

Moscow Institute of Physics and Technology

My Pity

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Whatever contest today

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Moscow IPT (Alekseev, Ivaschenko, Kolodzey)
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 Manacher.h \ \dots \dots \dots \dots \dots \dots \dots \dots
Contest (1)
template.cpp
                                13 lines
#include <bits/extc++.h>
using namespace std;
#define WHOLE(v) v.begin(), v.end()
#define sz(v) static cast<int>(v.size())
using i64 = int64_t;
int main() {
 cin.sync_with_stdio(false);
 cin.tie(nullptr);
cin.exceptions(cin.failbit);
                                 3 lines
set nocp si aw ai is ts=2 sw=2 et tm=100 nu bg=dark
im jj <esc>
<u>Data structures</u> (2)
SparseTable.h
                                27 lines
template < class T, class Better = std::less < T >>
struct SparseTable {
 explicit SparseTable(vector<T> vals) {
  log2.push_back(0);
for (int i = 1; i <= sz(vals); ++i) {</pre>
   log2.push\_back(log2.back() + (2 << log2.back() < i));
```

```
explicit SparseTable(vector<T> vals) {
  log2.push_back(0);
  for (int i = 1; i <= sz(vals); ++i) {
    log2.push_back(log2.back() + (2 << log2.back() < i));
  }

  table.push_back(std::move(vals));
  for (int p = 1; log2.back() >= sz(table); ++p) {
    auto& row = table.emplace_back();
    for (int i = 0; i + (1<<p) <= sz(table[0]); ++i) {
        row.push_back(get(i, i + (1<<p)));
    }
  }
}

T get(int begin, int end) const {
  int p = log2[end - begin];</pre>
```

return min(table[p][begin], table[p][end - (1<<p)], better);</pre>

Numerical (3)

vector<vector<T>> table; vector<int> log2; Better better;

PolvRoots.h

private:

```
Description: Finds the real roots to a polynomial. 
Usage: poly_roots (\{\{2,-3,1\}\},-1e9,1e9\}) // solve x^2-3x+2=0 
Time: \mathcal{O}\left(n^2\log(1/\epsilon)\right)
```

```
vector<double> poly_roots(Poly p, double xmin, double xmax) {
  if (sz(p.a) == 2) { return {-p.a[0]/p.a[1]}; }
   vector<double> ret;
   Poly der = p;
  der.diff();
  auto dr = poly_roots(der, xmin, xmax);
  dr.push_back(xmin-1):
  dr.push back(xmax+1);
  sort(all(dr));
   rep(i,0,sz(dr)-1)
     double 1 = dr[i], h = dr[i+1];
     bool sign = p(1) > 0;
if (sign ^ (p(h) > 0))
       clean (p(n) > 0) (
rep(it,0,60) { // while (h - l > 1e-8)
double m = (1 + h) / 2, f = p(m);
if ((f <= 0) ^ sign) l = m;</pre>
          else h = m;
        ret.push_back((1 + h) / 2);
  return ret;
```

PolyInterpolate.h

Description: Given n points (x[i], y[i]), computes an n-1-degree polynomial p that passes through them: $p(x) = a[0] * x^0 + \ldots + a[n-1] * x^{n-1}$. For numerical precision, pick $x[k] = c * \cos(k/(n-1) * \pi), k = 0 \ldots n-1$. **Time:** $\mathcal{O}(n^2)$

```
typedef vector<double> vd;
vd interpolate(vd x, vd y, int n) {
  vd res(n), temp(n);
  rep(k,0,n-1) rep(i,k+1,n)
    y[i] = (y[i] - y[k]) / (x[i] - x[k]);
  double last = 0; temp[0] = 1;
  rep(k,0,n) rep(i,0,n) {
    res[i] += y[k] * temp[i];
    swap(last, temp[i]);
    temp[i] -= last * x[k];
  }
  return res;
}
```

${ m Solve Linear.h}$

Description: Solves A*x=b. If there are multiple solutions, an arbitrary one is returned. Returns rank, or -1 if no solutions. Data in A and b is lost. **Time:** $\mathcal{O}\left(n^2m\right)$

