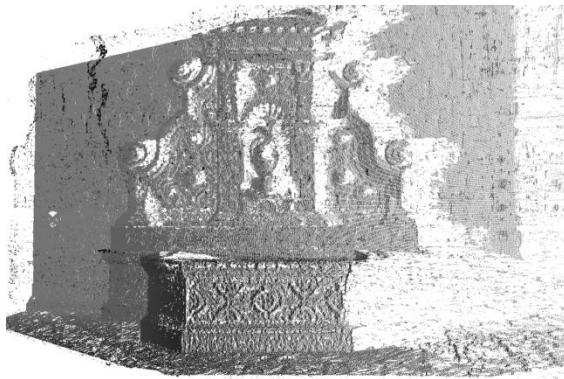
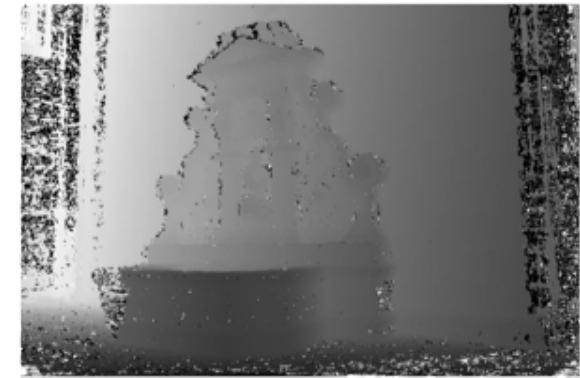
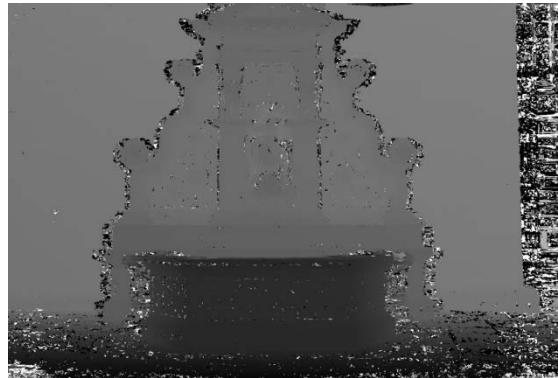
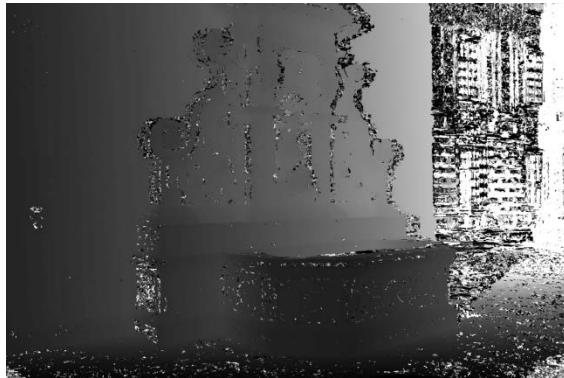
- Depth maps from plane sweeping are noisy
  - No occlusion handling
  - No consistency across views
- Use multiple depth estimates to:
  - Correct errors
  - Reduce redundancy in the model
- Minimize *occlusions* and *free-space violations*
  - Occluded depth estimates are too far from the camera
  - Depth estimates violating free space of other surfaces are too close

# Inputs

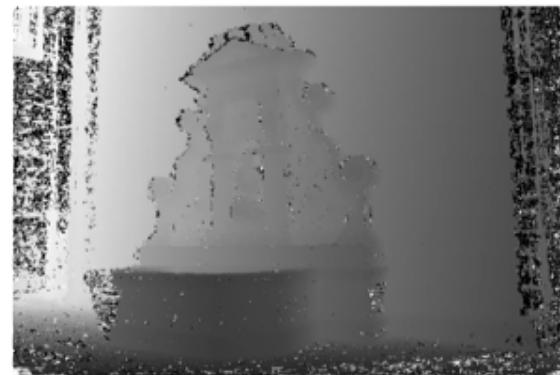
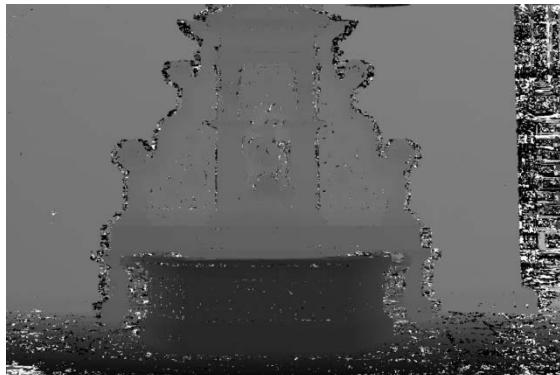
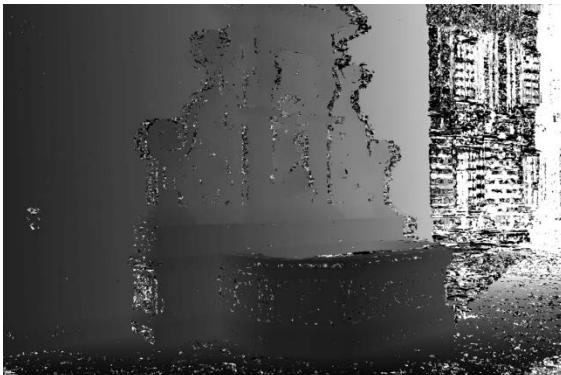


- Depth maps from plane sweeping
- Confidence maps (optionally)

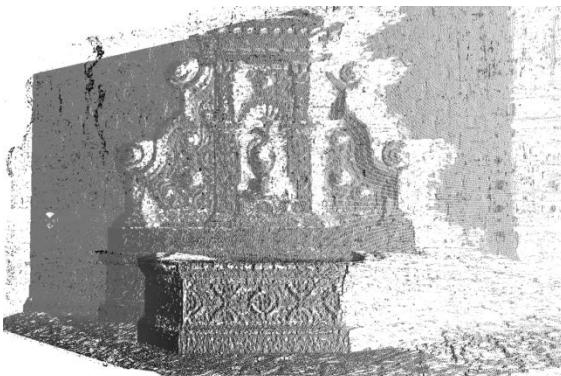




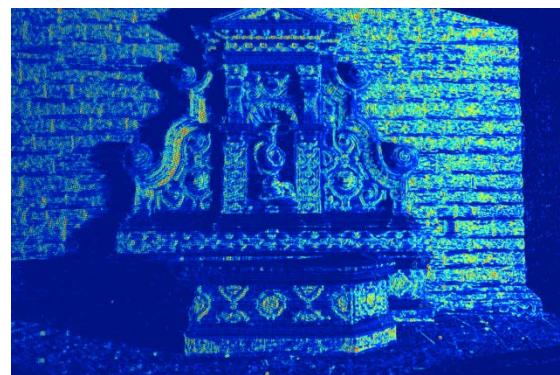
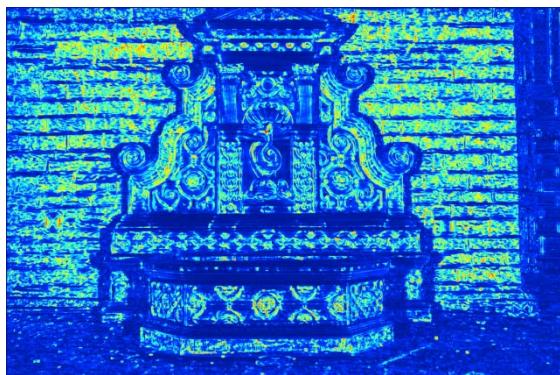
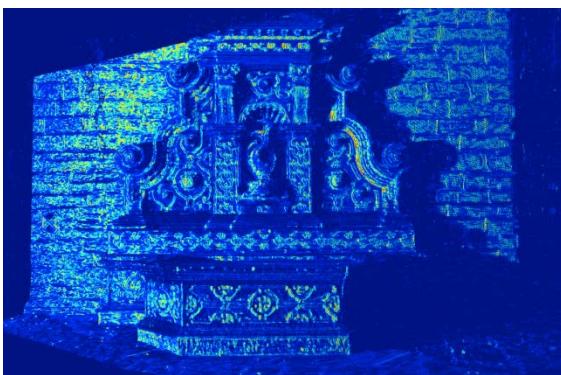
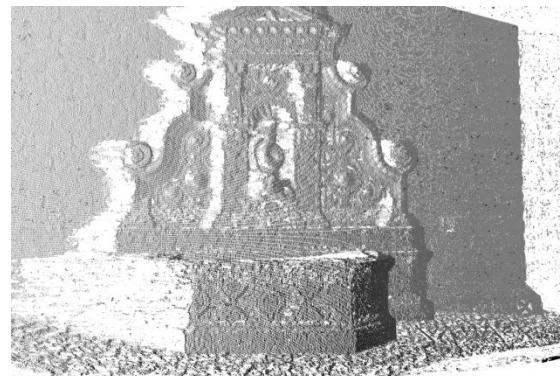
Render depth map of target views to reference view and fuse them according to visibility constraints and confidence



