

# Multivariate Symbolic Aggregate Approximation for ECG Analysis

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# Outline

1 Introduction and Background

2 Methods

3 Results

4 Conclusions

# Motivation and Relevance

- heart diseases kill more people a year than any other disease
  - ischemic heart disease (IHD) makes up 16% of global deaths
  - IHD can be diagnosed using a stress test and electrocardiogram (ECG or EKG)
  - manual ECG analysis is slow and error-prone
- computerized ECG analysis can help

# What is an ECG?

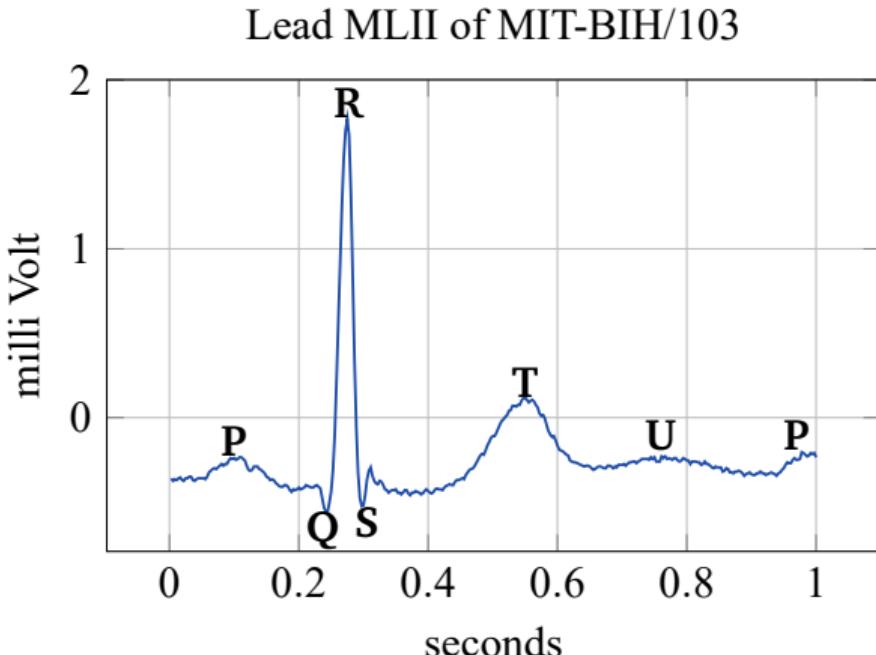


Figure 1: Annotated ECG of one heartbeat

- records the heart's electrical activity
- contains up to 12 leads (simultaneous measurements)

# Steps of ECG Analysis I

General steps:

- (1) signal acquisition and filtering
- (2) data transformation or preparation for processing
- (3) waveform recognition
- (4) feature extraction
- (5) classification or diagnosis

# Steps of ECG Analysis II

This work's focus:

- (1) signal acquisition and filtering
  - **data transformation** or preparation for processing
- (3) waveform recognition
- (4) feature extraction
  - **classification** or diagnosis

# Research Questions & Hypothesis

- using the MIT-BIH ECG database, determine the parameters maximizing HOT SAX and HOT MSAX recall
  - compare recall value for best parameters
- HOT MSAX should have higher recall than HOT SAX if both use their best parameters

# Previous Research

- Lin *et al.* (2003):  
Symbolic Aggregate Approximation (SAX)—simplified, symbolic representation
- Keogh *et al.* (2005):  
Heuristically Ordered Time series using SAX (HOT SAX)—discord discovery algorithm using SAX
- Anacleto *et al.* (2020):  
Multivariate SAX (MSAX)—expands SAX to multivariate time series

# This Work's Novel Contributions

- application of MSAX to ECG discord discovery
- the HOT MSAX algorithm
- the expansion of HOT SAX to multivariate time series through HOT MSAX

# SAX and MSAX – Overview

SAX	MSAX
Application	
univariate time series e.g. a single ECG lead	multivariate time series e.g. multiple ECG leads
Steps	
(1) univariate z-normalization (2) PAA dimension reduction (3) SAX discretization	(1) multivariate z-normalization (2) PAA dimension reduction (3) SAX discretization

