### Pennsylvania PSSA 2019 Grade 4 Math

Reference Materials
Page 2

Exam & Answer Key Materials Pages 3 - 36

#### **INFORMATION ABOUT MATHEMATICS**

#### **Grade 4 Formula Sheet**

Formulas and conversions that you may need on this test are found below. You may refer back to this page at any time during the mathematics test.

2019 Grade 4

#### **Standard Conversions**

$$1 \text{ yard (yd)} = 3 \text{ feet (ft)}$$

$$1 \text{ foot} = 12 \text{ inches (in.)}$$

1 pound (lb) = 
$$16$$
 ounces (oz.)

$$1 \text{ pint} = 2 \text{ cups (c)}$$

#### **Metric Conversions**

$$1 \text{ kilogram (kg)} = 1,000 \text{ grams (g)}$$

1 liter (L) = 
$$1,000$$
 milliliters (mL)

#### **Time Conversions**

1 year (yr) = 12 months (mo)

1 year = 52 weeks (wk)

1 year = 365 days

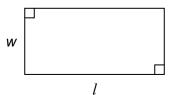
1 week = 7 days

1 day = 24 hours (hr)

1 hour = 60 minutes (min)

1 minute = 60 seconds (sec)

#### Rectangle



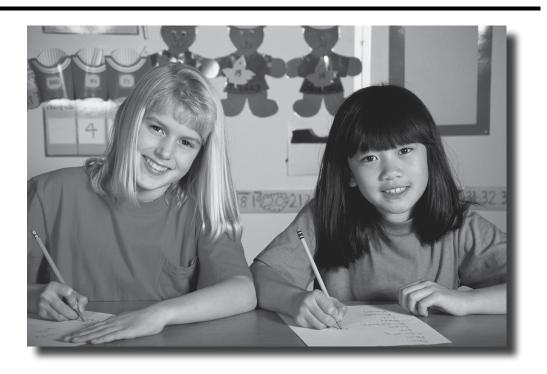
$$A = l \times w$$

Perimeter = length + length + width + width 
$$P = l + l + w + w$$



### The Pennsylvania System of School Assessment

### Mathematics Item and Scoring Sampler



2019-2020 Grade 4

Pennsylvania Department of Education Bureau of Curriculum, Assessment and Instruction—September 2019

#### MATHEMATICS TEST DIRECTIONS

On the following pages are the mathematics questions.

- You may <u>not</u> use a calculator for question 1. You may use a calculator for all other questions on this test.
- You may need a protractor for questions on this test.

#### **Directions for Multiple-Choice Questions:**

Some questions will ask you to select an answer from among four choices.

For the multiple-choice questions:

- First solve the problem on scratch paper.
- Choose the correct answer and record your choice in the answer booklet.
- If none of the choices matches your answer, go back and check your work for possible errors.
- Only one of the answers provided is the correct response.

#### **Directions for Open-Ended Questions:**

Some guestions will require you to write your response.

For the open-ended questions:

- These questions have more than one part. Be sure to read the directions carefully.
- You cannot receive the highest score for an open-ended question without completing all tasks in the question. For example, if the question asks you to show your work or explain your reasoning, be sure to show your work or explain your reasoning in the space provided.
- If the question does **not** ask you to show your work or explain your reasoning, you may use the space provided, but only those parts of your response that the question specifically asks for will be scored.
- Write your response in the appropriate location within the response box in the answer booklet. Some answers may require graphing, plotting, labeling, drawing, or shading. If you use scratch paper, be sure to transfer your final response and any needed work or reasoning to the answer booklet.

#### **INFORMATION ABOUT MATHEMATICS**

#### **General Description of Scoring Guidelines for Mathematics Open-Ended Questions**

4— The response demonstrates a *thorough* understanding of the mathematical concepts and procedures required by the task.

The response provides correct answer(s) with clear and complete mathematical procedures shown and a correct explanation, as required by the task. Response may contain a minor "blemish" or omission in work or explanation that does not detract from demonstrating a *thorough* understanding.

3— The response demonstrates a *general* understanding of the mathematical concepts and procedures required by the task.

The response and explanation (as required by the task) are mostly complete and correct. The response may have minor errors or omissions that do not detract from demonstrating a *general* understanding.

2— The response demonstrates a *partial* understanding of the mathematical concepts and procedures required by the task.

The response is somewhat correct with *partial* understanding of the required mathematical concepts and/or procedures demonstrated and/or explained. The response may contain some work that is incomplete or unclear.

