

Connected Stocks: Evidence from Tehran Stock Exchange

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- 1 Motivation
- 2 Literature
 - Common-ownership measurements
 - Main Effect
- 3 Empirical Studies
 - Measuring Common-ownership
 - Correlation Calculation
 - Controls
- 4 Methodology
- 5 Results
 - Normalized Rank-Transformed
 - Discontinuity
- 6 Correlated trading
- 7 Conclusion

- **Can the common ownership cause stock return comovement ?**
 - We connect stocks through the common ownership by blockholders (ownership $> 1\%$)
 - We focus on excess return comovement for a pair of the stocks
 - We use common ownership to forecast cross-sectional variation in the realized correlation of four-factor + industry residuals

Why does it matter?

- Covariance

- Covariance is a key component of risk in many financial applications.
(Portfolio selection, Risk management, Hedging and Asset pricing)
- Covariance is a significant input in risk measurement models
(Such as Value-at-Risk)

- Return predictability

- If it's valid, we can build a profitable buy-sell strategy

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Common-ownership measurements

Model based measures

- $HJL^A(A, B) = \sum_{i \in I^{A,B}} \frac{\alpha_{i,B}}{\alpha_{i,A} + \alpha_{i,B}}$

Harford et al. (2011)

- $MHHI = \sum_j \sum_k s_j s_k \frac{\sum_i \mu_{ij} \nu_{ik}}{\sum_i \mu_{ij} \nu_{ij}}$

Azar et al. (2018)

- $Top5_j = \frac{1}{n-1} \sum_i^5 \sum_{j \neq k} \nu_{ik}$

Antón et al. (2020)

- $\kappa_{ij} = \cos(\nu_i, \nu_j) \cdot \sqrt{\frac{IHHI_j}{IHHI_i}}$

Backus et al. (2020)

- $GGL^A(A, B) = \sum_{i=1}^I \alpha_{i,A} g(\beta_{i,A}) \alpha_{i,B}$

Gilje et al. (2020) , Lewellen and Lewellen (2021)

- $MHHI_{\text{Delta}} = \sum_{j=1}^J \sum_{k \neq j}^K \frac{\sum_{i=1}^N w_j * w_k * \mu_{i,j} * \mu_{i,k}}{\sum_{i=1}^N \mu_{i,j} * \mu_{i,k}}$

Lewellen and Lowry (2021)

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Backus et al. (2020)
- $GGL^A(A, B) = \sum_{i=1}^I \alpha_{i,Ag}(\beta_{i,A}) \alpha_{i,B}$
Gilje et al. (2020) , Lewellen and Lewellen (2021)
- $MHHI_{Delta} = \sum_{j=1}^J \sum_{k \neq j}^K \frac{\sum_{i=1}^N w_j * w_k * \mu_{i,j} * \mu_{i,k}}{\sum_{i=1}^N \mu_{i,j} * \mu_{i,k}}$
Lewellen and Lowry (2021)

Ad-hoc measures

- $Overlap_{AP}(A, B) = \sum_{i \in I^{A,B}} \alpha_{i,A} \frac{\bar{\nu}_A}{\bar{\nu}_A + \bar{\nu}_B} + \alpha_{i,B} \frac{\bar{\nu}_B}{\bar{\nu}_A + \bar{\nu}_B}$
Anton and Polk (2014)
- $Overlap_{Count}(A, B) = \sum_{i \in I^{A,B}} 1$
He and Huang (2017), He et al. (2019)
- $Overlap_{Min}(A, B) = \sum_{i \in I^{A,B}} \min\{\alpha_{i,A}, \alpha_{i,B}\}$
Newham et al. (2018)
- $Overlap_{HL}(A, B) = \sum_{i \in I^{A,B}} \alpha_{i,A} \times \sum_{i \in I^{A,B}} \alpha_{i,B}$
Hansen and Lott Jr (1996) , Freeman (2019)

Common-ownership measurements

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Hansen and Lott Jr (1996) , Freeman (2019)

Selected measure

We need a pair-level measure, which is bi-directional, so we use the AP measure.

Measures' detail

Main effect

Comovement effect

Papers

Main effect

Common-ownership

Comovement effect

Papers

Main effect



Papers

Main effect



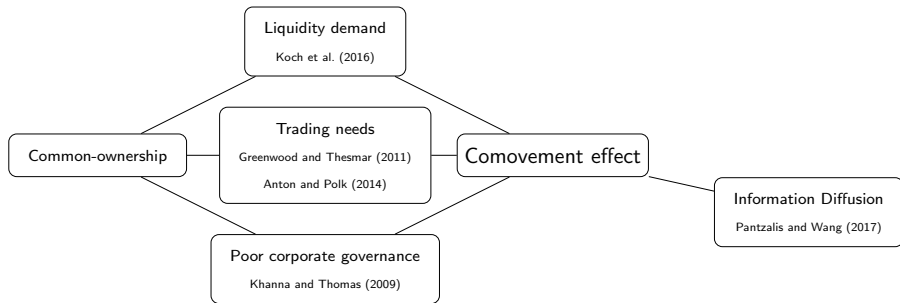
Papers

Main effect



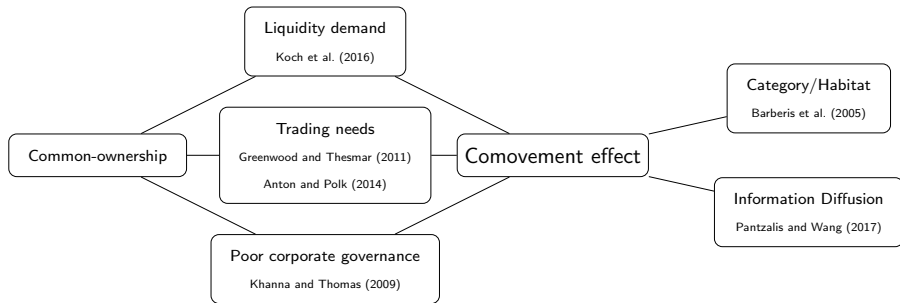
Papers

Main effect



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Papers

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Measuring Common-ownership

Anton and Polk (2014)

$$FCAP_{ij,t} = \frac{\sum_{f=1}^F (S_{i,t}^f P_{i,t} + S_{j,t}^f P_{j,t})}{S_{i,t} P_{i,t} + S_{j,t} P_{j,t}}$$

Measuring Common-ownership

Anton and Polk (2014)

$$FCAP_{ij,t} = \frac{\sum_{f=1}^F (S_{i,t}^f P_{i,t} + S_{j,t}^f P_{j,t})}{S_{i,t} P_{i,t} + S_{j,t} P_{j,t}}$$

SQRT

$$\left[\frac{\sum_{f=1}^F (\sqrt{S_{i,t}^f P_{i,t}} + \sqrt{S_{j,t}^f P_{j,t}})}{\sqrt{S_{i,t} P_{i,t}} + \sqrt{S_{j,t} P_{j,t}}} \right]^2$$

Quadratic

$$\left[\frac{\sum_{f=1}^F [(S_{i,t}^f P_{i,t})^2 + (S_{j,t}^f P_{j,t})^2]}{(S_{i,t} P_{i,t})^2 + (S_{j,t} P_{j,t})^2} \right]^{-1}$$

Measuring Common-ownership

Anton and Polk (2014)

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SQRT

$$\left[\frac{\sum_{f=1}^F (\sqrt{S_{i,t}^f P_{i,t}} + \sqrt{S_{j,t}^f P_{j,t}})}{\sqrt{S_{i,t} P_{i,t}} + \sqrt{S_{j,t} P_{j,t}}} \right]^2$$

