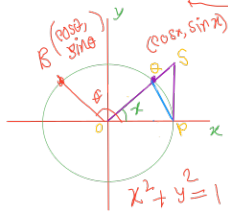


① $g(x) \leq f(x) \leq h(x)$ $\lim_{x \rightarrow 2} (x^3) = 8$
 $x \rightarrow 2 = 2 \in (a, b)$

② if $\lim_{x \rightarrow c} g(x) = \lim_{x \rightarrow c} h(x) = L$
then $\lim_{x \rightarrow c} f(x) = L$

$\lim_{x \rightarrow 0} \frac{\sin x}{x}$

$g(x) \leq \frac{\sin x}{x} \leq h(x)$



$\frac{1}{2} x \leq \sin x \leq \frac{1}{2} x$

$\frac{1}{2} x \leq \sin x \leq \frac{1}{2} x$

$\tan x = \frac{SP}{OP}$
 $\Rightarrow \tan x = \frac{SP}{1}$

$x < y < \frac{1}{y}$

$\lim_{x \rightarrow 0} h(x) = \lim_{x \rightarrow 0} 1 = 1$

$\frac{\sin x}{x} \leq \frac{1}{x} \leq \frac{\tan x}{x}$

$\Rightarrow \sin x \leq x \leq \tan x$

$\Rightarrow 1 \leq \frac{x}{\sin x} \leq \frac{1}{\cos x}$

$\cos x \leq \frac{\sin x}{x} \leq 1$

$\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$

$\frac{x}{\sin x} \geq 1$

$\lim_{x \rightarrow 0} g(x) = \lim_{x \rightarrow 0} \cos x = \cos 0 = 1$

$f(x) = \ln x \rightarrow D_f = (0, +\infty)$

$f(x) = e^x \rightarrow D_f = (-\infty, +\infty)$

time (t)	distance travelled
t = 10	d = 0
t = 10:30	d = 5
t = 11:00	d = 7.25
t = 12:00	d = 13

What is the rate of change?

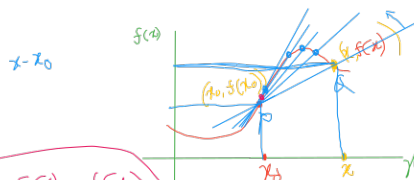
$y = f(x)$

$\lim_{x \rightarrow x_0} \frac{f(x) - f(x_0)}{x - x_0}$

$\rightarrow f'(x_0)$

$y = mx + c$

$y = 2x + 3$



$\lim_{x \rightarrow p} \frac{f(x) - f(p)}{x - p}$

x	y
0	5
1	8
2	11
3	14

