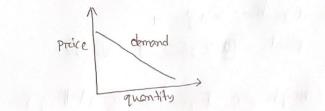
The greaph of an equation in two varciables x and y consists of the set of points in the Xy Plane whose coottdinates (x, y) satisfy the equation.

Greaphs Play an important teale in helping us to visualize the relationships that exist between two varciables.

Say For example, the domand curive/line represents the telationship between the price and the demand of the quantity



Determine whether a point is on the graph of on Equation?

Defermine if the following points are on the graph of the equation 2x-y=6 (a) (2,3) (b) (2,-2)

Solm: (a) For the point (2,3), chack to see if x=2 and y=3 patisties the equation 2x-y=6 If we pubstitute x = 2 and y = 3 on the left hand side of the ear 2x-y=6 we get

 $2(2) - 3 = 4 - 3 = 1 \neq 6$ So the point (2,3) is that on the graph of ean 2x-y=6 because it does not satisfy the equation.

(b)
$$(2,-2)$$
. Here $x=2$, $y=-2$

2x-y=(2)(2)-(-2)=4+2=6 which satisfies the given equation.

So the point (2,-2) lies on the egn of graph of the

Exercise:

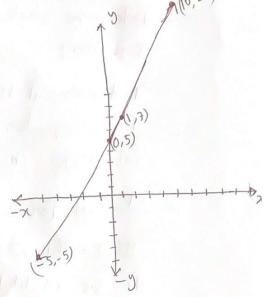
1. Equation: $y = x^4 - \sqrt{x}$ Points: (0,0); (1,1): (-1,0)

2. Equation: $x^{2}+y^{2}=4$ Points: (0,2); (-2,2); $(\sqrt{2},\sqrt{2})$

Greaph an Equation by Plotling points:

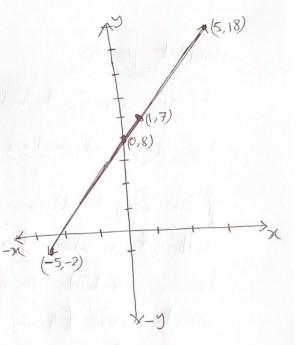
Example: y = 2x +5

zlf.	Then	Points on graph	
7=0	J=0+5=5	(0,5)	
21=1	y=2+5=7	(F,I)	
2 = -5	y=-10+5=-5	(-5,-5)	-7
X=10	y = 20 +5 = 25	(10, 25)	Va.



$$y = 2x + 8$$

14	then	Points on greaph
21=0	J=0+8=8	(0,8)
X= 1	y=2+8=10	(1,10)
71=-5	y = -10+8=-2	(-5,-2)
7=5	y=10+8=18	(5,18)

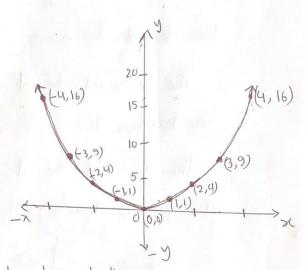


Exercise:

Example: 3

Greaph the equation y=x2

X	y=x2	(51,7)
-4	y=16	(-4,16)
-3	y = 9	(-3,9)
-2	7 = 4	(-2, 4)
-1	9=11	(-1,1)
0	y = 0	(0,0)
1	5 = 1	(1,1)
2	y = 4	(2,4)
3	My=911	(3,9)
4	y = 16	(4,16)



Exercise: Find the intercepts and streph the egh.

Complete greaph:

use are nows to indicate that the pattern shows in the greeph will continue.

one way to obtain a complete graph is to plot a sufficient number of points on the graph until a patheren becomes evident. Then these points are connected with a smooth curve following the suggested pathern But how many points are sufficients.

Two tellmiques can treduce the numbers of points trequirred to greaph an equation involve finding intercepts and checking for symmetry.

Intercepts:

The points, if any, at which a greaph crosses on touches the coordinate axes are called the intercepts.

The x-coordinate of a point of which the grouph crosses on touches the x-axis is called an x-intercept.

the y-coordinate of a point at which the graph crosses or touches the y-axis is colled the y-intercept.

Graph

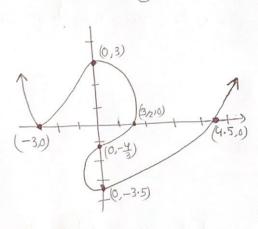
Cruster yexis

Graph

Touches

X-axis

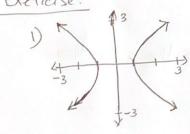
Find the intercepts of the graph. what are its x-intercepts?



The points on the graph are (-3,0), (0,3), $(\frac{3}{2},0)$, $(0,-\frac{4}{3})$, $(0,-\frac{3\cdot5}{3})$

The X intercepts are $-3, \frac{3}{2}, 4.5$ The y 11 $11 - 3.5, -\frac{4}{3}, 3$

Exeticise:



(I) 3 -3 3

Find intercepts from an equation:

Procedure!

