Pennsylvania PSSA 2016 Grade 8 Math

Reference Materials
Page 2

Exam & Answer Key Materials Pages 3 - 38

Grade 8 Formula Sheet

Formulas that you may need to work questions on this test are found below. You may refer back to this page at any time during the mathematics test. You may use calculator π or the number 3.14.

2016 Grade 8

Exponential Properties

$$a^m \cdot a^n = a^{m+n}$$

$$(a^m)^n = a^{m \cdot n}$$

$$\frac{a^m}{a^n} = a^{m-n}$$

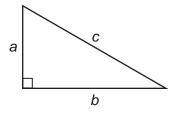
$$a^{-1} = \frac{1}{a}$$

Algebraic Equations

Slope:
$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

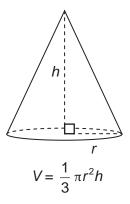
Slope-Intercept Form: y = mx + b

Pythagorean Theorem

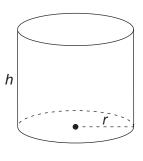


$$a^2 + b^2 = c^2$$

Cone

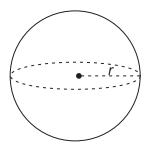


Cylinder



$$V = \pi r^2 h$$

Sphere

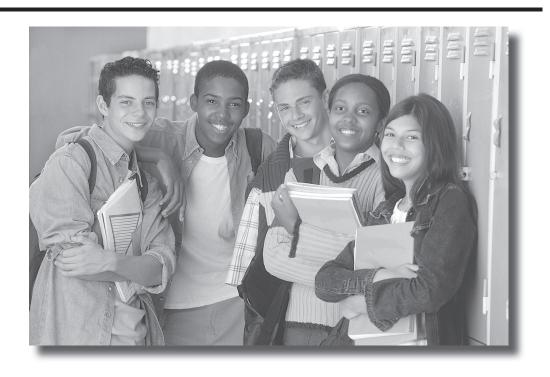


$$V = \frac{4}{3} \pi r^3$$



The Pennsylvania System of School Assessment

Mathematics Item and Scoring Sampler



2016-2017 **Grade 8**

Pennsylvania Department of Education Bureau of Curriculum, Assessment and Instruction—September 2016

MATHEMATICS TEST DIRECTIONS

On the following pages are the mathematics questions.

 You may <u>not</u> use a calculator for question 1. You may use a calculator for all other questions on this test.

Directions for Multiple-Choice Questions:

Some questions will ask you to select an answer from among four choices.

For the multiple-choice questions:

- First solve the problem on scratch paper.
- Choose the correct answer and record your choice in the answer booklet.
- If none of the choices matches your answer, go back and check your work for possible errors.
- Only one of the answers provided is the correct response.

Directions for Open-Ended Questions:

Some questions will require you to write your response.

For the open-ended questions:

- These questions have more than one part. Be sure to read the directions carefully.
- You cannot receive the highest score for an open-ended question without completing
 all tasks in the question. For example, if the question asks you to show your work or
 explain your reasoning, be sure to show your work or explain your reasoning in the
 space provided.
- If the question does **not** ask you to show your work or explain your reasoning, you
 may use the space provided, but only those parts of your response that the question
 specifically asks for will be scored.
- Write your response in the appropriate location within the response box in the
 answer booklet. Some answers may require graphing, plotting, labeling, drawing, or
 shading. If you use scratch paper, be sure to transfer your final response and any
 needed work or reasoning to the answer booklet.

INFORMATION ABOUT MATHEMATICS

General Description of Scoring Guidelines for Mathematics Open-Ended Questions

4 – The response demonstrates a *thorough* understanding of the mathematical concepts and procedures required by the task.

The response provides correct answer(s) with clear and complete mathematical procedures shown and a correct explanation, as required by the task. Response may contain a minor "blemish" or omission in work or explanation that does not detract from demonstrating a *thorough* understanding.

3 – The response demonstrates a *general* understanding of the mathematical concepts and procedures required by the task.

The response and explanation (as required by the task) are mostly complete and correct. The response may have minor errors or omissions that do not detract from demonstrating a *general* understanding.

2 – The response demonstrates a *partial* understanding of the mathematical concepts and procedures required by the task.

The response is somewhat correct with *partial* understanding of the required mathematical concepts and/or procedures demonstrated and/or explained. The response may contain some work that is incomplete or unclear.

- 1 The response demonstrates a *minimal* understanding of the mathematical concepts and procedures required by the task.
- 0 The response has no correct answer and *insufficient* evidence to demonstrate any understanding of the mathematical concepts and procedures required by the task for that grade level.

Response may show only information copied from the question.

Special Categories within zero reported separately:

BLK (blank)......Blank, entirely erased, or written refusal to respond OT.....Off task

LOEResponse in a language other than English

ILIllegible

Question 1 in this sampler is to be solved without the use of a calculator.

