



GRADE 8

Mathematics

Administered April 2021

RELEASED

STAAR GRADE 8 MATHEMATICS REFERENCE MATERIALS



Slope-intercept form	$y = mx + b$
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Direct variation	$y = kx$
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Slope of a line	$m = \frac{y_2 - y_1}{x_2 - x_1}$
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CIRCUMFERENCE

Circle	$C = 2\pi r$	or	$C = \pi d$
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AREA

Triangle	$A = \frac{1}{2}bh$
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Rectangle or parallelogram	$A = bh$
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Trapezoid	$A = \frac{1}{2}(b_1 + b_2)h$
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Circle	$A = \pi r^2$
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SURFACE AREA

	Lateral	Total
Prism	$S = Ph$	$S = Ph + 2B$
Cylinder	$S = 2\pi rh$	$S = 2\pi rh + 2\pi r^2$

VOLUME

Prism or cylinder	$V = Bh$
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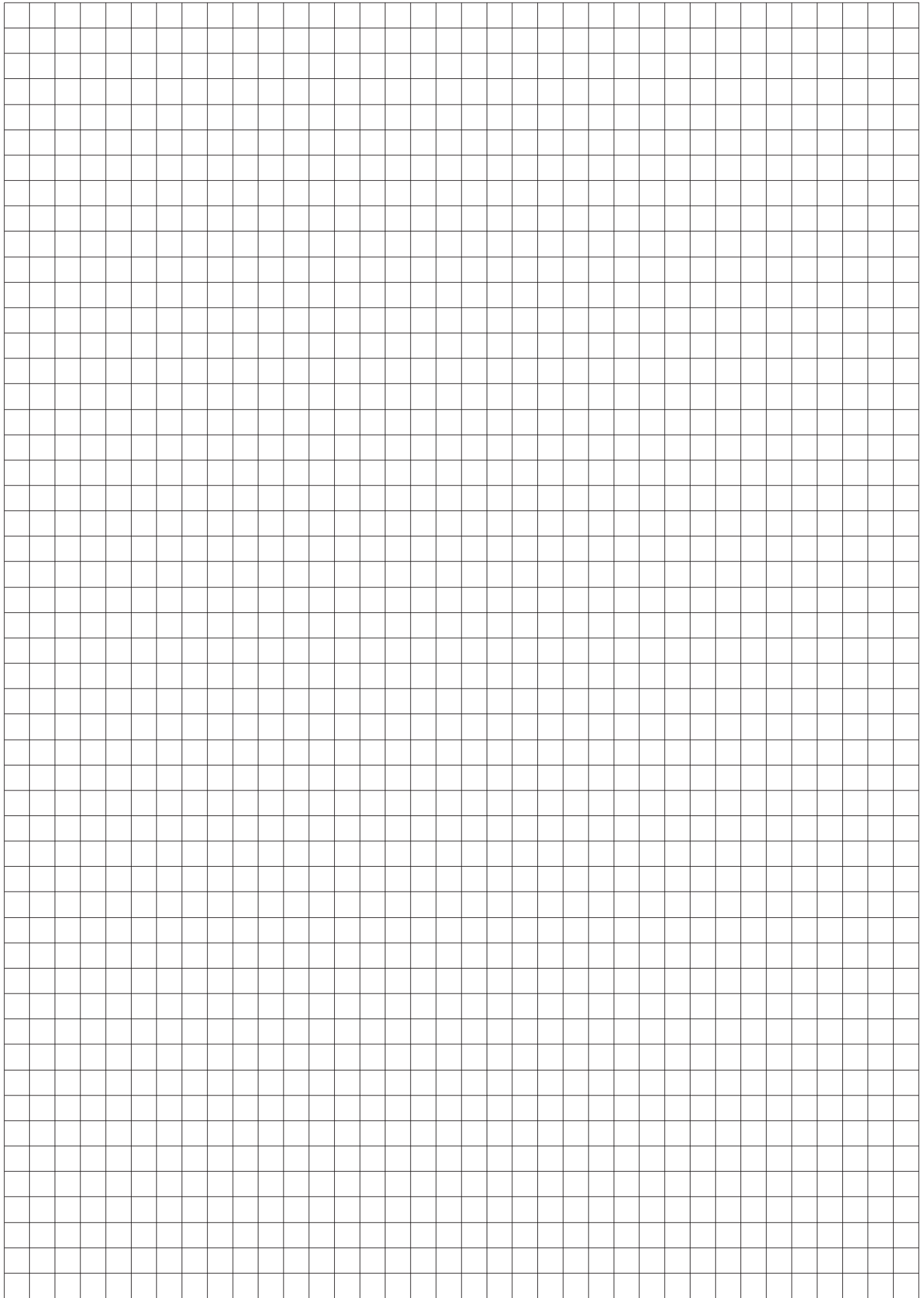
Pyramid or cone	$V = \frac{1}{3}Bh$
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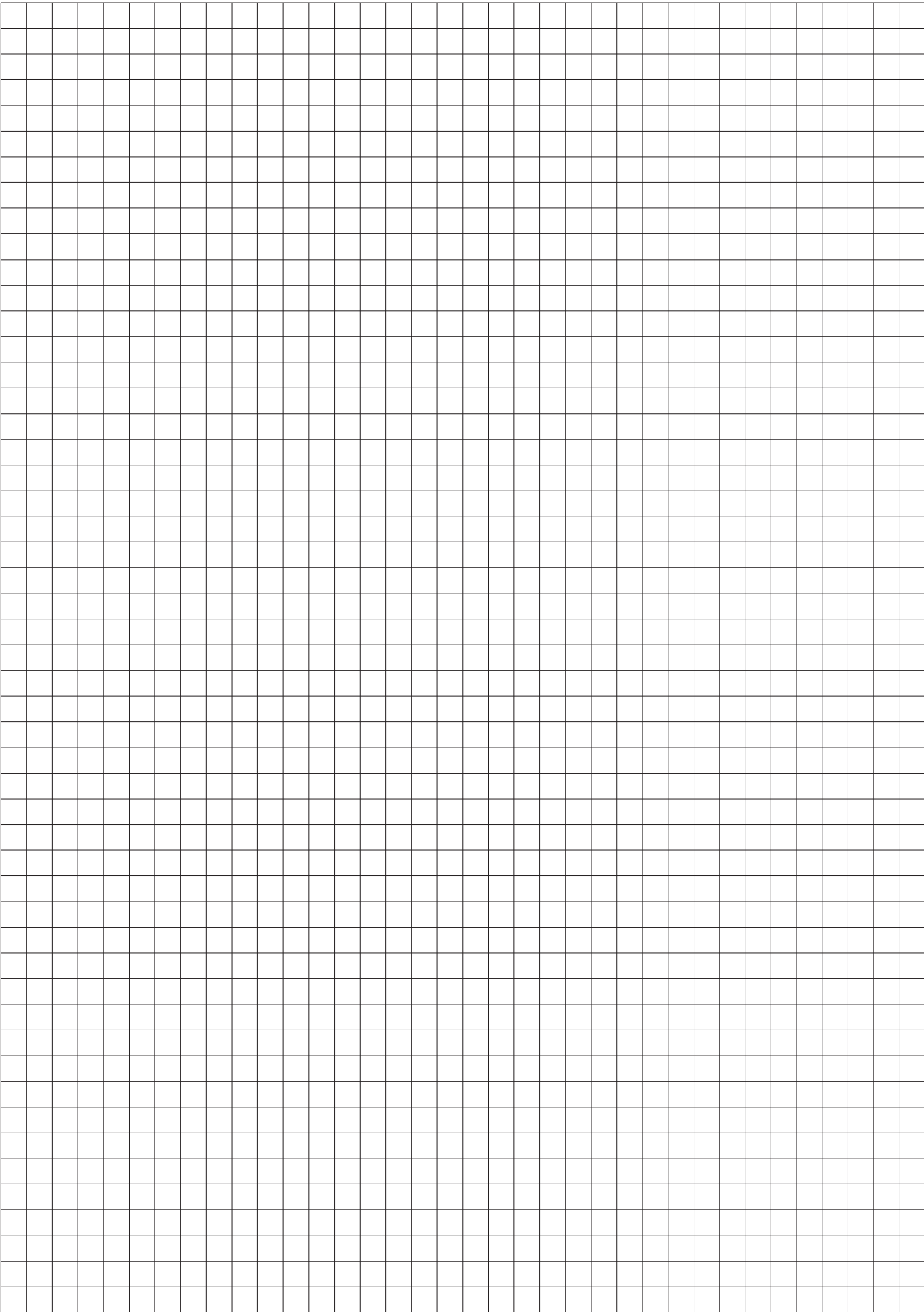
Sphere	$V = \frac{4}{3}\pi r^3$
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Pythagorean theorem	$a^2 + b^2 = c^2$
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Simple interest	$I = Prt$
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Compound interest	$A = P(1 + r)^t$
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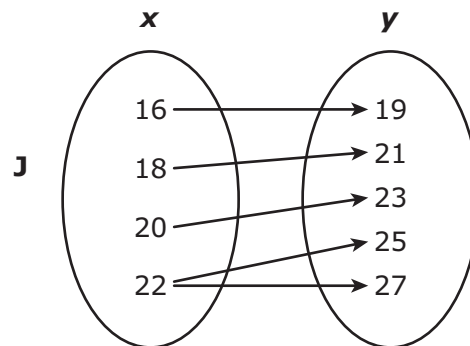
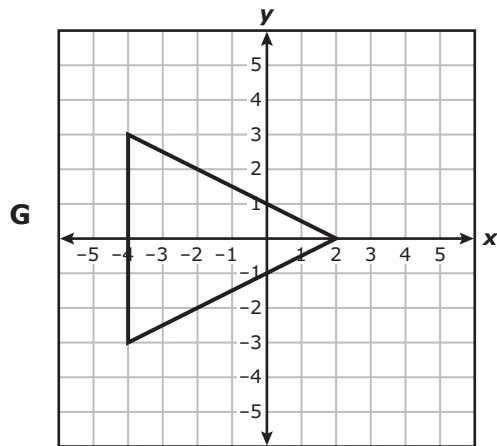
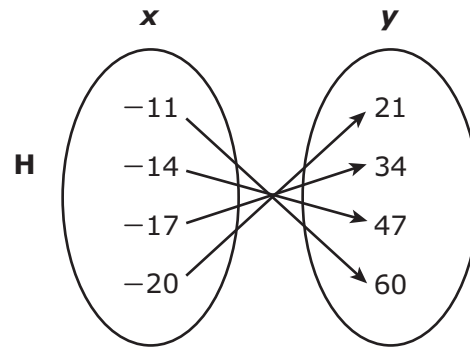
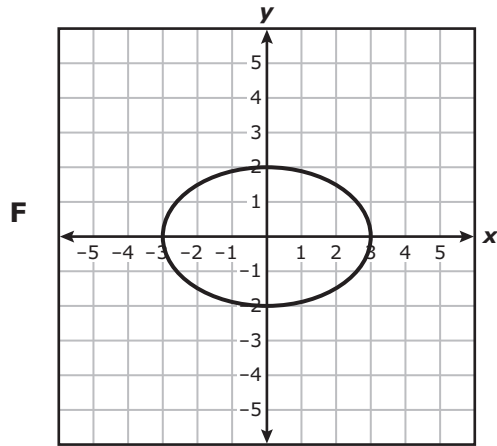
DIRECTIONS

Read each question carefully. For a multiple-choice question, determine the best answer to the question from the four answer choices provided. For a griddable question, determine the best answer to the question. Then fill in the answer on your answer document.

- 1 Trapezoid $WKRP$ was translated 4 units to the left and 5 units up on a coordinate grid to create trapezoid $W'K'R'P'$. Which rule describes this transformation?

- A $(x, y) \rightarrow (x - 4, y + 5)$
- B $(x, y) \rightarrow (x + 4, y - 5)$
- C $(x, y) \rightarrow (x + 4, y + 5)$
- D $(x, y) \rightarrow (x - 4, y - 5)$

2 Which representation shows y as a function of x ?



3 A bowling ball shaped like a sphere has a diameter of 21.6 centimeters. Which measurement is closest to the volume of the bowling ball in cubic centimeters?

- A 1,954.3 cm³
- B 5,276.7 cm³
- C 488.6 cm³
- D 42,213.4 cm³

4 A customer will borrow \$12,000 to buy a car. Which loan option would allow the customer to pay the least amount of interest?

F A 4-year loan with a 5.2% annual simple interest rate

G A 5-year loan with a 4.2% annual simple interest rate

H A 6-year loan with a 4.7% annual simple interest rate

J A 3-year loan with an 8.4% annual simple interest rate

5 Which table represents a non-proportional relationship between x and y ?

A

x	y
1	-4
3	-12
7	-28
15	-60

C

x	y
1	7.5
4	30
7	52.5
10	75

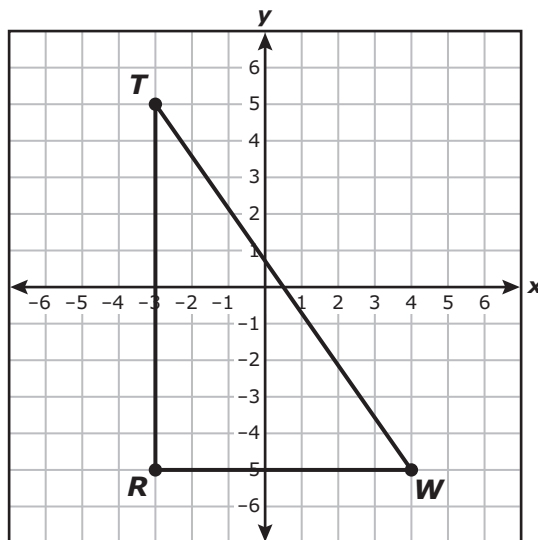
B

x	y
-17	93.5
-5	27.5
2	-11
10	-55

D

x	y
-5	11
-1	-1
1	-7
8	-28

- 6 Triangle TRW is shown on the coordinate grid.



Triangle TRW will be dilated by a scale factor of n with the origin as the center of dilation to create triangle $T'R'W'$. Which ordered pair best represents the location of point R' ?

F $(-\frac{3}{n}, -\frac{5}{n})$

G $(-3n, -5n)$

H $(-3 + n, -5 + n)$

J $(-3 - n, -5 - n)$

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- 7 A student's parents invested \$5,000 in a college savings account that pays 4.85% annual simple interest. No additional deposits or withdrawals will be made.