- 1— The response demonstrates a *minimal* understanding of the mathematical concepts and procedures required by the task.
- 0— The response has no correct answer and *insufficient* evidence to demonstrate any understanding of the mathematical concepts and procedures required by the task for that grade level.

Response may show only information copied from the question.

Special Categories within zero reported separately:

Blank	Blank, entirely erased, entirely crossed out, or consists entirely of whitespace	
Refusal	Refusal to respond to the task	
Off Task	Makes no reference to the item but is not an intentional refusal	
Foreign Language	Written entirely in a language other than English	
Illegible	Illegible or incoherent	

Question 1 in this sampler is to be solved without the use of a calculator.

#### **MULTIPLE-CHOICE ITEMS**

- **1.** Which decimal number is equal to  $\frac{79}{100}$ ?
  - A. 0.079
  - B. 0.709
  - C. 0.79
  - D. 7.9

Item Information		
Alignment	A-F.3.1.2	
Answer Key	С	
Depth of Knowledge	1	
p-value A	15%	
p-value B	5%	
p-value C	75% (correct answer)	
p-value D	5%	
Option Annotations	A. misplaces decimal     B. misplaces a 0 after the decimal     C. correct     D. misplaces decimal	

#### A calculator is permitted for use in solving questions 2–16 in this sampler.

- 2. Greg buys 21 bags of nails. Each bag has 85 nails in it. Greg rounds both numbers to the nearest ten to find an estimate of the total number of nails. What is the difference between Greg's estimate of the total number of nails and the actual total number of nails?
  - A. 4
  - B. 6
  - C. 15
  - D. 185

Item Information		
Alignment	A-T.2	
	A-T.1.1.4	
Answer Key	С	
Depth of Knowledge	2	
p-value A	18%	
p-value B	12%	
p-value C	37% (correct answer)	
p-value D	33%	
Option Annotations	A. compares the sum of 21 + 85 with the sum of 20 + 90 B. compares the sum of 21 + 85 with the sum of 20 + 80 C. correct D. rounds to 20 and 80	

- 3. Amanda ate  $\frac{5}{8}$  of her chocolate bar. Cody ate more of his chocolate bar than Amanda ate of hers. Which fraction could represent the amount of Cody's chocolate bar that he ate?
  - A.  $\frac{2}{3}$
  - B.  $\frac{3}{5}$
  - C.  $\frac{5}{10}$
  - D.  $\frac{7}{12}$

Item Information		
Alignment	A-F.1.1.2	
Answer Key	A	
Depth of Knowledge	2	
p-value A	42% (correct answer)	
p-value B	16%	
p-value C	21%	
p-value D	21%	
Option Annotations	A. correct	
	B. confuses the value of $\frac{3}{5}$ with the value of $\frac{3}{4}$	
	C. thinks a larger denominator is a larger amount	
	D. thinks a larger denominator is a larger amount	

- **4.** In Ms. Lassiter's class,  $\frac{1}{8}$  of the students have blue eyes and  $\frac{5}{8}$  of the students have brown eyes. What fraction of the students in Ms. Lassiter's class have neither blue eyes nor brown eyes?
  - A.  $\frac{2}{8}$
  - B.  $\frac{4}{8}$
  - C.  $\frac{5}{8}$
  - D.  $\frac{6}{8}$

Item Information		
Alignment	A-F.2.1.4	
Answer Key	A	
Depth of Knowledge	2	
p-value A	50% (correct answer)	
p-value B	18%	
p-value C	7%	
p-value D	25%	
Option Annotations	<ul> <li>A. correct</li> <li>B. subtracts the fraction of blue-eyed students from the fraction of browneyed students</li> <li>C. adds the numerators and denominators of the fractions before finding the difference from the whole and reducing</li> <li>D. finds the fraction of students with either blue or brown eyes</li> </ul>	

- **5.** A store sold 6 sandwiches. Each sandwich contained between  $\frac{1}{3}$  and  $\frac{1}{2}$  pound of meat. How much meat did the 6 sandwiches contain?
  - A. between 2 and 3 pounds
  - B. between 3 and 4 pounds
  - C. between 5 and 6 pounds
  - D. between 6 and 7 pounds

Item Information		
Alignment	A-F.2.1.7	
Answer Key	A	
Depth of Knowledge	2	
p-value A	52% (correct answer)	
p-value B	15%	
p-value C	22%	
p-value D	11%	
Option Annotations	A. correct	
	B. calculates $6 \times \frac{1}{2}$ and thinks that $6 \times \frac{1}{3}$ is a little greater than $6 \times \frac{1}{2}$	
	C. calculates $6\left(\frac{1}{3} + \frac{1}{2}\right)$	
	D. calculates $6 + \frac{1}{3} + \frac{1}{2}$	