MULTIPLE-CHOICE ITEMS

- **1.** Simplify: $7^{-8} \times 7^{-4}$
 - A. $\frac{1}{7^{12}}$
 - B. $\frac{1}{7^4}$
 - C. 7^{12}
 - D. 7³²

Item Information				Option Annotations
	Alignme	nt B-E.1	.1.1	A. correct
	Answer Key A			B. ignores the negative in the second exponent C. thinks 2 negatives make it positive D. multiplies the exponents
Depth of	Knowledg	edge 1		
	p-values			
Α	В	С	D	
41%	12%	29%	18%	

A calculator is permitted for use in solving questions 2–17 in this sampler.

2. Which equation shows how to find the product of 1,000,000 and 1,000,000 using scientific notation?

A.
$$1,000,000 \times 1,000,000 = (1 \times 10^6) \times (1 \times 10^6) = 1 \times 10^{(6+6)} = 1 \times 10^{12}$$

B.
$$1,000,000 \times 1,000,000 = (1 \times 10^6) \times (1 \times 10^6) = 1 \times 10^{(6 \times 6)} = 1 \times 10^{36}$$

C.
$$1,000,000 \times 1,000,000 = (1 \times 10^7) \times (1 \times 10^7) = 1 \times 10^{(7+7)} = 1 \times 10^{14}$$

D.
$$1,000,000 \times 1,000,000 = (1 \times 10^7) \times (1 \times 10^7) = 1 \times 10^{(7 \times 7)} = 1 \times 10^{49}$$

	Item Infor	mation		Option Annotations
	Alignmer	nt B-E.1	.1.4	A. correct
	Answer Key A			B. multiplies the exponents C. incorrectly uses 7, because of 7 digits
Depth of	Knowledg	e 1		D. incorrectly uses 7, because of 7 digits, and multiplies the
				exponents
	p-values			
Α	В	С	D	
75%	13%	7%	5%	

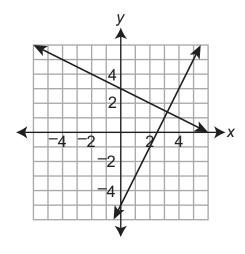
3. Mr. Carter is mapping the boundaries of a park on a coordinate grid. The park's headquarters are located at the origin. The equations shown below represent two boundaries of the park.

$$y = 2x - 5$$

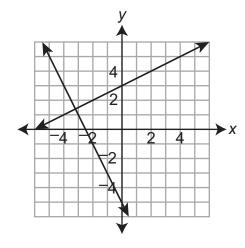
$$2x + 4y = 12$$

The park's entrance is located at the intersection of these two boundaries. Which coordinate grid correctly shows the two boundaries and the park's entrance?

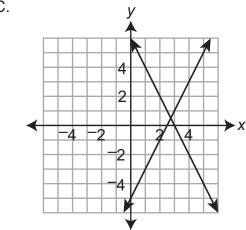
A.



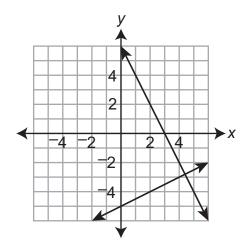
В.



C.



D.



Item Information				
	Alignme	ent	B-E.3	.1.4
	Answer K	еу	Α	
Depth of Knowledge 1				
p-values				
	p-vai	ues	'	
Α	В		С	D
46%	19%	2	2%	13%

- A. correct
- B. uses a negative slope for the first equation and a positive slope for the second equation

Option Annotations

- C. uses the correct first equation but reverses the intercepts for the second equation
- D. uses the reciprocal of the slope for the first equation and reverses the intercepts for the second equation

- **4.** A cleaning company charges *x* dollars per hour to clean floors and *y* dollars per hour to clean the rest of a house.
 - When the company spends 2 hours to clean floors and 3 hours to clean the rest of a house, the total charge is \$84.
 - When the company spends 1 hour to clean floors and 4 hours to clean the rest of a house, the total charge is \$87.

Which ordered pair represents the hourly charges to clean floors and to clean the rest of the house?

- A. (12, 20)
- B. (15, 18)
- C. (18, 15)
- D. (20, 12)

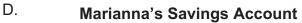
Item Information				Option Annotations
	Alignme	nt B-E.3	.1.5	A. tries these values in the first example; $2 \times 12 + 3 \times 20 = 84$
	Answer Key B			B. correct C. reverses the solution
Depth of	f Knowledge 2			D. reverses the meaning of each value in the ordered pair and tries
				the values in the first example
	p-values			
Α	В	С	D	
19%	55%	15%	11%	
			•	

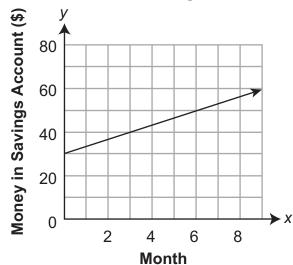
5. Marianna has been adding \$30 to her savings account every month. Which model could represent the money in Marianna's savings account (*y*) after *x* months?

