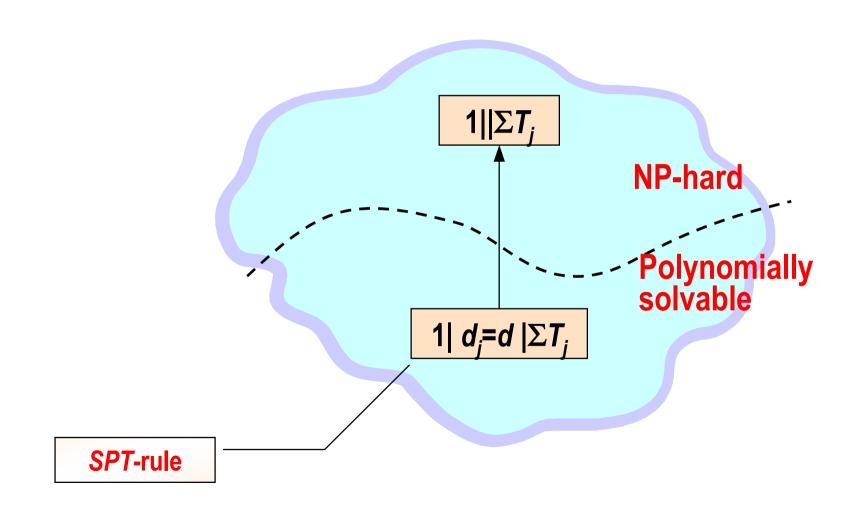
## **Previous lecture:**

- Computational complexity
- Approximation algorithms for 'hard' problems

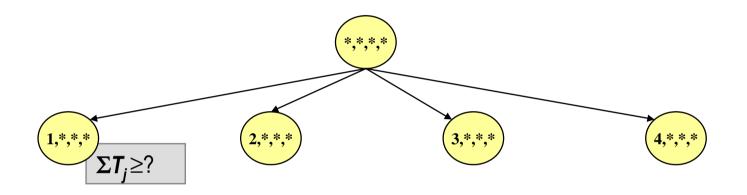
## **This lecture**:

- Exact algorithms: branch and bound

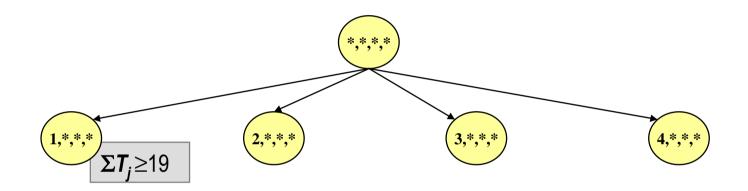
# Problem $1||\Sigma T_j|$ : Complexity



| Jobs                  | 1  | 2  | 3  | 4  |
|-----------------------|----|----|----|----|
| <b>p</b> <sub>j</sub> | 12 | 8  | 15 | 9  |
| d <sub>j</sub>        | 16 | 26 | 25 | 27 |

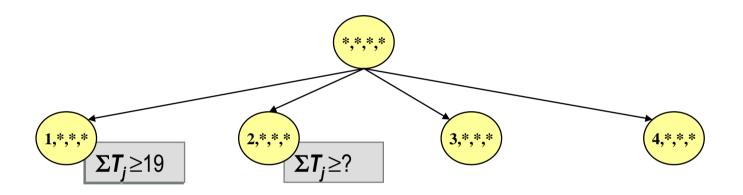


| Jobs           | 1  | 2  | 3  | 4  |
|----------------|----|----|----|----|
| <b>p</b> j     | 12 | 8  | 15 | 9  |
| d <sub>j</sub> | 16 | 26 | 25 | 27 |



