

Pennsylvania PSSA 2018 Grade 7 Math

Reference Materials

Page 2

Exam & Answer Key Materials

Pages 3 - 39

Grade 7 Formula Sheet

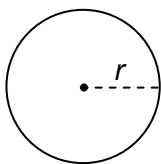
Formulas that you may need on this test are found below.
 You may refer back to this page at any time during the mathematics test.
 You may use calculator π or the number 3.14 as an approximation of π .

2018
 Grade 7

Simple Interest

$$I = Prt$$

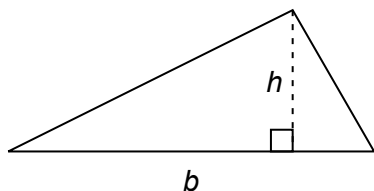
Circle



$$C = 2\pi r$$

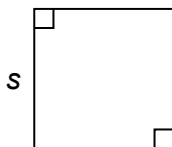
$$A = \pi r^2$$

Triangle



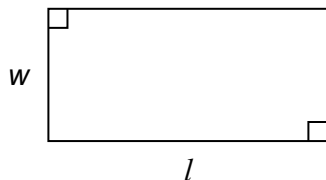
$$A = \frac{1}{2}bh$$

Square



$$A = s^2$$

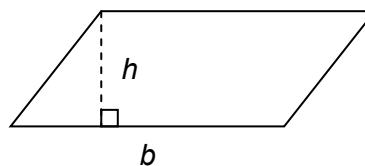
Rectangle



$$A = lw$$

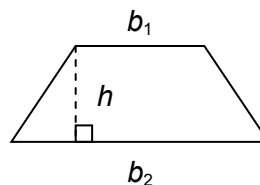
$$P = 2l + 2w$$

Parallelogram



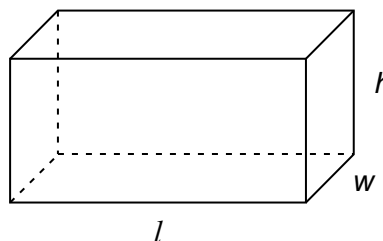
$$A = bh$$

Trapezoid



$$A = \frac{1}{2}h(b_1 + b_2)$$

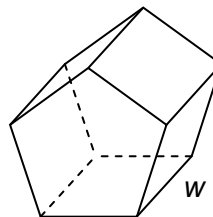
Rectangular Prism



$$V = lwh$$

$$SA = 2lw + 2lh + 2wh$$

Polygonal Prism



$$V = Bw, \text{ where } B = \text{area of the base}$$

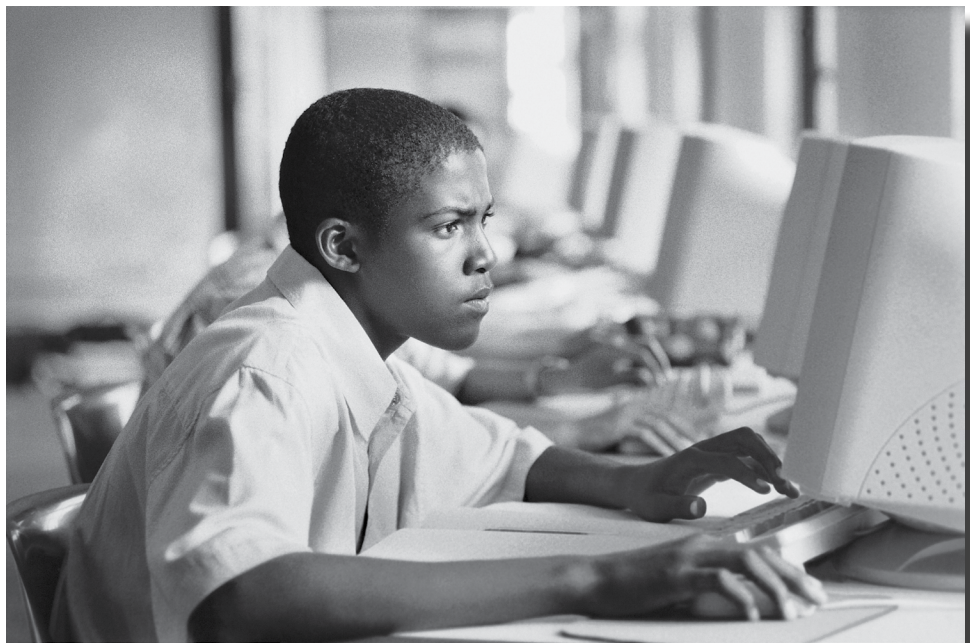
$$SA = Pw + 2B, \text{ where } P = \text{perimeter of base}$$



pennsylvania
DEPARTMENT OF EDUCATION

The Pennsylvania System of School Assessment

Mathematics Item and Scoring Sampler



2018–2019
Grade 7

Mathematics Test Directions

On the following pages are the mathematics questions.

- You may not use a calculator for question 1. You may use a calculator for all other questions on this test.

Directions for Multiple-Choice Questions:

Some questions will ask you to select an answer from among four choices.

For the multiple-choice questions:

- First solve the problem on scratch paper.
- Choose the correct answer and record your choice in the answer booklet.
- If none of the choices matches your answer, go back and check your work for possible errors.
- Only one of the answers provided is the correct response.

Directions for Open-Ended Questions:

Some questions will require you to write your response.

