

Data Structures and Algorithms

Introduction to Data Structures

Design and Analysis of Algorithms

Week 1



Hello World ©



HELLO my name is

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dsa





IDE:

Dev-C++ (download:

https://sourceforge.net/project
s/orwelldevcpp/)

NetBeans

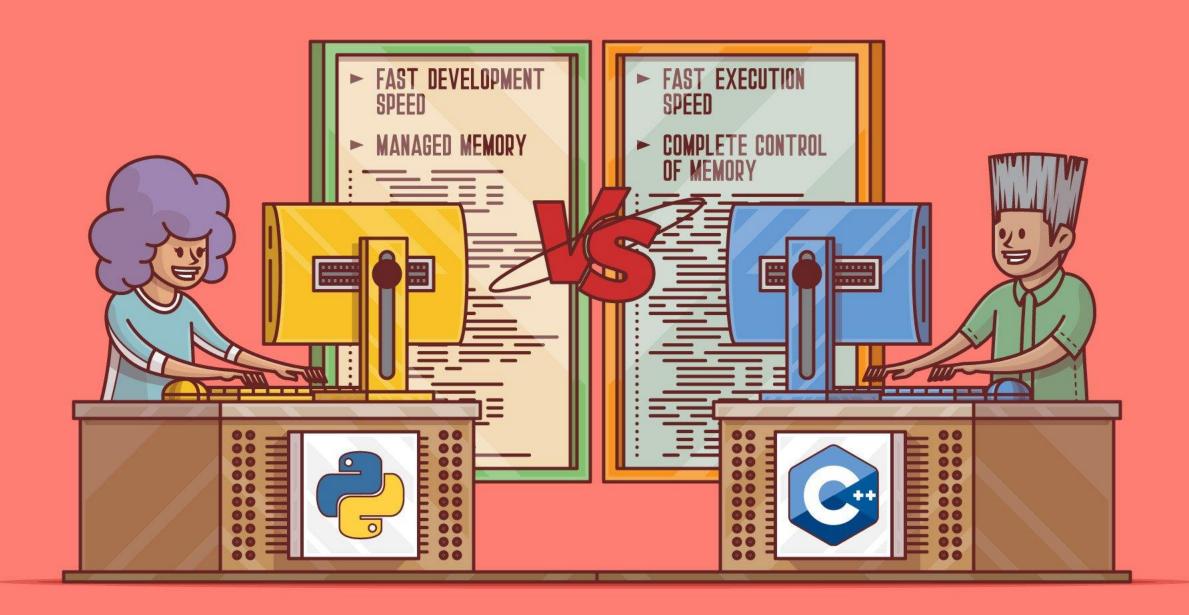
Visual Studio (Express)

Eclipse

Etc...







Real Python



Python vs C++

#1

Advantages:

- Easy to learn
- Easy to access libraries
- Scientific community sharing (open source, many libraries)

<u>Disadvantages:</u>

- Slow
- Interpreted (dependencies)
- Not typed (errors at runtime)

Advantages:

- Execution speed
- Pre-Compiled (exe on machine)
- Typed (well defined)
- Modern professional libraries

<u>Disadvantages:</u>

- Learning curve
- Harder to acces libraries (less sharing than in Python)



Syntax

```
C++ (CPP)
```

Strong Typing

```
int a;
a = 5; //Correct
a = "string"; //Error!!

Type must be known by the compiler
```

Python

You need to pay attention to the indentation Weak typing

```
a = 5  #Correct
a = "stringa" #Correct
a = 1.3  #Correct
```

No explicit type declaration

```
hello! select your level: easy
how many plays do you want?: 2
2x8= 333
wrong!
5x1= 5
true!
score: 1/2
Process exited after 6.042 seconds with return value 0
Premere un tasto per continuare . . .
```

import random

```
random.seed()
score =0
def generate (1v1):
    j=random.randrange(lv1)
level = input ("hello! select your level: ")
if (level == "easy"):
    max = 10
elif (level == "medium"):
    max = 20
else:
    max =30
plays = int (input ("how many plays do you want?: "))
for c in range (plays):
    x= generate (max)
    y= generate (max)
    risposta = int (input("()x()=".format (x,y)))
    if (risposta == x*y):
        score = score+1
        print ("true!\n")
    else:
        print ("wrong!\n")
 print ("score: ", score, "/", plays)
```

```
Differences?
```

```
#include <stdlib.h>
  using namespace std;
  int generate (int lvl)
- {
      int j = rand()%1v1+1;
      return j;
  int main()
- {
      int max, plays, score=0, x, y;
      string level;
      cout<<"hello! select your level: "; cin>> level;
      if (level == "easy")
Н
          max=10;
      else if (level == "medium")
max = 20;
max = 30;
      cout<<"how many plays do you want?: "; cin>> plays;
      for (int s=0; s <plays; s++)
Н
          x= generate(max);
          y= generate (max);
          int risposta;
          cout<<x<<"x"<<y<<"= "; cin>> risposta;
          if (risposta == x*y)
cout<<"true!\n";
              score++;
Н
              cout<<"wrong!\n";
      cout<<"score: "<<score<<"/"<<plays;
```



Please prepare your IDE

(we will use it later....)





