

Resource Reallocation with Carbon Emission Policies

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- Key policies: carbon pricing, renewable subsidies to curb emissions.
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 - Limitation in fossil fuel usage.
 - Adoption of renewable technologies.
 - **Reallocation of resources to greener firms/industries.**

- **What is the Economic Outcomes of environmental policies due to resources reallocation?**
 - Industry output
 - Firm-level productivity
 - Sector size
 - Emission intensity
 - Total Emission

- Effectiveness of Carbon policies:
 - Martinsson et al. (2024); Shapiro and Walker (2018); Ahmadi, Yamazaki, and Kabore (2022); Andersson (2019)
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Contribution: **Quantify substitution between green and brown capital**
- Misallocation:
 - Whited and Zhao (2021); Hsieh and Klenow (2009); Ai, Li, and Yang (2020); Asker, Collard-Wexler, and De Loecker (2014)
Contribution: **Misallocation (Reallocation) in the context of environmental policies**

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Contribution: **Misallocation (Reallocation) in the context of environmental policies**
- Climate Policy Design:
 - Acemoglu, Gancia, and Zilibotti (2012); Acemoglu et al. (2016); Oehmke and Opp (2023)
Contribution: **Assess alternative instruments in Emission Intensity / resource reallocation trade off**

Road map

- ① Develop Economic model with Emission
- ② Characterize the allocation of resources
- ③ Estimate the model by Swedish data
- ④ Compare the optimal Policy with resource reallocation
- ⑤ Discuss the cost of the environmental policies

Road map

- ① Develop Economic model with Emission ✓
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Standard Framework

Hsieh and Klenow (2009)

- Heterogeneous monopolistic competitive firms
- Partial equilibrium
- Cobb-Douglas Production function
- CES aggregator for output
- Normal aggregation of emissions

Extension

Production functions

- Industry s , firm i :

$$Y_{si} = \hat{A}_{si} \hat{K}_{si}^{\beta_s} L_{si}^{1-\beta_s}$$

- \hat{A}_{si} : total factor of productivity

Firm's profit

Extension

Production functions

- Industry s , firm i :

$$Y_{si} = \hat{A}_{si} \hat{K}_{si}^{\beta_s} L_{si}^{1-\beta_s}, \quad \hat{K} = (\alpha_s G_{si}^{\frac{\gamma_s-1}{\gamma_s}} + (1 - \alpha_s) B_{si}^{\frac{\gamma_s-1}{\gamma_s}})^{\frac{\gamma_s}{\gamma_s-1}}$$

$$E_{si} = \tilde{A}_{si} B_{si}$$

Emission General Model

- \hat{A}_{si} : total factor of productivity
- α_s : importance of Green capital in the production
- γ_s : elasticity of substitution between Green and Brown capital
- \tilde{A}_{si} : emission inefficiency
- Firms maximize over G , B , and L

