# Planning and Scheduling: State-Space Planning



Hochschule Bonn-Rhein-Sieg Prof. Dr.-Ing. Gerhard K. Kraetzschmar



# Acknowledgements

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- Some improvements have been implemented by Iman Awaad

#### **Motivation**

- Planning as search...
- Which search space?
- State Space
  - Each node represents a state of the world
  - A plan is a path through the space
- Plan Space
  - Each state is a set of partially instantiated operators and some constraints
  - Impose more and more constraints until we get a plan

#### Linear Search

- Basic Idea:
  - Work on one goal until completely solved before moving on to the next goal
  - Order in which problems are solved is linearly-related to the order in which the plan actions are executed
- Planning algorithms maintain a goal stack
- Implications:
  - No interleaving of goal achievement
  - Efficient search if goals do not interact (much)
- Search space is still larger than it should be...

# Means-End Analysis

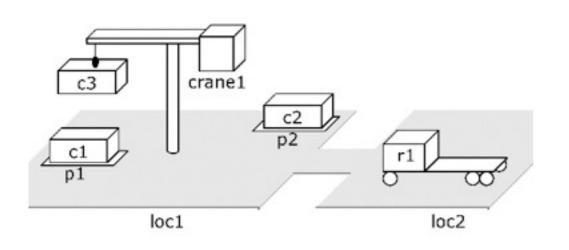
- Basic Idea:
  - Search only relevant aspects of problem
  - What means (operators) are available to achieve the desired ends (goals)
  - I) Find difference between goal and current state
  - 2) Find operator to reduce difference
  - 3) Perform means-end analysis on new sub-goals...
- Introduced by Newell, Simon, Ernest:
  General Problem Solver (GPS) [in the 1960s]

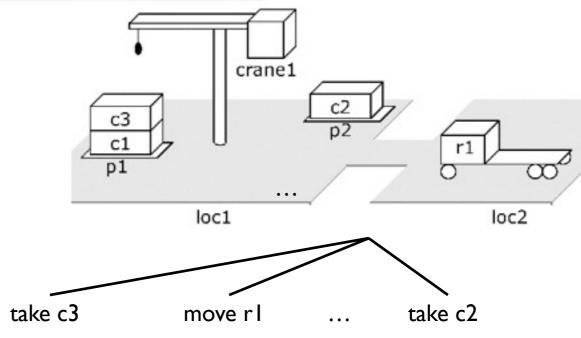
#### Outline

- Forward Search
- Backward Search
- Lifting
- STRIPS (Fikes, Nielson 1971)
  - Same idea as GPS,
  - but solved the frame problem with the STRIPS assumption,
  - introduced operator representation,
  - operationalized ideas of difference, sub-goals and applicability
  - dealt (to some degree) with plan execution and learning
- Block stacking

#### Forward Search

```
Forward-search(O, s_0, g)
s \leftarrow s_0
\pi \leftarrow the empty plan loop
if s satisfies g then return \pi
E \leftarrow \{a|a \text{ is a ground instance an operator in } O,
and \operatorname{precond}(a) is true in s\}
if E = \emptyset then return failure
nondeterministically choose an action a \in E
s \leftarrow \gamma(s, a)
\pi \leftarrow \pi.a
```





#### **Properties**

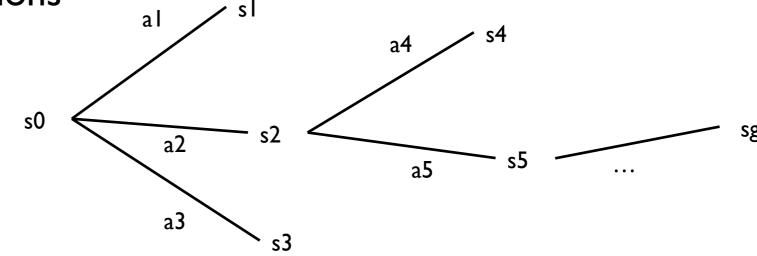
- Forward-search is sound:
  - For any plan returned by any of its nondeterministic traces, this plan is guaranteed to be a solution.
- Forward-search also is complete:
  - If a solution exists, then at least one of Forward-search's *nondeterministic* traces will return a solution.