- 6. In Chang's garden,  $\frac{7}{10}$  of the plants are tomato plants and  $\frac{12}{100}$  of the plants are cucumber plants. Which decimal is equal to the fraction of the plants in Chang's garden that are either tomato plants or cucumber plants?
  - A. 0.19
  - B. 0.50
  - C. 0.58
  - D. 0.82

Item Information		
Alignment	A-F.3.1.1	
	A-F.3.1.2	
Answer Key	D	
Depth of Knowledge	1	
p-value A	29%	
p-value B	10%	
p-value C	9%	
p-value D	52% (correct answer)	
Option Annotations	A. adds 12 and 7 and then converts to decimal	
	B. subtracts 7 from 12 and then converts to decimal form incorrectly	
	C. converts $\frac{7}{10}$ to $\frac{70}{100}$ and then subtracts $\frac{12}{100}$	
	D. correct	

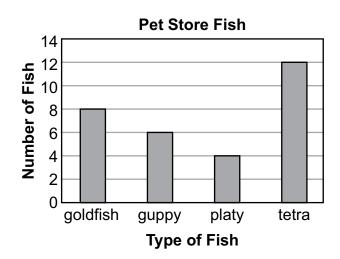
7. In the equation below, each shape stands for a different whole number.

Which expression has the same value as  $\triangle$ ?

- B. \_ + O
- C. □÷○

Item Information		
Alignment	B-O.1.1	
Answer Key	A	
Depth of Knowledge	1	
p-value A	59% (correct answer)	
p-value B	23%	
p-value C	11%	
p-value D	7%	
Option Annotations	A. correct     B. adds instead of subtracts     C. divides instead of subtracts     D. multiplies instead of subtracts	

8. The bar graph below shows the numbers of four types of fish available at a pet store.



The store owner wants to place an equal number of each type of fish into 4 tanks. For which type of fish will the store owner **not** be able to place an equal number of fish into 4 tanks?

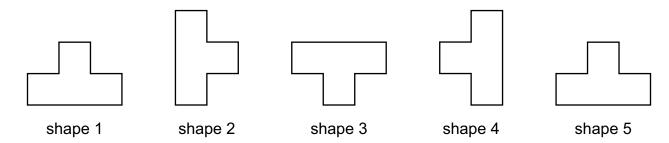
- A. goldfish
- B. guppy
- C. platy
- D. tetra

Item Information	
Alignment	B-O.2.1
	D-M.2.1
Answer Key	В
Depth of Knowledge	2
p-value A	6%
p-value B	42% (correct answer)
p-value C	23%
p-value D	29%
Option Annotations	A. finds a factor of 4
	B. correct
	C. finds a factor of 4
	D. finds a factor of 4

- 9. Claire packages 42 T-shirts for an order. She puts the same number of T-shirts in each package. How many T-shirts could be in each package?
  - A. 6
  - B. 8
  - C. 9
  - D. 12

Item Information		
Alignment	B-O.2.1.1	
Answer Key	A	
Depth of Knowledge	2	
p-value A	72% (correct answer)	
p-value B	9%	
p-value C	6%	
p-value D	13%	
Option Annotations	A. correct B. thinks 8 is a factor of 42 C. thinks 9 is a factor of 42 D. thinks 12 is a factor of 42	

**10.** Emmett makes a shape pattern. He starts with shape 1. He turns the shape 90° clockwise to create the next shape in the pattern. The first five shapes of the pattern are shown below.



The pattern continues. Which list shows **only** the shape numbers that will be in the **same** position as shape 2 in Emmett's pattern?

- A. 4, 6, 8, 10
- B. 4, 8, 12, 16
- C. 6, 8, 10, 12
- D. 6, 10, 14, 18

Item Information		
Alignment	B-O.3	
Answer Key	D	
Depth of Knowledge	2	
p-value A	28%	
p-value B	21%	
p-value C	16%	
p-value D	35% (correct answer)	
Option Annotations	<ul> <li>A. counts by 2, not noticing that 1 and 3 are reflections</li> <li>B. correctly counts by 4 but starts at 4</li> <li>C. starts counting at the right number, but counts by 2 and not 4</li> <li>D. correct</li> </ul>	

**11.** Oscar runs the same number of miles each week. The table below shows the total number of miles he had run through the end of some of the weeks.

**Oscar's Running** 

Weeks	Total Miles
2	26
4	52
5	?
7	91

The pattern continues. Which number sentence could be used to find the total number of miles Oscar had run through the end of week 5?