Firm's profit

Parameter	Source/Moment
Panel A: Estimation	
α_s	β_G/β_B
β_s	β_G/β_L
σ_s	WL/PY
γ_s	$\beta_{GB}/\beta_B\beta_G$
$Mean(\log(\hat{A}_{si}))$	$Mean(L_{si})$
$Sd(\log(\hat{A}))$	$Sd(L_{si})$
$Mean(\log(\hat{A}_{si}))$	$Mean(E/PY)$
$Sd(\log(\hat{A}))$	$Sd(E/PY)$
$Corr(\log(\hat{A}), \log(\hat{A}))$	$Corr(PY, E/PY)$
Panel B: Additional Moments	
$\left(\frac{\alpha_s}{1-\alpha_s} \frac{(1+\tau_E^B)r_{si}+\tau_E^E\hat{A}}{(1+\tau_s^E)r_{si}} \right)^{\gamma_s}$	$z_k = G/B$
$\frac{1-\beta}{\beta} \frac{1}{\alpha} \left(\alpha_s + (1-\alpha_s)z_{si}^k - \frac{\gamma_s-1}{\gamma_s} \right)^{\frac{1}{\gamma_s-1}} \frac{(1+\tau_s^E)r_{si}}{(1+\tau_s^E)w_{si}}$	$z_l = L/K$
$\gamma \frac{\hat{A}}{r^B+\tau_E\hat{A}} z_k$	$\partial z_k/\partial \tau_E$
$\frac{\frac{1-\alpha}{\alpha z_{si}^k} \frac{\gamma_s-1}{\gamma_s} + (1-\alpha)}{r^B+\tau_E\hat{A}} \frac{\hat{A}}{r^B+\tau_E\hat{A}} z_l$	$\partial z_l/\partial \tau_E$
$\frac{\hat{A}}{r^B+\tau_E\hat{A}} \left[-\frac{\gamma_s}{\alpha} - \left(\frac{w}{z_l + w} \right)^{\frac{1-\alpha}{\Delta}} \right]$	$\partial \ln \epsilon/\partial \tau_E$
$\frac{\partial \ln \epsilon/\partial \tau_E}{\frac{1}{\tau_E} + \partial \ln \epsilon/\partial \tau_E}$	$\Delta(\frac{E}{PY})/\Delta(\frac{C}{PY})$
Panel C: Calibration	
r	5%
w	500 TSEK

Calibration

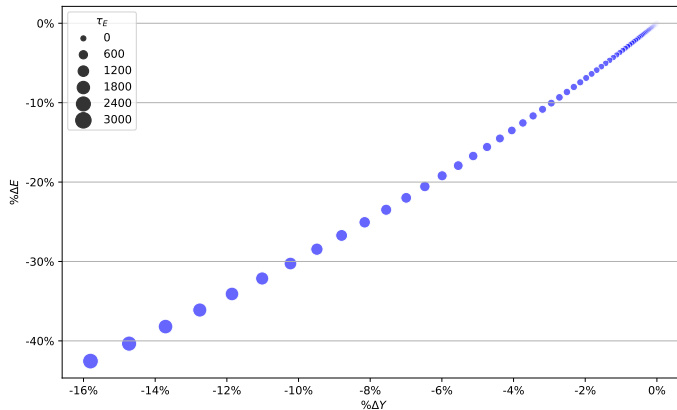
- I just reasonably calibrate the model to match the summary statistics of Martinsson et al. (2024)

Parameter	Value	Source/Moment
Panel A: Estimated Value		
γ	2.48	$\Delta(\frac{E}{PY})/\Delta(\frac{C}{PY})$
\tilde{A}	0.002	E/PY
Panel B: Inputs		
σ	5	-
r	5%	-
w	500 TSEK	-
Panel C: Calibrated Value		
β_s	0.6	Martinsson et al. (2024)
α_s	0.25	G/B , Wiedemann (2023)