Quadratic

$$\left[\frac{\sum_{f=1}^F [(S_{i,t}^f P_{i,t})^2 + (S_{j,t}^f P_{j,t})^2]}{(S_{i,t} P_{i,t})^2 + (S_{j,t} P_{j,t})^2} \right]^{-1}$$

Intuition

If for a pair of stocks with n mutual owners, all owners have even shares of each firm's market cap, then the proposed indexes will be equal to n . [Proof](#)

Measuring Common Ownership

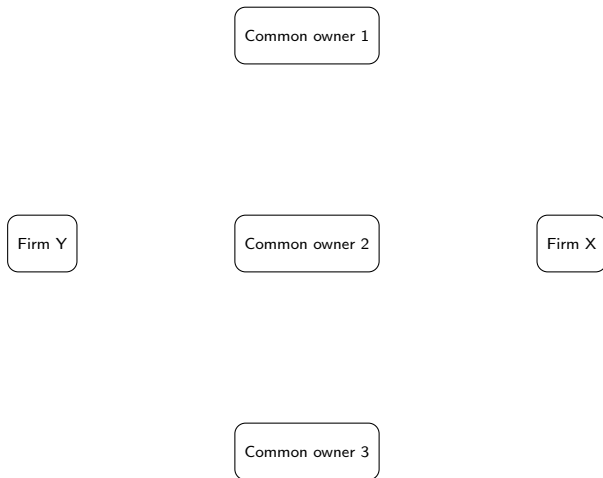
Example of three common owner

Firm Y

Firm X

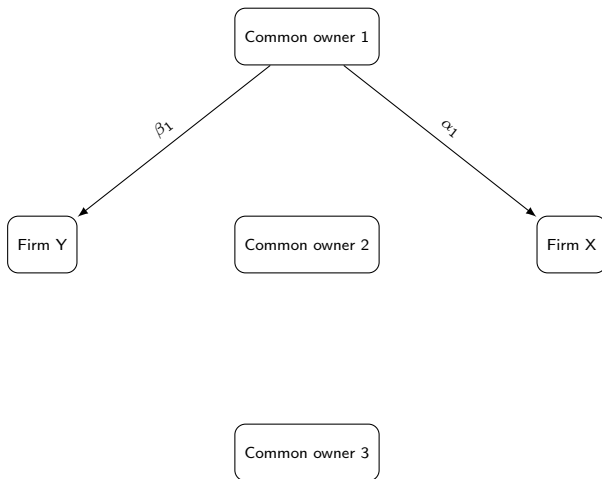
Measuring Common Ownership

Example of three common owner



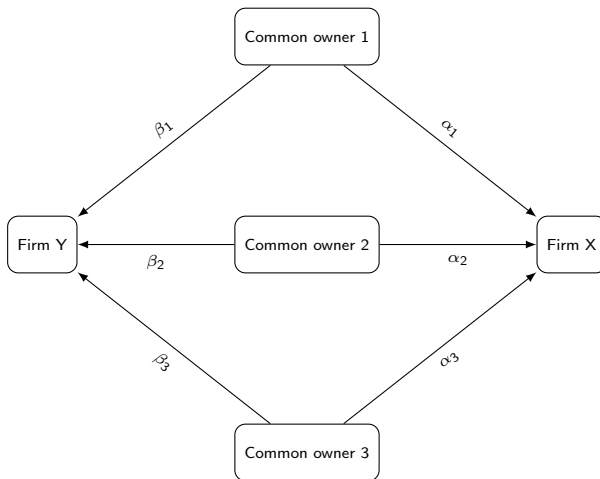
Measuring Common Ownership

Example of three common owner



Measuring Common Ownership

Example of three common owner



Measuring Common Ownership

Example of three common owner

Ownership	Type I	Type II	Type III	Type IV	Type V	Type VI	Type VII
α_1	1/3	20	10	20	10	5	1
β_1	1/3	10	10	20	10	5	1
α_2	1/3	10	80	20	10	5	1
β_2	1/3	20	80	20	10	5	1
α_3	1/3	70	10	20	10	5	1
β_3	1/3	70	10	20	10	5	1
SQRT	3	2.56	2.33	1.8	0.9	0.45	0.09
SUM	1	1	1	0.6	0.3	0.15	0.03
Quadratic	3	1.85	1.52	8.33	33.33	133.33	3333.33

Measuring Common Ownership

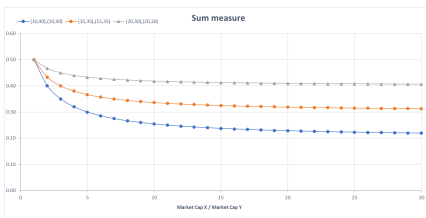
Comparison

- For better comparison we relax previous assumptions:
 - Two Firms with different market caps.

$\frac{\text{MarketCap}_x}{\text{MarketCap}_y}$	$(\alpha_1, \beta_1), (\alpha_2, \beta_2)$					
	$(10,40), (10,40)$		$(15,35), (15,35)$		$(20,30), (20,30)$	
	SQRT	SUM	SQRT	SUM	SQRT	SUM
1	0.90	0.50	0.96	0.50	0.99	0.50
2	0.80	0.40	0.89	0.43	0.96	0.47
3	0.75	0.35	0.85	0.40	0.94	0.45
4	0.71	0.32	0.83	0.38	0.92	0.44
5	0.69	0.30	0.81	0.37	0.91	0.43
6	0.67	0.29	0.80	0.36	0.91	0.43
7	0.65	0.28	0.79	0.35	0.90	0.43
8	0.64	0.27	0.78	0.34	0.90	0.42
9	0.63	0.26	0.77	0.34	0.89	0.42
10	0.62	0.25	0.76	0.34	0.89	0.42

Measuring Common Ownership

Comparison



Comparison of two methods for calculating common ownership

Conclusion

We use the SQRT measure because it has an acceptable variation and has fair values at a lower level of aggregate common ownership.

Pair Composition and Business Group

Business Group

Ultimate Owner

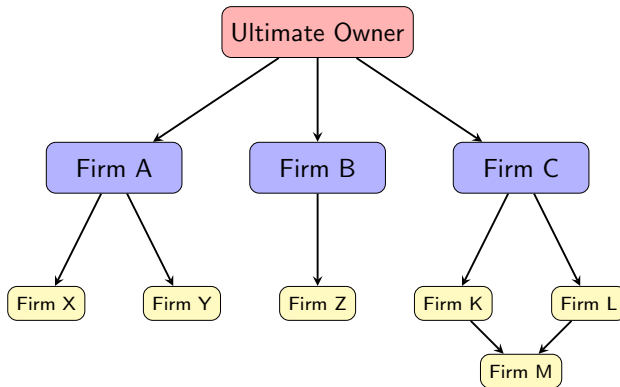
Pair Composition and Business Group

Business Group



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Business Group



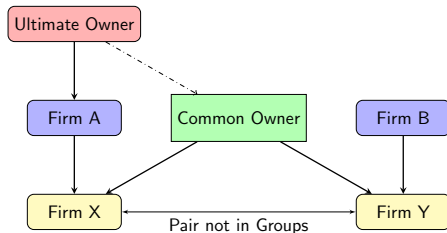
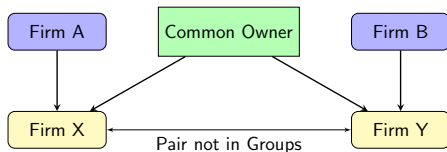
Pair Composition and Business Group