A.
$$y = 10x + 30$$

Month (x)	Money in Savings Account (y)
3	\$100
5	\$160
7	\$220

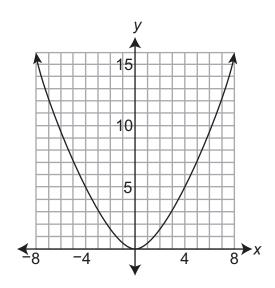
B.
$$y = 10 - 30x$$





	Item Info	rmation		Option Annotations
	Alignme	nt B-F.1.	.1	A. sees 30 is represented, but not as slope
Answer Key C			B. sees 30 and ignores the negative part of the slope C. correct	
Depth of	of Knowledge 2			D. identifies slope as 30/1 instead of 10/3
	<i>p</i> -values			
Α	В	С	D	
28%	9%	48%	15%	
			•	

6. The graph below represents a function.



Which single transformation could be applied to the graph so that it no longer represents a function?

- A. reflection across the *x*-axis
- B. reflection across the y-axis
- C. rotation of 90° clockwise about the origin
- D. translation 5 units to the left

Item Information				Option Annotations
	Alignment B-F.1.1.1 C-G.1.1.1			 A. thinks a function must have some positive <i>y</i>-values B. confuses this with a reflection across y = x C. correct D. thinks all functions must go through the origin
Answer Key C		С		
Depth of	Depth of Knowledge 2			
			_	
	p-values			
Α	В	С	D	
14%	22%	48%	16%	
			-	

7. Two linear functions of x are shown below.

$$y = 30x + 19$$

Function 2

X	У
-12	-311
-8	-211
-3	-86
1	14

Which statement about the functions is true?

- A. Function 2 can be described by the equation y = 35x 109.
- B. Function 2 can be described by the equation y = 100x 11.
- C. The *y*-intercept of function 1 is less than the *y*-intercept of function 2.
- D. The rate of change of function 1 is greater than the rate of change of function 2.

Item Information				Option Annotations
	Alignme	nt B-F.1. B-F.1.		A. sees $35x + 109$ works for first pair in table, but writes as $35x - 109$
Answer Key D		ey D		B. uses difference of first two <i>y</i> -values as slope C. misidentifies <i>y</i> -intercept of function 2 D. correct
Depth of	Depth of Knowledge 2			
	p-values			
Α	В	С	D	
10%	12%	30%	48%	

- **8.** Luis is building a new deck and needs to have a slab of concrete poured. He knows the contractor charges an initial cost of \$75 plus an additional \$2.50 per square foot of concrete. Which equation can be used to determine the cost (*y*), in dollars, to pour a concrete slab with an area of *x* square feet?
 - A. y = 2.5x + 75
 - B. y = 7.5x + 2.5
 - C. y = 75x + 2.5
 - D. y = 77.5x

Item Information				Option Annotations
	Alignme	nt B-F.2.	.1.1	A. correct
	Answer Key A			B. converts 75 to 7.5 and uses it as the rate C. reverses the rate and initial cost
Depth of	Knowled	ge 2		D. adds 75 and 2.5 and assumes that is the rate per square foot
	p-values			
Α	В	С	D	
70%	8%	17%	5%	

9. The graph below shows the relationship between the number of years after a car is purchased and the car's value.



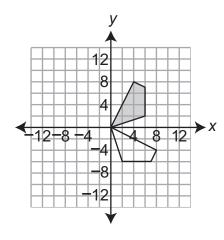
Which statement correctly describes the relationship shown in the graph?

- A. The car's initial value is \$2,000, and the car's value increases \$30,000 each year.
- B. The car's initial value is \$18,000, and the car's value increases \$2,000 each year.
- C. The car's initial value is \$30,000, and the car's value decreases \$2,000 each year.
- D. The car's initial value is \$30,000, and the car's value decreases \$12,000 each year.

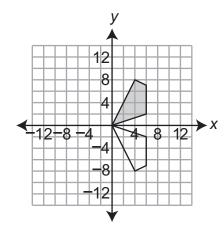
	Item Infor	mation		Option Annotations
	Alignmer	nt B-F.2.	1.2	A. reverses meaning for slope and <i>y</i> -intercept and misreads
	Answer Key C			direction of slope in graph B. reads graph from right to left
Depth of	Knowledg	e 2		C. correct
				D. uses change in value at end of 6 years as rate of change
	<i>p</i> -values			
Α	В	С	D	
3%	5%	79%	13%	

10. Which coordinate plane shows that the shaded polygon is the image of the unshaded polygon after a 90° counterclockwise rotation about the origin?

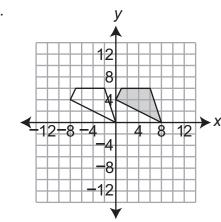
A.



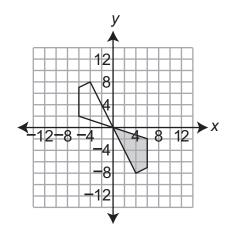
В.



C.

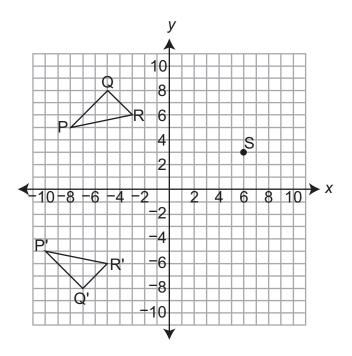


D.