# SAX and MSAX – Step (2)

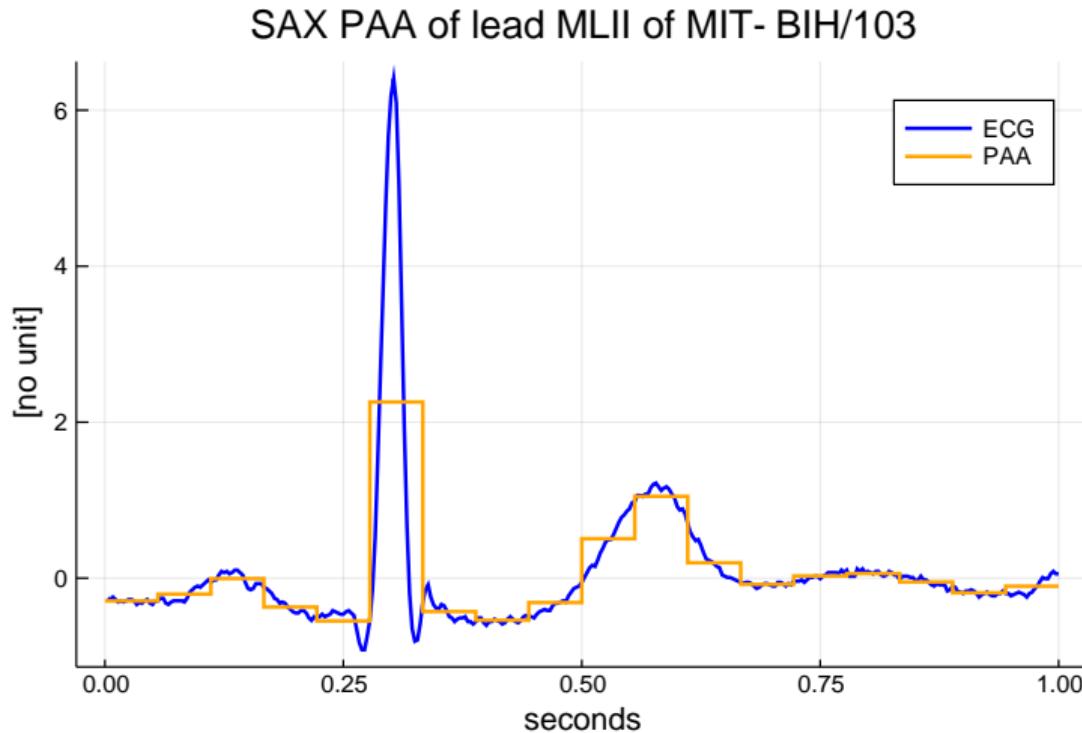
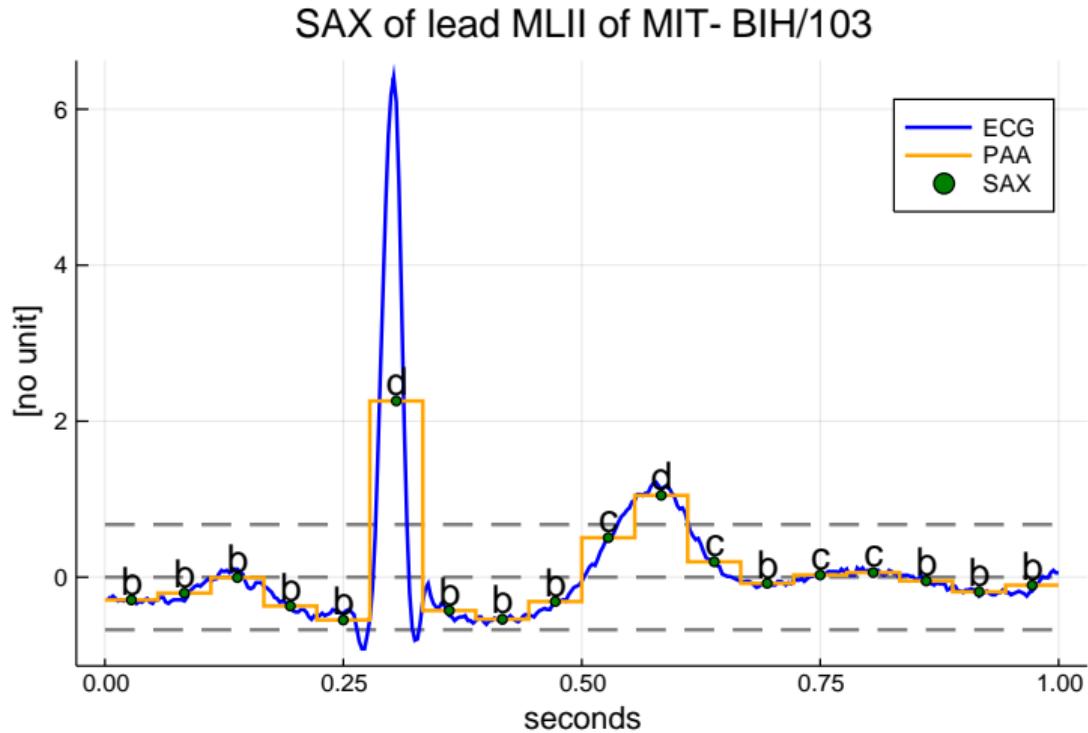


