

c)

$$\begin{aligned} x \rightarrow r(x) &= \operatorname{argmax}\{p(k) \cdot p(x|k)\} \\ &= \operatorname{argmax}\{p(k) \cdot N(x|\mu_k, \Sigma)\} \\ &= \operatorname{argmax}\{p(k) \cdot \frac{1}{\prod_{d=1}^D \sqrt{2\pi\sigma_{kd}^2}} \cdot \exp[-\frac{1}{2} \sum_{d=1}^D (\frac{x_d - \mu_{kd}}{\sigma_{kd}})^2]\} \end{aligned}$$

$p(k)$ stays unchanged because we can calculate it directly from counts in the training data. Because we have a pooled diagonal variance, we also cancel out $\frac{1}{\prod_{d=1}^D \sqrt{2\pi\sigma_{kd}^2}}$ because its the same for each class. Same for the $\frac{1}{2}$ in the exponent. So the decisionrule we calculate with in our python script is:

$$x \rightarrow r(x) = \operatorname{argmax}\{p(k) \cdot \exp[-\sum_{d=1}^D (\frac{x_d - \mu_{kd}}{\sigma_{kd}})^2]\}$$