Pennsylvania PSSA 2016 Grade 7 Math

Reference Materials
Page 2

Exam & Answer Key Materials
Pages 3 - 36

Grade 7 Formula Sheet

Formulas that you may need to work questions on this test are found below. You may refer back to this page at any time during the mathematics test. You may use calculator π or the number 3.14.

2016 Grade 7

Simple Interest

$$I = Prt$$

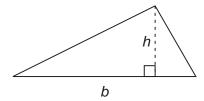
Circle



$$C = 2\pi r$$

$$A = \pi r^2$$

Triangle



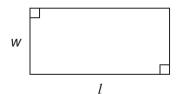
 $A = \frac{1}{2} bh$

Square



$$A = s^2$$

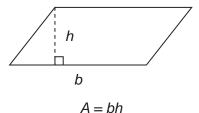
Rectangle



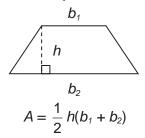
$$A = l w$$

$$P = 2l + 2w$$

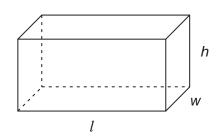
Parallelogram



Trapezoid

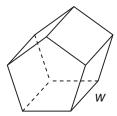


Rectangular Prism



$$V = lwh$$
 $SA = 2lw + 2lh + 2wh$

Polygonal Prism

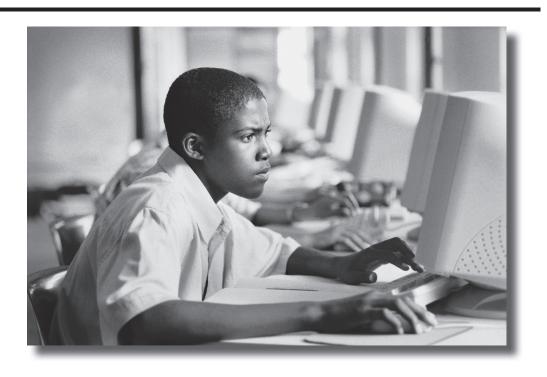


V = Bw, where B = area of the base SA = Pw + 2B, where P = perimeter of base



The Pennsylvania System of School Assessment

Mathematics Item and Scoring Sampler



2016-2017 **Grade 7**

Pennsylvania Department of Education Bureau of Curriculum, Assessment and Instruction—September 2016

MATHEMATICS TEST DIRECTIONS

On the following pages are the mathematics questions.

 You may <u>not</u> use a calculator for question 1. You may use a calculator for all other questions on this test.

Directions for Multiple-Choice Questions:

Some questions will ask you to select an answer from among four choices.

For the multiple-choice questions:

- First solve the problem on scratch paper.
- Choose the correct answer and record your choice in the answer booklet.
- If none of the choices matches your answer, go back and check your work for possible errors.
- Only one of the answers provided is the correct response.

Directions for Open-Ended Questions:

Some questions will require you to write your response.

For the open-ended questions:

- These questions have more than one part. Be sure to read the directions carefully.
- You cannot receive the highest score for an open-ended question without completing
 all tasks in the question. For example, if the question asks you to show your work or
 explain your reasoning, be sure to show your work or explain your reasoning in the
 space provided.
- If the question does **not** ask you to show your work or explain your reasoning, you
 may use the space provided, but only those parts of your response that the question
 specifically asks for will be scored.
- Write your response in the appropriate location within the response box in the
 answer booklet. Some answers may require graphing, plotting, labeling, drawing, or
 shading. If you use scratch paper, be sure to transfer your final response and any
 needed work or reasoning to the answer booklet.

INFORMATION ABOUT MATHEMATICS

General Description of Scoring Guidelines for Mathematics Open-Ended Questions

4 – The response demonstrates a *thorough* understanding of the mathematical concepts and procedures required by the task.

The response provides correct answer(s) with clear and complete mathematical procedures shown and a correct explanation, as required by the task. Response may contain a minor "blemish" or omission in work or explanation that does not detract from demonstrating a *thorough* understanding.

3 – The response demonstrates a *general* understanding of the mathematical concepts and procedures required by the task.

The response and explanation (as required by the task) are mostly complete and correct. The response may have minor errors or omissions that do not detract from demonstrating a *general* understanding.

2 – The response demonstrates a *partial* understanding of the mathematical concepts and procedures required by the task.

The response is somewhat correct with *partial* understanding of the required mathematical concepts and/or procedures demonstrated and/or explained. The response may contain some work that is incomplete or unclear.

- 1 The response demonstrates a *minimal* understanding of the mathematical concepts and procedures required by the task.
- 0 The response has no correct answer and *insufficient* evidence to demonstrate any understanding of the mathematical concepts and procedures required by the task for that grade level.