Item Information				Option Annotations
	Alignme	nt C-G	.1.1.1	A. correct
	Answer Key A			B. uses reflection across <i>x</i> -axis C. uses a translation, but thinks 90 degrees because of shifting
Depth of	Knowled	ge 2		from one quadrant to another
				D. uses 180-degree rotation
	<i>p</i> -values			
Α	В	С	D	
49%	20%	7%	24%	

11. In the figure shown below, triangle PQR is transformed to create triangle P'Q'R'.



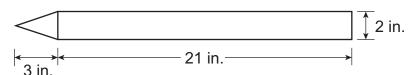
Point S will be transformed the same way as triangle PQR. Which sentence could describe how point S will be transformed?

- A. Point S will be translated to (6, 0) and then rotated to (0, 6).
- B. Point S will be translated to (6, 0) and then rotated to (0, -6).
- C. Point S will be translated to (4, 3) and then reflected to (-4, 3).
- D. Point S will be translated to (4, 3) and then reflected to (4, -3).

	Item Inforn	nation		Option Annotations
Alignment C-G.1.1.2 C-G.1.1.3				A. picks an option that includes the axes B. thinks the two triangles are rotations of one another
	, D		C. reflects the point across the wrong axis D. correct	
Depth of	Depth of Knowledge			2. 35.133.
	p-value	25		
Α	В	С	D	
15%	20%	22%	43%	

12. A balloon in the shape of a crayon is shown below.

Crayon Balloon



The crayon balloon is made up of a cone and a cylinder. What is the volume, in cubic inches, of the crayon balloon?

- A. 69.12
- B. 75.40
- C. 138.23
- D. 276.46

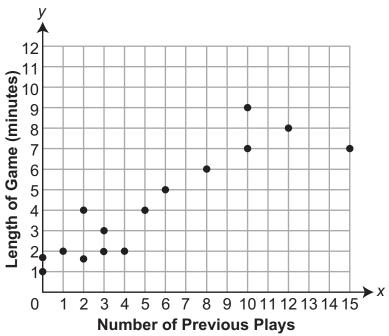
	Item Infor	mation		Option Annotations
	Alignme	nt C-G.3	3.1.1	A. correct
Answer Key		еу А		B. uses formula for volume of a cylinder instead of a cone C. calculates 1 squared as 1 times 2
Depth of	Depth of Knowledge 2			D. uses 2 inches as the radius
	<i>p</i> -valu	ues		
Α	В	С	D	
49%	19%	18%	14%	
	<u>'</u>		•	

- 13. Part of a sculpture is a stone sphere with a volume of 36π cubic feet. What is the radius, in feet, of the stone sphere?
 - A. 3
 - B. 6
 - C. 9
 - D. 12

	Item Infor	mation		Option Annotations
	Alignme	nt C-G.	3.1.1	A. correct
Answer Key A			B. finds square root of 36 C. finds value of <i>r</i> cubed and then divides by 3	
Depth of	Depth of Knowledge			D. divides 36 by 3
	<i>p</i> -valu	ies		
Α	В	С	D	
40%	26%	15%	19%	
	<u>'</u>		•	

14. Christy created the scatter plot shown below.



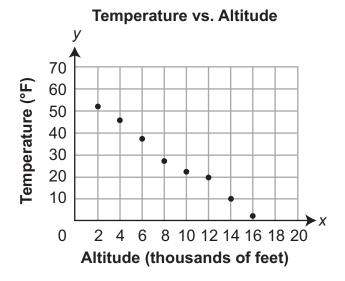


Christy finds that the line of best fit for the data has the equation y = 0.51x + 1.48. Which statement **best** explains how removing the point (15, 7) would affect the slope of the line of best fit?

- A. The slope of the line of best fit would decrease because the point lies below the original line of best fit.
- B. The slope of the line of best fit would decrease because the point lies above the original line of best fit.
- C. The slope of the line of best fit would increase because the point lies below the original line of best fit.
- D. The slope of the line of best fit would increase because the point lies above the original line of best fit.

	Item Infor	mation		Option Annotations						
	Alignmer	nt D-S.1	.1.1	A. identifies where the point lies but thinks removing it would						
Answer Key C				cause the line to move further down B. gets the correct relationship between the location of the point						
Depth of Knowledge		e 2		and the slope but the wrong location of the point						
				C. correct						
	<i>p</i> -valu	es		D. gets the location of the line incorrect and thinks that removing a point above the line will cause the slope of the line to increase						
A B C D point above the line will cause the slope of the line to										
20%	9%	56%	15%							

15. The scatter plot below shows the temperatures (y), in degrees Fahrenheit (°F), that were recorded at different altitudes (x), in thousands of feet.



Which equation could represent the line of best fit for the temperatures, in degrees Fahrenheit, based on the altitudes, in thousands of feet?