Sensitivity of α

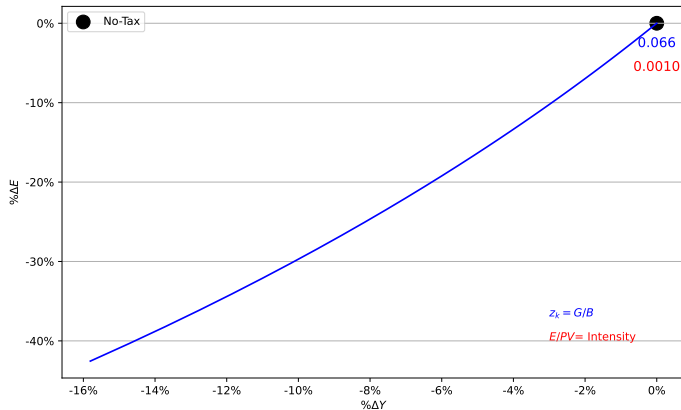
Emission and Production

Results



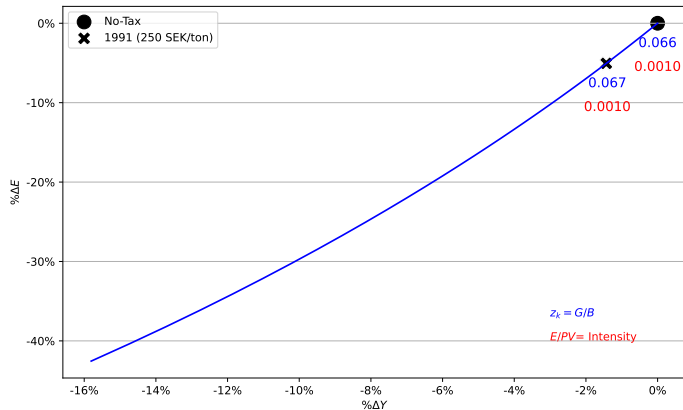
Emission and Production

Results



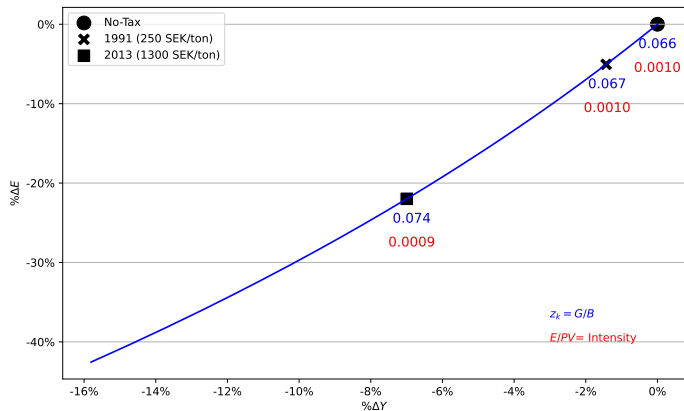
Emission and Production

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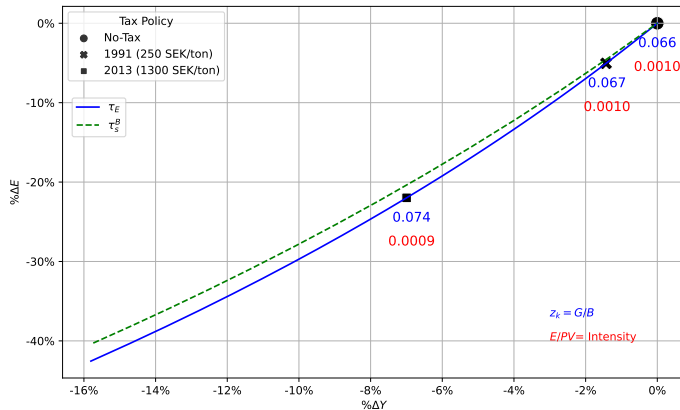
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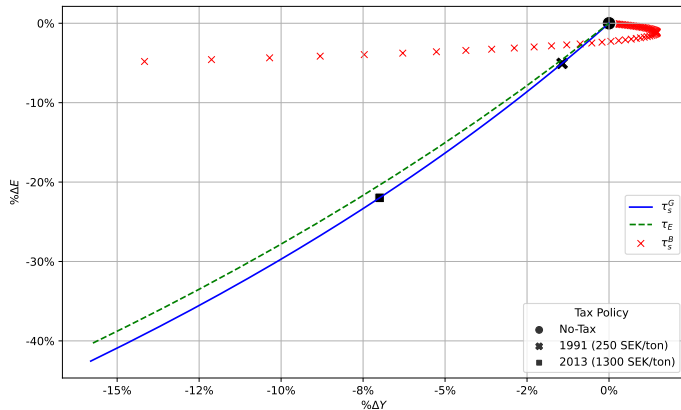
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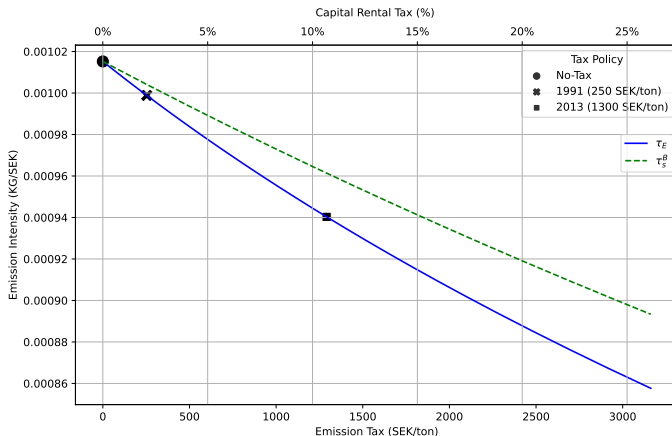
Emission and Production