#### Deterministic Implementations

- Some deterministic implementations of forward search:
  - breadth-first search
  - best-first search
  - depth-first search
  - greedy search

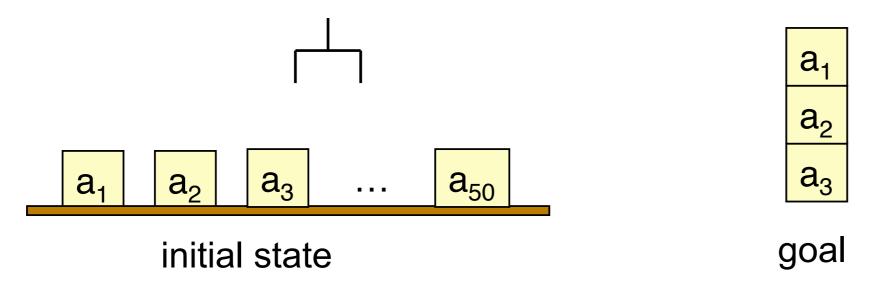


- But they usually aren't practical because they require too much memory
- Memory requirement is exponential in the length of the solution
- In practice, more likely to use a depth-first search or greedy search
  - Worst-case memory requirement is linear in the length of the solution
  - Sound but not complete
    - But classical planning has only finitely many states
    - Thus, can make depth-first search complete by doing loop-checking



# Branching Factor of Forward Search

- Forward search can have a very large branching factor (see example)
- Why this is bad:
  - Deterministic implementations can waste time trying lots of irrelevant actions
- Need a good heuristic function and/or pruning procedure
  - See Section 4.5 (Domain-Specific State-Space Planning) and Part III (Heuristics and Control Strategies)



Search space is still larger than it should be...

#### **Backward Search**

- Use means-end-analysis: search only relevant aspects of the problem
- For forward search, we started at the initial state and computed state transitions:
  - new state  $s' = \gamma(s, a)$
- For backward search, we start at the goal and compute inverse state transitions
  - new set of subgoals  $g' = \gamma^{-1}(g, a)$

#### **Inverse State Transitions**

- What do we mean by  $\gamma^{-1}(g,a)$  ?
- First need to define relevance:
  - An action a is relevant for a goal g if
    - a makes at least one of g's literals true

$$g \cap effects(a) \neq \emptyset$$

a does not make any of g's literals false

$$g_{+} \cap effects_{-}(a) = \emptyset$$
  
 $g_{-} \cap effects_{+}(a) = \emptyset$ 

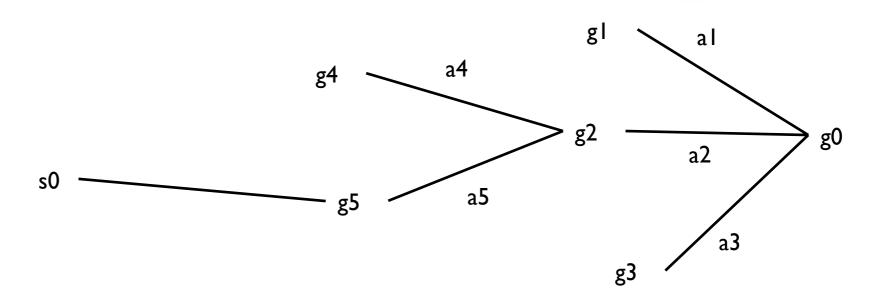
If a is relevant for g, then

$$\gamma^{-1}(g, a) = (g \setminus effects(a)) \cup precond(a)$$

E.g.:  $g = \{on(b1,b2), on(b2,b3)\}$  a = stack(b1,b2)What is  $\gamma^{-1}(g,a)$  ?

