

Phy-107
Assignment

Name: Sunjare Zulfiken

ID: 1912050642

① Two vectors are given by $\vec{a} = (9.0\text{m})\hat{i} + (2.0\text{m})\hat{j}$ and $\vec{b} = (2.0\text{m})\hat{i} + (1.0\text{m})\hat{j} + (3.0\text{m})\hat{k}$ in unit vector notation find

① $\vec{a} + \vec{b}$

$$\begin{aligned}\vec{a} + \vec{b} &= (9.0\text{m} + 2.0\text{m})\hat{i} + (2.0\text{m} + 1.0\text{m})\hat{j} + (3.0\text{m})\hat{k} \\ &= (11.0\text{m})\hat{i} + (3.0\text{m})\hat{j} + (3.0\text{m})\hat{k}\end{aligned}$$

② $\vec{a} - \vec{b}$

$$\begin{aligned}\vec{a} - \vec{b} &= (9.0\text{m} - 2.0\text{m})\hat{i} + (2.0\text{m} - 1.0\text{m})\hat{j} - (3.0\text{m})\hat{k} \\ &= (7.0\text{m})\hat{i} + (1.0\text{m})\hat{j} - (3.0\text{m})\hat{k}\end{aligned}$$

③ a third vector \vec{c} such that $\vec{a} + \vec{b} - \vec{c} = 0$

w.k., $\vec{a} + \vec{b} = (11.0\text{m})\hat{i} + (3.0\text{m})\hat{j} + (3.0\text{m})\hat{k}$

So, \vec{c} will be $-(11.0\text{m})\hat{i} - (3.0\text{m})\hat{j} - (3.0\text{m})\hat{k}$



② Vectors \vec{A} and \vec{B} lie in an xy plane. \vec{A} has magnitude 5.00 and angle 150° , \vec{B} has components $B_x = -6.50$ and $B_y = -0.20$.

What are the angles between the negative direction of the y axis and (a) the direction of \vec{A}

$$\textcircled{a} \quad \vec{A} = 5.00 (\cos 150^\circ \hat{i} + \sin 150^\circ \hat{j})$$
$$= -4.3 \hat{i} + 2.5 \hat{j}$$

$$\vec{B} = B_x \hat{i} + B_y \hat{j}$$
$$= -6.50 \hat{i} - 0.20 \hat{j}$$

$$\textcircled{b} \quad \vec{A} \cdot (-\hat{j}) = A \cos \theta$$

$$\theta = \cos^{-1} \left(\frac{\vec{A} \cdot (-\hat{j})}{A} \right)$$

$$= \cos^{-1} \left(\frac{-2.5}{\sqrt{(-4.3)^2 + (2.5)^2}} \right)$$

$$= \cos^{-1} \left(\frac{-2.5}{4.92} \right)$$

$$= 120.2^\circ$$

⑥ $\vec{A} \times \vec{B}$ is perpendicular to the y axis
So, answer will be 90°

$$\textcircled{c} \quad \vec{A} \times (\vec{B} + 7.00\hat{k}) \\ = (-4.3\hat{i} + 2.5\hat{j}) \times (-6.50\hat{i} - 9.20\hat{j} + 7.00\hat{k})$$

$$\text{Now, } \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -4.3 & 2.5 & 0 \\ -6.50 & -9.2 & 7 \end{vmatrix} \\ \vec{A} \times \vec{B} = 17.5\hat{i} + 30.1\hat{j} + 55.81\hat{k}$$

$$|\vec{A} \times \vec{B}| = \sqrt{(17.5)^2 + (30.1)^2 + (55.81)^2} \\ = 65.74$$

$$\therefore \theta = \cos^{-1}\left(\frac{-30.1}{65.74}\right) \\ = 117.23^\circ$$

③ An iPhone is shot from the ground into the air. At a height of 7.8 m, its velocity is $\vec{v} = (6.7\hat{i} + 5.2\hat{j}) \text{ ms}^{-1}$, with \hat{i} horizontal and \hat{j} upward.

