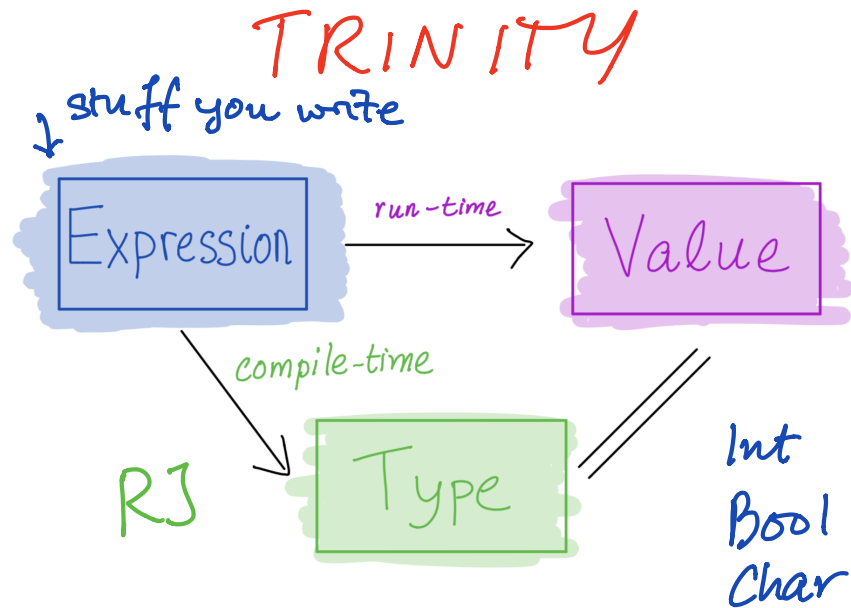


Types



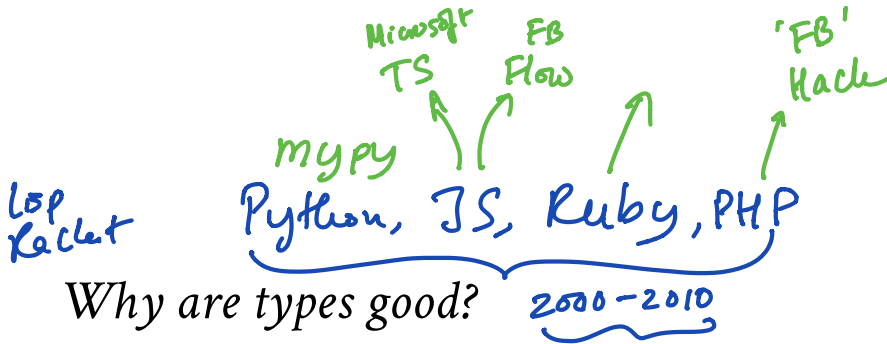
In *Haskell* every expression either

- **ill-typed** and *rejected at compile time* or
- **has a type** and can be *evaluated* to obtain **— a value** of the same type.

Ill-typed* expressions are rejected statically at *compile-time*, before execution starts

- like in Java
- unlike λ -calculus or Python ...

weirdo = 1 0 -- rejected by GHC



Why are types good? 2000-2010

- Helps with program design
- Types are contracts (ignore ill-typed inputs!)
- Catches errors early ✓
- Allows compiler to generate code
- Enables compiler optimizations

make junk values
not representable

Function Types

Functions have **arrow types**:

- $\lambda x. e$ has type $A \rightarrow B$
- if e has type B assuming x has type A

For example:

```
> :t (\x -> if x then `a` else `b`) -- ???
```

Always annotate your function bindings

First understand *what the function does*

- Before you think about *how to do it*

```
sum :: Int -> Int
sum 0 = 0
sum n = n + sum (n - 1)
```

*When you have *multiple arguments*

For example

```
add3 :: Int -> (Int -> (Int -> Int))
add3 x y z = x + y + z
```

why? because the above is the same as:

```
add3 :: Int -> (Int -> (Int -> Int))
add3 = \x -> (\y -> (\z -> x + y + z))
```

however, as with the lambdas, the `->` **associates to the right** so we will just write:

```
add3 :: Int -> Int -> Int -> Int
add3 x y z = x + y + z
```