Response may show only information copied from the question.

Special Categories within zero reported separately:

BLK (blank)......Blank, entirely erased, or written refusal to respond OT.....Off task

LOEResponse in a language other than English

ILIllegible

Question 1 in this sampler is to be solved without the use of a calculator.

MULTIPLE-CHOICE ITEMS

- **1.** Subtract: -10 21
 - A. -31
 - B. -11
 - C. 11
 - D. 31

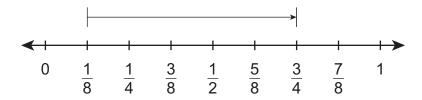
	Item Info	rmation		Option Annotations
	Alignme	nt A-N.1	.1.1	A. correct
	Answer K	ey A]B. 10 + −21]C. −10 + 21
Depth of	Depth of Knowledge 1			D. 10 + 21
	p-val	ues		
Α	A B C D		D	
57%	11%	23% 9%		
	,			

A calculator is permitted for use in solving questions 2–17 in this sampler.

- 2. Laura has a board that measures $6\frac{11}{12}$ feet in length. She will cut the board into pieces that are each $\frac{11}{12}$ foot long. How many full pieces can Laura cut from her board, and how much of her board will be remaining?
 - A. Laura can cut the board into 6 pieces with nothing remaining.
 - B. Laura can cut the board into 6 pieces with $\frac{11}{12}$ foot remaining.
 - C. Laura can cut the board into 7 pieces with $\frac{1}{12}$ foot remaining.
 - D. Laura can cut the board into 7 pieces with $\frac{1}{2}$ foot remaining.

Item Information				Option Annotations
	Alignme	nt A-N.1	1.1	A. thinks 6 11/12 = 66/12
	Answer Key D			B. removes the whole number part from the length of the board C. converts 6 11/12 to an improper fraction by doing 6 × 11 + 12 D. correct
Depth of	Depth of Knowledge 2			
				4
	p-values			
Α	A B C D		D	
16%	19%	22%	43%	

3. The gas tank in Phil's car was $\frac{1}{8}$ full. He put more gasoline in the car's gas tank. The number line below shows how full the car's gas tank was before and after Phil put in more gasoline.



Which equation represents the change in the amount of gasoline in the car's tank?

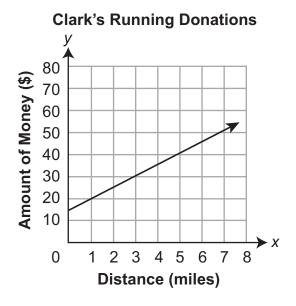
- A. $\frac{1}{8} + \frac{2}{4} = \frac{3}{4}$
- B. $\frac{1}{8} + \frac{5}{8} = \frac{3}{4}$
- C. $\frac{1}{8} + \frac{3}{4} = \frac{7}{8}$
- D. $\frac{1}{8} + \frac{3}{4} = \frac{4}{12}$

Item Information				Option Annotations
	Alignmer	A-N.1 A-N.1		A. adds the numerators and keeps the smaller denominator B. correct
	Answer Key B			C. adds the starting and ending fractions D. adds the starting and ending fractions by adding their numerators and denominators
Depth of	Depth of Knowledge 2			
	<i>p</i> -values			
Α	В	С	D	
12%	66%	16%	6%	

- **4.** For a science experiment, Annie removes a cold liquid from a refrigerator and measures its temperature every $\frac{1}{2}$ minute. Annie finds that the temperature increases by $1\frac{3}{4}$ degrees Fahrenheit (°F) between each measurement for three minutes. What is the rate per minute of the temperature increase?
 - A. $\frac{7}{8}$ °F per minute
 - B. $1\frac{1}{4}$ °F per minute
 - C. $2\frac{1}{4}$ °F per minute
 - D. $3\frac{1}{2}$ °F per minute

	Item Info	rmation		Option Annotations
	Alignme	nt A-R.1	.1.1	A. divides the given rate by 2
	Answer Key D			B. subtracts 1/2 from the given rate C. adds 1/2 to the given rate D. correct
Depth of	Depth of Knowledge 2			
	p-values			
Α	В	С	D	
29%	15%	16%	40%	

Clark and Phil are each running to raise money. The amount of money (y), in dollars, they each raise is based on the distance (x), in miles, they each run. Clark has an initial donation that he has received regardless of how many miles he runs. The graphs shown below model the amount of money each will raise based on the distance they each run.





What is the unit rate for the person for whom the amount of money and the number of miles are proportionally related?