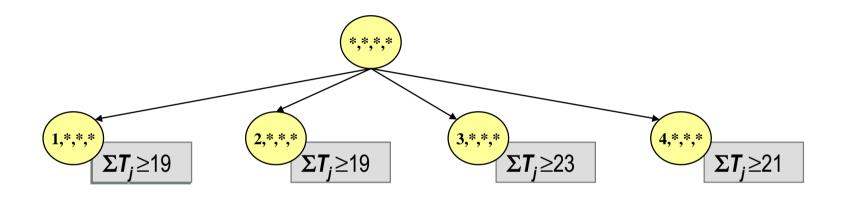


| Jobs                  | 1  | 2  | 3  | 4  |
|-----------------------|----|----|----|----|
| <b>p</b> <sub>j</sub> | 12 | 8  | 15 | 9  |
| d <sub>j</sub>        | 16 | 26 | 25 | 27 |

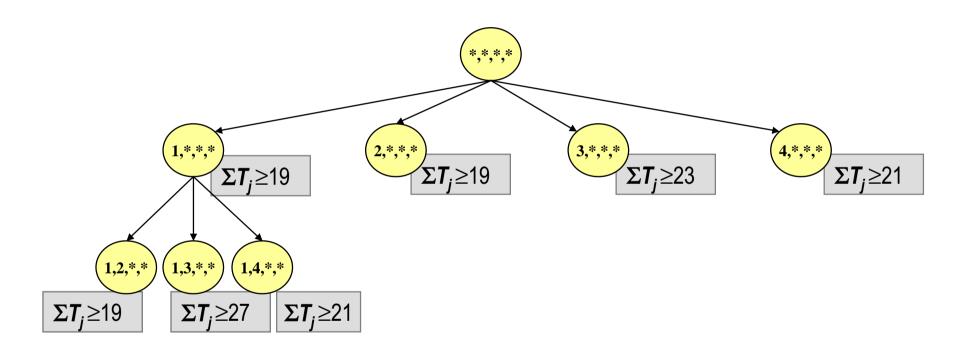




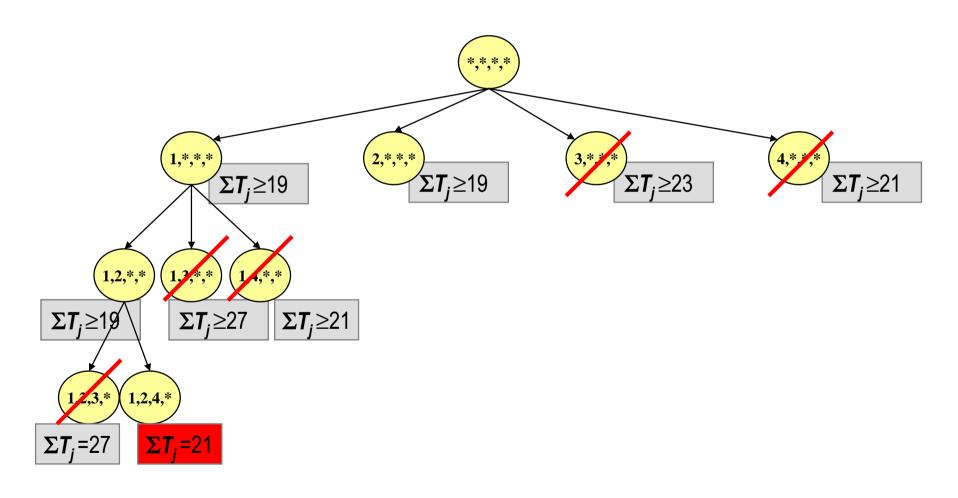
| Jobs                  | 1  | 2  | 3  | 4  |
|-----------------------|----|----|----|----|
| <b>p</b> <sub>j</sub> | 12 | 8  | 15 | 9  |
| d <sub>j</sub>        | 16 | 26 | 25 | 27 |