For the open-ended questions:

- These questions have more than one part. Be sure to read the directions carefully.
- You cannot receive the highest score for an open-ended question without completing all tasks in the question. For example, if the question asks you to show your work or explain your reasoning, be sure to show your work or explain your reasoning in the space provided.
- If the question does **not** ask you to show your work or explain your reasoning, you may use the space provided, but only those parts of your response that the question specifically asks for will be scored.
- Write your response in the appropriate location within the response box in the answer booklet. Some answers may require graphing, plotting, labeling, drawing, or shading. If you use scratch paper, be sure to transfer your final response and any needed work or reasoning to the answer booklet.

General Description of Scoring Guidelines for Mathematics Open-Ended Questions

- 4— The response demonstrates a *thorough* understanding of the mathematical concepts and procedures required by the task.**

The response provides correct answer(s) with clear and complete mathematical procedures shown and a correct explanation, as required by the task. Response may contain a minor “blemish” or omission in work or explanation that does not detract from demonstrating a *thorough* understanding.

- 3— The response demonstrates a *general* understanding of the mathematical concepts and procedures required by the task.**

The response and explanation (as required by the task) are mostly complete and correct. The response may have minor errors or omissions that do not detract from demonstrating a *general* understanding.

- 2— The response demonstrates a *partial* understanding of the mathematical concepts and procedures required by the task.**

The response is somewhat correct with *partial* understanding of the required mathematical concepts and/or procedures demonstrated and/or explained. The response may contain some work that is incomplete or unclear.

- 1— The response demonstrates a *minimal* understanding of the mathematical concepts and procedures required by the task.**

- 0— The response has no correct answer and *insufficient* evidence to demonstrate any understanding of the mathematical concepts and procedures required by the task for that grade level.**

Special Categories within zero reported separately:

- Blank**.....Blank, entirely erased, entirely crossed out, or consists entirely of whitespace
- Refusal**.....Refusal to respond to the task
- Off Task**.....Makes no reference to the item but is not an intentional refusal
- Foreign Language**.....Written entirely in a language other than English
- Illegible**Illegible or incoherent

Question 1 in this sampler is to be solved without the use of a calculator.

MULTIPLE-CHOICE ITEMS

1. Subtract: $\frac{8}{9} - \frac{-2}{3}$

A. $\frac{2}{9}$

B. $\frac{5}{6}$

C. $\frac{6}{6}$

D. $\frac{14}{9}$

| Item Information | |
|--------------------|---|
| Alignment | A-N.1.1.1 |
| Answer Key | D |
| Depth of Knowledge | 1 |
| p-value A | 26% |
| p-value B | 12% |
| p-value C | 28% |
| p-value D | 34% (correct answer) |
| Option Annotations | <p>A. solves $\frac{2}{3} = \frac{6}{9}$; $\frac{8}{9} - \frac{6}{9} = \frac{2}{9}$</p> <p>B. solves $\frac{(8 + 2)}{(9 + 3)} = \frac{10}{12} = \frac{5}{6}$</p> <p>C. solves $\frac{(8 - 2)}{(9 - 3)} = \frac{6}{6}$</p> <p>D. correct</p> |

A calculator is permitted for use in solving questions 2–17 in this sampler.

2. Three students request different lengths of string to use for science experiments.
- Jaime requests 3 pieces of string that are each 3.25 inches long and 1 piece that is $4\frac{1}{2}$ inches long.
 - Priya requests 6 pieces of string that are each $5\frac{1}{8}$ inches long.
 - Franco requests a piece of string that can be cut into 9 pieces that are each $\frac{1}{4}$ inch long.

The science teacher cuts the pieces of string for the three students' experiments from a spool containing 2 **yards** of string. How many **inches** of string remain on the spool?

- A. 9
- B. 20.7
- C. $24\frac{3}{4}$
- D. $47\frac{1}{4}$

| Item Information | |
|--------------------|---|
| Alignment | A-N.1.1 |
| Answer Key | C |
| Depth of Knowledge | 2 |
| p-value A | 16% |
| p-value B | 20% |
| p-value C | 49% (correct answer) |
| p-value D | 15% |
| Option Annotations | <p>A. converts $\frac{1}{4}$ to 4 in multiplication of Franco's length; finds the positive difference between 2 yards (72 inches) and total length used (81 inches)</p> <p>B. converts $5\frac{1}{8}$ to 5.8 for calculation</p> <p>C. correct</p> <p>D. finds total number of inches used, not remaining</p> |

3. What is the value of the expression $1\frac{1}{4} \cdot \left(-\frac{2}{3} \div -\frac{5}{8}\right)$?

A. $-3\frac{3}{4}$

B. $-1\frac{1}{15}$

C. $1\frac{11}{64}$

D. $1\frac{1}{3}$

| Item Information | |
|--------------------|---|
| Alignment | A-N.1.1.3 |
| Answer Key | D |
| Depth of Knowledge | 1 |
| p-value A | 7% |
| p-value B | 11% |
| p-value C | 9% |
| p-value D | 73% (correct answer) |
| Option Annotations | <p>A. attempts to distribute and uses $\frac{\left(\frac{5}{4}\right)}{\left(-\frac{2}{3}\right)} \times \frac{\left(\frac{5}{4}\right)}{\left(-\frac{5}{8}\right)}$; sign error</p> <p>B. attempts to distribute $\frac{5}{4}$ as $\left(\frac{5}{4} \times -\frac{2}{3}\right)$ divided by $\left(\frac{5}{4} \times -\frac{5}{8}\right)$; sign error</p> <p>C. inverts $-\frac{2}{3}$ instead of $-\frac{5}{8}$; uses $\left(\frac{5}{4}\right)\left(-\frac{3}{2} \times -\frac{5}{8}\right)$</p> <p>D. correct</p> |

