

# North South University

Department of Electrical and Computer Engineering

Final Exam, Spring 2019

Semiconductor Devices Technology (EEE 313.01/ETE 411.01/EEE 410.01/ETE 443.01)

Time: 70 minutes

Full marks: 30

There are three questions. Attempt answers to all. Individual marks are indicated at the right margin.

1. (a) How built-in voltage  $V_{bi}$  is related to diode on current? If  $V_{bi}$  of a diode is higher or lower, how does it impact the magnitude of diode on current?

(b) A silicon pn junction at  $T = 300$  K has the following parameters:  $N_A = 4 \times 10^{15} \text{ cm}^{-3}$ ,  $N_D = 7 \times 10^{16} \text{ cm}^{-3}$ ,  $D_n = 25 \text{ cm}^2/\text{s}$ ,  $D_p = 15 \text{ cm}^2/\text{s}$ ,  $\tau_{n0} = 7.9 \times 10^{-7} \text{ s}$  and  $\tau_{p0} = 3.8 \times 10^{-7} \text{ s}$ . The cross sectional area is  $A = 4 \times 10^{-4} \text{ cm}^2$  and the forward bias voltage is  $V_a = 0.6$  V. Calculate the total current  $I_{\text{total}}$  (A) in the p-n junction diode. Value of  $n_i$  at  $T = 300$  K is  $1.5 \times 10^{10} \text{ cm}^{-3}$ .

[4+6=10]

Useful equations:

$$I_{\text{diode}} = q \left( \frac{D_p p_{n0}}{L_p} + \frac{D_n n_{p0}}{L_n} \right) \left( \exp\left(\frac{V_a}{V_T}\right) - 1 \right) \quad (\text{A/cm}^2) \quad L_p^2 = D_p \tau_{p0}$$

$$L_n^2 = D_n \tau_{n0} \quad V_T = \frac{kT}{q} \quad V_{bi} = \frac{kT}{q} \ln \left( \frac{N_A N_D}{n_i^2} \right)$$

2. (a) At flat band voltage  $V_{FB}$ , is the surface band bending  $\psi_s = 0$  or  $<0$  or  $>0$ . Explain.

(b) How can you achieve a low enhancement mode  $V_T > 0$  for an n-MOS capacitor? (Hint: write the  $V_T$  equation and identify the parameters that affect  $V_T$ ).

(c) For a n-MOS silicon capacitor, at  $T = 300$  K, the substrate doping is  $N_A = 3.2 \times 10^{16} \text{ cm}^{-3}$ .

(i) What is bulk potential,  $\phi_B$ ?

(ii) At inversion condition what is  $\psi_s$ ? (Hint:  $\phi_s$  is total band bending at the surface).

(iii) For  $\phi_{ms} = 4.45$  eV and  $\chi = 4.01$  eV (for silicon), what is the flatband voltage  $V_{FB} = \phi_{ms}$ ?

(iv) Find the maximum depletion width  $x_{dT}$  ( $\mu\text{m}$ ) at the inversion condition of the surface. Value of  $n_i$  at  $T = 300$  K is  $1.5 \times 10^{10} \text{ cm}^{-3}$ .

[2+2+1.5x4=10]

Useful equations:

$$x_{dT} = \left( \frac{2\epsilon_s \psi_s}{qN_A} \right)^{1/2} \quad \epsilon_0 = 11.7 \epsilon_{\text{vac}} \quad \phi_B = \frac{kT}{q} \ln \left( \frac{N_A}{n_i} \right)$$

3. (a) Suppose for a n-channel MOSFET, drain current at a particular  $V_T$  is in the linear mode operation. Consider two cases: (i) high  $V_{gs}$ , low  $V_{ds}$  and (ii) high  $V_{gs}$ , high  $V_{ds}$ ? Which case will produce higher value of drain current? Explain. (Hint: use the MOSFET drain current equation for linear mode).