Input depth maps



Depth maps rendered  
on reference view

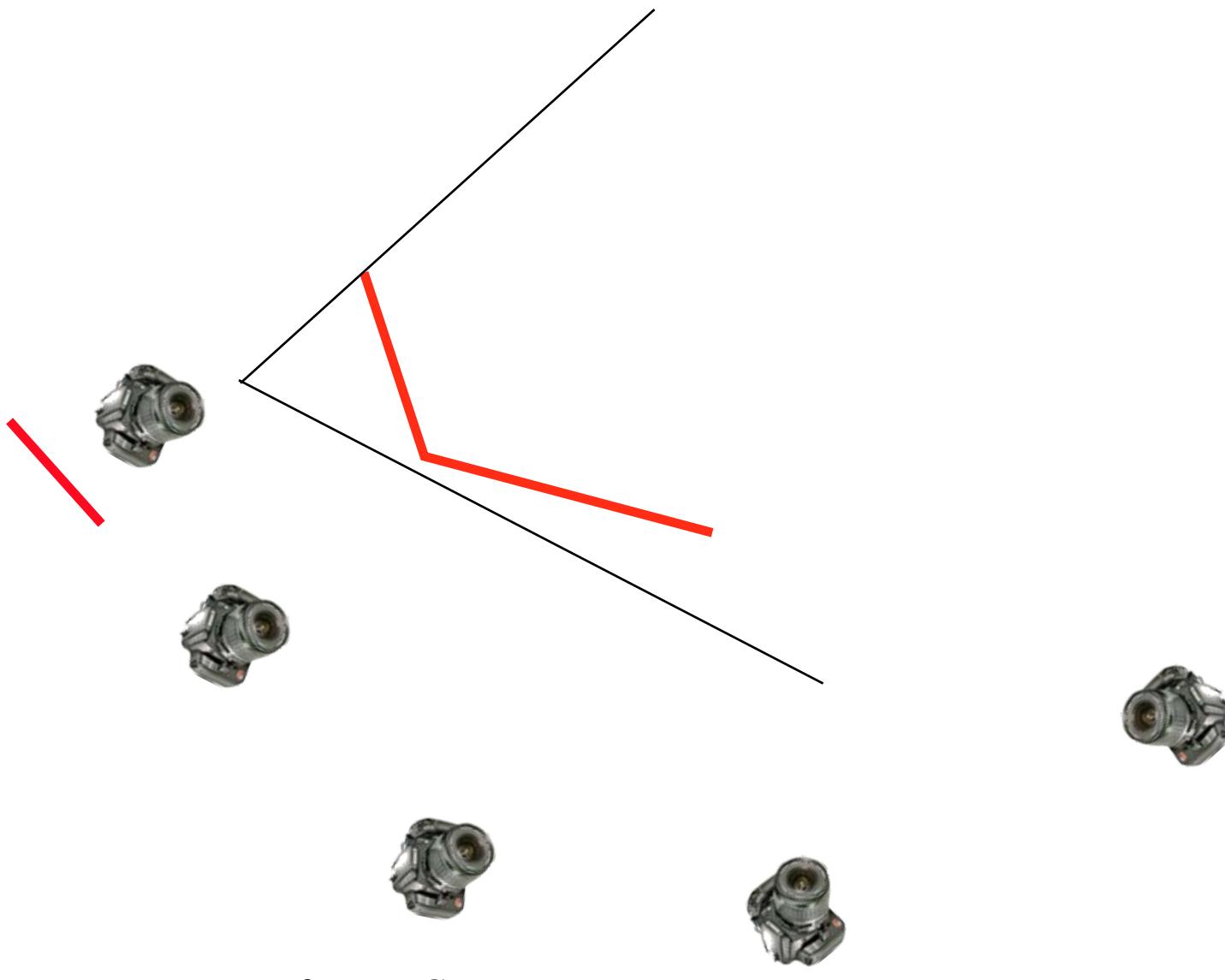


Confidence maps rendered on reference view

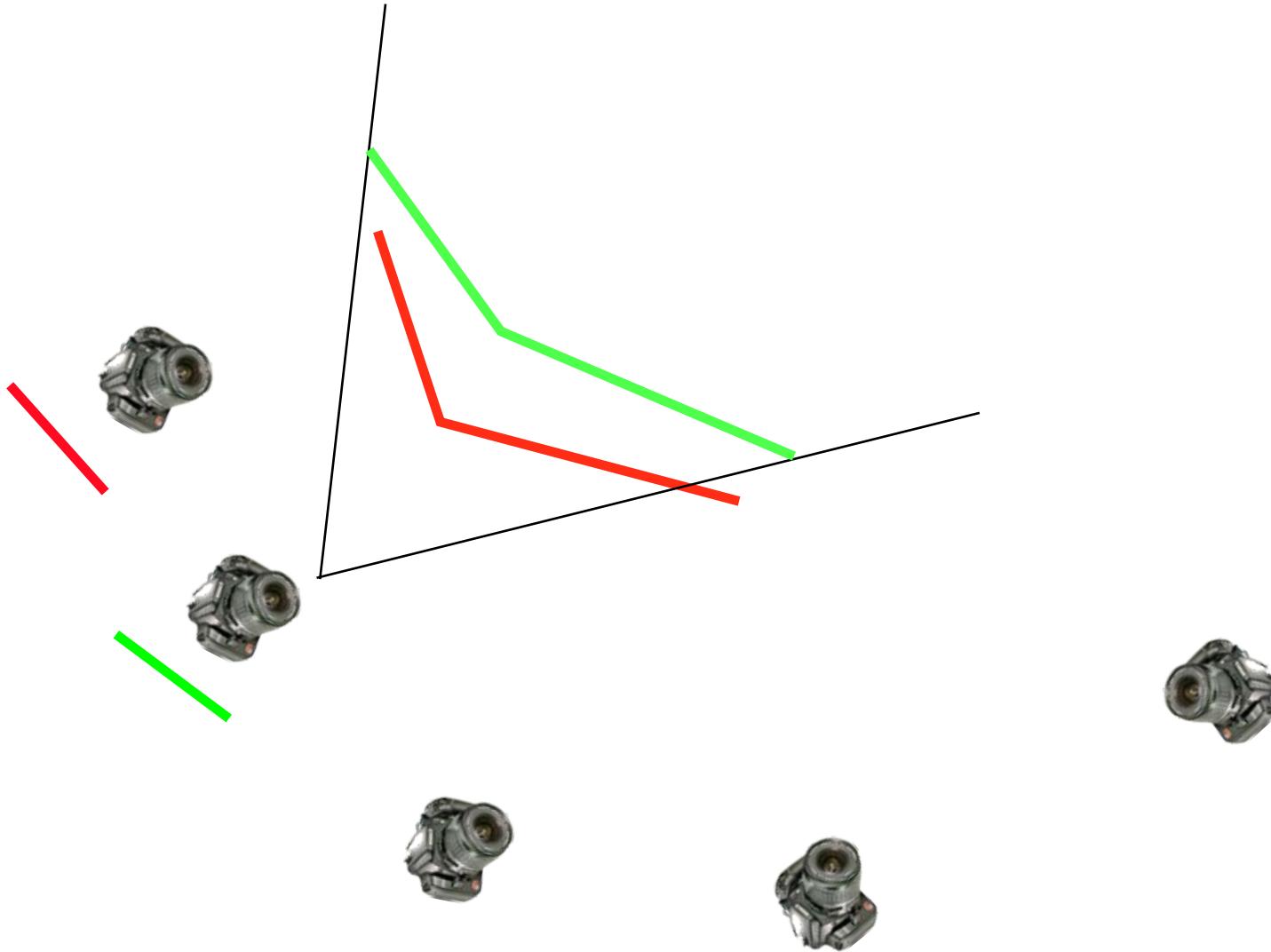
# Render Depth Maps to Reference View



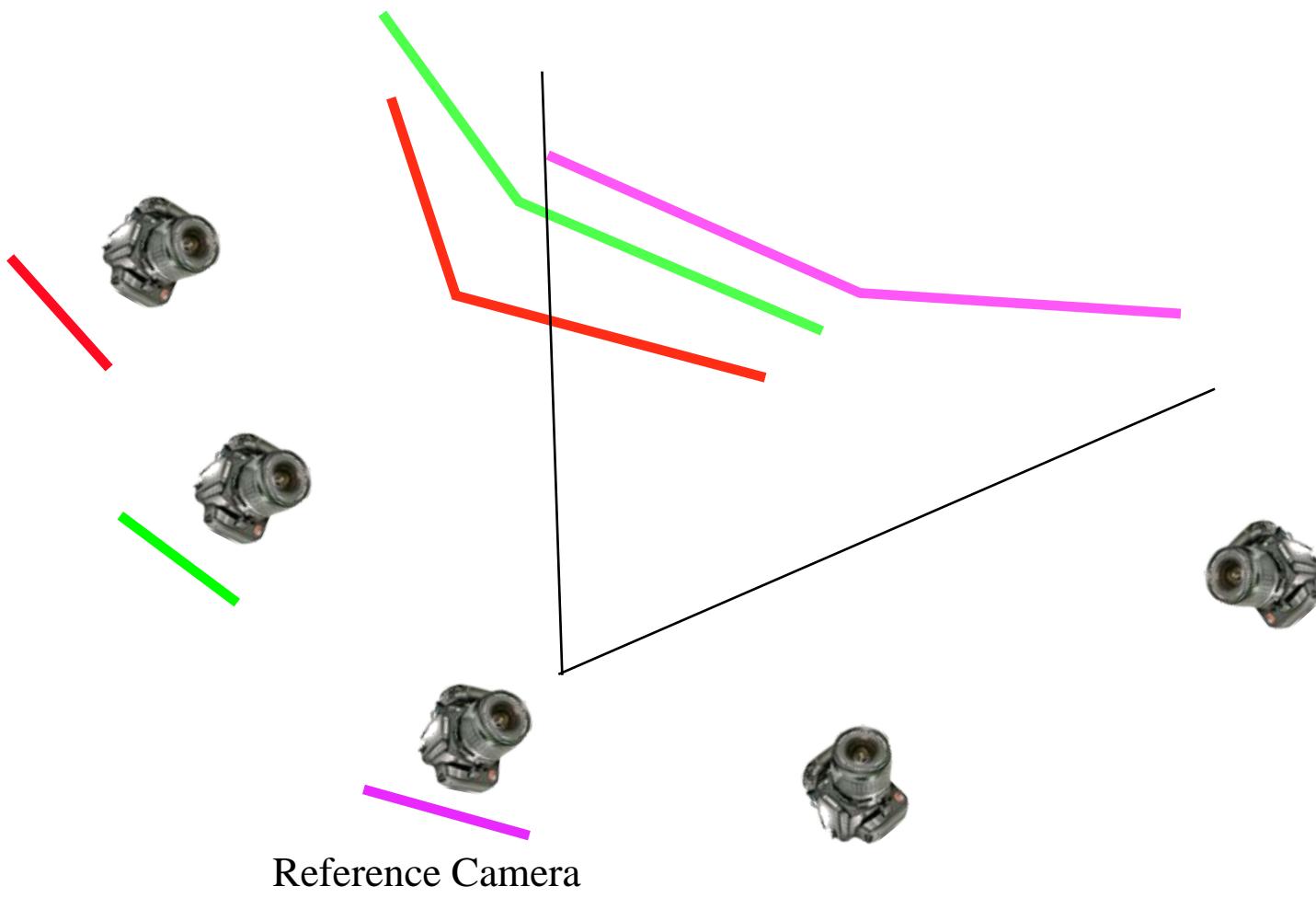
Reference Camera

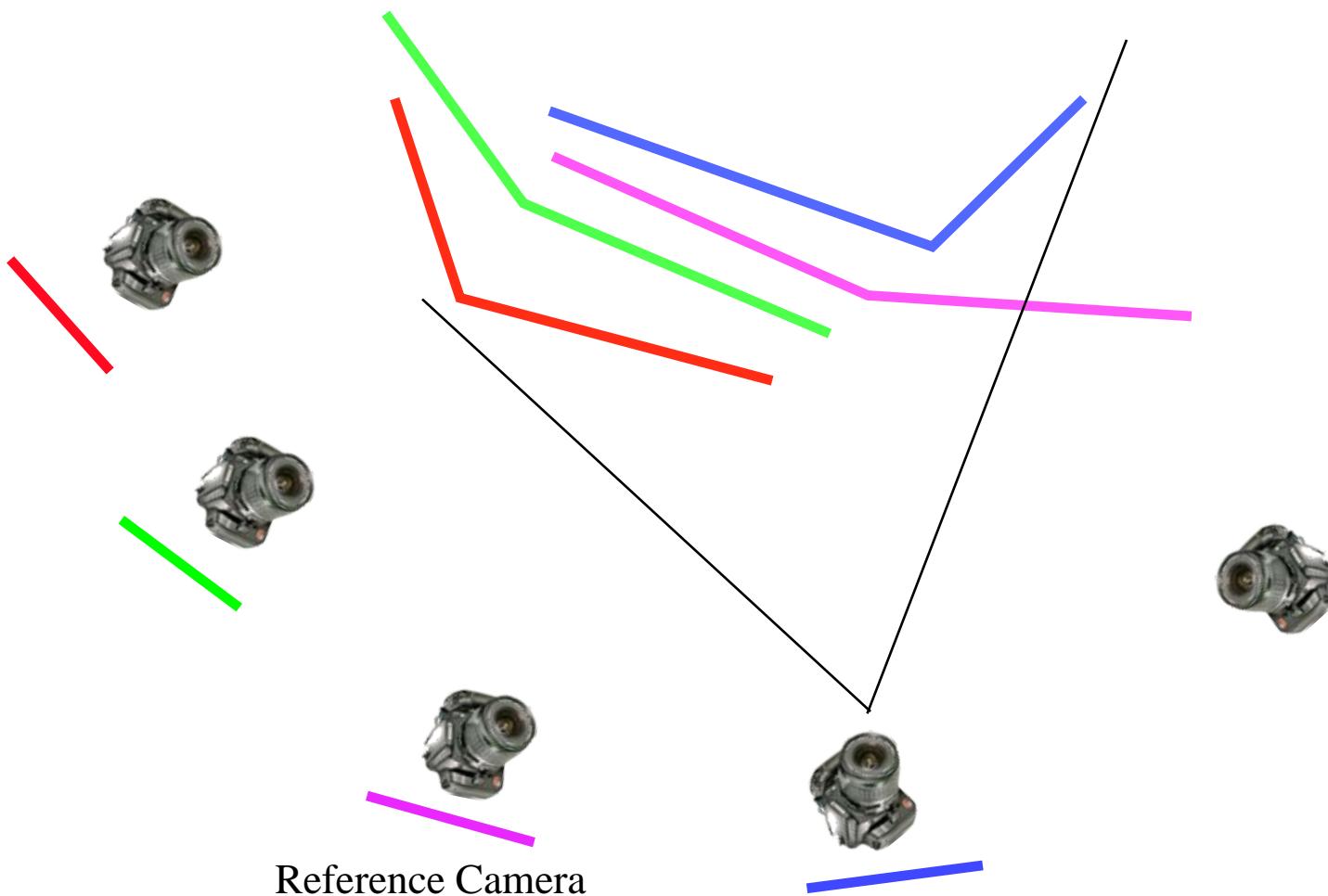


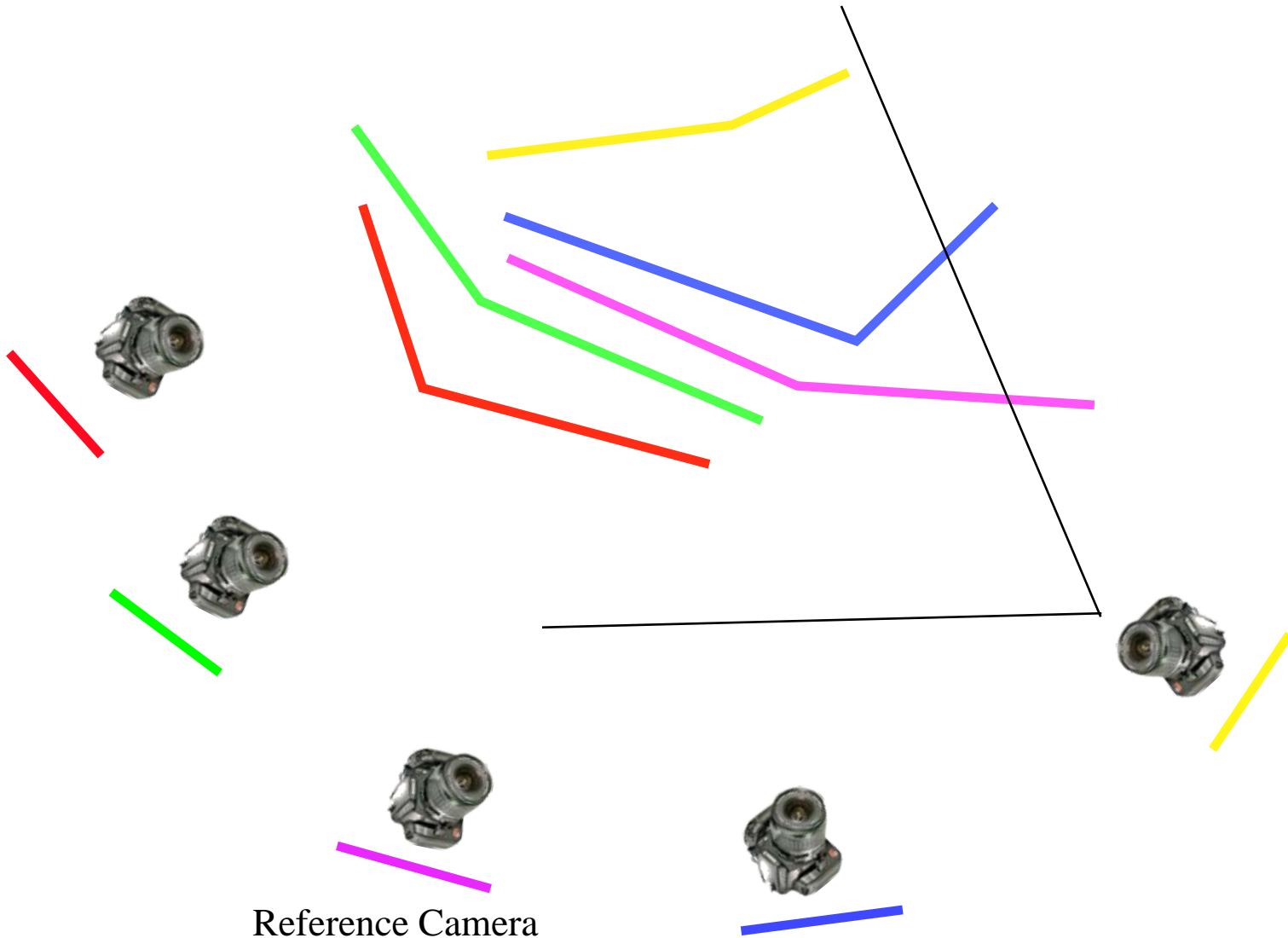
Reference Camera

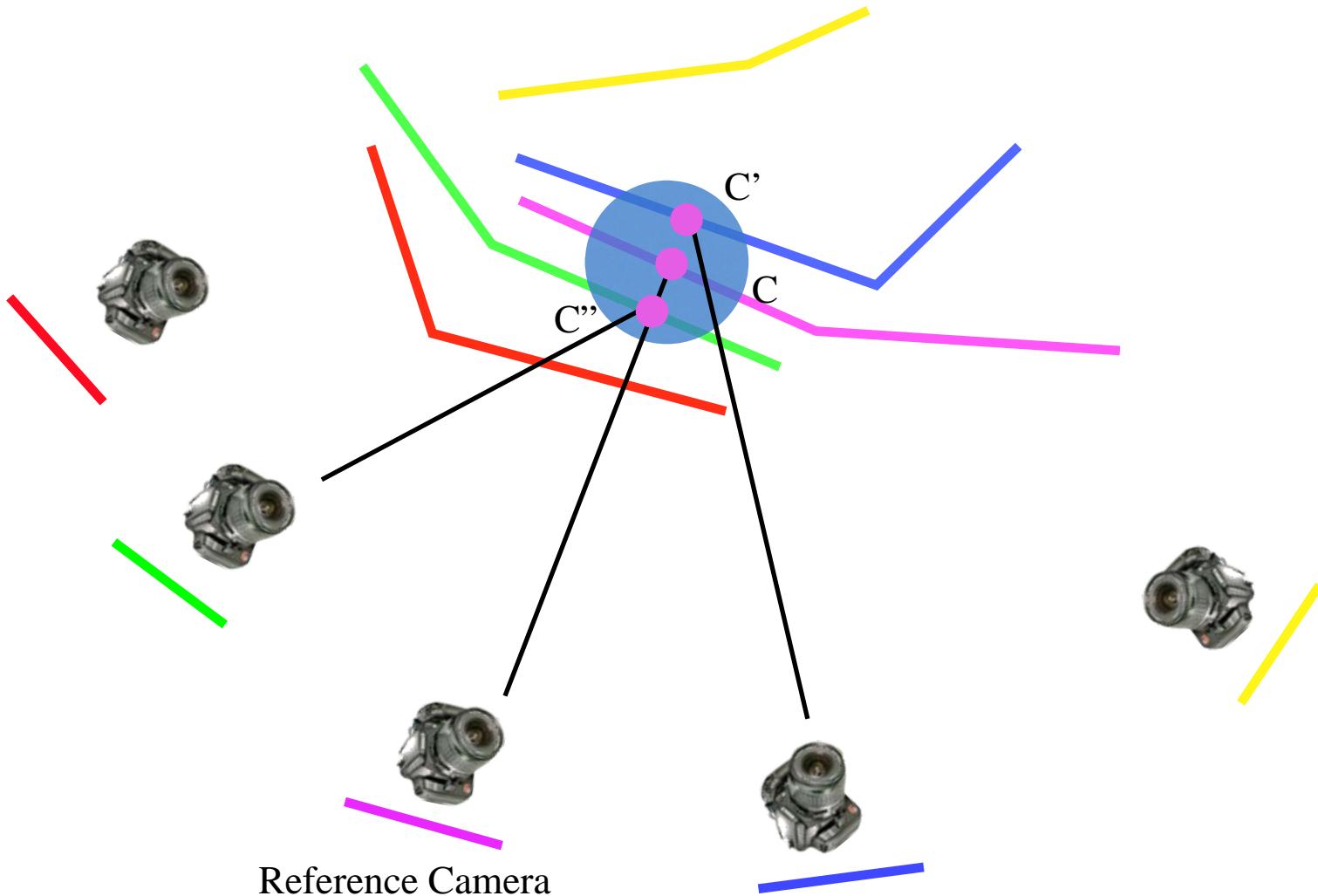


Reference Camera

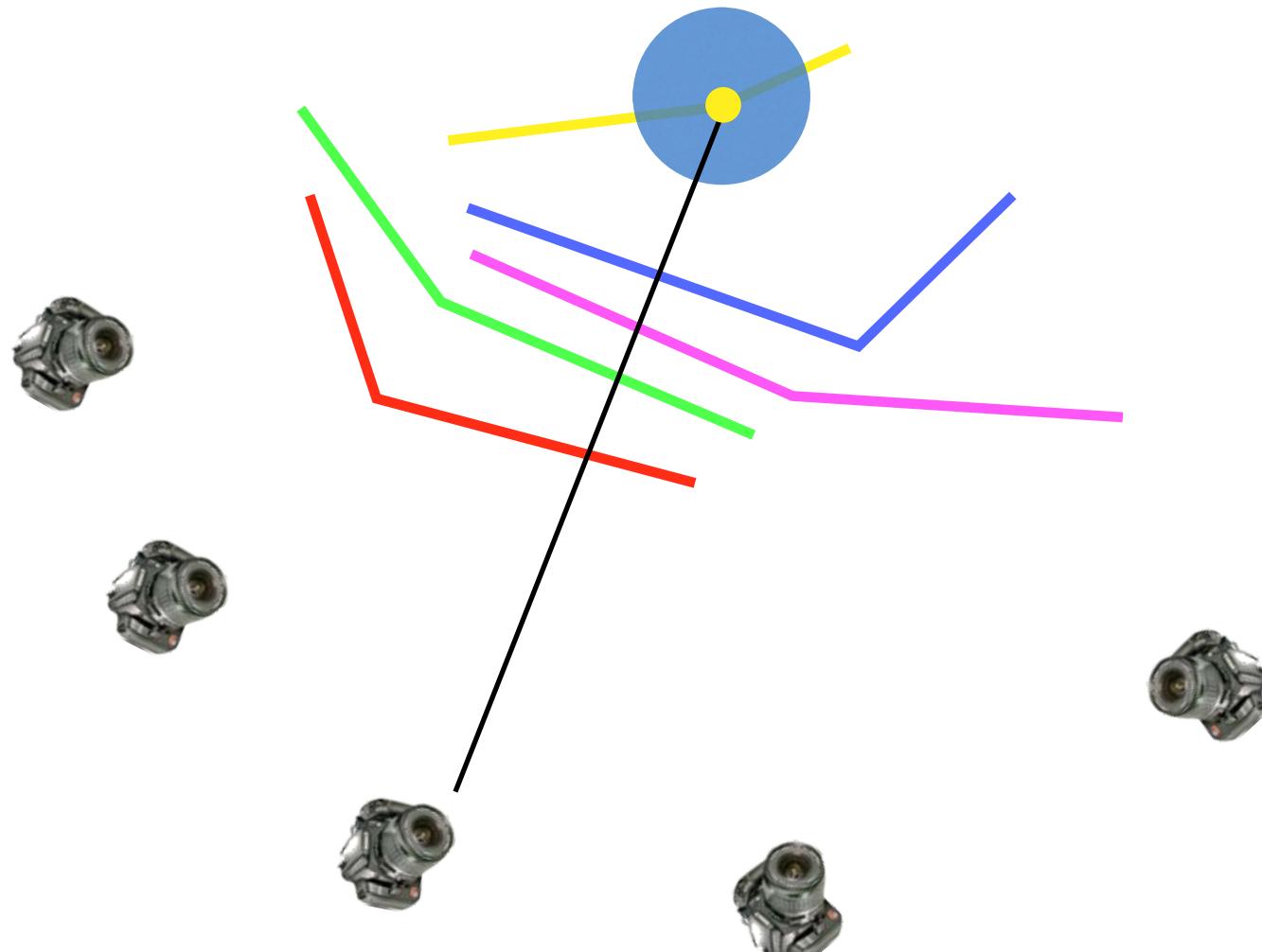




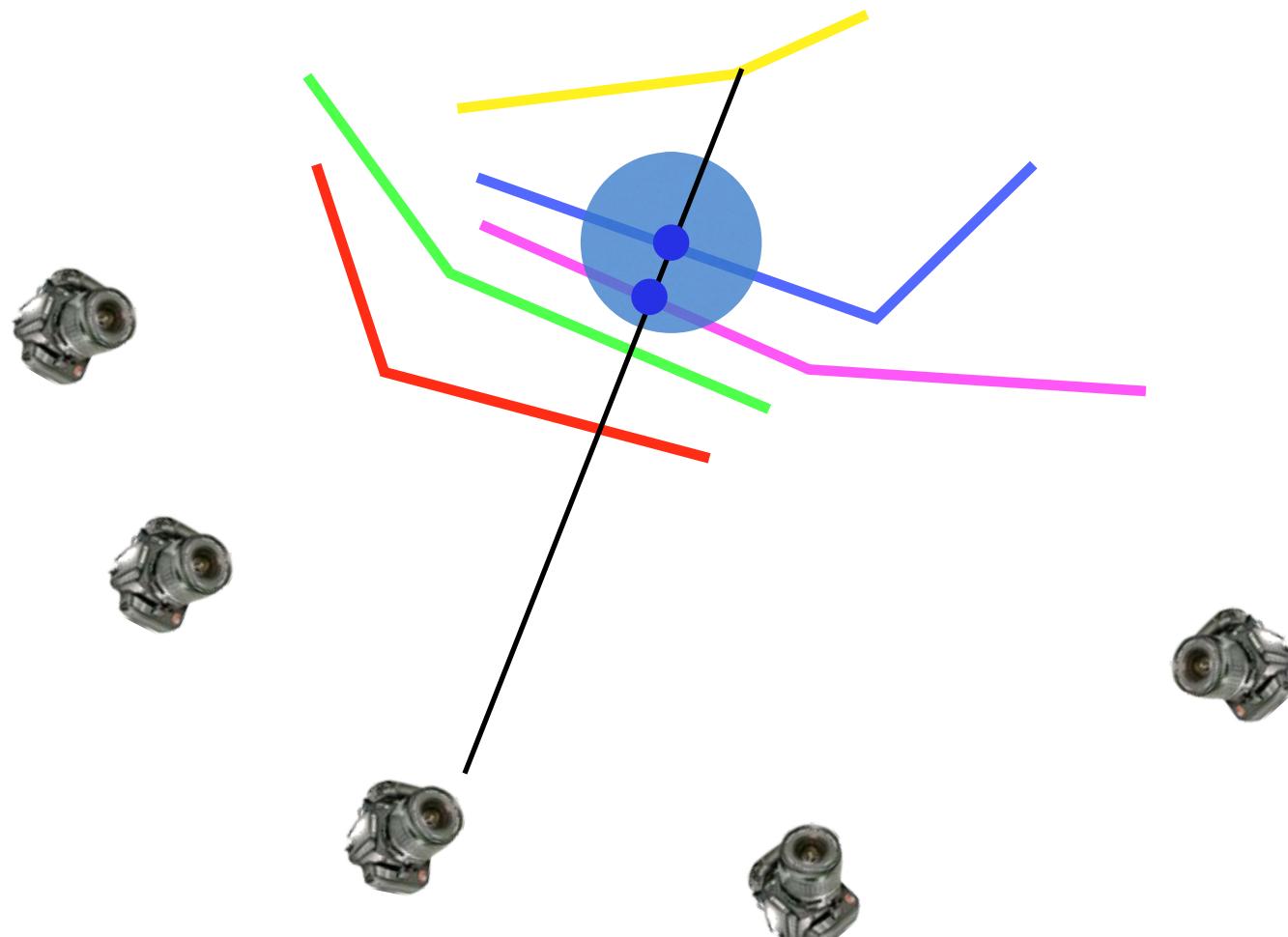




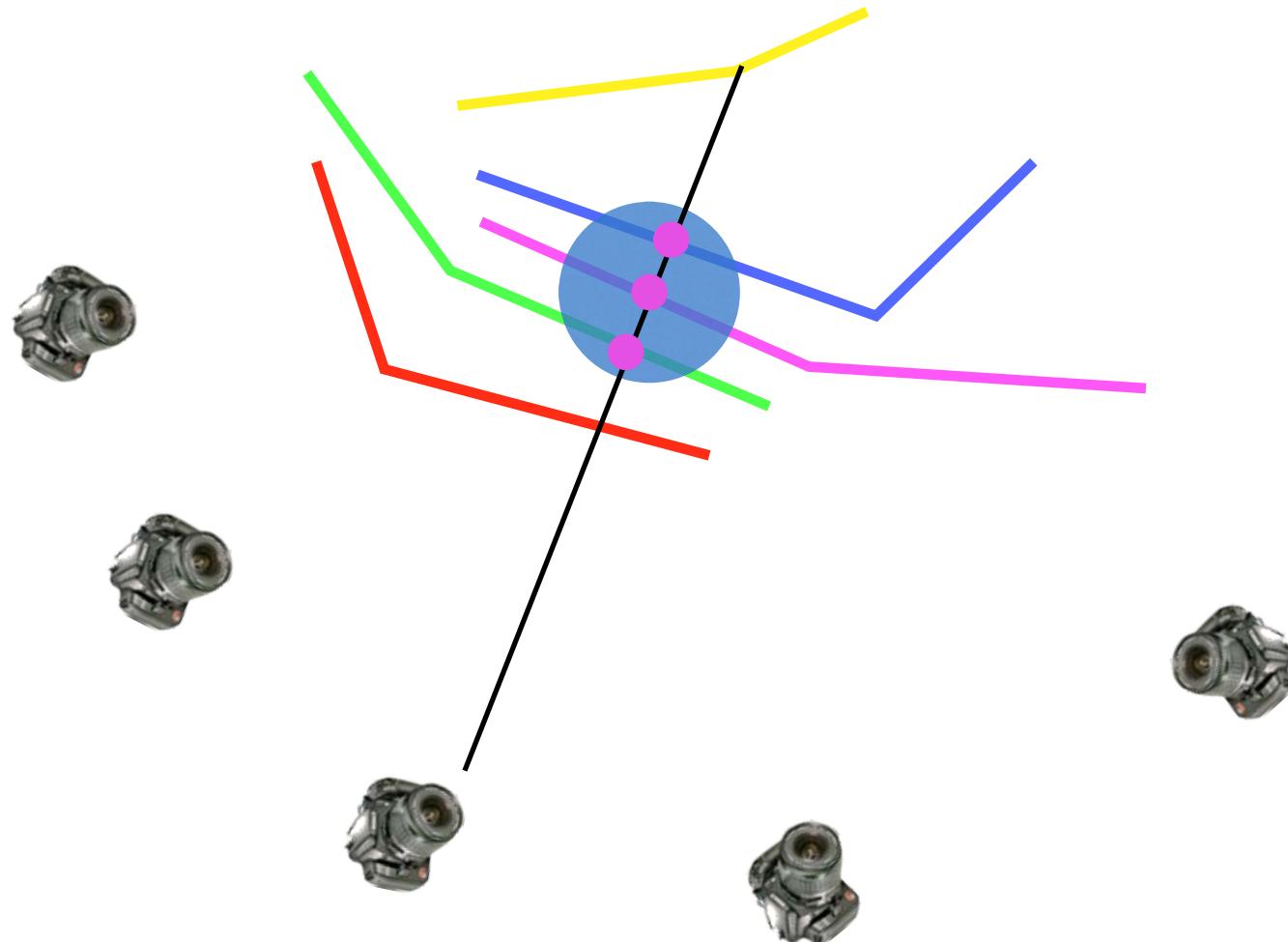
Support is calculated for every depth hypothesis within range determined by geometric uncertainty