- A. \$5.00 per mile
- B. \$7.50 per mile
- C. \$15.00 per mile
- D. \$30.00 per mile

	Item Info	rmation		Option Annotations
	Alignment A-R.1.1.2 A-R.1.1.3			A. chooses Clark's unit rate but does not realize Clark's quantities are not proportionally related
	Answer Key			B. correct C. picks Clark's <i>y</i> -intercept
Depth of	Depth of Knowledge			D. picks the first value with integer coordinates for Phil
	p-values			1
Α	В	С	D	
23%	54%	16%	7%	
			•	1

6. Joe has a picture that measures 8 centimeters by 12 centimeters. He creates four enlargements of the picture. The table below shows the width and the length of each enlargement.

Joe's Picture Enlargements

Width (cm)	Length (cm)
10	15
12	18
20	30
25	37.5

What is the constant of proportionality between the width and the length of the pictures?

- A. 0.5
- B. 1.2
- C. 1.5
- D. 2.5

Item Information				Option Annotations
	Alignme	nt A-R.1	.1.3	A. solves (15 – 10)/10
	Answer Key C			B. uses ratio of first two values in either column (12/10 or 18/15) C. correct
Depth of	Depth of Knowledge 1			D. uses ratio of first and last values in either column (25/10
				or 37.5/15)
	p-values			
Α	A B C D		D	
15%	12%	54%	19%	
			•	

- 7. Jaya is painting her room. She mixes 2 pints of blue paint with 5 pints of red paint to get her desired color. Which equation can be used to find the number of pints of blue paint (x) Jaya should mix with 18 pints of red paint?
 - A. $\frac{2}{x} = \frac{18}{5}$
 - B. $\frac{2}{5} = \frac{x}{18}$
 - C. $\frac{2}{18} = \frac{5}{x}$
 - D. $\frac{x}{18} = \frac{5}{2}$

Item Information				Option Annotations
	Alignme	nt A-R.1	.1.4	A. sets up the equation 2:x equals to 18:5 instead of 5:18
	Answer Key B			B. correct C. reverses placement of 18 and x
Depth of	Depth of Knowledge 2			D. sets up the equation <i>x</i> :18 equals to 5:2 instead of 2:5
	p-values			
Α	В	С	D	
16%	63%	12%	9%	
			'	

- **8.** Ernesto made a graph of the distance (*y*), in miles, he can ride a bicycle in *x* hours. Ernesto can ride 5.5 miles in 0.5 hour. Which point on the graph represents Ernesto's rate of travel, in miles per hour?
 - A. (0, 5.5)
 - B. (0, 11)
 - C. (1, 5.5)
 - D. (1, 11)

	Item Infor	mation		Option Annotations
				A. thinks starting at 5.5 mph B. uses wrong <i>x</i> -value
	Answer Ke	ey D		C. thinks 5.5 mph D. correct
Depth of	Depth of Knowledge 1			
	p-values			
Α	АВ		D	
26%	8%	23%	43%	
	'			

- 9. The ratio of the number of students in the chess club to the number of students on the math team is 1:3. The ratio of the number of students on the math team to the number of students on the quiz bowl team is 1:2. There are 4 students in the chess club. How many students are on the quiz bowl team?
 - A. 7
 - B. 9
 - C. 12
 - D. 24

Item Information				Option Annotations
	Alignme	nt A-R.1	.1.6	A. adds the ratio difference to the chess club total $(4 + 2 + 1)$
Answer Key D			B. adds the larger number to the chess club total (4 + 3 + 2) C. finds the math team total	
Depth of	Depth of Knowledge 2			D. correct
	p-values			
Α	В	С	D	
17%	19%	23%	41%	
	<u>'</u>			

- **10.** Arnie buys $2\frac{2}{5}$ pounds of red grapes for \$1.95 per pound. He buys $2\frac{2}{5}$ pounds of green grapes for \$2.20 per pound. Which expression can be used to determine the total cost, in dollars, of the grapes Arnie buys?
 - A. 2.4(1.95 + 2.20)
 - B. 2.4 1.95 2.20
 - C. (2.4 + 2.4)(1.95 + 2.20)
 - D. $(2.4 \cdot 2.4) + (1.95 \cdot 2.20)$

	Item Infor	mation		Option Annotations
	Alignmer	nt B-E.2	.1.1	A. correct
,	Answer Key A			B. multiplies all C. multiplies total weight by sum of rates
Depth of	Depth of Knowledge 2			D. adds product of weights and product of rates
	p-values			
Α	ВС		D	
52%	11%	22%	15%	

11. An author receives \$0.75 for each hardcover book or paperback book that is sold. There were *x* hardcover books and 42,000 paperback books sold of her most recent book. The author received a total of \$60,000 for the book sales. The equation below can be used to determine the number of hardcover books that were sold.

$$0.75(x + 42,000) = 60,000$$

How many hardcover books were sold?