(b) An ideal n-channel MOSFET has the following parameters:  $V_T = 0.42$  V,  $\mu_n = 730 \text{ cm}^2/\text{V-s}$ ,  $t_{ox} = 10.4$  nm,  $W = 11 \mu\text{m}$  and  $L = 1.2 \mu\text{m}$ . Find the drain current  $I_{ds}$  for this MOSFET when

(i)  $V_{gs} = 0.25$  V and  $V_{ds} = 0.15$  V.

(ii)  $V_{gs} = 1.6$  V and  $V_{ds} = 0.4$  V.

(iii)  $V_{gs} = 1.8$  V and  $V_{ds} = 2.4$  V.

[3+2+2.5x2=10]

# North South University

Department of Electrical and Computer Engineering

Final Exam, Spring 2019

Semiconductor Devices Technology (EEE 313.02/ETE 411.02/EEE 410.02/ETE 443.02)

Full marks: 30

Time: 70 minutes

There are three questions. Attempt answers to all. Individual marks are indicated at the right margin.

- 1 (a) Using the diode current equation, show that for a p-n junction diode, electron current density is enhanced if p-side doping is lower than n-side doping. Explain. Why  $D_n$  is higher than  $D_p$ ?
- (b) A silicon pn junction at  $T = 300$  K has the following parameters:  $N_A = 5 \times 10^{15} \text{ cm}^{-3}$ ,  $N_D = 7.5 \times 10^{16} \text{ cm}^{-3}$ ,  $D_n = 24 \text{ cm}^2/\text{s}$ ,  $D_p = 14 \text{ cm}^2/\text{s}$ ,  $\tau_{n0} = 7.8 \times 10^{-7} \text{ s}$  and  $\tau_{p0} = 3.7 \times 10^{-7} \text{ s}$ . The cross sectional area is  $A = 4.5 \times 10^{-3} \text{ cm}^2$  and the forward bias voltage is  $V_a = 0.6 \text{ V}$ . Calculate the total current  $I_{\text{diode}}$  (A) in the p-n junction diode. Value of  $n_i$  at  $T = 300$  K is  $1.5 \times 10^{10} \text{ cm}^{-3}$ .

[4+6=10]

Useful equations:

$$J_{\text{Diode}} = q \left( \frac{D_p p_{n0}}{L_p} + \frac{D_n n_{p0}}{L_n} \right) \left( \exp\left(\frac{V_a}{V_T}\right) - 1 \right) \quad (\text{A/cm}^2) \quad L_p^2 = D_p \tau_{p0}$$

$$L_n^2 = D_n \tau_{n0} \quad V_T = \frac{kT}{q} \quad V_{bi} = \frac{kT}{q} \ln \left( \frac{N_A N_D}{n_i^2} \right)$$

2. (a) If at the threshold of inversion, electron concentration at the surface is  $n_s = N_A$  which is at the bulk for n-MOS capacitor, then at (i) depletion and (ii) moderate inversion, comment whether  $n_s > N_A$  or  $n_s < N_A$ .
- (b) How can you achieve a low depletion mode  $V_T < 0$  for an n-MOS capacitor? (Hint: write the  $V_T$  equation and identify the parameters that affect  $V_T$ ).
- (c) For a n-MOS silicon capacitor, at  $T = 300$  K, the substrate doping is  $N_A = 3.5 \times 10^{16} \text{ cm}^{-3}$ .
- (i) What is bulk potential,  $\phi_B$ ?
- (ii) At inversion condition what is  $\psi_s$ ? (Hint:  $\phi_s$  is total band bending at the surface).
- (iii) For  $\phi_m = 4.49 \text{ eV}$  and  $\chi = 4.01 \text{ eV}$  (for silicon), what is the flatband voltage  $V_{FB} = \phi_{ms}$ ?
- (iv) Find the maximum depletion width  $x_{dT}$  ( $\mu\text{m}$ ) at the inversion condition of the surface. Value of  $n_i$  at  $T = 300$  K is  $1.5 \times 10^{10} \text{ cm}^{-3}$ .