Results



Carbon Intensity and Tax

Counterfactual



τ_E	τ_G	τ_B
100	9 %	2 %
250	18 %	2 %
500	27 %	4 %
1300	42 %	12 %
3000	55 %	26 %

Future Steps

- ① Develop Economic model with Emission
 - Firms could R&D
 - Add Household and Government
 - Firms could enter and exit the market
- ② Characterize the allocation of resources
- ③ Provide a definition of Green and Brown capital
- ④ Estimate the model by Swedish data
- ⑤ Compare the optimal Policy with resource reallocation
- ⑥ Discuss the cost of the environmental policies

Thank you!

References I

- Acemoglu, Daron, Gino Gancia, and Fabrizio Zilibotti.** 2012. "Competing engines of growth: Innovation and standardization." *Journal of Economic Theory*, 147(2): 570–601.
- Acemoglu, Daron, Ufuk Akcigit, Douglas Hanley, and William Kerr.** 2016. "Transition to clean technology." *Journal of political economy*, 124(1): 52–104.
- Ahmadi, Younes, Akio Yamazaki, and Philippe Kabore.** 2022. "How do carbon taxes affect emissions? Plant-level evidence from manufacturing." *Environmental and Resource Economics*, 82(2): 285–325.
- Ai, Hengjie, Kai Li, and Fang Yang.** 2020. "Financial intermediation and capital reallocation." *Journal of Financial Economics*, 138(3): 663–686.
- Andersson, Julius J.** 2019. "Carbon taxes and CO2 emissions: Sweden as a case study." *American Economic Journal: Economic Policy*, 11(4): 1–30.
- Asker, John, Allan Collard-Wexler, and Jan De Loecker.** 2014. "Dynamic inputs and resource (mis) allocation." *Journal of Political Economy*, 122(5): 1013–1063.
- Hsieh, Chang-Tai, and Peter J Klenow.** 2009. "Misallocation and manufacturing TFP in China and India." *The Quarterly journal of economics*, 124(4): 1403–1448.
- Krueger, Philipp, Daniel Metzger, and Jiaxin Wu.** 2023. "The sustainability wage gap." *Swedish House of Finance Research Paper*, , (20-14): 21–17.

References II

- Martinsson, Gustav, László Sajtos, Per Strömberg, and Christian Thomann.** 2024. "The Effect of Carbon Pricing on Firm Emissions: Evidence from the Swedish CO2 Tax." *The Review of Financial Studies*, hhad097.
- Oehmke, Martin, and Marcus M Opp.** 2023. "A theory of socially responsible investment." *Swedish House of Finance Research Paper*, , (20-2).
- Shapiro, Joseph S, and Reed Walker.** 2018. "Why is pollution from US manufacturing declining? The roles of environmental regulation, productivity, and trade." *American Economic Review*, 108(12): 3814–3854.
- Whited, Toni M, and Jake Zhao.** 2021. "The misallocation of finance." *The Journal of Finance*, 76(5): 2359–2407.
- Wiedemann, Moritz.** 2023. "Green stewards: Responsible institutional investors foster green capex." *Available at SSRN 4618793*.