- A. 18,000
- B. 24,000
- C. 28,500
- D. 38,000

	Item Info	rmation		Option Annotations
	Alignme	nt B-E.2	.2.1	A. "distributes" to 60,000
	Answer K	ey D		B. does not distribute to 42,000 C. does not distribute to <i>x</i>
Depth of	Depth of Knowledge 1			D. correct
	p-values			-
Α	A B C D		D	
24%	16%	15%	45%	

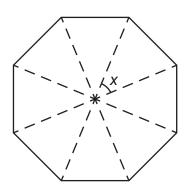
- 12. Tasha sells gift boxes and cookies at her bakery.
 - Gift boxes sell for \$26.00 each.
 - Cookies sell for \$1.50 each.
 - Tasha would like her total sales to be at least \$50.00 from the sale of one gift box and some cookies.

Which inequality describes all the numbers of cookies (x) that Tasha needs to sell?

- A. $x \ge 2$
- B. $x \ge 8$
- C. $x \ge 16$
- D. $x \ge 24$

Item Information				Option Annotations
	Alignment B-E.2.2.2			A. solves $(26.00 + 1.50)x \ge 50.00$; rounds up
	Answer Key C			B. solves $x \ge (50.00/1.50) - 26.00$; rounds up C. correct D. solves $50.00 - 26.00$
Depth of	Depth of Knowledge 2			
	p-values			
Α	В	С	D	
9%	8%	57%	26%	

13. A stained glass window is in the shape of a regular octagon as shown below.

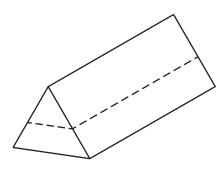


The window is separated into sections by drawing straight, dashed lines that intersect in the center of the octagon. What is the value of x?

- A. 22.5°
- B. 37.5°
- C. 45°
- D. 50°

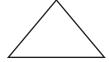
Item Information				Option Annotations
	Alignment C-G.1			A. divides 180 by 8
	Answer Key C			B. thinks a full circle is 300° C. correct
Depth of	Depth of Knowledge 2			D. thinks a full circle is 400°
]
	<i>p</i> -valu	ies		
Α	В	С	D	
25%	11%	55%	9%	

14. Melinda's candy bar is in the shape of a triangular prism. She cuts her candy bar parallel to its bottom. The dotted line in the picture below represents Melinda's cut.

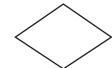


What is the shape of the cross section of Melinda's cut?

A.



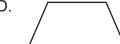
B.



C.

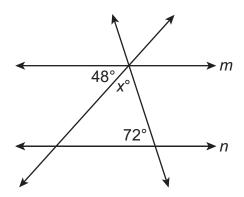


D.



Item Information				Option Annotations
Alignment C-G.1.1.4			.1.4	A. chooses shape of the base (triangle), not the lateral face B. chooses rhombus (prisms have rectangular faces) C. correct D. chooses side face after cut
Answer Key C				
Depth of Knowledge 1				
	p-values			
Α	В	С	D	
21%	3%	47%	29%	

15. Two lines intersect parallel lines m and n as shown below.



What is the value of x?

- A. 24
- B. 48
- C. 60
- D. 66

Item Information				Option Annotations
Alignment C-G.2.1.2			2.1.2	A. solves 72 – 48
Answer Key		еу С		B. thinks value is equal to the adjacent angle C. correct
Depth of	Depth of Knowledge 2			D. solves 90 – 72 = 18 and then adds 18 to 48
	p-valu	ıes		
Α	A B C		D	
19%	26%	46%	9%	

21

- **16.** The diameter of Jacob's circular tabletop is 6 feet. What is the area, in square feet, of Jacob's tabletop?
 - A. 6π
 - B. 9π
 - C. 12π
 - D. 36π

Item Information				Option Annotations
	Alignment C-G.2.2.1			A. finds circumference
	Answer Key			B. correct C. finds circumference using $r = 6$ D. uses the diameter
Depth of	Depth of Knowledge 1			
	p-val	ues		
Α	В	С	D	
21%	37%	19%	23%	

OPEN-ENDED QUESTION

17. The table below shows the number of pencils of each color for all 25 pencils in a box.

Pencils in the Box

Color	Number
red	11
blue	11
green	3

The likelihood of an event occurring may be described as certain, more likely, equally likely, less likely, or impossible.

A single pencil is drawn from the box.

A. Describe the likelihood that the pencil is a yellow pencil. Explain your reasoning.

The pencils have all been placed back in the box.