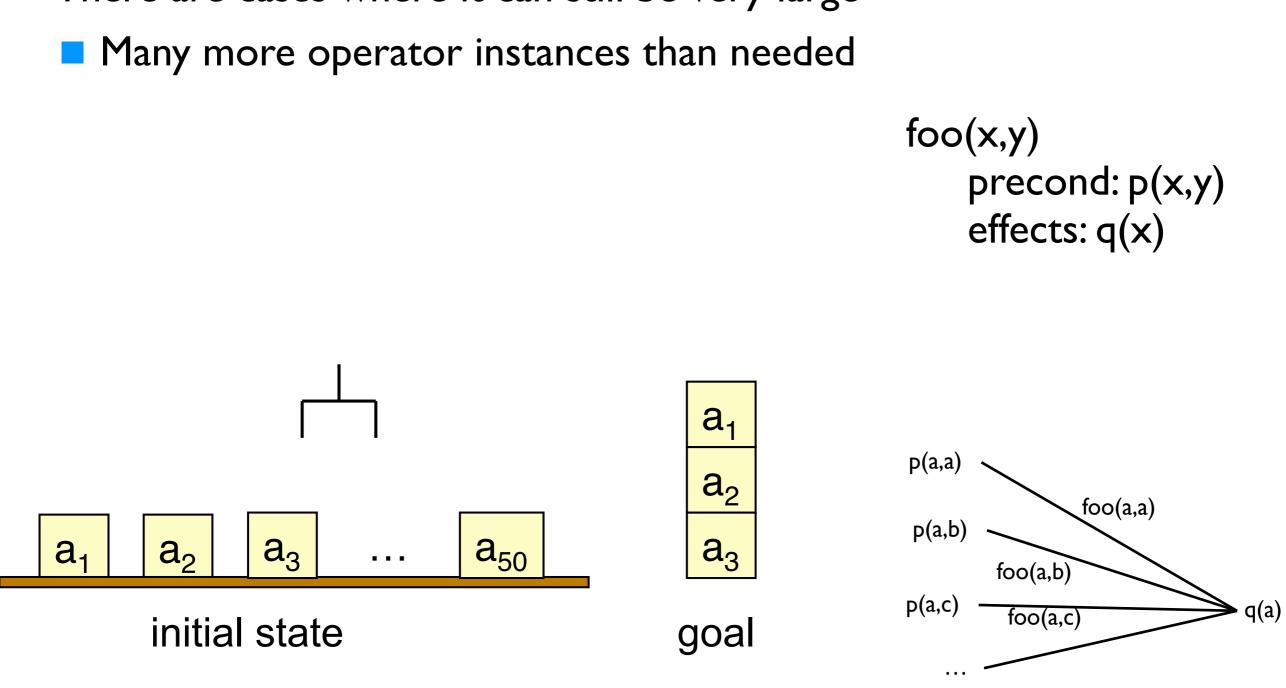
# **Backward Search Algorithm**

```
 \begin{array}{l} \operatorname{Backward-search}(O,s_0,g) \\ \pi \leftarrow \operatorname{the\ empty\ plan} \\ \operatorname{loop} \\ \text{if\ } s_0 \operatorname{\ satisfies\ } g \operatorname{\ then\ return\ } \pi \\ A \leftarrow \{a|a \operatorname{\ is\ a\ ground\ instance\ of\ an\ operator\ in\ } O \\ & \operatorname{\ and\ } \gamma^{-1}(g,a) \operatorname{\ is\ defined} \} \\ \text{if\ } A = \emptyset \operatorname{\ then\ return\ failure\ } \\ \operatorname{\ nondeterministically\ choose\ an\ action\ } a \in A \\ \pi \leftarrow a.\pi \\ g \leftarrow \gamma^{-1}(g,a) \end{array}
```