- The firm's emission is:

$$E_{si} = \tilde{A}_{si} \tilde{K}_{si}^{\theta_s} L_{si}^{1-\theta_s} \quad , \quad \tilde{K} = \left(\mu_s G_{si}^{\frac{\eta_s-1}{\eta_s}} + (1 - \mu_s) B_{si}^{\frac{\eta_s-1}{\eta_s}} \right)^{\frac{\eta_s}{\eta_s-1}}$$

- The nominal profit for firms:

$$\pi_{si} = (1 + \tau_{si}^p) P_{si} Y_{si} - ([(1 + \tau_{G_s}) r_{si} G_{si} + (1 + \tau_{B_s}) r_{si} B_{si} + (1 + \tau_{l_s}) w_{si} l_{si}] + \tau_E E_{si})$$

Back

Firm's profit

- The nominal profit for firms:

$$\pi_{si} = (1 + \tau_s^P) P_{si} Y_{si}$$

- where

- τ_s^P is the tax / Demand preference for the firm

Back

- The nominal profit for firms:

$$\pi_{si} = (1 + \tau_s^P) P_{si} Y_{si} - \left((1 + \tau_s^G) r_s G_{si} \right)$$

- where

- τ_s^P is the **tax** / **Demand preference** for the firm
- τ_s^G is the Green capital **subsidy** / **ESG preference** of Financier

- The nominal profit for firms:

$$\pi_{si} = (1 + \tau_s^P) P_{si} Y_{si} - \left((1 + \tau_s^G) r_s G_{si} + (1 + \tau_s^B) r_s B_{si} \right)$$

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Firm's profit

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- τ_s^W is the Labor market preference to work in the green/brown sector (Krueger, Metzger, and Wu, 2023)

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 - τ_s^W is the **Labor market preference** to work in the green/brown sector (Krueger, Metzger, and Wu, 2023)
- The firm chooses the optimal capital and labor to minimize the cost of production and then chooses the price level to maximize the profit

Back

$$\max_{G_{si}, B_{si}, L_{si}} -Cost \quad \text{s.t.} \quad \hat{A}_{si} \hat{K}_{si}^{\beta_s} L_{si}^{1-\beta_s} = \bar{Y}_{si}$$

General Model Solution

$$\max_{G_{si}, B_{si}, L_{si}} -Cost \quad \text{s.t.} \quad \hat{A}_{si} \hat{K}_{si}^{\beta_s} L_{si}^{1-\beta_s} = \bar{Y}_{si}$$

$$\frac{G_{si}}{B_{si}} = z_{si}^k$$

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$$\frac{G_{si}}{B_{si}} = z_{si}^k = \left(\frac{\alpha_s}{1 - \alpha_s} \frac{(1 + \tau_s^B) r_s + \tau_s^E \tilde{A}}{(1 + \tau_s^G) r_s} \right)^{\gamma_s}$$

General Model Solution

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$$\frac{L_{si}}{\hat{K}_{si}} = z_{si}^l$$

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$$\frac{L_{si}}{\hat{K}_{si}} = z_{si}^l = \frac{1 - \beta}{\beta} \frac{1}{\alpha_s} \left(\alpha_s + (1 - \alpha_s) z_{si}^k \right)^{\frac{1}{1-\gamma_s}} \frac{(1 + \tau_s^G) r_s}{(1 + \tau_s^W) w_{si}}$$

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$$E_{si} = \frac{\tilde{A}_{si}}{\hat{A}_{si}} \left(\alpha_s z_{si}^{k \gamma_s - 1} + (1 - \alpha_s) \right)^{\frac{\gamma_s}{1-\gamma_s}} z_{si}^l^{1-\beta} \bar{Y}_{si}$$

