

Assignment # 2

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<https://colab.research.google.com/drive/19ihokHezJHFtyzJBuCwyjYTVCTiDJP3x?usp=sharing>

Assignment2

Tuesday, February 7, 2023 6:30 AM

Test = Gold Standard Labels

Predicted

0 = non - fraudulent emails

1 = Fraudulent emails

	F	NF	Total
F	22	4	26
NF	4	10	14

"important"

	F	NF
F	true +	false -
NF	false +	true -

$$\text{Accuracy} = \frac{(TP + TN)}{(TP + FP + FN + TN)}$$

$$= \frac{(22 + 10)}{40} = \frac{32}{40} = 0.80$$

$$\text{Precision} = \frac{TP}{(TP + FP)} = \frac{22}{26} = 0.85$$

$$\text{Sensitivity} = \frac{TP}{(TP + FN)} = \frac{22}{26} = 0.85$$

$$\text{Specificity} = \frac{TN}{(TN + FP)} = \frac{10}{14} = 0.71$$

$$\begin{aligned} \text{F1 measure} &= \frac{2 * (\text{sensitivity} * \text{precision})}{\text{sensitivity} + \text{precision}} \\ &= \frac{2 * (0.85 * 0.85)}{0.85 + 0.85} = \frac{1.445}{1.7} \\ &= 0.85 \end{aligned}$$

```

1 from keras.datasets import mnist

1 import numpy as np
2 import matplotlib.pyplot as plt

1 import matplotlib.image as mpimg
2 import random

1 # a)
2
3 #Load mnist data set and split into training and testing sets
4 (x_train, y_train), (x_test, y_test) = mnist.load_data()
5
6 # Print number of images in each training and testing set
7 # and the image width and height
8 print(x_train.shape, y_train.shape)
9 height = x_train.shape[1]
10 width = x_train.shape[2]
11 print("Image height =", height, "pixels")
12 print("Image width =", width, "pixels")
13
14 print(x_test.shape, y_test.shape)
15 height2 = x_test.shape[1]
16 width2 = x_test.shape[2]
17 print("Image height =", height, "pixels")
18 print("Image width =", width, "pixels")

(60000, 28, 28) (60000,)
Image height = 28 pixels
Image width = 28 pixels
(10000, 28, 28) (10000,)
Image height = 28 pixels
Image width = 28 pixels

1 # b) - First edition: contains the for loop inside of the function
2
3 # Function takes a set of images and its labels as inputs and plots a figure
4 # with 10 subplots for each digit 0-9. Each subplot is labeled with digit in title
5 def plot_digits(images, labels):
6     total = 0
7     digits = [0,1,2,3,4,5,6,7,8,9]

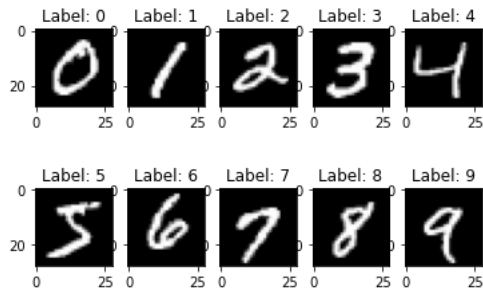
```

```

8
9 for digit in digits:
10     x_train_digit = images[labels==digit,:,:] # can use 0, 27 instead of :,
11     total += x_train_digit.shape[0]
12
13     x_train_single = x_train_digit[0,:,:]
14     plt.subplot(2, 5, digit+1)
15     plt.imshow(x_train_single, cmap='gray')
16     plt.title('Label: ' + str(digit))
17
18 # Verifies that every digit in the set has been accounted for
19 print(total)
20
21 plot_digits(x_train, y_train)

```

60000



```

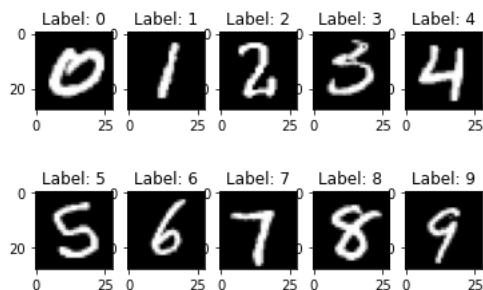
1 # b) - Second Edition: takes a single image and its label to create the subplot
2
3 # Function takes a set of images and its labels as inputs and plots a figure
4 # with 10 subplots for each digit 0-9. Each subplot is labeled with digit in title
5 def plot_digits2(image, label):
6     global counter
7     plt.subplot(2, 5, counter)
8     plt.imshow(image, cmap='gray')
9     plt.title('Label: ' + str(label))
10    counter +=1
11

