

CIS560

Obtaining a Good Database Design – Part 2

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Computer Science



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What's next?

- We briefly discussed the 3NF and BCNF.
- They are defined using:
 - Functional Dependencies
 - Keys
- We defined functional dependencies.
- We defined closures and how they help us find all functional dependencies.
- Now let's review keys.

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Superkeys and Keys

- A **superkey** is a set of attributes A_1, \dots, A_n s.t. for any other attribute B , we have $A_1, \dots, A_n \rightarrow B$
- A **key** is a minimal superkey
 - A set of attributes which is a superkey
 - And for which no subset is a superkey



Computing Keys

- Compute X^+ for all sets X
- If $X^+ = \text{all attributes}$, then X is a superkey
- We only want the keys
(*minimal superkeys*)



Example - What are the key(s)?

Enrollment(student, address, course, room, time)

student \rightarrow address
 room, time \rightarrow course
 student, course \rightarrow room, time

HINT: You can have more than one key.

Keys: {student, room, time}, {student, course}



How do we use keys to eliminate anomalies?

Each attribute must provide a fact
 about the **key**,
 the **whole key**,
 and **nothing but the key**.

Chris Date's adaptation to William Kent's summary



Boyce-Codd Normal Form

- A relation R is in BCNF if and only if for every functional dependency $X \rightarrow A$:
 - $X \rightarrow A$ is a trivial functional dependency
or
 - X is a superkey for R
- Equivalently: $\forall X$, where X is a set of attributes, either $(X^+ = X)$ or $(X^+ = \text{all attributes})$



Example

Name	ID	Phone	Department
Fred	123	206-555-1234	CIS
Fred	123	206-555-6543	CIS
Joe	987	908-555-2121	Math
Joe	987	206-151-7839	Math

$ID \rightarrow \text{Name, Department}$

What is the key?
{ID, Phone}

Hence $ID \rightarrow \text{Name, Department}$
is a “bad” dependency



BCNF Decomposition – Using FDs

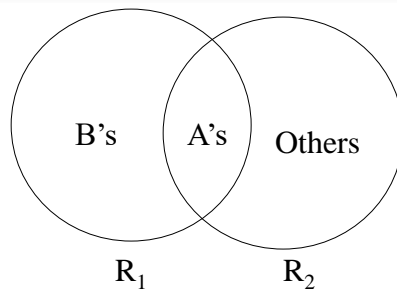
repeat

choose $A_1, \dots, A_m \rightarrow B_1, \dots, B_n$ that violates BCNF (bad FD)

split R into $R_1(A_1, \dots, A_m, B_1, \dots, B_n)$ and $R_2(A_1, \dots, A_m, [\text{others}])$

continue with both R_1 and R_2

until no more violations



A two-attribute relation
is always in BCNF.

Example

Name	ID	Phone	Department
Fred	123	206-555-1234	CIS
Fred	123	206-555-6543	CIS
Joe	987	908-555-2121	Math
Joe	987	206-151-7839	Math

$ID \rightarrow \text{Name, Department}$ is a bad functional dependency

Relation Decomposition

Name	<u>ID</u>	Department	Phone
Fred	123	CIS	206-555-1234
Fred	123	CIS	206-555-6543
Joe	987	Math	908-555-2121
Joe	987	Math	206-151-7839



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Relation Decomposition

Name	<u>ID</u>	Department
Fred	123	CIS
Joe	987	Math

<u>ID</u>	Phone
123	206-555-1234
123	206-555-6543
987	908-555-2121
987	206-151-7839



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BCNF Decomposition – Using Closures

repeat

find X s.t.: $X \neq X^+ \neq [\text{all attributes}]$

if (not found) **then** “ R is in BCNF”

let $Y = [\text{all attributes}] - X^+$

decompose R into $R_1(X^+)$ and $R_2(X \cup Y)$

continue with both R_1 and R_2

until no X is found



Example BCNF Decomposition – Using Closures

Student(name, ID, age, hairColor, phoneNumber)

ID \rightarrow name, age

age \rightarrow hairColor

Iteration 1: Student $X = \text{ID}$

$\text{ID}^+ = \{\text{ID}, \text{name}, \text{age}, \text{hairColor}\}$

Decompose into: Student1(ID, name, age, hairColor)

Phone(ID, phoneNumber)

Iteration 2: Student1 $X = \text{age}$

$\text{age}^+ = \{\text{age}, \text{hairColor}\}$

Decompose: Hair(age, hairColor)

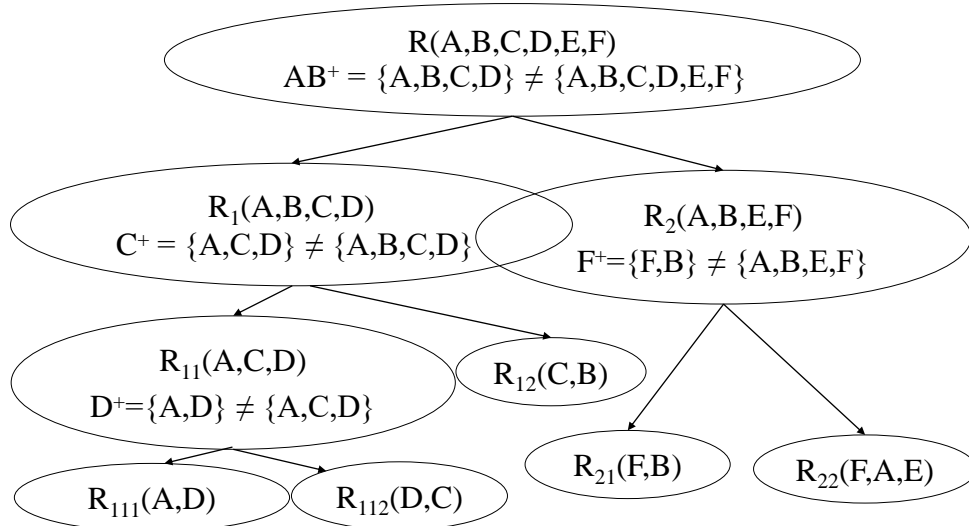
Student2(ID, name, age)