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$$\frac{G_{si}}{B_{si}} = z_{si}^k = \left(\frac{\alpha_s}{1 - \alpha_s} \frac{(1 + \tau_s^B) r_s + \tau_s^E \tilde{A}}{(1 + \tau_s^G) r_s} \right)^{\gamma_s}$$

$$\frac{L_{si}}{\hat{K}_{si}} = z_{si}^l = \frac{1 - \beta}{\beta} \frac{1}{\alpha_s} \left(\alpha_s + (1 - \alpha_s) z_{si}^k \right)^{\frac{1}{1-\gamma_s}} \frac{(1 + \tau_s^G) r_s}{(1 + \tau_s^W) w_{si}}$$

$$E_{si} = \frac{\tilde{A}_{si}}{\hat{A}_{si}} \left(\alpha_s z_{si}^{k \gamma_s - 1} + (1 - \alpha_s) \right)^{\frac{\gamma_s}{1-\gamma_s}} z_{si}^l^{1-\beta} \bar{Y}_{si} = \psi_{si} \bar{Y}_{si}$$

$$\max_{G_{si}, B_{si}, L_{si}} -Cost \quad \text{s.t.} \quad \hat{A}_{si} \hat{K}_{si}^{\beta_s} L_{si}^{1-\beta_s} = \bar{Y}_{si}$$

$$\frac{G_{si}}{B_{si}} = z_{si}^k = \left(\frac{\alpha_s}{1 - \alpha_s} \frac{(1 + \tau_s^B) r_s + \tau_s^E \tilde{A}}{(1 + \tau_s^G) r_s} \right)^{\gamma_s}$$

$$\frac{L_{si}}{\hat{K}_{si}} = z_{si}^l = \frac{1 - \beta}{\beta} \frac{1}{\alpha_s} \left(\alpha_s + (1 - \alpha_s) z_{si}^k \right)^{\frac{1}{1-\gamma_s}} \frac{(1 + \tau_s^G) r_s}{(1 + \tau_s^W) w_{si}}$$

$$E_{si} = \frac{\tilde{A}_{si}}{\hat{A}_{si}} \left(\alpha_s z_{si}^{k \gamma_s - 1} + (1 - \alpha_s) \right)^{\frac{\gamma_s}{1-\gamma_s}} z_{si}^{l 1-\beta} \bar{Y}_{si} = \psi_{si} \bar{Y}_{si}$$

- Firm will then charge markup over the marginal cost

$$\max \quad -Cost \quad \text{s.t.} \quad \hat{A}_{si} \hat{K}_{si}^{\beta_s} L_{si}^{1-\beta_s} = \bar{Y}_{si}$$

$$z_{si}^k \equiv \frac{G_{si}}{B_{si}} = \left[\frac{\alpha_s}{1 - \alpha_s} \frac{\frac{\partial}{\partial B} Cost_{si}}{\frac{\partial}{\partial G} Cost_{si}} \right]^{\gamma_s}$$

$$\begin{aligned} z_{si}^l \equiv \frac{L_{si}}{\hat{K}_{si}} &= \frac{1 - \beta_s}{\beta_s} \frac{1}{1 - \alpha_s} (\alpha_s z_{si}^{k(\gamma_s-1)} + (1 - \alpha_s))^{\frac{1}{1-\gamma_s}} \frac{\frac{\partial}{\partial B} Cost_{si}}{\frac{\partial}{\partial L} Cost_{si}} \\ &= \frac{1 - \beta_s}{\beta_s} \frac{1}{\alpha_s} (\alpha_s + (1 - \alpha_s) z_{si}^{k(1-\gamma_s)})^{\frac{1}{1-\gamma_s}} \frac{\frac{\partial}{\partial G} Cost_{si}}{\frac{\partial}{\partial L} Cost_{si}} \end{aligned}$$

$$E_{si} = \frac{\tilde{A}_{si}}{\hat{A}_{si}} \left(\frac{\phi_{si}}{z_{si}^l} \right)^{\theta_s} z_{si}^{l\beta_s} \bar{Y}_{si} = \psi_{si} \bar{Y}_{si}, \quad \text{where} \quad \phi_{si} = \frac{(\mu_s + (1 - \mu_s) z_{si}^{k(1-\eta_s)})^{\frac{\eta_s}{\eta_s-1}}}{(\alpha_s + (1 - \alpha_s) z_{si}^{k(1-\gamma_s)})^{\frac{\gamma_s}{\gamma_s-1}}}$$