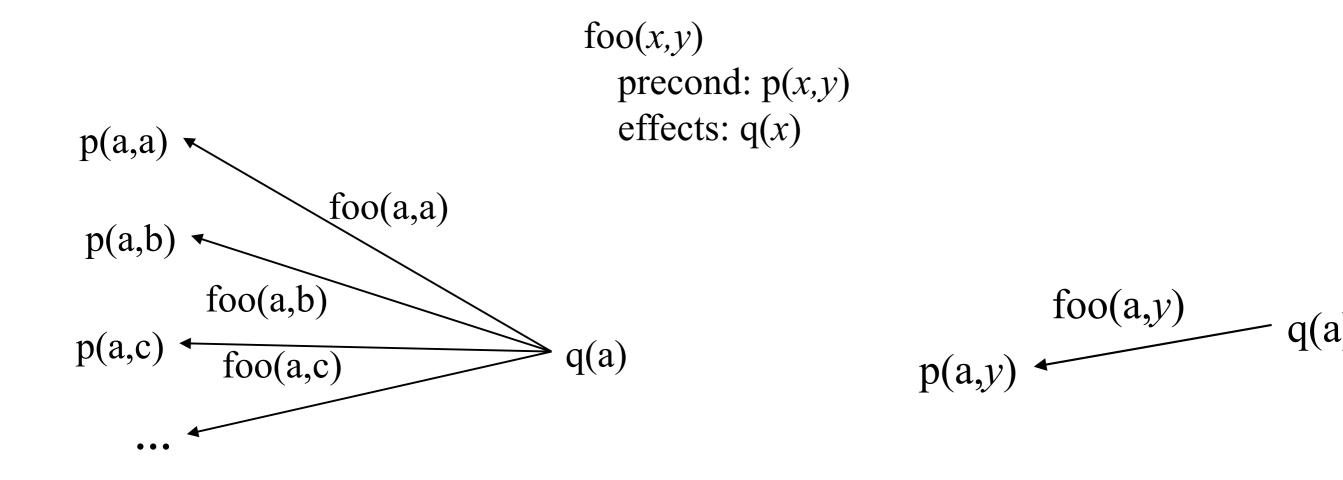
# Efficiency of Backward Search

- Backward search's branching factor is small in our example
- There are cases where it can still be very large



# Lifting

- We can reduce the branching factor if we partially instantiate the operators
  - this is called lifting



#### Lifted Backward Search

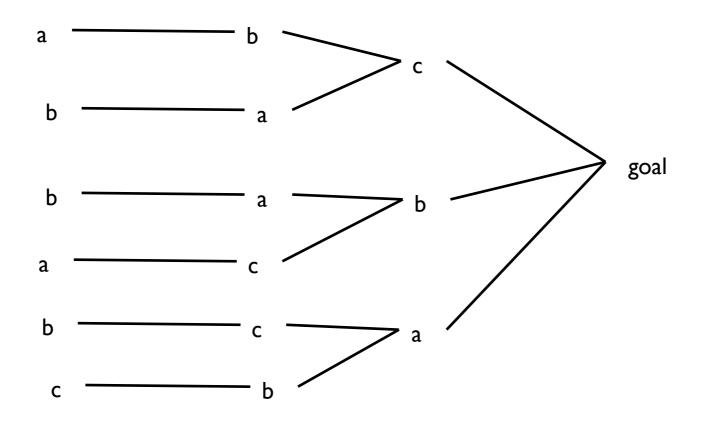
```
Lifted-backward-search(O, s_0, g)
    \pi \leftarrow the empty plan
    loop
        if s_0 satisfies g then return \pi
        A \leftarrow \{(o,\theta)|o \text{ is a standardization of an operator in } O,
                     \theta is an mgu for an atom of g and an atom of effects<sup>+</sup>(o),
                     and \gamma^{-1}(\theta(g), \theta(o)) is defined
        if A = \emptyset then return failure
        nondeterministically choose a pair (o, \theta) \in A
        \pi \leftarrow the concatenation of \theta(o) and \theta(\pi)
        g \leftarrow \gamma^{-1}(\theta(g), \theta(o))
```