Example

 $R(A,B,C,D,E,F)$
 $AB \rightarrow C$
 $C \rightarrow D$
 $F \rightarrow B$
 $D \rightarrow A$

What are the keys ?

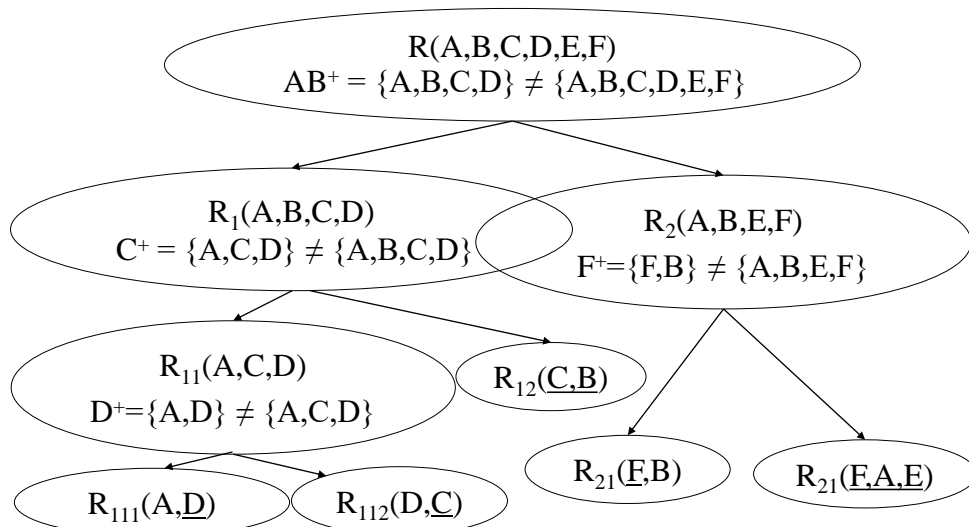


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Example

 $R(A,B,C,D,E,F)$
 $AB \rightarrow C$
 $C \rightarrow D$
 $F \rightarrow B$
 $D \rightarrow A$

What are the keys ?



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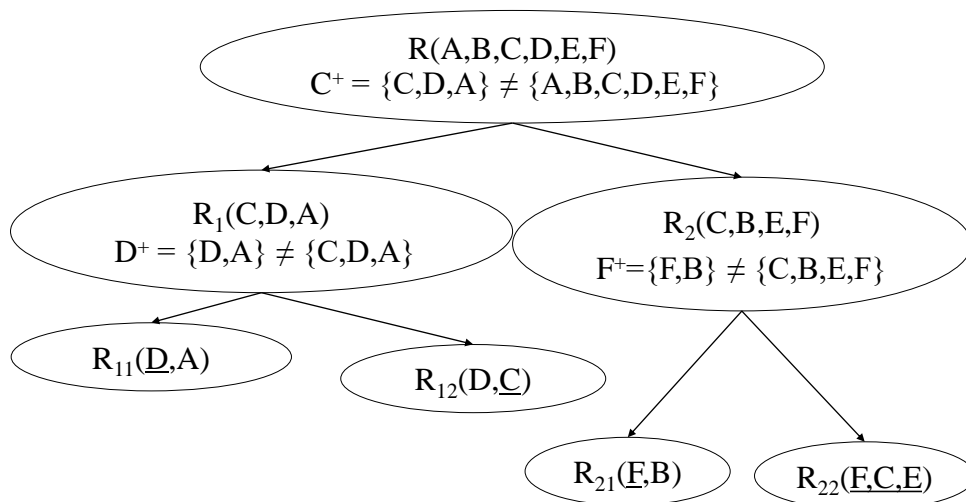
Is the resulting BCNF schema unique?



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Example – Solution 2

$R(A,B,C,D,E,F)$	$AB \rightarrow C$
	$C \rightarrow D$
	$F \rightarrow B$
	$D \rightarrow A$



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Which solution is better?

$$R_{111}(A, \underline{D}), R_{112}(D, \underline{C}), R_{12}(\underline{C}, \underline{B}), R_{21}(\underline{E}, B), R_{22}(\underline{E}, \underline{A}, \underline{E})$$

OR

$$R_{11}(A, \underline{D}), R_{12}(D, \underline{C}), R_{21}(\underline{E}, B), R_{22}(\underline{E}, \underline{C}, \underline{E})$$


Which solution is better?

- From the theoretical point of view...
Both solutions are good.
- From a practical point of view...
It depends.
- Look at the common ways they are queried, for example.