- A. 52 + 5 = 57
- B.  $5 \times 13 = 65$
- C. 91 5 = 86
- D.  $5 \times 26 = 130$

Item Information		
Alignment	B-O.3.1.2	
	B-O.3.1.3	
Answer Key	В	
Depth of Knowledge	2	
p-value A	11%	
p-value B	61% (correct answer)	
p-value C	19%	
p-value D	9%	
Option Annotations	A. adds 5 to the previous total	
	B. correct	
	C. subtracts 5 from week 7 total	
	D. multiplies 5 by the first total in the table	

- **12.** A wheel of cheddar cheese weighs 22 **pounds**. How many **ounces** does the cheese wheel weigh?
  - A. 220 ounces
  - B. 320 ounces
  - C. 342 ounces
  - D. 352 ounces

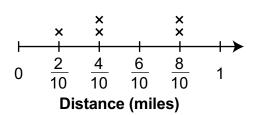
Item Information		
Alignment	D-M.1.1.1	
Answer Key	D	
Depth of Knowledge	1	
p-value A	24%	
p-value B	8%	
p-value C	6%	
p-value D	62% (correct answer)	
Option Annotations	A. uses 10 ounces as a conversion factor B. finds the number of ounces for 20 pounds C. does not regroup when multiplying D. correct	

- **13.** Gertrude practices the piano on Monday from a quarter past 3:00 until 5 minutes before 4:00. On Tuesday, she practices the piano from 5 minutes after 3:00 until a quarter to 4:00. How many minutes does Gertrude practice the piano in all?
  - A. 80
  - B. 90
  - C. 110
  - D. 120

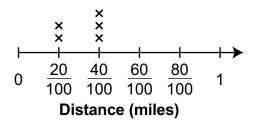
Item Information		
Alignment	D-M.1.1.4 D-M.1.1.2	
Answer Key	A	
Depth of Knowledge	1	
p-value A	41% (correct answer)	
p-value B	19%	
p-value C	21%	
p-value D	19%	
Option Annotations	<ul> <li>A. correct</li> <li>B. finds 50 + 40, thinking Gertrude stopped on Monday at 5 minutes after 4</li> <li>C. finds 40 + 70, thinking Gertrude stopped on Tuesday at a quarter after 4</li> <li>D. finds 50 + 70, thinking Gertrude stopped on Monday at 5 minutes after 4 and on Tuesday at a quarter after 4</li> </ul>	

**14.** Deb and Kendal each walked five times in a week. The line plots below show the distance of each of their walks.

**Deb's Walks** 



#### Kendal's Walks

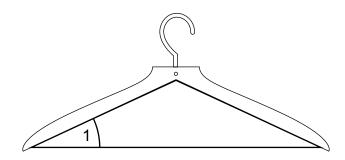


How many miles farther is Deb's longest walk than Kendal's longest walk?

- A.  $\frac{1}{40}$
- B.  $\frac{1}{4}$
- C.  $\frac{4}{10}$
- D.  $\frac{4}{100}$

Item Information		
Alignment	D-M.2.1.2	
Answer Key	С	
Depth of Knowledge	2	
p-value A	10%	
p-value B	11%	
p-value C	55% (correct answer)	
p-value D	24%	
A. creates a unit fraction with 80 – 40 B. creates a unit fraction with 8 – 4 C. correct D. combines both scales		

15. The bottom of a clothes hanger and its side form an angle as shown below.

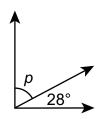


Using your protractor, what is the measure of angle 1 formed by the clothes hanger?

- A. 25°
- B. 35°
- C. 155°
- D. 165°

Item Information		
Alignment	D-M.3.1.1	
Answer Key	A	
Depth of Knowledge	1	
p-value A	52% (correct answer)	
p-value B	27%	
p-value C	13%	
p-value D	8%	
Option Annotations  A. correct B. starts at 30° and counts "up" 5 degrees C. reads obtuse measure instead of acute D. starts at 160° and counts "up" 5 degrees		

**16.** A picture of a right angle is shown below.



Which expression can be used to find the measure, in degrees, of angle p?

- A. 80 + 28
- B. 80 28
- C. 90 + 28
- D. 90 28

Item Information		
Alignment	D-M.3.1.2	
Answer Key	D	
Depth of Knowledge	1	
p-value A	12%	
p-value B	12%	
p-value C	17%	
p-value D	59% (correct answer)	
A. incorrectly identifies a right angle as 80 degrees, and then adds to the B. incorrectly identifies a right angle as 80 degrees C. adds the measurements D. correct		

#### **OPEN-ENDED QUESTION**

17. Gary, Erin, and Brayden are studying populations of different cities.

Gary lives in a city that has a population of one hundred thirty thousand, seventy-eight people.