Model

Optimal firm level price

- Now Firm need to choose the price level to maximize the profit:

$$\max_{P_{si}} \pi_{si} = P_{si}F_{si} - C_{si}F_{si}$$

- Firm-level real output is a function of the sector price, firm price, and sector real output (i.e. $F_{si} = (\frac{P_s}{P_{si}})^{\sigma_s} F_s$)
- Therefore, because the optimal ratio does not depend on the price, the ratio can be maximized out of the problem of the optimal determination of the price, leaving the firm's real output as just a function of price

$$P_{si} = \frac{1}{1 + \tau_{si}^p} \frac{\sigma_s}{\sigma_s - 1} C_{si}$$

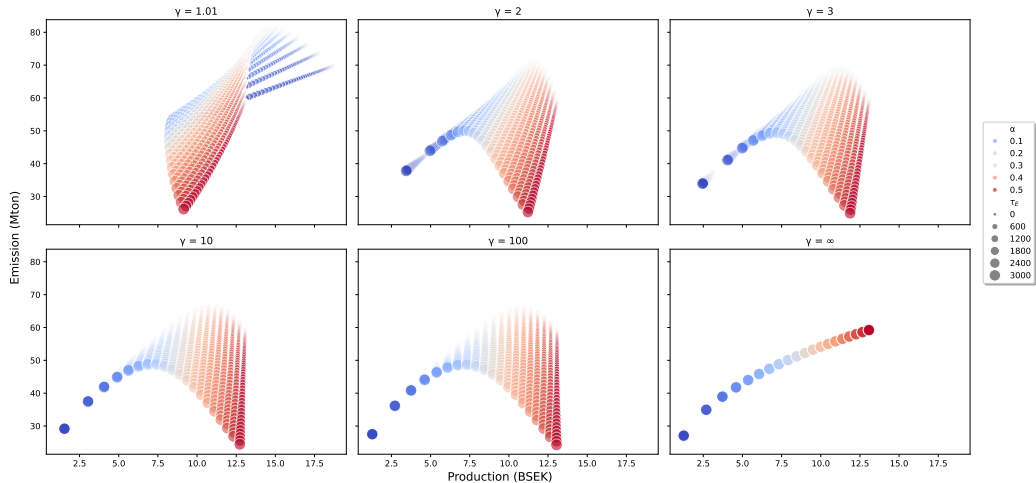
Estimation / Calibration

- My goal is to estimate the parameters sector by sector for Sweden
- I just reasonably calibrate the model to match the summary statistics of Martinsson et al. (2024)

Parameter	Value	Source/Moment
Panel A: Inputs		
σ	∞	Fully competitive
r	5%	-
w	500 TSEK	-
L	250 (sd = 900)	Martinsson et al. (2024)
Panel B: Calibrated Value		
β_s	0.6	Martinsson et al. (2024)
α_s	0.25	G/B , Wiedemann (2023)
Panel C: Estimated Value		
γ	2.48	$\Delta(\frac{E}{PY})/\Delta(\frac{C}{PY})$
\tilde{A}	0.002	E/PY