```
int solveLinear(vector<vector<double>& A, vector<double>& b,
      vector<double& x) {</pre>
  int n = sz(A), m = sz(x), rank = 0, br, bc;
if (n) assert(sz(A[0]) == m);
  vector<int> col(m); iota(WHOLE(col), 0);
  for (int i = 0; i < n; ++i) {
     double v, bv = 0;
     for (int r = i; r < n; ++r) for (int c = i; c < m; ++c)
        if ((v = fabs(A[r][c])) > bv)
          br = r, bc = c, bv = v;
     if (bv < eps) {
  for (int j = 0; j < n; ++j)</pre>
          if (fabs(b[j]) > eps)
             return -1;
       break;
     swap(A[i], A[br]);
     swap(b[i], b[br]);
swap(col[i], col[bc]);
     for (int j = 0; j < n; ++j)
  swap(A[j][i], A[j][bc]);</pre>
     bv = 1. / A[i][i];
for (int j = i + 1; j < n; ++j) {
   double fac = A[j][i] * bv;</pre>
        b[j] -= fac * b[i];

for (int k = i + 1; k < m; ++k)
          A[j][k] -= fac * A[i][k];
     rank++;
  x.assign(m, 0);
  for (int i = rank; i--;) {
    b[i] /= A[i][i];
     x[col[i]] = b[i];
for (int j = 0; j < i; ++j)
b[j] -= A[j][i] * b[i];</pre>
```

SolveLinear2.h

 $23 \underline{\text{lines}}$

Description: To get all uniquely determined values of x back from SolveLinear, make the following changes:

return rank; // (multiple solutions if rank < m)

```
"SolveLinear.h" 8 lines
for(int j = 0; j < n; ++j)if(j != i) // instead of for(j=i+1; j<n)
// ... then at the end:
x.assign(m, undefined);
for (int i = 0; i < rank; ++i) {</pre>
```

```
for (int j = rank; j < m; ++j)
  if (fabs(A[i][j]) > eps) goto fail;
x[col[i]] = b[i] / A[i][i];
Fail:; }
```

FastFourierTransform.h

Description: Computes $\hat{f}(k) = \sum_x f(x) \exp(-2\pi i k x/N)$ for all k. Useful for convolution: conv (a, b) = c, where $c[x] = \sum_x a[i]b[x-i]$. a and b should be of roughly equal size. For convolutions of integers, consider using a number-theoretic transform instead, to avoid rounding issues.

Time: $\mathcal{O}\left(N\log N\right)$

```
typedef valarray<complex<double> > carray;
void fft (carray& x, carray& roots) {
  int N = sz(x);
   if (N <= 1) return;</pre>
  carray even = x[slice(0, N/2, 2)];

carray odd = x[slice(1, N/2, 2)];

carray rs = roots[slice(0, N/2, 2)];
   fft(even, rs);
   fft(odd, rs);
   rep(k,0,N/2) {
     auto t = roots[k] * odd[k];
x[k] = even[k] + t;
x[k+N/2] = even[k] - t;
  }
typedef vector<double> vd;
vd conv(const vd& a, const vd& b) {
  int s = sz(a) + sz(b) - 1, L = 32-_builtin_clz(s), n = 1<<L;</pre>
   if (s <= 0) return {};
  carray av(n), bv(n), roots(n);
rep(i,0,n) roots[i] = polar(1.0, -2 * M_PI * i / n);
   copy(all(a), begin(av)); fft(av, roots);
   copy(all(b), begin(bv)); fft(bv, roots);
  roots = roots.apply(conj);
carray cv = av * bv; fft(cv, roots);
   vd c(s); rep(i,0,s) c[i] = cv[i].real() / n;
```

NumberTheoreticTransform.h

Description: Can be used for convolutions modulo specific nice primes of the form 2^ab+1 , where the convolution result has size at most 2^a . For other primes/integers, use two different primes and combine with CRT. May return negative values.