**A.** Write the number of people who live in Gary's city in standard form.

Erin's city has a population of 104,712 people.

**B.** Write the population of Erin's city in expanded form.

Go to the next page to finish question 17.

GO ON

17. Continued. Please refer to the previous page for task explanation.

Brayden compares the population of city C to the population of city D. When rounded to the nearest thousand, the populations each round to 145,000 people. When rounded to the nearest ten-thousand, the populations round to two different numbers.

**C.** What could be the population of city C and the population of city D? Explain why the numbers you chose fit this situation.

city C: \_\_\_\_\_\_people

city D: \_\_\_\_\_ people

After you have checked your work, close your answer booklet and test booklet so your teacher will know you are finished.



#### **Item-Specific Scoring Guideline**

#### **#17 Item Information**

Alignment	A-T.1	Depth of Knowledge	3	Mean Score	1.34
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#### Assessment Anchor this item will be reported under:

M04.A-T.1 — Generalize place-value understanding for multi-digit whole numbers.

#### **Specific Anchor Descriptor addressed by this item:**

M04.A-T.1.1 — Apply place-value and numeration concepts to compare, find equivalencies, and round.

#### **Scoring Guide**

Score	In this item, the student
4	Demonstrates a thorough understanding of how to generalize place-value understanding for multi-digit whole numbers by correctly solving problems and clearly explaining procedures.
3	Demonstrates a general understanding of how to generalize place-value understanding for multi- digit whole numbers by correctly solving problems and clearly explaining procedures with only minor errors or omissions.
2	Demonstrates a partial understanding of how to generalize place-value understanding for multi- digit whole numbers by correctly performing a significant portion of the required task.
1	Demonstrates minimal understanding of how to generalize place-value understanding for multi-digit whole numbers.
0	The response has no correct answer and insufficient evidence to demonstrate any understanding of the mathematical concepts and procedures as required by the task. Response may show only information copied from the question.

#### **Top-Scoring Student Response and Training Notes**

Score	Description	
4	Student earns 4 points.	
3	Student earns 3.0–3.5 points.	
2	Student earns 2.0–2.5 points.	
1	Student earns 0.5–1.5 points.  OR  Student demonstrates minimal understanding of properties of how to generalize place-value understanding for multi-digit whole numbers.	
0	Response is incorrect or contains some correct work that is irrelevant to the skill or concept being measured.	

#### **Top-Scoring Response**

#### Part A (1 point):

1 point for correct answer

What?	Why?
130,078	

#### Part B (1 point):

1 point for correct answer

What?	Why?
100,000 + 4,000 + 700 + 10 + 2 OR equivalent	

#### Part C (2 points):

- 1 point for correct answer
- 1 point for correct and complete explanation

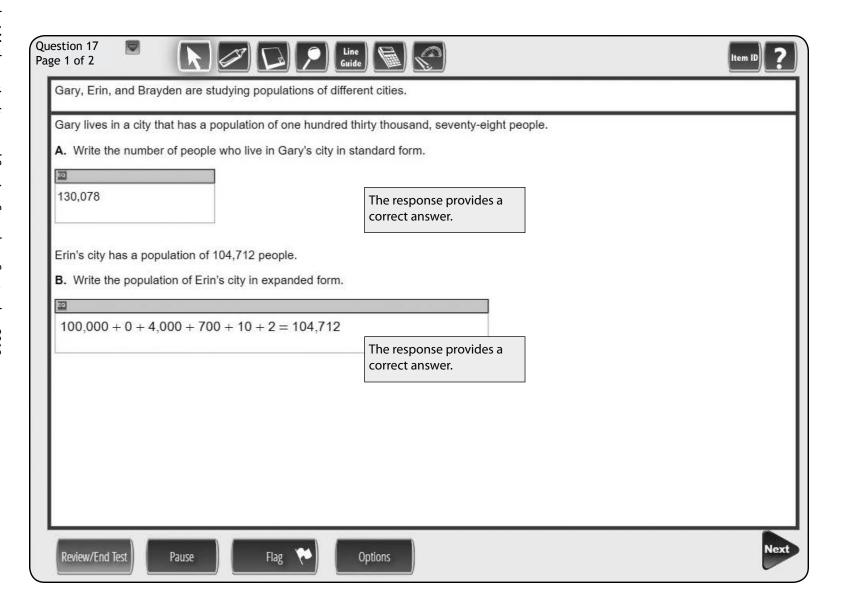
What?	Why?
What?  Answers may vary. One answer should be in the interval 144,500 through 144,999. The other answer should be in the interval 145,000 through 145,499.  Sample Response: city C: 144,750 city D: 145,263	Why?  Sample Explanation:  When rounding 144,750 to the thousands place, it is closer to 145,000 because the 7 in the hundreds place is higher than 5. When rounding 145,263 to the thousands place, it rounds down to 145,000 also because the 2 in the hundreds place is 4 or less. When rounding to the ten thousands place, 144,750 rounds to 140,000 because the number in the thousands place
	is 4 or less so it rounds down. When rounding 145,263 to the ten thousands place it rounds up to 150,000 because the thousands place is a 5 or higher. Depending on the digit that is being rounded to, the numbers may be different.  OR Equivalent