Pair in the Business Group



Pair Composition and Business Group

Pair not in any of Business Groups



Data Summary

- We use blockholders' data from 2014/03/25 (1393/01/06) to 2020/03/18 (1398/12/28)
 - Includes of 1203 Days and 60 Months
 - Consists of 618 firm including 562 firm with common owners

Year	1393	1394	1395	1396	1397	1398
No. of Firms	365	376	447	552	587	618
No. of Blockholders	777	803	984	1297	1454	1458
No. of Groups	38	41	43	44	40	43
No. of Firms not in Groups	116	108	147	216	241	243
No. of Firms in Groups	249	268	300	336	346	375
Mean Number of Members	7	7	7	8	9	9
Med. of Number of Members	5	5	5	6	6	5
Mean Of each Blockholder's ownership	21	22	22	21	22	23
Med. of Owners' Percent	7	8	8	8	8	9
Mean Number of Owners	5	5	5	5	5	5
Med. Number of Owners	4	4	4	4	5	4
Mean Block. Ownership	76	77	75	75	75	71
Med. Block. Ownership	82	82	81	80	80	77

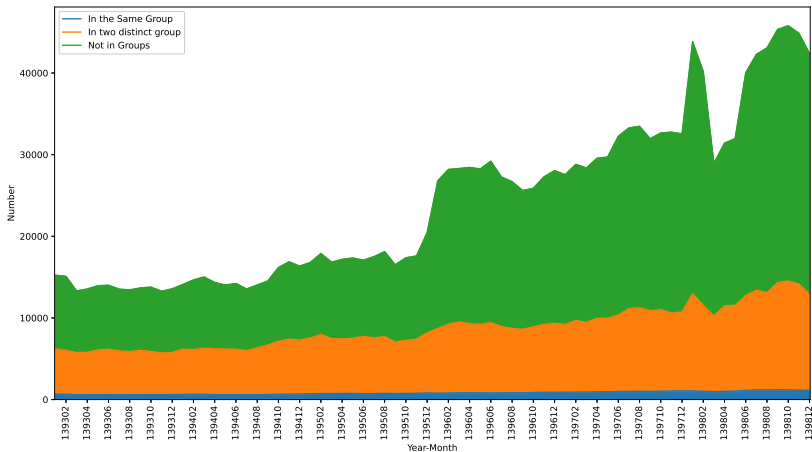
Pair Composition

- Pairs consist of two firms with at least one common owner
 - 93442 unique pairs which is 60% of possible pairs ($\frac{562 \times 561}{2} = 149878$)

	mean	min	Median	max
Number of unique paris	24139	13272	23024	45795

year	1393	1394	1395	1396	1397	1398
No. of Pairs	20876	21187	27784	41449	47234	67232
No. of Groups	37	40	42	43	39	43
No. of Pairs not in Groups	11452	11192	15351	26530	29182	43433
Number of Pairs not in the same Group	7962	8731	10971	12916	15366	20745
Number of Pairs in the same Group	923	955	1099	1260	1536	1774
Mean Number of Common owner	1	1	1	1	1	1
Med. Number of Common owner	1	1	1	1	1	1
Mean Percent of each blockholder	19	19	19	19	19	20
Med. Percent of each blockholder	13	12	12	12	12	14
Mean Number of Pairs in one Group	31	30	30	34	39	44
Med. Number of Pairs in one Group	8	10	8	10	9	10
Mean Number of Owners	5	5	5	5	4	5
Med. Number of Owners	5	5	5	5	4	5
Mean Block. Ownership	73	73	72	70	70	70
Med. Block. Ownership	73	73	73	71	71	71

Number of Pairs



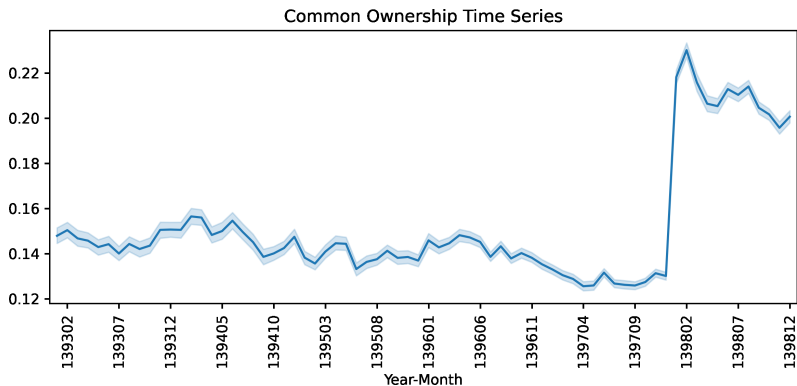
FCA vs. FCAP Summary

	variable	mean	std	min	25%	50%	75%	max
All	FCA	0.158	0.234	0.002	0.031	0.079	0.191	12.650
	FCAP	0.144	0.166	0.002	0.030	0.077	0.193	1.000
Same Group	FCA	0.474	0.478	0.005	0.096	0.367	0.691	6.174
	FCAP	0.346	0.265	0.004	0.081	0.321	0.561	1.000
Not Same Group	FCA	0.087	0.154	0.003	0.020	0.038	0.087	6.184
	FCAP	0.072	0.102	0.003	0.020	0.037	0.078	0.998
Same Industry	FCA	0.274	0.383	0.003	0.044	0.126	0.351	6.262
	FCAP	0.207	0.215	0.003	0.041	0.120	0.314	0.999
Not Same Industry	FCA	0.150	0.217	0.002	0.030	0.077	0.183	12.650
	FCAP	0.140	0.161	0.002	0.029	0.074	0.187	1.000

Results

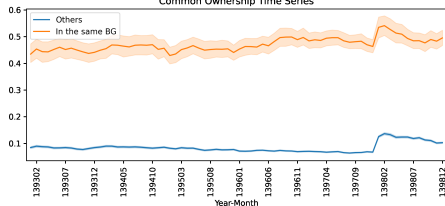
- By the proposed measurement, common ownership increases
- Common ownership is greater in pairs that are in the same business group and industry

FCA's time series

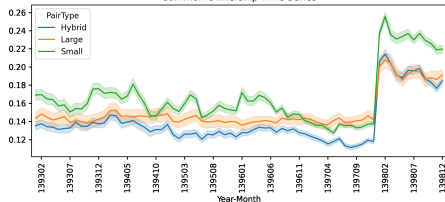


FCA's time series

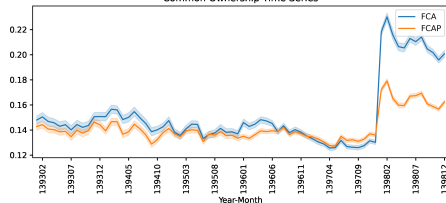
Common Ownership Time Series



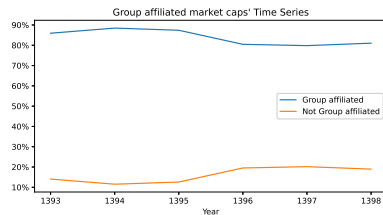
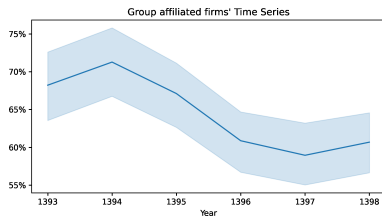
Common Ownership Time Series



Common Ownership Time Series



Group affiliated firm's time series



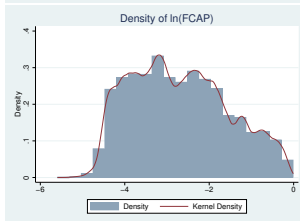
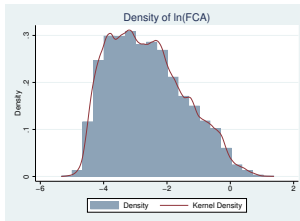
FCA vs. FCAP Distributions