[2+2+1.5 x 4=10]

Useful equations:

$$x_{dT} = \left( \frac{2\epsilon_s \psi_s}{q N_A} \right)^{1/2} \quad \epsilon_s = 11.7 \epsilon_0 \quad \phi_B = \frac{kT}{q} \ln \left( \frac{N_A}{n_i} \right)$$

0.625<sup>0</sup>

3. (a) Suppose for a n-channel MOSFET, drain current at a particular  $V_T$  is in the saturation mode of operation. Consider two cases: (i) high  $V_{ds}$  (sat) and (ii) low  $V_{ds}$  (sat). Comment whether drain current for case (i) is higher or lower than case (ii). Explain. (Hint: use the MOSFET drain current equation for saturation mode).
- (b) An ideal n-channel MOSFET has the following parameters:  $V_T = 0.44 \text{ V}$ ,  $\mu_n = 725 \text{ cm}^2/\text{V-s}$ ,  $t_{ox} = 10.7 \text{ nm}$ ,  $W = 11.3 \mu\text{m}$  and  $L = 1.3 \mu\text{m}$ . Find the drain current  $I_{ds}$  for this MOSFET when

- (i)  $V_{gs} = 0.22 \text{ V}$  and  $V_{ds} = 0.14 \text{ V}$ .

[3+2+2.5x2=10]

(ii)  $V_{gs} = 1.4 \text{ V}$  and  $V_{ds} = 0.45 \text{ V}$ .

(iii)  $V_{gs} = 1.75 \text{ V}$  and  $V_{ds} = 2.4 \text{ V}$ .

Make sure to apply the above bias conditions to determine cut-off, linear case and saturation case for calculation of drain current.

Useful equations:

$$I_{ds} = \mu_n C_{ox} \frac{W}{L} \left\{ (V_{gs} - V_T) V_{ds} - \frac{V_{ds}^2}{2} \right\}$$

$$I_{ds} = \mu_n C_{ox} \frac{W}{L} \frac{(V_{gs} - V_T)^2}{2}$$



**North South University**  
Department of Electrical and Computer Engineering  
Final Exam, Summer 2017

**Semiconductor Devices Technology (EEE 313.01/ETE 411.01/EEE 410.01/ETE 443.01)**

Full marks: 30

Time: 70 minutes

There are three questions. Attempt answers to all. Individual marks are indicated at the right margin.

1. A silicon pn junction at  $T = 300$  K has the following parameters:  $N_A = 5 \times 10^{16} \text{ cm}^{-3}$ ,  $N_D = 3 \times 10^{17} \text{ cm}^{-3}$ ,  $D_n = 22 \text{ cm}^2/\text{s}$ ,  $D_p = 15 \text{ cm}^2/\text{s}$ ,  $\tau_{n0} = 5.5 \times 10^{-7} \text{ s}$  and  $\tau_{p0} = 2.2 \times 10^{-7} \text{ s}$ . The cross sectional area is  $A = 3 \times 10^{-4} \text{ cm}^2$  and the forward bias voltage is  $V_a = 0.69 \text{ V}$ . Calculate the total current  $I_{\text{diode}}$  (A) in the p-n junction diode. Value of  $n_i$  at  $T = 300$  K is  $1.5 \times 10^{10} \text{ cm}^{-3}$ . [10]

Useful equations:

$$J_{D \text{ Total}} = q \left( \frac{D_p p_{n0}}{L_p} + \frac{D_n n_{p0}}{L_n} \right) \left( \exp\left(\frac{V_a}{V_T}\right) - 1 \right) \text{ (A/cm}^2\text{)} \quad L_p^2 = D_p \tau_{p0}$$

$$L_n^2 = D_n \tau_{n0} \quad V_T = \frac{kT}{q}$$

2. For a p-substrate silicon MOS capacitor, at  $T = 300$  K, the substrate doping is  $N_A = 7 \times 10^{16} \text{ cm}^{-3}$ .