Which amount is closest to the interest earned on the account at the end of 15 years?

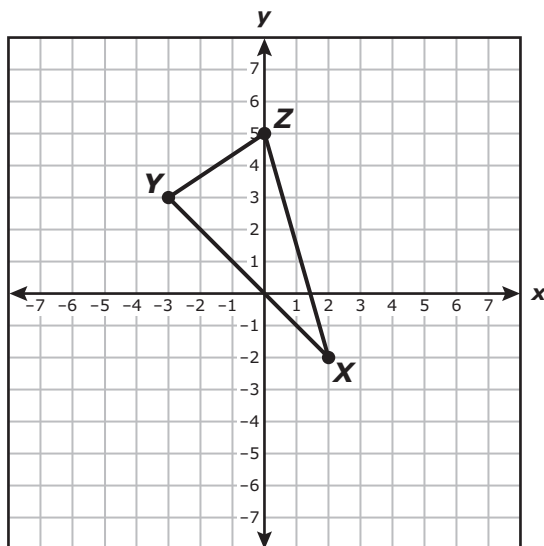
A \$5,174.11

B \$10,174.11

C \$3,637.50

D \$8,637.50

- 8 Triangle XYZ is rotated 90° clockwise about the origin to form triangle $X'Y'Z'$.



Which statement is true?

- F** The sum of the angle measures of triangle XYZ is 90° less than the sum of the angle measures of triangle $X'Y'Z'$.
- G** The angle measures of triangle XYZ are less than the corresponding angle measures of triangle $X'Y'Z'$.
- H** Triangle XYZ is not congruent to triangle $X'Y'Z'$.
- J** The area of triangle XYZ is equal to the area of triangle $X'Y'Z'$.

9 A college has two classrooms of students.

- Classroom A had 70 students.
- Classroom B had 30 students.
- Classroom A sent groups of 4 students to Classroom B until both classrooms had the same number of students.

The equation shown can be used to find the number of groups that Classroom A sent to Classroom B so each classroom had the same number of students.

$$70 - 4x = 30 + 4x$$

How many groups did Classroom A send to Classroom B?

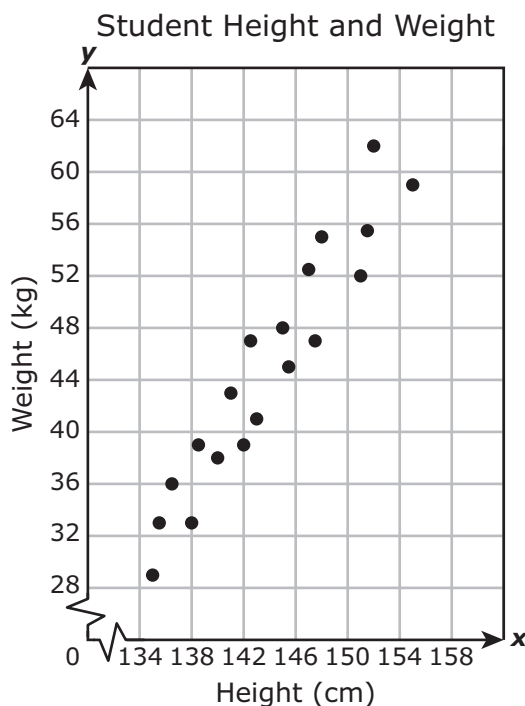
Record your answer and fill in the bubbles on your answer document. Be sure to use the correct place value.

- 10** A water tank currently contains 275 gallons of water. The amount of water in the tank will decrease at a constant rate of 15 gallons per week.

Which function can be used to find t , the total number of gallons of water in the tank after w weeks?

- F** $t = 15w - 275$
G $t = -15w + 275$
H $t = 275w - 15$
J $t = -275w + 15$
-

- 11** The scatterplot shows the height in centimeters and weight in kilograms of several students.



Based on the scatterplot, which is the best prediction of the height in centimeters of a student with a weight of 64 kilograms?

- A** 152 cm
B 160 cm
C 162 cm
D 156 cm

12 A transformation is applied to a figure to create a new figure on a coordinate grid. Which transformation does NOT preserve congruence?

- F** A rotation of 270° counterclockwise
- G** A reflection across the y -axis
- H** A dilation by a scale factor of 1.5
- J** A translation of 50 units down

13 A teacher bought markers at a cost of \$3 per set. The teacher had a \$2-off coupon to use toward the total cost of the markers bought.

Which table shows the relationship between x , the number of sets of markers bought by the teacher, and y , the total cost of the markers?

A Markers

Sets of Markers Bought, x	Total Cost, y
3	\$7
9	\$25
12	\$34
24	\$70

C Markers

Sets of Markers Bought, x	Total Cost, y
3	\$11
9	\$29
12	\$38
24	\$74

B Markers

Sets of Markers Bought, x	Total Cost, y
9	\$1
12	\$2
15	\$3
24	\$6

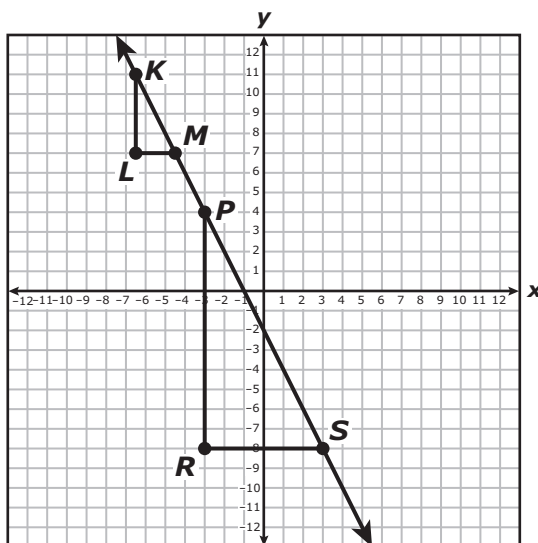
D Markers

Sets of Markers Bought, x	Total Cost, y
9	\$5
12	\$6
15	\$7
24	\$10

- 14 The diameter of a cylinder is 2.5 inches, and the height is 7.5 inches. Which equation can be used to find V , the volume of the cylinder in cubic inches?

- F $V = \pi(2.5)^2(7.5)$
- G $V = \pi(7.5)^2(2.5)$
- H $V = \pi(1.25)^2(7.5)$
- J $V = \pi(3.75)^2(2.5)$

- 15 Triangle KLM and triangle PRS are similar right triangles.



Which proportion can be used to show that the slope of \overline{KM} is equal to the slope of \overline{PS} ?

- A $\frac{KL}{LM} = \frac{PR}{RS}$
- B $\frac{RS}{SP} = \frac{LM}{MK}$
- C $\frac{ML}{LK} = \frac{SP}{RP}$
- D $\frac{PS}{PR} = \frac{KM}{KL}$

- 16** The table shows the diagonal lengths of TV screens at a store.

TV Screen Diagonal Lengths

Screen	Length (feet)
W	$\sqrt{12.25}$
X	$2\frac{1}{6}$
Y	$\frac{37}{\sqrt{144}}$
Z	$\frac{8}{3}$

Which TV screen has the smallest diagonal length in feet?

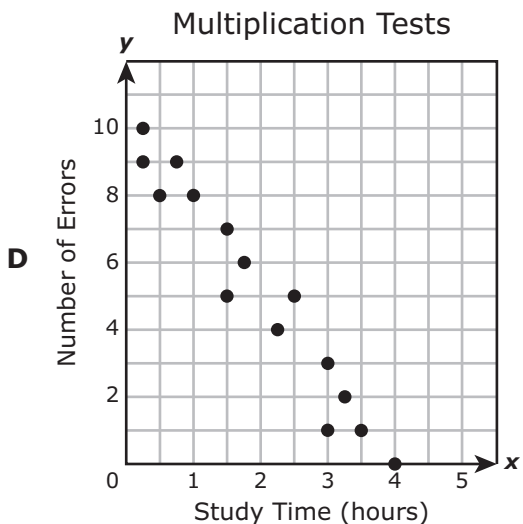
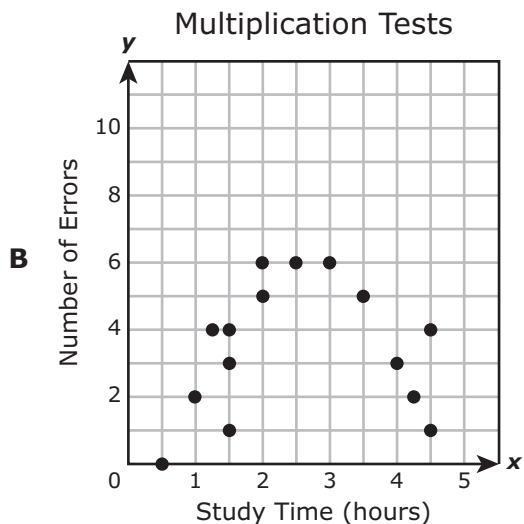
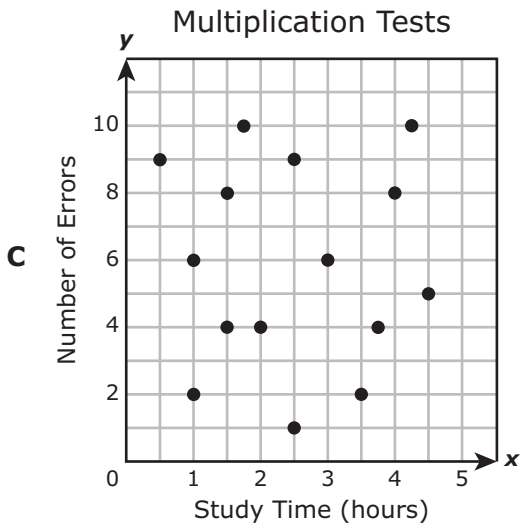
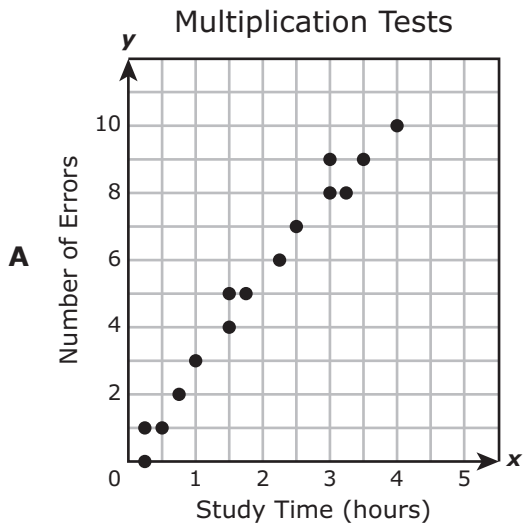
F W

G X

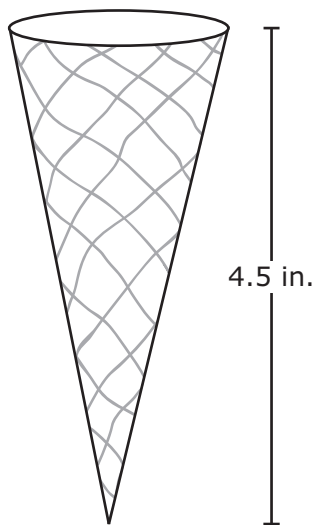
H Y

J Z

17 A math teacher observed that as the number of hours students studied their multiplication facts increased, the number of errors the students made on their multiplication tests decreased. Which scatterplot could support this teacher’s observation?



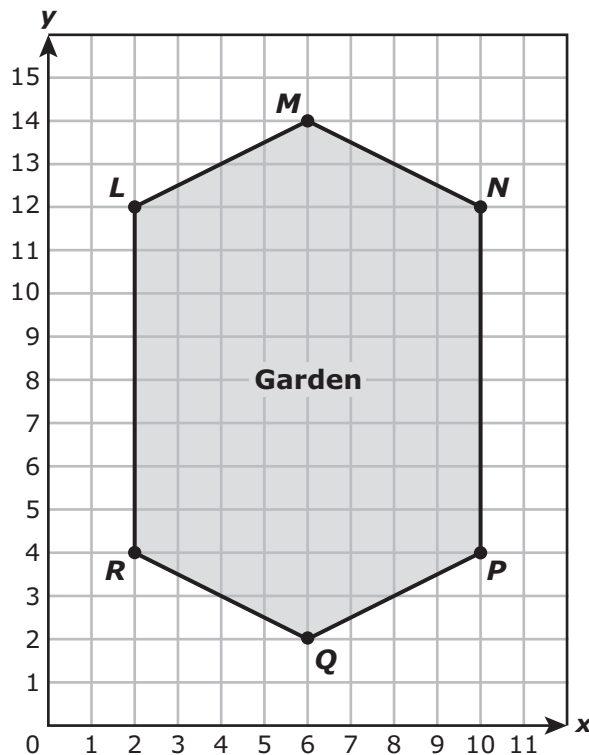
- 18** The diagram shows the height of a cone that holds ice cream. The cone has a volume of 1.5π cubic inches.



Which measurement is closest to the radius of the cone in inches?

- F** 0.6 in.
G 1.4 in.
H 1.0 in.
J 0.5 in.
-
- 19** Which set of ordered pairs represents y as a function of x ?
- A** $\{(0, 0.5), (2, 1.5), (-5.5, 5), (-5.5, -6)\}$
B $\{(5, -7), (3, -7), (-9.2, -7), (9.2, -7)\}$
C $\{(9.3, -1), (7.3, -2), (7.3, 2), (9.3, 1)\}$
D $\{(8.1, 9), (9.1, 10), (10.1, 9), (9.1, 8)\}$

- 20** Polygon $LMNPQR$ is shown on the coordinate grid and models the shape of a garden in a park. Polygon $LMNPQR$ will be dilated with the origin as the center of dilation to create polygon $L'M'N'P'Q'R'$. The vertex Q' will be located at $(21, 7)$.



Which rule best represents the dilation?