- 1. Find x-intercept, let y=0 in the eqn and solve for x.
- 11) Find y-intercepts, let x=0 inthe ear and solve for y.

Examples

Find the x intercepts and y intercepts of the graph $y = x^2 - y$. The graph $y = x^2 - y$

Solution!

To find the x-intercepts, let y=0 in the given equation.

$$y(^{2}-4=0)$$

=) $(x+2)(x-2)=0$

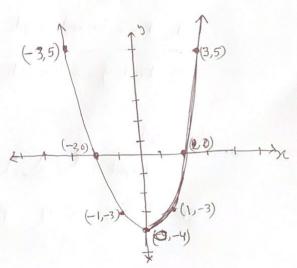
$$=) x = -2 \quad \text{or} \quad x = 2$$

The ear has two solutions, -2 and 2. The x-intercepts are -2 and 2.

To find y-intercepts, let x=0 in the equation.

The y-intercept is -4.

Since x > 0 for all x, we deduce from the extry = x - 4
that y > - 4 for all x.



Test an equation for symmetry:

A greaph is said to be symmetric with trespect to the x-axis, if for every point (x, y) on the greaph, the point (x, y) is also on the greaph.

(x,y) (x,-y)

Agreeph is said to be symmetric with trespect to the y-axis if, for every point (x,y) on the greeph, the point (x,y) is also on the greeph.

A greaph is said to be symmetric with trespect to the otigin if, for every point (x, y) on the graph, the point (-x,-y) is also on the graph.

(-4,-4)

Procedures:

71-axis > Replace y by -y, if an equivalent eqn tresult then the graph of the eqn is symmetric with trespect to x-axis

y-axis -> Replace x by -x, if an equivalent eqn tresults, then the graph of the eqn is symmetric with trespect to y-axis

Otagin -> Replace x by -x and y by -y.

Test $y = \frac{4x^2}{x^2+1}$ for symmetry

Solution:

xaxis: Replace y by -y.

 $y = -\frac{4x^{2}}{x^{2}+1}$ whach is not equivalent to $y = \frac{4x^{2}}{x^{2}+1}$.

So the greaph of this ext is not symmetric about x - ax = x = x.

Yaxis: Replace x = by - x.

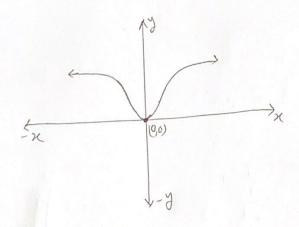
 $y = \frac{4(-x)^{2}}{(-x)^{2}+1} = \frac{4x^{2}}{x^{2}+1}$ which is equivalent to $y = \frac{4x^{2}}{x^{2}+1}$. So the graph of the given eqn is symmetric about x-axis.

otalgin: Replace x by -x and y by -y.

$$-y = \frac{4(-x)^2}{(-x)^2 + 1}$$

$$= -y = \frac{4x^{2}}{x^{2}+1}$$

the given equation. Thus the graph of $y = \frac{4\pi^2}{2^2+1}$ is not symmetric about ordgin.

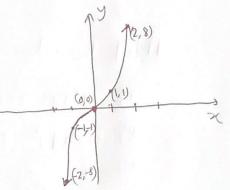


 $\chi - axis \Rightarrow -y = \chi^3 \Rightarrow y = -\chi^3 \neq \text{ortiginal etn.}$

$$y - axis = y = (x)^3 \Rightarrow y = -x^3 \neq 11$$

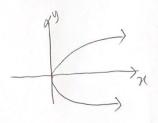
oragin $\rightarrow -y = (-x)^3 \Rightarrow y = x^3$ equivalent to oraginal eqn. Symmetry about oragin

Y=23	(21,4)
O	(0,0)
1	(1,1)
8	(2,8)
27	(3,27)
	8



Example: x=y2

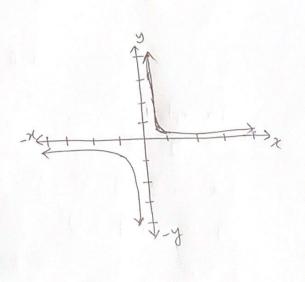
U=± \(\times \), Symmetric about \(\ta - axis \)



$$\begin{array}{c} y \\ \uparrow \\ \\ \chi = 1^{2}, \ y > 0 \end{array}$$

Symmetric about orcigin.

y= 1	(71,7)
10	$(\frac{1}{10}, 10)$
3	$\left(\frac{1}{3},3\right)$
2	$\left(\frac{1}{2},2\right)$
1	(1,1)
1/2	$\left(2,\frac{1}{2}\right)$
1/3	$(3,\frac{1}{3})$
10	$(30, \frac{1}{10})$
	10 3 2 1 12 13



1 list the intercepts and test for symmetry

$$y = \frac{3x}{x^{2}+9}$$

田 If (3,6) is a point on the greek of y= 4×1, then what is b?