Figure 2:  
ECG with  
PAA (MIT-  
BIH/103,  
 $w = 18$ ,  
 $T = 360$ )

## SAX and MSAX – Step (3)



**Figure 3:**  
ECG with  
SAX (MIT-  
BIH/103,  
 $w = 18$ ,  
 $T = 360$ )

# SAX and MSAX – Distance Measure

- basically the sum of distances between symbols
- symbol distance is based on difference of breakpoints
- lower-bounds Euclidean Distance, corresponds to “real” distance

Table 1: Distance matrix for 5 symbols.

	a	b	c	d	e
a	0	0	0.59	1.09	1.68
b	0	0	0	0.51	1.09
c	0.59	0	0	0	0.59
d	1.09	0.51	0	0	0
e	1.68	1.09	0.59	0	0

# HOT SAX and HOT MSAX – Overview

- HOT SAX: find discords in SAX-represented time series
- speeds up the “brute force” approach
- classifies time series segments into “discord” and “non-discord”
- HOT MSAX: uses MSAX instead of SAX
- HOT MSAX can work with multivariate time series

# HOT SAX and HOT MSAX – Heuristic

- two assumptions:
  - time series discords are rare
  - similar segments are similarly rare
- speed up discord discovery:
  - consider rarest segments first
  - consider segments similar to the rarest first

# Parameter Optimization

- perform HOT SAX and HOT MSAX for many parameter combinations
- find recall for each combination
- recall threshold of 95%, then sort by precision
- choose top 10 of those parameters for each method
- choose best parameters using box plot, interquartile range, outliers

# Overview of Results

**Table 2:** Coarse Overview of Results. Shown are sets of parameters for each method that satisfy the recall threshold of 95%.

Method	Total Sets	Sets Satisfying recall $\geq 95\%$
S-SAX		99 (1.2%)
D-SAX	4,968	192 (3.9%)
MSAX		255 (5.1%)