Course Description



COMP6571 – Data Structures and Algorithms



SCU 4+2 credits



Lecture session



Lab session



Syllabus



Course Description

- This course serves as a one of the foundation courses in Computer Science.
- It provides students with an understanding of the principles of data structures and algorithms in the design and development of computer software.
- Students will learn basic data structures and its use in different algorithms that are commonly used in making structured and efficient software programs



Session Learning Outcomes

Upon completion of this session, students are expected to be able to

- 1. Describe the use of various data structures
- 2. Apply appropriate operations for maintaining common data structures.
- 3. Apply appropriate data structures and simple algorithms for solving computing problems.
- 4. Design computer programs by applying different data structures and related algorithms
- 5. Explain the efficiency of some basic algorithms
- 6. Design efficient software solutions that are appropriate for specific problems



Textbooks



- Aho, A., Hopcroft, J. Ullman, J. (1987). Data Structures and Algorithms. Stanford, California: Addison-Wesley Publishing Company. ISBN:0-201-0023-7
- Malik, D. S. (2010). Data Structures Using C++ (2nd Ed.). Cambridge, Massachusetts: Course Technology. ISBN-13: 978-0-324-78201-1
 - Cormen, T.H., Leiserson, C.E., Rivest, R.L., Stein, C. (2009). Introduction to Algorithms, 3rd Edition, Cambridge, Massachusetts: The MIT Press
 - Drozdek, A. (2000). Data Structures and Algorithms in C++, Second Edition 2nd Edition, Cambridge, Massachusetts: Course Technology
 - Weiss, M. A. (2007). Data structures and algorithm analysis in C++, 3/E, (3rd Ed.). Boston, Massachusetts: Addison Wesley
 - Gilberg, R. F., & Behrouz A. F. (2005). Data structures - A pseudocode approach with C (2nd Ed.). Boston, Massachusetts: Thomson Course Technology
 - Sedgewick, R. (1998). Algorithms in C++ (3rd Ed.).
 Boston, Massachusetts: Addison-Wesley.



Week	Topics		
1.	 Introduction to Data Structures 		
	Design and Analysis of Algorithms		
2.	Basic Data Types		
3.	• Stacks		
	Final Project: Idea - consultation		
4.	Queues		
5.	• Trees		
6.	• Sets		
	• Quiz		
7.	Advanced Set Representation		
	Final Project: Proposal -		
	presentation		
8.	Directed Graphs		
9.	Undirected Graphs		
10.	Sorting and Searching		
11.	 Algorithm Analysis Techniques 		
12.	Algorithm Design Techniques		
	• Quiz		
13.	Final Project Presentation		



Assessment

No.	Components	Percentage	Course Intended
	•		Learning Outcomes
1.	Quizzes	20 %	LO 1, LO 2, LO 3
	Assignments	10 %	LO 1, LO 2
3.	Laboratory	20 %	LO 2, LO 3, LO 4
4.	Project	30 %	LO 2, LO 3, LO 4, LO 6
5.	Final Examination	20 %	LO 1, LO 2, LO 3, LO 5



Project (Final Project)

To be announced (TBA)





Questions?

Form The Groups

- 2-3 students (max. 3)
- Group:
 - Final Project
 - Group assignment(s)
 - Discussions



Weekly Group Presentation

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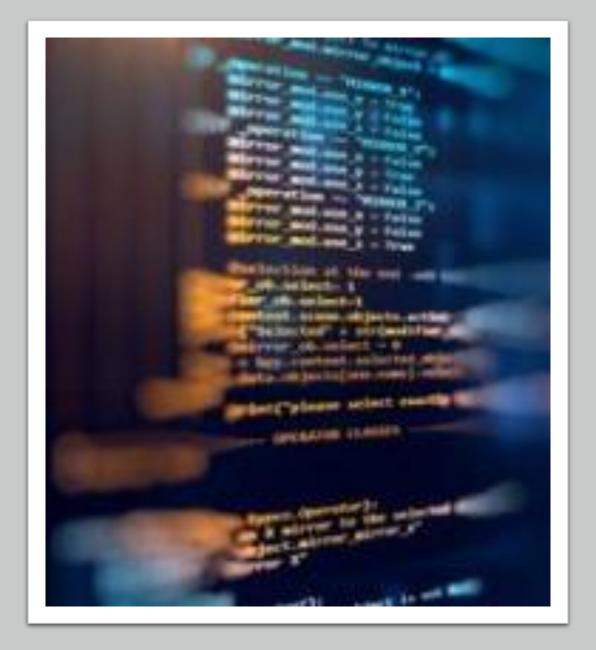
Topics