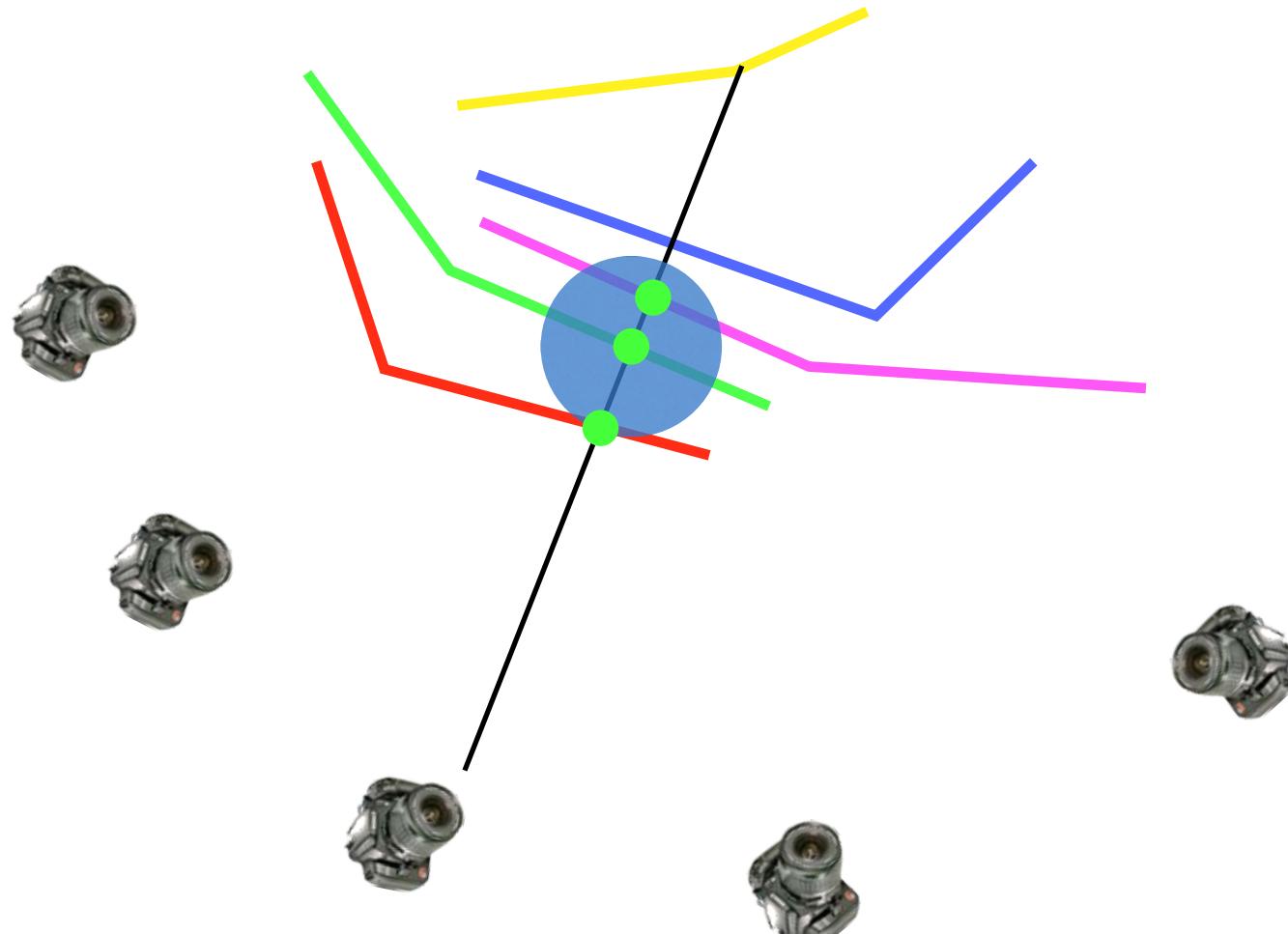
Reference Camera



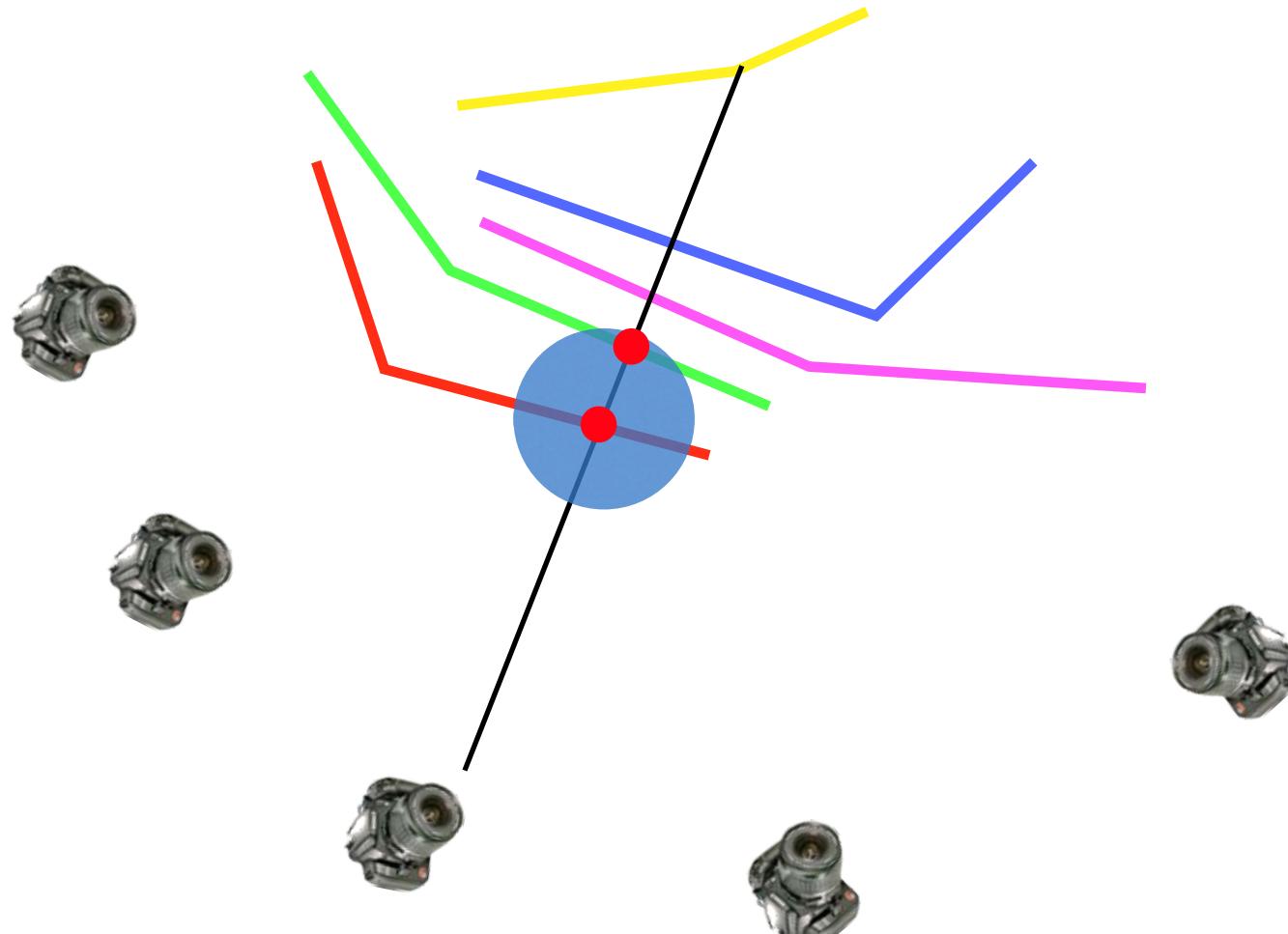
Reference Camera



Reference Camera

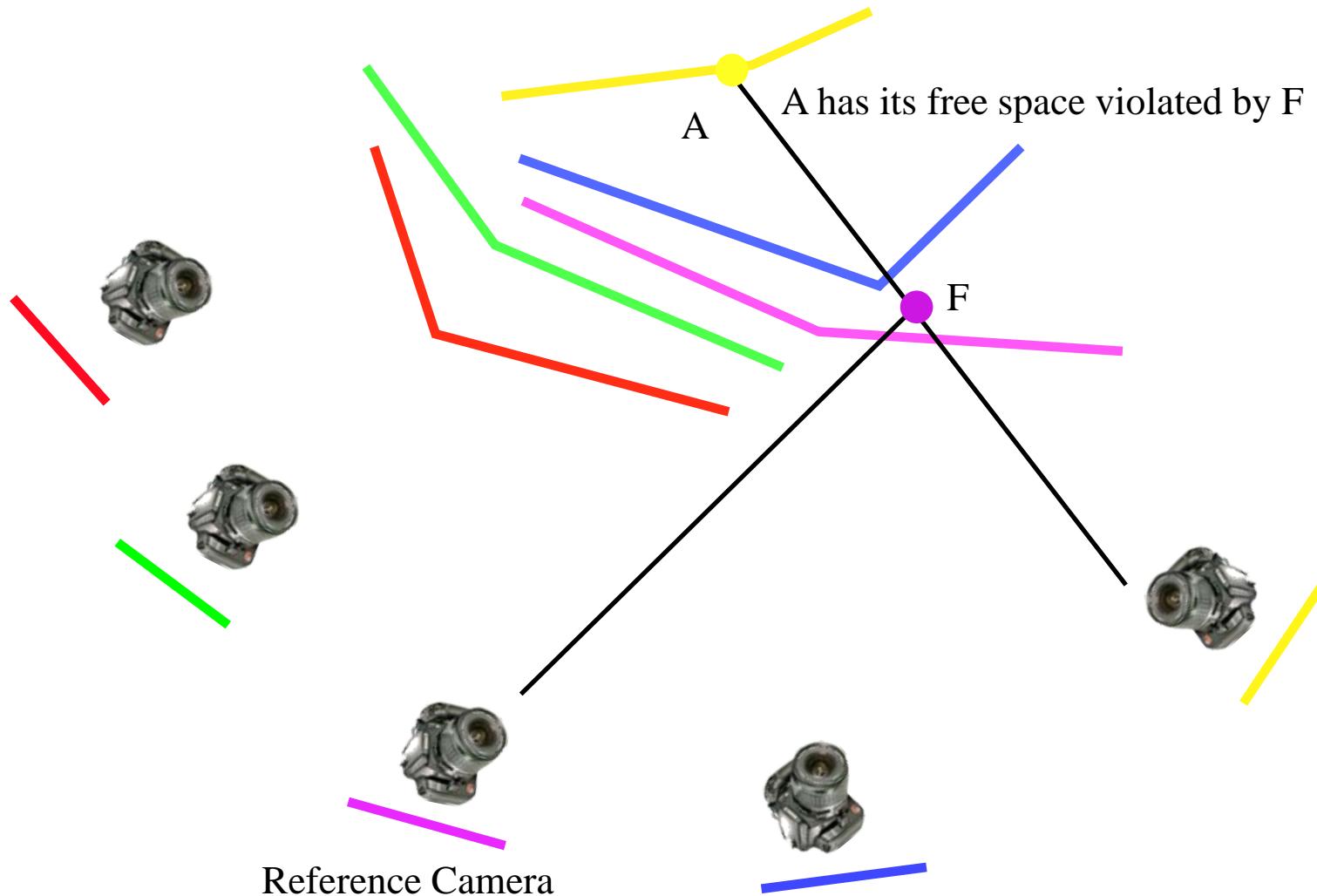


Reference Camera



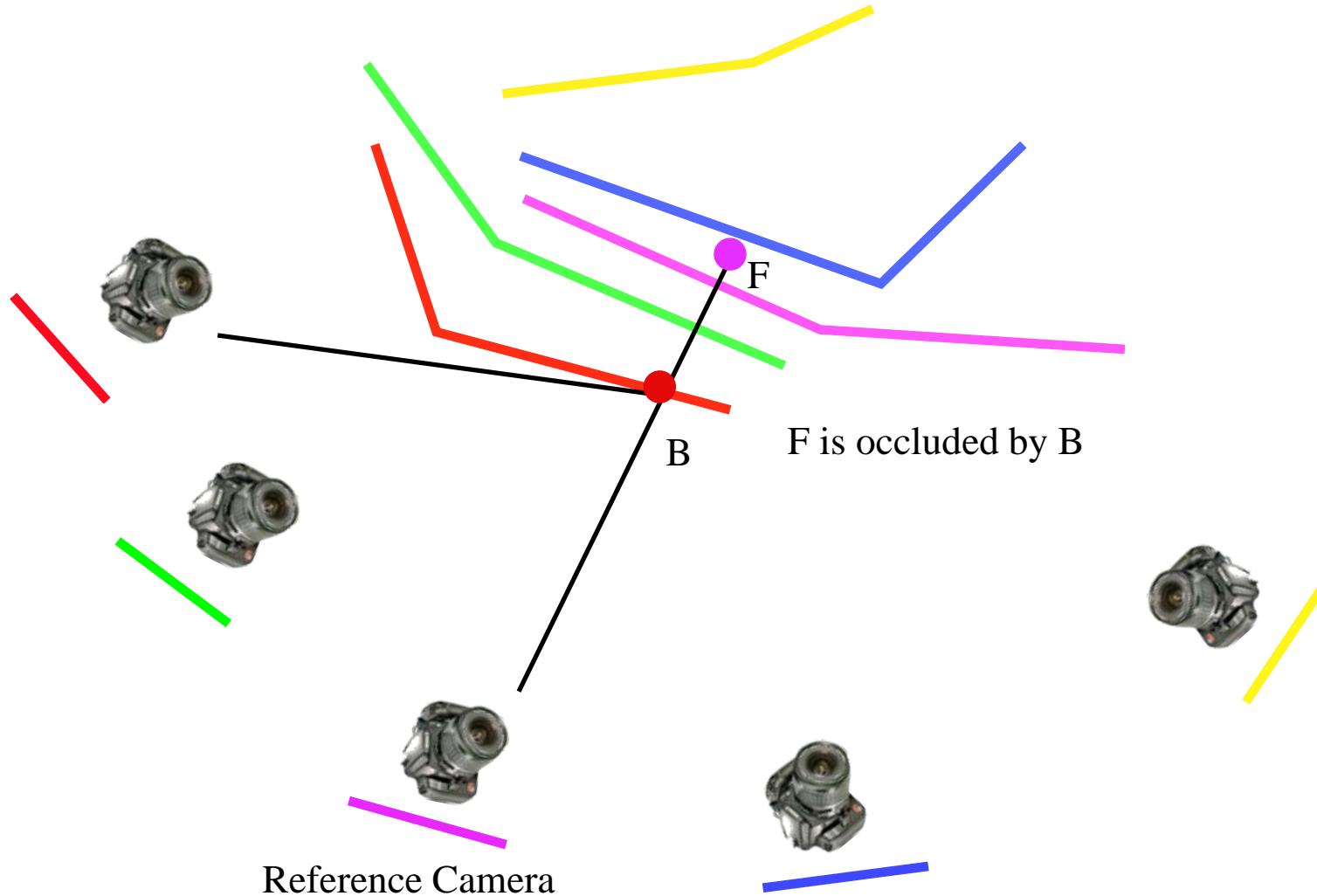
Reference Camera

# Visibility Constraints



Free-space violations occur on rays of target views

# Visibility Constraints



Occlusions occur on rays of the reference view

# Confidence Updates

- Add confidence values of all supporting depth hypotheses
  - Fused depth is weighted average of supporting depths
- Decrease confidence if there are visibility violations

# Hypothesis Selection

- Select blended hypothesis with the highest confidence for each pixel
- The number of supporting depth candidates is also considered
- Holes are filled by median filtering



# Experimental Results

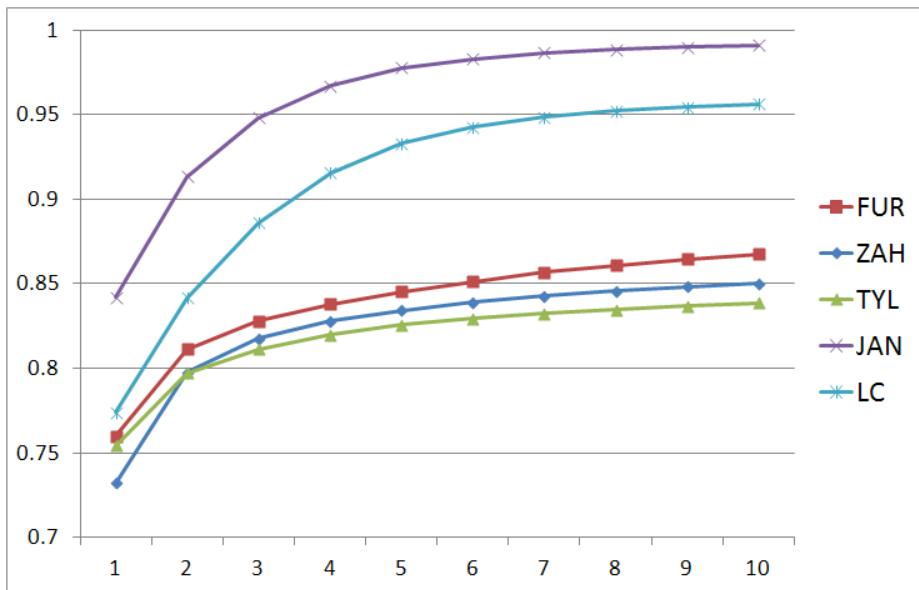
Final fused depth maps are evaluated in terms of absolute errors and relative errors

$$e_{abs} = |Z - Z_{GT}|$$

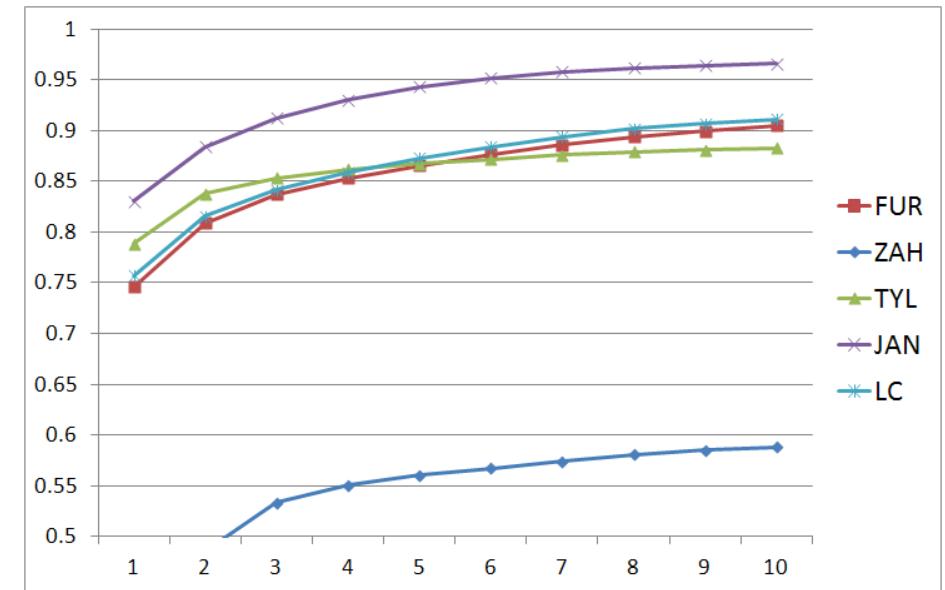
$$e_{rel} = \frac{|Z - Z_{GT}|}{\frac{Z_{GT}^2}{bf}}$$



# Comparison With State of the Art



Relative error of fountain-P11



Relative error of Herz-Jesu-P8

LC: Hu and Mordohai, 2012.

FUR: Y. Furukawa and J. Ponce, 2010.

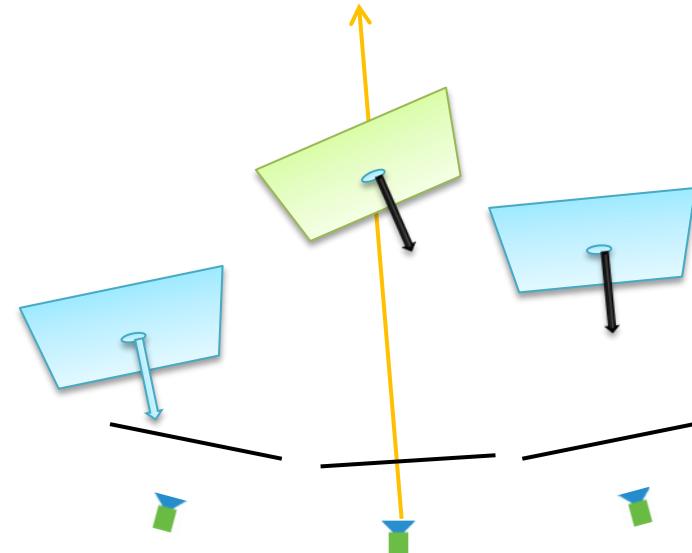
ZAH: A. Zaharescu, E. Boyer, and R. P. Horaud, 2011.

TYL: R. Tylecek and R. Sara, 2010.

JAN: M. Jancosek and T. Pajdla, 2011.

# Representations

- Depth maps
- Point clouds
- Surface patches
- Level sets
- Voxels grids
- Meshes
- ...

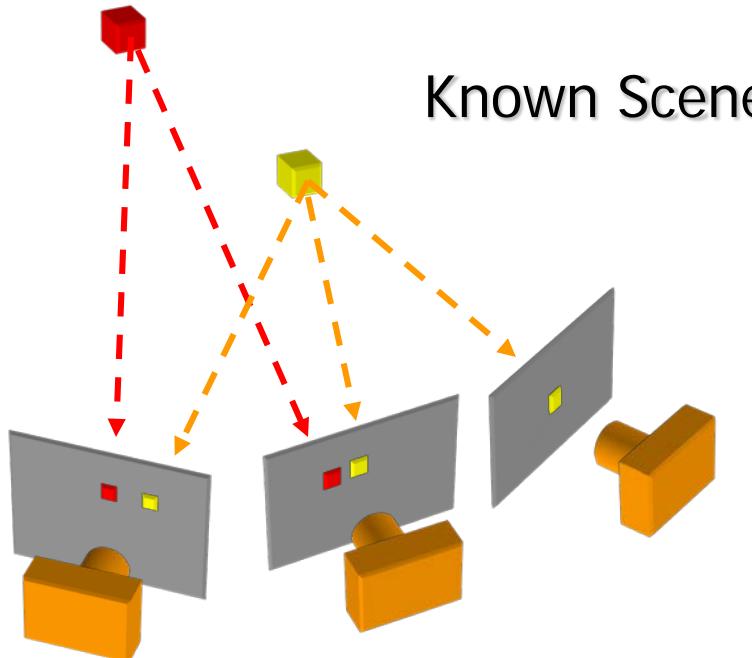


# Depth Maps

- Compact representation
  - 3D quantities (points) can be indexed via pixel coordinates
  - Easy to determine neighborhood relationships and connectivity
  - Plane sweeping can be done very efficiently on GPUs
- Enable straightforward visibility estimation
- Viewpoint dependent
  - Does not allow more than one layer (2 ½ D representation)
  - Viewpoint cannot be altered without revealing holes
- Depth maps are no consistent after fusion
  - They are redundant when they are consistent...

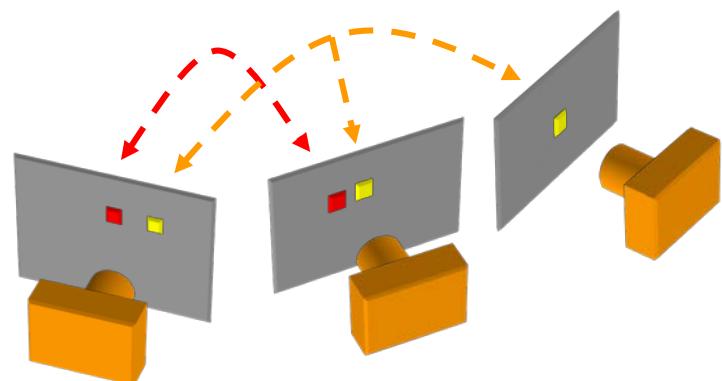
# The Visibility Problem

- Which points are visible in which images?



Known Scene

Unknown Scene



*Forward Visibility*

*Inverse Visibility*

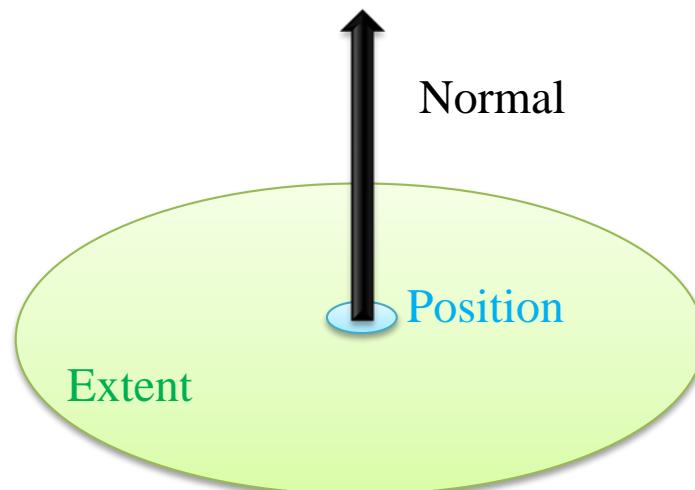
# Patch-based MVS (PMVS)

Y. Furukawa and J. Ponce (PAMI 2010)



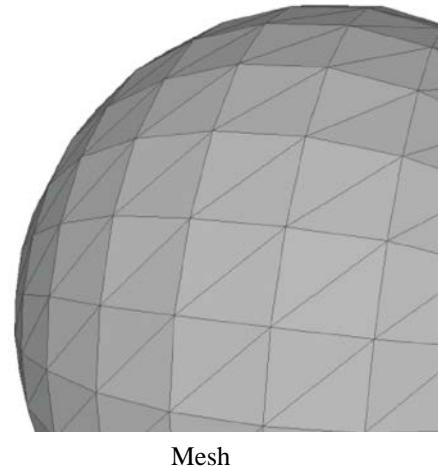
# What is a Patch?

- Patch consists of
  - Position ( $x, y, z$ )
  - Normal ( $n_x, n_y, n_z$ )
  - Extent (*radius*)
- Tangent plane approximation

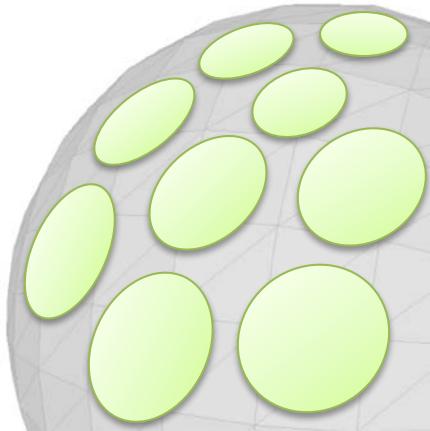
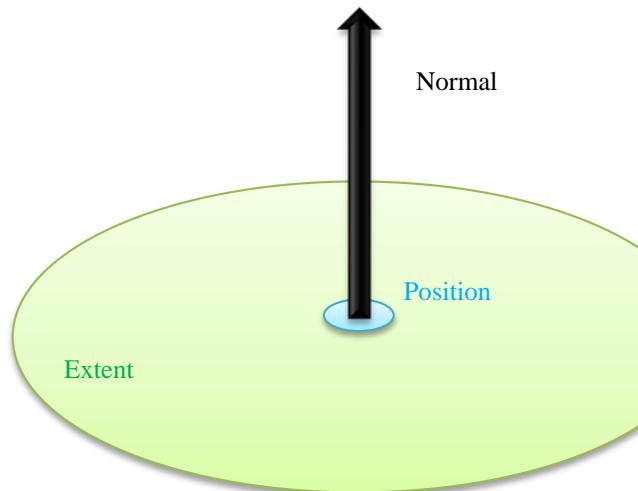


# What is a Patch?

- Patch consists of
  - Position ( $x, y, z$ )
  - Normal ( $nx, ny, nz$ )
  - Extent (*radius*)
- Tangent plane approximation



Mesh



# Why Patches?

- Flexible



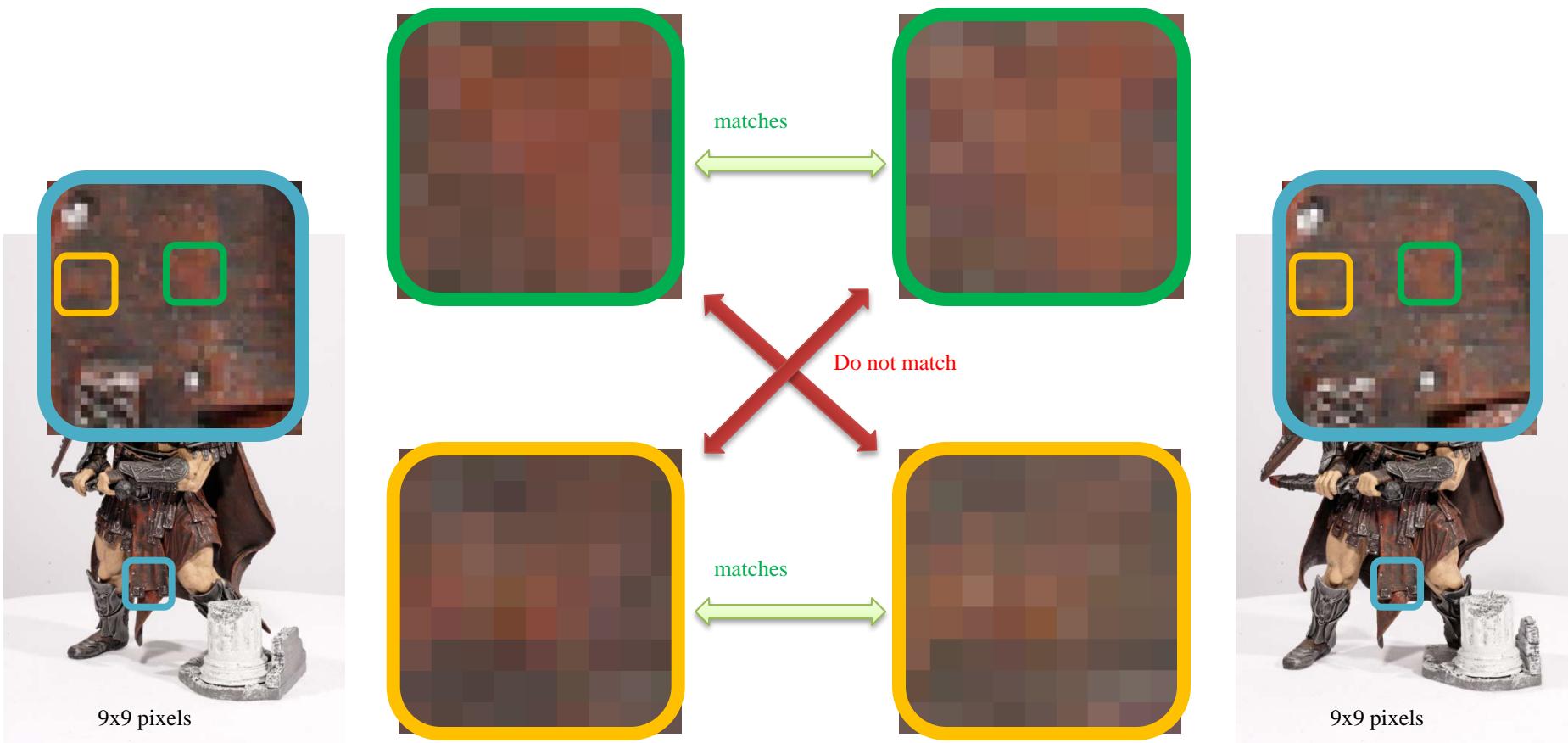
# Why Patches?

- Flexible  $\longleftrightarrow$  Hard to enforce regularization



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- Flexible  $\longleftrightarrow$  Hard to enforce regularization



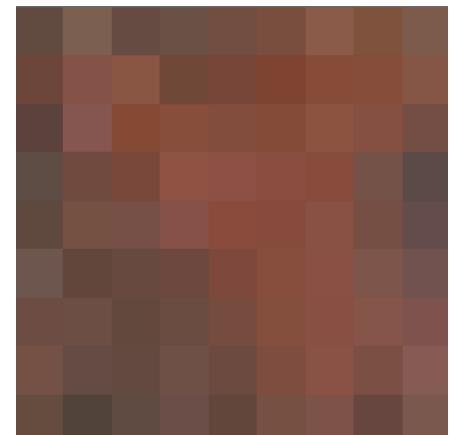
# Why Patches?

- Flexible  $\longleftrightarrow$  Hard to enforce regularization

Regularization not really necessary

because

Local image patch is descriptive enough



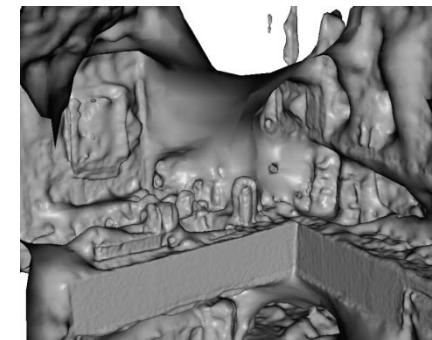
9x9 pixels

# Why Patches?

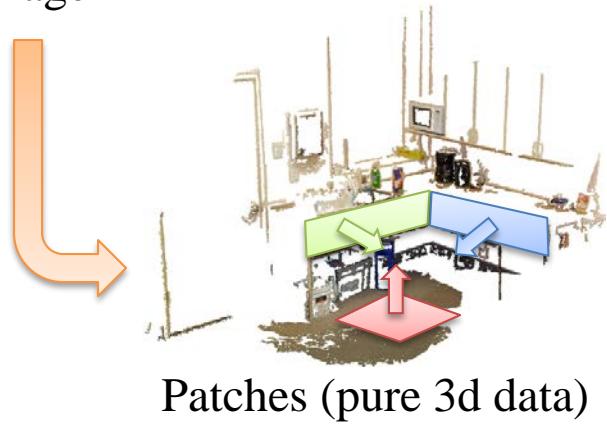
- Pure 3d data w/o interpolation



Meshing w/  
standard interpolation



Image



Scene analysis from  
pure 3d data



Meshing w/  
smart interpolation

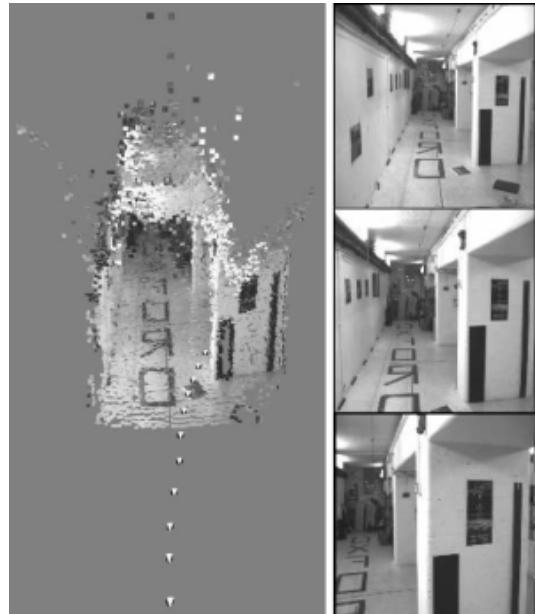
# By the way...