# STUDENT RESPONSE

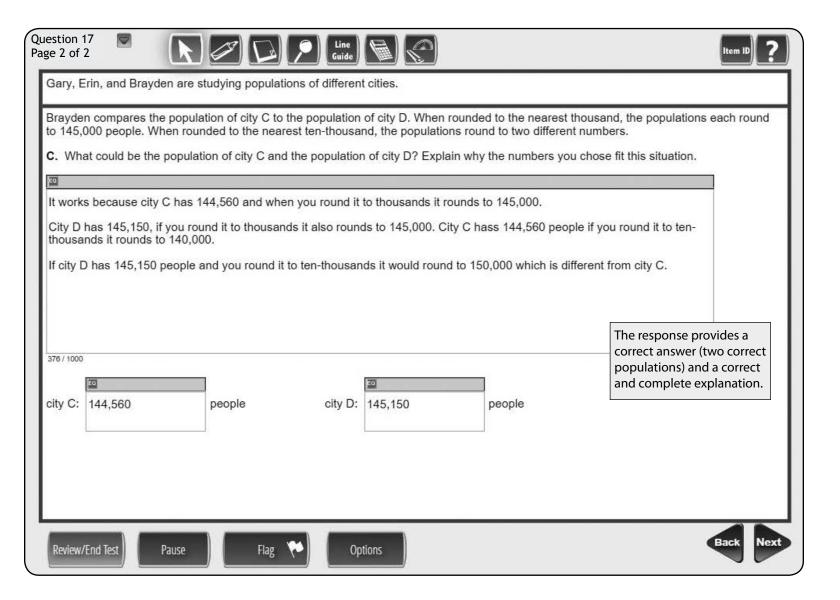
**PARTS A AND B** 

**Response Score: 4 points** 





**PART C** 



#### STUDENT RESPONSE

**Response Score: 3 points** 

17. Gary, Erin, and Brayden are studying populations of different cities.

Gary lives in a city that has a population of one hundred thirty thousand, seventy-eight people.

**A.** Write the number of people who live in Gary's city in standard form.

130,078

The response provides a correct answer.

Erin's city has a population of 104,712 people.

**B.** Write the population of Erin's city in expanded form.

one hundred thousand four seven hundred twelve

The response provides an incorrect answer.

Go to the next page to finish question 17.

GO ON

17. Continued. Please refer to the previous page for task explanation.

Brayden compares the population of city C to the population of city D. When rounded to the nearest thousand, the populations each round to 145,000 people. When rounded to the nearest ten-thousand, the populations round to two different numbers.

**C.** What could be the population of city C and the population of city D? Explain why the numbers you chose fit this situation.

I chose those numbers because if you round 144,960 to the nearest thousand you get 145,000 and if you round 145,370 to the nearest thousand you get 145,000 and it said that they have to have the same rounded number at the end. Then, if you round 144,960 to the nearest ten-thousand you would get 140,000 and if you rounded the number 145,370 to the nearest ten thousand you would get 150,000 and in the problem it says that you have to have have a different rounded numbers in the end. That is how I know why this situation is able to fit into this problem.

The response provides a correct answer (two correct populations) and a correct and complete explanation.

After you have checked your work, close your answer booklet and test booklet so your teacher will know you are finished.