- Introduction to Data Structures
- Introduction to Analysis of Algorithm



Introduction

- Without software a computer is of no use
- It is the software that enables you to do things that were, perhaps, fiction a few years ago
- However, software is not created overnight.
- From the time a software program is conceived until it is delivered, it goes through several phases.
- There is a branch of computer science, called software engineering, which specializes in this area



Software Life Cycle

- A program goes through many phases from the time it is first conceived until the time it is retired, called the *life cycle* of the program.
- The three fundamental stages through which a program goes are:
 - · development,
 - use,
 - and maintenance.
 - the program is modified to fix the (identified) problems and/or to enhance it



When a program is considered too expensive to maintain, the developer might decide to retire the program and no new version of the program will be released.

Software Development Phase

- The software development phase is the first and perhaps most important phase of the software life cycle.
- A program that is well developed will be easy and less expensive to maintain.
- Software engineers typically break the software development process into the following four phases:
 - Analysis
 - Design
 - Implementation
 - Testing and debugging





Discussion – 10 minutes

- What do you think of these phases (what you need to do?)
 - Analysis
 - Design
 - Implementation
 - Testing and debugging





Data Structures vs Algorithms

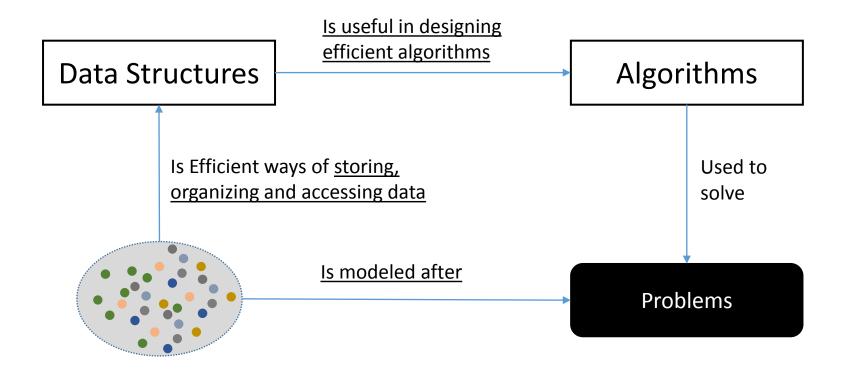
Data Structures

- Efficient ways of <u>storing</u>, <u>organizing and accessing data</u>
- "how to store, organize and access data"

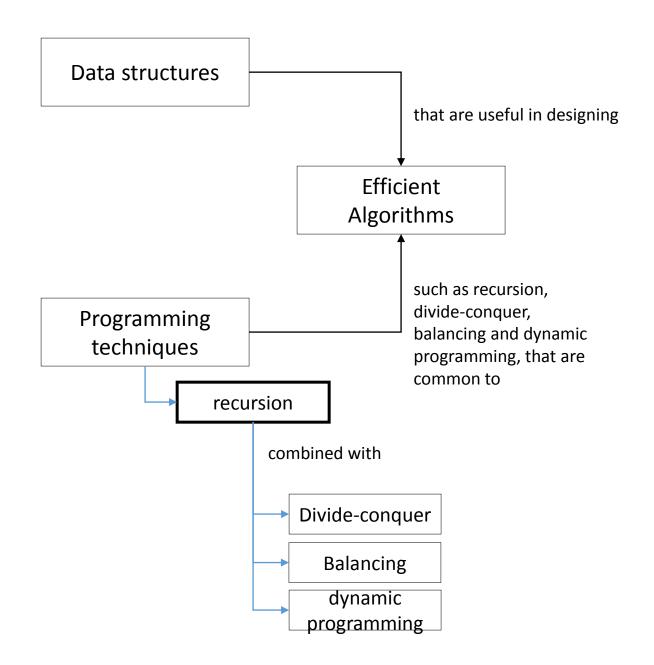
Algorithms

- Step by step method to solve a problem
- "how to solve problem using step by step method"
- So, eventhough Data Structures often comes together with Algorithms, such as Data Structures and Algorithms, but
 - BY ABSTRACTION, Data Structures is different than Algorithms
 - Data structures are useful in designing efficient algorithms











From Problem to Program

- 6 steps that you should follow in order to solve a problem:
 - 1. Understand the Problem
 - Formulate a Model
 - 3. Develop an Algorithm
 - 4. Write the Program
 - 5. Test the Program
 - 6. Evaluate the Solution

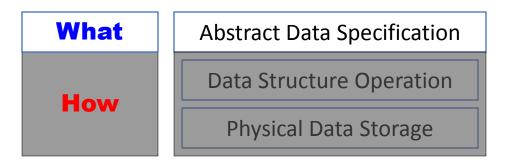




Abstract Data Types

- Definitions
 - An abstract data type (ADT) is a collection of related data items together with basic relations between them and operations to be performed on them.
- Why "abstract?" Data, operations, and relations are studied independently of how they are going to be implemented.

