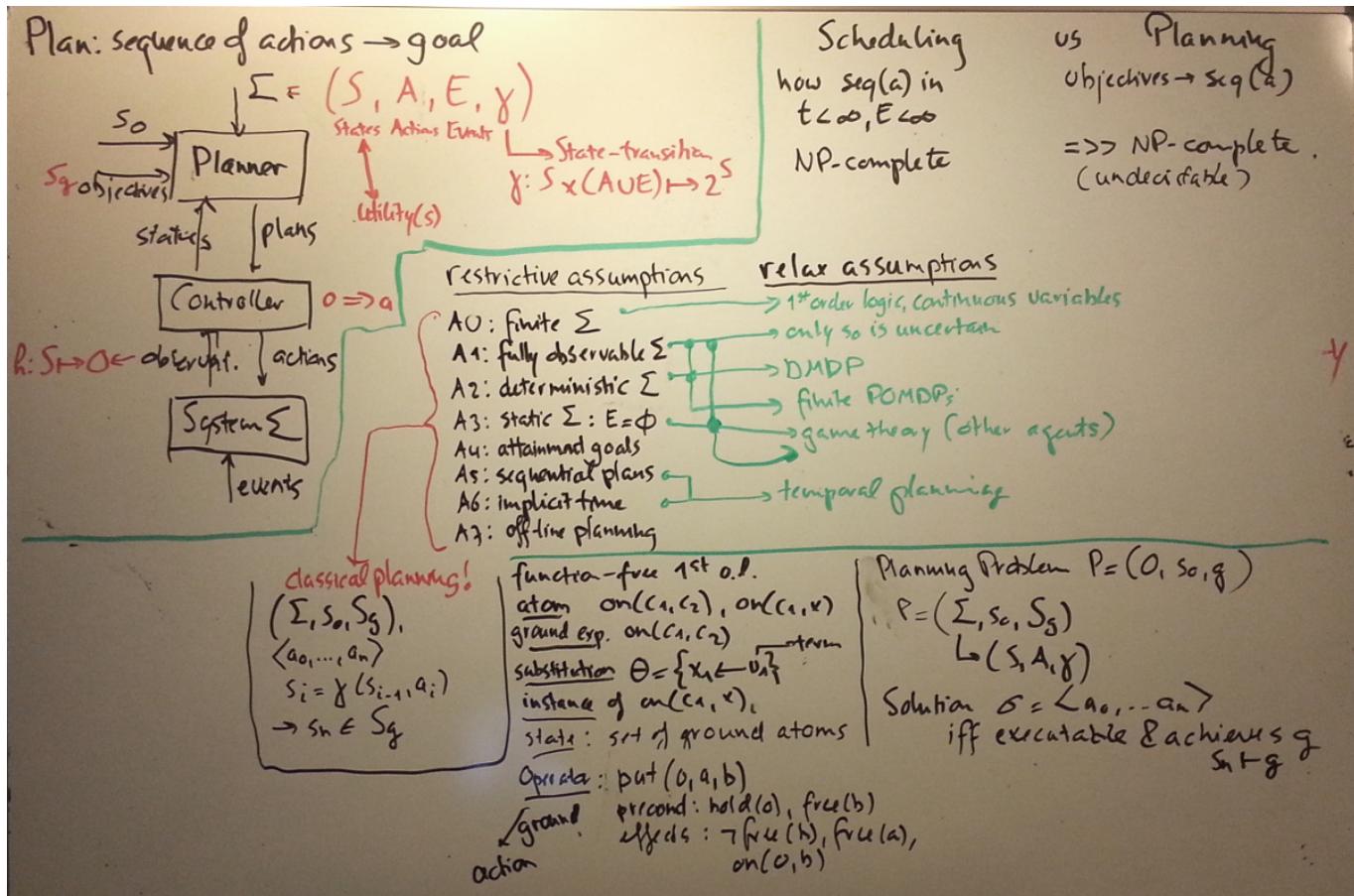


# Summary Planning and Scheduling

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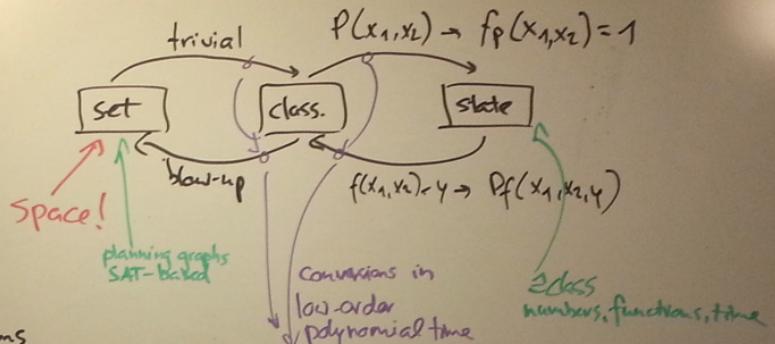
Sankt Augustin, December 5, 2013