```

```

1 # c) - For loop calls the function in b Second Edition to create the figure with subplots
2
3 counter = 1
4
5 for i in range(0,10):
6
7     # Each one of these is the group of each individual digit
8     x_train_digit = x_train[y_train==i,:,:]
9
10    # I used random.randint to choose a random index in each group of digits
11    # to select different images to use in the subplot
12    # Every time you run this, the subplots will be built of different images
13    x_train_single = x_train_digit[random.randint(0, 1000),:,:]
14
15    # Call Function to build figure
16    plot_digits2(x_train_single, i)

```



```

1 # d) - Select the 0 and 8 digits from the training and testing sets and rename
2
3
4 # Extracting 0s and 8s from training set and concatenating
5

```

```

6 zeros = x_train[y_train==0,:,:]
7 #zeros_labels = np.full(shape=len(zeros), fill_value=0)
8 zeros_labels = np.zeros(len(zeros)) # Does the same as above line
9
10 eights = x_train[y_train==8,:,:]
11 #eights_labels = np.full(shape=len(eights), fill_value=8)
12 eights_labels = np.ones(len(eights))*8 # Does the same as above line
13
14 x_train_01 = np.concatenate((zeros, eights), axis=0)
15 y_train_01 = np.concatenate((zeros_labels, eights_labels), axis=0)
16
17 print(x_train_01.shape)
18 print(y_train_01.shape)
19
20
21 # Extracting 0s and 8s from testing set and concatenating
22
23 zeros2 = x_test[y_test==0,:,:]
24 #zeros_labels = np.full(shape=len(zeros), fill_value=0)
25 zeros_labels2 = np.zeros(len(zeros2)) # Does the same as above line
26
27 eights2 = x_test[y_test==8,:,:]
28 #eights_labels = np.full(shape=len(eights), fill_value=8)
29 eights_labels2 = np.ones(len(eights2))*8 # Does the same as above line
30
31 x_test_01 = np.concatenate((zeros2, eights2), axis=0)
32 y_test_01 = np.concatenate((zeros_labels2, eights_labels2), axis=0)
33
34 print(x_test_01.shape)
35 print(y_test_01.shape)
36

```

```

(11774, 28, 28)
(11774,)
(1954, 28, 28)
(1954,)

```

```

1 # e)
2
3 # Random indices to create validation set
4 indices = random.sample(range(len(x_train_01)), 500)
5
6 # Creation of validation set from training sets
7 x_valid_01 = x_train_01[indices]
8 y_valid_01 = y_train_01[indices]
9 # Show the length of these validation sets
10 print("Length of x_valid_01 =", len(x_valid_01))
11 print("Length of y_valid_01 =", len(y_valid_01))
12
13 # Show the removal of items in validation sets from training sets
14 print("Original size of x_train_01 =", len(x_train_01))
15 x_train_01 = np.delete(x_train_01, indices, 0)
16 print("Size of x_train_01 after 500 random removed =", len(x_train_01))
17
18 print("Original size of y_train_01 =", len(y_train_01))
19 y_train_01 = np.delete(y_train_01, indices, 0)
20 print("Size of y_train_01 after 500 random removed =", len(y_train_01))
21

```

```

Length of x_valid_01 = 500
Length of y_valid_01 = 500
Original size of x_train_01 = 11774
Size of x_train_01 after 500 random removed = 11274
Original size of y_train_01 = 11774
Size of y_train_01 after 500 random removed = 11274

```

```

1 # f)
2
3 # Show the shapes of the validation sets and the training sets
4 print("Validation Sets =", x_valid_01.shape, y_valid_01.shape)
5 print("Number of images in Validation Set =", x_valid_01.shape[0], "\n")
6 print("Training Sets =", x_train_01.shape, y_train_01.shape)
7 print("Number of images in Training Set =", x_train_01.shape[0], "\n")
8 print("Testing Sets =", x_test_01.shape, y_test_01.shape)
9 print("Number of images in Testing Set =", x_test_01.shape[0], "\n")