What not How





Example of ADT: List

- List: A collection of elements of the same type.
- The length of a list is the number of elements in the list.
- **Operations** on a list:
 - Create the list. The list is initialized to an empty state.
 - Determine whether the list is empty.
 - Determine whether the list is full.
 - Find the size of the list.
 - Destroy, or clear, the list.
 - Determine whether an item is the same as a given list element.
 - Insert an item in the list at the specified location.
 - Remove an item from the list at the specified location.
 - Replace an item at the specified location with another item.
 - Retrieve an item from the list from the specified location.
 - Search the list for a given item.



An implementation of an ADT

- An implementation of an ADT consists of storage structures (commonly called data structures) to store the data items and algorithms for the basic operations and relations.
- ADT is a way of thinking about Data Abstraction: Separating the definition of a data type from its implementation.
 - An important concept in software design.
 - Usually the storage structures / data structures used in implementation are those provided in a language or built from them.

Good reference:

https://www.cs.odu.edu/~zeil/cs330/latest/Public/implementingADTS/index.html



ADT and Data Structures

- The terms abstract data type and data structure are often used interchangeably.
- However, we will use abstract data type when data is studied at a logical or conceptual level, independent of any programming language or machine considerations.
- The term data structure refers to a construct in some programming language that can be used to store data.



Header Files and Template

- Traditionally, definitions of member functions have been put in an implementation file ClassName.cpp corresponding to the class' header file.
- This is done to enforce data abstraction separating the interface of the ADT from its implementation details.
 - (Unfortunately, the class data members, which store data and are therefore part of the implementation, must be in the .h file.)
- With the increasing use of templates, however, this practice is becoming less common because current compiler technology doesn't permit this split for templates — everything has to be in the same file.
 - Thus the reason for <u>dropping the ".h" from standard class libraries</u>.
 - They're really class-template libraries, and there are therefore no corresponding ".cpp" files.



Steps of Working with Data Structures

- Step 1:
 - Understand the problem and think about the suitable data structure
- Step 2:
 - Define the ADT, that is the specification of the data structure (valid value and operation)
- Step 3:
 - Select the low-level storage: Arrays or Linked List
- Step 4:
 - Implement the ADT (the structured data and operation on the data)
- Step 5:
 - Analyze the algorithm complexity of the operations (worst case analysis)



Algorithm Analysis

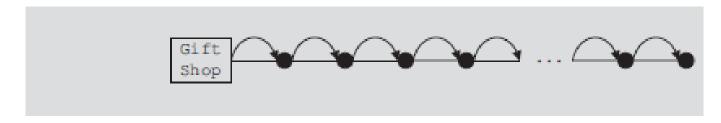
- Just as a problem is analyzed before writing the algorithm and the computer program, after an algorithm is designed it should also be analyzed.
 - Usually, there are <u>various ways to design a particular algorithm</u>.
 - **Speed**: certain algorithms take very little computer time to execute, whereas others take a considerable amount of time.
 - **Space**: certain algorithms take more memory to store the data while executing the program, whereas others take a less memory.



- Just as a problem is analyzed before writing the algorithm and the computer program, after an algorithm is designed it should also be analyzed.
- Usually, there are various ways to design a particular algorithm.
- Certain algorithms take very little computer time to execute, whereas others take a considerable amount of time.

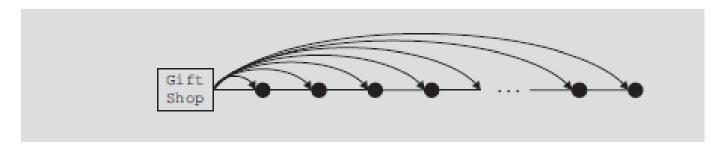


- 50 packages are to be delivered to 50 different houses.
- The shop, while making the route, finds that the 50 houses are one mile apart and are in the same area.