- Depthmap-fusion
  - is also “flexible”
  - can also extract pure 3d data

# Patches vs. Multiple Depth Maps (according to Y. Furukawa)

- Patches → Single global 3D model  
Depthmaps → Multiple redundant 3D models
- Patches → Clean 3D points  
Depthmaps → Noisy without merging
- Patches → Hard to compute fast  
Depthmaps → Easy to compute fast

# Patch-based MVS



[Lhuillier and Quan,  
PAMI 05]



[Furukawa and Ponce,  
CVPR 07 and PAMI 2010]

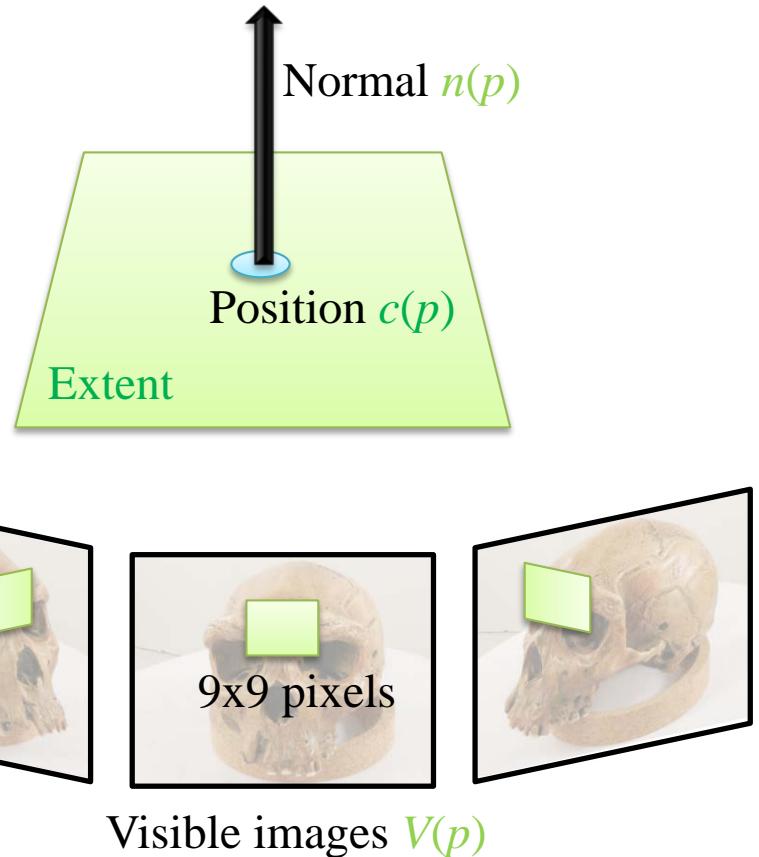


[Habbecke and Kobbelt,  
CVPR 07]



# Patch Definition

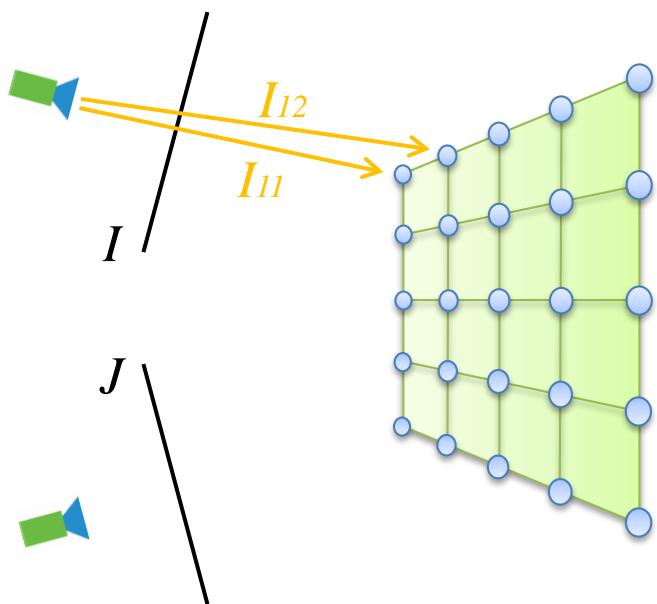
- Patch  $p$  is defined by
  - Position  $c(p)$
  - Normal  $n(p)$
  - Visible images  $V(p)$
- Extent is set so that  $p$  is roughly 9x9 pixels in  $V(p)$



# Photo-consistency

- Photo-consistency  $N(I, J, p)$  of  $p$  between two images  $I$  and  $J$

$I_{xy}$ : pixel color in image  $I$



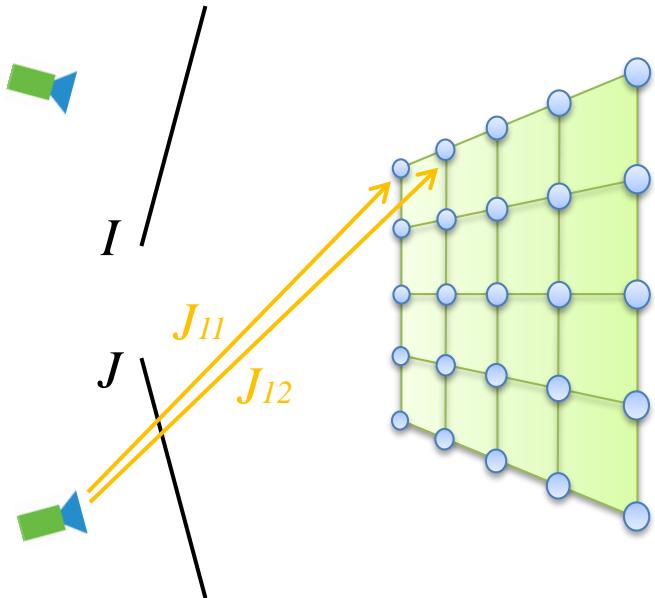
# Photo-consistency

- Photo-consistency  $N(I, J, p)$  of  $p$  between two images  $I$  and  $J$

$I_{xy}$ : pixel color in image  $I$

$J_{xy}$ : pixel color in image  $J$

$$N(I, J, p) = \frac{\sum (I_{xy} - \bar{I}_{xy}) \cdot (J_{xy} - \bar{J}_{xy})}{\sqrt{(I_{xy} - \bar{I}_{xy})^2} \sqrt{(J_{xy} - \bar{J}_{xy})^2}}$$



# Photo-consistency

- Photo-consistency  $N(I, J, p)$  of  $p$  between two images  $I$  and  $J$

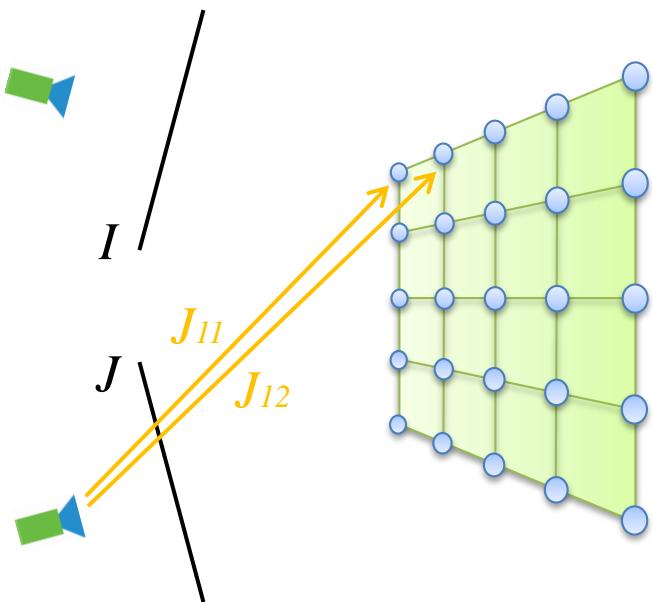
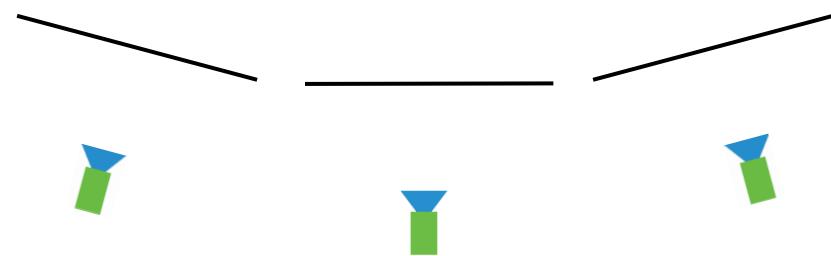
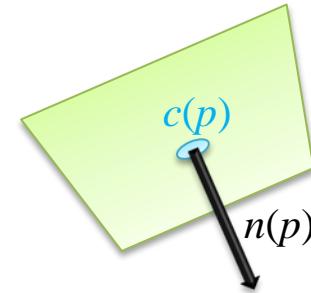


Photo-consistency  $N(p)$  of  $p$  with visible images  $V(p) = \{I_1, I_2, \dots, I_n\}$

$$N(p) = \frac{\sum_{i=1}^n \sum_{j=i+1}^n N(I_i, I_j, p)}{(n+1)n/2}$$

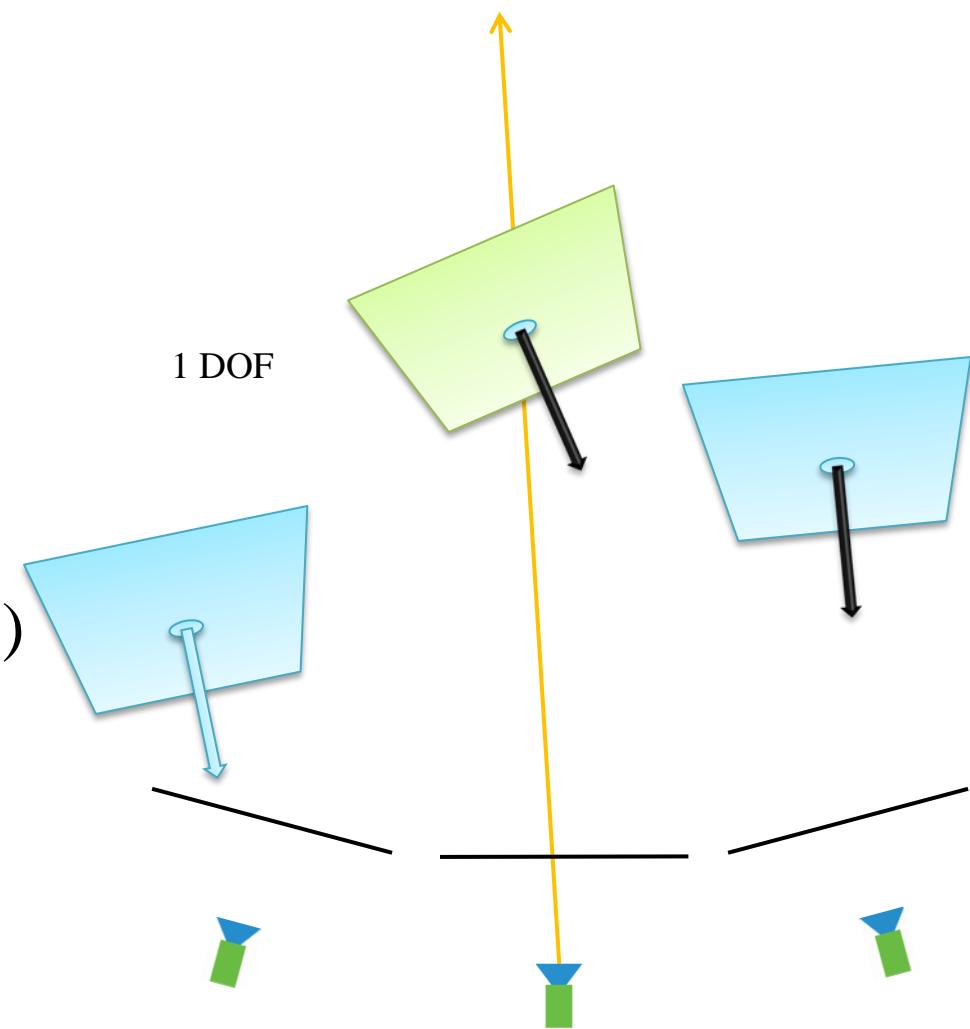
# Reconstruct Patch $p$

- Given initial estimates of
  - Position  $c(p)$
  - Normal  $n(p)$
  - Visible images  $V(p)$
- $\{c(p), n(p)\} = \arg \max_{\{c(p), n(p)\}} N(p)$



# Reconstruct Patch $p$

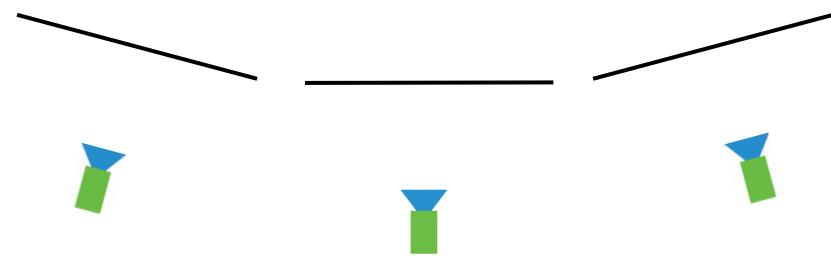
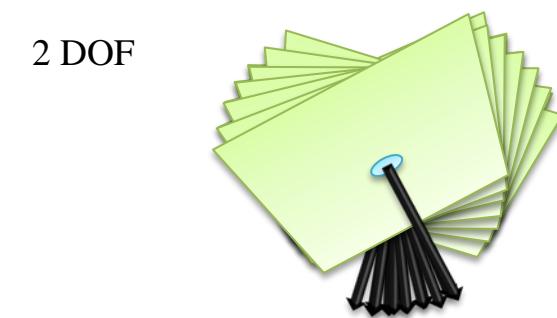
- Given initial estimates of
  - Position  $c(p)$
  - Normal  $n(p)$
  - Visible images  $V(p)$
- $\{c(p), n(p)\} = \arg \max_{\{c(p), n(p)\}} N(p)$



# Reconstruct Patch $p$

- Given initial estimates of
  - Position  $c(p)$
  - Normal  $n(p)$
  - Visible images  $V(p)$
- $\{c(p), n(p)\} = \arg \max_{\{c(p), n(p)\}} N(p)$

2 DOF



# Verify a Patch

- Textures may match by accident
- Photo-consistency must be reasonably high
- Verification process
  - Keep only high photo-consistency images in  $V(p)$
  - Accept if  $|V(p)| \geq 3$

# Update $V(p)$

$V(p) = \{ \text{Image1}, \text{Image2}, \cancel{\text{Image3}}, \text{Image4} \}$



Image1

Image2



Image4

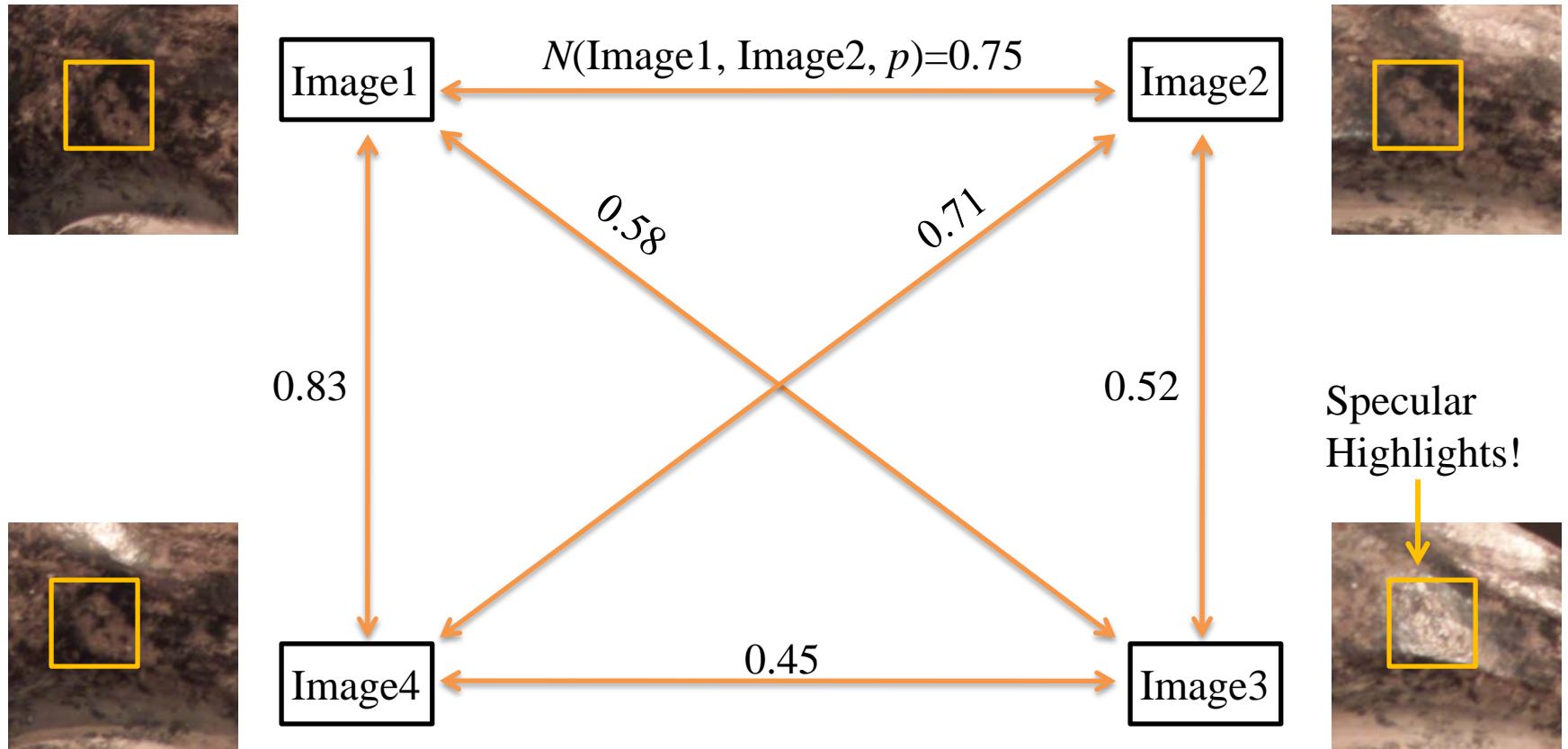
Image3



Specular  
Highlights!