```

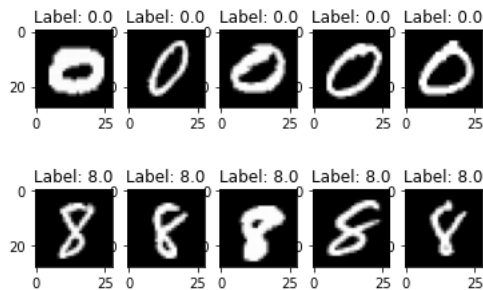
```
Validation Sets = (500, 28, 28) (500,)
Number of images in Validation Set = 500
```

```
Training Sets = (11274, 28, 28) (11274,)
Number of images in Training Set = 11274
```

```
Testing Sets = (1954, 28, 28) (1954,)
Number of images in Testing Set = 1954
```

```
1 # g)
2
3 counter = 1
4
5 x = random.randint(0, 490)
6
7 for i in range(x, x+10):
8 #for i in range(0, 10):
9
10 plot_digits2(x_valid_01[i], y_valid_01[i])
11
12
13 v = x_valid_01[i]
14 y = y_valid_01[i]
15 valid = np.sum(v[12:16, 12:16], axis=1)
16 valid = np.sum(valid, axis=0)/4
17 print(valid)
18
19
```

```
350.5
59.75
100.75
0.0
16.0
745.5
713.5
732.5
598.25
363.5
```



```
1 # h)
2
3 # Convert each image to an average of 4x4 center pixels for training data
4 train_features = np.sum(x_train_01[:,12:16, 12:16], axis=2)
5 train_features = np.sum(train_features, axis=1)/4
6 print(train_features.shape)
7
8 # Convert each image to an average of 4x4 center pixels for validation data
9 validate_features = np.sum(x_valid_01[:,12:16, 12:16], axis=2)
10 validate_features = np.sum(validate_features, axis=1)/4
11 print(validate_features.shape)
12
13 # Convert each image to an average of 4x4 center pixels for testing data
14 testing_features = np.sum(x_test_01[:,12:16, 12:16], axis=2)
15 testing_features = np.sum(testing_features, axis=1)/4
16 print(testing_features.shape)
17
```

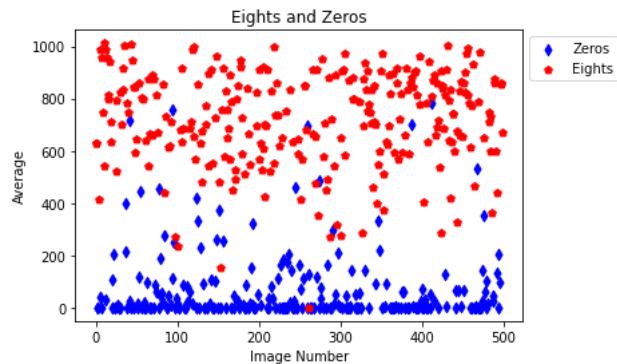
```
(11274,)
(500,)
(1954,)
```

```
1 # i)
2
```

```

3 def plot_eights_and_zeros(y_valid_01, validate_features):
4
5     Zeros = []
6     ZeroImageNumber = []
7     Eights = []
8     EightImageNumber = []
9
10    for i in range(len(validate_features)):
11
12        if (y_valid_01[i] == 0.0):
13            Zeros.append(validate_features[i])
14            ZeroImageNumber.append(i)
15            #plt.scatter(i, validate_features[i], color='blue', marker='d')
16            pass
17        elif (y_valid_01[i] == 8.0):
18            Eights.append(validate_features[i])
19            EightImageNumber.append(i)
20            #plt.scatter(i, validate_features[i], color='red', marker='p')
21            pass
22
23    plt.scatter(ZeroImageNumber, Zeros, color='blue', marker='d')
24    plt.scatter(EightImageNumber, Eights, color='red', marker='p')
25    plt.ylabel('Average')
26    plt.xlabel('Image Number')
27    plt.title('Eights and Zeros')
28    #plt.axis([-1, 5, -1, 5])
29    plt.legend(['Zeros', 'Eights', 'threshold_y', 'threshold_x'], bbox_to_anchor=(1, 1), loc='upper left')
30    #plt.figure(figsize=(2,2))
31    plt.figure(figsize=(4,4))
32    plt.show()
33
34 plot_eights_and_zeros(y_valid_01, validate_features)