Monthly



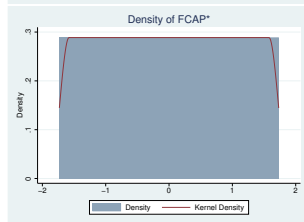
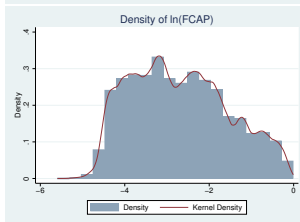
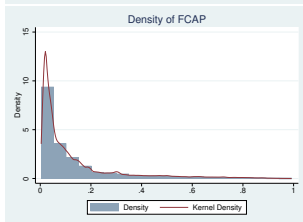
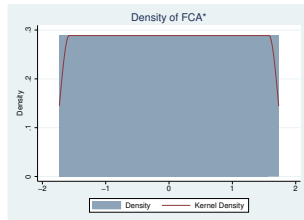
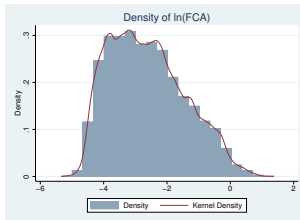
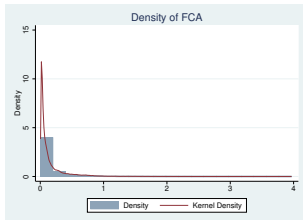
FCA vs. FCAP Distributions

Monthly



FCA vs. FCAP Distributions

Monthly



Correlation Calculation

4 Factor + Industry

1 First Step:

Estimate each of these models on periods of three month:

- CAPM + Industry (2 Factor):

$$R_{i,t} = \alpha_i + \beta_{mkt,i}R_{M,t} + \beta_{Ind,i}R_{Ind,t} + \boxed{\varepsilon_{i,t}}$$

- 4 Factor :

$$R_{i,t} = \alpha_i + \beta_{mkt,i}R_{M,t} + \beta_{HML,i}HML_t + \beta_{SMB,i}SMB_t + \beta_{UMD,i}UMD_t + \boxed{\varepsilon_{i,t}}$$

- 4 Factor + Industry (5 Factor) :

$$R_{i,t} = \alpha_i + \beta_{mkt,i}R_{M,t} + \beta_{Ind,i}R_{Ind,t} + \beta_{HML,i}HML_t + \beta_{SMB,i}SMB_t + \beta_{UMD,i}UMD_t + \boxed{\varepsilon_{i,t}}$$

2 Second Step:

Calculate monthly correlation of each stock pair's daily abnormal returns (residuals)

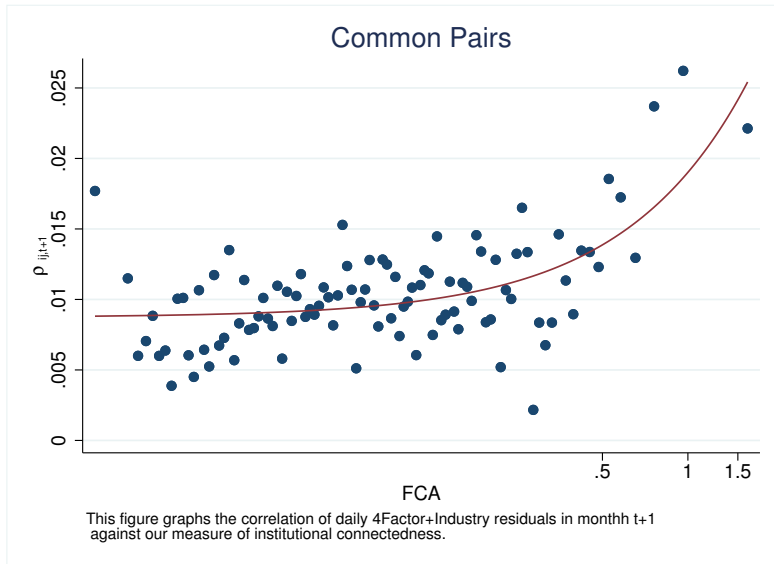
Correlation Calculation Results

	mean	std	min	25%	50%	75%	max
CAPM + Industry	0.021	0.200	-1.0	-0.047	0.016	0.084	1.0
4 Factor	0.032	0.202	-1.0	-0.040	0.025	0.096	1.0
4 Factor + Industry	0.016	0.199	-1.0	-0.051	0.010	0.076	1.0
4 Factor + Industry (With Lag)	0.015	0.198	-1.0	-0.051	0.010	0.076	1.0

Conclusion

We use the 4 Factor + Industry model to control for exposure to systematic risk because it almost captures all correlations between two firms in each pair.

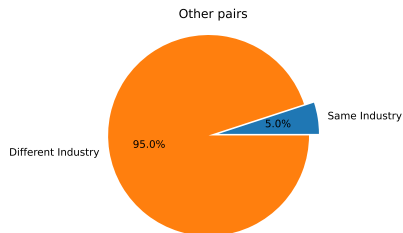
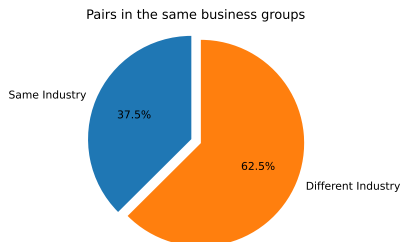
Future Correlation via *FCA*



- ρ_t : Current period correlation
- **SameGroup** : Dummy variable for whether the two stocks belong to the same business group.
- **SameIndustry** : Dummy variable for whether the two stocks belong to the same Industry.
- **SameSize** : The negative of absolute difference in percentile ranking of size across a pair
- **SameBookToMarket** : The negative of absolute difference in percentile ranking of the book to market ratio across a pair
- **CrossOwnership**: The maximum percent of cross-ownership between two firms

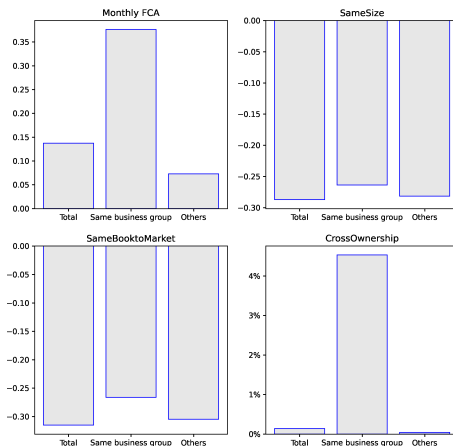
Industry & Business group

	Yes	No
SameIndustry	753806 (5.7%)	12422942 (94.3%)
SameGroup	304444 (6.3%)	4508062 (93.7%)
SameGroup & SameIndustry	115536 (0.9%)	13176748 (99.1%)



Business group

Pairs' characteristic



Summary of Controls

Variables' distribution

	mean	std	min	25%	50%	75%	max
sgroup	0.06	0.23	0.00	0.00	0.00	0.00	1.00
sBgroup	0.06	0.24	0.00	0.00	0.00	0.00	1.00
Monthlysize1	0.58	0.23	0.01	0.40	0.58	0.77	1.00
Monthlysize2	0.30	0.20	0.00	0.13	0.25	0.41	0.99
MonthlySameSize	-0.29	0.20	-0.97	-0.41	-0.24	-0.13	-0.00
MonthlyB/M1	0.54	0.25	0.00	0.36	0.57	0.75	1.00
MonthlyB/M2	0.55	0.24	0.00	0.36	0.56	0.75	1.00
MonthlySameB/M	-0.32	0.20	-0.99	-0.44	-0.27	-0.16	-0.00
MonthlyCrossOwnership	0.14	2.59	0.00	0.00	0.00	0.00	95.77

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- Fama-MacBeth regression analysis is implemented using a two-step procedure.
 - The first step is to run periodic cross-sectional regression for dependent variables using data of each period.
 - The second step is to analyze the time series of each regression coefficient to determine whether the average coefficient differs from zero.