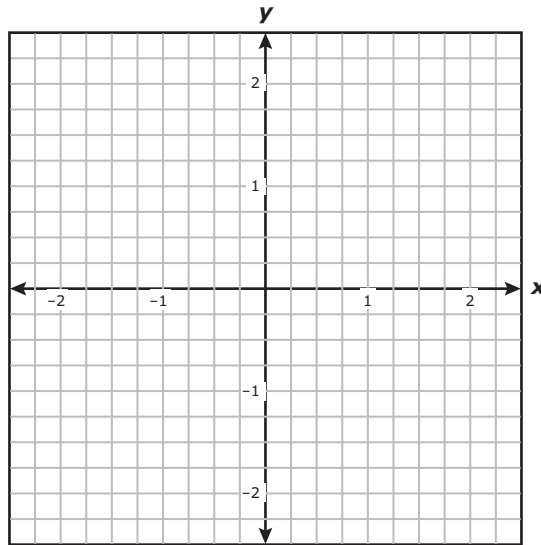
F $(x, y) \rightarrow (\frac{2}{7}x, \frac{2}{7}y)$

G $(x, y) \rightarrow (x + 15, y + 5)$

H $(x, y) \rightarrow (x - 15, y - 5)$

J $(x, y) \rightarrow (\frac{7}{2}x, \frac{7}{2}y)$

- 21** The graph of a linear function passes through the points $(-1, -\frac{1}{4})$ and $(1, -\frac{3}{4})$.



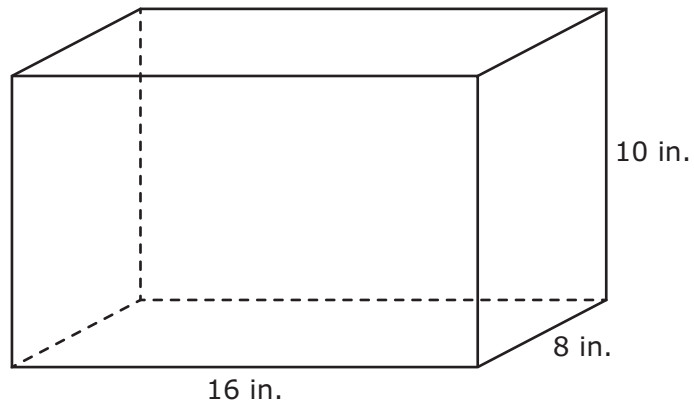
Which equation represents the function?

- A** $y = -\frac{1}{2}x - \frac{1}{4}$
- B** $y = \frac{1}{2}x + \frac{1}{4}$
- C** $y = -\frac{1}{4}x - \frac{1}{2}$
- D** $y = \frac{1}{4}x + \frac{1}{2}$

-
- 22** The area of a piece of land is 4,951,000 square meters. How is this number of square meters written in scientific notation?

- F** 4.951×10^6
- G** 4.951×10^{-6}
- H** $4,951 \times 10^3$
- J** $4,951 \times 10^{-3}$

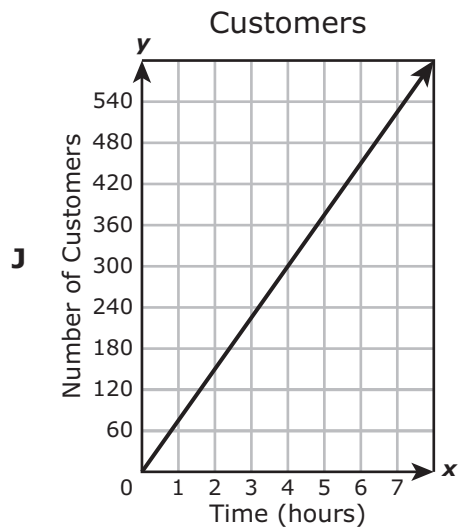
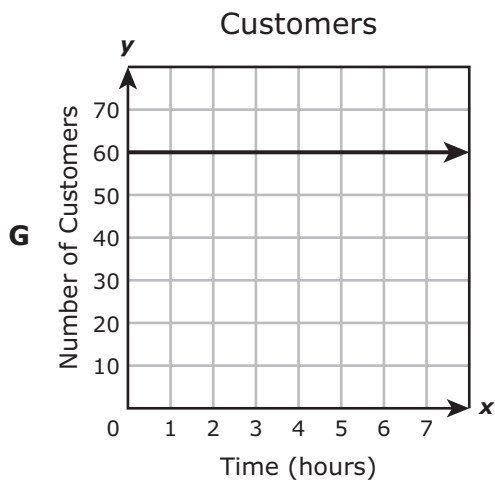
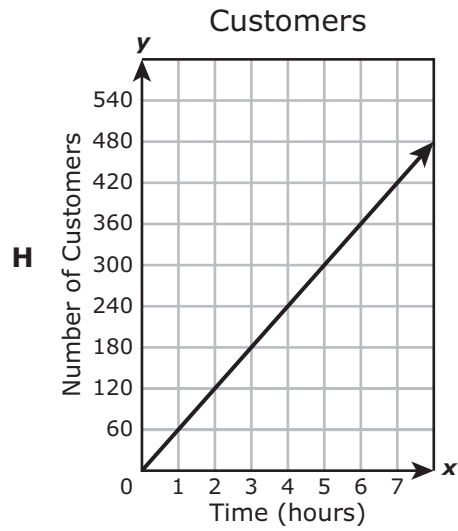
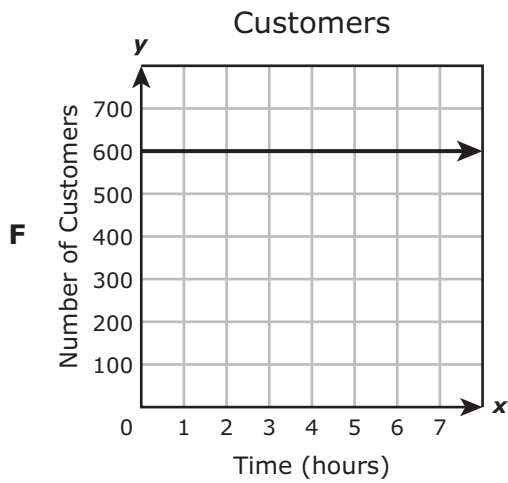
- 23** The dimensions of a rectangular prism are shown in the diagram.



What is the total surface area in square inches of the prism?

Record your answer and fill in the bubbles on your answer document. Be sure to use the correct place value.

- 24 At a restaurant 600 customers were served during a 10-hour period of time. Which graph has a slope that best represents the number of customers that were served per hour at this restaurant?



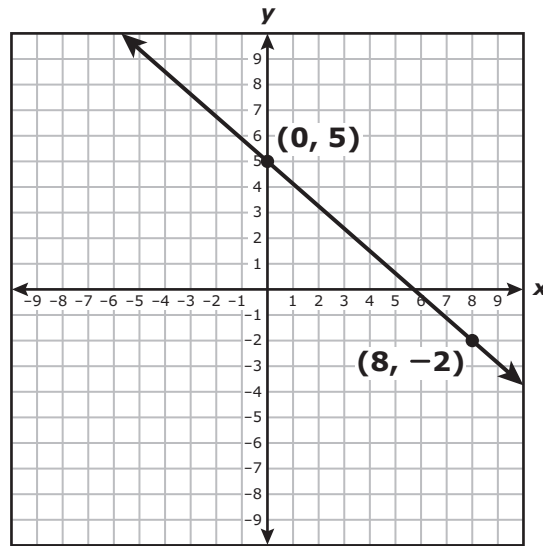
25 Ben deposits \$1,750 into each of two savings accounts.

- Account I earns 2.75% annual simple interest.
- Account II earns 2.75% interest compounded annually.

Ben does not make any additional deposits or withdrawals. Which amount is closest to the difference between the interest Ben will earn in Account I and the interest Ben will earn in Account II at the end of 2 years?

- A** \$96.25
- B** \$1.32
- C** \$97.57
- D** \$193.82

- 26** A linear function is represented on the coordinate grid.



What is the y -intercept of the graph of this function?

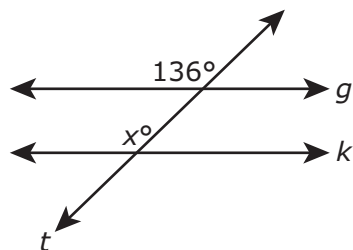
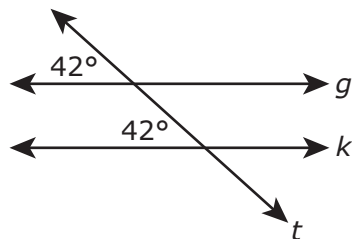
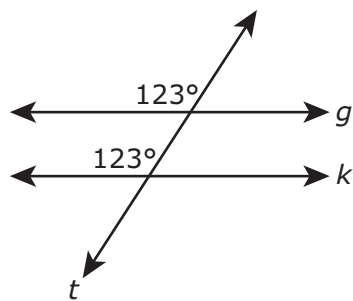
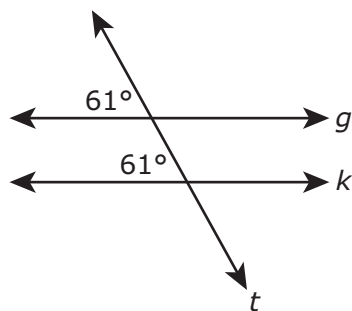
F 5

G 6

H $-\frac{7}{8}$

J $-\frac{8}{7}$

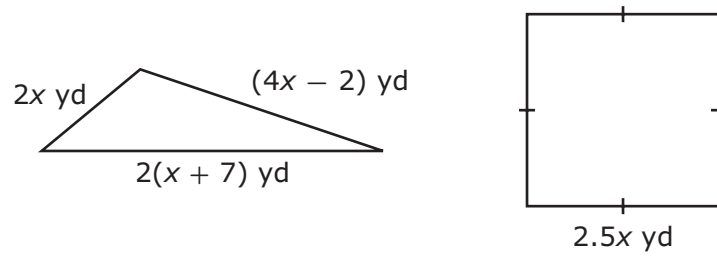
- 27** In each diagram, line g is parallel to line k , and line t intersects lines g and k .



Based on the diagrams, which statement about x is true?

- A** The value of x is 180, because the labeled angles in each diagram are supplementary and the sum of the measures of supplementary angles is 180 degrees.
- B** The value of x is 90, because the labeled angles in each diagram are complementary and the sum of the measures of complementary angles is 90 degrees.
- C** The value of x is 44, because the sum of the measures of the labeled angles in each diagram is 180 degrees.
- D** The value of x is 136, because the labeled angles in each diagram are congruent.

- 28** The side lengths in yards of a triangle and a square are shown in the diagram.



The perimeter of the triangle is equal to the perimeter of the square. What is the value of x ?

F -4

G $\frac{2}{3}$

H 6

J $\frac{5}{2}$

- 29** A teacher opened an investment account at a bank. At the end of each year, the bank paid 6.4% annual simple interest on the money in the account. The table shows the activity in the account for three years.

Investment Account Activity

Year	Beginning Balance for Year	Amount Deposited at Beginning of Year	New Balance	Interest Rate	Interest Earned	Ending Balance for Year
1	\$0.00	\$500.00	\$500.00	6.4%	\$32.00	\$532.00
2	\$532.00	\$500.00	\$1,032.00	6.4%	\$66.05	\$1,098.05
3	\$1,098.05	\$500.00	\$1,598.05	6.4%	\$102.28	\$1,700.33

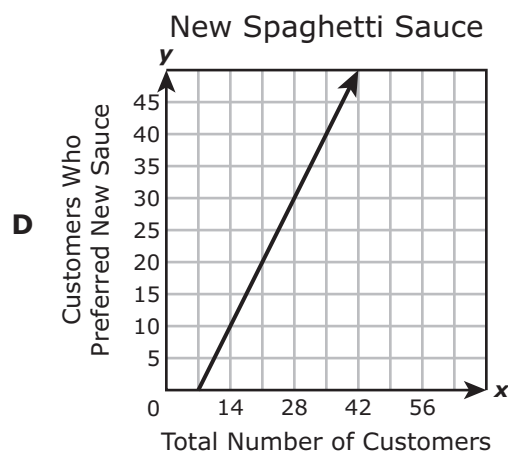
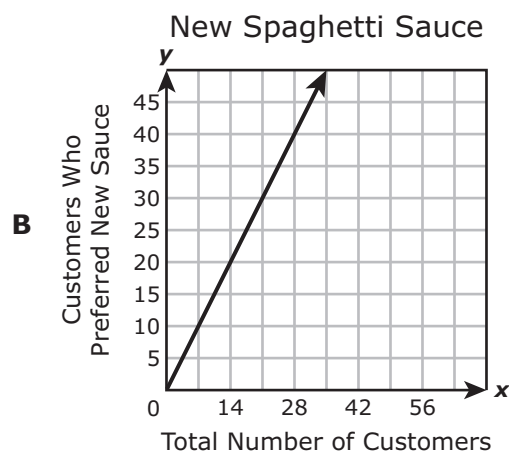
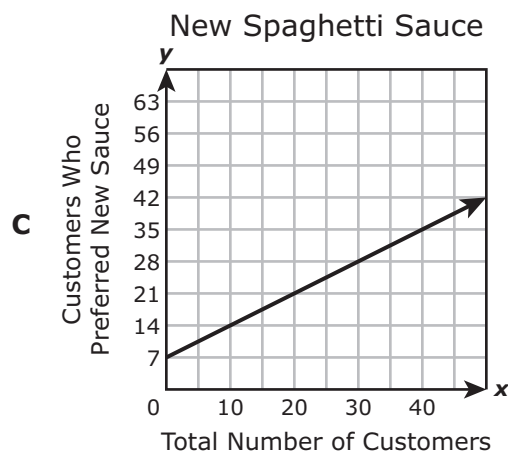
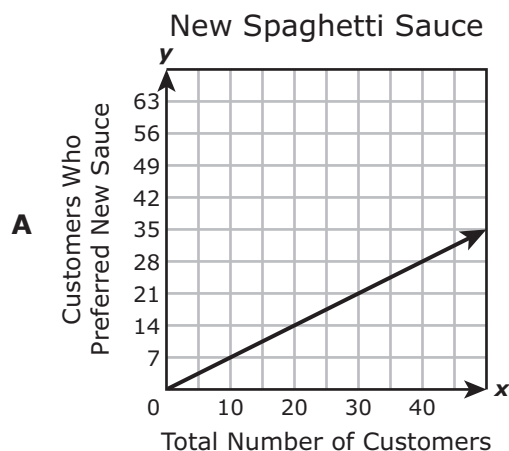
Which statement explains why the balance in this account has grown?

- A** The balance in the account has grown only because regular deposits were made to the account.
- B** The balance in the account has grown because regular deposits were made to the account and interest was earned on the previous year's balance.
- C** The balance in the account has grown only because interest was earned on the account.
- D** There is not enough information to determine why the balance in the account has grown.