(a) To what maximum height does the iPhone rise?

$$v_y^2 = (v_{0y})^2 - 2gh$$

$$\begin{aligned} v_{0y} &= \sqrt{v_y^2 + 2gh} \\ &= \sqrt{5.2^2 + (2 \times 9.8 \times 7.8)} \\ &= 13.41 \end{aligned}$$

So, at the maximum height of the phone, the vertical component of the velocity is 0

Now,

$$\begin{aligned} v_y^2 &= (v_{0y})^2 - 2gH \\ H &= \frac{v_y^2 - v_{0y}^2}{-2g} \quad | v_y = 0 \\ &= \frac{13.41^2}{2 \times 9.8} \\ &= 9.1 \text{ m} \end{aligned}$$

⑥ what total horizontal distance does the iphone travel?

Wk,

$$R = \frac{2v_{x1}v_{y1}}{g}$$
$$= \frac{2 \times 6.7 \times 13.41}{9.8}$$
$$= 18.33 \text{ m}$$

⑦ what are the magnitude and angle of the iphone's velocity just before it hits the ground?

$$V^2 = (v_x)^2 + (v_{y1})^2$$
$$V = \sqrt{(v_x)^2 + (v_{y1})^2}$$
$$= \sqrt{(6.7)^2 + (13.41)^2}$$
$$= 14.99 \text{ ms}^{-1}$$

Now,

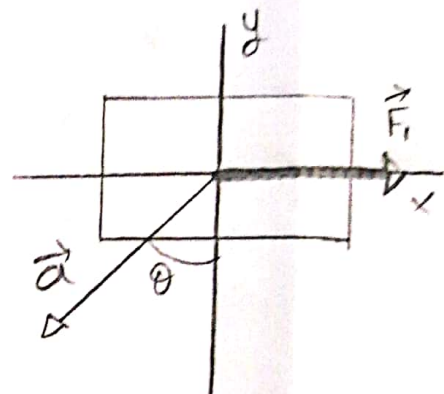
$$\theta = \tan^{-1}\left(\frac{v_y}{v_x}\right)$$
$$= \tan^{-1}\left(\frac{13.41}{6.7}\right) = 63.45^\circ$$

④ There are two forces on the 500 kg box in the overhead ~~view~~ view of the figure, but only one is shown. For $F_1 = 25.0 \text{ N}$, $a = 17.0 \text{ m/s}^2$ and $\theta = 30^\circ$, find the second force

① in unit vector notation

Here,

$$\begin{aligned} \vec{F} &= -(ma \sin \theta) \hat{i} - (ma \cos \theta) \hat{j} \\ &= -(5 \times 17 \times \sin 30) \hat{i} - (5 \times 17 \times \cos 30) \hat{j} \\ &= -42.5 \hat{i} - 73.6 \hat{j} \end{aligned}$$



② a magnitude

$$\begin{aligned} \text{Here } \vec{F}_2 &= (-25.0 - 42.5) \hat{i} - 73.6 \hat{j} \\ &= -67.5 \hat{i} - 73.6 \hat{j} \end{aligned}$$

$$\begin{aligned} |\vec{F}_2| &= \sqrt{(-67.5)^2 + (-73.6)^2} \\ &= 99.87 \text{ N} \end{aligned}$$

③ an angle relative to the positive direction of the x axis

$$\begin{aligned} \theta &= \tan^{-1} \left(\frac{-73.6}{-67.5} \right) \\ &= 47.47 - 180 \end{aligned}$$

So, -132.53 from positive x axis

⑤ A labor drags a crate across a factory floor by pulling on a rope tied to the crate. The labor exerts a force of magnitude $F = 470 \text{ N}$ on the rope, which is inclined at an upward angle $\theta = 43^\circ$ to the horizontal and the floor exerts a horizontal force of magnitude $F = 125 \text{ N}$ that opposes the motion. Calculate the magnitude of the acceleration of the crate if

(a) mass is 360 kg

$$\begin{aligned} F_x &= F \cos \theta \\ &= (470 \text{ N}) \cos 43^\circ \\ &= 343.73 \text{ N} \end{aligned}$$

$$\text{Now, } F_x - f = ma$$

$$\begin{aligned} \Rightarrow a &= \frac{F_x - f}{m} \\ &= \frac{343.73 - 125}{360} \\ &= 0.6 \text{ m/s}^2 \end{aligned}$$

⑥ Wk,

$$W = mg$$

$$m = \frac{W}{g} = \frac{360}{9.8} = 36.73$$

Now,

$$F_x - f = ma$$

$$a = \frac{F_x - f}{m}$$

$$= \frac{343.73 - 125}{36.73}$$

$$= 5.95 \text{ ms}^{-2}$$