Fama-MacBeth (1973)

- Two Step Regression

- First Step

$$\begin{aligned}Y_{i1} &= \delta_{0,1} + \delta_{1,1}^1 X_{i,1}^1 + \cdots + \delta_{k,1}^k X_{i,1}^k + \varepsilon_{i,1} \\&\vdots \\Y_{iT} &= \delta_{0,1} + \delta_{1,T}^1 X_{i,T}^1 + \cdots + \delta_{k,T}^k X_{i,T}^k + \varepsilon_{i,T}\end{aligned}$$

- Second Step

$$\begin{bmatrix} \bar{Y}_1 \\ \vdots \\ \bar{Y}_T \end{bmatrix}_{T \times 1} = \begin{bmatrix} 1 & \delta_1^0 & \delta_1^1 & \cdots & \delta_1^k \\ \vdots & \vdots & \vdots & \cdots & \vdots \\ 1 & \delta_T^0 & \delta_T^1 & \cdots & \delta_T^k \end{bmatrix}_{T \times (k+2)} \times \begin{bmatrix} \lambda \\ \lambda_0 \\ \lambda_1 \\ \vdots \\ \lambda_k \end{bmatrix}_{(k+2) \times 1}$$

- Fama-MacBeth technique was developed to account for correlation between observations on different firms in the same period

Calculating standard errors

- In most cases, the standard errors are adjusted following Newey and West (1987).
 - Newey and West (1987) adjustment to the results of the regression produces a new standard error for the estimated mean that is adjusted for autocorrelation and heteroscedasticity.
 - Only input is the number of lags to use when performing the adjustment

$$Lag = 4(T/100)^{\frac{2}{9}}$$

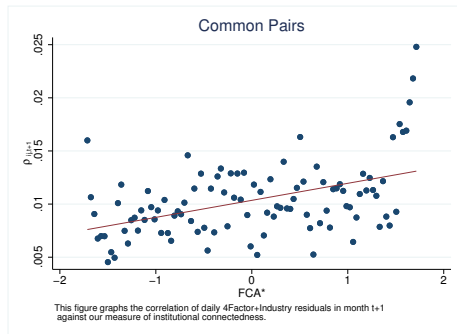
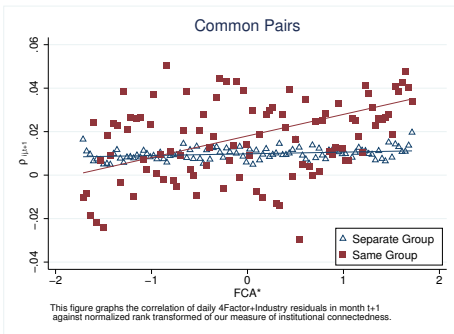
where T is the number of periods in the time series

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Future Correlation via *FCA*

Normalized Rank-Transformed



- Use Fama-MacBeth to estimate this model

$$\begin{aligned}\rho_{ij,t+1} = & \beta_0 + \beta_1 * FCA_{ij,t}^* + \beta_2 * \text{SameGroup}_{ij} \\ & + \beta_3 * FCA_{ij,t}^* \times \text{SameGroup}_{ij} \\ & + \sum_{k=1}^n \alpha_k * \text{Control}_{ij,t} + \varepsilon_{ij,t+1}\end{aligned}\tag{1}$$

- Estimate the model on a monthly frequency
- Adjust standard errors by Newey and West adjustment with 4 lags
($4(70/100)^{\frac{2}{9}} = 3.69 \sim 4$)

Model Estimation

Normalized Rank-Transformed

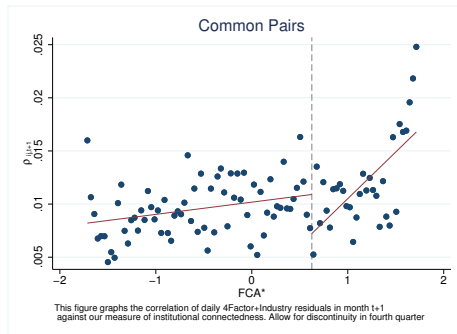
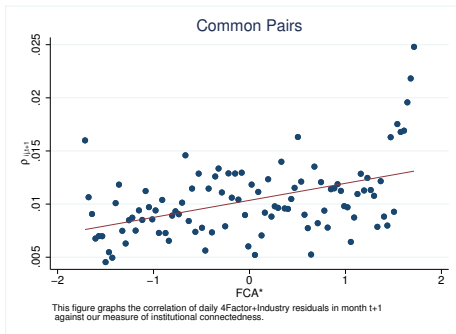
Dependent Variable: Future Monthly Correlation of 4F+Industry Residuals									
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
Same Group	0.0166*** (8.54)	0.0153*** (7.90)			0.0147*** (6.97)			0.00624*** (2.81)	0.00549** (2.27)
FCA*			0.00150*** (2.90)	0.00112** (2.11)	0.000736 (1.33)	0.00944*** (7.24)	0.000397 (0.68)	0.000377 (0.65)	-0.0000113 (-0.02)
(FCA*) × SameGroup								0.00992*** (6.49)	0.0107*** (6.97)
Observations	1665996	1665996	1665996	1665996	1665996	58337	1607659	1665996	1665996
Sub-sample	All	All	All	All	All	SameGroup	Others	All	All
Group Effect	No	No	No	No	No	No	No	No	Yes
Controls	No	Yes	No	Yes	Yes	Yes	Yes	Yes	Yes
R ²	0.000180	0.000637	0.000170	0.000652	0.000804	0.0112	0.000577	0.000898	0.00575

t statistics in parentheses

* $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$

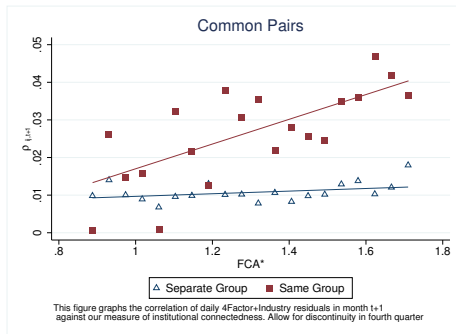
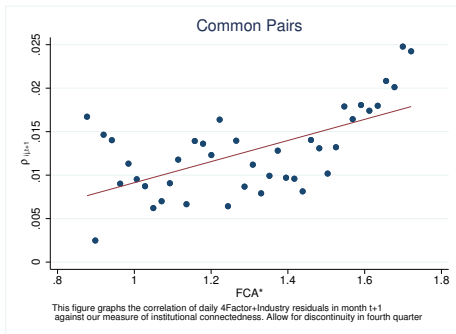
Future Correlation via *FCA*