- More complicated than Backward-search
  - Have to keep track of what substitutions were performed
- But it has a much smaller branching factor



# The Search Space is Still Too Large

- Lifted-backward-search generates a smaller search space than Backward-search, but it still can be quite large
  - If some sub-problems are independent and something else causes problems elsewhere, we'll try all possible orderings before realizing there is no solution
  - More about this in Chapter 5 (Plan-Space Planning)

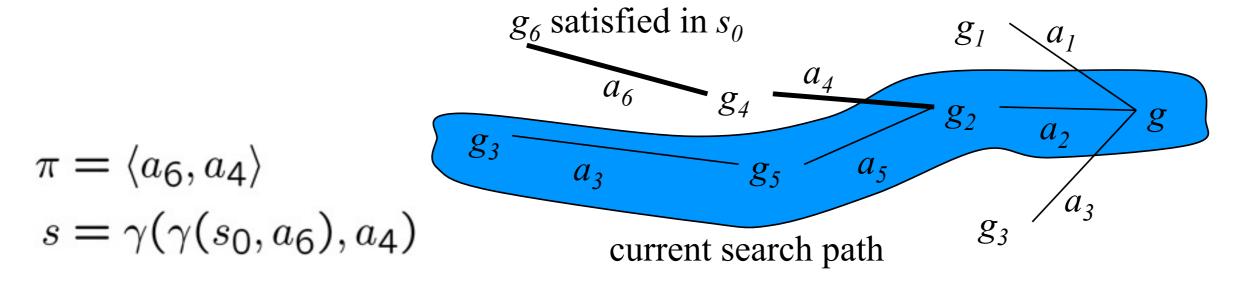


## Other Ways to Reduce the Search

- Search Control Strategies
  - Part III of the textbook E.g.: Least Commitment Strategies
- For now two examples:
  - STRIPS
  - Block stacking

#### **STRIPS**

- $\blacksquare$   $\pi$  the empty plan
- do a modified backward search from g
  - instead of  $\gamma^{-1}(s,a)$ , each new set of sub-goals is just precond(a)
  - whenever you find an action that's executable in the current state, then go forward on the current search path as far as possible, executing actions and appending them to  $\pi$
  - repeat until all goals are satisfied



#### Quick Review of Blocks World

#### unstack(x,y)

Pre: on(x,y), clear(x), handempty

Eff:  $\sim on(x,y)$ ,  $\sim clear(x)$ ,  $\sim handempty$ ,

holding(x), clear(y)

#### stack(x,y)

Pre: holding(x), clear(y)

Eff: ~holding(x), ~clear(y),

on(x,y), clear(x), handempty

#### pickup(x)

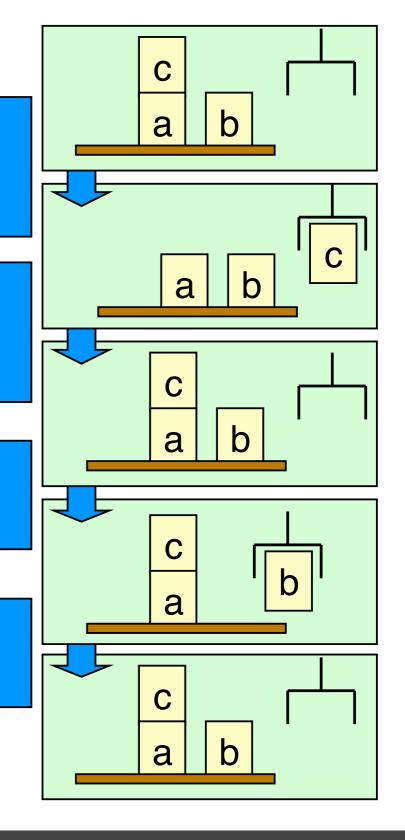
Pre: ontable(x), clear(x), handempty

Eff: ~ontable(x), ~clear(x), ~handempty, holding(x)