B. Compare the likelihood of drawing a red pencil to the likelihood of drawing a blue pencil from the box. Explain your reasoning.

Go to the next page to finish question 17.

The original 25 colored pencils have all been placed back in the box and another 11 colored pencils have been added to the box. The new pencils are either red, blue, or green. The likelihood of drawing a green pencil is now **greater** than the

17. Continued. Please refer to the previous page for task explanation.

11 colored pencils have been added to the box. The new pencils are either red, blue, or green. The likelihood of drawing a green pencil is now greater than the likelihood of drawing a red pencil, but less than the likelihood of drawing a blue pencil.
C. How many pencils of each color were added to the box? Explain how you know that your answer is the only possible outcome that meets all of the conditions.

Item-Specific Scoring Guideline

#17 Item Information

Alignment	D-S.3	Depth of Knowledge	3	Mean Score	2.16
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Assessment Anchor this item will be reported under:

M07.D-S.3—Investigate chance processes and develop, use, and evaluate probability models.

Specific Anchor Descriptor addressed by this item:

M07.D-S.3.1—Predict or determine the likelihood of outcomes.

Scoring Guide

Score	In this item, the student
4	Demonstrates a thorough understanding of predicting or determining whether some outcomes are certain, more likely, less likely, equally likely, or impossible by correctly solving problems and clearly explaining procedures.
3	Demonstrates a general understanding of predicting or determining whether some outcomes are certain, more likely, less likely, equally likely, or impossible by correctly solving problems and clearly explaining procedures with only minor errors or omissions.
2	Demonstrates a partial understanding of predicting or determining whether some outcomes are certain, more likely, less likely, equally likely, or impossible by correctly performing a significant portion of the required task.
1	Demonstrates minimal understanding of predicting or determining whether some outcomes are certain, more likely, less likely, equally likely, or impossible.
0	The response has no correct answer and insufficient evidence to demonstrate any understanding of the mathematical concepts and procedures as required by the task. Response may show only information copied from the question.

Top-Scoring Student Response and Training Notes

Score	Description			
4	Student earns 4 points.			
3	Student earns 3.0-3.5 points.			
2	Student earns 2.0–2.5 points.			
1	Student earns 0.5–1.5 points. OR Student demonstrates minimal understanding of predicting or determining whether some outcomes are certain, more likely, less likely, equally likely, or impossible.			
0	Response is incorrect or contains some correct work that is irrelevant to the skill or concept being measured.			

Top-Scoring Response

Part A (1 point):

 $\frac{1}{2}$ point for correct answer

 $\frac{1}{2}$ point for complete explanation

What?	Why?	
impossible	Sample Explanation: There are no yellow pencils in the box, so it is not possible to draw out a yellow pencil.	

Part B (1 point):

 $\frac{1}{2}$ point for correct answer

 $\frac{1}{2}$ point for complete explanation

What?	Why?
equally likely	Sample Explanation: Since there is the same number of each color of pencil, both outcomes are equally likely.

Part C (2 points):

1 point for correct answer

1 point for complete explanation

OR $\frac{1}{2}$ point for correct but incomplete explanation

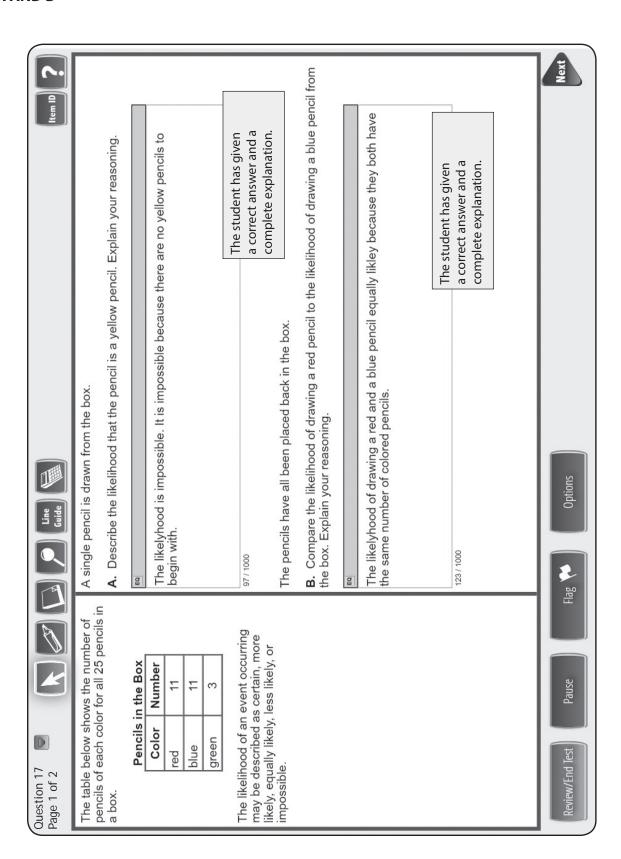
What?	Why?
9 green pencils AND 2 blue pencils	Sample Explanation: Since the likelihood of drawing a green pencil is now greater than the likelihood of drawing a red pencil, there were at least 9 green pencils added $(3 + 9 = 12; 12 > 11)$. Since the likelihood of drawing a green pencil is now less likely than drawing a blue pencil, there were at least 2 blue pencils added $(11 + 2 = 13; 13 > 12)$. Since there were 11 pencils added to the box, this is the only possible answer $(9 + 2 = 11)$.