4. One pound of pasta noodles can be made using the ingredients shown in the recipe below.

Recipe for Pasta NoodlesIngredients

$3\frac{1}{2}$ cups of flour

4 large eggs

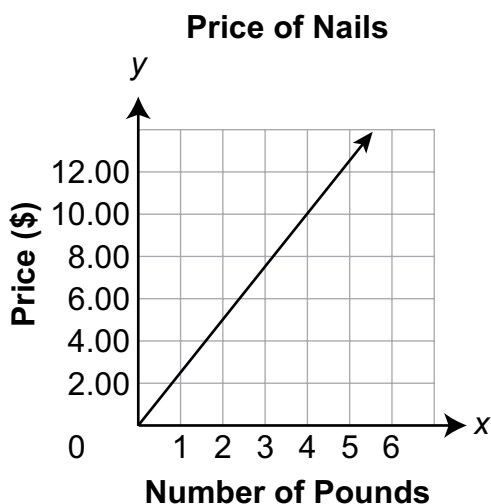
2 teaspoons of olive oil

A chef uses $166\frac{1}{4}$ cups of flour each week to make noodles. How many pounds of noodles does the chef make each week?

- A. $28\frac{1}{2}$
- B. $47\frac{1}{2}$
- C. $53\frac{1}{4}$
- D. $55\frac{1}{2}$

| Item Information | |
|--------------------|--|
| Alignment | A-R.1.1.1 |
| Answer Key | B |
| Depth of Knowledge | 2 |
| p-value A | 11% |
| p-value B | 70% (correct answer) |
| p-value C | 10% |
| p-value D | 9% |
| Option Annotations | <p>A. adds numbers in numerators and denominators and adds each sum to the corresponding whole number; (1 + 4) added to 166 and (1 + 2) added to 3; divides resulting numbers, $\frac{171}{6}$</p> <p>B. correct</p> <p>C. converts fractional parts of each value to decimals in a literal fashion; $\frac{166.14}{3.12}$</p> <p>D. divides the whole number and fractional parts separately</p> |

5. A hardware store sells nails by the pound. The graph below represents the price of nails at the store.

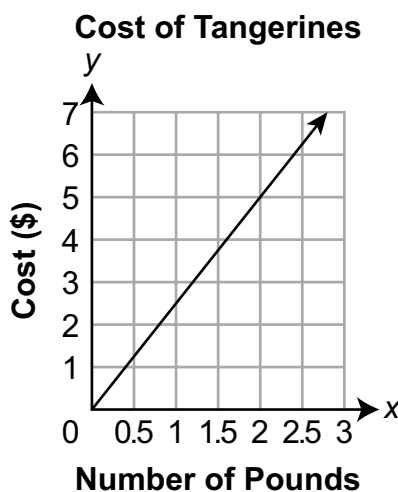


What is the unit price of nails at the hardware store?

- A. \$0.40 per pound
- B. \$2.50 per pound
- C. \$3.00 per pound
- D. \$5.00 per pound

| Item Information | |
|--------------------|--|
| Alignment | A-R.1.1.3 |
| Answer Key | B |
| Depth of Knowledge | 2 |
| p-value A | 11% |
| p-value B | 76% (correct answer) |
| p-value C | 7% |
| p-value D | 6% |
| Option Annotations | <p>A. divides pounds by cost; $\frac{2}{5}$</p> <p>B. correct</p> <p>C. subtracts 5 – 2 from point (2, 5)</p> <p>D. uses \$5.00 from point (2, 5)</p> |

6. The graph below shows the relationship between the number of pounds of tangerines purchased and the cost.



Based on the graph, which statement about the cost of tangerines is true?

- A. The cost of 1 pound of tangerines is \$2.
- B. The cost of 2 pounds of tangerines is \$1.
- C. The cost of 2 pounds of tangerines is \$5.
- D. The cost of 5 pounds of tangerines is \$2.

| Item Information | |
|--------------------|--|
| Alignment | A-R.1.1.5 |
| Answer Key | C |
| Depth of Knowledge | 2 |
| p-value A | 9% |
| p-value B | 8% |
| p-value C | 67% (correct answer) |
| p-value D | 16% |
| Option Annotations | A. rounds down for y-value when $x = 1$ B. rounds down for y-value when $x = 1$; reverses definitions of x and y in relationship C. correct D. reverses definitions of x and y in relationship |

7. The perimeter of a square is $28x - 4$. What is the length of one side of the square?
- A. $x - 1$
 - B. $7x - 1$
 - C. $14x - 2$
 - D. $24x - 4$

| Item Information | |
|--------------------|---|
| Alignment | B-E.1.1 |
| Answer Key | B |
| Depth of Knowledge | 2 |
| p-value A | 6% |
| p-value B | 63% (correct answer) |
| p-value C | 15% |
| p-value D | 16% |
| Option Annotations | <p>A. divides 4 by 4 to get 1; does not include coefficient for variable</p> <p>B. correct</p> <p>C. represents the length of 2 sides of the square</p> <p>D. subtracts 4 from 28 to represent 4 sides of a square; does not change original perimeter value of 4</p> |

8. Which expression is equivalent to $3.5x + 4.8$?

- A. $3 \bullet 0.5x + 4 \bullet 0.8$
- B. $3x \bullet 0.5x + 4 \bullet 0.8$
- C. $3 + 0.5x + 4 + 0.8$
- D. $3x + 0.5x + 4 + 0.8$

| Item Information | |
|--------------------|--|
| Alignment | B-E.1.1.1 |
| Answer Key | D |
| Depth of Knowledge | 1 |
| p-value A | 11% |
| p-value B | 9% |
| p-value C | 40% |
| p-value D | 40% (correct answer) |
| Option Annotations | A. thinks $(3)(0.5x) = 3.5x$; separates 4 and 0.8 by multiplication B. thinks $(3x)(0.5x) = 3.5x$; separates 4 and 0.8 by multiplication C. thinks $3 + 0.5x = 3.5x$ D. correct |

9. Kelly has a savings account with a beginning balance of \$800.
- She earns \$340 a week at her job.
 - For 8 weeks, she puts 15% of her weekly earnings into the savings account.
 - Kelly makes 3 withdrawals of \$45 each.