Discontinuity

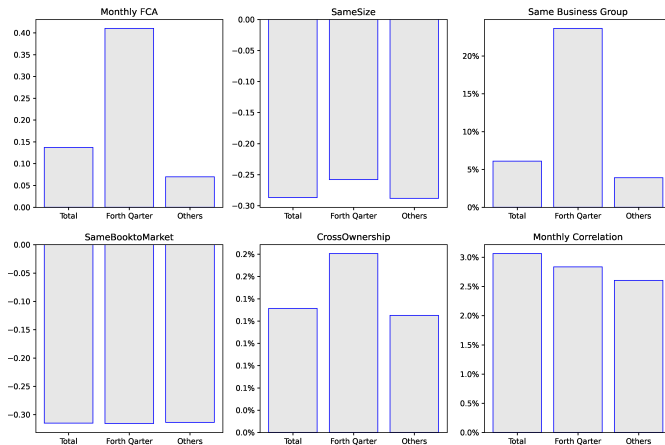


4 Factor + Industry Future Correlation via FCA^*

Discontinuity & Business Groups



Forth quarter summary



Fama-MacBeth Estimation

Discontinuity (sub-sample)

Dependent Variable: Future Monthly Correlation of 4F+Ind. Res.							
	(1)	(2)	(3)	(4)	(5)	(6)	(7)
Same Group	0.0229*** (9.86)		0.0220*** (8.34)	0.0206*** (7.28)	0.0195*** (7.24)	-0.0230* (-2.21)	-0.0201 (-1.94)
FCA*		0.0122** (3.11)	0.00516 (1.23)	0.00494 (1.18)	0.00485 (1.17)	0.00270 (0.60)	0.00194 (0.46)
(FCA*) × SameGroup						0.0287*** (3.55)	0.0269** (3.42)
SameIndustry				0.00367 (1.67)	0.00277 (1.20)	0.00232 (0.97)	0.00404 (1.62)
SameSize					0.00282 (0.78)	0.00233 (0.66)	0.00385 (1.03)
SameBookToMarket					0.0104*** (3.55)	0.0103*** (3.54)	0.0113*** (4.04)
CrossOwnership					0.0360 (1.46)	0.0402 (1.62)	0.0487 (1.99)
Observations	416514	416514	416514	416514	416514	416514	416514
Group FE	No	No	No	No	No	No	Yes
R ²	0.000923	0.000353	0.00124	0.00151	0.00232	0.00253	0.0150

t statistics in parentheses

* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$

All non-common owner pairs

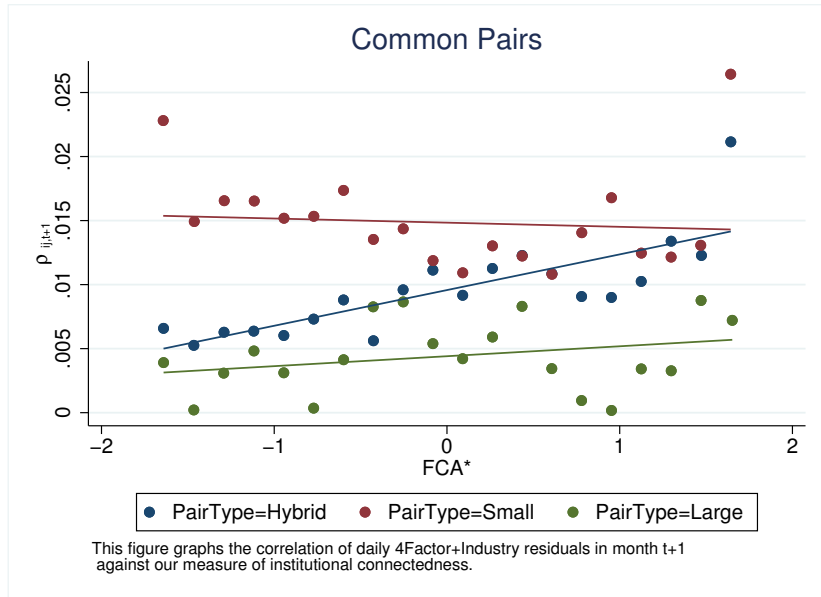
regression

Dependent Variable: Future Monthly Correlation of 4F+Industry Residuals														
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
SameGroup	0.0153*** (9.38)		0.0150*** (9.26)			0.0134*** (7.81)	0.0124*** (7.10)		0.0151*** (9.03)				0.0104*** (6.09)	0.00926*** (5.34)
FCA*		0.000676*** (3.50)	0.000496* (2.56)	0.00212 (1.79)	0.000427* (2.20)	0.000408* (2.11)	0.000116 (0.67)							
(FCA*) × SameGroup						0.00247* (2.15)	0.00321** (2.90)							
(FCA > Q3[FCA])								0.00226* (2.63)	0.000744 (0.97)	0.00226* (2.63)	0.0122*** (4.40)	-0.0000291 (-0.03)	-0.0000725 (-0.07)	-0.00110 (-1.32)
(FCA > Q3[FCA]) × SameGroup													0.0141*** (4.65)	0.0161*** (5.54)
Observations	6018646	6018646	6018646	114526	5904120	6018646	6018646	6018646	5851137	6018646	114526	5904120	6018646	6018646
Sub Sample	Total	Total	Total	SameGroups	Others	Total	Total	Total	Total	Total	SameGroups	Others	Total	Total
Group Effect	No	No	No	No	No	No	Yes	No	No	No	No	No	No	Yes
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
R ²	0.000445	0.000392	0.000491	0.00699	0.000338	0.000515	0.00330	0.000372	0.00127	0.000372	0.00721	0.000323	0.000508	0.00330

t statistics in parentheses

* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$

Grouped by size



Model Estimation

Grouped by size

Dependent Variable: Future Monthly Correlation of 4F+Ind. Res.								
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
Same Group	0.00624** (2.81)	0.0102*** (3.95)	-0.00153 (-0.53)	0.0117*** (3.76)	0.00661* (2.15)	0.0366*** (10.31)	0.0268*** (6.57)	0.00750*** (3.53)
FCA*	0.000377 (0.65)	0.000698 (1.25)	-0.000175 (-0.31)	0.00199*** (3.56)	0.00177** (3.00)	-0.00151 (-1.58)	-0.00177 (-1.84)	-0.0000771 (-0.14)
(FCA*) × SameGroup	0.00992*** (6.49)		0.0134*** (4.80)		0.00599* (2.34)		0.0123*** (4.17)	0.0105*** (6.72)
Observations	1665996	346170	346170	693728	693728	626098	626098	1665996
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Sub-sample	All Firms	Large Firms	Large Firms	Hybrid Firms	Hybrid Firms	Small Firms	Small Firms	All Firms
Pair Size FE	No	No	No	No	No	No	No	Yes
R ²	0.000898	0.00193	0.00232	0.00135	0.00149	0.00180	0.00198	0.00130

t statistics in parentheses

* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$

Model Estimation

Grouped by size

Dependent Variable: Future Monthly Correlation of 4F+Ind. Res.								
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
SameGroup	0.0134*** (7.81)	0.00954*** (4.63)	0.00853*** (3.71)	0.0136*** (7.35)	0.0118*** (6.46)	0.0314*** (10.19)	0.0267*** (7.93)	0.0138*** (8.27)
FCA*	0.000408* (2.11)	-0.0000120 (-0.05)	-0.000115 (-0.47)	0.000514* (2.09)	0.000401 (1.67)	-0.00143*** (-3.86)	-0.00154*** (-3.97)	-0.000390** (-2.70)
(FCA*) × SameGroup	0.00247* (2.15)		0.00178 (1.30)		0.00272 (1.59)		0.00545** (3.38)	0.00313** (2.80)
Observations	6018646	1753614	1753614	2992221	2992221	1272811	1272811	6018646
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Sub-sample	All Firms	Large Firms	Large Firms	Hybrid Firms	Hybrid Firms	Small Firms	Small Firms	All Firms
Pair Size FE	No	No	No	No	No	No	No	Yes
R ²	0.000515	0.000796	0.000860	0.000688	0.000735	0.00191	0.00199	0.000829

t statistics in parentheses

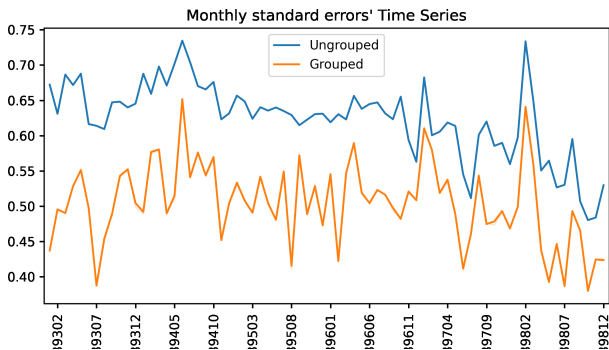
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$