Therefore, the total distance traveled by the driver to deliver the packages and then getting back to the shop is:

FIGURE 1-2 Package delivering scheme



2 . (1+2+3+...+50) = 2550 miles

50 + 50 = 100 miles

FIGURE 1-3 Another package delivery scheme



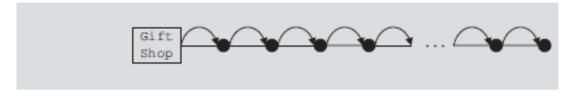


FIGURE 1-2 Package delivering scheme

Therefore, the total distance traveled by the driver to deliver the packages and then getting back to the shop is:

50 + 50 = 100 miles

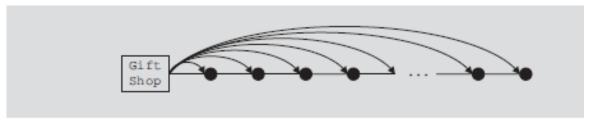


FIGURE 1-3 Another package delivery scheme

2. (1+2+3+...+50) = 2550 miles

- First method = 1 + 1 + ... + 1 + n = 2n
- Second method = 2 . (1+2+3+...+n) = 2 . $(n(n+1)/2) = n^2+n$



Algorithm Analysis: The Big-O Notation - Example

```
Assume that
                                                        //Line 1
cout << "Enter two numbers";
                                                                    all variables
cin >> num1 >> num2;
                                                        //Line 2
                                                                    are properly
                                                                    declared
                                                        //Line 3
if (num1 >= num2)
                                                        //Line 4
    max = num1;
                                                        //Line 5
else
    max = num2;
                                                        //Line 6
cout << "The maximum number is: " << max << endl;
                                                       //Line 7
```

- Line 1 has one operation, <<;
- Line 2 has two operations;
- Line 3 has one operation, >=;
- Line 4 has one operation, =;
- Line 6 has one operation;
- and Line 7 has three operations.
- Either Line 4 or Line 6 executes.
- Therefore, the total number of operations executed in the preceding code is 1 + 2 + 1 + 1 + 3 = 8. In this algorithm, the number of operations executed is fixed.



f(n)

TABLE 1-2 Growth rates of various functions

п	log ₂ n	n log ₂ n	n²	2 "
1	0	0	1	2
2	1	2	4	4
4	2	8	16	16
8	3	24	64	256
16	4	64	256	65,536
32	5	160	1024	4,294,967,296



TABLE 1-2 Growth rates of various functions

п	log ₂ n	n log ₂ n	n²	2 ⁿ
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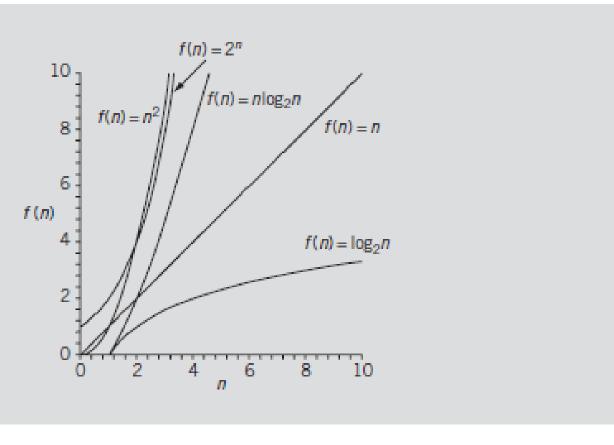


FIGURE 1-4 Growth rate of various functions

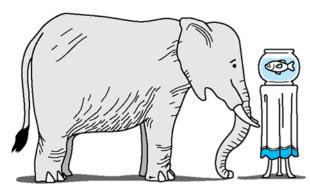


The Big-O Notation

Big-O notation is a notation that expresses computing time (complexity)
as the term in a function that increases most rapidly relative to the size of
a problem.

$$f(n) = n^4 + 100n^2 + 10n + 50$$

- f(n) is of order n^4 —or, in **Big-O notation**, $O(n^4)$.
 - When we compare algorithms using Big-O, we are concerned with what happens when *n* is "large" (asymptotic)





Dominant Operations

- While analyzing a particular algorithm, we usually count the number of operations performed by the algorithm.
- Usually, in an algorithm, certain operations are dominant.
- Consider the functions $g(n) = n^2$ and $f(n) = n^2 + 4n + 20$.
 - Clearly, the function g does not contain any linear term, that is, the coefficient of n in g is zero
 - As n becomes larger and larger the term 4n + 20 in f(n) becomes insignificant, and the term n^2 becomes the dominant term.

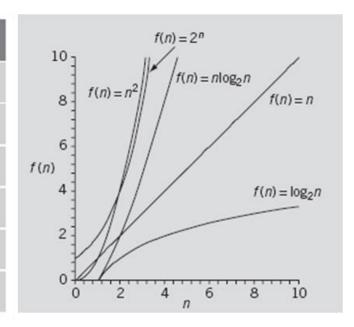
п	$g(n) = n^2$	$f(n)=n^2+4n+20$
10	100	160
50	2500	2720
100	10,000	10,420
1000	1,000,000	1,004,020
10,000	100,000,000	100,040,020



Asymptotic Growth Rate

- For large values of n, we can predict the behavior of f(n) by looking at the behavior of g(n).
- In algorithm analysis, if the complexity of a function can be described by the complexity of a quadratic function without the linear term, we say that the function is of $O(n^2)$, called Big-O of n^2 .