- What is bulk potential,  $\phi_B$ ?
- At inversion condition what is  $\phi_s$ ? (Hint:  $\phi_s$  is total band bending at the surface).
- For  $\phi_m = -4.28 \text{ eV}$  and  $\chi = 4.01 \text{ eV}$  (for silicon), what is the flatband voltage  $V_{FB} = \phi_{ms}$ ?
- Find the maximum depletion width  $x_{dT}$  ( $\mu\text{m}$ ) at the inversion condition of the surface. Value of  $n_i$  at  $T = 300$  K is  $1.5 \times 10^{10} \text{ cm}^{-3}$ . [5×2=10]

Useful equations:

$$x_{dT} = \left( \frac{2\epsilon_s \phi_s}{q N_A} \right)^{1/2} \quad \epsilon_s = 11.7 \epsilon_0 \quad \phi_B = \frac{kT}{q} \ln \left( \frac{N_A}{n_i} \right)$$

3. An ideal n-channel MOSFET has the following parameters:  $V_T = 0.42 \text{ V}$ ,  $\mu_n = 560 \text{ cm}^2/\text{V-s}$ ,  $t_{ox} = 10 \text{ nm}$ ,  $W = 10 \mu\text{m}$  and  $L = 0.8 \mu\text{m}$ . Find the drain current  $I_{ds}$  for this MOSFET when

- $V_{gs} = 0.9 \text{ V}$  and  $V_{ds} = 0.2 \text{ V}$ . [3.5]
- $V_{gs} = 1.6 \text{ V}$  and  $V_{ds} = 1.5 \text{ V}$ . [3.5]
- $V_{gs} = 0.1 \text{ V}$  and  $V_{ds} = 0.2 \text{ V}$ . [3.0]

Make sure to apply the above bias conditions to determine cut-off, linear case and saturation case for calculation of drain current.

Useful equations:

$$I_{ds} = \mu_n c_{ox} \frac{W}{L} \left\{ (V_{gs} - V_T) V_{ds} - \frac{V_{ds}^2}{2} \right\} \quad I_{ds} = \mu_n c_{ox} \frac{W}{L} \frac{(V_{gs} - V_T)^2}{2}$$

# North South University

Department of Electrical and Computer Engineering

Final Exam, Fall 2017

**Semiconductor Devices Technology (EEE 313.01/ETE 411.01/EEE 410.01/ETE 443.01)**

Full marks: 30

Time: 70 minutes

There are three questions. Attempt answers to all. Individual marks are indicated at the right margin.

1. A silicon pn junction at  $T = 300$  K has the following parameters:  $N_A = 7 \times 10^{16} \text{ cm}^{-3}$ ,  $N_D = 1.5 \times 10^{17} \text{ cm}^{-3}$ ,  $D_n = 20 \text{ cm}^2/\text{s}$ ,  $D_p = 13 \text{ cm}^2/\text{s}$ ,  $\tau_{n0} = 5.6 \times 10^{-7} \text{ s}$  and  $\tau_{p0} = 1.9 \times 10^{-7} \text{ s}$ . The cross sectional area is  $A = 3 \times 10^{-4} \text{ cm}^2$  and the forward bias voltage is  $V_a = 0.15 \text{ V}$ . For recombination current calculation,  $\tau_{n0r} = 7 \times 10^{-4} \text{ s}$ ,  $\tau_{p0r} = 7 \times 10^{-4} \text{ s}$ . Calculate the total current  $I_{\text{diode}}$  (A) in the p-n junction diode. Value of  $n_i$  at  $T = 300$  K is  $1.5 \times 10^{10} \text{ cm}^{-3}$ . [10]