A.
$$y = -\frac{9}{4}x + 47$$

B.
$$y = -\frac{7}{2}x + 59$$

C.
$$y = -5x + 69$$

D.
$$y = -5x + 80$$

	Item Infor	mation		Option Annotations						
	Alignme	nt D-S.1	.1.2	A. chooses line that passes through data points (8, 29) and (12, 20)						
Answer Key B		у В		B. correct C. chooses line that passes through data points (6, 39) and (8, 29)						
Depth of Knowledge		je 2		D. chooses line that passes through data points (12, 20)						
				and (14, 10)						
	<i>p</i> -valu	ıes								
Α	В	С	D							
20% 46% 21% 13%										
			•							

16. Blake interviewed 24 students to see whether they collected sports cards and whether they participated in sports. The table below shows his data.

Sports-Card Collecting and Sports Participation

	Participates in Sports	Does Not Participate in Sports
Collects Sports Cards	6	3
Does Not Collect Sports Cards	х	7

How many of the students Blake interviewed participate in sports?

- A. 4
- B. 10
- C. 14
- D. 15

	Item Infor	mation		Option Annotations
	Alignmer	nt D-S.1	.2.1	A. thinks both columns should be equal $(6 + x = 3 + 7)$
	Answer Ke	у С		B. finds how many do not participate in sports C. correct
Depth of	Depth of Knowledge			D. finds how many do not collect sports cards
	p-valu	es		
Α	В	С	D	
16% 17% 63% 4%		4%		

OPEN-ENDED QUESTION

17. Bill used a rain gauge to measure how much rain fell, in centimeters (cm), during a rainfall.

The rain fell at the same rate throughout the first 180 minutes of the rainfall.

A. Complete the table below with the number of minutes it took for 9 centimeters of rain to fall and the number of centimeters of rain that fell through 150 minutes.

Rainfall

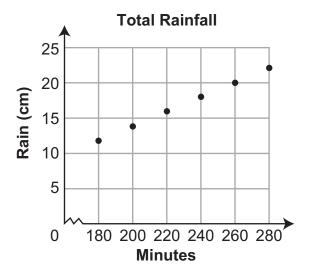
Time (minutes)	30	45	60	90		150	180
Rain (cm)	2	3	4	6	9		12

B. Write an equation to describe the relationship between the time (t), in minutes, and the amount of rain (r), in centimeters.

Go to the next page to finish question 17.

17. Continued. Please refer to the previous page for task explanation.

The total amount of rain that fell from 180 minutes through 280 minutes is shown in the scatter plot below.



C. Describe the change in the slope between the first 180 minutes and the following 100 minutes, and explain what it means in terms of the total amount of rainfall.

After 280 minutes, the slope of the graph is 0.

D. Explain what a slope of 0 means in this situation.

Item-Specific Scoring Guideline

#17 Item Information

Alignment	B-E.2	Depth of Knowledge	2	Mean Score	1.73
-----------	-------	--------------------	---	------------	------

Assessment Anchor this item will be reported under:

M08.B-E.2—Understand the connections between proportional relationships, lines, and linear equations.

Specific Anchor Descriptor addressed by this item:

M08.B-E.2.1—Analyze and describe linear relationships between two variables, using slope.

Scoring Guide

Score	In this item, the student
4	Demonstrates a thorough understanding of connections between proportional relationships, lines, and linear equations by correctly solving problems and clearly explaining procedures.
3	Demonstrates a general understanding of connections between proportional relationships, lines, and linear equations by correctly solving problems and clearly explaining procedures with only minor errors or omissions.
2	Demonstrates a partial understanding of connections between proportional relationships, lines, and linear equations by correctly performing a significant portion of the required task.
1	Demonstrates minimal understanding of connections between proportional relationships, lines, and linear equations.
0	The response has no correct answer and insufficient evidence to demonstrate any understanding of the mathematical concepts and procedures as required by the task. Response may show only information copied from the question.

Top-Scoring Student Response and Training Notes

Score	Description
4	Student earns 4 points.
3	Student earns 3.0–3.5 points.
2	Student earns 2.0–2.5 points.
1	Student earns 0.5–1.5 points. OR Student demonstrates minimal understanding of connections between proportional relationships, lines, and linear equations.
0	Response is incorrect or contains some correct work that is irrelevant to the skill or concept being measured.

Top-Scoring Response

Part A (1 point):

 $\frac{1}{2}$ point for <u>each</u> correct answer

	What?											Wŀ	ıy?		
	Rainfall														
Time (minutes)	30	45	60	90	135	150	180								
Rain (cm)	2	3	4	6	9	10	12								
								1							

Part B (1 point):

1 point for correct equation

What?	Why?
<i>t</i> = 15 <i>r</i>	
OR	
$r = \frac{1}{15}t$	
OR equivalent	

Part C (1 point):

1 point for complete explanation

 $OR\frac{1}{2}$ point for correct but incomplete explanation

What?	Why?
	Sample Explanation: The slope is steeper for the second part. This means it is raining more during that time.

Part D (1 point):

1 point for complete explanation

What?	Why?
	Sample Explanation: A slope of 0 means it stopped raining.