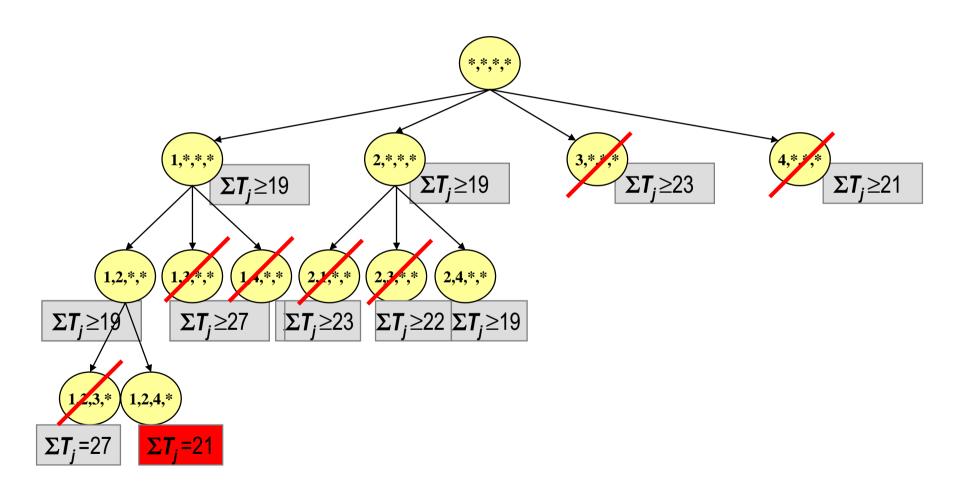
| Jobs                  | 1  | 2  | 3  | 4  |
|-----------------------|----|----|----|----|
| <b>p</b> <sub>j</sub> | 12 | 8  | 15 | 9  |
| <b>d</b> <sub>j</sub> | 16 | 26 | 25 | 27 |



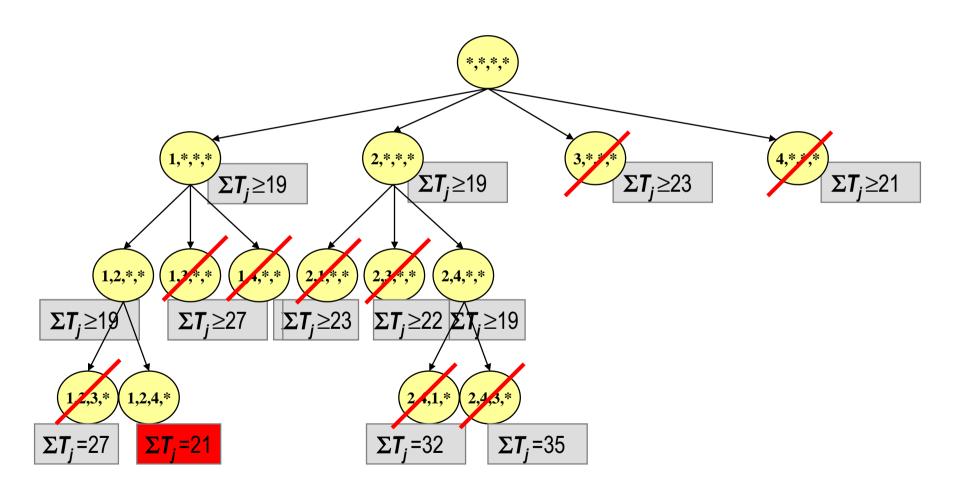
| Jobs                  | 1  | 2  | 3  | 4  |
|-----------------------|----|----|----|----|
| <b>p</b> <sub>j</sub> | 12 | 8  | 15 | 9  |
| d <sub>j</sub>        | 16 | 26 | 25 | 27 |



| Jobs                  | 1  | 2  | 3  | 4  |
|-----------------------|----|----|----|----|
| <b>p</b> <sub>j</sub> | 12 | 8  | 15 | 9  |
| <b>d</b> <sub>j</sub> | 16 | 26 | 25 | 27 |



| Jobs                  | 1  | 2  | 3  | 4  |
|-----------------------|----|----|----|----|
| <b>p</b> <sub>j</sub> | 12 | 8  | 15 | 6  |
| d <sub>j</sub>        | 16 | 26 | 25 | 27 |



# Conclusions

### Advantages of Branch & Bound algorithm:

 Finds an optimal solution (if the problem is of limited size and enumeration can be done in reasonable time).

### <u>Disadvantages of Branch & Bound algorithm:</u>

 Extremely time-consuming: the number of nodes in a branching tree can be too large.