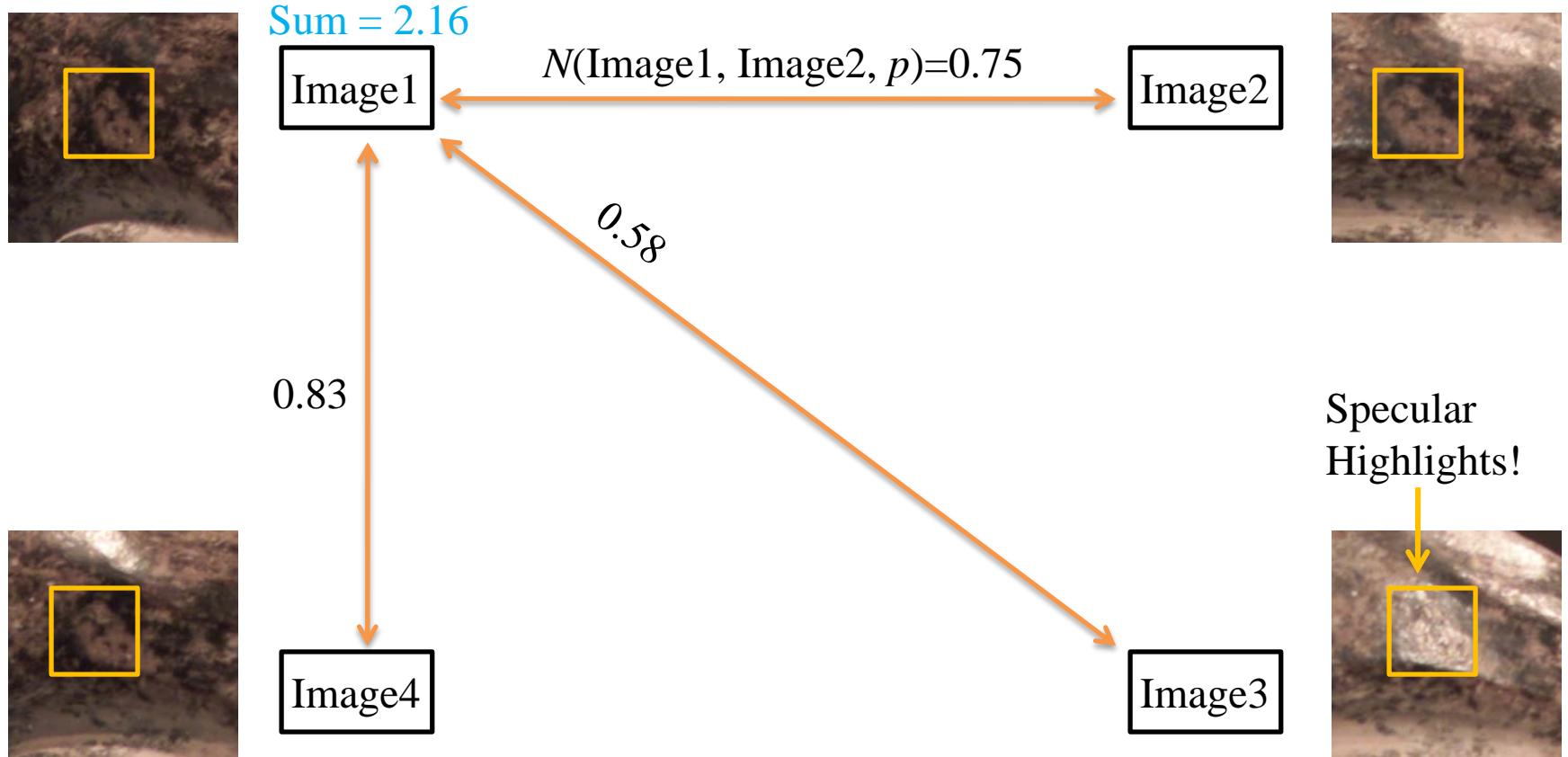
# Update $V(p)$

$$V(p) = \{ \text{Image1}, \text{Image2}, \text{Image3}, \text{Image4} \}$$



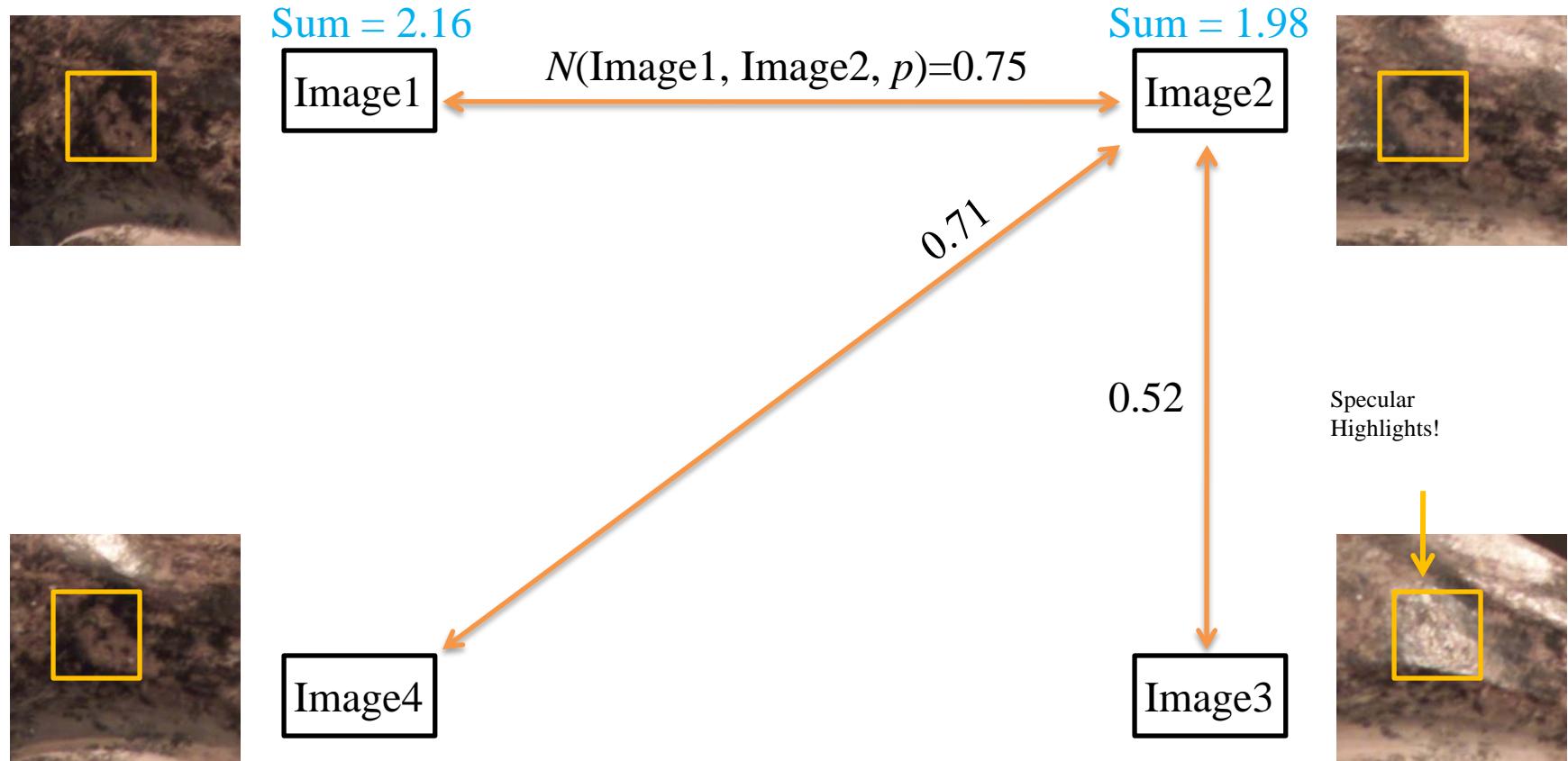
# Update $V(p)$

$V(p) = \{ \text{Image1}, \text{Image2}, \text{Image3}, \text{Image4} \}$



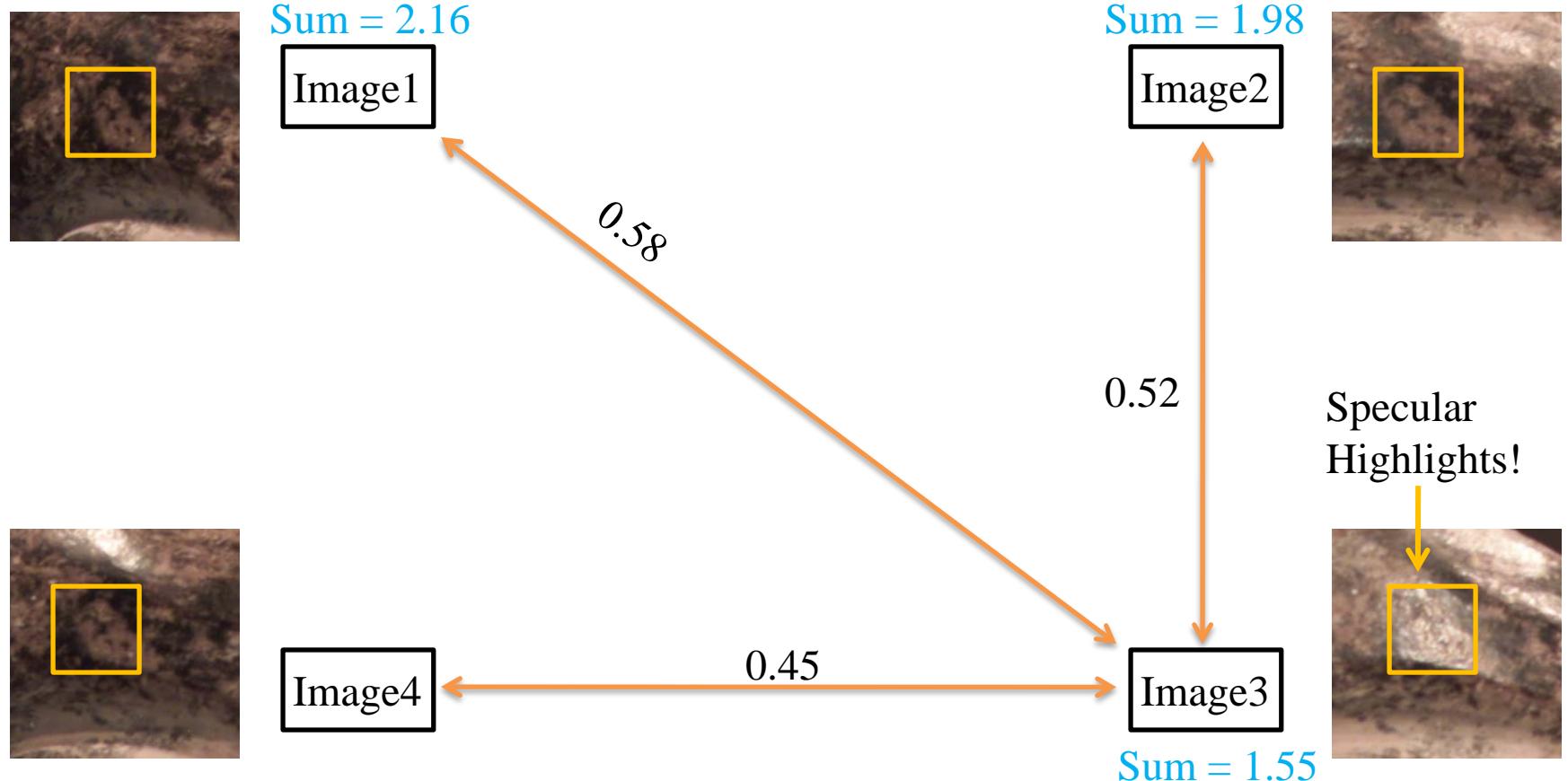
# Update $V(p)$

$V(p) = \{ \text{Image1}, \text{Image2}, \text{Image3}, \text{Image4} \}$



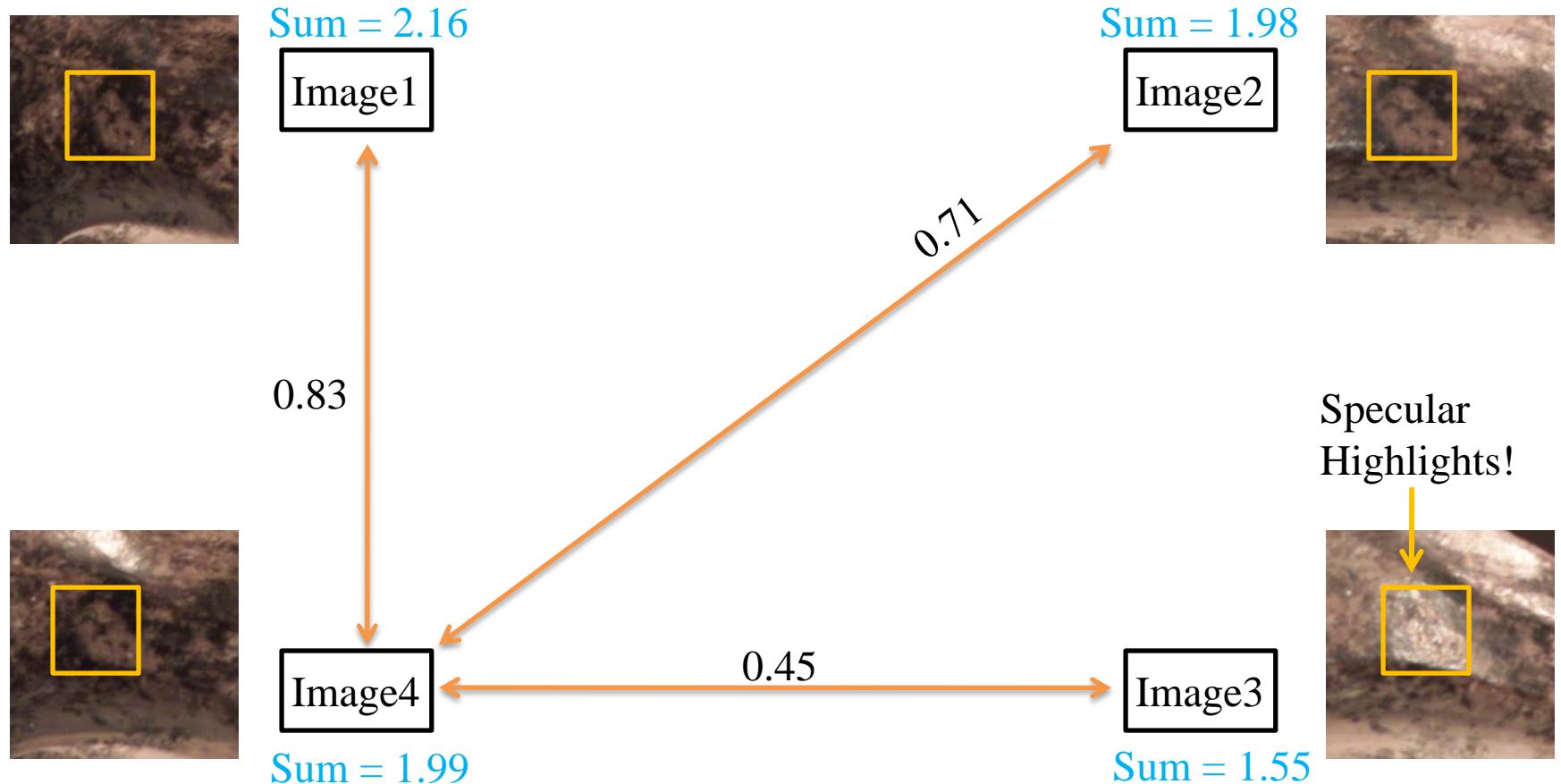
# Update $V(p)$

$V(p) = \{ \text{Image1}, \text{Image2}, \text{Image3}, \text{Image4} \}$



# Update $V(p)$

$V(p) = \{ \text{Image1}, \text{Image2}, \text{Image3}, \text{Image4} \}$



# Update $V(p)$

$V(p) = \{ \text{Image1}, \text{Image2}, \text{Image3}, \text{Image4} \}$



Sum = 2.16

Image1

Sum = 1.98

Image2

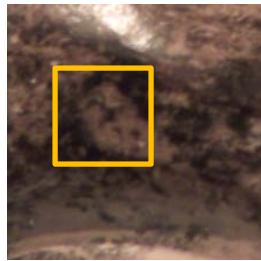


Image4

Sum = 1.99



Image3

Sum = 1.55

# Update $V(p)$

$V(p) = \{ \text{Image1}, \text{Image2}, \text{Image3}, \text{Image4} \}$



Sum = 2.16

Image1

Image2



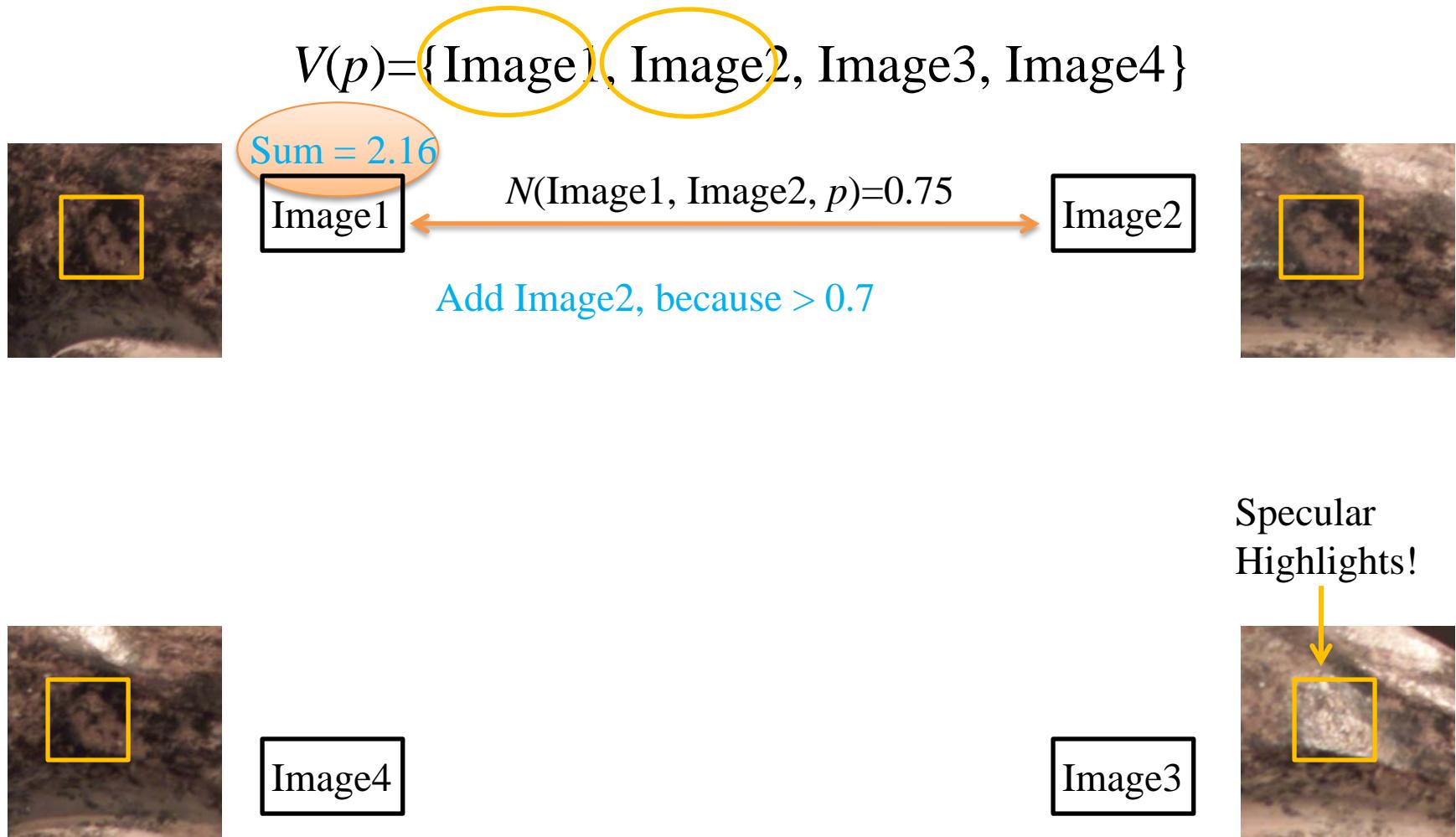
Image4

Image3

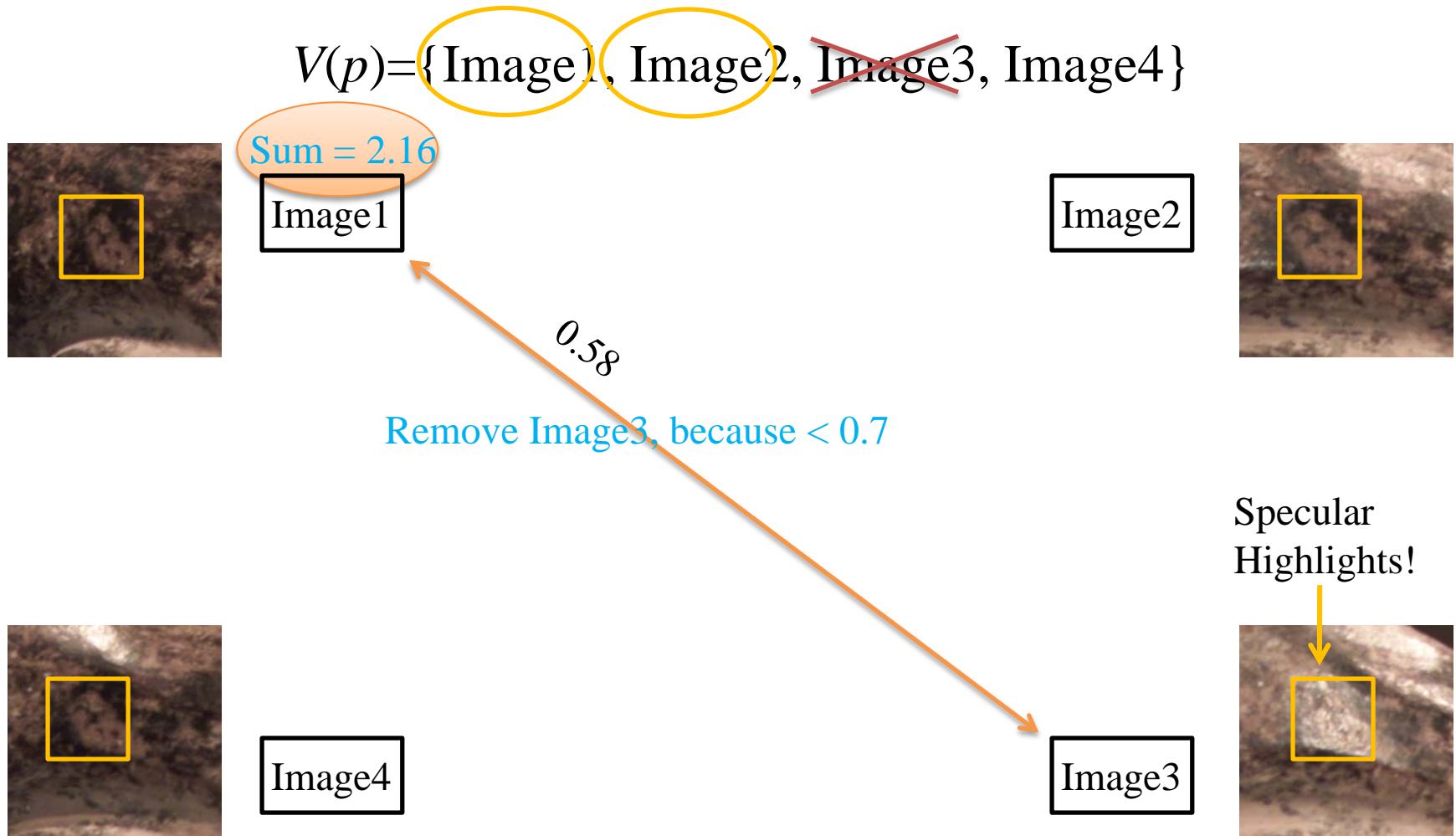


Specular  
Highlights!

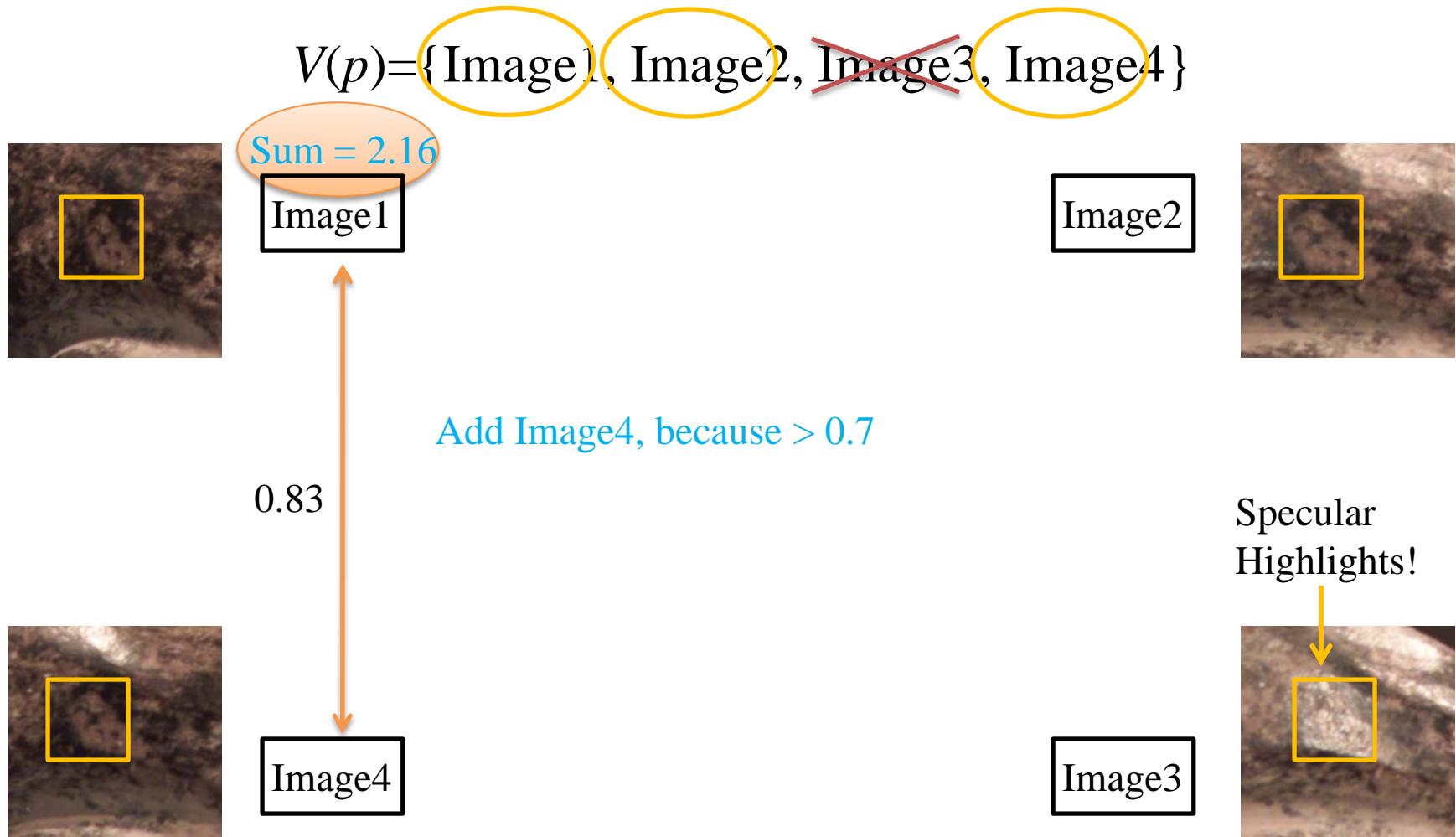
# Update $V(p)$



# Update $V(p)$



# Update $V(p)$

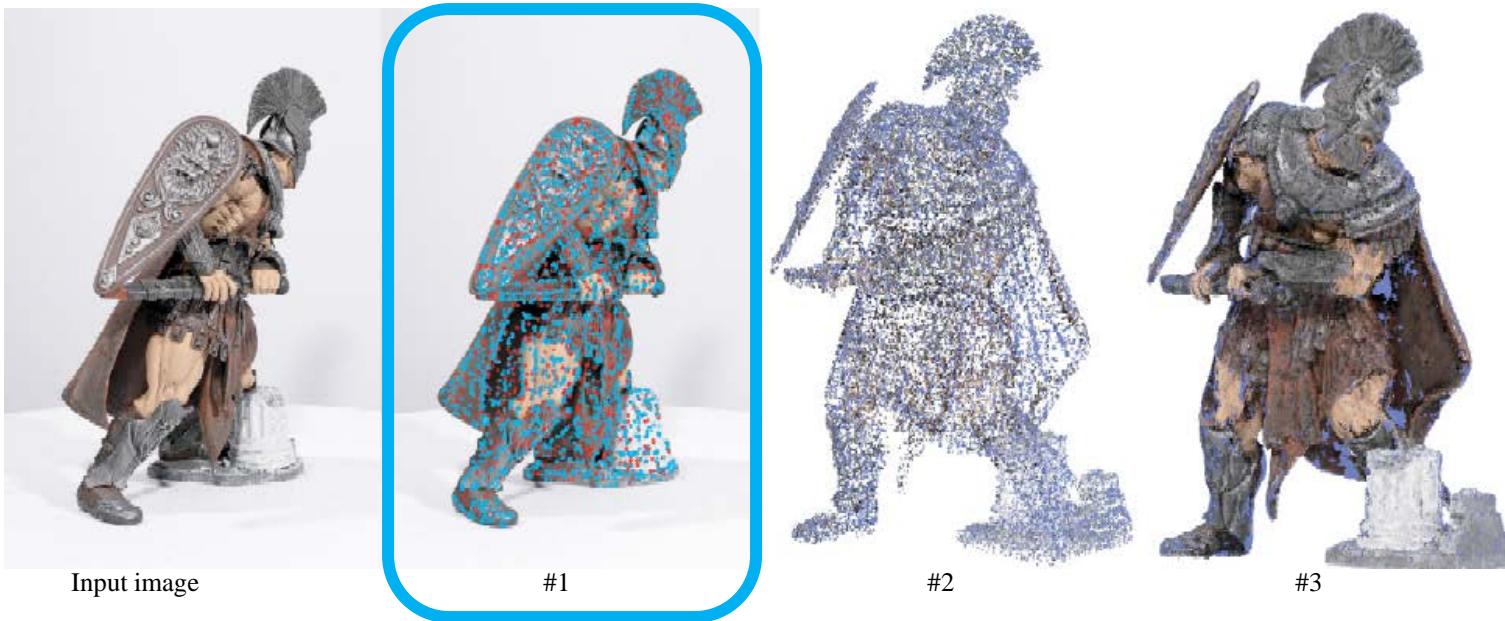


# Algorithm Overview

#1. Feature detection

#2. Initial feature matching

#3. Patch expansion and filtering



# Feature Detection

- Extract local maxima of
  - Harris corner detector (corners)
  - Difference of Gaussian (blobs)

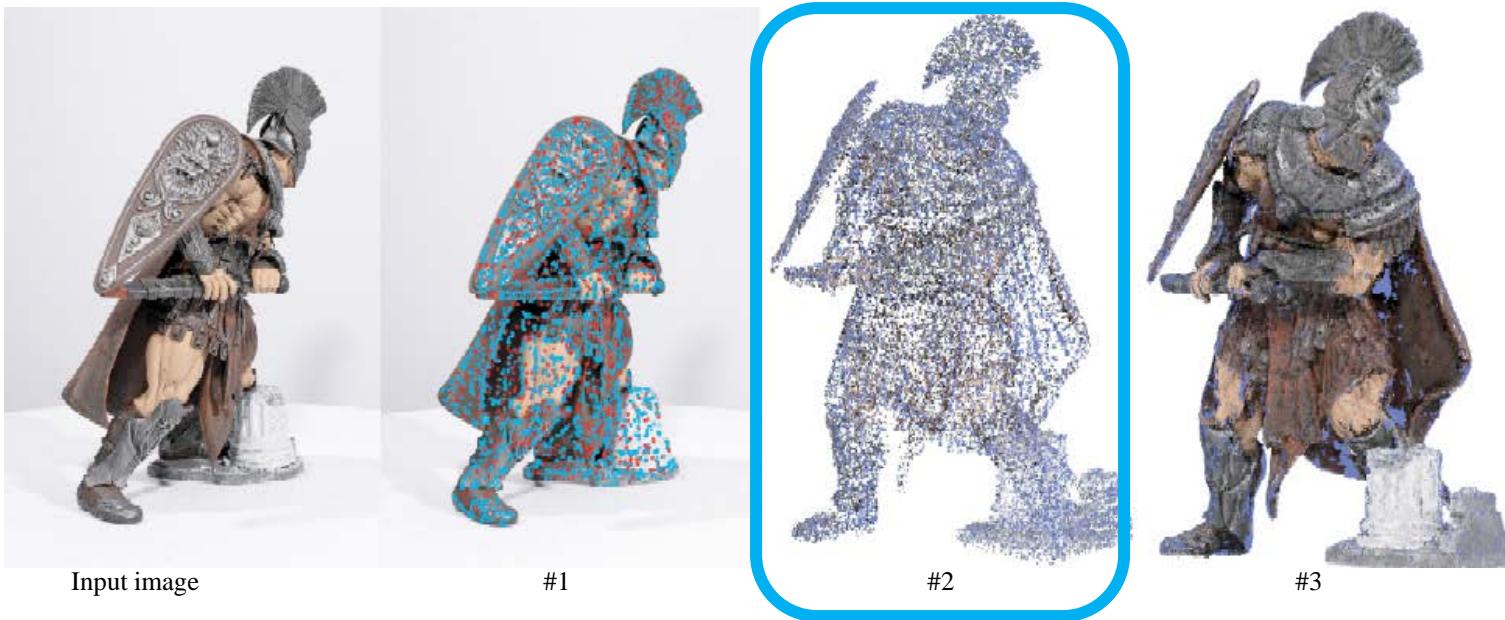


# Algorithm Overview

#1. Feature detection

**#2. Initial feature matching**

#3. Patch expansion and filtering

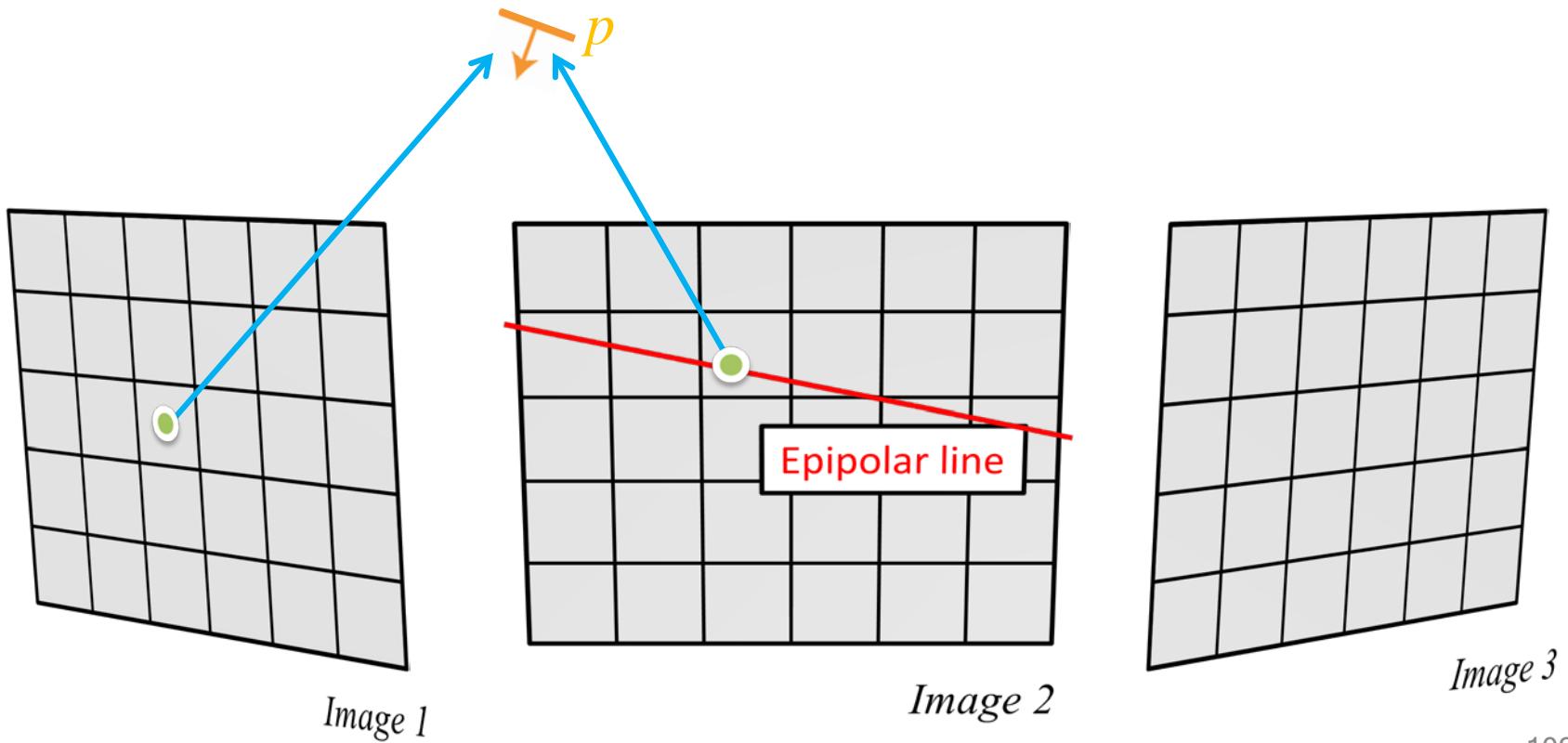


# Initial feature matching

$c(p)$ : triangulation

$n(p)$ :

$V(p)$ :