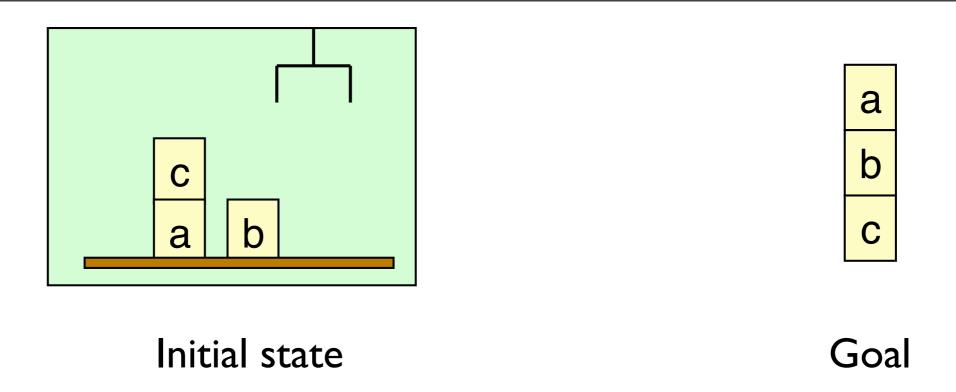
#### putdown(x)

Pre: holding(x)

Eff: ~holding(x), ontable(x), clear(?x), handempty



# The Sussman Anomaly



- For this problem, STRIPS can not produce an irredundant solution!
  - Try and see!
- Shows the weakness of non-interleaved planning
- Problem in the 'divide and conquer' strategy of the planner

# The Register Assignment Problem

#### State-variable formulation:

- Initial State:  $\{value(r1)=3, value(r2)=5, value(r3)=0\}$
- Goal:  $\{value(r1)=5, value(r2)=3\}$
- Operator: assign(r,v,r',v')
  - Preconditions: value(r)=v, value(r')=v'
  - Effects: value(r)=v'

STRIPS can not solve this problem at all!

#### Linear Planning: Discussion

- Advantages
  - Reduced search space, since goals are solved one at a time
  - Advantageous if goals are (mainly) independent
  - Linear planning is sound
- Disadvantages
  - Linear planning may produce suboptimal solutions (based on the number of operators in the plan)
  - Linear planning is incomplete

# How to Fix Linear Planning?

- Several ways:
  - Do something other than state-space search
    - e.g., Chapters 5–8 in the text book
  - Use forward or backward state-space search, with domain-specific knowledge to prune the search space
    - Can solve both problems quite easily this way
    - Example: block stacking using forward search

# Domain-Specific Knowledge

- A blocks-world planning problem  $P = (O, s_0, g)$  is solvable if s0 and g satisfy some simple consistency conditions:
  - g should not mention any blocks not mentioned in s0
  - a block cannot be on two other blocks at once
  - etc.

Can check these in time O(n log n)

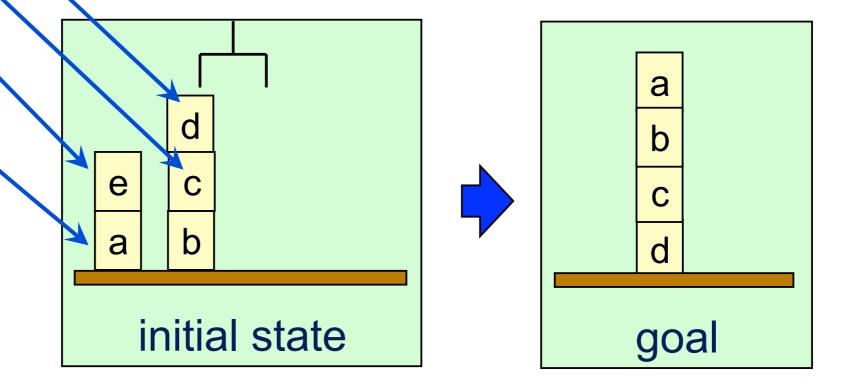
- If P is solvable, can easily construct a solution of length O(2m), where m is the number of blocks
  - Move all blocks to the table, then build up stacks from the bottom