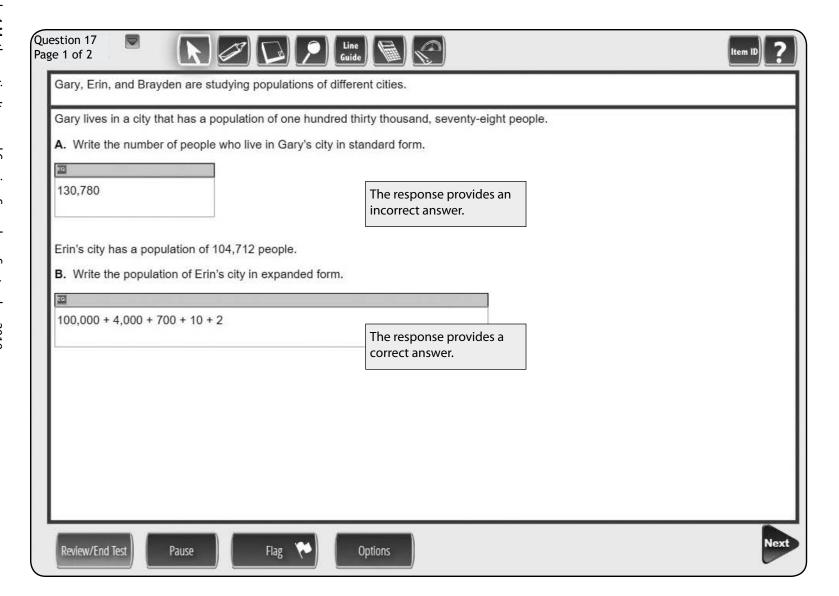


# STUDENT RESPONSE

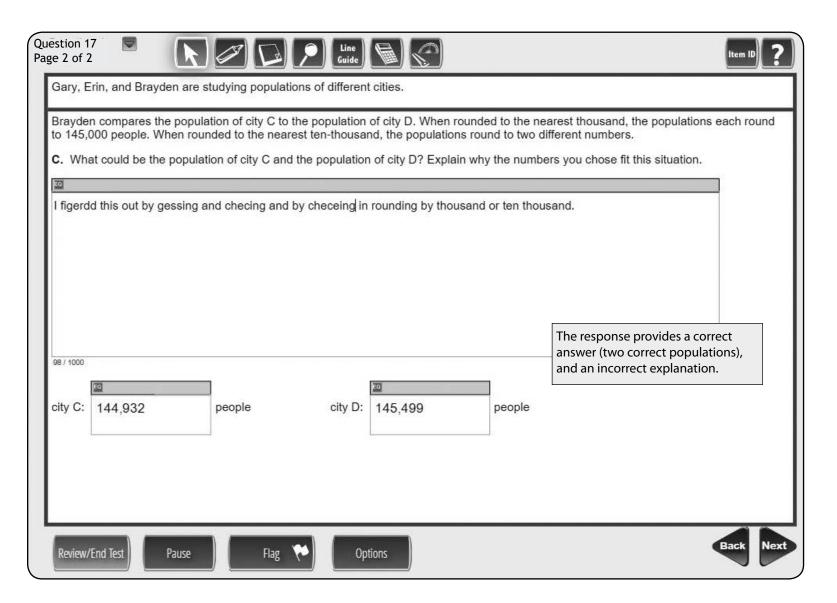
**PARTS A AND B** 

**Response Score: 2 points** 





**PART C** 





#### STUDENT RESPONSE

**Response Score: 1 point** 

17. Gary, Erin, and Brayden are studying populations of different cities.

Gary lives in a city that has a population of one hundred thirty thousand, seventy-eight people.

**A.** Write the number of people who live in Gary's city in standard form.

130,780

The response provides an incorrect answer.

Erin's city has a population of 104,712 people.

B. Write the population of Erin's city in expanded form.

The response provides a correct answer.

Go to the next page to finish question 17.

GO ON

17. Continued. Please refer to the previous page for task explanation.

Brayden compares the population of city C to the population of city D. When rounded to the nearest thousand, the populations each round to 145,000 people. When rounded to the nearest ten-thousand, the populations round to two different numbers.

**C.** What could be the population of city C and the population of city D? Explain why the numbers you chose fit this situation.

They fit this situation because they both round to 145000 when rounding by thousands and different this when rounded by the ten-thousand.

city C: 145,38) people

city D: 145, 396 people

The response provides an incorrect answer (There is no credit for one correct population.) and an incorrect explanation.

After you have checked your work, close your answer booklet and test booklet so your teacher will know you are finished.