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Ins Imbalance

$$\text{InsImbalance}_i = \left(\frac{\text{InsBuy} - \text{InsSell}}{\text{InsBuy} + \text{InsSell}} \right)_{\text{value}}$$



Ins Imbalance

	Future Monthly Corr. of 4F+Ind. Residuals							
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
FCA*	0.000308 (0.60)	0.000384 (0.81)	0.000320 (0.68)		0.00945*** (6.07)	0.0000347 (0.07)	0.000123 (0.17)	0.0000843 (0.11)
Same Group	0.0164*** (8.68)	0.0164*** (8.68)	0.00765*** (3.64)	0.00786*** (3.90)		0.00974*** (5.36)	0.00241 (0.79)	0.00154 (0.48)
Low Imbalance std		0.00119 (1.29)	0.000325 (0.35)	0.000192 (0.19)	0.0241*** (6.15)	0.000469 (0.52)	0.0000788 (0.08)	0.000481 (0.31)
Low Imbalance std × SameGroup			0.0238*** (6.85)	0.0240*** (6.90)			0.0142** (2.95)	0.0142** (3.14)
(FCA*) × SameGroup							0.00580** (2.77)	0.00645** (2.94)
Low Imbalance std × (FCA*)							-0.000584 (-0.77)	-0.000483 (-0.57)
Low Imbalance std × SameGroup × (FCA*)						0.0209*** (9.69)	0.0126*** (4.44)	0.0120*** (3.91)
Observations	1665996	1665996	1665996	1665996	58337	1665996	1665996	1665996
Group Effect	No	No	No	No	No	No	No	Yes
Pair Size FE	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Sub-sample	Total	Total	Total	Total	Same Groups	Total	Total	Total
Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
R ²	0.00120	0.00132	0.00144	0.00129	0.0210	0.00149	0.00166	0.00643

t statistics in parentheses

* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$

$$\Delta \text{TurnOver} = \ln\left(\frac{\text{TurnOver}_{i,t}}{\text{TurnOver}_{i,t-1}}\right) = \ln\left(\frac{\text{volume}_{i,t}}{\text{MarketCap}_{i,t}}\right) - \ln\left(\frac{\text{volume}_{i,t-1}}{\text{MarketCap}_{i,t-1}}\right)$$

Dependent Variable: $\Delta \text{TurnOver}_i$						
	(1)	(2)	(3)	(4)	(5)	(6)
$\Delta \text{TurnOver_Market}$	0.431*** (14.56)	0.453*** (14.49)	0.287*** (8.23)	0.321*** (14.03)	0.288*** (6.92)	0.321*** (14.14)
$\Delta \text{TurnOver_Group}$			0.245*** (6.31)	0.234*** (7.15)	0.284*** (6.02)	0.273*** (7.19)
$\Delta \text{TurnOver_Industry}$	0.155*** (6.53)	0.169*** (6.99)	0.174* (2.08)	0.118*** (3.68)	0.152 (1.47)	0.0430 (1.19)
Observations	626813	623759	305563	301329	305563	301329
Weight	-	-	MC \times CR	MC \times CR	MC	MC
Control	No	Yes	No	Yes	No	Yes
R^2	0.141	0.180	0.242	0.282	0.236	0.277

t statistics in parentheses

* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$

Cross-sectional analyze of Group turnover

	Dependent Variable: β_Group													
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
Excess	0.355*** (4.99)	0.505*** (6.94)												
ExcessDummy			0.00604 (0.16)	0.101** (2.77)										
ExcessDiff					0.716*** (5.99)	0.961*** (7.77)								
ExcessHigh							0.344*** (6.61)	0.412*** (8.48)						
Low Imbalance std									-0.0211 (-0.53)	-0.144*** (-3.59)				
Position											-0.00268 (-0.17)	0.0308 (1.94)		
Centrality													0.397* (2.47)	-0.153 (-1.04)
Observations	1349	1349	1367	1367	1349	1349	1367	1367	1341	1341	1349	1349	1299	1299
Time FE	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Controls	No	Yes	No	Yes	No	Yes	No	Yes	No	Yes	No	Yes	No	Yes
R ²	0.0251	0.0970	0.000973	0.0600	0.0436	0.123	0.0436	0.109	0.00130	0.0640	0.00128	0.0581	0.00415	0.0456

t statistics in parentheses

* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$

Pairwise correlations in turnover

	Dependent Variable: Future Monthly Correlation of Delta turnover						
	(1)	(2)	(3)	(4)	(5)	(6)	(7)
Same Group	0.0349*** (11.20)	0.0217*** (7.38)			0.0227*** (7.73)	0.0182*** (6.22)	0.0176*** (6.19)
FCA*			0.000871 (0.63)	-0.000438 (-0.37)	-0.00110 (-0.93)	-0.00134 (-1.08)	-0.00171 (-1.51)
(FCA*) × SameGroup						0.00619* (2.45)	0.00631* (2.42)
Observations	1447955	1341445	1447955	1341445	1341445	1341445	1341445
Group Effect	No	No	No	No	No	No	Yes
Pair Size FE	No	Yes	No	Yes	Yes	Yes	Yes
Controls	No	Yes	No	Yes	Yes	Yes	Yes
R ²	0.000465	0.00431	0.000461	0.00448	0.00471	0.00481	0.0157

t statistics in parentheses

* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$

	Dep. Var.: Future Monthly Cor. of 4F+Ind. Res.			
	(1)	(2)	(3)	(4)
Same Group	0.00637* (2.22)	0.00940** (2.96)		0.0172* (2.40)
FCA*	-0.000339 (-0.80)	-0.000491 (-1.02)	0.0123*** (3.50)	-0.000292 (-0.69)
(FCA*) × SameGroup	0.0120*** (7.57)			0.00898** (3.27)
$\rho_t(\text{Turnover})$	0.00515*** (8.45)	0.00512*** (8.56)	0.0204*** (4.88)	0.00454*** (7.28)
ρ_t	0.0246*** (17.07)	0.0246*** (17.10)	0.0911*** (12.29)	0.0221*** (14.58)
BigGroup		-0.00187* (-2.03)		
BigGroup × SameGroup × FCA*		0.0109*** (5.20)		
Observations	1459585	1459585	45678	1413907
Controls	Yes	Yes	Yes	Yes
Pari Size FE	Yes	Yes	Yes	Yes
SubSample	All	All	Same Big Groups	Others
R^2	0.00241	0.00256	0.0444	0.00195

t statistics in parentheses

* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$

Bearish/Bullish Market

	Fu. Monthly Cor. of 4F+Ind. Residuals		
	(1)	(2)	(3)
FCA*	0.000363 (0.64)	0.000363 (0.64)	0.000464 (0.82)
(FCA*) \times SameGroup	0.00966*** (6.43)	0.00968*** (6.47)	
Same Group	0.00607** (2.77)	0.00529 (0.55)	0.00974 (1.02)
Bearish Market \times SameGroup		-0.00531 (-0.50)	4.724 (0.99)
Bullish Market \times SameGroup		0.00513 (0.57)	0.00659 (0.68)
(FCA*) \times Bullish Market \times SameGroup			0.00570 (1.28)
(FCA*) \times Bearish Market \times SameGroup			-2.774 (-0.99)
Observations	1665996	1665996	1665996
R^2	0.002	0.002	0.002

t statistics in parentheses

* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$

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Conclusion

- We derive a measure that captures the extent of common ownership distribution.
- The common ownership comovement effect with a extra explanation:
 - Common ownership that crosses a threshold affect on comovement
 - Be in the same business group has a major effect on comovement