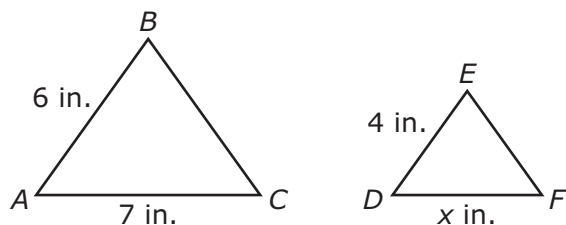
30 A figure was transformed on a coordinate grid using the rule $(x, y) \rightarrow (-x, -y)$. Which of the following describes this transformation?

- F** A reflection across the x -axis
- G** A reflection across the y -axis
- H** A 90° clockwise rotation about the origin
- J** A 180° clockwise rotation about the origin

31 A survey of customers at a restaurant revealed that 7 out of 10 customers preferred the restaurant's new spaghetti sauce. Which graph shows the relationship between y , the number of customers who preferred the new spaghetti sauce, and x , the total number of customers?



- 32** Triangle ABC and triangle DEF are similar.



Which proportion must be true?

F $\frac{7}{x} = \frac{4}{6}$

G $\frac{4}{6} = \frac{x}{7}$

H $\frac{6}{4} = \frac{x}{7}$

J $\frac{4}{x} = \frac{7}{6}$

-
- 33** Which list shows these numbers in order from least to greatest?

$$\sqrt{38}, -6.35, 63\%, -\frac{19}{3}$$

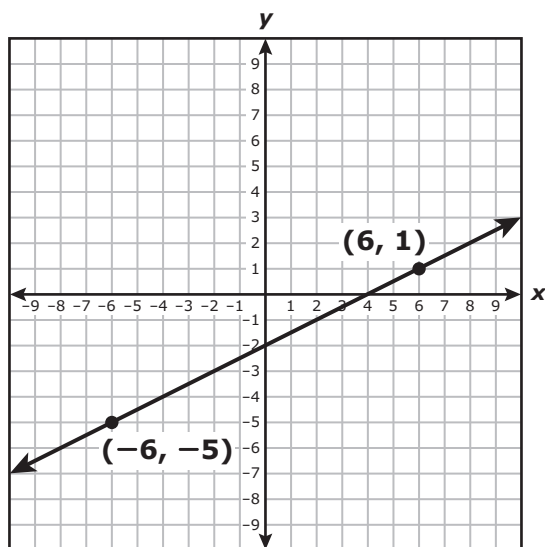
A $-6.35, -\frac{19}{3}, 63\%, \sqrt{38}$

B $63\%, \sqrt{38}, -\frac{19}{3}, -6.35$

C $-6.35, -\frac{19}{3}, \sqrt{38}, 63\%$

D $-\frac{19}{3}, -6.35, 63\%, \sqrt{38}$

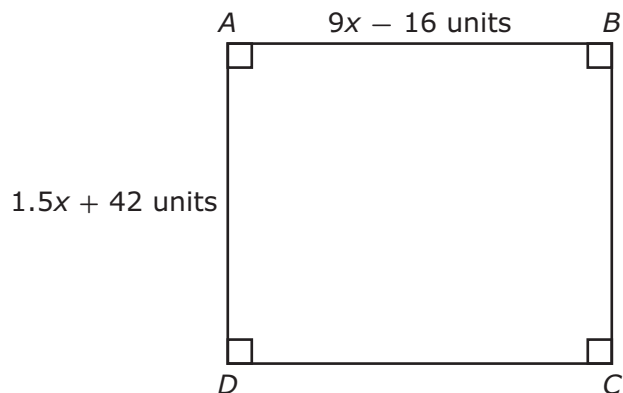
- 34** The graph of a linear function is shown on the coordinate grid.



What is the slope of the graph of this function in decimal form?

Record your answer and fill in the bubbles on your answer document. Be sure to use the correct place value.

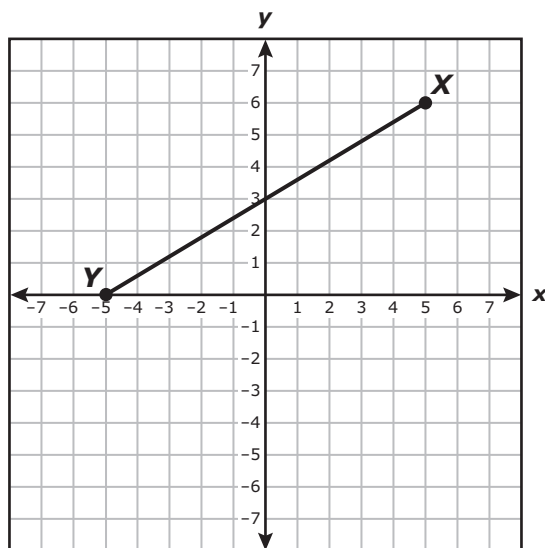
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- 35** Rectangle $ABCD$ is shown with the dimensions given in units.



The length of \overline{AB} is greater than the length of \overline{AD} . Which inequality represents this situation?

- A** $9x - 16 < 1.5x + 42$
- B** $9x - 16 > 1.5x + 42$
- C** $10.5x < 26$
- D** $10.5x > 26$

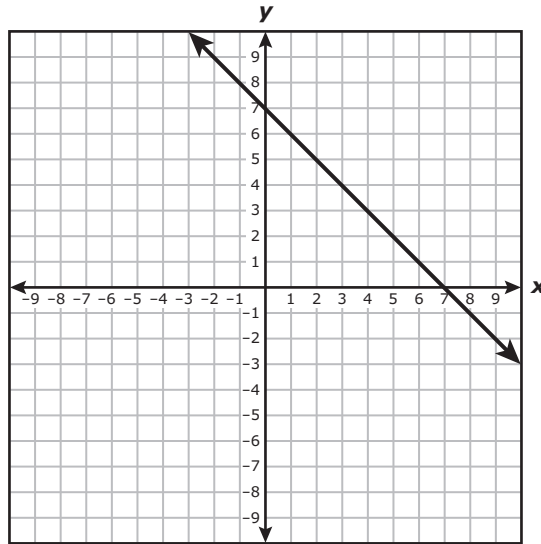
- 36 The coordinate grid shows \overline{XY} .



Which measurement is closest to the length of \overline{XY} in units?

- F 7.8 units
- G 16.0 units
- H 13.0 units
- J 11.7 units

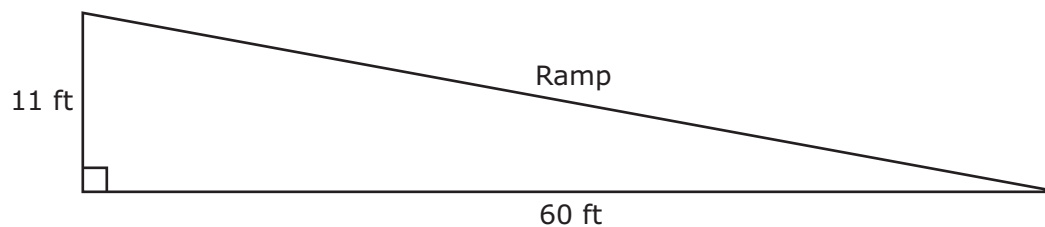
37 The graph shows a relationship between x and y .



Which statement is true?

- A** The graph shows a non-proportional relationship because the graph has a negative slope.
- B** The graph shows a non-proportional relationship because the graph does not contain the origin.
- C** The graph shows a proportional relationship because the x and y intercepts both contain 7.
- D** The graph shows a proportional relationship because the graph passes through 3 different quadrants.

- 38** The diagram represents a ramp in the shape of a right triangle and the lengths of two of its sides in feet.



What is the length of the ramp in feet?

Record your answer and fill in the bubbles on your answer document. Be sure to use the correct place value.

- 39** A student solved the equation $x^2 = 132$ to find the length of the diagonal of a square in centimeters. Which measurement is closest to x , the length of the diagonal of this square, in centimeters?

A 66 cm
B 44 cm
C 33 cm
D 11 cm

- 40** The table shows the dimensions of three cylinders.

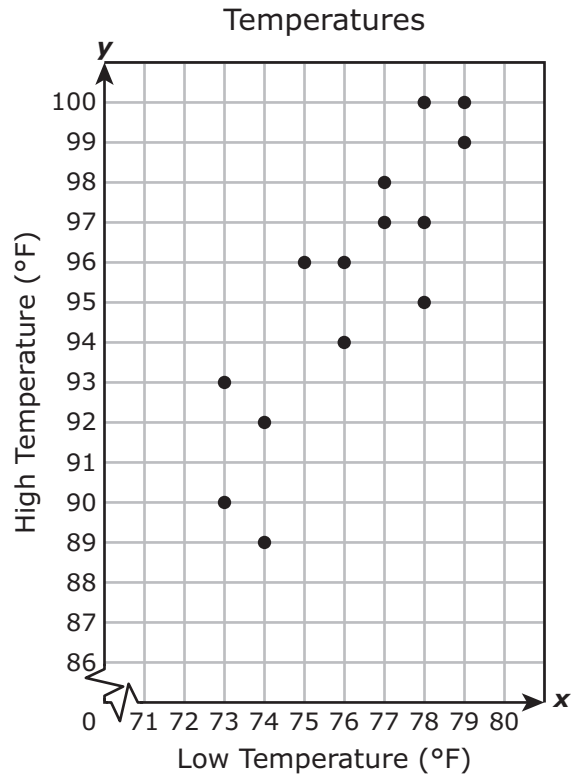
Cylinders

Cylinder	Radius (inches)	Height (inches)
W	3	9
X	4	2
Y	4.5	6

Which two cylinders have the same lateral surface area in square inches?

F Cylinders W and Y
G Cylinders W and X
H Cylinders X and Y
J None of these

- 41** The scatterplot shows the low temperature and high temperature each day for a two-week period of time.

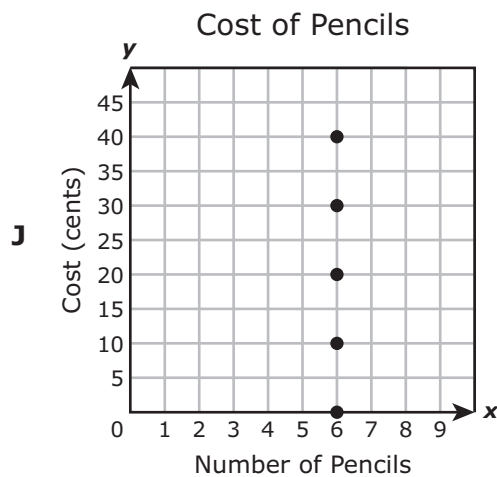
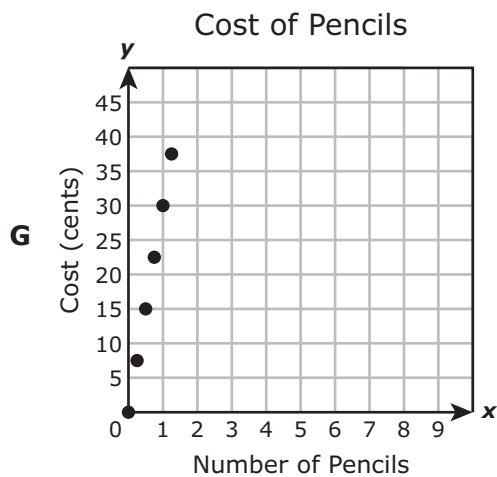
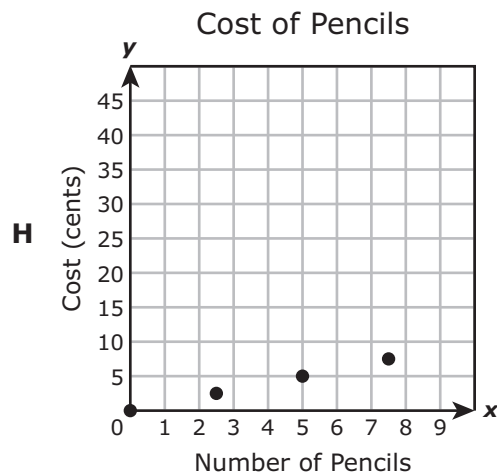
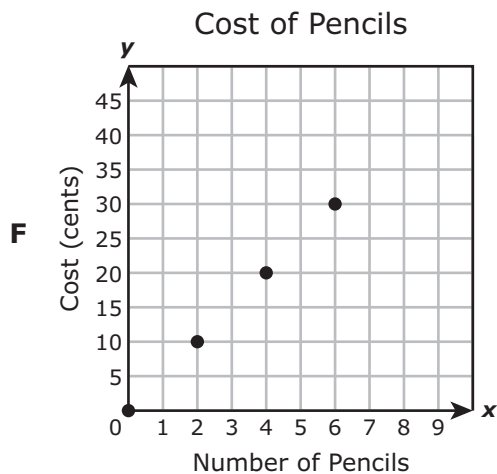


Based on the scatterplot, which is the best prediction of the high temperature in degrees Fahrenheit on a day when the low temperature is 71 °F?

- A** 92 °F
- B** 101 °F
- C** 88 °F
- D** 100 °F

- 42** The cost of 6 pencils at a store is 30 cents. Each pencil has the same cost.

Which graph has a slope that best represents the cost of each pencil at this store?



