



North South University
Department of Electrical & Computer Engineering

LAB REPORT

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Course Title: Electrical Circuit 2

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Experiment Number: 06 Experiment
Name:

Experiment on RLC Resonance, Bandwidth and Quality Factor

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Submitted By

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Lab 6; RLC Resonance, Bandwidth and Quality Factor

A. Objectives:-

To investigate and verify the Resonance phenomena in RLC circuit. Analyze the Resonant Frequency and Bandwidth of given circuit and regulate the effect of the load resistance.

B. Background:-

B.1 Resonance in a Series RLC circuit:

The resonance of a series RLC circuit occurs when the inductive and capacitive reactances are equal in magnitude but cancel each other because they are 180 degrees apart in phase.

Here, both X_C and X_L are frequency dependent. However X_C is inversely proportional to frequency and X_L is

Resonant frequency Q = quality factor.
A high Q resonant circuit has a narrow bandwidth as compared to a low Q . Bandwidth is measured between the 0.707 current amplitude points.

Equipment :-

- Bread board
- Function generator
- Digital storage oscilloscope
- connecting wires
- resistors
- capacitors
- Inductor.

Circuit :-

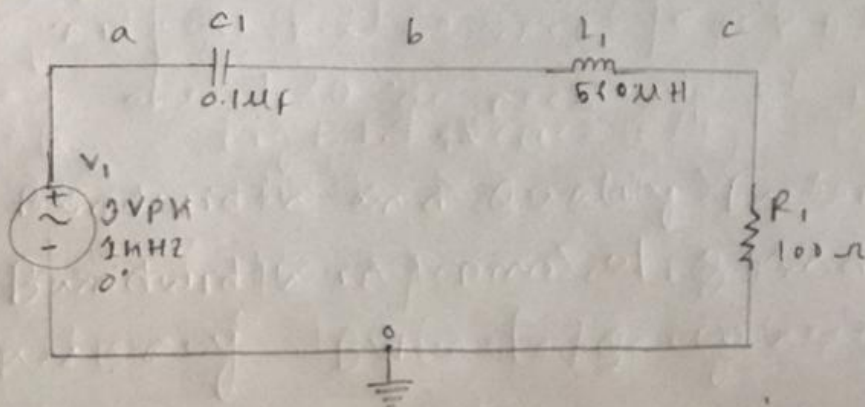


Fig B.1.1: Series RLC circuit

directly proportional. When frequency is increased, X_C decreases and X_L increases. That means, $X_C = X_L$. According to the resonance condition $X_C = X_L$ which means $\frac{1}{j\omega C} = j\omega L$ and the resonance frequency is f_0 .

$$f_0 = \frac{1}{2\pi\sqrt{LC}}$$

Now, the impedance in the below circuit can be expressed as $Z = R + jX_L - jX_C$

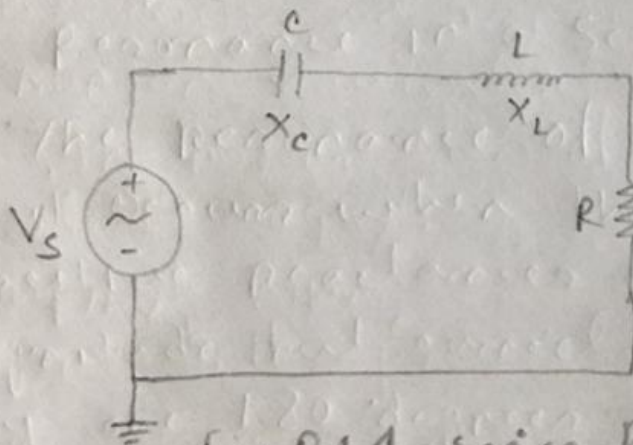


Fig B.1.1: Series RLC circuit

B.2 Bandwidth and Quality Factor:-

Bandwidth in terms of Q and resonant frequency $BW = f_c/Q$ where $f_c =$

Table 1.1: Component Values:

	$R_1 (\Omega)$	$R_2 (\Omega)$	$C_1 (F)$	$L_1 (H)$
Nominal	100 Ω	200 Ω	1×10^{-7}	5.6×10^{-4}
Measured	100 Ω	200	1×10^{-7}	5.6×10^{-4}

Table 1.2: The magnitude of V_e , V_L , V_R at different frequencies for a high Q circuit.

Frequency (f) kHz	Peak Voltage, V_R (V)	Peak Voltage, V_e (V)	Peak voltage, V_L (V)
1	0.19	3.0	6.68×10^{-3}
10	1.89	2.997	0.67
20	2.99	2.37	2.11
30	2.65	1.4	2.8
40	2.107	0.83	2.97
50	1.71	0.54	3.0
60	1.424	0.38	3.02
70	1.22	0.28	3.02
80	1.07	0.21	3.02
90	0.95	0.17	3.01
100	0.85	0.14	3.01

Table 1.3: Resonant frequency, Quality factor & Bandwidth for a high Q circuit

	Theoretical (a)	Experimental (b)	Deviation (%) $\frac{a-b}{a} \times 100$
f_0	21.27	20	5.97
f_1	11.8	14	18.64
f_2	40.21	38	5.496
Bandwidth ($f_2 - f_1$)	28.41	24	15.52
Q-factor (f_0 /Bandwidth)	0.75	0.833	11.07

Table 1.4: The magnitudes of V_C , V_L & V_R at different frequencies for a low Q circuit.