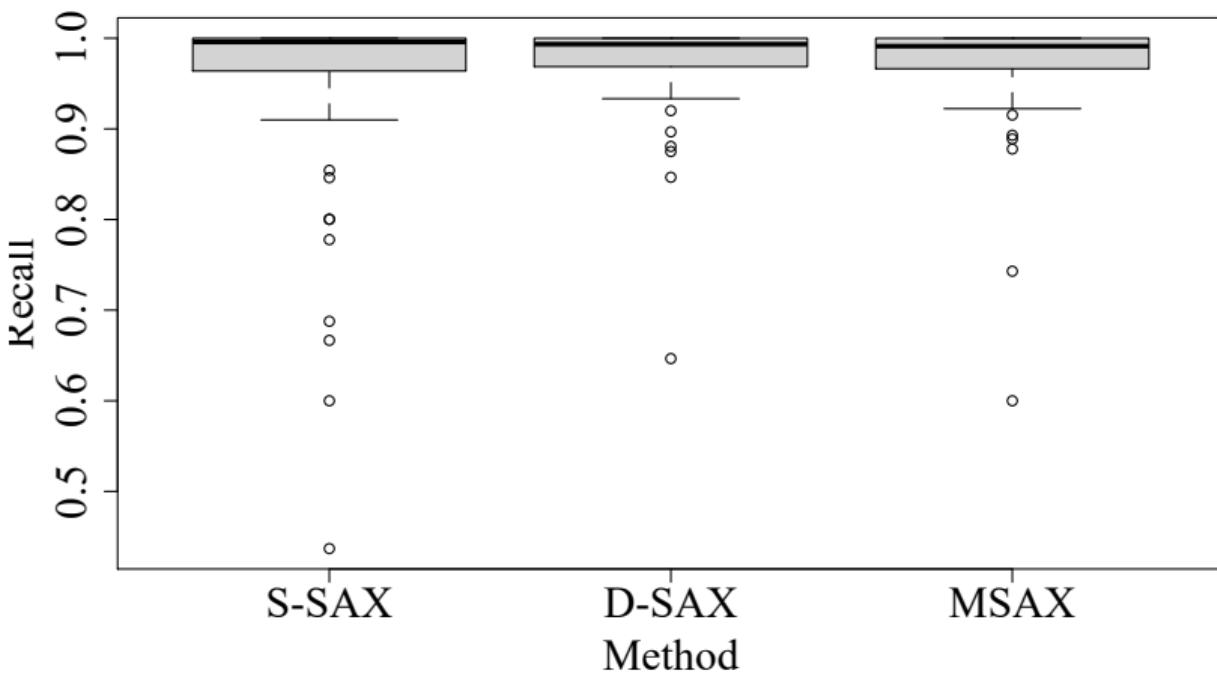
# Best Parameter Sets by Method

**Table 3:** Best Parameter sets for each of the methods. Best overall parameters highlighted in bold.

Method \ Parameter	$k$	$w, m$	$a$
S-SAX	-1	36	21
D-SAX	-1	<b>12</b>	24
MSAX	-1	<b>12</b>	<b>17</b>

# Comparing Best Parameter Sets – Recall

## Boxplot of Recall by Method for Optimal Parameter



# Comparing Best Parameter Sets – Recall

**Table 4:** Statistical measures for recall of optimal parameter sets. Best overall values highlighted in bold.

Method \ Measure	IQR	Median	Outliers
S-SAX	0.035	<b>99.60%</b>	11
D-SAX	<b>0.030</b>	99.35%	<b>6</b>
MSAX	0.033	99.13%	<b>6</b>

# Discussion

- no statistically significant difference in recall for the methods
  - hypothesis cannot be supported
- MSAX has both the smallest alphabet size and highest dimension reduction
  - this points to MSAX being more efficient in achieving the same results
- Anacleto, Vinga, and Carvalho [5] showed similar performance for ECG classification, supports this work's conclusion

# Conclusion

- could not demonstrate superiority of HOT MSAX for best parameters
- contributed the HOT MSAX method to literature
- HOT MSAX was found to be more efficient than HOT SAX
- showed viability of a discord classifier for ECG analysis

# References I

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- [4] E. Keogh, J. Lin, and A. Fu, “HOT SAX: Efficiently Finding the Most Unusual Time Series Subsequence,” in *Fifth IEEE International Conference on Data Mining (ICDM'05)*, Houston, TX, USA: IEEE, 2005, pp. 226–233. doi: 10.1109/ICDM.2005.79.

## References II

- [5] M. Anacleto, S. Vinga, and A. M. Carvalho, “MSAX: Multivariate Symbolic Aggregate Approximation for Time Series Classification,” in *Computational Intelligence Methods for Bioinformatics and Biostatistics*, P. Cazzaniga, D. Besozzi, I. Merelli, and L. Manzoni, Eds., ser. Lecture Notes in Computer Science, Cham: Springer International Publishing, 2020, pp. 90–97. doi: [10.1007/978-3-030-63061-4\\_9](https://doi.org/10.1007/978-3-030-63061-4_9).

Thank You!