

(c) What is the speed  $V_f$  at the end of 8.5 m displacement.

$$W_f = K_f - K_i$$

$$= \frac{1}{2} m V_f^2 - \frac{1}{2} m V_i^2 \quad V_i = 0$$

$$V_f = \sqrt{\frac{2W}{m}} = \sqrt{\frac{2 \times 153}{222 \text{ kg}}} = 1.17 \text{ m/s Ans}$$

problem:

During a storm, a box is sliding across a slick, oily parking lot through a displacement  $\vec{d} = (-30\text{m})\hat{i}$  while a steady wind pushes against the crate with a force  $\vec{F} = (2\text{N})\hat{i} + (-6\text{N})\hat{j}$ .

(a) How much work does this force do on the crate during the displacement.

$$W = \vec{F} \cdot \vec{d} = [(2\text{N})\hat{i} + (-6\text{N})\hat{j}] \cdot [-3\text{m}\hat{i}]$$
$$= -6\text{J}$$

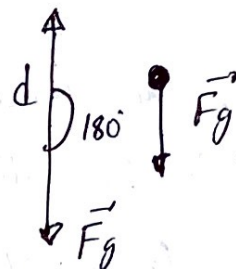
(b) If the box has a kinetic energy of 10J at the beginning of the displacement  $\vec{d}$ , what is its kinetic energy at the end of  $\vec{d}$ ?

$$K_f - K_i = W \quad \text{or} \quad K_f = W + K_i$$
$$= (-6\text{J}) + 10\text{J} = 4\text{J}$$

less kinetic energy means the box has been slowed.

## Work done by the Gravitational Force:

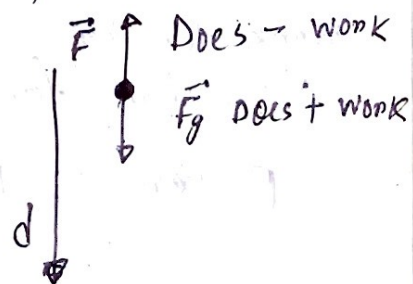
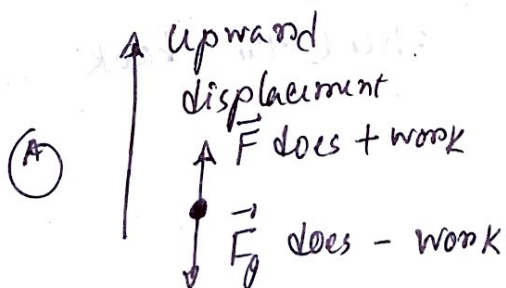
$$\begin{aligned} W_g &= mg d \cos\theta \\ &= mgd (-1) \\ &= -mgd \end{aligned}$$



The minus sign tells us that during the object's rise, the gravitational force acting on the object transfers energy in the amount  $mgd$  from the kinetic energy of the object. That's why the object is slowing down.

- After the object has reached its maximum height, it will fall back, the  $\phi$  would be zero between  $F_g$  &  $d$   
 $W_g = mgd \cos 0^\circ = +mgd$ .

\* If we lift a particle-like object by applying a vertical force  $\vec{F}$  to it, the applied force does positive work. However the gravitational force does negative work.





sample problem 7.06

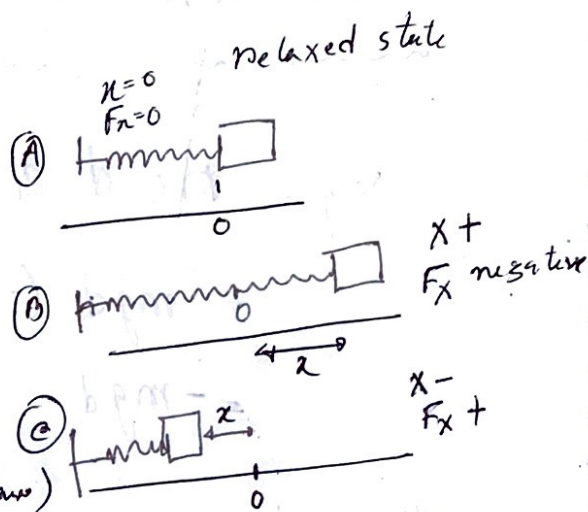
Work done by a spring force

For Spring, the force  $\vec{F}_s$  from is proportional to the displacement  $\vec{d}$  of the free end from its position:

The spring force  $\vec{F}_s = (-)k\vec{d}$  (Hook's law)

$\vec{F}$  is opposite to  $\vec{d}$

$$\vec{F}_x = -kx$$



$$F = \frac{1}{2}kx^2$$

If  $x$  is positive (B), (pulled toward right),  $F_x$  is negative

If  $x$  is negative (pulled toward left),  $F_x$  is positive

\* Notably Spring force is a variable force because it is a function of ~~xxxx~~  $x$ . Hook's law is a linear relationship between  $F$  &  $x$ .

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work done by

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check the expression  
for work done in  
spring force.

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Power

The time rate at which work is done by a force is said to be the power due to the force. If a force does an amount of work  $W$  in an amount of time  $\Delta t$ , the average power due to the force during that time interval is  $P_{\text{avg}} = \frac{W}{\Delta t}$ .

The instantaneous power  $P$  is the instantaneous <sup>time</sup> rate of doing work, can be written as  $P = \frac{dW}{dt}$ .

Unit of power is the watt (W) after James Watt, who greatly improved the rate at which steam engines could do work.

$$1 \text{ watt} = 1 \text{ W} = 1 \text{ J/s}$$

$$1 \text{ horse power} = 1 \text{ hp} = 746 \text{ W}.$$

If you apply a force on an object with  $30^\circ$  angle,

$$P = \frac{dW}{dt} = \frac{F \cos \theta dx}{dt} = F \cos \theta \frac{dx}{dt}$$

$$P = F v \cos \theta = \vec{F} \cdot \vec{v}$$