Can do this in time O(n)

With additional domain-specific knowledge can do even better...

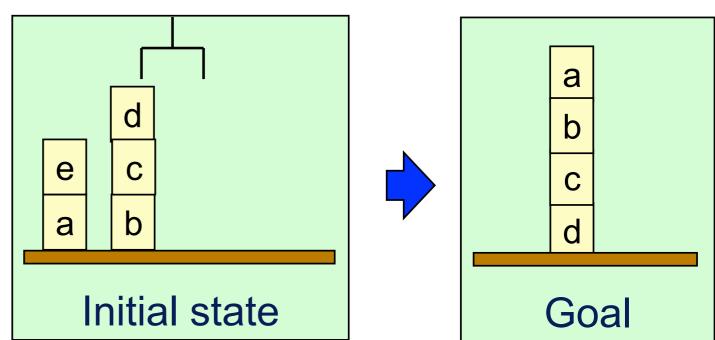
# Additional Domain-Specific Knowledge

- A block x needs to be moved if any of the following is true:
  - $\rightarrow$  s contains ontable(x) and g contains on(x,y)
  - contains on(x,y) and g contains ontable(x)
  - $\blacksquare$  s contains on(x,y) and g contains on(x,z) for some y $\neq$ z
  - s contains on(x,y) and y needs to be moved



## Domain-Specific Algorithm

c else if the goal is satisfied then return the plan else return failure repeat



## Easily Solves the Sussman Anomaly

#### loop

if there is a clear block x such that

x needs to be moved and

x can be moved to a place where it won't need to be moved

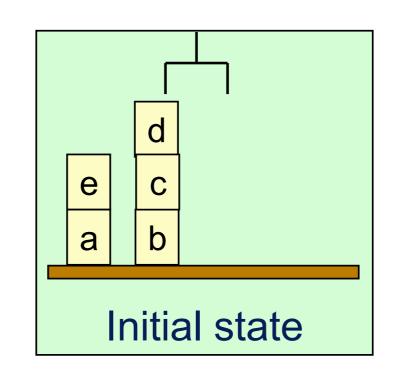
then move x to that place

else if there is a clear block x such that

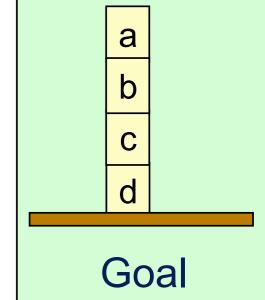
x needs to be moved

then move x to the table

else if the goal is satisfied
then return the plan
else return failure
repeat







#### **Properties**

- The block-stacking algorithm is:
  - Sound, complete, guaranteed to terminate
  - Runs in time  $O(n^3)$  Can can be modified to run in time O(n)
  - Often finds optimal (shortest) solutions
  - But sometimes only near-optimal (Exercise 4.22 in the book)
    - Recall that PLAN-LENGTH is NP-complete

## Next Week: Non-Linear Planning

- Basic Idea:
  - Use goal set instead of goal stack
  - Include in the search space all possible sub-goal orderings
    - Handles goal interactions by interleaving
- Advantages
  - Sound & Complete
  - May be optimal with respect to plan length (depending on search strategy employed)
- Disadvantages
  - Larger search space,
     since all possible goal orderings may have to be considered
  - Somewhat more complex algorithm; more bookkeeping