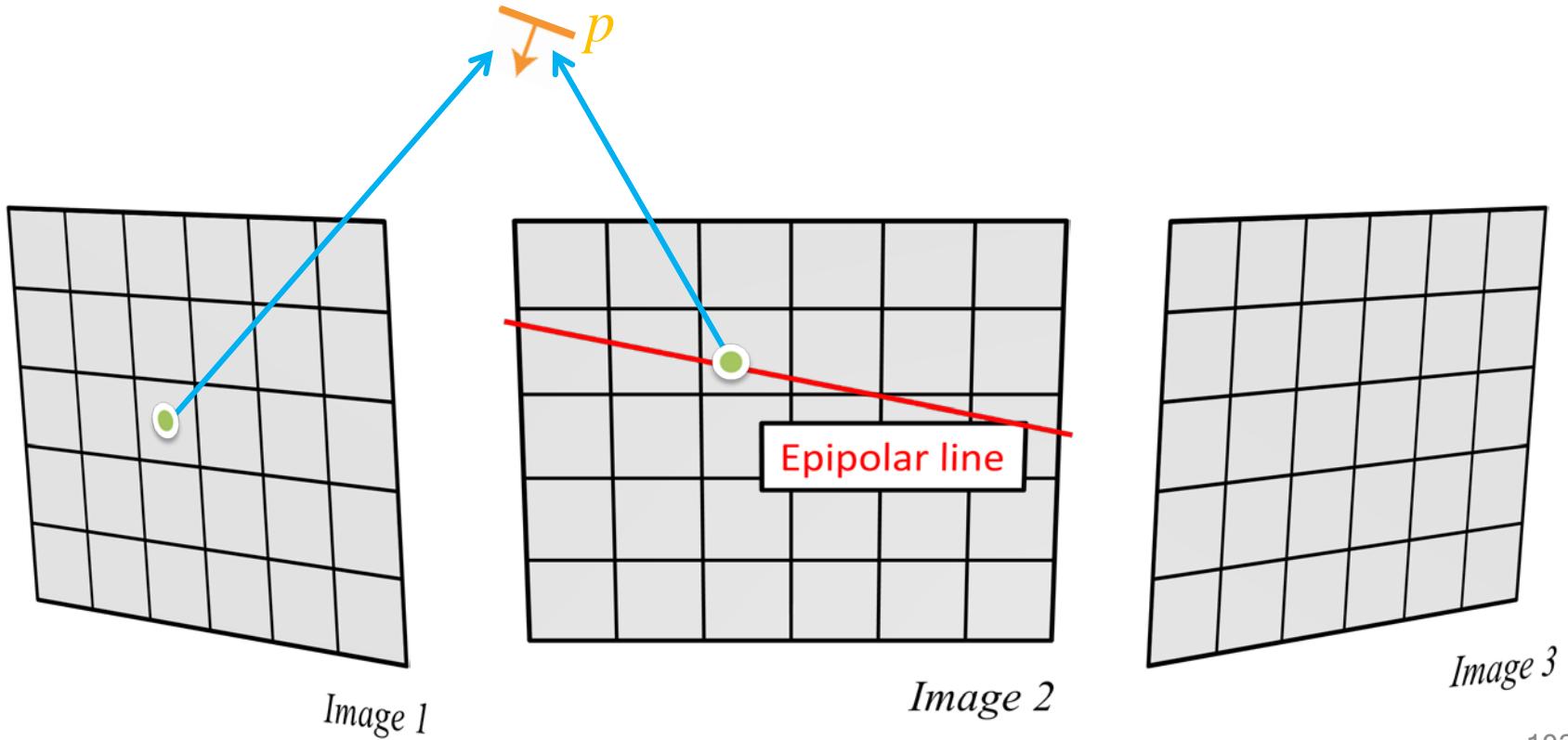


# Initial feature matching

$c(p)$ : triangulation

$n(p)$ : parallel to *Image1*

$V(p)$ :  $\{\text{Image1}, \text{Image2}\}$

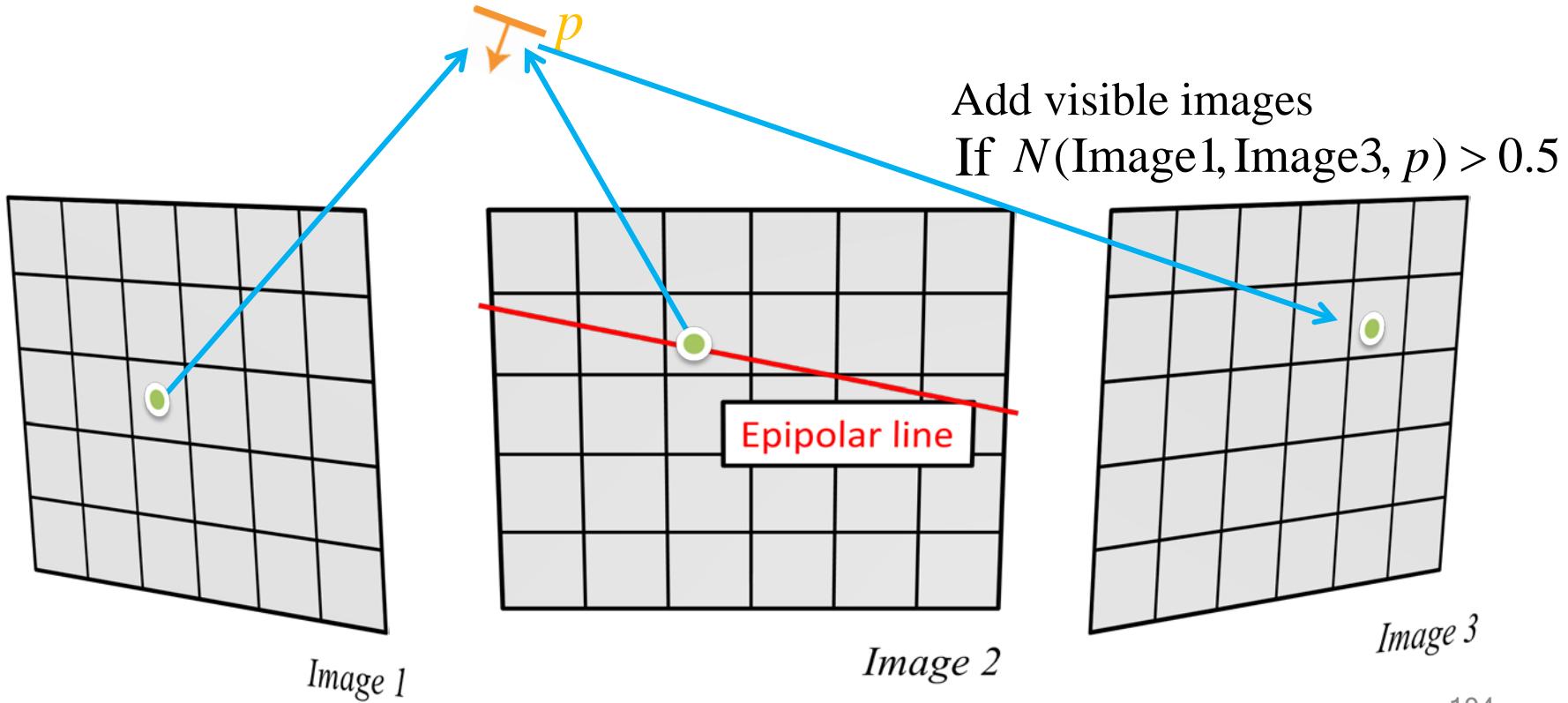


# Initial feature matching

$c(p)$ : triangulation

$n(p)$ : parallel to *Image1*

$V(p)$ : {*Image1*, *Image2*, *Image3*}



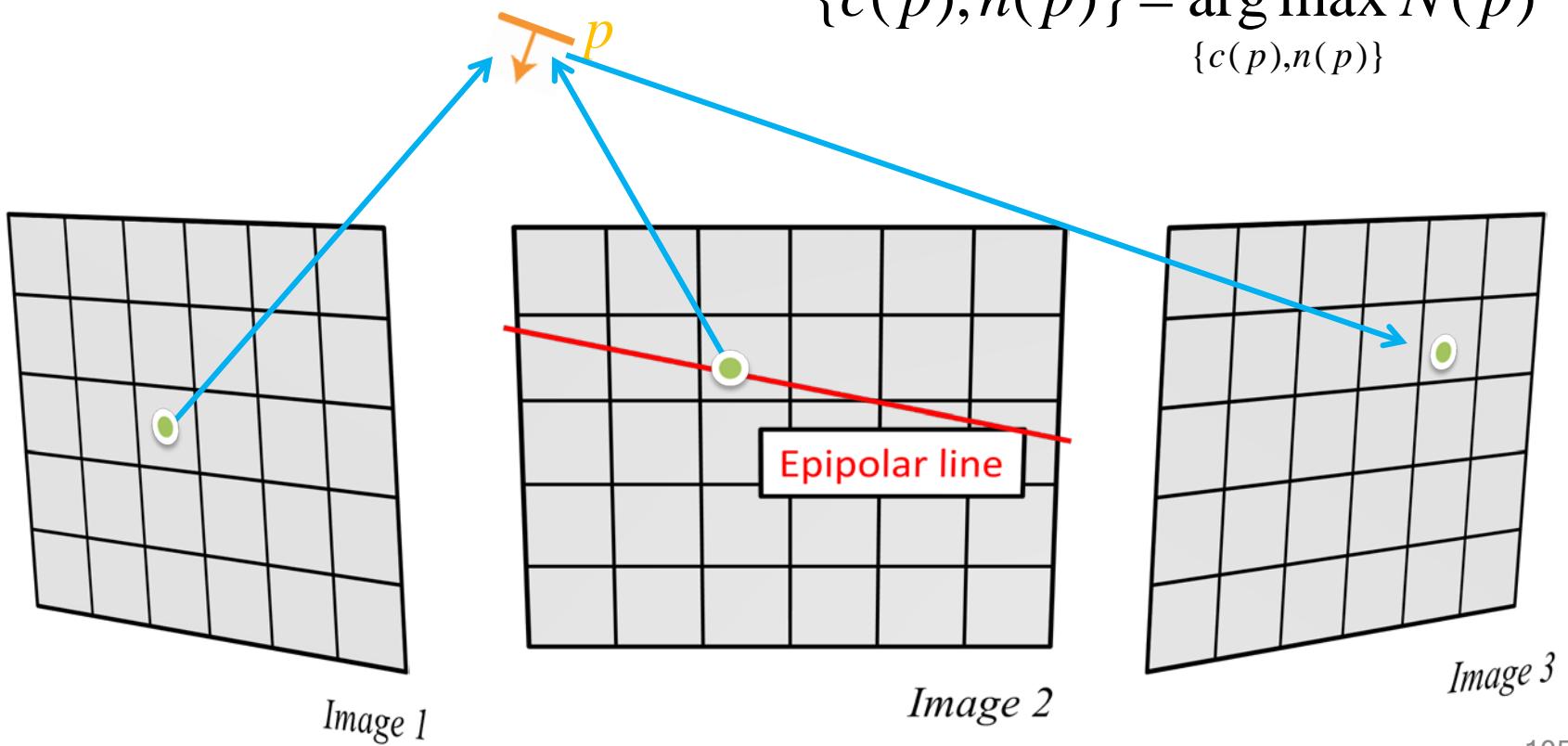
# Initial feature matching

$c(p)$ : refine

$n(p)$ : refine

$V(p)$ : {Image1, Image2, Image3}

$$\{c(p), n(p)\} = \arg \max_{\{c(p), n(p)\}} N(p)$$



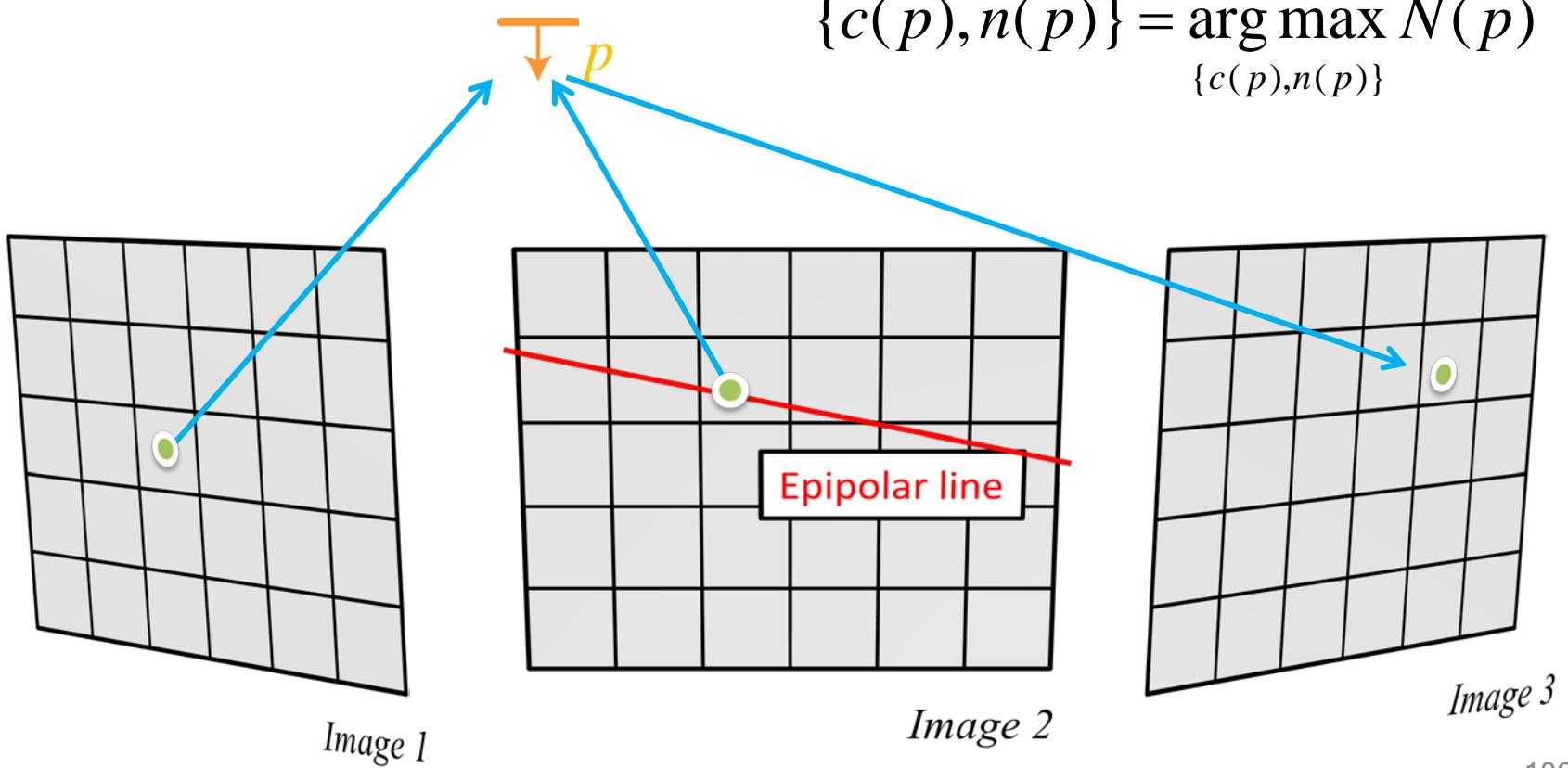
# Initial feature matching

$c(p)$ : refine

$n(p)$ : refine

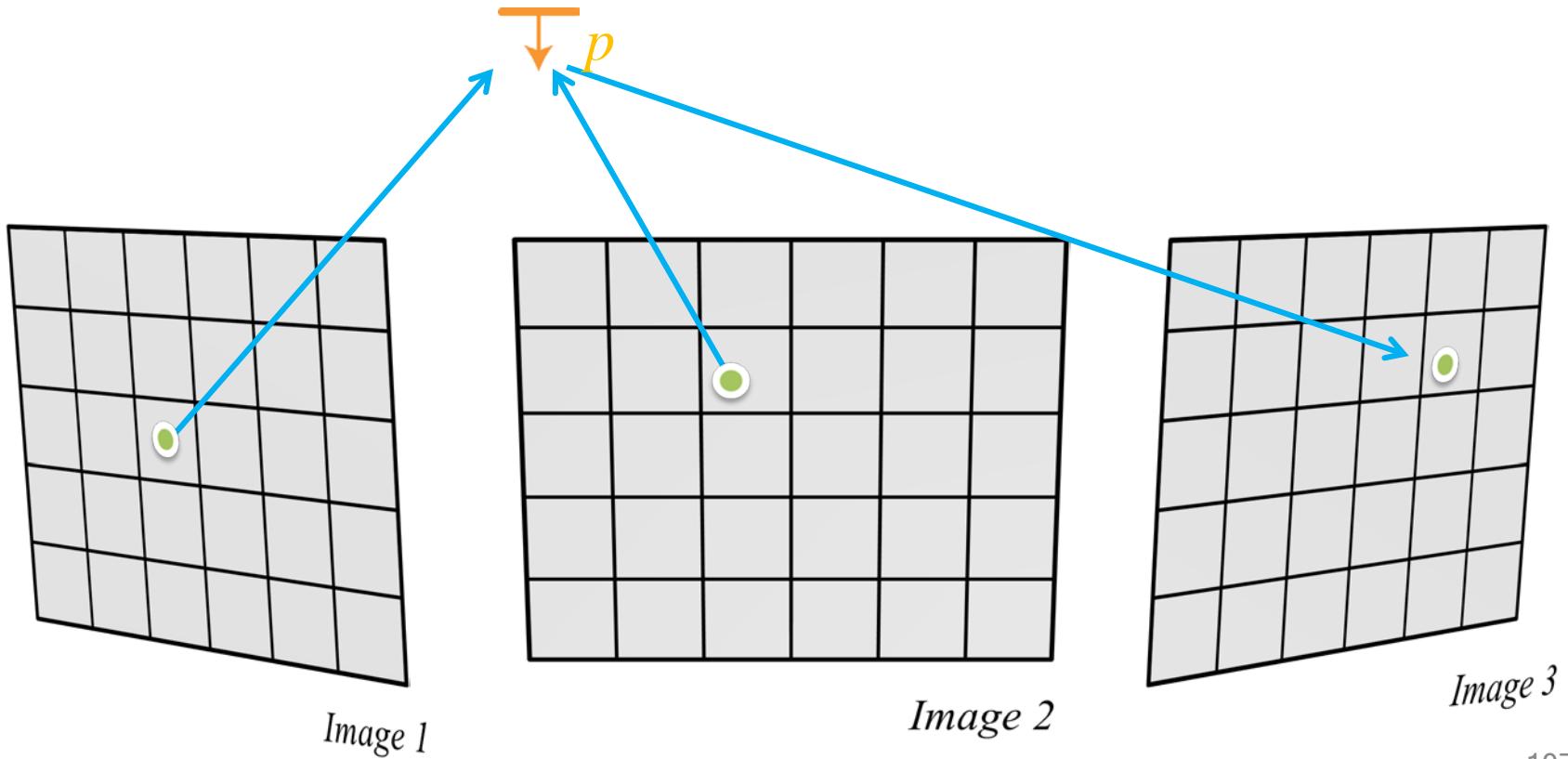
$V(p)$ : {Image1, Image2, Image3}

$$\{c(p), n(p)\} = \arg \max_{\{c(p), n(p)\}} N(p)$$

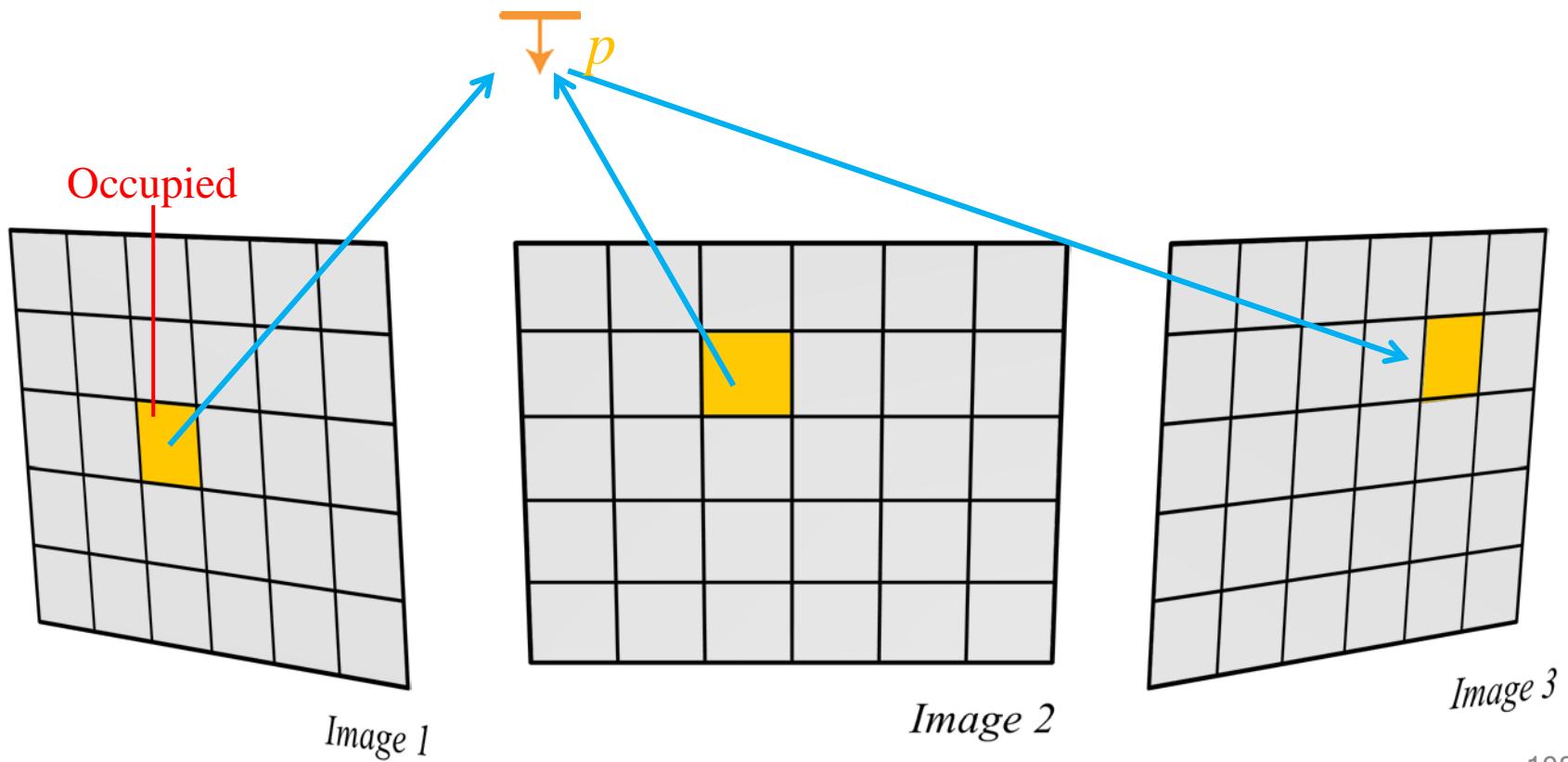


# Initial feature matching

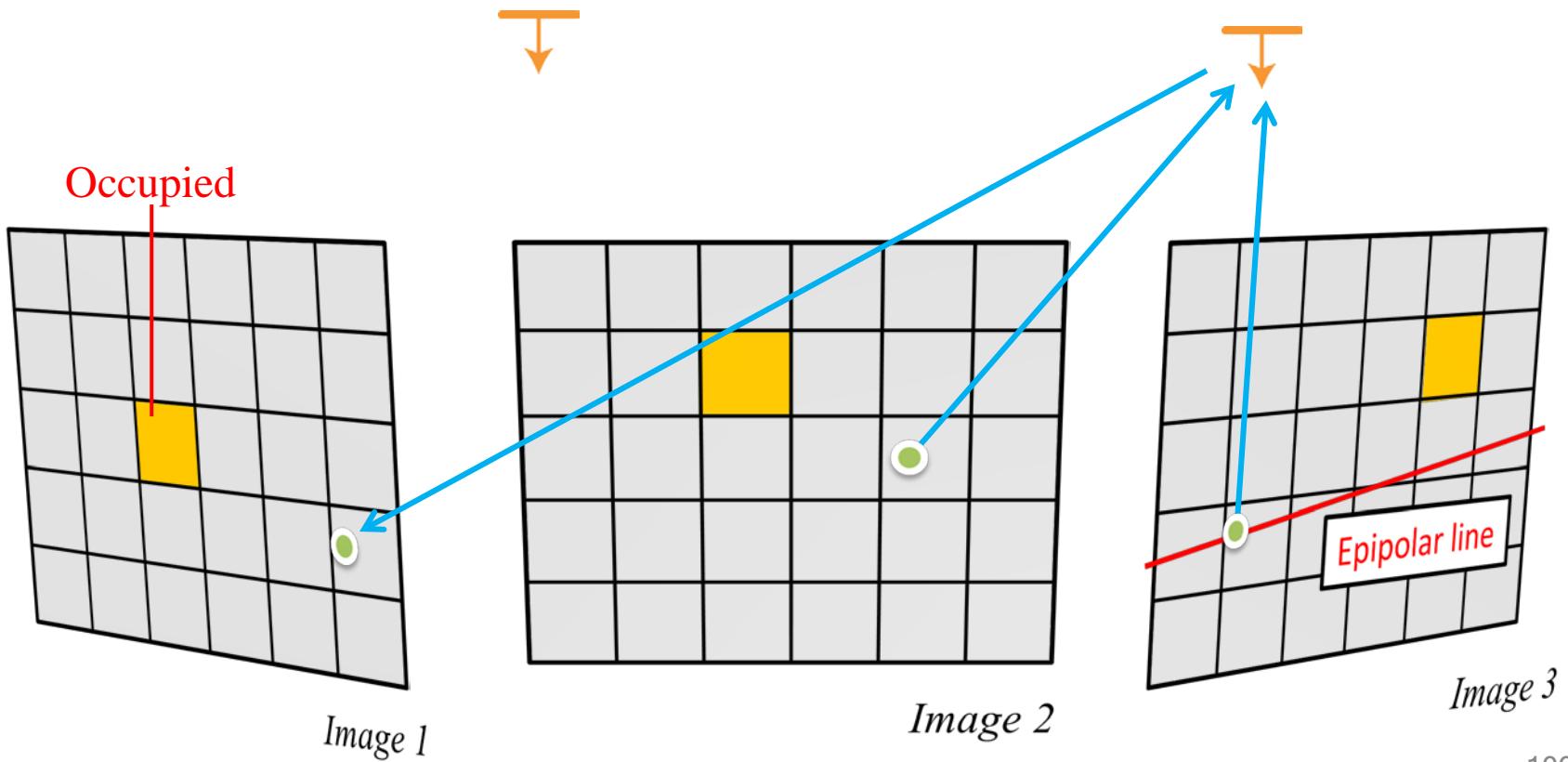
Verification  
(update  $V(p)$  and check  $|V(p)| \geq 3$ )