What is the account balance at the end of 8 weeks?

- A. \$785
- B. \$848
- C. \$1,073
- D. \$1,163

| Item Information | |
|--------------------|--|
| Alignment | B-E.2.1.1 A-R.1.1.6 |
| Answer Key | C |
| Depth of Knowledge | 2 |
| p-value A | 12% |
| p-value B | 15% |
| p-value C | 58% (correct answer) |
| p-value D | 15% |
| Option Annotations | A. adds 15×8 to beginning balance and then subtracts 3×45 B. subtracts 8×45 instead of 3×45 C. correct D. subtracts 45 instead of 3×45 |

10. A group of adults and students buy tickets for a dance performance.

- Each ticket costs \$4.65.
- The total cost of the tickets for the group is \$93.00.
- There are exactly 3 adults in the group.

What is the number of students in the group?

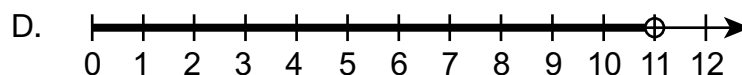
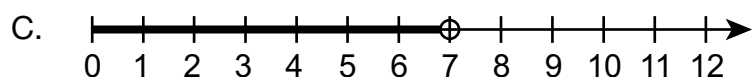
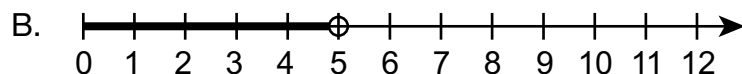
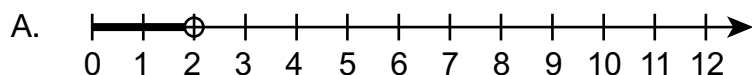
- A. 17
- B. 20
- C. 23
- D. 31

| Item Information | |
|--------------------|--|
| Alignment | B-E.2.2.1 |
| Answer Key | A |
| Depth of Knowledge | 2 |
| p-value A | 67% (correct answer) |
| p-value B | 19% |
| p-value C | 5% |
| p-value D | 9% |
| Option Annotations | <p>A. correct</p> <p>B. solves equation $4.65x = 93.00$ and finds total number in group</p> <p>C. starts with correct equation $4.65(s + 3) = 93.00$; gets $s + 3 = 20$, but then adds 3 to 20</p> <p>D. ignores price of tickets and solves $3x = 93$</p> |

11. Walter is buying strawberries and grapes.

- The total amount he spends on the fruit must be less than \$14.00.
- He spends \$5.25 on a basket of strawberries.
- Grapes cost \$1.75 per pound.

Which graph **best** represents all the numbers of pounds of grapes Walter can buy?

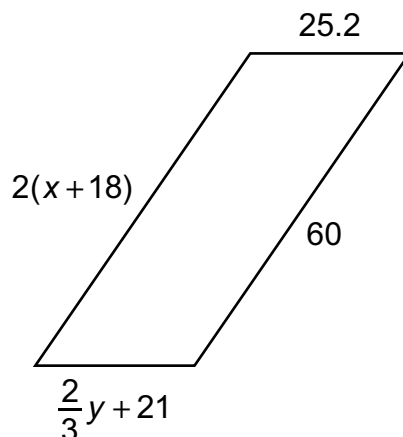


| Item Information | |
|--------------------|--|
| Alignment | B-E.2.2.2 |
| Answer Key | B |
| Depth of Knowledge | 2 |
| p-value A | 12% |
| p-value B | 58% (correct answer) |
| p-value C | 22% |
| p-value D | 8% |
| Option Annotations | <p>A. sets up inequality correctly as $1.75x + 5.25 < 14$; adds $1.75 + 5.25$, gets 7 and divides into 14</p> <p>B. correct</p> <p>C. does not use an inequality; calculates $14 - 5.25 - 1.75$</p> <p>D. sets up inequality correctly as $1.75x + 5.25 < 14$; adds 5.25 to 14, gets $1.75x < 19.25$ and then $x < 11$</p> |

12. A club plans to spend no more than 85% of the \$1,200.00 in its activity budget to buy as many radio-controlled helicopters as possible. The price of a helicopter is \$110.99 plus sales tax of 6%. What is the **greatest** number of helicopters the club can buy?
- A. 8
 - B. 9
 - C. 10
 - D. 11

| Item Information | |
|--------------------|--|
| Alignment | B-E.2.3 |
| Answer Key | A |
| Depth of Knowledge | 2 |
| p-value A | 42% (correct answer) |
| p-value B | 24% |
| p-value C | 24% |
| p-value D | 10% |
| Option Annotations | <p>A. correct</p> <p>B. solves $\frac{(0.85 \times 1,200.00)}{(110.99 \times 1.065)}$ and rounds up</p> <p>C. solves $\frac{(1,200.00)}{(110.99 \times 1.065)}$ and rounds down</p> <p>D. solves $\frac{(1,200.00)}{(110.99 \times 1.065)}$ and rounds up</p> |

13. A quadrilateral is shown below.



What values of x and y make the quadrilateral a parallelogram?