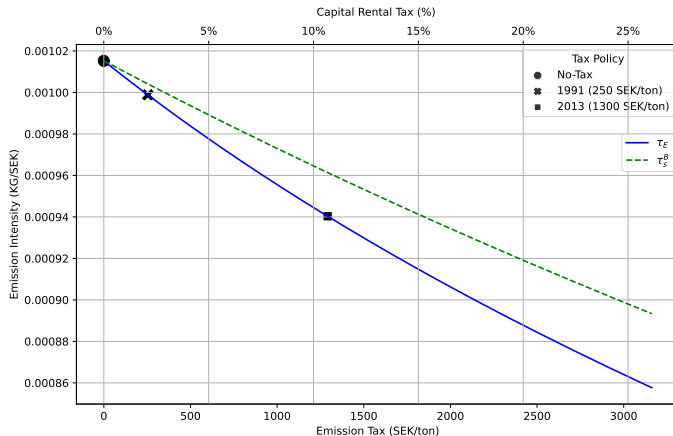
Sensitivity analysis

Production vs Emission with different Carbon Tax on different α and γ



Carbon Intensity and Tax

Counterfactual



τ_E	τ_G	τ_B
100	9 %	2 %
250	18 %	2 %
500	27 %	4 %
1300	42 %	12 %
3000	55 %	26 %

Reallocation

Resources allocation

- Now, we need to find the optimal allocation of resources in the economy under two scenarios:

Back

Reallocation

Resources allocation

- Now, we need to find the optimal allocation of resources in the economy under two scenarios:

$$\hat{L}_{si} = \frac{\hat{A}_{si}^{\sigma-1}}{\sum_j \hat{A}_{sj}^{\sigma-1}} L_s$$

$$\hat{G}_{si} = \frac{\hat{A}_{si}^{\sigma-1}}{\sum_j \hat{A}_{sj}^{\sigma-1}} \frac{z_s^k}{1 + z_s^k} K_s$$

$$\hat{B}_{si} = \frac{\hat{A}_{si}^{\sigma-1}}{\sum_j \hat{A}_{sj}^{\sigma-1}} \frac{1}{1 + z_s^k} K_s$$

Back

Reallocation

Resources allocation

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$$\hat{G}_{si} = \frac{\hat{A}_{si}^{\sigma-1}}{\sum_j \hat{A}_{sj}^{\sigma-1}} \frac{z_s^k}{1 + z_s^k} K_s$$

$$\hat{B}_{si} = \frac{\hat{A}_{si}^{\sigma-1}}{\sum_j \hat{A}_{sj}^{\sigma-1}} \frac{1}{1 + z_s^k} K_s$$

$$\tilde{L}_{si} = \frac{\hat{A}_{si}^{\sigma-1} / \tilde{A}_{si}^{\sigma}}{\sum_j \hat{A}_{sj}^{\sigma-1} / \tilde{A}_{sj}^{\sigma}} L_s$$

Back

Reallocation

Resources allocation

- Now, we need to find the optimal allocation of resources in the economy under two scenarios:

$$\begin{aligned}\hat{L}_{si} &= \frac{\hat{A}_{si}^{\sigma-1}}{\sum_j \hat{A}_{sj}^{\sigma-1}} L_s \\ \hat{G}_{si} &= \frac{\hat{A}_{si}^{\sigma-1}}{\sum_j \hat{A}_{sj}^{\sigma-1}} \frac{z_s^k}{1 + z_s^k} K_s \\ \hat{B}_{si} &= \frac{\hat{A}_{si}^{\sigma-1}}{\sum_j \hat{A}_{sj}^{\sigma-1}} \frac{1}{1 + z_s^k} K_s\end{aligned}$$

$$\begin{aligned}\tilde{L}_{si} &= \frac{\hat{A}_{si}^{\sigma-1} / \tilde{A}_{si}^{\sigma}}{\sum_j \hat{A}_{sj}^{\sigma-1} / \tilde{A}_{sj}^{\sigma}} L_s \\ \tilde{G}_{si} &= \frac{\hat{A}_{si}^{\sigma-1} / \tilde{A}_{si}^{\sigma}}{\sum_j \hat{A}_{sj}^{\sigma-1} / \tilde{A}_{sj}^{\sigma}} \frac{z_s^k}{1 + z_s^k} K_s \\ \tilde{B}_{si} &= \frac{\hat{A}_{si}^{\sigma-1} / \tilde{A}_{si}^{\sigma}}{\sum_j \hat{A}_{sj}^{\sigma-1} / \tilde{A}_{sj}^{\sigma}} \frac{1}{1 + z_s^k} K_s\end{aligned}$$

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