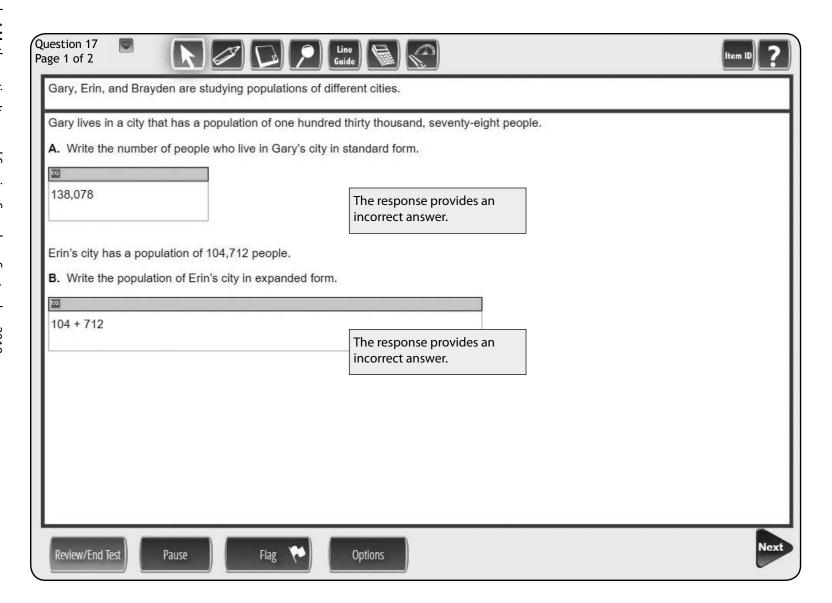


# STUDENT RESPONSE

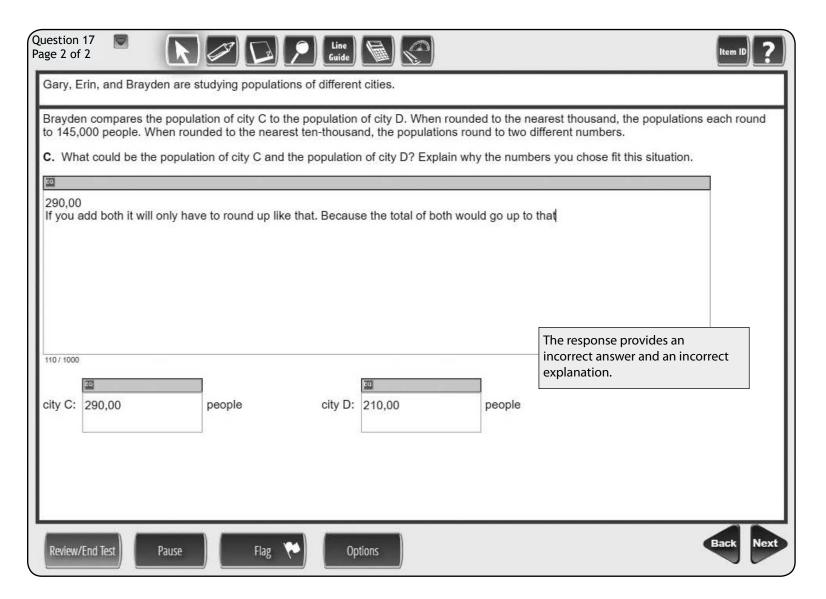
**PARTS A AND B** 

**Response Score: 0 points** 





**PART C** 





#### **MATHEMATICS—SUMMARY DATA**

#### **MULTIPLE-CHOICE**

Sample Number	Alignment	Answer Key	Depth of Knowledge	p-values A	<i>p</i> -values B	p-values C	<i>p</i> -values D
1	A-F.3.1.2	С	1	15%	5%	75%	5%
2	A-T.2 A-T.1.1.4	С	2	18%	12%	37%	33%
3	A-F.1.1.2	А	2	42%	16%	21%	21%
4	A-F.2.1.4	А	2	50%	18%	7%	25%
5	A-F.2.1.7	А	2	52%	15%	22%	11%
6	A-F.3.1.1 A-F.3.1.2	D	1	29%	10%	9%	52%
7	B-O.1.1	А	1	59%	23%	11%	7%
8	B-O.2.1 D-M.2.1	В	2	6%	42%	23%	29%
9	B-O.2.1.1	А	2	72%	9%	6%	13%
10	B-O.3	D	2	28%	21%	16%	35%
11	B-O.3.1.2 B-O.3.1.3	В	2	11%	61%	19%	9%
12	D-M.1.1.1	D	1	24%	8%	6%	62%
13	D-M.1.1.4 D-M.1.1.2	А	1	41%	19%	21%	19%
14	D-M.2.1.2	С	2	10%	11%	55%	24%
15	D-M.3.1.1	А	1	52%	27%	13%	8%
16	D-M.3.1.2	D	1	12%	12%	17%	59%

#### **OPEN-ENDED**

Sample Number	Alignment	Points	Depth of Knowledge	Mean Score
17	A-T.1	4	3	1.34