

Example: Given $f(x) = x + 3$ and $g(x) = x^2 - 3$
Determine:

a. $f(g(x)) = (x^2 - 3) + 3$
 $= x^2$

b. The domain and range of $f(g(x))$.

Domain & Range of inside function:

$$g(x) = x^2 - 3$$

$$D: \{x | x \in \mathbb{R}\}$$

$$R: \{y | y \geq -3, y \in \mathbb{R}\}$$

Domain & Range of composite.
 $f(x) = x + 3$

Domain is restricted by range of inside function.

$$D: \{x | x \geq -3, x \in \mathbb{R}\}$$

Range is restricted by domain.

Since $x \geq -3$, the lowest y-value is:

$$\begin{aligned} f(x) &= x + 3 \\ &= -3 + 3 \\ &= 0 \end{aligned}$$

$$R: \{y | y \geq 0, y \in \mathbb{R}\}$$