Item Number	Reporting Category	Readiness or Supporting	Content Student Expectation	Correct Answer
1	3	Readiness	8.10(C)	A
2	2	Readiness	8.5(G)	H
3	3	Readiness	8.7(A)	B
4	4	Supporting	8.12(A)	F
5	2	Supporting	8.5(H)	D
6	3	Readiness	8.3(C)	G
7	4	Readiness	8.12(D)	C
8	3	Supporting	8.10(A)	J
9	2	Readiness	8.8(C)	5
10	2	Readiness	8.5(I)	G
11	4	Readiness	8.5(D)	D
12	3	Supporting	8.10(B)	H
13	2	Supporting	8.5(B)	A
14	3	Supporting	8.6(A)	H
15	2	Supporting	8.4(A)	A
16	1	Readiness	8.2(D)	G
17	4	Supporting	8.11(A)	D
18	3	Readiness	8.7(A)	H
19	2	Readiness	8.5(G)	B
20	3	Readiness	8.3(C)	J
21	2	Readiness	8.5(I)	C
22	1	Supporting	8.2(C)	F
23	3	Readiness	8.7(B)	736
24	2	Readiness	8.4(B)	H
25	4	Readiness	8.12(D)	B
26	2	Readiness	8.4(C)	F
27	3	Supporting	8.8(D)	D
28	2	Readiness	8.8(C)	H
29	4	Supporting	8.12(C)	B
30	3	Readiness	8.10(C)	J
31	2	Supporting	8.5(A)	A
32	3	Supporting	8.3(A)	G
33	1	Readiness	8.2(D)	A
34	2	Readiness	8.4(C)	0.5
35	2	Supporting	8.8(A)	B
36	3	Supporting	8.7(D)	J
37	2	Supporting	8.5(F)	B
38	3	Readiness	8.7(C)	61
39	1	Supporting	8.2(B)	D
40	3	Readiness	8.7(B)	F
41	4	Readiness	8.5(D)	C
42	2	Readiness	8.4(B)	F

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
1	Option A is correct	To identify the rule that describes the transformation (change of a shape using a rotation (circular movement), reflection (flip), translation (slide), or dilation (resize)), the student should have recognized that when a shape is translated 4 units to the left, each x -coordinate (horizontal position from 0) is decreased by 4 units, which is represented by the expression $x - 4$. When a shape is translated 5 units up, each y -coordinate (vertical position from 0) is increased by 5 units, which is represented by the expression $y + 5$. Therefore the rule $(x, y) \rightarrow (x - 4, y + 5)$ describes this transformation.
	Option B is incorrect	The student likely reversed the relationship between the effect on x and y and identified the rule for translating the figure 4 units to the right and 5 units down. The student needs to focus on writing rules for translations and explaining the effect.
	Option C is incorrect	The student likely reversed the relationship of the effect on x and translated the figure to the right rather than to the left and identified the rule for translating the figure 4 units to the right and 5 units up. The student needs to focus on writing rules for translations and explaining the effect.
	Option D is incorrect	The student likely reversed the relationship of the effect on y and translated the figure down rather than up and identified the rule for translating the figure 4 units to the left and 5 units down. The student needs to focus on writing rules for translations and explaining the effect.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
2	Option H is correct	To identify the representation of y as a function of x , the student should have determined that in order for the representation to show a function (a relationship where each input (value put into an equation, x) has a single output (value that comes out of the equation, y)), each value of x can only be paired with one value of y . The mapping shows each of the four values of x mapped to a single value of y . Therefore this representation shows y as a function of x .
	Option F is incorrect	The student likely did not recognize that the x -values of -1 and 1 have two y -values, and therefore the graph does not represent a function. The student needs to focus on the definition of a function and on applying it to determine whether a set of ordered pairs that are part of a graphed line represents a function.
	Option G is incorrect	The student likely did not recognize that the x -values of -3 and -2 have two y -values, and therefore the graph does not represent a function. The student needs to focus on the definition of a function and on applying it to determine whether a set of ordered pairs that are part of a graphed line represents a function.
	Option J is incorrect	The student likely confused which variable (symbol used to represent an unknown number) was the input of the function and which variable was the output of the function. The student needs to focus on how to determine whether any of the given representations show a function by determining whether each value of x is paired with a single value of y .

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
3	Option B is correct	To determine the volume (amount of three-dimensional space taken up) of the bowling ball shaped like a sphere in cubic centimeters, the student should have used the formula for the volume of a sphere, $V = \frac{4}{3}\pi r^3$. To determine the value of r , the radius (distance from the center to the circumference of a circle), the student should have divided the diameter (straight line going through the center of a circle connecting two points on the circumference) by 2. The student should have then evaluated $V = \frac{4}{3}\pi(10.8)^3$, which is approximately equal to 5,276.7.
	Option A is incorrect	The student likely used the length of the diameter in place of the radius in the volume formula and squared the diameter instead of cubing the diameter. The student needs to focus on understanding and properly applying the formula for determining the volume of a sphere.
	Option C is incorrect	The student likely used the correct formula to calculate the volume of the sphere but squared the radius instead of cubing the radius. The student needs to focus on understanding and properly applying the formula for determining the volume of a sphere.
	Option D is incorrect	The student likely used the length of the diameter in place of the radius in the volume formula. The student needs to focus on understanding and properly applying the formula for determining the volume of a sphere.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
4	Option F is correct	To determine the loan option that would allow the customer to pay the least amount of interest, the student should have first calculated the amount of interest for each option using the simple interest formula $I = Prt$, in which P represents the principal (initial loan amount), r represents the rate (in decimal form), and t represents the length of time in years. To determine the amount of interest for a 4-year loan with a 5.2% annual simple interest rate (option A), the student should have calculated $I = (\$12,000)(0.052)(4) = \$2,496$. To determine the amount of interest for a 5-year loan with a 4.2% annual simple interest rate (option B), the student should have calculated $I = (\$12,000)(0.042)(5) = \$2,520$. To determine the amount of interest for a 6-year loan with a 4.7% annual simple interest rate (option C), the student should have calculated $I = (\$12,000)(0.047)(6) = \$3,384$. To determine the amount of interest for a 3-year loan with an 8.4% annual simple interest rate (option D), the student should have calculated $I = (\$12,000)(0.084)(3) = \$3,024$. Finally the student should have determined that a 4-year loan with a 5.2% annual simple interest rate (option A) results in the least amount of interest.
	Option G is incorrect	The student likely thought the lowest interest rate (4.2%) would result in the least amount of interest. The student needs to focus on attending to the details of the question in problems.
	Option H is incorrect	The student likely thought the question was asking for the greatest amount of interest instead of the least amount of interest. The student needs to focus on attending to the details of the question in problems.
	Option J is incorrect	The student likely thought the shortest length of time (3 years) would result in the least amount of interest. The student needs to focus on attending to the details of the question in problems.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
5	Option D is correct	To determine which table appears to show a non-proportional relationship between x and y , the student should have recognized that in a non-proportional relationship, the y -value is not equal to 0 when the corresponding (paired) x -value is 0. In this table, when the x -value is equal to 0, the corresponding y -value would equal -4 .
	Option A is incorrect	The student likely identified that the given x -values do not increase at a constant rate but likely did not use the pattern in the table to determine that when $x = 0$, $y = 0$. The student needs to focus on understanding the definition of a proportional relationship and on applying it to determine whether a table represents a proportional relationship or a non-proportional relationship.
	Option B is incorrect	The student identified a table that has two x -values that are negative (-17 and -5) and could have thought the relationship was non-proportional as a result of the negative x -values. The student likely did not use the pattern in the table to determine that when $x = 0$, $y = 0$. The student needs to focus on understanding the definition of a proportional relationship and on applying it to determine whether a table represents a proportional relationship or a non-proportional relationship.
	Option C is incorrect	The student likely reversed the meaning of a proportional relationship and a non-proportional relationship. The table shows a proportional relationship since the pattern in the table can be extended to show when $x = 0$, $y = 0$. The student needs to focus on understanding the definition of a proportional relationship and on applying it to determine whether a table represents a proportional relationship or a non-proportional relationship.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
6	Option G is correct	To determine the ordered pair that best represents the location of point R' , the student should have determined that when a figure is dilated (enlarged or reduced in size), its measurements increase or decrease based on the scale factor (ratio of the length of a side of one figure to the length of the corresponding (paired) side of a similar figure). A scale factor of n , with the origin (point where the x -axis (horizontal) and y -axis (vertical) on a coordinate grid intersect (cross); also, the point represented by the ordered pair $(0, 0)$) as the center of dilation means that each point on the dilated figure will be n times as far from the origin as it was on the original figure. If the location of point R was originally represented by $(-3, -5)$, then the location of the corresponding point on the dilated figure, point R' , will be $(-3n, -5n)$.
	Option F is incorrect	The student divided the x - and y -coordinates by the scale factor instead of multiplying them by n . The student needs to focus on the effect a dilation by a given scale factor has on a figure and how to determine the rule to explain the effect.
	Option H is incorrect	The student added the scale factor instead of multiplying by n . The student needs to focus on understanding how the scale factor affects the dilation.
	Option J is incorrect	The student subtracted the scale factor instead of multiplying by n . The student needs to focus on understanding how the scale factor affects the dilation.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
7	Option C is correct	To determine the amount of interest the account earned at the end of 15 years, the student should have used the formula $I = Prt$, in which P represents the principal (initial loan amount), r represents the interest rate (in decimal form), and t represents the length of time in years. Using the given information, the student should have written the equation as $I = (\$5,000)(0.0485)(15)$, which results in \$3,637.50.
	Option A is incorrect	The student likely calculated the amount of interest using the formula for compound interest, $A = P(1 + r)^t$, first calculating $A = (\$5,000)(1 + 0.0485)^{15} = \$10,174.11$. Then subtracting the principal from the total, calculating $\$10,174.11 - \$5,000 = \$5,174.11$. The student needs to focus on understanding the difference between simple and compound interest, the formula for each, and how to apply them.
	Option B is incorrect	The student likely calculated the balance in the account using the formula for compound interest, $A = P(1 + r)^t$, calculating $A = (\$5,000)(1 + 0.0485)^{15} = \$10,174.11$. The student needs to focus on understanding the difference between simple and compound interest, the formula for each, and how to apply them.
	Option D is incorrect	The student likely calculated the balance in the account. The student used the correct formula but added the interest to the principal, calculating $\$3,637.50 + \$5,000 = \$8,637.50$. The student needs to focus on attending to the details of the question in problems.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
8	Option J is correct	To determine the statement that is true, the student should have determined that because a rotation (circular movement) preserves congruence (same shape and size), triangle $X'Y'Z'$ will be congruent to triangle XYZ , which means the area of triangle XYZ is equal to the area of triangle $X'Y'Z'$.
	Option F is incorrect	The student likely misunderstood the effect a rotation has on the angle measures of a figure and thought that the sum (total) of the angle measures of triangle $X'Y'Z'$ would be 90° greater than the sum of the angle measures of triangle XYZ . The student needs to focus on the effect a rotation has on a figure and on the fact that a rotation preserves congruence.
	Option G is incorrect	The student likely misunderstood the effect a rotation has on the angle measures of a figure and thought that the corresponding (paired) angle measures of triangle $X'Y'Z'$ would be greater than the corresponding angle measures of triangle XYZ . The student needs to focus on the effect a rotation has on a figure and on the fact that a rotation preserves congruence.
	Option H is incorrect	The student likely misunderstood the effect a rotation has on the congruency of a figure and thought that triangle $X'Y'Z'$ would not be congruent to triangle XYZ . The student needs to focus on the effect a rotation has on a figure and on the fact that a rotation preserves congruence.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
9	5 and any equivalent values are correct	To determine the number of groups that Classroom A sent to Classroom B, the student could have solved the given equation for x . The student could have first added $4x$ to both sides of the equation, resulting in $70 = 30 + 8x$. The student then could have subtracted 30 from both sides of the equation, resulting in $40 = 8x$. Finally, the student could have divided both sides of the equation by 8, resulting in $x = 5$. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
10	Option G is correct	<p>To determine which function (equation) represents t, the total number of gallons of water in the tank after w weeks, the student could have determined the values of m and b in the slope-intercept form of the line, $y = mx + b$. The m represents the rate of change (also referred to as slope, which is the steepness of a straight line when graphed on a coordinate grid; $m = \frac{y_2 - y_1}{x_2 - x_1}$). The b represents the y-intercept (value where the line crosses the y-axis (vertical)) and the initial value in the scenario. In this scenario the student should have thought of the slope-intercept form of line $y = mx + b$, replacing y with t and x with w, resulting in $t = mw + b$. The student then should have determined “the amount of water in the tank will decrease at a constant rate of 15 gallons per week” represents the rate of change (m) and “currently contains 275 gallons of water” represents the y-intercept (b). The student should have substituted these values into the slope-intercept form of the line for this scenario, resulting in $t = -15w + 275$.</p>
	Option F is incorrect	<p>The student likely reversed the sign (positive and negative value) of m when substituting into the slope-intercept form of the line for this scenario, resulting in $t = 15w - 275$. The student needs to focus on paying attention to detail when identifying the value for the rate of change and initial value and using these values to write the function representing the situation.</p>
	Option H is incorrect	<p>The student likely reversed the values of m and b when substituting into the slope-intercept form of the line for this scenario, resulting in $t = 275w - 15$. The student needs to focus on paying attention to detail when identifying the value for the rate of change and initial value and using these values to write the function representing the situation.</p>
	Option J is incorrect	<p>The student likely reversed the values of m and b when substituting into the slope-intercept form of the line for this scenario and reversed the signs of 275 and -15, resulting in $t = -275w + 15$. The student needs to focus on paying attention to detail when identifying the value for the rate of change and initial value and using these values to write the function representing the situation.</p>