*(+) = \x y -> 'call x86
inst to add x,y*

$$(t_1 \rightarrow (t_2 \rightarrow (t_3 \rightarrow T)))$$

$\text{Int} \rightarrow \text{Bool}$

$\text{List } T$

Lists

A list is

- either an *empty list*

`[]` -- pronounced "nil"

- or a *head element* attached to a *tail list*

`x:xs` -- pronounced "x cons xs"

Examples:

```
[]                -- A list with zero elements

1 : []           -- A list with one element: 1

(:) 1 []         -- As above: for any infix op, `x op y` is same as `(op) x y`

1:(2:(3:(4:[]))) -- A list with four elements: 1, 2, 3, 4

1:2:3:4:[]       -- Same thing (: is right associative)

[1,2,3,4]        -- Same thing (syntactic sugar)
```

Terminology: constructors and values

[] and (:) are called the list **constructors**

We've seen constructors before:

- True and False are Bool constructors
- 0, 1, 2 are ... well, you can think of them as Int constructors

- The `Int` constructors don't take any parameters, we just called them *values*

In general, a **value** is a constructor applied to **other values**

- examples above are *list* values

The Type of a List

A list has type `[Thing]` if each of its elements has type `Thing`

Examples:

```
intList :: [Int]
intList = [1,2,3,4]
```

```
boolList :: [Bool]
boolList = [True, False, True]
```

```
strList :: [String]
strList = ["nom", "nom", "burp"]
```

Lets write some Functions

A Recipe (<https://www.htdp.org/>)

Step 1: Write some tests

Step 2: Write the type

Step 3: Write the code

Functions on lists: range

1. Tests

lo hi

```
-- >>> ???
```

2. Type

```
range :: ???
```

3. Code

```
range = ???
```

Syntactic Sugar for Ranges

There's also syntactic sugar for this!

```
[1..7]    -- [1,2,3,4,5,6,7]
```

```
[1,3..7]  -- [1,3,5,7]
```

Functions on lists: length

1. Tests

```
-- >>> ???
```

2. Type

```
len :: ???
```

3. Code

```
len = ???
```

Pattern matching on lists

```
-- / Length of the list
len :: [Int] -> Int
len []      = 0
len (_:xs) = 1 + len xs
```

~~A pattern is either a variable (incl. `_`) or a value~~

A pattern is

- either a *variable* (incl. `_`)
- or a *constructor* applied to other *patterns*

Pattern matching attempts to match *values* against *patterns* and, if desired, *bind* variables to successful matches.

Functions on lists: take

Let's write a function to `take` first `n` elements of a list `xs`.

1. Tests

```
-- >>> ???
```

2. Type

```
take :: ???
```

3. Code

```
take = ???
```

QUIZ

Which of the following is **not** a pattern?

A. $(1:xs)$

B. $(_:_:_)$

C. $[x]$

D. $[1+2,x,y]$

E. all of the above

Strings are Lists-of-Chars

For example

```
λ> let x = ['h', 'e', 'l', 'l', 'o']
```

```
λ> x
```

```
"hello"
```

```
λ> let y = "hello"
```

```
λ> x == y
```

```
True
```

```
λ> :t x
```

```
x :: [Char]
```

```
λ> :t y
```

```
y :: [Char]
```

shout Shout SHOUT

How can we convert a string to upper-case, e.g.

```
ghci> shout "like this"
```

```
"LIKE THIS"
```

```
shout :: String -> String
```

```
shout s = ???
```

Some useful library functions

```
-- | Length of the list
```

```
length :: [t] -> Int
```

```
-- | Append two lists
```

```
(++) :: [t] -> [t] -> [t]
```

```
-- | Are two lists equal?
```

```
(==) :: [t] -> [t] -> Bool
```

You can search for library functions on Hoogle (<https://www.haskell.org/hoogle/>)!

Tuples

```
myPair :: (String, Int) -- pair of String and Int
```

```
myPair = ("apple", 3)
```