- A. $x = 12$ and $y = 6.3$
- B. $x = 21$ and $y = 16.8$
- C. $x = 60$ and $y = 25.2$
- D. $x = 5.4$ and $y = 58.5$

| Item Information | |
|--------------------|--|
| Alignment | C-G.1.1 B-E.2 |
| Answer Key | A |
| Depth of Knowledge | 2 |
| p-value A | 58% (correct answer) |
| p-value B | 15% |
| p-value C | 18% |
| p-value D | 9% |
| Option Annotations | <p>A. correct</p> <p>B. solves $2x + 18 = 60$ for x and $\frac{2}{3}(y + 21) = 25.2$ for y</p> <p>C. uses measures of opposite sides as lengths, but does not use in equations</p> <p>D. thinks consecutive sides must be congruent; solves $2(x + 18) = 25.2$ with a sign error in solution; solves $\left(\frac{2}{3}\right)y + 21 = 60$ correctly</p> |

14. Lee will conduct a survey at his school. He will select a random sample of students at the school to take the survey. Which sample is the **best** random sample for Lee to use?
- A. every other student in the drama club
 - B. every fifth student who enters the school
 - C. every student who rides the same bus as Lee
 - D. every fourth student in Lee's homeroom class

| Item Information | |
|--------------------|---|
| Alignment | D-S.1.1.1 |
| Answer Key | B |
| Depth of Knowledge | 2 |
| p-value A | 7% |
| p-value B | 73% (correct answer) |
| p-value C | 11% |
| p-value D | 9% |
| Option Annotations | A. selects a sample, but not the best random sample B. correct C. selects a sample, but not the best random sample D. selects a sample, but not the best random sample |

15. As of 2012, there have been 8 players in the history of professional baseball who have each hit more than 600 home runs in his career. There have been over 15,000 professional baseball players throughout the history of professional baseball. Which term **best** describes the likelihood that a randomly chosen professional baseball player has hit more than 600 home runs in his career?
- A. impossible
 - B. unlikely
 - C. neither unlikely nor likely
 - D. likely

| Item Information | |
|--------------------|--|
| Alignment | D-S.3.1.1 |
| Answer Key | B |
| Depth of Knowledge | 2 |
| p-value A | 7% |
| p-value B | 67% (correct answer) |
| p-value C | 13% |
| p-value D | 13% |
| Option Annotations | <p>A. thinks since the probability is so small, it is “virtually” impossible</p> <p>B. correct</p> <p>C. thinks that since there are only two possibilities (i.e., they’ve hit 600 home runs or they haven’t), the probability is 50%</p> <p>D. misunderstands the terms likely and unlikely</p> |

16. A chair can be purchased in one of four colors: red, white, green, or blue. The number of chairs purchased in each color is listed below.

- red: 150
- white: 450
- green: 225
- blue: 375

Based on the information shown in the list, what is the probability that the next chair purchased will be red?

A. $\frac{1}{8}$

B. $\frac{1}{7}$

C. $\frac{1}{4}$

D. $\frac{2}{5}$

| Item Information | |
|--------------------|---|
| Alignment | D-S.3.2.1 |
| Answer Key | A |
| Depth of Knowledge | 2 |
| p-value A | 55% (correct answer) |
| p-value B | 7% |
| p-value C | 31% |
| p-value D | 7% |
| Option Annotations | <p>A. correct</p> <p>B. chooses red out of not red</p> <p>C. chooses 1 color out of 4</p> <p>D. focuses on two least amounts to calculate probability; red out of red + green or $\frac{150}{375}$, since red is least</p> |

OPEN-ENDED QUESTION

17. Archie has a bag of grass seed that he will use to cover a new field. The bag contains information about the area of the ground to be covered and the number of scoops of grass seed needed, as shown in the table below.

Grass Seed

| | | | | |
|--|----|-----|-----|-----|
| Area of Ground to Be Covered (square yards) | 50 | 100 | 150 | 200 |
| Number of Scoops | 2 | 4 | 6 | 8 |

- A. What is the constant of proportionality between the number of square yards of ground to be covered and the number of scoops of grass seed needed?

The field Archie will cover with grass seed is rectangular and measures 100 yards long by 60 yards wide.

- B. Write an equation that describes the relationship between the number of square yards (x) of ground to be covered and the number of scoops (y) of grass seed needed. Use the equation to determine the number of scoops of grass seed Archie needs to cover the entire field. Show or explain all your work.

Go to the next page to finish question 17.



17. Continued. Please refer to the previous page for task explanation.

Archie has a goal to finish covering the field before $1\frac{2}{3}$ hours have elapsed. He will use any remaining time to water the field. After 1 hour has elapsed, he has covered 4,000 square yards of the field.

- C.** Explain why Archie will be able to meet his goal by working at this rate. As part of the explanation, determine the amount of time, in hours, Archie will have to water the field.

After you have checked your work, close your answer booklet and test booklet so your teacher will know you are finished.



Item-Specific Scoring Guideline

#17 Item Information

| | | | | | |
|-----------|-------|--------------------|---|------------|------|
| Alignment | A-R.1 | Depth of Knowledge | 2 | Mean Score | 1.15 |
|-----------|-------|--------------------|---|------------|------|

Assessment Anchor this item will be reported under:

M07.A-R.1 — Demonstrate an understanding of proportional relationships.

Specific Assessment Anchor Descriptor addressed by this item:

M07.A-R.1.1 — Analyze, recognize, and represent proportional relationships and use them to solve real-world and mathematical problems.