п	log ₂ n	n log ₂ n	n²	2"
1	0	0	1	2
2	1	2	2	4
4	2	8	16	16
8	3	24	64	256
16	4	64	256	65,536
32	5	160	1024	4,294,967,296





- Exercise 15 minutes
 - Consider the following code, where m and n are int variables and their values are nonnegative:

```
for (int i = 0; i < m; i++) //Line 1
for (int j = 0; j < n; j++) //Line 2
cout << i * j << endl; //Line 3
```

• Big-O?



TABLE 1-5 Some Big-O functions that appear in algorithm analysis

Function g(n)	Growth rate of $f(n)$
g(n) = 1	The growth rate is constant and so does not depend on \emph{n} , the size of the problem.
$g(n) = \log_2 n$	The growth rate is a function of $\log_2 n$. Because a logarithm function grows slowly, the growth rate of the function f is also slow.
g(n) = n	The growth rate is linear. The growth rate of f is directly proportional to the size of the problem.
$g(n) = n \log_2 n$	The growth rate is faster than the linear algorithm.
$g(n) = n^2$	The growth rate of such functions increases rapidly with the size of the problem. The growth rate is quadrupled when the problem size is doubled.
$g(n)=2^n$	The growth rate is exponential. The growth rate is squared when the problem size is doubled.



CPP / C++

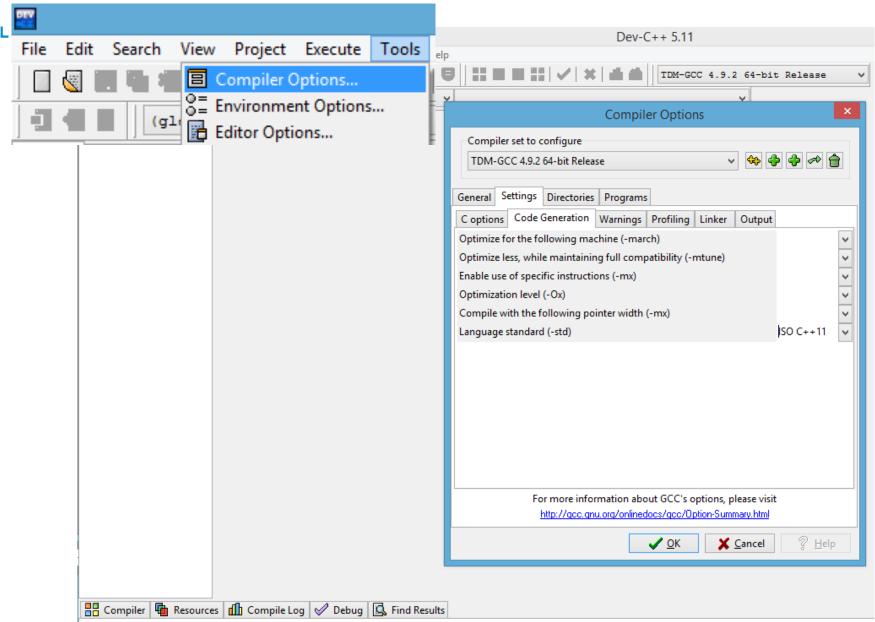


IDE

- Dev-C++ (download: https://sourceforge.net/projects/orwelldevcpp/)
- NetBeans
- Visual Studio (Express)
- Eclipse
- Xcode
- Etc...

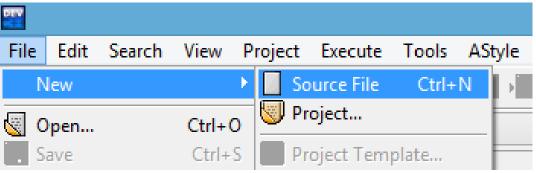


Dev-C++ (choose language standard)





Develop your own C++



stream	description
cin	standard input stream
cout	standard output stream
cerr	standard error (output) stream
clog	standard logging (output) stream

cout << "Hello"; // prints Hello
cout << Hello; // prints the content of variable Hello</pre>

int age; cin >> age;