```



<Figure size 288x288 with 0 Axes>

```

1 # j)
2
3 # My guess is that choosing a threshold of "y=400" will yield the greatest accuracy.

4
5 # k)
6
7 import numpy as np
8 import matplotlib.pyplot as plt
9 import time
10
11 def classification_accuracy(threshold_x, threshold_y, C1, C2):
12
13     correct = 0
14     incorrect = 0
15     total = len(C1) + len(C2)
16     print(total)
17
18     for i in range(0, len(C1)):
19
20         # Zeros
21         y = C1[i][1]
22
23         if (y >= threshold_y):
24             incorrect += 1
25         elif (y < threshold_y):
26             correct += 1

```

```

23
24 for i in range(0, len(C2)):
25
26     # Eights
27     y2 = C2[i][1]
28
29     if (y2 >= threshold_y):
30         correct += 1
31     elif (y2 < threshold_y):
32         incorrect += 1
33
34
35 return correct, incorrect, total
36
37 def obtain_thresholds():
38
39     while (True):
40         try:
41             var = input("Threshold x must be a number, please enter an integer: ")
42             if (var == 'x'):
43                 testing = False
44                 threshold_x = 'x'
45                 break
46             threshold_x = int(var)
47         except ValueError:
48             print("Threshold must be an integer, please try again.")
49             continue
50         else:
51             break
52
53     while (True):
54         try:
55             var2 = input("Threshold y must be a number, please enter an integer: ")
56             if (var2 == 'x'):
57                 testing = False
58                 threshold_y = 'x'
59                 break
60             threshold_y = int(var2)
61         except ValueError:
62             print("Threshold must be an integer, please try again.")
63             continue
64         else:
65             break
66
67     return threshold_x, threshold_y
68
69 def print_accuracy_results(results):
70
71     print('Correct: ' + str(results[0]))
72     print('Incorrect: ' + str(results[1]))
73     print('Total: ' + str(results[2]))
74     print('Classification Accuracy: ' + str(results[0]/results[2]))
75
76
77 def create_plot(C1, C2, threshold_x, threshold_y):
78
79     zero = []
80     zerolabel = []
81     eight = []
82     eightlabel = []
83
84     for i in range(0, len(C1)):
85
86         zero.append(C1[i][1])
87         zerolabel.append(C1[i][0])
88
89     for i in range(0, len(C2)):
90
91         eight.append(C2[i][1])
92         eightlabel.append(C2[i][0])
93
94
95     plt.scatter(zerolabel, zero, color='blue', marker='d')
96     plt.scatter(eightlabel, eight, color='red', marker='P')
97     plt.hlines(y=threshold_y, xmin=0, xmax=500, linestyle='dashed', color='gray')
98     plt.vlines(x=threshold_x, ymin=0, ymax=1000, linestyle='dashed', color='cyan')
99

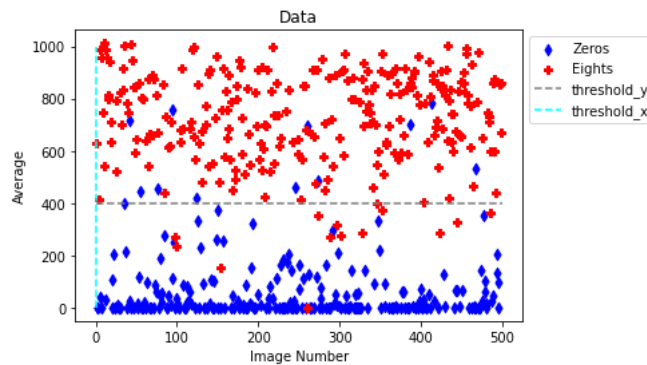
```

```

100 plt.ylabel('Average')
101 plt.xlabel('Image Number')
102 plt.title('Data')
103 #plt.axis([-25, 10000, -25, 1200])
104 plt.legend(['Zeros', 'Eights', 'threshold_y', 'threshold_x'], bbox_to_anchor=(1, 1), loc='upper left')
105 plt.show()
106 print('\n')
107
108 def main(C1, C2):
109
110     thresholds = obtain_thresholds()
111     threshold_x = thresholds[0]
112     threshold_y = thresholds[1]
113
114     if (threshold_x == 'x' or threshold_y == 'x'):
115         return 'x'
116     else:
117         results = classification_accuracy(threshold_x, threshold_y, C1, C2)
118         print_accuracy_results(results)
119         create_plot(C1, C2, threshold_x, threshold_y)
120         return 'Please enter another set of thresholds, or x to quit.'
121
122
123 def build_tuples(y_valid_01, validate_features):
124
125     Zeros = []
126     Eights = []
127
128     for i in range(len(validate_features)):
129
130         if (y_valid_01[i] == 0.0):
131             Zeros.append((i, validate_features[i]))
132             #plt.scatter(i, validate_features[i], color='blue', marker='d')
133             pass
134         elif (y_valid_01[i] == 8.0):
135             Eights.append((i, validate_features[i]))
136             #plt.scatter(i, validate_features[i], color='red', marker='p')
137             pass
138
139     return Zeros, Eights
140
141 do_all = []
142
143 all_sets = [(validate_features, y_valid_01), (testing_features, y_test_01), (train_features, y_train_01)]
144 for a_set in all_sets:
145
146     C1, C2 = build_tuples(a_set[1], a_set[0])
147
148     do_all.append((C1, C2))
149
150
151 for i in range(0, len(do_all)):
152
153     testing = True
154     while (testing == True):
155         # Validate
156         if (i == 0):
157             print("\n", "Validation Set")
158         elif (i == 1):
159             print("\n", "Testing Set")
160         elif (i == 2):
161             print("\n", "Training Set")
162
163         message = main(do_all[i][0], do_all[i][1])
164         if (message == 'x'):
165             testing = False
166             print('User Terminated Program')
167         else:
168             print(message)
169