Item-Specific Scoring Guideline

| Score | In this item, the student . . . |
|-------|---|
| 4 | Demonstrates a thorough understanding of proportional relationships by correctly solving problems and clearly explaining procedures. |
| 3 | Demonstrates a general understanding of proportional relationships by correctly solving problems and clearly explaining procedures with only minor errors or omissions. |
| 2 | Demonstrates a partial understanding of proportional relationships by correctly performing a significant portion of the required task. |
| 1 | Demonstrates minimal understanding of proportional relationships. |
| 0 | The response has no correct answer and insufficient evidence to demonstrate any understanding of the mathematical concepts and procedures as required by the task. Response may show only information copied from the question. |

Top-Scoring Student Response and Training Notes

| Score | Description |
|-------|--|
| 4 | Student earns 4 points. |
| 3 | Student earns 3.0–3.5 points. |
| 2 | Student earns 2.0–2.5 points. |
| 1 | Student earns 0.5–1.5 points. OR Student demonstrates minimal understanding of proportional relationships. |
| 0 | Response is incorrect or contains some correct work that is irrelevant to the skill or concept being measured. |

Top-Scoring Response

Part A (1 point):

1 point for correct answer

| What? | Why? |
|---|------|
| $\frac{1}{25}$ OR 25 OR EQUIVALENT | |

Part B ($1\frac{1}{2}$ points):

$\frac{1}{2}$ point for correct equation

$\frac{1}{2}$ point for correct answer

$\frac{1}{2}$ point for correct and complete support

| What? | Why? |
|---|--|
| $y = \frac{1}{25}x$ OR EQUIVALENT AND 240 (scoops) | <p>Sample Work:</p> $y = \frac{1}{25}x \quad 100 \cdot 60 = 6,000 \quad y = \frac{1}{25} \cdot 6,000$ $y = 240$ <p>OR</p> <p>Sample Explanation:</p> <p>The equation relating x and y is $y = \frac{1}{25}x$. Multiply 100 by 60 to determine the number of square yards that need to be covered, which is 6,000. Substitute 6,000 into the equation for x and multiply to determine 240 scoops are needed.</p> <p>OR EQUIVALENT</p> |

Part C ($1\frac{1}{2}$ points): $\frac{1}{2}$ point for correct answer

1 point for correct and complete explanation

OR $\frac{1}{2}$ point for correct but incomplete explanation

| What? | Why? |
|----------------------|---|
| $\frac{1}{6}$ (hour) | <p>Sample Explanation:</p> <p>At the rate Archie is working, he will be able to meet his goal because a rate of 4,000 square yards covered per 1 hour is equivalent to $6,666\frac{2}{3}$ square yards covered per $1\frac{2}{3}$ hours. Since he only has to cover 6,000 square yards, he will meet his goal. A rate of 4,000 square yards covered per 1 hour is equivalent to 6,000 square yards covered per $1\frac{1}{2}$ hours. Archie will finish $\frac{1}{6}$ hour before $1\frac{2}{3}$ hours have elapsed since $1\frac{2}{3} - 1\frac{1}{2} = \frac{1}{6}$.</p> <p>OR EQUIVALENT</p> |

STUDENT RESPONSE

Response Score: 4 points



PARTS A AND B

Question 17

Page 1 of 2

Item ID

?

Line Guide

Calculator

Eraser

Highlighter

Selection

Archie has a bag of grass seed that he will use to cover a new field. The bag contains information about the area of the ground to be covered and the number of scoops of grass seed needed, as shown in the table below.

| Area of Ground to Be Covered (square yards) | 50 | 100 | 150 | 200 |
|---|----|-----|-----|-----|
| Number of Scoops | 2 | 4 | 6 | 8 |

A. What is the constant of proportionality between the number of square yards of ground to be covered and the number of scoops of grass seed needed?

Eq

$\frac{50}{2} = 25$

The response provides a correct answer.

The field Archie will cover with grass seed is rectangular and measures 100 yards long by 60 yards wide.

B. Write an equation that describes the relationship between the number of square yards (x) of ground to be covered and the number of scoops (y) of grass seed needed. Use the equation to determine the number of scoops of grass seed Archie needs to cover the entire field. Show or explain all your work.

Eq

$$y = \frac{x}{25} = \frac{100 \cdot 60}{25} = \frac{6000}{25} = 240$$

240 scoops of grass seed

The response provides a correct equation and answer. The support is correct and complete.

48 / 1000

Next

Review/End Test

Pause

Flag

Options

PART C

Question 17
Page 2 of 2

Item ID



Archie has a bag of grass seed that he will use to cover a new field. The bag contains information about the area of the ground to be covered and the number of scoops of grass seed needed, as shown in the table below.

Grass Seed

| Area of Ground to Be Covered (square yards) | 50 | 100 | 150 | 200 |
|--|----|-----|-----|-----|
| Number of Scoops | 2 | 4 | 6 | 8 |

Archie has a goal to finish covering the field before $1\frac{2}{3}$ hours have elapsed. He will use any remaining time to water the field. After 1 hour has elapsed, he has covered 4,000 square yards of the field.

C. Explain why Archie will be able to meet his goal by working at this rate. As part of the explanation, determine the amount of time, in hours, Archie will have to water the field.

Eq

Archie will be able to meet his goal working at this rate because in $\frac{2}{3}$ hours more he would have covered 6666.666... square yards and he only has 6000 square yards to cover. archie only needs half of an hour to finish at this rate so he has $\frac{1}{6}$ of an hour to water the field.

The response provides a correct answer and a complete explanation.