STUDENT RESPONSE

Response Score: 4 points

17. Bill used a rain gauge to measure how much rain fell, in centimeters (cm), during a rainfall.

The rain fell at the same rate throughout the first 180 minutes of the rainfall.

A. Complete the table below with the number of minutes it took for 9 centimeters of rain to fall and the number of centimeters of rain that fell through 150 minutes.

Rainfall

Time (minutes)	30	45	60	90	138	150	180
Rain (cm)	2	3	4	6	9		12

The student has given two correct answers.

B. Write an equation to describe the relationship between the time (t), in minutes, and the amount of rain (r), in centimeters.

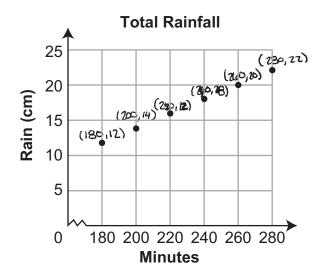
t= 150

The student has given a correct equation.

17. *Continued.* Please refer to the previous page for task explanation.

The total amount of rain that fell from 180 minutes through 280 minutes is shown in the scatter plot below.

 $m = \frac{1}{10}$



C. Describe the change in the slope between the first 180 minutes and the following 100 minutes, and explain what it means in terms of the total amount of rainfall.

In this scatter plot it takes 10 minutes to get a cmn of rain compaired to the previous 15 minutes. This means it is steadily increasing and will yelld a larger amount of rain faster.

The student has given a

complete description.

After 280 minutes, the slope of the graph is 0.

D. Explain what a slope of 0 means in this situation.

It means the rain has stopped.

The student has given a complete explanation.

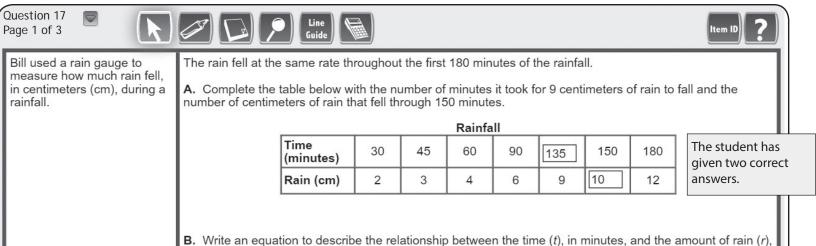
STUDENT RESPONSE

Response Score: 3 points

PARTS A AND B

Next





The student has given a

correct equation.

Options

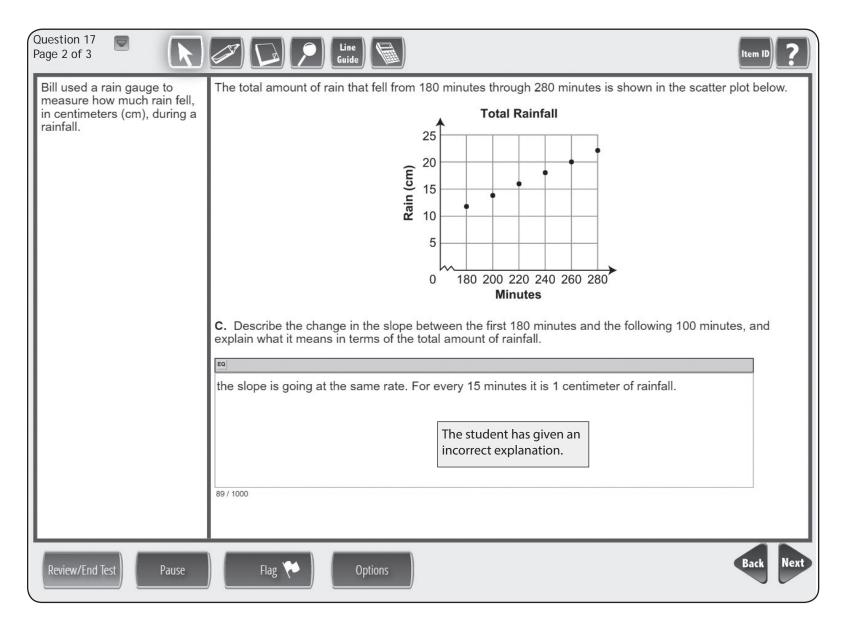
in centimeters.