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Measuring Common Ownership

Proof

- If two stocks in pair have n mutual owner, which total market cap divides them equally, the mentioned indexes equal n .
 - Each holder owns $1/n$ of each firm.
 - Firm's market cap is α_1 and α_2 :
 - So for each holder of firms we have $S_{i,t}^f P_{i,t} = \alpha_i$
 - SQRT

$$\left[\frac{\sum_{f=1}^n \sqrt{\alpha_1/n} + \sum_{f=1}^n \sqrt{\alpha_2/n}}{\sqrt{\alpha_1} + \sqrt{\alpha_2}} \right]^2 = \left[\frac{\sqrt{n}(\sqrt{\alpha_1} + \sqrt{\alpha_2})}{\sqrt{\alpha_1} + \sqrt{\alpha_2}} \right]^2 = n$$

- Quadratic

$$\left[\frac{\sum_{f=1}^n (\alpha_1/n)^2 + \sum_{f=1}^n (\alpha_2/n)^2}{\alpha_1^2 + \alpha_2^2} \right]^{-1} = \left[\frac{\alpha_1^2 + \alpha_2^2}{n(\alpha_1^2 + \alpha_2^2)} \right]^{-1} = n$$

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- Common-ownership and comovement effect

[Anton and Polk (2014)]

Stocks sharing many common investors tend to comove more strongly with each other in the future than otherwise similar stocks.

- Common-ownership and liquidity demand

[Koch et al. (2016), Pastor and Stambaugh (2003), Acharya and Pedersen (2005)]

Commonality in stock liquidity is likely driven by correlated trading among a given stock's investors. Commonality in liquidity is important because it can influence expected returns

- Trading needs and comovement

[Greenwood and Thesmar (2011)]

If the investors of mutual funds have correlated trading needs, the stocks that are held by mutual funds can comove even without any portfolio overlap of the funds themselves

- Stock price synchronicity and poor corporate governance

[Boubaker et al. (2014), Khanna and Thomas (2009), Morck et al. (2000)]

Stock price synchronicity has been attributed to poor corporate governance and a lack of firm-level transparency. On the other hand, better law protection encourages informed trading, which facilitates the incorporation of firm-specific information into stock prices, leading to lower synchronicity

Graph

Synchronicity and firm interlocks

JFE-2009-Khanna

- Three types of network

- 1 Equity network
- 2 Director network
- 3 Owner network

- Dependent variables

Using detrended weekly return for calculation

- 1 Pairwise returns synchronicity = $\frac{\sum_t (n_{i,j,t}^{up} n_{i,j,t}^{down})}{T_{i,j}}$

- 2 Correlation = $\frac{Cov(i,j)}{\sqrt{Var(i) \cdot Var(j)}}$

- Tobit estimation of

$$f_{i,j}^d = \alpha l_{i,j} + \beta(1 * N_{i,j}) + \gamma Ind_{i,j} + \varepsilon_{i,j}$$

being in the same director network has a significant effect

Large controlling shareholder and stock price synchronicity

JBFB-2014-Boubaker

- Stock price synchronicity:

$$SYNCH = \log\left(\frac{R_{i,t}^2}{1 - R_{i,t}^2}\right)$$

where $R_{i,t}^2$ is the R-squared value from

$$RET_{i,w} = \alpha + \beta_1 MKRET_{w-1} + \beta_2 MKRET_w + \beta_3 INDRET_{i,w-1} + \beta_4 INDRET_{i,w} + \varepsilon_{i,w}$$

- OLS estimation of

$$\begin{aligned} SYNCH_{i,t} = & \beta_0 + \beta_1 Excess_{i,t} + \beta_2 UCF_{i,t} + \sum_k \beta_k Control_{i,t}^k \\ & + IndustryDummies + YearDummies + \varepsilon_{i,t} \end{aligned}$$

- Stock price synchronicity increases with excess control
- Firms with substantial excess control are more likely to experience stock price crashes

- Common active mutual fund owners
- Measuring Common Ownership
 - $FCAP_{ij,t} = \frac{\sum_{f=1}^F (S_{i,t}^f P_{i,t} + S_{j,t}^f P_{j,t})}{S_{i,t} P_{i,t} + S_{j,t} P_{j,t}}$
 - Using normalized rank-transformed as $FCAP_{ij,t}^*$
- $\rho_{ij,t}$: within-month realized correlation of each stock pair's daily four-factor returns

•

$$\rho_{ij,t+1} = a + b_f \times FCAP_{ij,t}^* + \sum_{k=1}^n CONTROL_{ij,t,k} + \varepsilon_{ij,t+1}$$

Estimate these regressions monthly and report the time-series average as in Fama-MacBeth

Commonownership measurements

Model-based measures

- $HJL_I^A(A, B) = \sum_{i \in I^{A,B}} \frac{\alpha_{i,B}}{\alpha_{i,A} + \alpha_{i,B}}$ Harford et al. (2011)
 - Bi-directional
 - Pair-level measure of common ownership
 - Its potential impact on managerial incentives
 - Measure not necessarily increases when the relative ownership increases
 - Accounts only for an investor's relative holdings
- $MHHI = \sum_j \sum_k s_j s_k \frac{\sum_i \mu_{ij} \nu_{ik}}{\sum_i \mu_{ij} \nu_{ij}}$ Azar et al. (2018)
 - Capture a specific type of externality
 - Measured at the industry level
 - Assumes that investors are fully informed about the externalities
- $GGL^A(A, B) = \sum_{i=1}^I \alpha_{i,AG}(\beta_{i,A}) \alpha_{i,B}$ Gilje et al. (2020)
 - Bi-directional
 - Less information
 - Not sensitive to the scope
 - Measure increases when the relative ownership of firm A increases

Commonownership measurements

Ad hoc common ownership measures

- $Overlap_{Count}(A, B) = \sum_{i \in I^{A,B}} 1$

He and Huang (2017), He et al. (2019)

- $Overlap_{Min}(A, B) = \sum_{i \in I^{A,B}} \min\{\alpha_{i,A}, \alpha_{i,B}\}$

Newham et al. (2018)

- $Overlap_{AP}(A, B) = \sum_{i \in I^{A,B}} \alpha_{i,A} \frac{\bar{v}_A}{\bar{v}_A + \bar{v}_B} + \alpha_{i,B} \frac{\bar{v}_B}{\bar{v}_A + \bar{v}_B}$

Anton and Polk (2014)

- $Overlap_{HL}(A, B) = \sum_{i \in I^{A,B}} \alpha_{i,A} \times \sum_{i \in I^{A,B}} \alpha_{i,B}$

Hansen and Lott Jr (1996) , Freeman (2019)

- Unappealing properties

- Unclear is whether any of these measures represents an economically meaningful measure of common ownership's impact on managerial incentives.
- Both $Overlap_{Count}$ and $Overlap_{AP}$ are invariant to the decomposition of ownership between the two firms, which leads to some unappealing properties.

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