Develop your own C++

Case sensitive

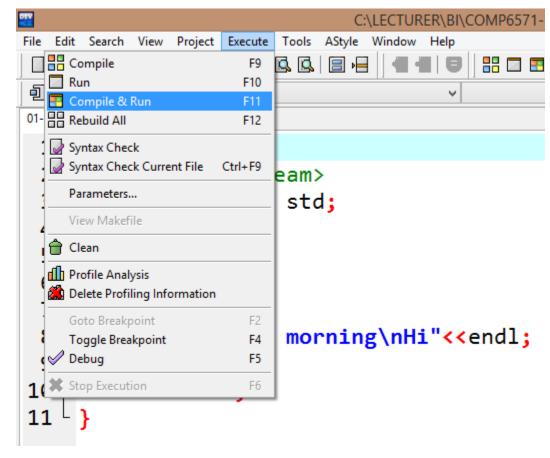
Program Structure



#include <iostream>

Lines beginning with a hash sign (#) are directives read and interpreted by what is known as the *preprocessor*. They are special lines interpreted before the compilation of the program itself begins. In this case, the directive #include <iostream>, instructs the preprocessor to include a section of standard C++ code, known as *header iostream*, that allows to perform standard input and output operations

```
// my first C++
#include <iostream>
int main()
{
    std::cout<<"Good morning";
}</pre>
```





```
// my first C++
    #include <iostream>
    using namespace std;
    int main()
5 ₽ {
6
        int a=100;
        cout<<"Good morning\nHi"<<endl;</pre>
        cout<<a;
                          Good morning
Hi
10
        return 0;
11
                          100
                          Process exited after 0.03047 seconds with return value 0
                           Press any key to continue . . .
```

Why??? What it means?

- Using namespace std;
- \n
- endl
- return 0;





Classes



Classes

- OOD (OO Design), the first step is to identify the components called objects; an object combines data and the operations on that data in a single unit, called encapsulation.
- In C++, the mechanism that allows you to combine data and the operations on that data in a single unit is called a class.
- A class is a collection of a fixed number of components.
- The components of a class are called the members of the class.

The general syntax for defining a class is

```
class classIdentifier
{
    class members list
};
```



Unified Modelling Language Diagrams

- A class and its members can be described graphically using a notation known as Unified Modeling Language (UML) notation.
- For example, Figure 1-5 shows the UML class diagram of the class clockType.

```
clockType

-hr: int
-min: int
-sec: int

+setTime(int, int, int): void
+getTime(int&, int&, int&) const: void
+printTime() const: void
+incrementSeconds(): int
+incrementMinutes(): int
+incrementHours(): int
+equalTime(clockType) const: bool
+clockType(int, int, int)
+clockType()
```

FIGURE 1-5 UML class diagram of the class clockType



Class

```
keyword
              user-defined name
  class ClassName
                            //can be private, public or protected
     Access specifier:
                            // Variables to be used
     Data members;
     Member Functions() { } //Methods to access data members
                            // Class name ends with a semicolon
```

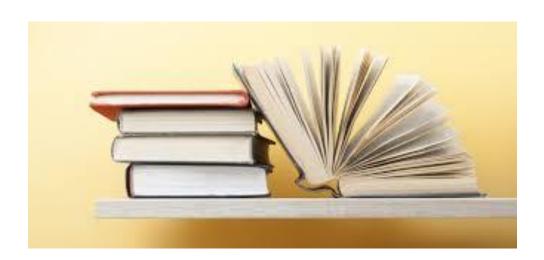


```
// Accessing of data
 2
    #include <bits/stdc++.h>
    using namespace std;
                                                      18
    class HiHo
                                                           int main()
 6 □ {
                                                       20 □ {
        // Access specifier
                                                               // Declare an object of class HiHo
                                                       21
         public:
                                                       22
                                                               HiHo obj1;
            // Data Members
                                                       23
10
             string abc;
                                                               // accessing data member
                                                       24
11
                                                               obj1.abc = "Hello Data Structure";
12
             // Member Functions()
                                                       26
             void printname()
13
                                                       27
                                                               // accessing member function
14 🗎
                                                       28
                                                               obj1.printname();
                cout << "Good afternoon: " << abc;</pre>
15
                                                       29
                                                               return 0;
16
17 L
                                                       30
```



Further readings

- 00
 - Private
 - Protected
 - Public
- Constructors
- Structs
- Destructors
- Data abstraction
 - ADT (abstract data type)
 - domain
 - set of operations
- Identifying Classes, Objects, and Operations





Exercise

1. Consider the following function

```
int funcExercise7(int list[], int size)
{
  int sum = 0;
  for (int index = 0; index < size; index++)
      sum = sum + list[index];
  return sum;
}</pre>
```

Find the number of operations executed by the function funcExercise7 if the value of size is 10!

- 2. Please create C++ code using Class to create this output
 - Enter "sun", output = "Good Morning"
 - Enter "moon", output = "Good Night"

```
Please enter your magic word = sun
Good Morning
-----
Process exited after 2.588 seconds with return value 0
Press any key to continue . . . _
```

```
Please enter your magic word = moon
Good Night
-----
Process exited after 2.332 seconds with return value Ø
Press any key to continue . . .
```



Thank you



FYI



Constructors

Constructors

C++ does not automatically initialize variables when they are declared. Therefore, when an object is instantiated, there is no guarantee that the data members of the object will be initialized. To guarantee that the instance variables of a class are initialized, you use constructors. There are two types of constructors: with parameters and without parameters. The constructor without parameters is called the **default constructor**.