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
11	Option D is correct	To determine the best prediction of the height in centimeters of a student with a weight of 64 kilograms using a scatterplot (a graph of plotted points that shows the relationship between two sets of data), the student could have drawn a line that closely follows the pattern formed by the points on the graph by keeping about half of the points above the line and the other half below the line. A good line for this scatterplot would pass slightly above the point at (135, 29) but very close to the point at (135.5, 33) and below the point at (152, 62), passing above the point at (155, 59), very close to (155, 61). The student could have then identified where the grid line marked 64 (representing a weight of 64 kilograms) intersects (crosses over) the line the student drew and determined that the height in centimeters corresponding to that point is about 156 centimeters. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.
	Option A is incorrect	The student likely chose the approximate height of the closest data point to 64 kilograms [(152, 62)], resulting in 152. The student needs to focus on drawing a line as close as possible to all points with a similar number of points above and below the line.
	Option B is incorrect	The student likely chose the points at (135, 29) and (138, 33) to draw the line to make the prediction. However, this line has 17 points above and 0 points below. The student needs to focus on drawing a line as close as possible to all points with a similar number of points above and below the line.
	Option C is incorrect	The student likely chose the greatest (tallest) height based on the increments of 4 shown on the horizontal axis, resulting in 162. The student needs to focus on drawing a line as close as possible to all points with a similar number of points above and below the line.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
12	Option H is correct	To determine the transformation applied to a figure on a coordinate grid that does NOT preserve congruence (same size and shape), the student should have recognized that a dilation will enlarge or reduce the size of the figure by a scale factor (relationship between the length of a side of one figure to the length of the corresponding (paired) side of a similar figure). The dilated figure will be similar (two figures with corresponding angles equal and corresponding sides proportional) to the original figure but NOT congruent.
	Option F is incorrect	The student likely recalled that a rotation (circular movement) of 270° counterclockwise may result in negative numbers being used as coordinates for the figure. The student may not have recognized that the congruence of the figure is preserved with a rotation. The student needs to focus on differentiating the characteristics of a rotation from the characteristics of a dilation.
	Option G is incorrect	The student likely recalled that a reflection (flip) across the y -axis (vertical) may result in negative numbers being used as coordinates for the figure. The student may not have recognized that the congruence of the figure is preserved with a reflection. The student needs to focus on differentiating the characteristics of a reflection from the characteristics of a dilation.
	Option J is incorrect	The student likely recalled that a translation (slide) 50 units down may result in negative numbers being used as coordinates for the figure. The student may not have recognized that the congruence of the figure is preserved with a translation. The student needs to focus on differentiating the characteristics of a translation from the characteristics of a dilation.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
13	Option A is correct	To determine which table shows the relationship between x , the number of sets of markers bought by the teacher, and y , the total cost of the markers, the student should have recognized that because the teacher had a \$2-off coupon to use toward the total cost of the markers bought, the y -intercept (value where the line crosses the y -axis (vertical)) and the initial (beginning) value of y is negative \$2. The student also should have recognized that because the teacher bought the markers at a cost of \$3 per set, the rate of change (constant increase or decrease) is 3. The student should have recognized that each corresponding (paired) x - and y -value in the table should fit the equation $y = 3x - 2$. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.
	Option B is incorrect	The student likely determined that the corresponding x - and y -values in the table fit the equation $y = \frac{1}{3}x - 2$. The student needs to focus on understanding and interpreting the initial value and the rate of change from a verbal situation to identify the table with the same relationship.
	Option C is incorrect	The student likely determined that the corresponding x - and y -values in the table fit the equation $y = 3x + 2$. The student needs to focus on understanding and interpreting the initial value and the rate of change from a verbal situation to identify the table with the same relationship.
	Option D is incorrect	The student likely determined that the corresponding x - and y -values in the table fit the equation $y = \frac{1}{3}x + 2$. The student needs to focus on understanding and interpreting the initial value and the rate of change from a verbal situation to identify the table with the same relationship.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
14	Option H is correct	To determine the volume (amount of three-dimensional space taken up) of the cylinder, the student should have used the formula $V = \pi r^2 h$, in which r represents the radius (distance from the center to the circumference of a circle) and h represents the height (vertical distance from top to bottom) of the cylinder. The student should have calculated the length of the radius by dividing the length of the diameter (straight line going through the center of a circle connecting two points on the circumference) by 2 ($2.5 \div 2 = 1.25$). Substituting $r = 1.25$ and $h = 7.5$ into the formula results in $V = \pi(1.25)^2(7.5)$.
	Option F is incorrect	The student likely used the length of the diameter in place of the length of the radius in the formula. The student needs to focus on understanding the formula for determining the volume of a cylinder.
	Option G is incorrect	The student likely used the length of the diameter in place of the length of the radius and reversed the placement of the values in the formula. The student needs to focus on understanding the formula for determining the volume of a cylinder.
	Option J is incorrect	The student likely divided the length of the height by 2 instead of the length of the diameter and reversed the placement of the values in the formula. The student needs to focus on understanding the formula for determining the volume of a cylinder.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
15	Option A is correct	<p>To determine the proportion that can be used to show that the slope (steepness of a straight line when graphed on a coordinate grid; $m = \frac{y_2 - y_1}{x_2 - x_1}$) of \overline{KM} is equal to the slope of \overline{PS}, the student should have determined that two of the sides of each triangle can be used to show the slope using the formula for slope. For \overline{KM}, the two sides of triangle KLM can be used to show the slope, where $y_2 - y_1$ can be represented by the difference in the vertical values, which is the same value as the length of side KL, and $x_2 - x_1$ can be represented by the difference in the horizontal values, which is the same value as the length of side LM. Plugging into the formula, the slope of \overline{KM} can be represented by $m = \frac{KL}{LM}$. For \overline{PS}, the two sides of triangle PRS can be used to show the slope where $y_2 - y_1$ can be represented by the difference in the vertical values, which is the same value as the length of side PR, and $x_2 - x_1$ can be represented by the difference in the horizontal values, which is the same value as the length of side RS. Plugging into the formula, the slope of \overline{PS} can be represented by $m = \frac{PR}{RS}$.</p> <p>Therefore the proportion $\frac{KL}{LM} = \frac{PR}{RS}$ shows the slopes of \overline{KM} and \overline{PS} are equal.</p>
	Option B is incorrect	<p>The student likely used the horizontal side of each triangle over the longest side of each triangle, resulting in $\frac{RS}{SP} = \frac{LM}{MK}$. The student needs to focus on correctly using the formula for the slope of a line and the correct sides of the triangle to show the slopes are equal.</p>
	Option C is incorrect	<p>The student likely reversed the formula for \overline{KM}, using $m = \frac{x_2 - x_1}{y_2 - y_1}$ instead of $m = \frac{y_2 - y_1}{x_2 - x_1}$, and for \overline{PS} the student likely used the longest side of the triangle over the vertical side of the triangle, resulting in $\frac{ML}{LK} = \frac{SP}{RP}$. The student needs to focus on correctly using the formula for the slope of a line and the correct sides of the triangle to show the slopes are equal.</p>

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
	Option D is incorrect	<p>The student likely used the longest side of each triangle over the vertical side of each triangle, resulting in $\frac{PS}{PR} = \frac{KM}{KL}$. The student needs to focus on correctly using the formula for the slope of a line and the correct sides of the triangle to show the slopes are equal.</p>

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
16	Option G is correct	<p>To determine the TV screen that has the smallest diagonal length in feet, the student should have ordered the diagonal lengths of the TV screens in the table from the shortest length to the longest length (smallest diagonal size to largest diagonal size) and could have then converted each number to a fraction with the same denominator (bottom number) (12, since the denominator of $\sqrt{144}$ is equal to 12). The diagonal length of Screen W ($\sqrt{12.25}$) results in the decimal 3.5, which converts to the fraction $\frac{42}{12}$. The diagonal length of Screen X ($2\frac{1}{6}$) results in the fraction $\frac{13}{6}$, which converts to the fraction $\frac{26}{12}$. The diagonal length of Screen Y ($\frac{37}{\sqrt{144}}$) converts to the fraction $\frac{37}{12}$. The diagonal length of Screen Z ($\frac{8}{3}$) converts to the fraction $\frac{32}{12}$. This results in fractions of $\frac{42}{12}$, $\frac{26}{12}$, $\frac{37}{12}$, and $\frac{32}{12}$. The student could then have ordered the diagonal lengths by comparing the fractions. The correct order of the fractions is $\frac{26}{12}$, $\frac{32}{12}$, $\frac{37}{12}$, and $\frac{42}{12}$, which means the shortest diagonal length is $\frac{26}{12}$, which is the diagonal length for Screen X. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.</p>
	Option F is incorrect	<p>The student likely chose the largest (longest) diagonal length instead of the smallest diagonal length. The student needs to focus on attending to the details of the question in problems that involve ordering different representations of real numbers correctly.</p>
	Option H is incorrect	<p>The student likely did not take the square root of 144 in the denominator for the diagonal length of Screen Y and therefore compared the fraction $\frac{37}{144}$ against the other fractions, which would be the smallest diagonal length. The student needs to focus on attending to the details of the question in problems that involve ordering different representations of real numbers correctly.</p>
	Option J is incorrect	<p>The student likely compared Screen Z as the fraction $\frac{3}{8}$ instead of $\frac{8}{3}$ against the other fractions, which would be the smallest diagonal length. The student needs to focus on attending to the details of the question in problems that involve ordering different representations of real numbers correctly.</p>

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
17	Option D is correct	To determine which scatterplot (a graph of plotted points that shows the relationship between two sets of data) supports the teacher's observation (as the number of hours students studied their multiplication facts increased, the number of errors the students made on their multiplication tests decreased), the student should have chosen the graph that shows the following association: as the study time (independent variable, x) increases, the number of errors (dependent variable, y) decreases. In this scenario the points on the correct graph represent a negative slope (the steepness of a straight line when graphed on a coordinate grid; $m = \frac{y_2 - y_1}{x_2 - x_1}$).
	Option A is incorrect	The student likely reversed the association based on the observation, resulting in a graph with a positive slope. The student needs to focus on choosing a scatterplot based on a description of the association.
	Option B is incorrect	The student chose a graph that shows a negative slope from the middle to the right side of the graph. The student needs to focus on choosing a scatterplot based on a description of the association.
	Option C is incorrect	The student likely focused on the words "increased" and "decreased" thinking the data points would be scattered randomly about the graph and therefore chose a graph that shows no association between the study time and number of errors. The student needs to focus on choosing a scatterplot based on a description of the association.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
18	Option H is correct	<p>To determine the radius (distance from the center to the edge of a circle) of the cone, the student should have used the formula for the volume (amount of three-dimensional space taken up) of a cone, $V = \frac{1}{3}Bh$, where B represents the area (amount of space covered by the surface) of the base of the cone (circle), which is also the formula for the area of a circle, $A = \pi r^2$. Combining the formulas results in the formula $V = \frac{1}{3}\pi r^2 h$. Substituting the values into the formula results in</p> $(1.5\pi) = \frac{1}{3}\pi r^2(4.5).$ <p>Solving the equation for r, $r^2 = (1.5\pi) \div \left(\frac{1}{3}\pi(4.5)\right) \rightarrow$</p> $r = \sqrt{(1.5\pi) \div \left(\frac{1}{3}\pi(4.5)\right)} = \sqrt{(1.5\pi) \div (1.5\pi)} = \sqrt{1}, \text{ results in } 1.0.$
	Option F is incorrect	<p>The student likely did not include $\frac{1}{3}$ in the formula and solved $(1.5\pi) = \pi r^2(4.5)$ for r, resulting in approximately 0.6. The student needs to focus on paying attention to detail to write the correct formula for the task.</p>
	Option G is incorrect	<p>The student likely used the correct formula but used half of the height in the calculation (2.25 instead of 4.5) and solved $(1.5\pi) = \frac{1}{3}\pi^2(2.25)$ for r, resulting in approximately 1.4. The student needs to focus on paying attention to detail to use the correct values in the formula for the task.</p>
	Option J is incorrect	<p>The student likely used $\frac{4}{3}$ instead of $\frac{1}{3}$ in the formula and solved $(1.5\pi) = \frac{4}{3}\pi r^2(4.5)$ for r, resulting in 0.5. The student needs to focus on paying attention to detail to write the correct formula for the task.</p>

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
19	Option B is correct	The student should have determined that in order for a set of ordered pairs to represent a function (relationship in which each input (value put into an equation, x) has a single output (value that comes out of the equation, y)), each value of x can only be paired with one value of y . The set of ordered pairs contains only one y -value for each x -value.
	Option A is incorrect	The student likely did not realize that the last two ordered pairs in the set have the same x -value (input value, -5.5) paired with different y -values (output values, 5 and -6). The student needs to focus on the definition of a function and on applying it to determine whether a set of ordered pairs represents a function.
	Option C is incorrect	The student likely confused which variable (symbol used to represent an unknown number) was the input for the function and which variable was the output for the function. The set has one x -value (input value, 9.3) paired with two different y -values (output values, -1 and 1) and another x -value (7.3) paired with two different y -values (-2 and 2). The student needs to focus on the definition of a function and on applying it to determine whether a set of ordered pairs represents a function.
	Option D is incorrect	The student likely did not realize that the second and last ordered pairs in the set have the same x -value (input value, 9.1) paired with different y -values (output values, 10 and 8). The student needs to focus on the definition of a function and on applying it to determine whether a set of ordered pairs represents a function.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
20	Option J is correct	To determine the rule that best represents the dilation, the student should have determined that when a figure is dilated (enlarged or reduced in size), its measurements increase or decrease based on the scale factor (ratio of the length of a side of one figure to the length of the corresponding (paired) side of a similar figure). A scale factor with the origin (point where the x-axis (horizontal) and y-axis (vertical) on a coordinate grid intersect (cross)); also, the point represented by the ordered pair (0, 0) as the center of dilation means that each point on the dilated figure will be a certain number of times as far from the origin as it was on the original figure. Since the location of vertex Q was originally represented at (6, 2), and the location of the corresponding vertex (vertex Q') on the dilated figure is at (21, 7), the scale factor of the dilation can be determined by dividing the value of each corresponding coordinate of vertex Q' by the value of each corresponding coordinate of vertex Q $\left(21 \div 6 = \frac{7}{2} \text{ and } 7 \div 2 = \frac{7}{2}\right)$, so the rule $(x, y) \rightarrow \left(\frac{7}{2}x, \frac{7}{2}y\right)$ represents the dilation.
	Option F is incorrect	The student likely divided the corresponding values of the original vertex (vertex Q) by the corresponding values of the dilated vertex (vertex Q') $\left(6 \div 21 = \frac{2}{7} \text{ and } 2 \div 7 = \frac{2}{7}\right)$ and therefore chose the rule $(x, y) \rightarrow \left(\frac{2}{7}x, \frac{2}{7}y\right)$. The student needs to focus on the effect a dilation by a given scale factor has on a figure and how to determine the rule to explain the effect.
	Option G is incorrect	The student likely thought of a translation (slide) and added different values to the coordinates of the original vertex (vertex Q) to get to vertex Q', instead of multiplying each coordinate by a single scale factor, choosing the rule $(x, y) \rightarrow (x + 15, y + 5)$. The student needs to focus on understanding how the scale factor affects the dilation.
	Option H is incorrect	The student likely thought of a translation (slide) and subtracted different values from the coordinates of vertex Q' to get to the original vertex (vertex Q), instead of multiplying each coordinate by a single scale factor, choosing the rule $(x, y) \rightarrow (x - 15, y - 5)$. The student needs to focus on understanding how the scale factor affects the dilation.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
21	Option C is correct	<p>To determine which function (equation) is represented by the graph (line) passing through the points $(-1, -\frac{1}{4})$ and $(1, -\frac{3}{4})$, the student should have determined the values of m and b in the slope-intercept form of the line, $y = mx + b$. The m represents the slope (steepness of a straight line when graphed on a coordinate grid; $m = \frac{y_2 - y_1}{x_2 - x_1}$) and the b represents the y-intercept (value where a line crosses the y-axis (vertical)) of the line. The student should have determined the slope using the given points; $m = \frac{-\frac{3}{4} - (-\frac{1}{4})}{1 - (-1)} = \frac{-\frac{1}{2}}{2} = -\frac{1}{2} \cdot \frac{1}{2} = -\frac{1}{4}$. The student could have then substituted the value of the slope and the point $(1, -\frac{3}{4})$ into the slope-intercept form equation, $(-\frac{3}{4}) = (-\frac{1}{4})(1) + b$, to solve for b; $b = (-\frac{3}{4}) + (\frac{1}{4}) = -\frac{1}{2}$. Substituting m with $-\frac{1}{4}$ and b with $-\frac{1}{2}$, the function that represents the line is $y = -\frac{1}{4}x - \frac{1}{2}$. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.</p>
	Option A is incorrect	<p>The student likely reversed the placement of the slope and the y-intercept in the slope-intercept form of the equation, resulting in $y = -\frac{1}{2}x - \frac{1}{4}$. The student needs to focus on attending to detail when substituting values into the formula to find the slope and when identifying the y-intercept in order to write the function that passes through two points.</p>
	Option B is incorrect	<p>The student likely reversed the placement of the slope and the y-intercept in the slope-intercept form of the equation and reversed the sign (positive and negative value) of each, resulting in $y = \frac{1}{2}x + \frac{1}{4}$. The student needs to focus on attending to detail when substituting values into the formula to find the slope and when identifying the y-intercept in order to write the function that passes through two points.</p>