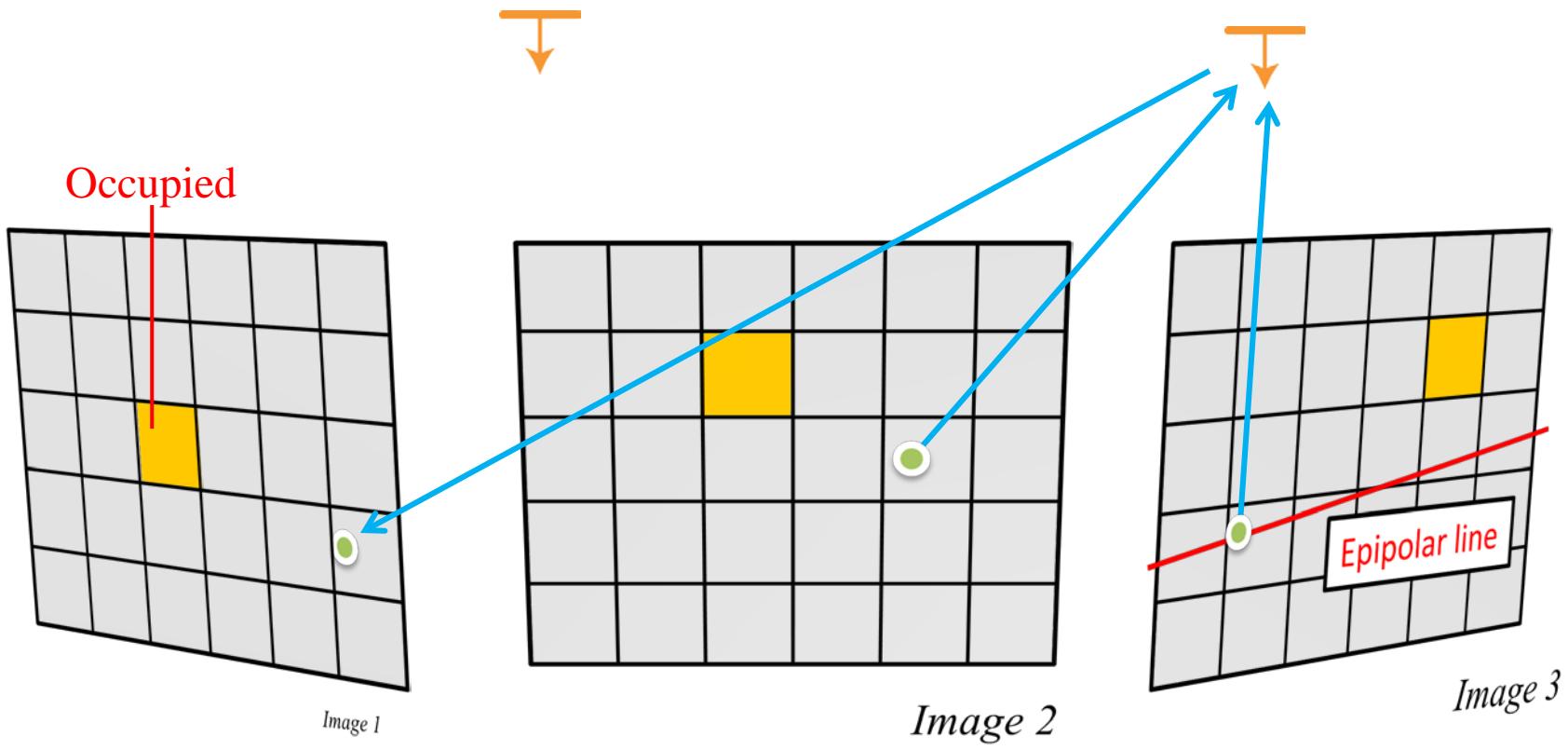
# Initial feature matching



# Initial feature matching

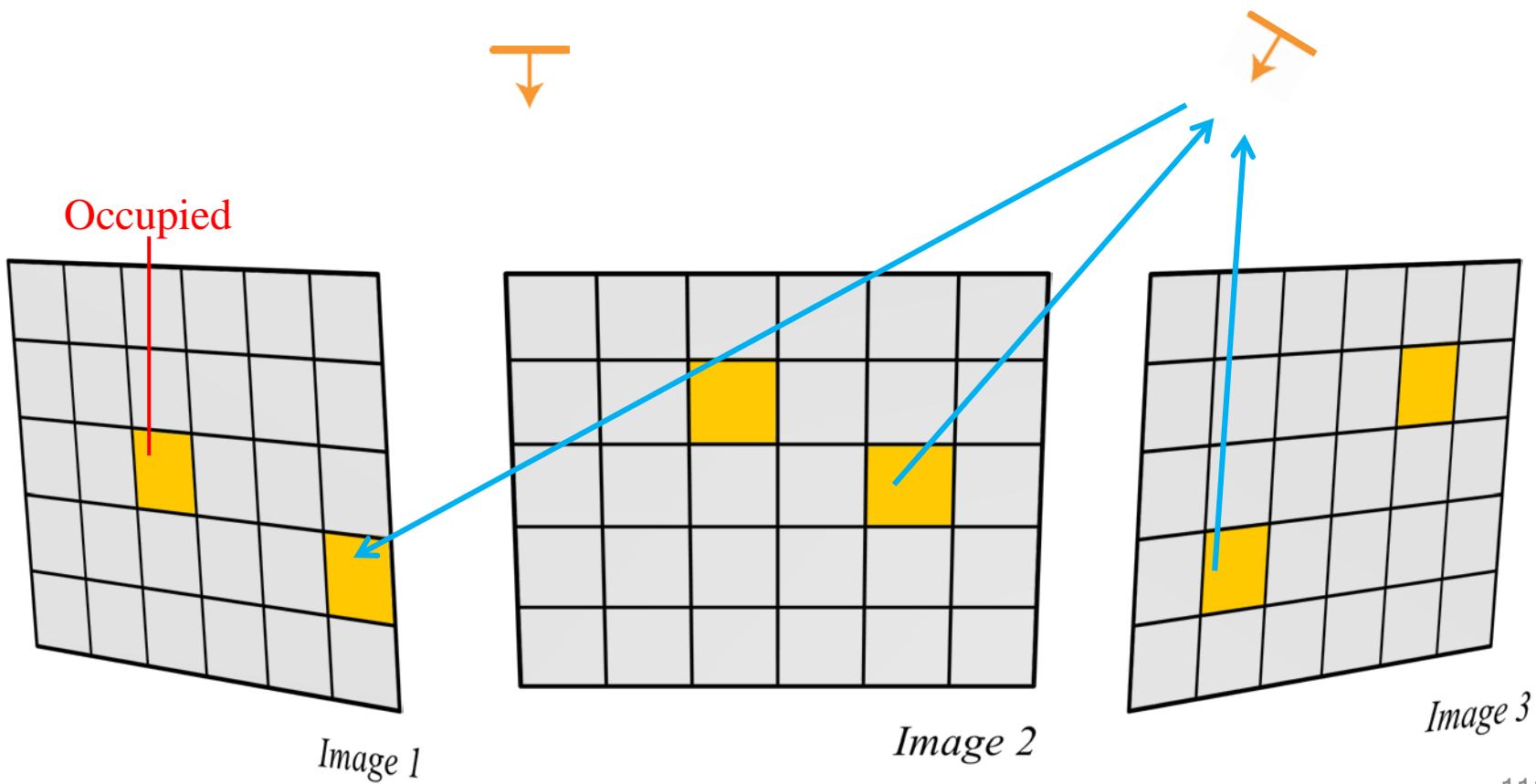


# Initial feature matching



# Initial feature matching

- Repeat for all image features



# Algorithm Overview

#1. Feature detection

#2. Initial feature matching

**#3. Patch expansion and filtering**



Input image



#1



#2



#3

# Patch expansion



Occupied pixel

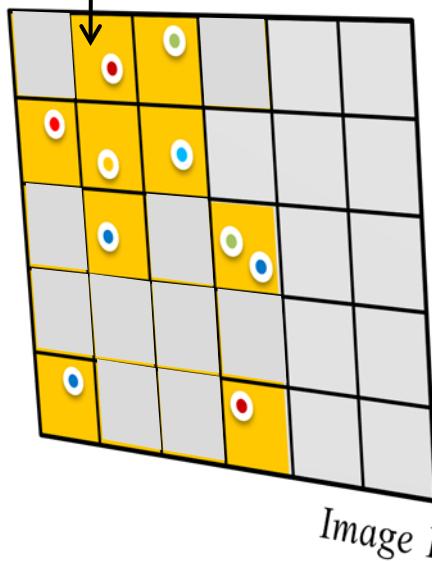


Image 1

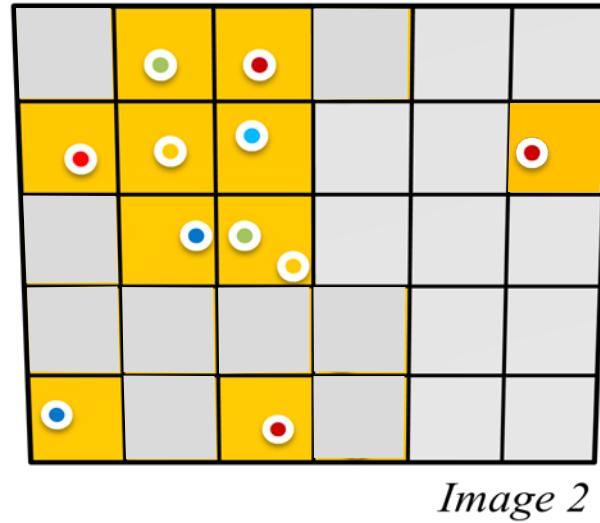


Image 2

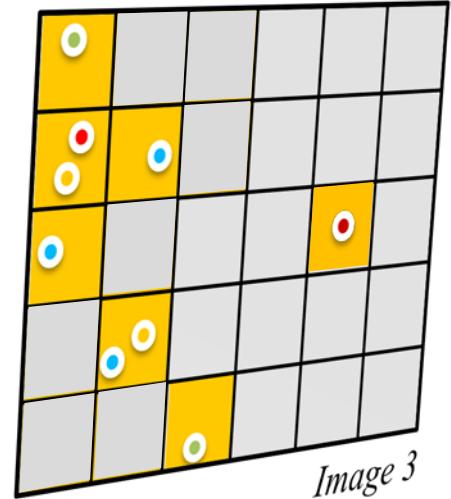
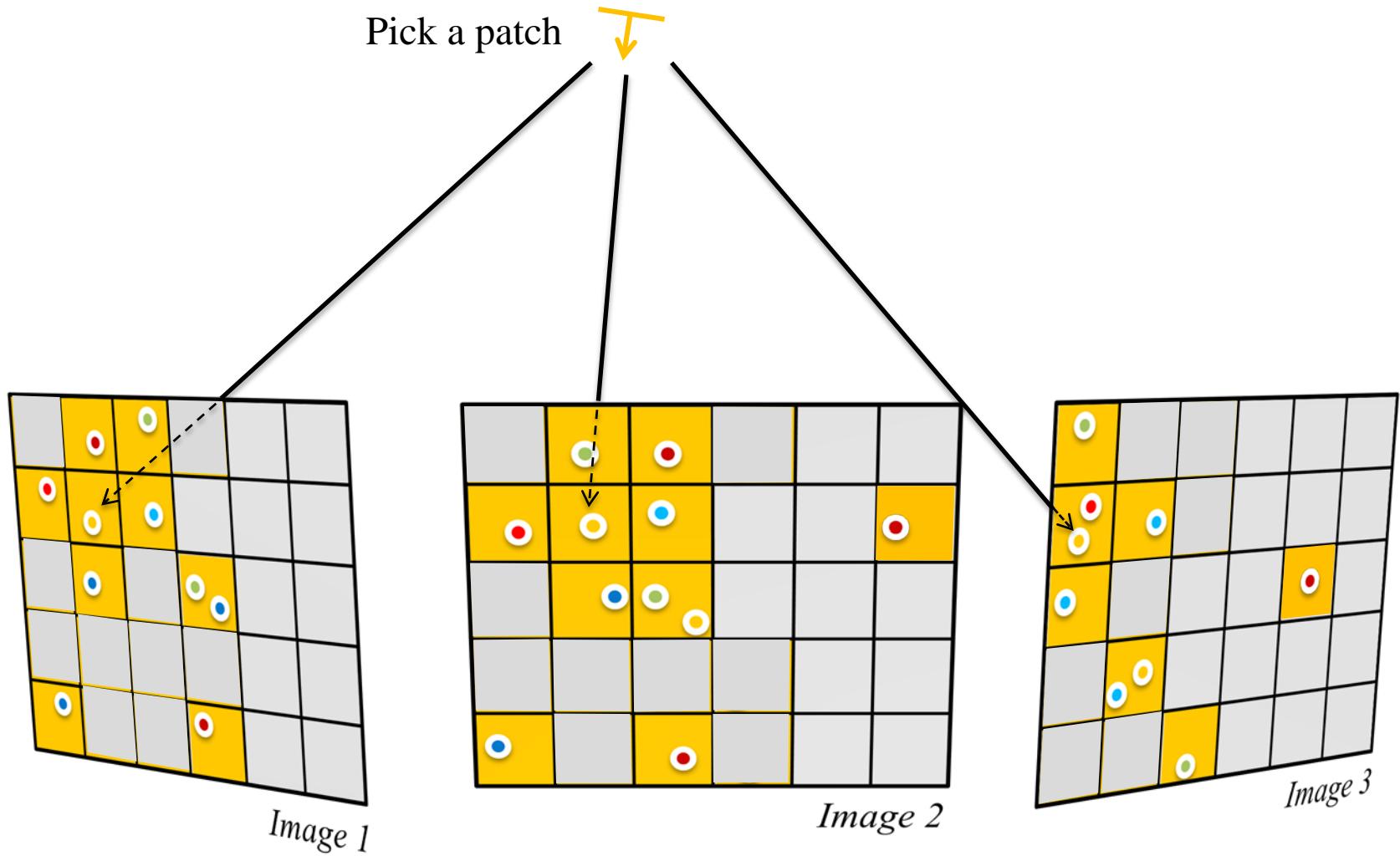
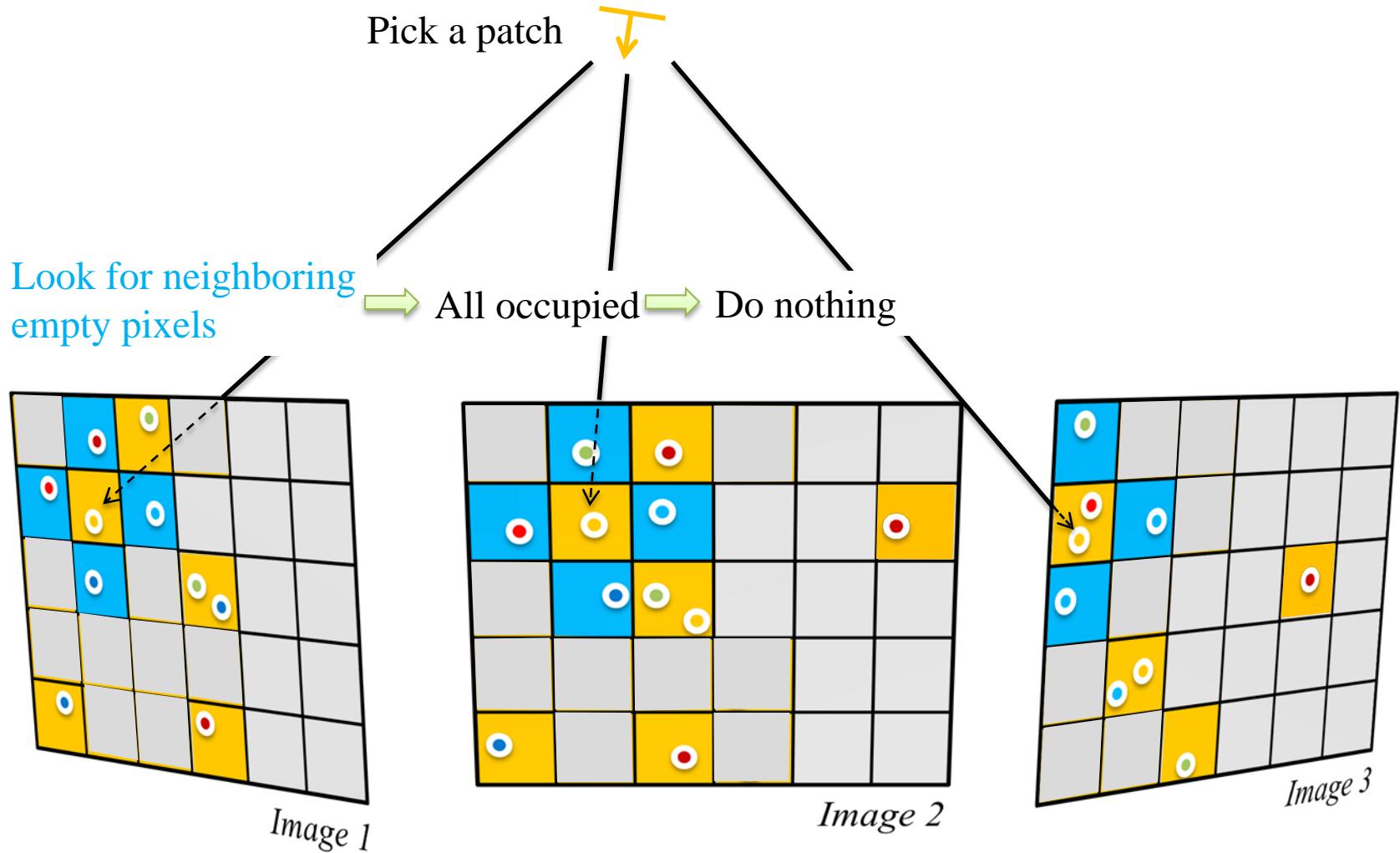


Image 3

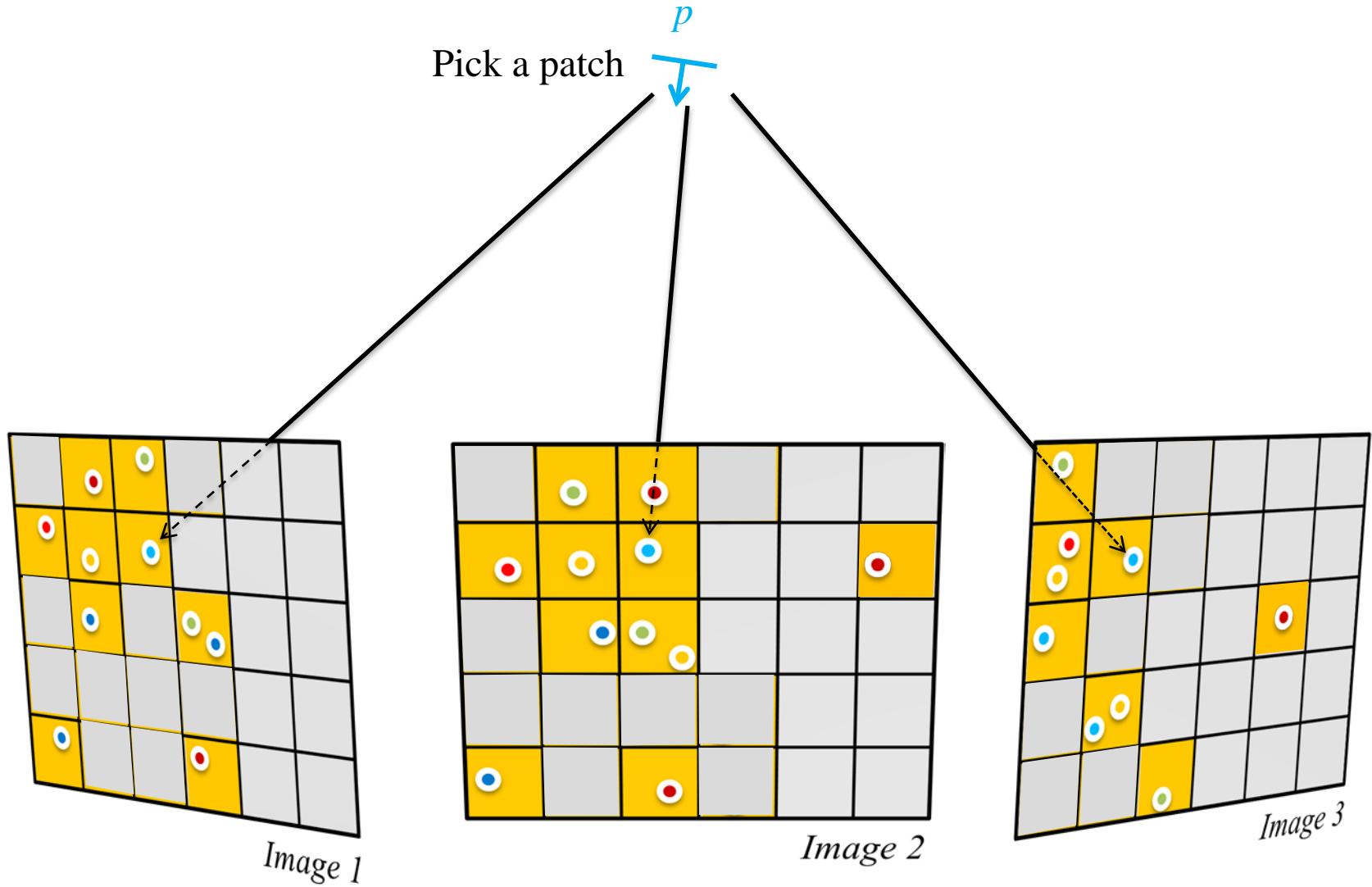
# Patch expansion



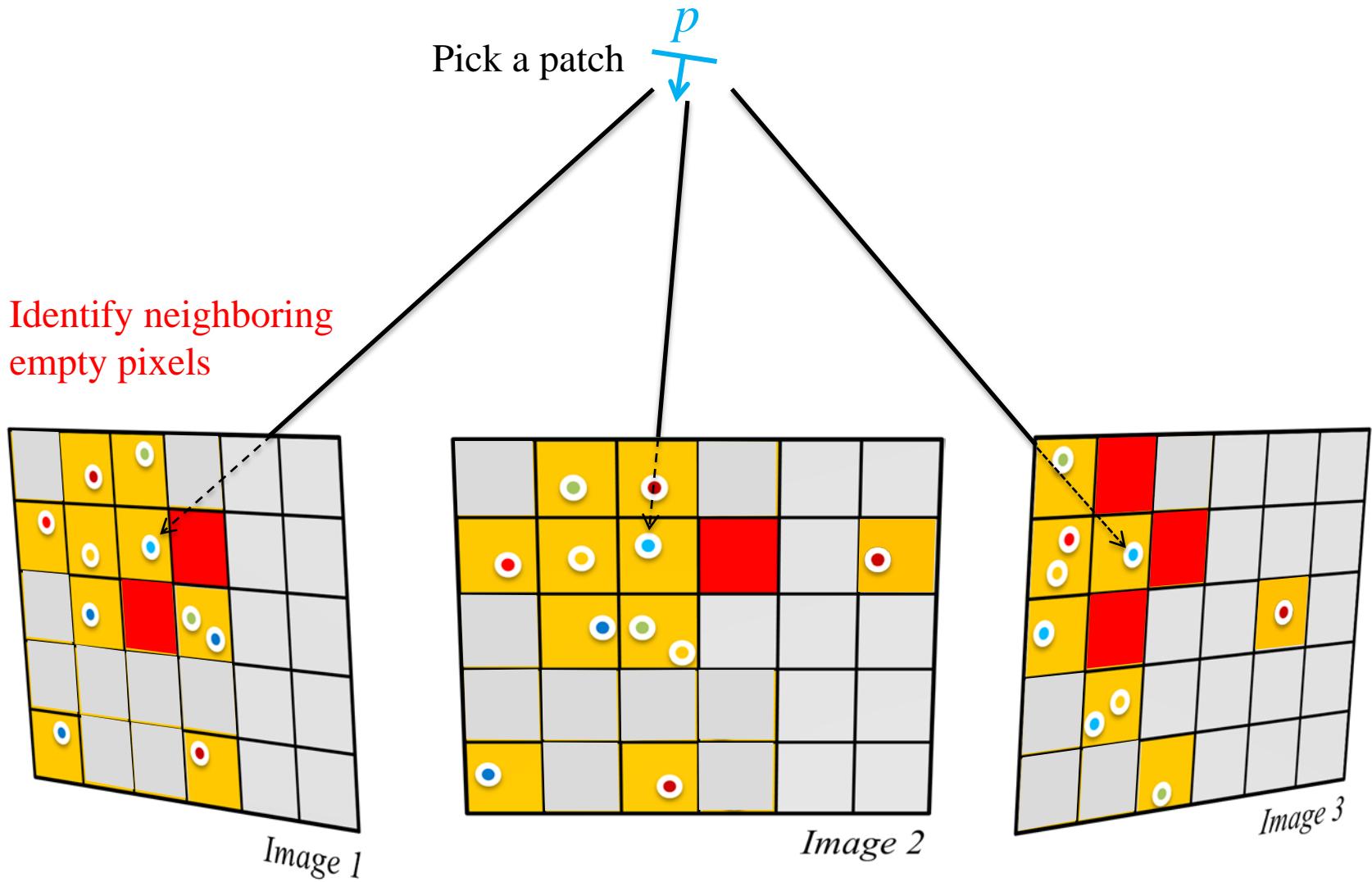
# Patch expansion



# Patch expansion

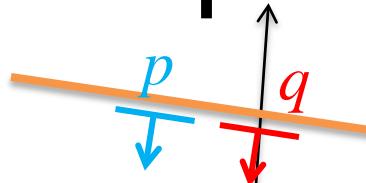


# Patch expansion



# Patch expansion

Reconstruct a patch  
visible in an empty pixel



$c(q)$ : { tangent plane of  $p$  intersects w/ ray }

$n(q)$ :

$V(q)$ :