EQ t = 15r

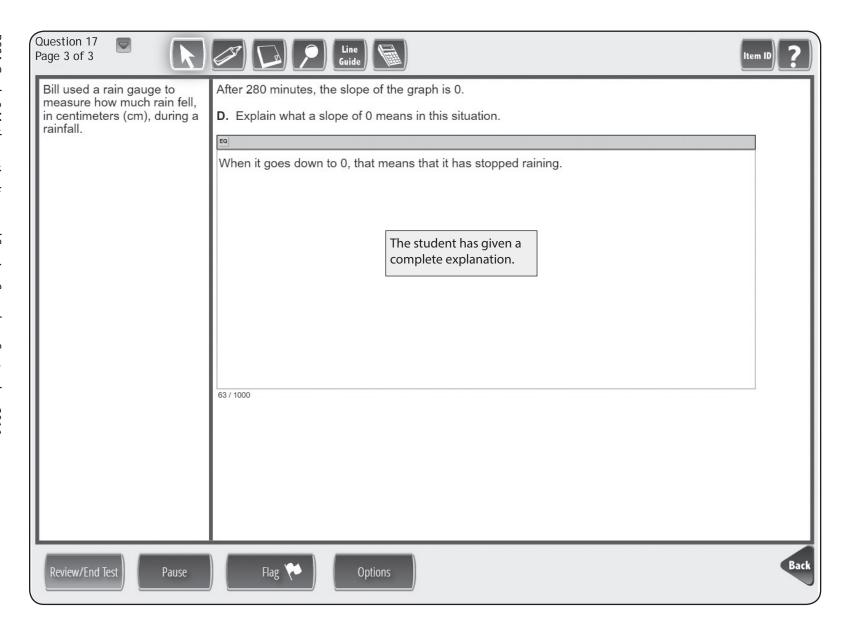
Review/End Test

Pause

PART C



PART D



STUDENT RESPONSE

Response Score: 2 points

17. Bill used a rain gauge to measure how much rain fell, in centimeters (cm), during a rainfall.

The rain fell at the same rate throughout the first 180 minutes of the rainfall.

A. Complete the table below with the number of minutes it took for 9 centimeters of rain to fall and the number of centimeters of rain that fell through 150 minutes.

Rainfall

Time (minutes)	30	45	60	90	135	150	180
Rain (cm)	2	3	4	6	9	10	12

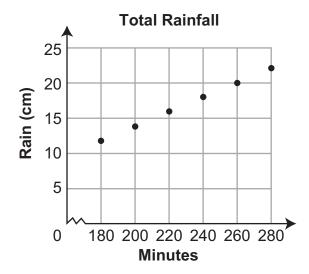
The student has given two correct answers.

B. Write an equation to describe the relationship between the time (t), in minutes, and the amount of rain (r), in centimeters.

The student has given a correct equation.

17. *Continued.* Please refer to the previous page for task explanation.

The total amount of rain that fell from 180 minutes through 280 minutes is shown in the scatter plot below.



C. Describe the change in the slope between the first 180 minutes and the following 100 minutes, and explain what it means in terms of the total amount of rainfall.

The change in Slope is because instead of the minutes increasing by 10. The student has given incorrect explanation.

The student has given an

After 280 minutes, the slope of the graph is 0.

D. Explain what a slope of 0 means in this situation.

of 0 means the line doesn't

move.

The student has given an incorrect explanation.

STUDENT RESPONSE

Response Score: 1 point

PARTS A AND B

The student has

answers.

given two incorrect

Next

Question 17 Page 1 of 3 Bill used a rain gauge to The rain fell at the same rate throughout the first 180 minutes of the rainfall. measure how much rain fell, A. Complete the table below with the number of minutes it took for 9 centimeters of rain to fall and the in centimeters (cm), during a number of centimeters of rain that fell through 150 minutes. rainfall.

Rainfall Time 30 45 60 90 105 150 180 (minutes) 11 3 4 6 9 12 Rain (cm)

B. Write an equation to describe the relationship between the time (t), in minutes, and the amount of rain (r), in centimeters.

 $t = r \cdot 10 + 15$

EQ

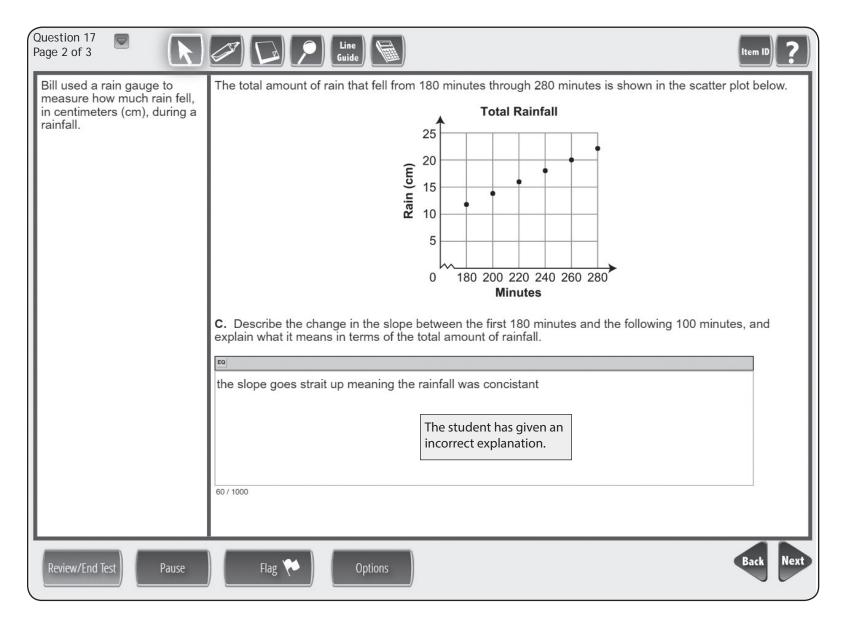
The student has given an incorrect equation.