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
	Option D is incorrect	<p>The student likely miscalculated the slope and the y-intercept by reversing the sign (positive and negative value) of each, resulting in $y = \frac{1}{4}x + \frac{1}{2}$. The student needs to focus on attending to detail when substituting values into the formula to find the slope and when identifying the y-intercept in order to write the function that passes through two points.</p>

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
22	Option F is correct	<p>Scientific notation is used to express very large and very small numbers. Instead of writing 0.00000001, this value can be expressed as a multiple of 10: $\frac{1}{100,000,000} = \frac{1}{10^8} = 10^{-8}$. The shorthand method of translating from standard form to scientific notation is to move the decimal point left (when the number is greater than 1) or right (when the number is less than 1) until there is only 1 non-zero number before the decimal point. Any extra zeros prior to that number are not included within the scientific notation. The number of decimal places the point moves determines the value of the exponent (number raised to a power). The direction the decimal point is moved determines whether the exponent is positive or negative. Moving the decimal point to the right creates a negative exponent. Moving the decimal point to the left creates a positive exponent. Since the decimal point moves to the left 6 places, the exponent is 6, resulting in 4.951×10^6.</p>
	Option G is incorrect	<p>The student likely only counted the number of places the decimal point moved and did not consider which direction the decimal point moved. The student needs to focus on understanding how to determine the exponent based on the place value when converting standard form to scientific notation.</p>
	Option H is incorrect	<p>The student likely counted the number of zeros before the decimal point (not shown in the original number) as the exponent. The student needs to focus on understanding how to determine the exponent based on the place value when converting standard form to scientific notation.</p>
	Option J is incorrect	<p>The student likely counted the number of zeros before the decimal point (not shown in the original number) as the exponent and did not consider which direction the decimal point moved. The student needs to focus on understanding how to determine the exponent based on the place value when converting standard form to scientific notation.</p>

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
23	736 and any equivalent values are correct	<p>To determine the total surface area (total area of the surfaces of a three-dimensional figure) of the prism, the student could have used the formula $S = Ph + 2B$, where P represents the perimeter of the base, h represents the height of the prism, and B represents the area of the base. To determine the perimeter of the rectangular base, the student should have added the four sides of the rectangle, $P = 16 + 16 + 8 + 8 = 48$. To determine the area of the rectangular base, the student should have multiplied 16 by 8, resulting in 128. The student should have identified h as 10 from the diagram and evaluated $S = (48)(10) + 2(128)$, which is equal to 736. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.</p>

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
24	Option H is correct	<p>To determine which graph has a slope (steepness of a straight line when graphed on a coordinate grid; $m = \frac{y_2 - y_1}{x_2 - x_1}$) that best represents the number of customers that were served per hour at the restaurant, the student should have identified that 600 customers served during a 10-hour period of time is the same as 60 customers served in 1 hour. The student could have identified that there were 0 customers served in 0 hours. Then the student could have determined that the graph appears to pass through the points located at (0, 0) and (1, 60) and the slope between these points is represented by the equation $m = \frac{60 - 0}{1 - 0} = \frac{60}{1}$, which is equal to 60. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.</p>
	Option F is incorrect	<p>The student likely calculated the slope as 600 and chose the graph in which the y-value is always equal to 600. The student needs to focus on understanding the meaning of the value of a slope and identifying the graph that correctly represents the slope.</p>
	Option G is incorrect	<p>The student likely calculated the slope correctly as 60 but chose the graph in which the y-value is always equal to 60. The student needs to focus on understanding the meaning of the value of a slope and identifying the graph that correctly represents the slope.</p>
	Option J is incorrect	<p>The student likely thought the line must pass through (0, 0) and through the grid line marked 600 (representing 600 customers) without regard to the corresponding (paired) x-value of the intersecting (crossing over) grid line. The student needs to focus on understanding the meaning of the value of a slope and identifying the graph that correctly represents the slope.</p>

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
25	Option B is correct	To determine the difference between the two savings accounts with different types of interest, the student should have calculated the amount of interest in each account and then subtracted the two amounts. To determine the amount of interest in Account I, the student should have used the formula for simple interest, $I = Prt$, in which P represents the principal (initial loan amount), r represents the interest rate (in decimal form), and t represents the length of time in years, $I = (\$1,750)(0.0275)(2) = \96.25 . To determine the balance in Account II, the student should have used the formula for compound interest, $A = P(1 + r)^t$, in which A represents the balance amount (principal and interest combined), $A = (\$1,750)(1 + 0.0275)^2 = \$1,847.57$. The student should have then subtracted the principal from the balance amount, $\$1,847.57 - \$1,750 = \$97.57$. Finally the student should have subtracted $(\$97.57 - \$96.25)$ and determined that the difference between the interest of the two accounts at the end of 2 years was \$1.32.
	Option A is incorrect	The student likely determined only the amount of the simple interest, resulting in \$96.25. The student needs to focus on attending to the details of the question in problems.
	Option C is incorrect	The student likely determined only the amount of the compound interest, resulting in \$97.57. The student needs to focus on attending to the details of the question in problems.
	Option D is incorrect	The student likely added the amount of interest from each account $(\$97.57 + \$96.25)$, resulting in \$193.82. The student needs to focus on attending to the details of the question in problems.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
26	Option F is correct	To determine the y -intercept (value where a line crosses the y -axis) of the graph of the function, the student could have identified the point on the graph where the line appears to pass through the y -axis (vertical), which is at 5. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.
	Option G is incorrect	The student likely confused the y -intercept by finding the approximate point on the graph where the line would pass through the x -axis (horizontal). The student needs to focus on paying attention to details when identifying the y -intercept of a linear function.
	Option H is incorrect	The student likely confused the y -intercept with the slope and used the formula $m = \frac{y_2 - y_1}{x_2 - x_1}$ when determining the slope, resulting in $m = \frac{(-2) - 5}{8 - 0} = -\frac{7}{8}$. The student needs to focus on paying attention to details when identifying the y -intercept of a linear function.
	Option J is incorrect	The student likely confused the y -intercept with the slope and used the incorrect formula, $m = \frac{x_2 - x_1}{y_2 - y_1}$, when determining the slope, resulting in $m = \frac{8 - 0}{(-2) - 5} = -\frac{8}{7}$. The student needs to focus on paying attention to details when using the formula to find the slope of a linear function and when identifying the y -intercept of a linear function.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
27	Option D is correct	To determine which statement about x is true, the student should have determined that the intersection (crossing) of transversal (line) t with the two parallel lines (g and k) produced pairs of angles that are congruent (same measure) and pairs of angles that are supplementary (have a sum of 180°). The student should have determined that the angles labeled x° and 136° are congruent.
	Option A is incorrect	The student most likely determined that the intersection of transversal t with the two parallel lines produced pairs of angles that are congruent and pairs of angles that are supplementary. The student then determined that the angle labeled $x^\circ = 180$, or 180° . The student needs to focus on the relationship between angles when parallel lines are intersected by a transversal.
	Option B is incorrect	The student most likely determined that the intersection of transversal t with the two parallel lines produced pairs of angles that are congruent and pairs of angles that are complimentary (have a sum of 90°) instead of supplementary. The student then determined that the angle labeled $x^\circ = 90$, or 90° . The student needs to focus on the relationship between angles when parallel lines are intersected by a transversal.
	Option C is incorrect	The student most likely determined that the intersection of transversal t with the two parallel lines produced pairs of angles that are congruent and pairs of angles that are supplementary. The student then determined that the angles labeled x° and 136° are supplementary and determined that $x^\circ = 180 - 136$, or 44° . The student needs to focus on the relationship between angles when parallel lines are intersected by a transversal.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
28	Option H is correct	To determine the value of x , the student could have written and solved an equation such as $2x + (4x - 2) + 2(x + 7) = 4(2.5x)$, where x is a fixed length in yards. The student could have distributed the values in front of the parentheses to the values inside the parentheses and combined x terms, resulting in the equation $8x + 12 = 10x$. The student then could have solved for x by subtracting $8x$ from both sides of the equation, resulting in $12 = 2x$. Finally the student could have solved for x by dividing both sides of the equation by 2, resulting in $x = 6$. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.
	Option F is incorrect	The student likely set up the equation incorrectly as $2x + (4x - 2) + 2(x + 7) = 2(2.5x)$. The student then likely rewrote the equation as $8x + 12 = 5x$. The student then likely solved for x by subtracting $8x$ from both sides of the equation, resulting in $-3x = 12$. To solve for x , the student likely divided both sides of the equation by -3 , resulting in $x = -4$. The student needs to focus on writing the correct equation for a word problem.
	Option G is incorrect	The student likely set up the correct equation and rewrote the equation as $8x + 12 = 10x$ but added $8x$ to both sides of the equation instead of subtracting, resulting in $12 = 18x$. To solve for x , the student likely divided both sides of the equation by 18, resulting in $x = \frac{2}{3}$. The student needs to focus on using the proper steps to solve an equation.
	Option J is incorrect	The student likely did not distribute 2 correctly to both x and 7 in the term $2(x + 7)$ and set up the equation incorrectly as $2x + (4x - 2) + (2x + 7) = 4(2.5x)$. The student then likely rewrote the equation as $8x + 5 = 10x$. The student then likely solved for x by subtracting $8x$ from both sides of the equation, resulting in $2x = 5$. To solve for x , the student likely divided both sides of the equation by 2, resulting in $x = \frac{5}{2}$. The student needs to focus on writing the correct equation for a word problem.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
29	Option B is correct	To determine why the balance in the account has grown, the student should have used the table to determine that money is being deposited into the account each year (\$500.00) and interest is being earned on the account balance each year (\$32.00, \$66.05, and \$102.28). This means that the balance in the account is growing due to the deposits made each year and the interest earned being added each year.
	Option A is incorrect	The student likely understood that deposits being made to the account increase the balance in the account but did not realize that the balance is also increasing by the amount of interest earned. The student needs to focus on understanding the vocabulary used for showing how an account balance may grow over time.
	Option C is incorrect	The student likely understood that interest earned increases the balance in the account but did not realize that the balance is also increasing by the amount being deposited. The student needs to focus on understanding the vocabulary used for showing how an account balance may grow over time.
	Option D is incorrect	The student likely misunderstood the meaning of the terms “amount deposited,” “interest earned,” or “ending balance.” The student needs to focus on understanding the vocabulary used for showing how an account balance may grow over time.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
30	Option J is correct	To identify the phrase that describes the transformation (change of a shape using a rotation (circular movement), reflection (flip), translation (slide), or dilation (resize)), the student should have determined that the transformation used was a rotation 180° clockwise about the origin (point where the x -axis (horizontal) and the y -axis (vertical) on a coordinate grid intersect (cross); also, the point represented by the ordered pair $(0, 0)$) because of the rule $(x, y) \rightarrow (-x, -y)$. The student made this determination based on how the x -value in the ordered pair changed to the opposite sign and the y -value in the ordered pair changed to the opposite sign. Therefore the phrase "A 180° clockwise rotation about the origin" describes the transformation.
	Option F is incorrect	The student likely identified the transformation as a reflection of (x, y) across the x -axis but did not realize that the sign of the x -value would have remained the same instead of changing to the opposite sign. The student needs to focus on correctly identifying the type of transformation that was used and using the rule to explain the effect on (x, y) when graphed on a coordinate grid.
	Option G is incorrect	The student likely identified the transformation as a reflection of (x, y) across the y -axis but did not realize that the sign of the y -value would have remained the same instead of changing to the opposite sign. The student needs to focus on correctly identifying the type of transformation that was used and using the rule to explain the effect on (x, y) when graphed on a coordinate grid.
	Option H is incorrect	The student likely identified the transformation as a rotation of (x, y) but did not realize that (x, y) would have used the rule $(x, y) \rightarrow (y, -x)$ instead of $(x, y) \rightarrow (-x, -y)$ for a 90° clockwise rotation about the origin. The student needs to focus on correctly identifying the type of transformation that was used and using the rule to explain the effect on (x, y) when graphed on a coordinate grid.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
31	Option A is correct	To determine which graph shows the relationship between y , the number of customers who preferred the new spaghetti sauce, and x , the total number of customers, the student could have determined that for every 10 customers, 7 prefer the new sauce, so the unit rate is $\frac{7}{10}$, graphing the ordered pairs $(0, 0)$ and $(10, 7)$. The student should have then identified the graph that shows a line that passes through those points (a survey of 0 customers shows 0 customers prefer the new sauce, and a survey of 10 customers shows 7 customers prefer the new sauce). The line in this graph appears to pass through these points.
	Option B is incorrect	The student likely inverted (flipped) the unit rate using $\frac{10}{7}$ instead of $\frac{7}{10}$, graphing the ordered pairs $(0, 0)$ and $(7, 10)$. The student needs to focus on determining the unit rate and how that translates to the graph.
	Option C is incorrect	The student likely used 7 customers who preferred the sauce as the y -intercept (value where the line intersects the y -axis (vertical)) along with the correct unit rate, graphing the ordered pairs $(0, 7)$ and $(10, 14)$. The student needs to focus on determining the y -intercept of the graph.
	Option D is incorrect	The student likely used 7 customers who preferred the sauce as the x -intercept (value where the line intersects the x -axis (horizontal)) along with the inverted (flipped) unit rate of $\frac{10}{7}$ instead of $\frac{7}{10}$, graphing the ordered pairs $(7, 0)$ and $(14, 10)$. The student needs to focus on determining the unit rate and the y -intercept of the graph.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
32	Option G is correct	To determine which proportion (comparison of two ratios) is true for similar figures (two figures with corresponding angles that are equal and corresponding sides that are proportional), the student should have determined that the angles in triangle ABC and triangle DEF are corresponding (paired) and are equal, which means that the sides of the figures forming those equal angles are also corresponding and their lengths are proportional. The student then should have determined that the ratio (comparison of two or more values) $\frac{4}{6}$ represents the ratio of the length in inches of the left side in triangle DEF to the length in inches of the left side in triangle ABC . The ratio $\frac{x}{7}$ represents the ratio of the length in inches of the bottom side in triangle DEF to the length in inches of the bottom side in triangle ABC .
	Option F is incorrect	The student likely reversed the proportions on the right side of the equation; $\frac{7}{x}$ equals $\frac{6}{4}$ instead of $\frac{4}{6}$. The student needs to focus on paying attention to detail when identifying the correspondence between the sides of similar figures.
	Option H is incorrect	The student likely reversed the proportions on the right side of the equation; $\frac{6}{4}$ equals $\frac{7}{x}$ instead of $\frac{x}{7}$. The student needs to focus on paying attention to detail when identifying the correspondence between the sides of similar figures.
	Option J is incorrect	The student likely reversed the proportions on the right side of the equation; $\frac{4}{x}$ equals $\frac{6}{7}$ instead of $\frac{7}{6}$. The student needs to focus on paying attention to detail when identifying the correspondence between the sides of similar figures.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
33	Option A is correct	To determine the order of the numbers from least (smallest) to greatest (largest), the student could have converted each value to the same form so a comparison could be made. The student could have converted $\sqrt{38}$ to approximately 6.16, 63% to 0.63, and $-\frac{19}{3}$ to approximately -6.33. Then the student should have ordered the decimal values (6.16, -6.35, 0.63, -6.33) from least to greatest, which means the correct order of the given values from least to greatest would be -6.35, $-\frac{19}{3}$, 63%, $\sqrt{38}$. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.
	Option B is incorrect	The student likely ignored the negative signs. The student needs to focus on attending to the details of the question in problems.
	Option C is incorrect	The student likely converted 63% to 6.3. The student needs to focus on converting percentages into decimals correctly in order to make comparisons.
	Option D is incorrect	The student likely reversed the order of the negative values thinking that -6.35 is greater than $-\frac{19}{3}$. The student needs to focus on comparing negative values correctly.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
34	0.5 and any equivalent values are correct	<p>To determine the slope (steepness of a straight line when graphed on a coordinate grid; $m = \frac{y_2 - y_1}{x_2 - x_1}$), the student could have calculated the slope of the line that passes through the points located at $(-6, -5)$ and $(6, 1)$ using $m = \frac{1 - (-5)}{6 - (-6)} = \frac{6}{12} = \frac{1}{2}$, which is equal to 0.5. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.</p>