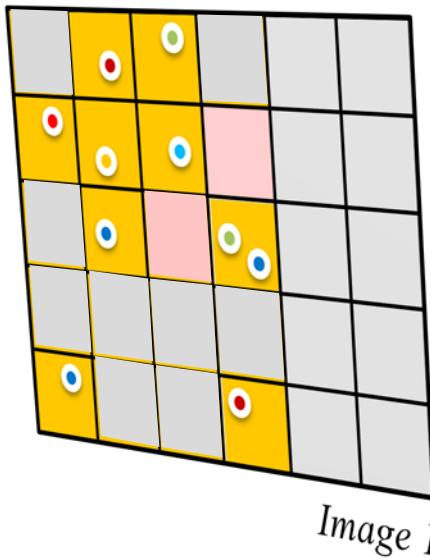


Image 1

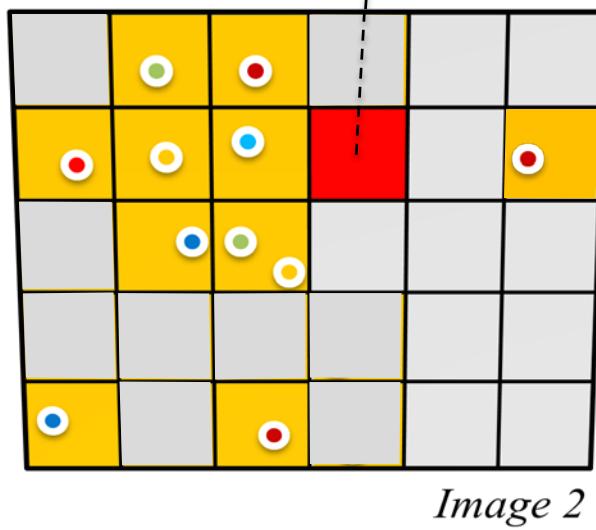


Image 2

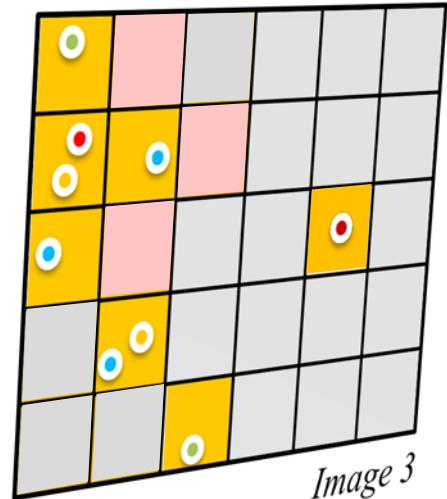
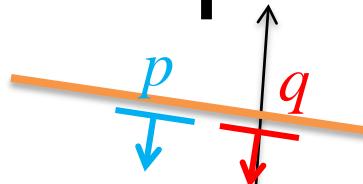


Image 3

# Patch expansion

Reconstruct a patch  
visible in an empty pixel



$c(q)$ : { tangent plane of  $p$  intersects w/ ray }

$n(q)$ :  $n(p)$

$V(q)$ :  $V(p)$

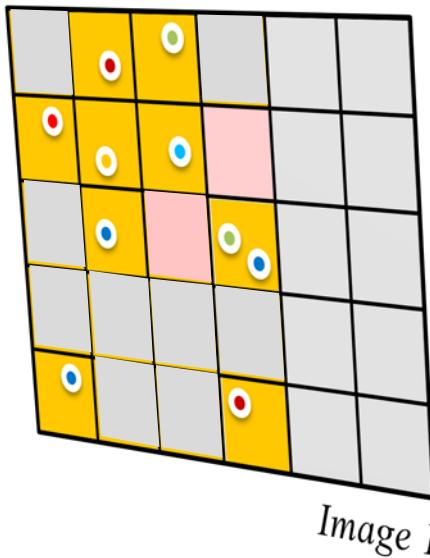


Image 1

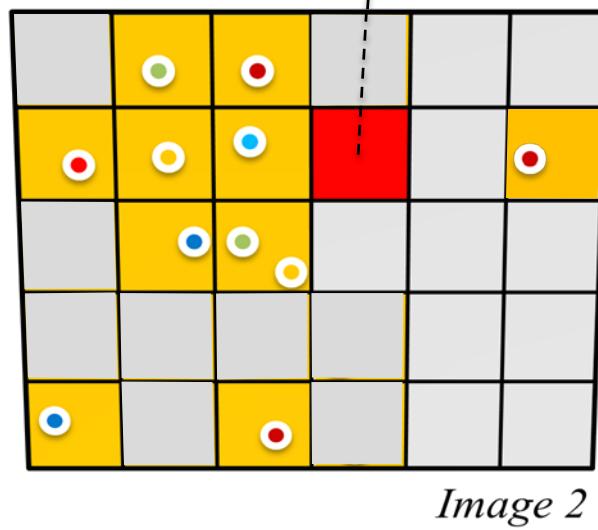


Image 2

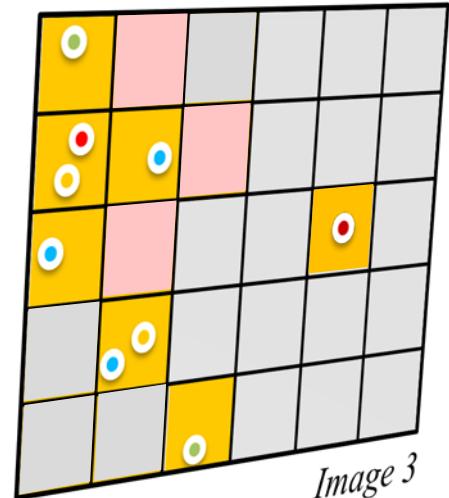
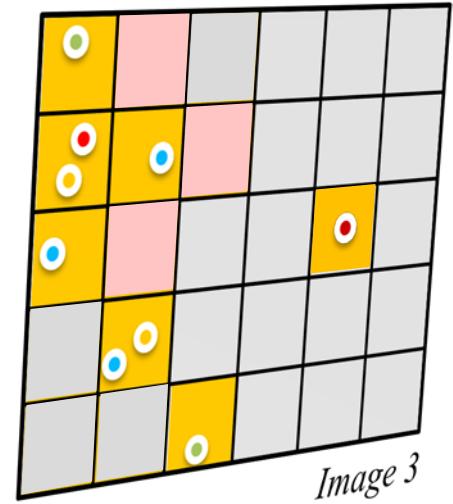
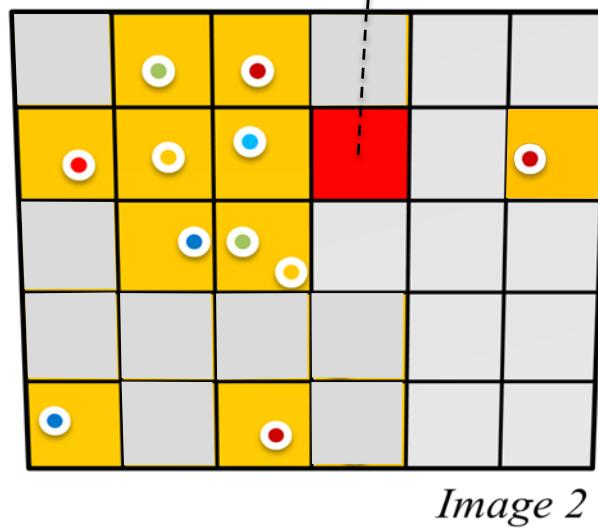
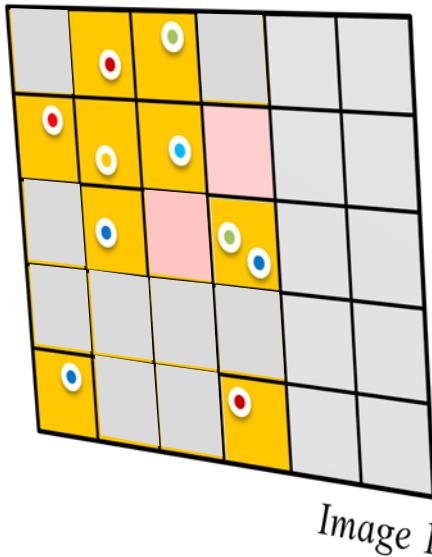


Image 3

# Patch expansion

Reconstruct a patch  
visible in an empty pixel

$p$   $\downarrow$   $q$  ↗  
 $c(q)$ : refine  
 $n(q)$ : refine  
 $V(q)$ :  $V(p)$



# Patch expansion

Reconstruct a patch  
visible in an empty pixel

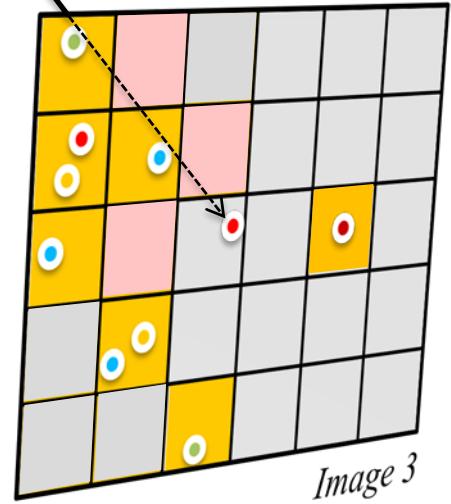
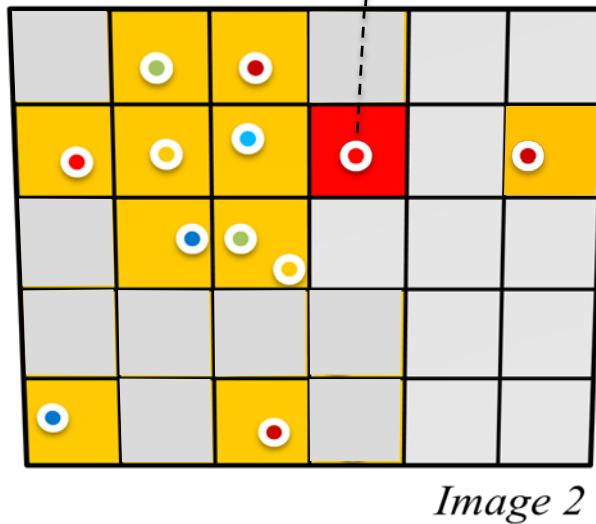
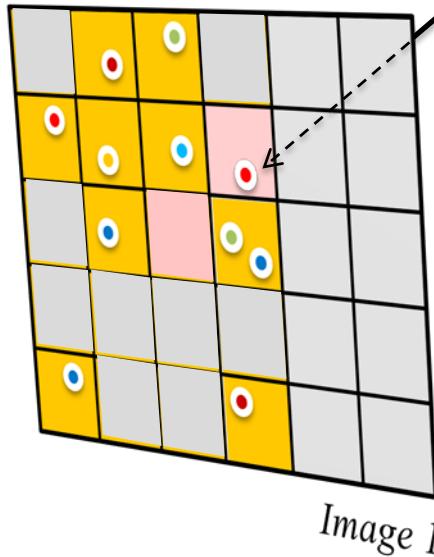
$p$   
 $q$

$c(q)$ : refine

$n(q)$ : refine

$V(q)$ :  $V(p)$

Patch verification!



# Patch expansion

Reconstruct a patch  
visible in an empty pixel

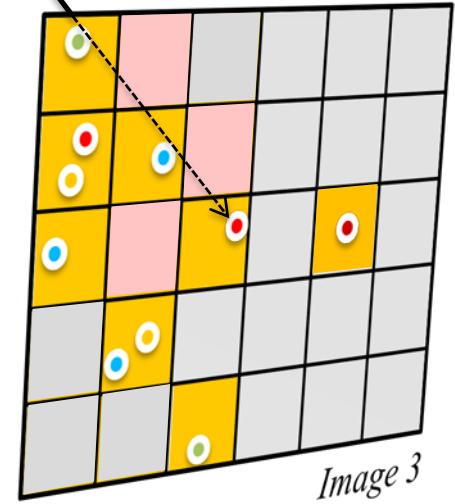
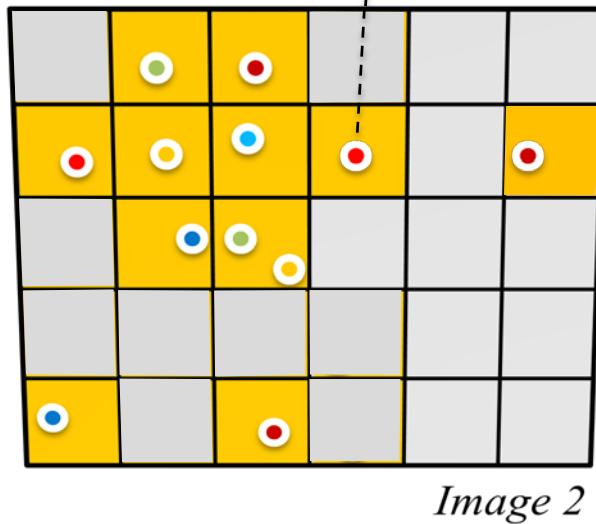
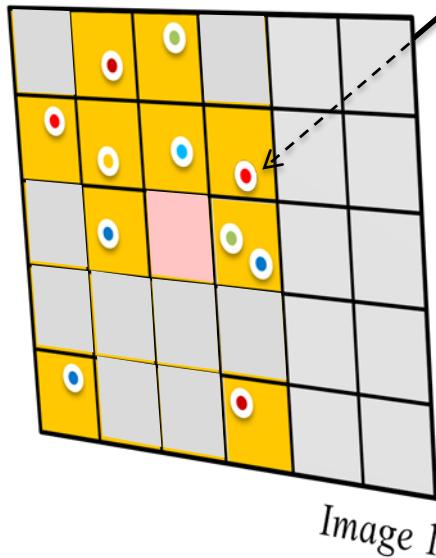
$p$   
 $q$

$c(q)$ : refine

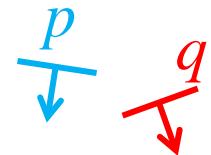
$n(q)$ : refine

$V(q)$ :  $V(p)$

Patch verification!

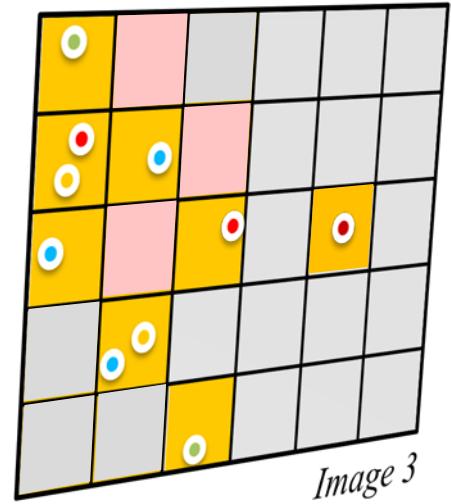
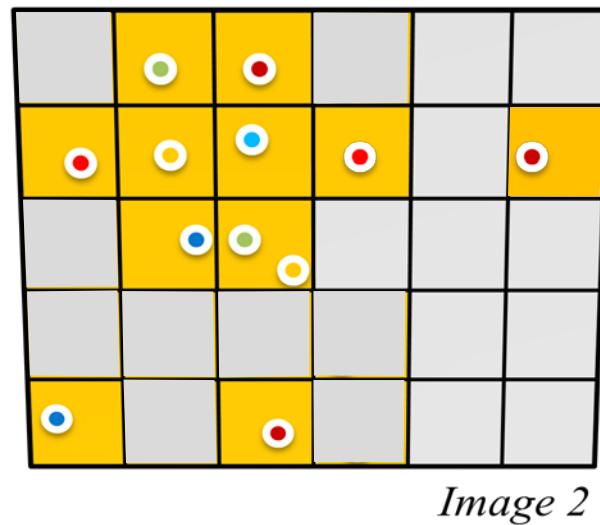
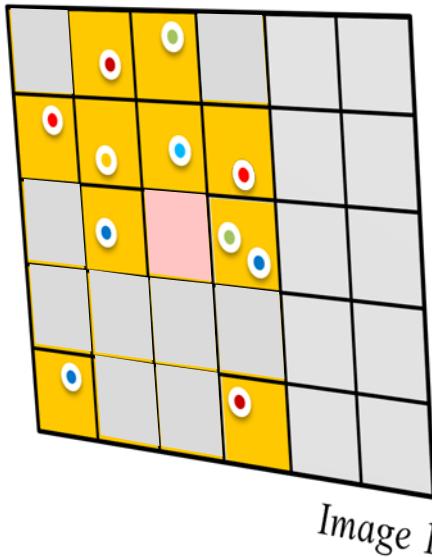


# Patch expansion



Repeat

- for every patch
- for every neighboring empty pixel



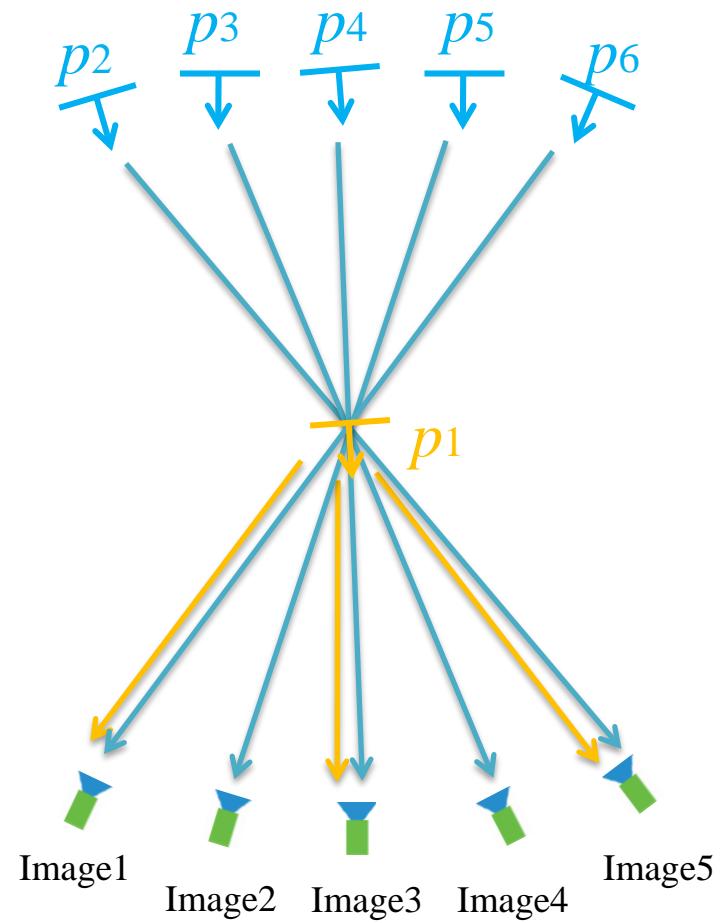
# Patch filtering

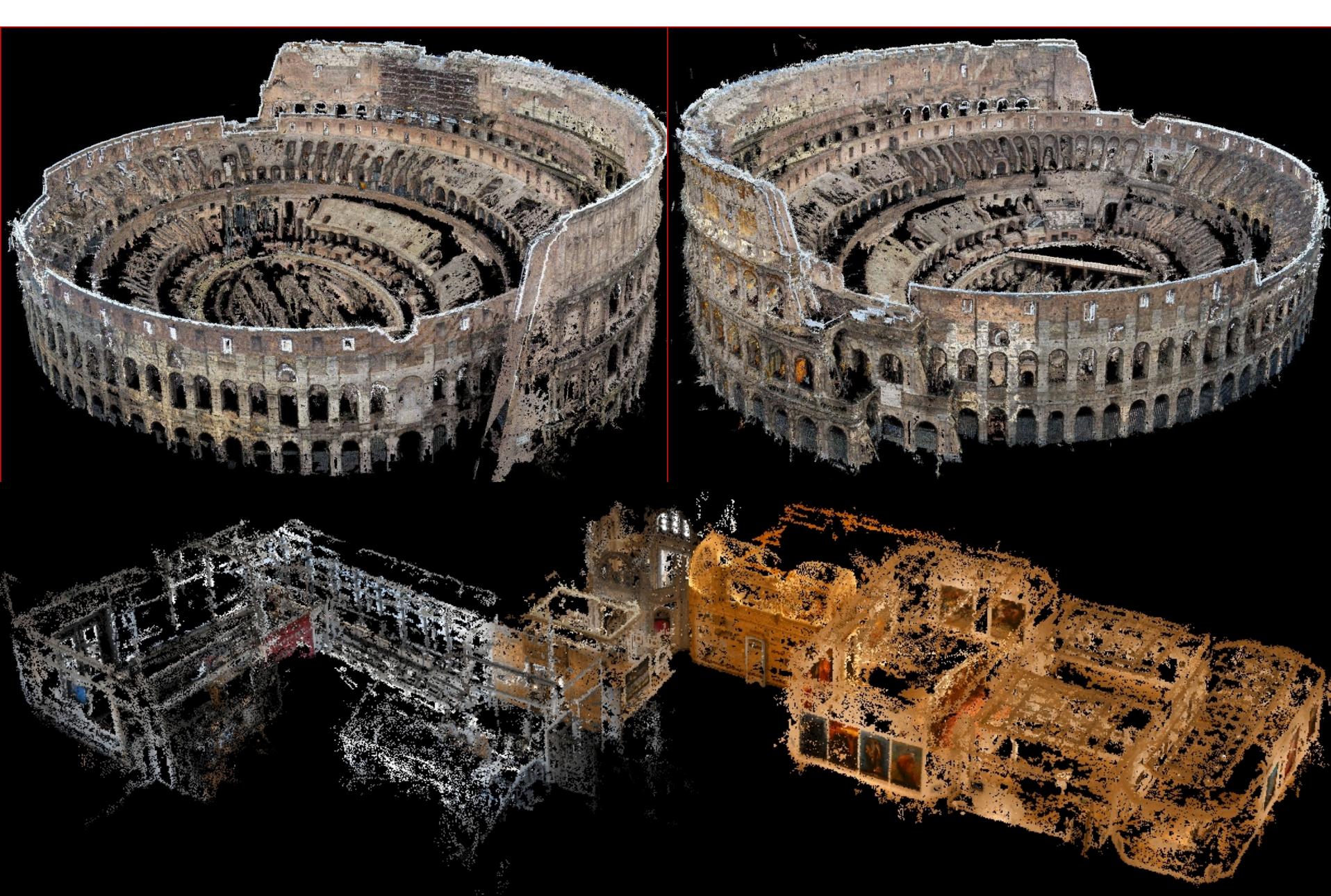
- Visibility consistency

Filter out  $p_1$  if

$$|V(p_1)| N(p_1) < \sum_{i=2}^6 N(p_i)$$

When  $p_1$  is an outlier, both  $V(p_1)$  and  $N(p_1)$  are expected to be small





# Limitations of MVS

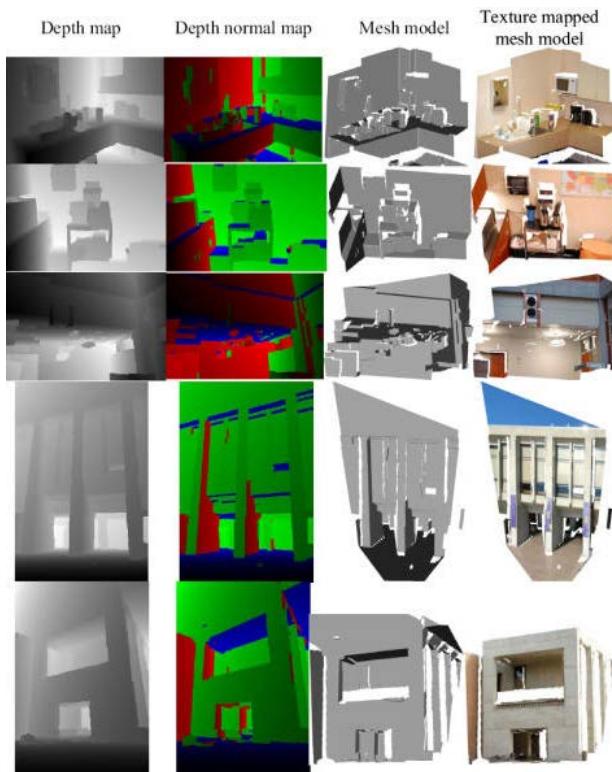
- Works well for various objects and scenes
- Surfaces must be Lambertian and well-textured
- Problematic for architectural scenes



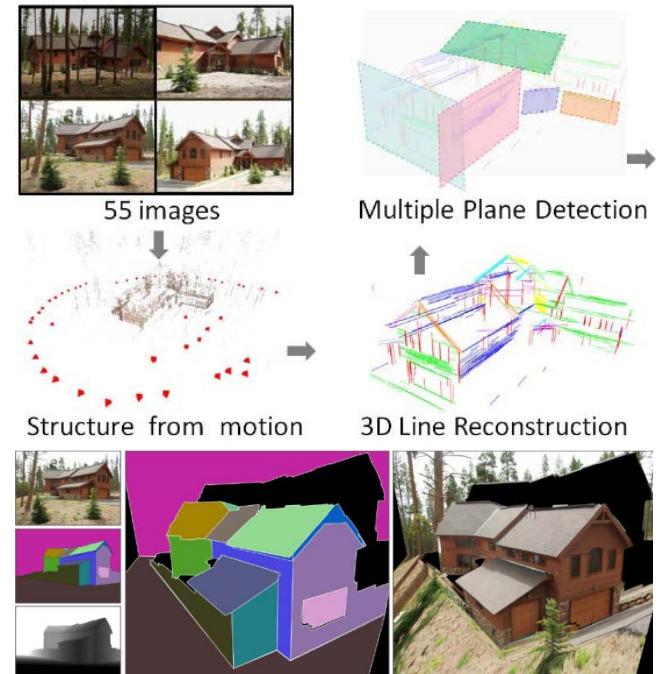
# Recent Literature



[Zebedin et al.,  
ECCV 2008]



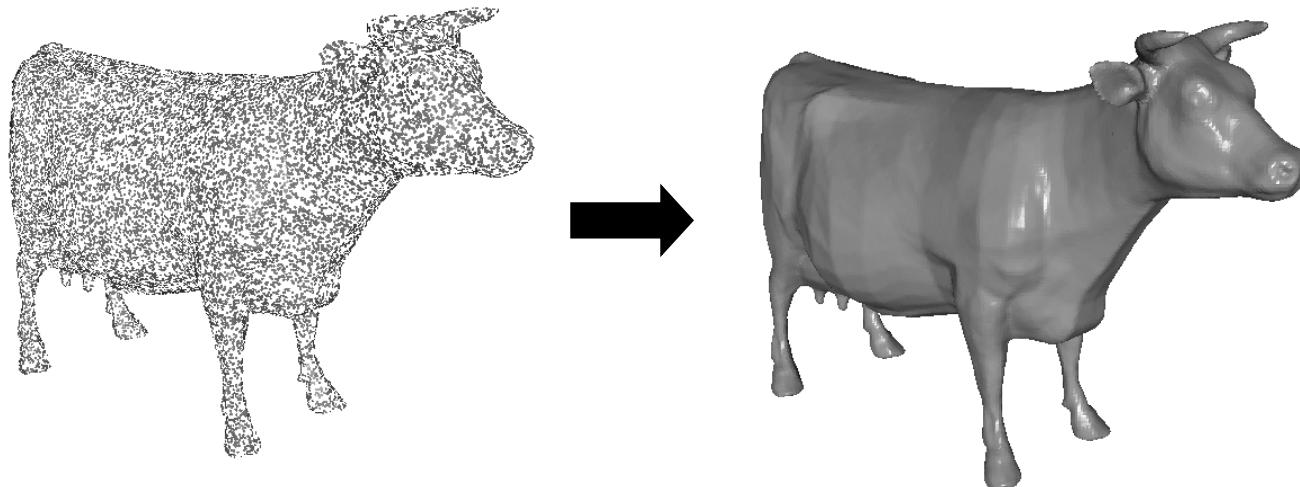
[Furukawa et al.,  
CVPR 2009]



[Sinha et al.,  
ICCV 2009]

# Poisson Surface Reconstruction

- Input: points with oriented normals (pointing outwards)
- Output: dense, connected, triangle mesh



<http://www.cs.jhu.edu/~misha/Code/PoissonRecon/Version8.0/>