Frequency (f) kHz	Peak Voltage, V_R (V)	Peak Voltage, V_C (V)	Peak Voltage, V_L (V)
1	0.37	2.98	6.64×10^{-3}
10	2.55	2.03	0.45
20	2.997	1.189	1.06
30	2.899	0.77	1.54
40	2.67	0.530	1.89
50	2.43	0.386	2.14
60	2.20	0.29	2.33
70	1.995	0.226	2.47
80	1.82	0.18	2.567
90	1.66	0.147	2.64
100	1.53	0.121	2.70

Table 1.5: Resonant frequency, Quality factor & Bandwidth for a Low Q-circuit

	Theoretical (a)	Experimental (b)	Deviation (%) $\frac{a-b}{a} \times 100$
f_0	21.27	21	1.27
f_1	7.6	7	7.89
f_2	64.42	64	0.65
Bandwidth ($f_2 - f_1$)	28.4 56.82	57	0.32
Q-factor (f_0 /Bandwidth)	0.37	0.368	0.54

Questions:-

1. Explain why the load voltage in RLC circuit is maximum at resonance condition.

Ans: Since the RLC circuit is driven by a variable frequency and $Z = R + jX_L - jX_C$, at resonance condition, $jX_L = jX_C$ resulting ($Z = R$) the circuit to be purely resistive. As the magnitude of the voltage V is directly proportional to the impedance Z , the entire source voltage acts across R . Thus the load voltage is maximum at resonance condition.

2. If a 5mH inductor was used instead of 560 μ H one, what capacitance value would be required to keep the resonant frequency (f_0) the same as the value obtained from the experiment.

$$\text{Ans: } f_0 = \frac{1}{2\pi\sqrt{LC}}$$

$$\Rightarrow 21268 = \frac{1}{2\pi\sqrt{5 \times 10^{-3} C}}$$

$$\Rightarrow C = \frac{1 \times 5 \times 10^{-3}}{\sqrt{21268 \times 2\pi}}$$

$$= 1.37 \times 10^{-5} \text{ F}$$

$$= 13.7 \mu\text{F}$$

Q.10. Is it possible to have a resonance condition in a parallel circuit RLC circuit? If so, briefly discuss a possible experimental set up which could be used to investigate resonance in a parallel RLC circuit.

Ans: It is possible to have a resonance condition in a parallel RLC circuit where energy will constantly be transferred back and forth between the inductor and the capacitor resulting in zero current and energy being absorbed from the supply. The experiment setup should be similar to the series RLC component wise except the resistor, inductor and capacitor should be connected in parallel respectively to frequency generator. Change the frequency until maximum peak voltage is obtained. That will be the resonant frequency for the parallel RLC circuit.

Q. Do the practical value of the resonant frequency, bandwidth and quality factor obtained from confirm with the theoretical values. If any percentage difference are above 10% suggest 3 possible reasons for the discrepancy.

3. How would the resonant frequency of the circuit given in figure B.11 change if the 100Ω resistor was replaced with a 50Ω one? explain.

Ans: No change will occur on the resonant frequency. Since resonant frequency depends wholly on the capacitance and inductance of the circuit, $f_0 = \frac{1}{2\pi\sqrt{LC}}$, any change in the value of the resistor will not affect the value of the resonant frequency. It will only affect the peak of the resonance as the current will in the oscilloscope as $V = IR$.

4. Use your experimental results and the graph obtained from the simulations to explain the concept of high and low quality factors in series RLC circuits.

Ans: Quality factor is the ratio of resonant frequency to bandwidth.

Answer No:4.

As per experimental value, we obtain a low-Q due to a high resistance in series RLC circuit. And, we obtain high Q is due to a low resistance in series. ~~with~~

Answer to question No:6.

For the first part of the experiment deviation percentage for Bandwidth & quality factor are above 10. Other measured values are close to theoretical values where deviation is less than 10%. Three possible reasons for the discrepancy:

- (i) We could not ~~measure~~ determine the exact values from graph.
- (ii) Instruments are not precise as desired.
- (iii) There might be some systematic error.

Discussions

For the first part of experiment our theoretical & practical value deviated ~~at~~ slightly larger than the second part where a larger resistor has been used. But, deviation percentage were never larger than 20%. In some cases it was only 0.3%.

Cause of errors might be instrumental, ~~error~~ procedural, & human. To determine the peak voltage we faced slight difficulty as the value was fluctuation too quickly. Thus, we took average value in some cases.

This experiment helped us to complete the gap between our theoretical learning & experimental learning. We learned about the resonance, Bandwidth & Quality factors & learned how to calculate them.

