

Part II: Mechanics. Given the following LP models (represented abstractly with decision variables X and Y), find the optimal solution using the 'graphing' approach.

Your solution MUST show the following:

A) Graph

- Plotting all 3 constraints
- Shading in the feasible region of the entire LP model
- Identification of the relevant extreme points

B) Relevant Extreme Points

- Calculate the (X,Y) values of each relevant Extreme Point
- Show the algebraic calculations of how the (X,Y) values of the Extreme Points were calculated (eyeballing a picture is not sufficient).

C) Optimal Solution

- Evaluate each Extreme Point by the objective function
- Identify which extreme point is the 'best'.

	X	Y	
A	4	32	324
B	12	16	332
C	36	0	612

5)

Minimize

$$17X + 8Y$$

Subject to:

$$2X + 3Y \geq 72$$

$$4X + 2Y \geq 80$$

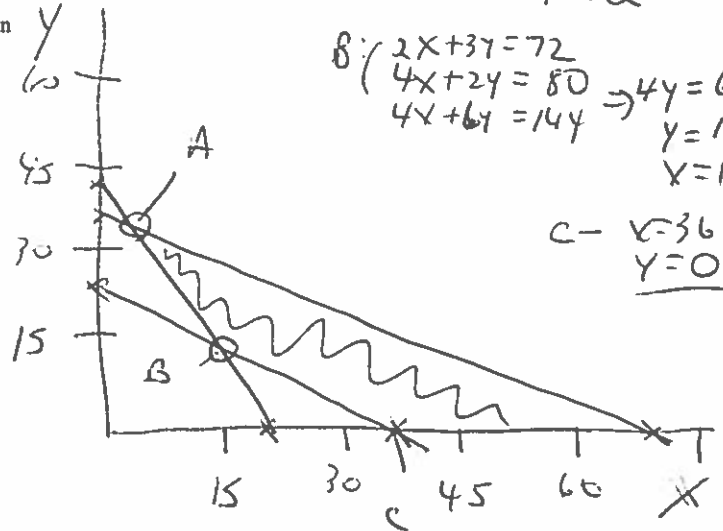
$$X + 2Y \leq 68$$

And non-negativity, of course.

$$\begin{array}{rcl} A: & X + 2Y = 68 & \\ & 4X + 2Y = 80 & \\ \hline & 3X = 12 & X = 4 \\ & & Y = 32 \end{array}$$

$$\begin{array}{rcl} B: & 2X + 3Y = 72 & \\ & 4X + 2Y = 80 & \\ & 4X + 6Y = 144 & \Rightarrow 4Y = 64 \\ & & Y = 16 \\ & & X = 12 \end{array}$$

$$C: X = 36, Y = 0$$



6)

Minimize

$$7X + 5Y$$

Subject to the following constraints:

$$6X + 8Y \geq 96$$

$$2X + 3Y \leq 54$$

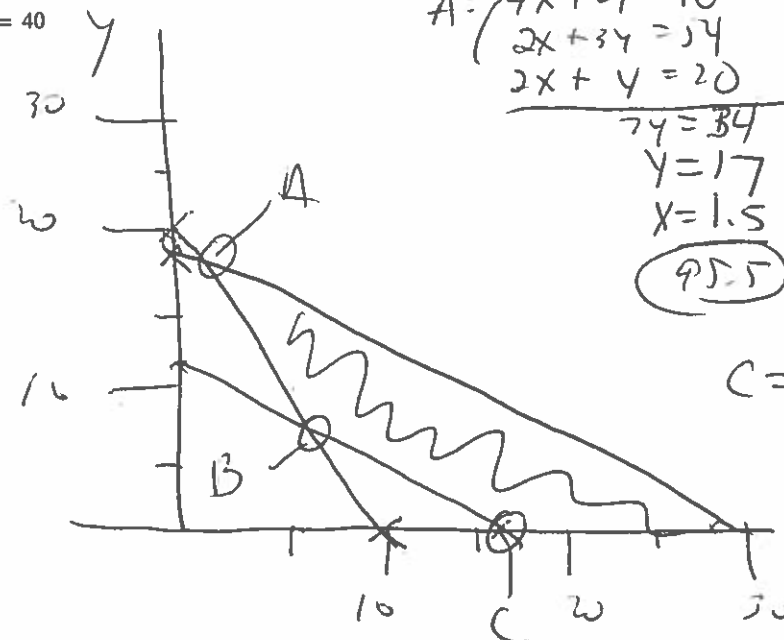
$$4X + 2Y \geq 40$$

And non-negativity, of course.

$$\begin{array}{rcl} A: & 4X + 2Y = 40 & \\ & 2X + 3Y = 54 & \\ & 2X + Y = 20 & \\ \hline & 7Y = 34 & Y = 4.857 \\ & & X = 1.5 \end{array}$$

$$\begin{array}{rcl} B: & 6X + 8Y = 96 & \\ & 4X + 2Y = 40 & \\ & 16X + 8Y = 160 & \\ \hline & 10X = 64 & X = 6.4 \\ & & Y = 7.2 \end{array}$$

$$C: X = 10, Y = 0 \quad 112$$



Best