Useful equations:

$$J_{D \text{ Total}} = q \left( \frac{D_p p_{n0}}{L_p} + \frac{D_n n_{p0}}{L_n} \right) \left( \exp\left(\frac{V_a}{V_T}\right) - 1 \right) \text{ (A/cm}^2\text{)} \quad L_p^2 = D_p \tau_{p0}$$

$$L_n^2 = D_n \tau_{n0} \quad V_T = \frac{kT}{q} \quad W = \sqrt{\left\{ \frac{2\epsilon_s(V_{bi} - V_a)}{q} \left[ \frac{N_A + N_D}{N_A N_D} \right] \right\}}$$

$$V_{bi} = \frac{kT}{q} \ln \left( \frac{N_A N_D}{n_i^2} \right) \quad J_{\text{rec}} = \frac{qWn_i}{\tau_{p0r} + \tau_{n0r}} \exp\left(\frac{V_a}{2V_T}\right) \quad J_{\text{diode}} = J_{D \text{ Total}} + J_{\text{rec}}$$

2. For a p-substrate silicon MOS capacitor, at  $T = 300$  K, the substrate doping is  $N_A = 5 \times 10^{16} \text{ cm}^{-3}$ .

- What is bulk potential,  $\phi_B$ ?
- At inversion condition what is  $\phi_s$ ? (Hint:  $\phi_s$  is total band bending at the surface).
- For  $\phi_m = 4.7 \text{ eV}$  and  $\chi = 4.01 \text{ eV}$  (for silicon), what is the flatband voltage  $V_{FB} = \phi_{ms}$ ?
- Find the maximum depletion width  $x_{dT}$  ( $\mu\text{m}$ ) at the inversion condition of the surface. Value of  $n_i$  at  $T = 300$  K is  $1.5 \times 10^{10} \text{ cm}^{-3}$ . [4×2.5=10]

Useful equations:

$$x_{dT} = \left( \frac{2\epsilon_s \phi_s}{qN_A} \right)^{1/2} \quad \epsilon_s = 11.7 \epsilon_0 \quad \phi_B = \frac{kT}{q} \ln \left( \frac{N_A}{n_i} \right)$$

3. An ideal n-channel MOSFET has the following parameters:  $V_T = 0.48 \text{ V}$ ,  $\mu_n = 580 \text{ cm}^2/\text{V-s}$ ,  $t_{ox} = 10 \text{ nm}$ ,  $W = 10 \mu\text{m}$  and  $L = 0.8 \mu\text{m}$ . Find the drain current  $I_{ds}$  for this MOSFET when

- $V_{gs} = 1.1 \text{ V}$  and  $V_{ds} = 0.3 \text{ V}$ . [3.5]
- $V_{gs} = 1.4 \text{ V}$  and  $V_{ds} = 1.8 \text{ V}$ . [3.5]
- $V_{gs} = 0.1 \text{ V}$  and  $V_{ds} = 0.2 \text{ V}$ . [3.0]



# North South University

Department of Electrical and Computer Engineering

Final Exam, Fall 2018

## Semiconductor Devices Technology (EEE 313.01/ETE 411.01/EEE 410.01/ETE 443.01)

Time: 70 minutes

Full marks: 30

There are three questions. Attempt answers to all. Individual marks are indicated at the right margin.

1. (a) There are two p-n junction diodes A and B. Diode A has high p-side and n-side doping but diode B has low p-side and n-side doping. For both diodes, comment on the electric field  $E_{max}$  at  $x = 0$  (whether  $E_{max}$  higher or lower). Plot  $E(x)$  versus  $x$  for both diodes where  $E(x)$  is electric field in the depletion region.

(b) A silicon pn junction at  $T = 300$  K has the following parameters:  $N_A = 2 \times 10^{15} \text{ cm}^{-3}$ ,  $N_D = 5 \times 10^{16} \text{ cm}^{-3}$ ,  $D_n = 26 \text{ cm}^2/\text{s}$ ,  $D_p = 16 \text{ cm}^2/\text{s}$ ,  $\tau_{n0} = 8.2 \times 10^{-7} \text{ s}$  and  $\tau_{p0} = 3.4 \times 10^{-7} \text{ s}$ . The cross sectional area is  $A = 3.2 \times 10^{-3} \text{ cm}^2$  and the forward bias voltage is  $V_a = 0.6 \text{ V}$ . Calculate the total current  $I_{diode}$  (A) in the p-n junction diode. Value of  $n_i$  at  $T = 300$  K is  $1.5 \times 10^{10} \text{ cm}^{-3}$ .