STUDENT RESPONSE

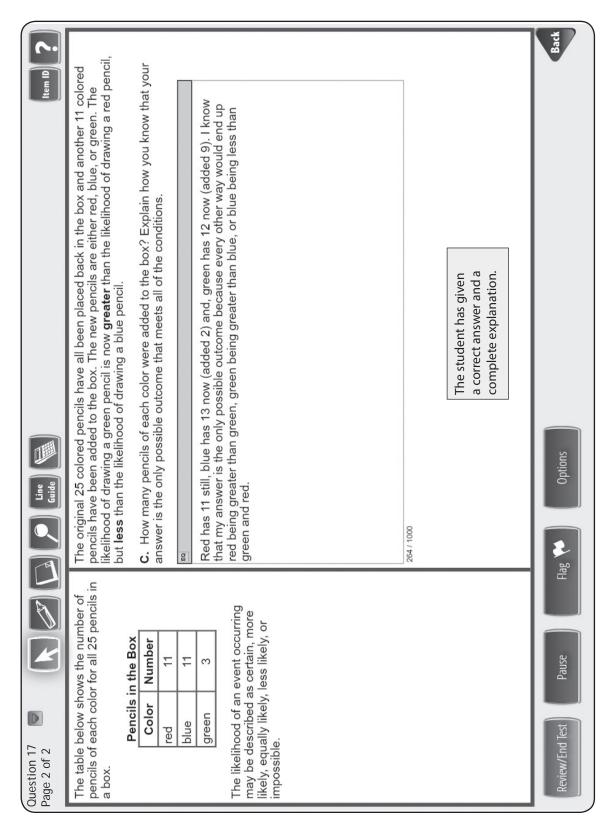
Response Score: 4 points



PARTS A AND B







STUDENT RESPONSE

Response Score: 3 points

17. The table below shows the number of pencils of each color for all 25 pencils in a box.

Pencils in the Box

Color	Number		
red	11		
blue	11		
green	3		

The likelihood of an event occurring may be described as certain, more likely, equally likely, less likely, or impossible.

A single pencil is drawn from the box.

A. Describe the likelihood that the pencil is a yellow pencil. Explain your reasoning.

The student has given a correct answer and a complete explanation.

The pencils have all been placed back in the box.

B. Compare the likelihood of drawing a red pencil to the likelihood of drawing a blue pencil from the box. Explain your reasoning.

The student has given a correct answer and a complete explanation.

Go to the next page to finish question 17.

17. Continued. Please refer to the previous page for task explanation.

The original 25 colored pencils have all been placed back in the box and another 11 colored pencils have been added to the box. The new pencils are either red, blue, or green. The likelihood of drawing a green pencil is now **greater** than the likelihood of drawing a red pencil, but **less** than the likelihood of drawing a blue pencil.

C. How many pencils of each color were added to the box? Explain how you know that your answer is the only possible outcome that meets all of the conditions.

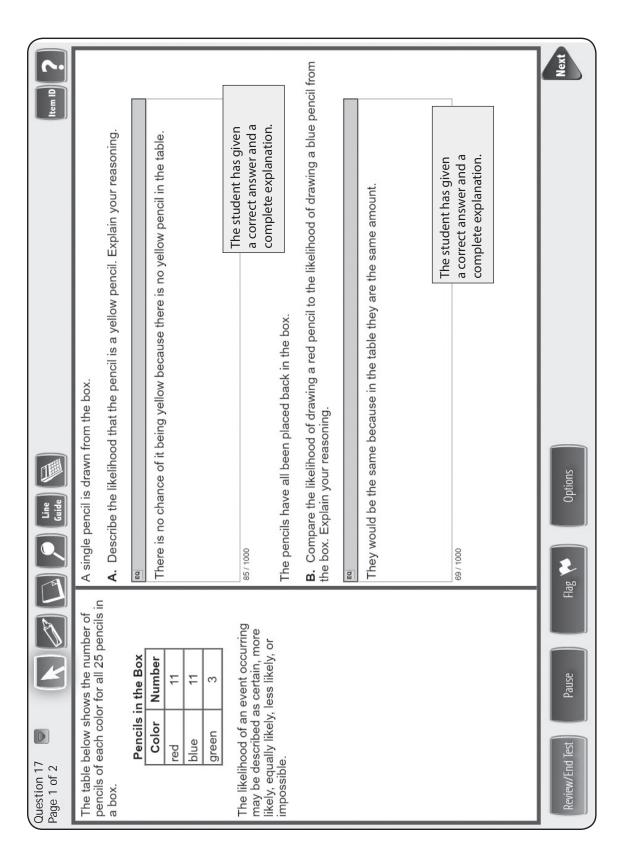
The student has given a correct answer and a correct but incomplete explanation (insufficient explanation of <u>only</u> possible outcome).