```
\mathbf{Time:} \ \mathcal{O}\left(N\log N\right)
```

```
<code>const</code> 11 mod = (119 << 23) + 1, root = 3; // = 998244353 // For p < 2^30 there is also e.g. (5 << 25, 3), (7 << 26, 3), // (479 << 21, 3) and (483 << 21, 5). The last two are > 10^9.
typedef vector<ll> v1;
void ntt(ll* x, ll* temp, ll* roots, int N, int skip) {
   if (N == 1) return;
   int n2 = N/2;
               , temp, roots, n2, skip*2);
  ntt(x+skip, temp, roots, n2, skip*2);
rep(i,0,N) temp[i] = x[i*skip];
   rep(i,0,n2) {
     ll s = temp[2*i], t = temp[2*i+1] * roots[skip*i];
      x[skip*i] = (s + t) % mod; x[skip*(i+n2)] = (s - t) % mod;
void ntt(vl& x, bool inv = false) {
   11 e = modpow(root, (mod-1) / sz(x));
   if (inv) e = modpow(e, mod-2);
   vl roots(sz(x), 1), temp = roots;
   rep(i,1,sz(x)) roots[i] = roots[i-1] * e % mod;
   \texttt{ntt}(\&x[0], \&\texttt{temp}[0], \&\texttt{roots}[0], \texttt{sz}(x), \texttt{1});
vl conv(vl a, vl b) {
  int s = sz(a) + sz(b) - 1; if (s <= 0) return {};
int L = s > 1 ? 32 - _builtin_clz(s - 1) : 0, n = 1 << L;
if (s <= 200) { // (factor 10 optimization for |a|, |b| = 10)</pre>
       \begin{array}{lll} \texttt{rep(i,0,sz(a))} & \texttt{rep(j,0,sz(b))} \\ \texttt{c[i+j]} & = (\texttt{c[i+j]} + \texttt{a[i]} * \texttt{b[j]}) \; \$ \; \texttt{mod;} \\ \end{array} 
      return c;
   a.resize(n); ntt(a);
   b.resize(n); ntt(b);
  v1 c(n); 11 d = modpow(n, mod-2);
rep(i,0,n) c[i] = a[i] * b[i] % mod * d % mod;
  ntt(c, true); c.resize(s); return c;
```

Strings (4)

SuffixArray.h

```
struct SuffixArray {
   string s;
   vector<int> order, rank, lcp;

SuffixArray(const string& _s): s(_s + '$') {
```

```
int n = sz(s);
     std::vector<int> count(n + 130), nextPos(count.size() + 1);
     std::vector<int> nextOrder(n), nextColor(n);
     std::vector<int> color(WHOLE(s));
     auto norm = [n] (int i) {
  return i < 0 ? i + n : i >= n ? i - n : i;
     order.resize(n);
     std::iota(WHOLE(order), 0);
     std::sort (WHOLE (order)
          [&] (int aa, int bb) { return s[aa] < s[bb]; });
     for (int half = 1; half < n; half *= 2) {</pre>
       count.assign(count.size(), 0);
       for (auto col : color)
          ++count[col];
       nextPos[0] = 0;
       partial sum(WHOLE(count), nextPos.begin() + 1);
       for (auto pos : order) {
          auto shifted = norm(pos - half);
          nextOrder[nextPos[color[shifted]]++] = shifted;
       order.swap(nextOrder);
       nextColor[order[0]] = 0;
       for (int i = 1; i < n; ++i) {
  auto pos = order[i], prev = order[i - 1];</pre>
         nextColor[pos] = nextColor[prev] + (
    tie(color[pos], color[norm(pos + half)]) !=
    tie(color[prev], color[norm(prev + half)])
         );
       color.swap(nextColor);
     rank.resize(n);
for (int i = 0; i < n; ++i)</pre>
       rank[order[i]] = i;
     lcp.resize(n);
for (int i = 0; i < n; ++i) if (rank[i]) {
  for (int p0 = order[rank[i] - 1]; s[i + h] == s[p0 + h];)</pre>
         h++;
       lcp[rank[i]] = h;
       h = h > 0;
  }
};
```

Hashes.h