276 / 1000

Review/End Test

Pause

Flag

Options

Back

Next

STUDENT RESPONSE

Response Score: 3 points

17. Archie has a bag of grass seed that he will use to cover a new field. The bag contains information about the area of the ground to be covered and the number of scoops of grass seed needed, as shown in the table below.

Grass Seed

| Area of Ground to Be Covered (square yards) | 50 | 100 | 150 | 200 |
|--|----|-----|-----|-----|
| Number of Scoops | 2 | 4 | 6 | 8 |

- A. What is the constant of proportionality between the number of square yards of ground to be covered and the number of scoops of grass seed needed?

The constant number of proportionality is $2\overline{)50}$ $4\overline{)100}$ $6\overline{)150}$
 25 sq. yd. per scoop.

The response provides a correct answer.

The field Archie will cover with grass seed is rectangular and measures 100 yards long by 60 yards wide.

- B. Write an equation that describes the relationship between the number of square yards (x) of ground to be covered and the number of scoops (y) of grass seed needed. Use the equation to determine the number of scoops of grass seed Archie needs to cover the entire field. Show or explain all your work.

$$x \div y = 240 \text{ scoops}$$

$$x = [100 \cdot 60] 6000 \text{ sq yd.}$$

$$y = [6000 \text{ sq yd} / 25 \text{ sq yd}] 240 \text{ scoops}$$

The response provides a correct answer. The equation provided is incorrect. The support is correct and complete.

Go to the next page to finish question 17.



17. **Continued.** Please refer to the previous page for task explanation.

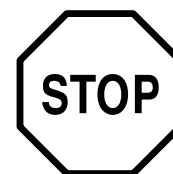
Archie has a goal to finish covering the field before $1\frac{2}{3}$ hours have elapsed. He will use any remaining time to water the field. After 1 hour has elapsed, he has covered 4,000 square yards of the field.

- C. Explain why Archie will be able to meet his goal by working at this rate. As part of the explanation, determine the amount of time, in hours, Archie will have to water the field.

If it takes Archie 1 hr out of an 1 hr and 40 min to cover $66\frac{2}{3}\%$ of the field, he'd have 40 min left to cover $33\frac{1}{3}\%$ of the field. Archie covers $33\frac{1}{3}\%$ of the field in 30 min. So, out of 40 min, Archie has 30 min to cover the rest of the field and $\frac{1}{6}$ hr to water it.

The response provides a correct answer and a complete explanation.

After you have checked your work, close your answer booklet and test booklet so your teacher will know you are finished.



STUDENT RESPONSE

Response Score: 2 points



PARTS A AND B

Question 17
Page 1 of 2

Item ID

?

Grass Seed

| Area of Ground to Be Covered (square yards) | 50 | 100 | 150 | 200 |
|---|----|-----|-----|-----|
| Number of Scoops | 2 | 4 | 6 | 8 |

Archie has a bag of grass seed that he will use to cover a new field. The bag contains information about the area of the ground to be covered and the number of scoops of grass seed needed, as shown in the table below.

A. What is the constant of proportionality between the number of square yards of ground to be covered and the number of scoops of grass seed needed?

Eq

25

The response provides a correct answer.

The field Archie will cover with grass seed is rectangular and measures 100 yards long by 60 yards wide.

B. Write an equation that describes the relationship between the number of square yards (x) of ground to be covered and the number of scoops (y) of grass seed needed. Use the equation to determine the number of scoops of grass seed Archie needs to cover the entire field. Show or explain all your work.

Eq

$(x \div 25) = y$ --> The constant proportionality is 25, so we have to divide it with the area ground to be covered.
 $6,000 \div 25 = y$ --> Since the area is a rectangle and it provides us with the length and width we multiply 100 yd by 60 yd and get 6,000.
 $y = 240$ scoops --> divide it by 25 to get the amount of scoops

The response provides a correct equation and answer. The support is correct and complete.

294 / 1000

Next

Review/End Test

Pause

Flag

Options

PART C

Question 17
Page 2 of 2

Item ID



Archie has a bag of grass seed that he will use to cover a new field. The bag contains information about the area of the ground to be covered and the number of scoops of grass seed needed, as shown in the table below.

Grass Seed

| Area of Ground to Be Covered (square yards) | 50 | 100 | 150 | 200 |
|--|----|-----|-----|-----|
| Number of Scoops | 2 | 4 | 6 | 8 |

Archie has a goal to finish covering the field before $1\frac{2}{3}$ hours have elapsed. He will use any remaining time to water the field. After 1 hour has elapsed, he has covered 4,000 square yards of the field.

C. Explain why Archie will be able to meet his goal by working at this rate. As part of the explanation, determine the amount of time, in hours, Archie will have to water the field.

Eq

Why Archie will achieve this goal by working at this rate is he's not taking breaks and in 1 hour he has already covered 4,000 sq yds of the field. What remaining Archie will have is $\frac{2}{3}$ of a hour.

The response provides an incorrect answer and incorrect explanation.

197 / 1000

Review/End Test

Pause

Flag

Options

Back

Next

STUDENT RESPONSE

Response Score: 1 point

17. Archie has a bag of grass seed that he will use to cover a new field. The bag contains information about the area of the ground to be covered and the number of scoops of grass seed needed, as shown in the table below.

Grass Seed

| | | | | |
|--|----|-----|-----|-----|
| Area of Ground to Be Covered (square yards) x | 50 | 100 | 150 | 200 |
| Number of Scoops y | 2 | 4 | 6 | 8 |

.04

- A. What is the constant of proportionality between the number of square yards of ground to be covered and the number of scoops of grass seed needed?

The constant proportionality
is .04.

The response provides a correct answer
(answer is equivalent).