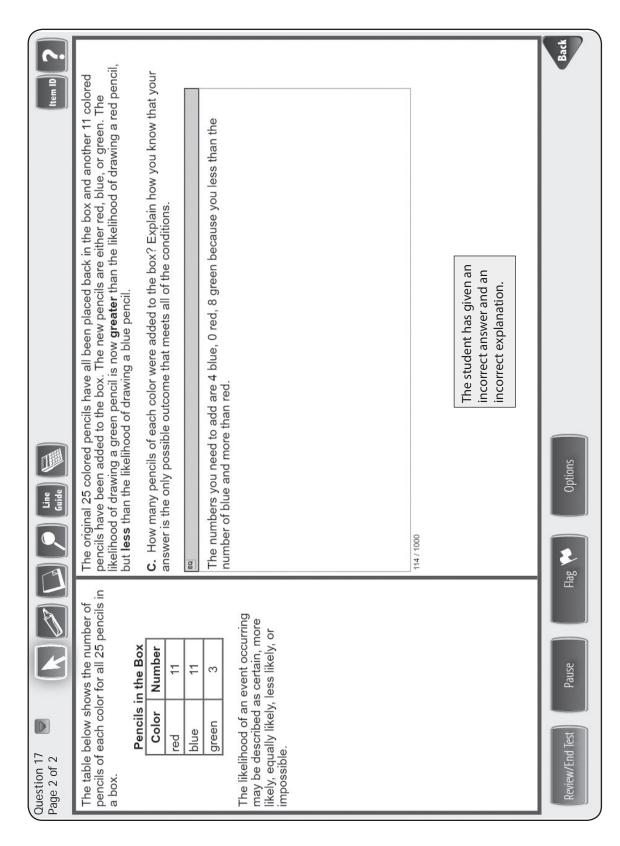
STUDENT RESPONSE

Response Score: 2 points



PARTS A AND B





STUDENT RESPONSE

Response Score: 1 point

17. The table below shows the number of pencils of each color for all 25 pencils in a box.

Pencils in the Box

Color	Number			
red	11			
blue	11			
green	3			

The likelihood of an event occurring may be described as certain, more likely, equally likely, less likely, or impossible.

A single pencil is drawn from the box.

A. Describe the likelihood that the pencil is a yellow pencil. Explain your reasoning.

it is less likely that you will draw a yellow pencil because there isn't any yellow pencil's

The student has given an incorrect answer and a complete explanation.

The pencils have all been placed back in the box.

B. Compare the likelihood of drawing a red pencil to the likelihood of drawing a blue pencil from the box. Explain your reasoning.

It is posibul that you will draw a red & blue pencil because there are more red and blue pencil's

The student has given an incorrect answer and an incorrect explanation.

Go to the next page to finish question 17.

17. Continued. Please refer to the previous page for task explanation.

The original 25 colored pencils have all been placed back in the box and another 11 colored pencils have been added to the box. The new pencils are either red, blue, or green. The likelihood of drawing a green pencil is now **greater** than the likelihood of drawing a red pencil, but **less** than the likelihood of drawing a blue pencil.

C. How many pencils of each color were added to the box? Explain how you know that your answer is the only possible outcome that meets all of the conditions.