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
35	Option B is correct	To determine which inequality represents the situation, the student could have used the information from the problem that the length of \overline{AB} ($9x - 16$ units) is greater than the length of \overline{AD} ($1.5x + 42$ units), resulting in $9x - 16 > 1.5x + 42$. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.
	Option A is incorrect	The student likely misinterpreted the inequality symbol. The student needs to focus on using the correct symbols to write inequalities.
	Option C is incorrect	The student likely misinterpreted the inequality symbol and created the inequality $9x - 16 < 1.5x + 42$ but moved $1.5x$ to the left side of the inequality and moved -16 to the right side of the inequality, resulting in $10.5x < 26$. The student needs to focus on using the correct symbols to write inequalities and needs to focus on accurately writing algebraic expressions that represent verbal descriptions.
	Option D is incorrect	The student likely created the inequality $9x - 16 > 1.5x + 42$ but moved $1.5x$ to the left side of the inequality and moved -16 to the right side of the inequality, resulting in $10.5x > 26$. The student needs to focus on accurately writing algebraic expressions that represent verbal descriptions.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
36	Option J is correct	To determine which measurement is closest to the length of \overline{XY} in units, the student should have determined that the line segment represents the hypotenuse (longest side) of a right triangle (a closed figure with three sides and one 90-degree angle). The lengths in units of the two legs of the right triangle can be represented by subtracting the x-coordinates (horizontal position from 0) of the two endpoints of the line segment (the part of a line connecting two endpoints) and by subtracting the y-coordinates (vertical position from 0) of the two endpoints of the line segment. This means that the lengths in units of the legs are $5 - (-5) = 10$ and $6 - 0 = 6$. Using the Pythagorean theorem (in a right triangle, the square of the hypotenuse (longest side) is equal to the sum (total) of the squares of the other two sides; $a^2 + b^2 = c^2$ or $c = \sqrt{a^2 + b^2}$), the length in units of line segment XY can be represented by the expression $\sqrt{10^2 + 6^2}$, or $\sqrt{136}$, which has a value of approximately 11.7 units. Therefore the approximate length of line segment XY is 11.7 units. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.
	Option F is incorrect	The student likely used the coordinates of point $X(5, 6)$ to identify the lengths of the sides of the right triangle as 5 and 6 (using only the values of those coordinates) and used the Pythagorean theorem, solving $\sqrt{5^2 + 6^2}$, or $\sqrt{61}$, resulting in a value of approximately 7.8 units. The student needs to focus on how to properly apply the Pythagorean theorem using the given information.
	Option G is incorrect	The student likely identified the lengths of the sides of the right triangle (10 and 6) but added them instead of using the Pythagorean theorem. The student needs to focus on recognizing when the Pythagorean theorem should be used and how to properly apply it with the given information.
	Option H is incorrect	The student likely counted the lengths of the sides of the right triangle incorrectly as 11 and 7 instead of 10 and 6 and used the Pythagorean theorem, solving $\sqrt{11^2 + 7^2}$, or $\sqrt{170}$, resulting in a value of approximately 13.0 units. The student needs to focus on how to properly apply the Pythagorean theorem using the given information.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
37	Option B is correct	To determine which statement is true, the student should have recognized that in a non-proportional relationship, the y -value is not equal to 0 when the corresponding (paired) x -value is 0. In this graph, when the x -value is equal to 0, the corresponding y -value would equal 7, resulting in the statement that the graph shows a non-proportional relationship because the graph does not contain the origin (point where the x -axis (horizontal) and the y -axis (vertical) on a coordinate grid intersect (cross); also, the point represented by the ordered pair (0, 0)).
	Option A is incorrect	The student likely identified the slope of the line as a negative slope (steepness of a straight line when graphed on a coordinate grid) and interpreted the negative slope as meaning the line showed a non-proportional relationship. The student needs to focus on the definition of a proportional relationship and on applying it to determine whether a graph represents a proportional relationship.
	Option C is incorrect	The student likely identified that the x -intercept (value where the line intersects the x -axis (horizontal)) and the y -intercept (value where the line crosses the y -axis (vertical)) of the line both contain 7 and interpreted these intercepts as meaning the line showed a proportional relationship. The student needs to focus on the definition of a proportional relationship and on applying it to determine whether a graph represents a proportional relationship.
	Option D is incorrect	The student likely identified that the line passes through three quadrants and interpreted the passing through three quadrants as meaning the line showed a proportional relationship, instead of recognizing that a proportional relationship can only be in two quadrants. The student needs to focus on the definition of a proportional relationship and on applying it to determine whether a graph represents a proportional relationship.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
38	61 and any equivalent values are correct	<p>To determine the length of the ramp in feet, the student should have determined that because the diagram represents a right triangle (a closed figure with three sides and one 90-degree angle) with legs of 60 feet and 11 feet, the Pythagorean theorem (in a right triangle, the square of the hypotenuse (longest side) is equal to the sum (total) of the squares of the other two sides, $a^2 + b^2 = c^2$ or $c = \sqrt{a^2 + b^2}$) can be used to calculate this distance. The distance in feet is equal to $\sqrt{60^2 + 11^2}$. When the two values under the radical symbol ($\sqrt{\quad}$) are squared, the result is $\sqrt{3,600 + 121}$, which equals $\sqrt{3,721}$. The value of $\sqrt{3,721}$ is 61, which means the distance of the ramp is 61 feet.</p>

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
39	Option D is correct	To determine which measurement is closest to x , the length of the diagonal of the square in centimeters, the student could have determined that $x^2 = 132$ can be solved for x by taking the square root of both sides of the equation ($\sqrt{x^2} = \sqrt{132}$ or $x = \sqrt{132}$), resulting in 11 centimeters being closest to the measurement of x . This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.
	Option A is incorrect	The student likely divided 132 by 2 instead of taking the square root, resulting in 66 centimeters. The student needs to focus on understanding how to find the square root of a number.
	Option B is incorrect	The student likely divided 132 by 3 instead of taking the square root, resulting in 44 centimeters. The student needs to focus on understanding how to find the square root of a number.
	Option C is incorrect	The student likely divided 132 by 4 instead of taking the square root, resulting in 33 centimeters. The student needs to focus on understanding how to find the square root of a number.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
40	Option F is correct	To determine which two cylinders have the same lateral surface area (total area of the surfaces of a three-dimensional figure, not including the area of the bases), the student could have used the formula for the lateral surface area of a cylinder, $S = 2\pi rh$, where r represents the radius (distance from the center to the circumference of a circle) of the circular base and h represents the height (vertical distance from top to bottom) of the cylinder. To determine the lateral surface area for Cylinder W, the student could have substituted the given values and an approximate value for π in the formula for lateral surface area and evaluated $S = (2)(3.14)(3)(9)$, which is approximately equal to 169.56 square inches. To determine the lateral surface area for Cylinder X, the student could have substituted the given values and an approximate value for π in the formula for lateral surface area and evaluated $S = (2)(3.14)(4)(2)$, which is approximately equal to 50.24 square inches. To determine the lateral surface area for Cylinder Y, the student could have substituted the given values and an approximate value for π in the formula for lateral surface area and evaluated $S = (2)(3.14)(4.5)(6)$, which is approximately equal to 169.56 square inches. The student then could have compared the values, resulting in Cylinder W and Cylinder Y having the same lateral surface area. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.
	Option G is incorrect	The student likely noticed that the sum (total) of each radius for Cylinders W and X is 7 ($3 + 4 = 7$) and the difference of each height for Cylinders W and X is 7 ($9 - 2 = 7$) and therefore assumed both cylinders had the same lateral surface area. The student needs to focus on understanding and properly applying the formula for determining the lateral surface area of cylinders.
	Option H is incorrect	The student likely noticed that the sum (total) of the radius and the height for Cylinder X is 6 ($4 + 2 = 6$) and the height for Cylinder Y is 6 and therefore assumed both cylinders had the same lateral surface area. The student needs to focus on understanding and properly applying the formula for determining the lateral surface area of cylinders.
	Option J is incorrect	The correct answer (Cylinders W and Y) was presented in one of the other answer options.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
41	Option C is correct	To determine the best prediction of the high temperature in degrees Fahrenheit on a day when the low temperature is 71° Fahrenheit using a scatterplot (a graph of plotted points that shows the relationship between two sets of data), the student could have drawn a line that closely follows the pattern formed by the points on the graph by keeping about half of the points above the line and the other half below the line. A good line for this scatterplot would pass above the point at (73, 90), slightly above the point at (74, 92), and slightly above the point at (79, 99), but passing below the point (79, 100). The student could have then identified where the grid line marked 71 (representing a low temperature of 71° Fahrenheit) intersects (crosses over) the line the student drew and determined that the high temperature in degrees Fahrenheit corresponding to that point is about 88° Fahrenheit. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.
	Option A is incorrect	The student likely chose the points at (76, 96) and (77, 97) to draw the line to make the prediction. However, this line has five points above and seven points below. The student needs to focus on drawing a line as close as possible to all points with a similar number of points above and below the line.
	Option B is incorrect	The student likely drew a line that closely follows the pattern formed by the points on the graph by keeping about half of the points above the line and the other half below the line but could have identified where the grid line marked 80 (representing a low temperature of 80° Fahrenheit) intersects the line the student drew and determined that the high temperature in degrees Fahrenheit corresponding to that point is about 101° Fahrenheit. The student needs to focus on attending to the details of the question in problems.
	Option D is incorrect	The student likely focused on the highest dot that is the furthest to the right located at (79, 100) and chose the high temperature at that point, resulting in 100° Fahrenheit. The student needs to focus on drawing a line as close as possible to all points with a similar number of points above and below the line.

2021 STAAR Grade 8 Mathematics Rationales

Item#	Rationale	
42	Option F is correct	<p>To identify the graph with a slope (steepness of a straight line when graphed on a coordinate grid; $m = \frac{y_2 - y_1}{x_2 - x_1}$) that best represents the cost of each pencil at the store, the student could have determined that the cost of 30 cents for 6 pencils is equivalent to a cost of 5 cents for each pencil ($30 \div 6 = 5$). Then the student could have determined that the graph appears to pass through the points located at (0, 0) and (6, 30) and the slope between these points is represented by the equation $m = \frac{30 - 0}{6 - 0} = \frac{30}{6} = \frac{5}{1}$, which is equal to 5. This is an efficient way to solve the problem; however, other methods could be used to solve the problem correctly.</p>
	Option G is incorrect	<p>The student likely misinterpreted 6 pencils as 1 pencil, resulting in a slope of 30. The student needs to focus on using the formula to find the value of the slope and identifying the graph that represents the slope.</p>
	Option H is incorrect	<p>The student likely calculated the slope correctly as 5 but chose the graph in which the x-value and the y-value are each equal to 5. The student needs to focus on understanding the meaning of the value of a slope and identifying the graph that correctly represents the slope.</p>
	Option J is incorrect	<p>The student likely calculated the slope as 6 and chose the graph in which the x-value is always equal to 6. The student needs to focus on understanding the meaning of the value of a slope and identifying the graph that correctly represents the slope.</p>