### Set-theoretic representation: propositional logic

$\text{on}(c_1, p_2) \rightarrow$  boolean:  $\text{On} - c_1 - p_2$   
exponential blow-up

State-variable representation  
 $\text{top}(p_1) = c_3$



Determining complexity of planning problems  
→ translate into language-recognition problem  
and examine its complexity

- 1) PLAN-EXISTENCE =  $\{P \mid P \text{ has solution}\}$
  - 2) PLAN-LENGTH =  $\{(P_n) \mid P \text{ solution of length } n\}$
- decidable iff not EX + function symbols

outside Classical planning:

- infinite init states
- function symbols
- operators: conditional effects

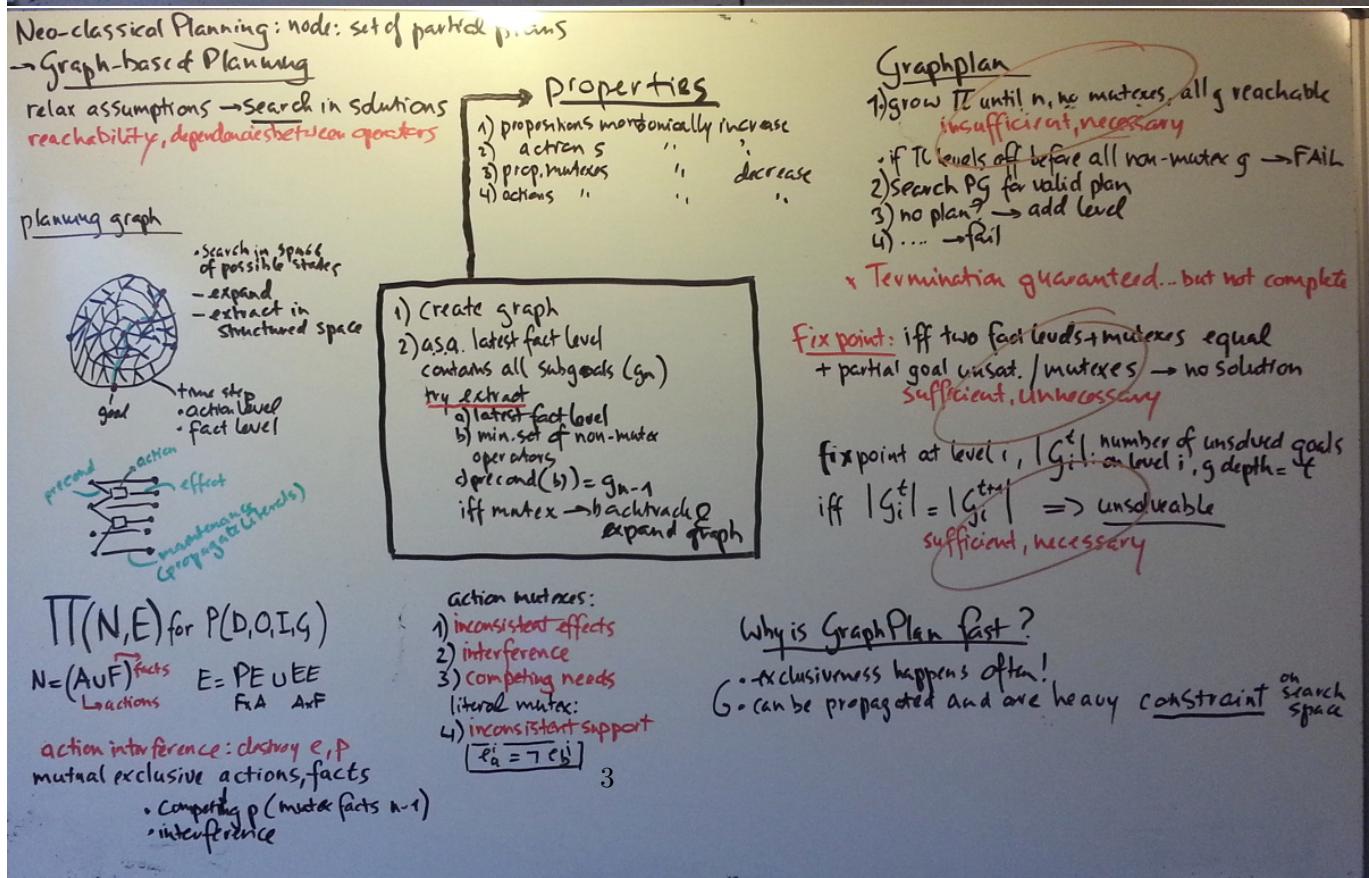
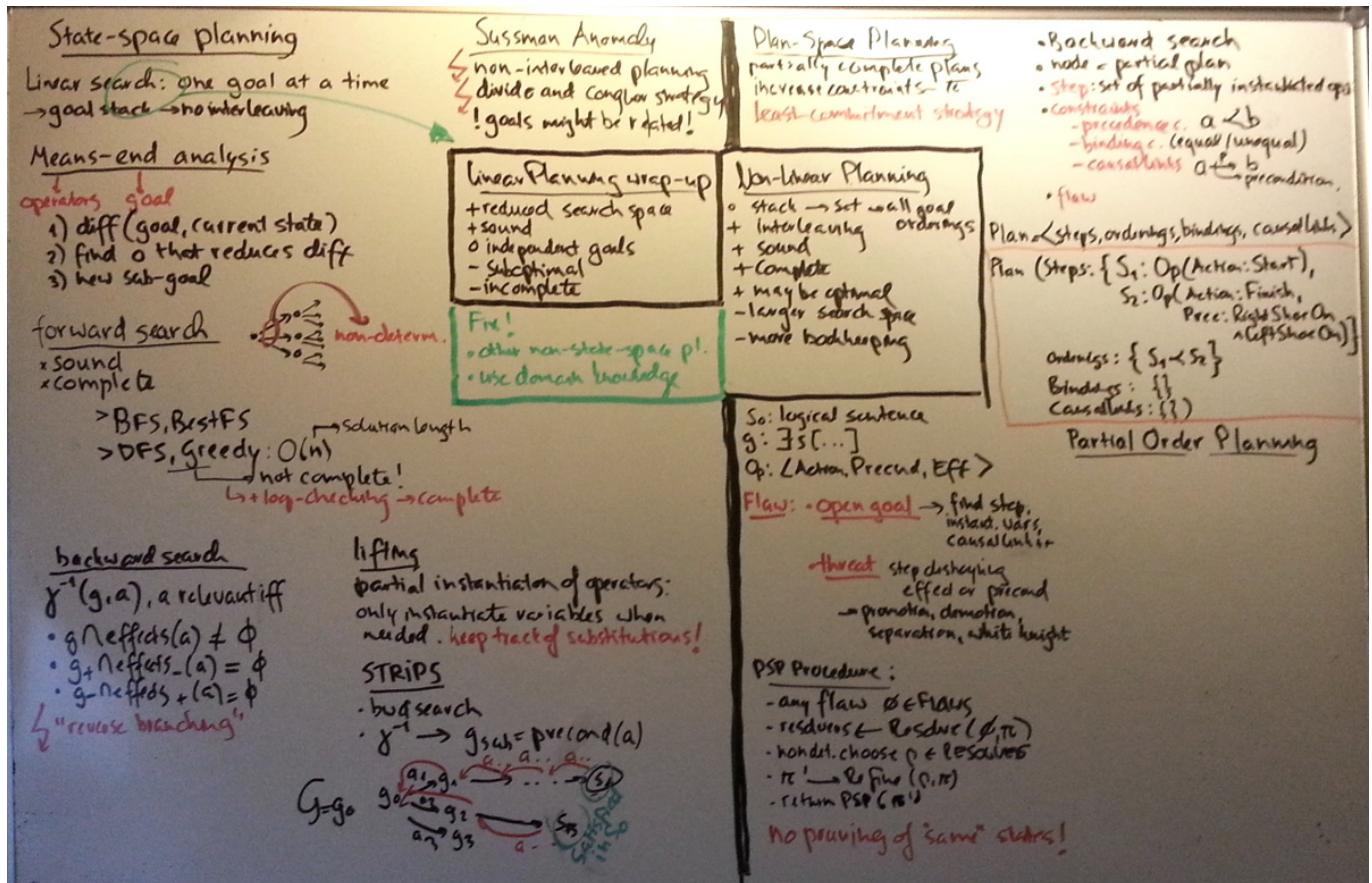


Figure 2: ..

STRIPS on So  
2023.01.