there are 50 of each pencil because if you add 11+11+3=25+ 25 = 50

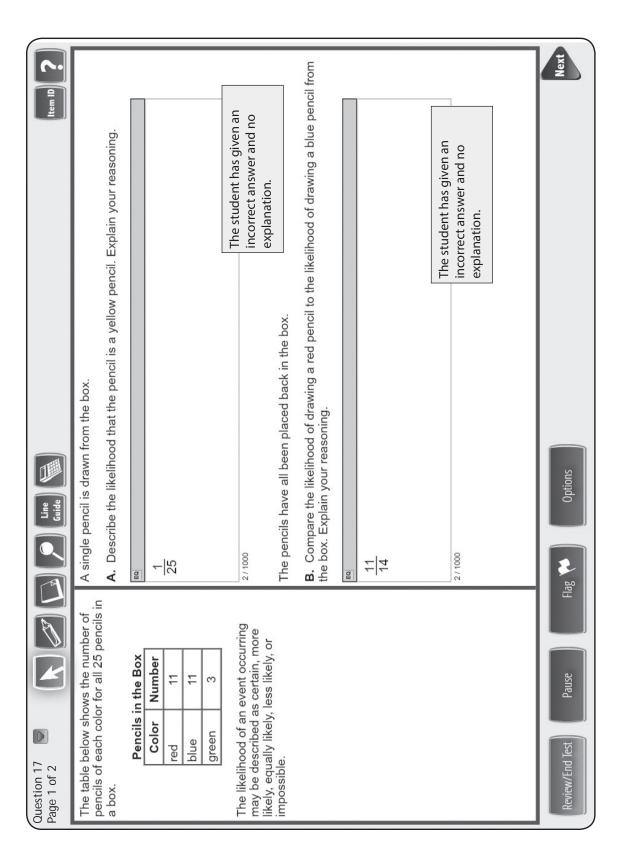
The student has given an incorrect answer and an incorrect explanation.

STUDENT RESPONSE

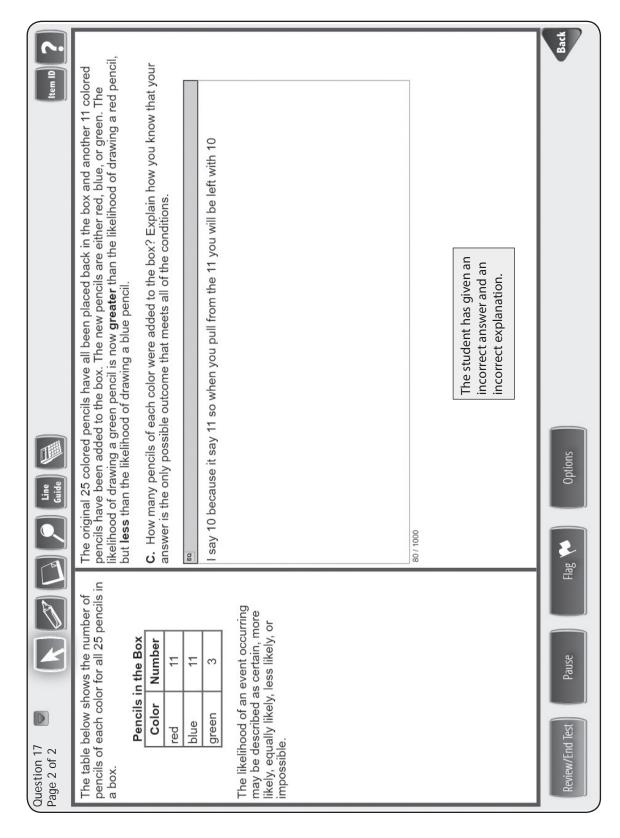
Response Score: 0 points



PARTS A AND B







MATHEMATICS—SUMMARY DATA

MULTIPLE-CHOICE

Sample			Depth of Knowledge	p-values			
Number	Alignment	Answer Key		Α	В	С	D
1	A-N.1.1.1	А	1	57%	11%	23%	9%
2	A-N.1.1	D	2	16%	19%	22%	43%
3	A-N.1.1.2 A-N.1.1.1	В	2	12%	66%	16%	6%
4	A-R.1.1.1	D	2	29%	15%	16%	40%
5	A-R.1.1.2 A-R.1.1.3	В	2	23%	54%	16%	7%
6	A-R.1.1.3	С	1	15%	12%	54%	19%
7	A-R.1.1.4	В	2	16%	63%	12%	9%
8	A-R.1.1.5 A-R.1.1.1	D	1	26%	8%	23%	43%
9	A-R.1.1.6	D	2	17%	19%	23%	41%
10	B-E.2.1.1	Α	2	52%	11%	22%	15%
11	B-E.2.2.1	D	1	24%	16%	15%	45%
12	B-E.2.2.2	С	2	9%	8%	57%	26%
13	C-G.1	С	2	25%	11%	55%	9%
14	C-G.1.1.4	С	1	21%	3%	47%	29%
15	C-G.2.1.2	С	2	19%	26%	46%	9%
16	C-G.2.2.1	В	1	21%	37%	19%	23%

OPEN-ENDED

Sample Number	Alignment	Points	Depth of Knowledge	Mean Score
17	D-S.3	4	3	2.16