```
using Hash = array<ui64, 3>;
#define HOP(op)
  inline Hash operator op (Hash a, Hash b) { \
    return {a[0] op b[0], a[1] op b[1], a[2] op b[2]}; \
HOP (+) HOP (-) HOP (*) HOP (%)
inline Hash makeHash(ui64 val) { return {val, val, val}; }
const Hash Multiplier{{228227, 227223, 22823}};
const Hash Modulus{{424242429, 2922827, 22322347}};
vector<Hash> pows(1);
struct Hashes {
  explicit Hashes(const string& s) {
    pows.front().fill(1);
    while (pows.size() <= s.size())</pre>
      pows.push_back(pows.back() * Multiplier % Modulus);
    prefs.push_back(makeHash(0));
    for (auto c : s)
      prefs.push_back((prefs.back() * Multiplier + makeHash(c))
          % Modulus);
  Hash get(size_t begin, size_t end) const {
  return (prefs[end] - prefs[begin] * pows[end - begin]
        % Modulus + Modulus) % Modulus;
private:
  vector<Hash> prefs;
```

AhoCorasick.h

57 lines

Description: on-line tracking of the set of suffixes of a text that are prefixes of some words from a dictionary.

```
struct AhoCorasick {
   AhoCorasick(): n(1) {
      n.reserve(TrieSize);
   }

void addWord(const string& word, int id) {
   int v = 0;
   for (int ch : word) {
      ch -= 'a';
      auto& u = n[v].trans[ch];
      if (!u) {
```

```
u = int(n.size());
           n.emplace_back();
     n[v].termId = id;
  void build() {
     queue<int> q;
      for (q.push(0); !q.empty(); q.pop()) {
         auto v = q.front();
        for (Char ch = 0; ch < Alph; ++ch) {
  auto& u = n[v].trans[ch];</pre>
            if (!u) {
              u = n[n[v].link].trans[ch];
              continue;
           q.push(u);
           q.pash(u),
auto i = n[u].link = (v ? n[n[v].link].trans[ch] : 0);
n[u].nextTerm = (n[i].termId >= 0 ? i : n[i].nextTerm);
private:
  struct Node {
     int trans[Alph]{};
     int nextTerm = -1, termId = -1, link = 0;
  vector<Node> n;
};
ZFunction.h
\textbf{Description:}\ z[x]\ is\ max\ L\colon s[x{:}x{+}L] == s[{:}L]
                                                                                          11 lines
vector<size_t> zFun(const string& s) {
  vector<size_t> z(s.size(), 0);
  for (size_t left = 0, right = 0, i = 1; i < s.size(); ++i) {
  z[i] = (i < right ? min(right - i, z[i - left]) : 0);
  while (i + z[i] < s.size() && s[i + z[i]] == s[z[i]])</pre>
         ++z[i];
     if (i + z[i] > right)
  tie(left, right) = {i, i + z[i]};
  return z;
PrefixFunction.h
Description: pi[x] is the length of the longest prefix of s that ends at x, other
than s[0..x] itself
                                                                                         10 lines
vector<size_t> pi(const string& s) {
  vector<size_t> p(s.size(), 0);
for (size_t i = 1; i < s.size(); ++i) {</pre>
     auto px = p[i - 1];
     while (px && s[i] != s[px])
     px = p[px - 1];

p[i] = px + (s[i] == s[g]);
  return p;
Manacher.h
Description: For each position in a string, computes p[0][i] = half length of
longest even palindrome around pos i, p[1][i] = longest odd (half rounded down).
void manacher(const string& s) {
  auto n = int(s.size());
   vector<int> p[2];
  p[0].resize(n + 1);
  p[1].resize(n);
  p[1].res12e(n);
for (int z = 0; z < 2; ++z) {
    for (int i=0, l=0, r=0; i < n; ++i) {
        int t = r - i + !z;
        if (i<r) p[z][i] = min(t, p[z][1 + t]);
        int L = i - p[z][i], R = i + p[z][i] - !z;
        while (L >= 1 && R + 1 < n && s[L - 1] == s[R + 1])</pre>
        p[z][i]++, L--, R++;
if (R > r)
           tie(1, r) = \{L, R\};
  }
```