### SAT

- $P \rightarrow (P, m)$  encodes  $\phi$  (satisfiability problem)
- add time step to clauses.  $\langle a_0, \dots, a_n \rangle$  [time step]

Fluent: proposition that changes over time steps  
 $at(c_i, t) \rightarrow at(c_i, t, i)$        $\begin{matrix} 0 & 1 & 2 & 3 & 4 \\ T & F & F & F & T \end{matrix}$   
 $l_i$  (literals)       $\dots$

- action at time step i

$move(a, b) \rightarrow move(a, b, i)$

int  $t_{lo}, t_{hi}$   
goal  $t_{lo}, t_{hi}$

for all a at all time steps i :

$l_i$  (preconds)  
 $l_{0i}$  ( $eff^+(a)$ )  
 $l_{1i}$  ( $eff^-(a)$ )

Explanatory frame axioms

$$\left( \begin{array}{l} l_{0i} \wedge l_{1i} \Rightarrow \forall a \in \{a | l \in eff^+(a)\} \\ l_{0i} \wedge l_{1i} \Rightarrow \forall a \in \{a | l \in eff^-(a)\} \end{array} \right) \wedge$$

$$\left( \begin{array}{l} l_{0i} \wedge l_{1i} \Rightarrow \forall a \in \{a | l \in eff^+(a)\} \\ l_{0i} \wedge l_{1i} \Rightarrow \forall a \in \{a | l \in eff^-(a)\} \end{array} \right)$$

Complete exclusion axiom:

$$\neg l_{0i} \vee \neg l_{1i}$$

Solution:

model  $\rightarrow$  action fluents  $\rightarrow \langle a_0, \dots, a_n \rangle$

Partial exclusion  $\rightarrow$  layered plans.  
(only do for incompatible actions)

Solutions:

DPLL: complete solver

- literal tree -> clause tree
- clause path -> sentence false
- pure symbol heuristic: always true
- unit clause heuristic: always true
- $(L_i), L_i = \text{false}, L_i \text{ can be deleted}$   
 $\Rightarrow (L_i) = \emptyset = \text{false}$ .

Local search

single state  $\rightarrow$  neighbors

O(1) memory

1) "hypothesis" of model: u

cost(u, v) = no. of unfulfilled clauses

flip(P, u)

• Sound

• not complete (local minima)

GSAT: choose P that min. cost (flip(P, u),  $\phi$ )

max flips  $\rightarrow$  restart

max restart  $\rightarrow$  fail

Blackbox: from STRIPS Plan:

build Graph plan for no. 0, 1, 2, ... 4  
for necessary/most conf. PLAN-EXIST

$\rightarrow$  SAT with actions from graph only

$\hookrightarrow$  reduce memory load

WalkSAT: prob. P: flip random

$\neg P$ : flip best

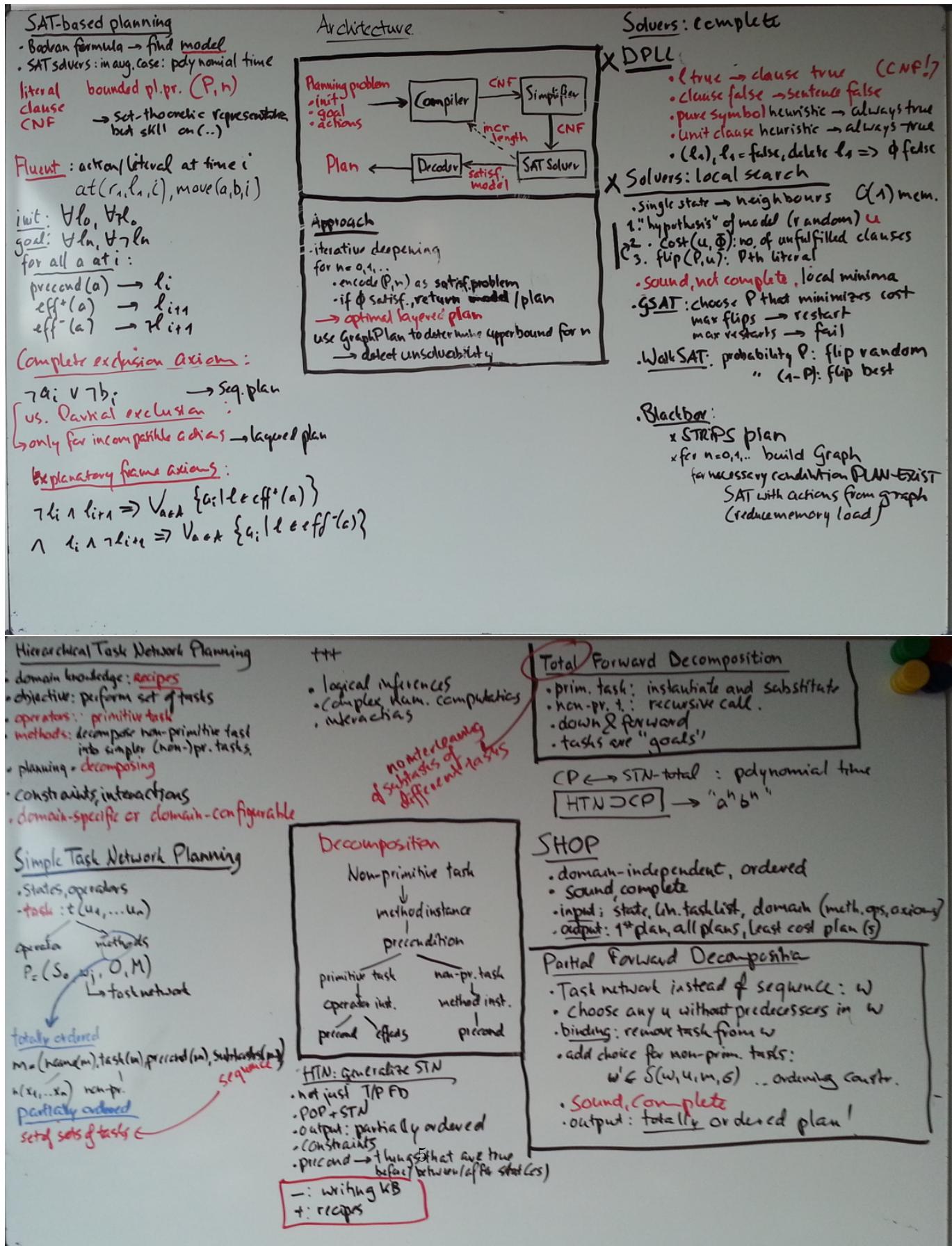


Figure 4: ..

Scheduling  
allocation of resources to activities over time  
Gantt charts

Classification

$\alpha | \beta | \gamma$

Machine environment

single stage:

$$\alpha = 1, \alpha = P$$

$$P_i, P_{ij}$$

multi stage:

def flow shop  
each machine 1, 2, 3, ...

$\alpha = 1$ : job shop

each job own route

$\alpha = 0$ : Open Shop  
arbitrary order

Job characteristics

$P_{ij}$ : processing time  
job  $j$ , machine  $i$

$r_j$ : release time

$d_j$ : due time

$w_j$ : weight

$p_{int}$ : preemption  
(interrupt/resume)

examples:

$1|r_j|L_{max}$

$1|r_j, P_{int}|L_{max}$

$P_1, P_2, \dots |C_{max}$

$J3 | P_{ij}=1 | C_{max}$

$C_j : completion time$

Makespan

$$C_{max} = \max\{C_j\}$$

Total completion time

$$\sum_{j=1}^n C_j$$

Total weighted c.t.

$$\sum_{j=1}^n w_j C_j$$

Lateness:  $L_j = C_j - d_j$

Tardiness:  $T_j = \max\{0, C_j - d_j\}$

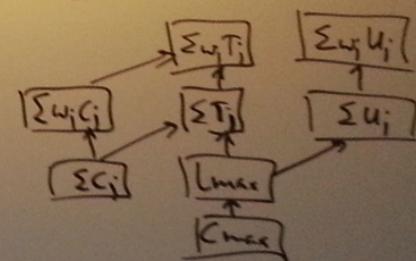
Uniquely:  $U_j = \begin{cases} 0 & \text{if } C_j \leq d_j \\ 1 & \text{otherwise} \end{cases}$

maximum lateness

total tardiness / weighted

total nr. of lat jobs / weighted

Complexity hierarchy



Single Machine: Total completion time

SPT: Shortest Processing Time first

WSPT: Weighted SPT

↳ non-decreasing order  $\frac{P_i}{w_i}$

↳ optimal for  $1|r_i| \sum w_i C_i$

$1|r_i, P_{int}| \sum C_i$ :  $\exists$  optimal sched w/o Preempt

SRPT: Shortest Remaining Processing Time

@ each time j complete next job has  
next release date smallest remaining  
processing time

↳ opt. for  $1|r_i, P_{int}| \sum C_i$

due date scheduling

$1|L_{max} \rightarrow EDD$  rule: Expected Date of Delivery

NP-hard  
Polynomial



↳ Branch & Bound

$1|\sum w_i \rightarrow$  Moore's Rule

1) add jobs in EDD order

2) if "add  $j$ "  $\rightarrow C_j > d_j$ , then  
remove job with largest  $C_j$ ...

3) late jobs: arbitrary order

Figure 5: ..