The field Archie will cover with grass seed is rectangular and measures 100 yards long by 60 yards wide.

- B. Write an equation that describes the relationship between the number of square yards (x) of ground to be covered and the number of scoops (y) of grass seed needed. Use the equation to determine the number of scoops of grass seed Archie needs to cover the entire field. Show or explain all your work.

Archie will need 4
scoops of grass to cover
the field completely.

The response provides an incorrect answer.
No equation or support are given.

Go to the next page to finish question 17.



17. **Continued.** Please refer to the previous page for task explanation.

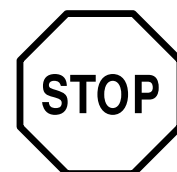
Archie has a goal to finish covering the field before $1\frac{2}{3}$ hours have elapsed. He will use any remaining time to water the field. After 1 hour has elapsed, he has covered 4,000 square yards of the field.

- C. Explain why Archie will be able to meet his goal by working at this rate. As part of the explanation, determine the amount of time, in hours, Archie will have to water the field.

Archie will be able to meet
his goal because he has
already covered 4,000 sq yards
in 1 hour and only needs
to cover a little bit
more to be done.

The response provides an incorrect answer and incorrect explanation.

After you have checked your work, close your answer booklet and test booklet so your teacher will know you are finished.



STUDENT RESPONSE

Response Score: 0 points



PARTS A AND B

Question 17

Page 1 of 2

Item ID

?

Line Guide

Calculator

Eraser

Highlighter

Selection

Archie has a bag of grass seed that he will use to cover a new field. The bag contains information about the area of the ground to be covered and the number of scoops of grass seed needed, as shown in the table below.

| Area of Ground to Be Covered (square yards) | 50 | 100 | 150 | 200 |
|---|----|-----|-----|-----|
| Number of Scoops | 2 | 4 | 6 | 8 |

A. What is the constant of proportionality between the number of square yards of ground to be covered and the number of scoops of grass seed needed?

Eq

200 and 8

The response provides an incorrect answer.

The field Archie will cover with grass seed is rectangular and measures 100 yards long by 60 yards wide.

B. Write an equation that describes the relationship between the number of square yards (x) of ground to be covered and the number of scoops (y) of grass seed needed. Use the equation to determine the number of scoops of grass seed Archie needs to cover the entire field. Show or explain all your work.

Eq

The number 100 and 60 go by tens.

The response provides an incorrect answer and incorrect support. No equation is given.

33 / 1000

Next

Review/End Test

Pause

Flag

Options

PART C

Question 17
Page 2 of 2

Item ID



Archie has a bag of grass seed that he will use to cover a new field. The bag contains information about the area of the ground to be covered and the number of scoops of grass seed needed, as shown in the table below.

Grass Seed

| Area of Ground to Be Covered (square yards) | 50 | 100 | 150 | 200 |
|--|----|-----|-----|-----|
| Number of Scoops | 2 | 4 | 6 | 8 |

Archie has a goal to finish covering the field before $1\frac{2}{3}$ hours have elapsed. He will use any remaining time to water the field. After 1 hour has elapsed, he has covered 4,000 square yards of the field.

C. Explain why Archie will be able to meet his goal by working at this rate. As part of the explanation, determine the amount of time, in hours, Archie will have to water the field.

Eq

$$1\frac{2}{3} + 4,000 = 5\frac{2}{3} \text{ is the answer}$$

The response provides an incorrect answer and no explanation.

24 / 1000

Review/End Test

Pause

Flag

Options

Back

Next

MATHEMATICS—SUMMARY DATA

MULTIPLE-CHOICE

| Sample Number | Alignment | Answer Key | Depth of Knowledge | p-values A | p-values B | p-values C | p-values D |
|---------------|------------------------|------------|--------------------|------------|------------|------------|------------|
| 1 | A-N.1.1.1 | D | 1 | 26% | 12% | 28% | 34% |
| 2 | A-N.1.1 | C | 2 | 16% | 20% | 49% | 15% |
| 3 | A-N.1.1.3 | D | 1 | 7% | 11% | 9% | 73% |
| 4 | A-R.1.1.1 | B | 2 | 11% | 70% | 10% | 9% |
| 5 | A-R.1.1.3 | B | 2 | 11% | 76% | 7% | 6% |
| 6 | A-R.1.1.5 | C | 2 | 9% | 8% | 67% | 16% |
| 7 | B-E.1.1 | B | 2 | 6% | 63% | 15% | 16% |
| 8 | B-E.1.1.1 | D | 1 | 11% | 9% | 40% | 40% |
| 9 | B-E.2.1.1 A-R.1.1.6 | C | 2 | 12% | 15% | 58% | 15% |
| 10 | B-E.2.2.1 | A | 2 | 67% | 19% | 5% | 9% |
| 11 | B-E.2.2.2 | B | 2 | 12% | 58% | 22% | 8% |
| 12 | B-E.2.3 | A | 2 | 42% | 24% | 24% | 10% |
| 13 | C-G.1.1 B-E.2 | A | 2 | 58% | 15% | 18% | 9% |
| 14 | D-S.1.1.1 | B | 2 | 7% | 73% | 11% | 9% |
| 15 | D-S.3.1.1 | B | 2 | 7% | 67% | 13% | 13% |
| 16 | D-S.3.2.1 | A | 2 | 55% | 7% | 31% | 7% |

OPEN-ENDED

| Sample Number | Alignment | Points | Depth of Knowledge | Mean Score |
|---------------|-----------|--------|--------------------|------------|
| 17 | A-R.1 | 4 | 2 | 1.15 |