Options

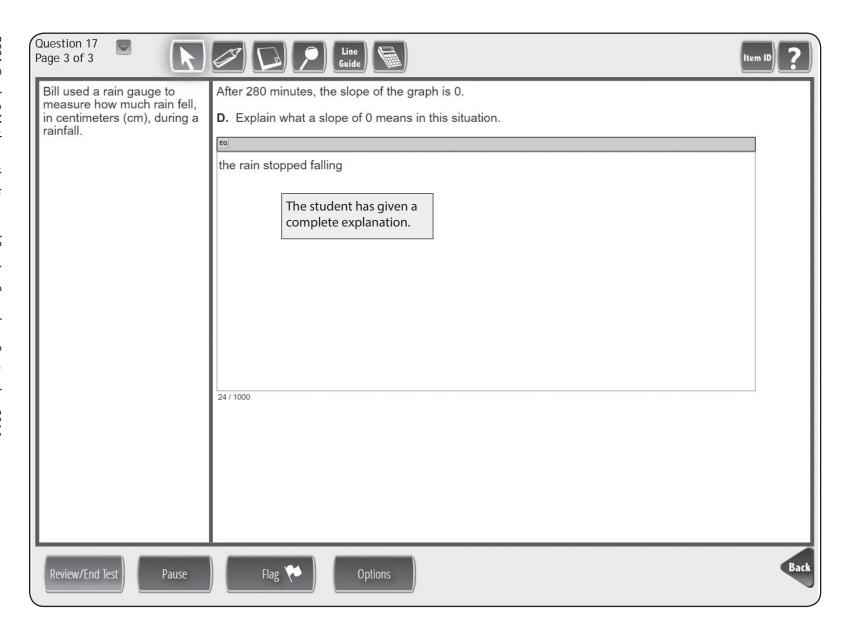
Review/End Test

Pause

PART C



PART D



STUDENT RESPONSE

Response Score: 0 points

17. Bill used a rain gauge to measure how much rain fell, in centimeters (cm), during a rainfall.

The rain fell at the same rate throughout the first 180 minutes of the rainfall.

A. Complete the table below with the number of minutes it took for 9 centimeters of rain to fall and the number of centimeters of rain that fell through 150 minutes.

Rainfall

Time (minutes)	30	45	60	90	120	150	180
Rain (cm)	2	3	4	6	9		12

The student has given two incorrect answers.

B. Write an equation to describe the relationship between the time (t), in minutes, and the amount of rain (r), in centimeters.

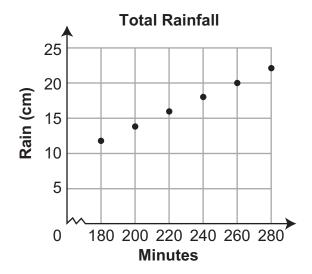
for every every 30 min there's 2cm of rain

The student has not given a correct equation.

Go to the next page to finish question 17.

17. *Continued.* Please refer to the previous page for task explanation.

The total amount of rain that fell from 180 minutes through 280 minutes is shown in the scatter plot below.



C. Describe the change in the slope between the first 180 minutes and the following 100 minutes, and explain what it means in terms of the total amount of rainfall.

the amount of roun went up alot

The student has given an incorrect explanation.

After 280 minutes, the slope of the graph is 0.

D. Explain what a slope of 0 means in this situation.

its not going up any more

The student has given an incorrect explanation.

MATHEMATICS—SUMMARY DATA

MULTIPLE-CHOICE

Sample		Depth of		Depth of p-values					
Number .	Alignment	Answer Key	Knowledge	Α	В	С	D		
1	B-E.1.1.1	А	1	41%	12%	29%	18%		
2	B-E.1.1.4	А	1	75%	13%	7%	5%		
3	B-E.3.1.4	А	1	46%	19%	22%	13%		
4	B-E.3.1.5	В	2	19%	55%	15%	11%		
5	B-F.1.1	С	2	28%	9%	48%	15%		
6	B-F.1.1.1 C-G.1.1.1	С	2	14%	22%	48%	16%		
7	B-F.1.1.2 B-F.1.1.3	D	2	10%	12%	30%	48%		
8	B-F.2.1.1	А	2	70%	8%	17%	5%		
9	B-F.2.1.2	С	2	3%	5%	79%	13%		
10	C-G.1.1.1	А	2	49%	20%	7%	24%		
11	C-G.1.1.2 C-G.1.1.3	D	2	15%	20%	22%	43%		
12	C-G.3.1.1	А	2	49%	19%	18%	14%		
13	C-G.3.1.1	А	2	40%	26%	15%	19%		
14	D-S.1.1.1	С	2	20%	9%	56%	15%		
15	D-S.1.1.2	В	2	20%	46%	21%	13%		
16	D-S.1.2.1	С	2	16%	17%	63%	4%		

OPEN-ENDED

Sample Number	Alignment	Points	Depth of Knowledge	Mean Score
17	B-E.2	4	2	1.73

42