```

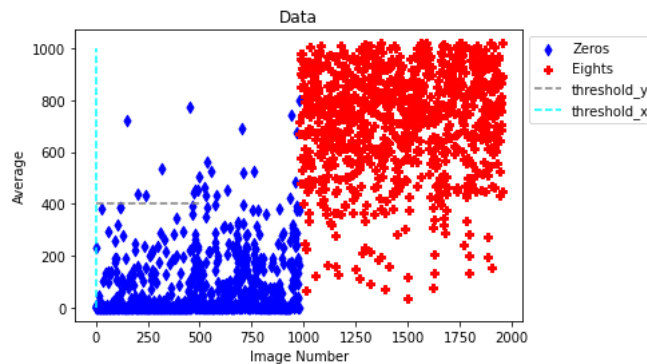

Validation Set
 Threshold x must be a number, please enter an integer: 0
 Threshold y must be a number, please enter an integer: 400
 500
 Correct: 474
 Incorrect: 26
 Total: 500
 Classification Accuracy: 0.948



Please enter another set of thresholds, or x to quit.

Validation Set
 Threshold x must be a number, please enter an integer: x
 Threshold y must be a number, please enter an integer: x
 User Terminated Program

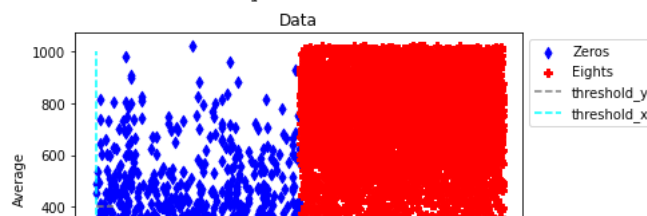
Testing Set
 Threshold x must be a number, please enter an integer: 0
 Threshold y must be a number, please enter an integer: 400
 1954
 Correct: 1869
 Incorrect: 85
 Total: 1954
 Classification Accuracy: 0.9564994882292733

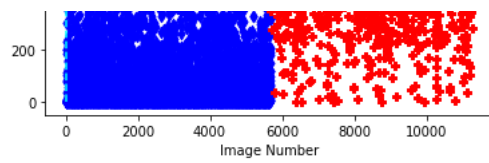


Please enter another set of thresholds, or x to quit.

Testing Set
 Threshold x must be a number, please enter an integer: x
 Threshold y must be a number, please enter an integer: x
 User Terminated Program

Training Set
 Threshold x must be a number, please enter an integer: 0
 Threshold y must be a number, please enter an integer: 400
 11274
 Correct: 10564
 Incorrect: 710
 Total: 11274
 Classification Accuracy: 0.9370232393116906





Please enter another set of thresholds, or x to quit.

Training Set

Threshold x must be a number, please enter an integer: x

Threshold y must be a number, please enter an integer: x

User Terminated Program

✓ 0s completed at 8:00 PM