Constructors have the following properties:

- The name of a constructor is the same as the name of the class.
- A constructor, even though it is a function, has no type. That is, it is neither a value-returning function nor a void function.
- A class can have more than one constructor. However, all constructors of a class have the same name.
- If a class has more than one constructor, the constructors must have different formal parameter lists. That is, either they have a different number of formal parameters or, if the number of formal parameters is the same, the data type of the formal parameters, in the order you list, must differ in at least one position.
- Constructors execute automatically when a class object enters its scope.
 Because they have no types, they cannot be called like other functions.
- Which constructor executes depends on the types of values passed to the class object when the class object is declared.



Constructors

Let us extend the definition of the class clockType by including two constructors:

```
class clockType
public:
    //Place the function prototypes of the functions setTime,
    //qetTime, printTime, incrementSeconds, incrementMinutes,
    //incrementHours, and equalTime as described earlier, here.
    clockType(int hours, int minutes, int seconds);
      //Constructor with parameters
      //The time is set according to the parameters.
      //Postconditions: hr = hours; min = minutes; sec = seconds
      //
            The constructor checks whether the values of hours,
            minutes, and seconds are valid. If a value is invalid,
            the default value 0 is assigned.
    clockType();
      //Default constructor with parameters
      //The time is set to 00:00:00.
      //Postcondition: hr = 0; min = 0; sec = 0
private:
    int hr; //stores the hours
    int min; //store the minutes
    int sec; //store the seconds
};
```



Identifying Classes, Objects, and Operations

The hardest part of OOD is to identify the classes and objects. This section describes a common and simple technique to identify classes and objects.

We begin with a description of the problem and then identify all of the nouns and verbs. From the list of nouns we choose our classes, and from the list of verbs we choose our operations.

For example, suppose that we want to write a program that calculates and prints the volume and surface area of a cylinder. We can state this problem as follows:

Write a program to input the dimensions of a cylinder and calculate and print its surface area and volume.

In this statement, the nouns are bold and the verbs are italic. From the list of nouns program, dimensions, cylinder, surface area, and volume—we can easily visualize cylinder to be a class—say, cylinderType—from which we can create many cylinder objects of various dimensions. The nouns—dimensions, surface area, and volume are characteristics of a cylinder and, thus, can hardly be considered classes.

After we identify a class, the next step is to determine three pieces of information:

- Operations that an object of that class type can perform
- · Operations that can be performed on an object of that class type
- · Information that an object of that class type must maintain

From the list of verbs identified in the problem description, we choose a list of possible operations that an object of that class can perform, or has performed, on itself. For example, from the list of verbs for the cylinder problem description—write, input, calculate, and print—the possible operations for a cylinder object are input, calculate, and print.

For the cylinderType class, the dimensions represent the data. The center of the base, radius of the base, and height of the cylinder are the characteristics of the dimensions. You can input data to the object either by a constructor or by a function.



Identifying Classes, Objects, and Operations

The verb calculate applies to determining the volume and the surface area. From this, you can deduce the operations: cylinderVolume and cylinderSurfaceArea. Similarly, the verb print applies to the display of the volume and the surface area on an output device.

Identifying classes via the nouns and verbs from the descriptions to the problem is not the only technique possible. There are several other OOD techniques in the literature.



big-O

$$O(g(n)) = \{f(n) : \text{ there exist positive constants } c \text{ and } n_0 \text{ such that } 0 \le f(n) \le cg(n) \text{ for all } n \ge n_0 \}$$
.

Alternatively, we say

$$f(n) = O(g(n))$$
 if there exist positive constants c and n_0 such that $0 \le f(n) \le cg(n)$ for all $n \ge n_0$

Informally, f(n) = O(g(n)) means that f(n) is asymptotically less than or equal to g(n).

- Each of the following expressions represents the number of operations for certain algorithms. What is the order of each of these Big-O expressions?
 - $n^2 + 3n + 5$
- Answer
 - Let $f(n) = n^2 + 3n + 5$ and $g(n) = n^2$
 - Now, $n^2+3n+5 \le n^2 + n^2 \le 2 n^2$. Hence $f(n) = O(n^2)$



Exercises: Algorithm Analysis

 Each of the following expressions represents the number of operations for certain algorithms. What is the order of each of these Big-O expressions?

```
a. 1

a. 6n + 4

b. 5n^2 + 2n + 8

c. (n^2 + 1) (3^n + 5)

d. 5(6^n + 4)

d. log(n + 4)

d. nlog(n)
```

• Write a function that uses a loop to find the sum of the squares of all integers between 1 and n. What is the order of your function?