[4+6=10]

Useful equations:

$$J_{Diode} = q \left( \frac{D_p p_{n0}}{L_p} + \frac{D_n n_{p0}}{L_n} \right) \left( \exp\left(\frac{V_a}{V_T}\right) - 1 \right) \quad (\text{A/cm}^2) \quad L_p^2 = D_p \tau_{p0}$$

$$L_n^2 = D_n \tau_{n0} \quad V_T = \frac{kT}{q} \quad V_{bi} = \frac{kT}{q} \ln \left( \frac{N_A N_D}{n_i^2} \right)$$

2. (a) For a p-substrate MOS capacitor, suppose  $V_{FB} = -3 \text{ V}$  and  $V_G = -3 \text{ V}$ . What is the value of surface band bending  $\phi_s$ ?
- (b) Suppose we have an enhancement mode ( $V_T > 0$ ) MOS-capacitor and a depletion mode ( $V_T < 0$ ) capacitor. We would like to reduce inversion charge formation at  $V_G = -1 \text{ V}$ . Which capacitor type will allow that? Explain.
- (c) For a p-substrate silicon MOS capacitor, at  $T = 300$  K, the substrate doping is  $N_A = 1.3 \times 10^{16} \text{ cm}^{-3}$ .
- What is bulk potential,  $\phi_B$ ?
  - At inversion condition what is  $\phi_s$ ? (Hint:  $\phi_s$  is total band bending at the surface).
  - For  $\phi_m = 4.35 \text{ eV}$  and  $\chi = 4.01 \text{ eV}$  (for silicon), what is the flatband voltage  $V_{FB} = \phi_{ms}$ ?
  - Find the maximum depletion width  $x_{dT}$  ( $\mu\text{m}$ ) at the inversion condition of the surface. Value of  $n_i$  at  $T = 300$  K is  $1.5 \times 10^{10} \text{ cm}^{-3}$ .

[2+2+1.5 x 4=10]

Useful equations:

$$x_{dT} = \left( \frac{2\epsilon_s \phi_s}{q N_A} \right)^{1/2} \quad \epsilon_s = 11.7 \epsilon_0 \quad \phi_B = \frac{kT}{q} \ln \left( \frac{N_A}{n_i} \right)$$

3. (a) Suppose for a n-channel MOSFETs, drain current is measured by saturation current. If  $V_{gs}$ ,  $W$  and  $L$  are fixed for this device, how can you increase  $I_{ds}(\text{sat})$  for this device? Consider all parameters that are essential for computation of  $I_{ds}(\text{sat})$ .
- (b) An ideal n-channel MOSFET has the following parameters:  $V_T = 0.4 \text{ V}$ ,  $\mu_n = 740 \text{ cm}^2/\text{V-s}$ ,  $t_{ox} = 10.9 \text{ nm}$ ,  $W = 9 \mu\text{m}$  and  $L = 0.9 \mu\text{m}$ . Find the drain current  $I_{ds}$  for this MOSFET when

- (i)  $V_{gs} = 0.2 \text{ V}$  and  $V_{ds} = 0.15 \text{ V}$ .
- (ii)  $V_{gs} = 1.5 \text{ V}$  and  $V_{ds} = 0.4 \text{ V}$ .
- (iii)  $V_{gs} = 1.8 \text{ V}$  and  $V_{ds} = 2.2 \text{ V}$ .

[3+2+2.5x2=10]

Make sure to apply the above bias conditions to determine cut-off, linear case and saturation case for calculation of drain current.

Useful equations:

$$I_{ds} = \mu_n c_{ox} \frac{W}{L} \left\{ (V_{gs} - V_T) V_{ds} - \frac{V_{ds}^2}{2} \right\}$$

$$I_{ds} = \mu_n c_{ox} \frac{W}{L} \frac{(V_{gs} - V_T)^2}{2}$$