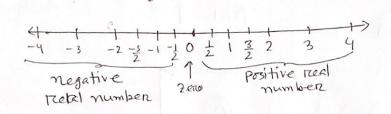
Real number lines

The treal numbers can be represented by points on a line is called the real numbers line.



Find distance on a reed number line:

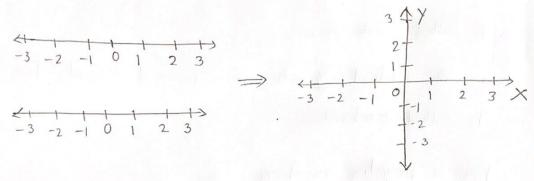
If P and Q are Points on a real number line with coordinates a and b respectively, then the distance bet P and Q, denoted by d(P,Q) as d(P,Q) = |b-a| $\frac{P(a,0)}{o} + \frac{Q(b,0)}{o}$

Example!

Say P, R, R be points on a tred number line with coordinated -5,7 and -3 trespectively. Find the distance between (1) P and R (11) R and R, (111) P and R.

(c)
$$J(PR) = |b-a| = |-3-(5)| = |-3+5| = 2$$

If we put two read numbers lines togethers we get 20 coordinates on carries an coordinates.



> the left-right (horrizontal direction)

1 the up-down (vertical direction)

Any point P in the my plane can be located by using an ordered Pair (2, y) of real numbers.

Hetre, redenote the signed distance & from y-axis
and y 11 11 11 11 P from x-axis

* Signed distance means, If P is to the tright of y-axis.
then 200;

if P is to the left of y-axis, then x<0

For example, 3 units (3,2) means 3 units to the tright along x direction and 2 units up/vertical direction.

The origin;

The point (0,0) is called origin.

The horizontal ox value in a pairs of coordinates is called as abordessa.

The vertical y value in a pair of coordinates is called oradinate.

For a negative number

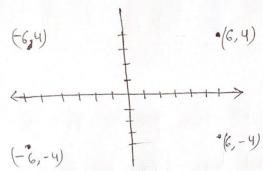
- · go backwards for x
- · go down for y

For example (-6,-5) means go back along the ox axis 6 units and then go down along y axis 5 units.

Quadrant:

When we include negative values, the x and y axes divides the space into 4 pieces:

Thus we can now locate points:



Exercise:

Tell in which quadrant or on what coordinate axis each point les,

(1)
$$A = (3,2)$$
 (11) $B = (6,0)$ (111) $C = (2,-2)$ (11) $D = (6,5)$

(V)
$$E = (6, -3)$$
 (VI) $F = (6, -3)$

Finding distance between two Points:

Find the distance of between the points (13)

and (5,6)

Som:

we have to find d.

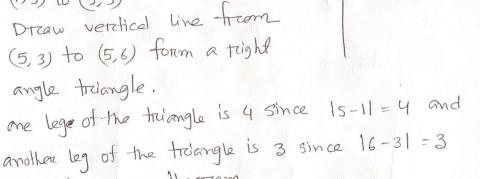
Dreaw horcizontal line tream

(1,3) to (5,3)

Dreaw vertical line from

(5,3) to (5,6) form a tright

angle triangle.



By Pythegoreen theorem $d^{2} = 4^{2} + 3^{2} = 25$ $= 3 + \sqrt{25} = 5$

The distance formula provides a straight forward method for computing distance been two points.

Distance formula:

The distance bet two points $P_1 = (x_1, y_1)$ and $P_2 = (x_2, y_2)$ denoted by $d(P_1, P_2)$ is $d(P_1, P_2) = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

Proofo

Let (x1, y1) and (x2, y2) denote the coordinates of

Point P, and P2 trespectively. Assume that the line

Joining P, and P2 are neither horrizontal non vertical.

The coordinate of P3 are (x2, y1). Then the

horrizontal distance from P1 to P3 is | 272-x11.

The vertical distance from P3 to P2 is | y2-y11

By using P3 the gorceen theorem, if follows that

If the line P, and B is horozontal than the y coordinate of P, is equal to y coordinate of P2 i.e y1=y2. In this case

$$d(P_1,P_2) = \sqrt{(n_2-n_1)^2 + 0^2} = \sqrt{(n_2-n_1)^2} = |n_2-n_1|$$

$$\frac{d(P_1,P_2)}{P_1 |n_2-n_1|} P_2$$

$$\frac{d(P_1,P_2)}{n_2} \chi$$

Example

Using distance formula, find the distance of better the points (-4,5) and (3,2),

$$\frac{501^{m}}{d} = \sqrt{(2-\pi)^{2} + (2-\pi)^{2}}$$

$$= \sqrt{[5-(-4)]^{2} + (2-5)^{2}} = \sqrt{7+(-3)^{2}}$$

$$= \sqrt{49+9}$$

$$= \sqrt{58} \approx 7.62$$

Exercise:

Plots the following points and find distance between P, and P2.

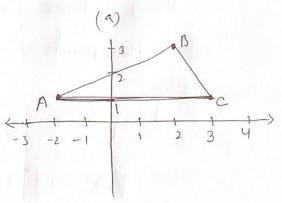
j)
$$P_1 = (4, -3), P_2 = (6, 4)$$
 j) $P_1 = (-4, -3), P_2 = (6, 2)$

111)
$$P_1 = (a, b)$$
, $P_2 = (b, 0)$ 1v) $P_1 = (-1, 0)$, $P_2 = (9, 8)$

Consider the three points A=(-2,1), B=(2,3) and C = (3,1)

- (a) Plot each point and form the trainingle ABC
- Find the length of each side of the triangle.
- (c) verify that the triangle is a right triangle.
- (d) Find the aree of the triangle.

$$\begin{array}{c} 501^{-3} \\ \hline (b) \ d(A,B) = \sqrt{[2-(-2)]^{2}+(3-1)^{2}} \\ = \sqrt{16+4} \\ = \sqrt{20} \\ = \sqrt{4\times5} \\ = 2\sqrt{5} \end{array}$$



$$d(B,C) = \sqrt{(3-2)^{2} + (1-3)^{2}} = \sqrt{1+4} = \sqrt{5}$$

$$d(A,C) = \sqrt{(3-(-2))^{2}+(1-1)^{2}} = \sqrt{25+0} = 5$$

(c) To show that the traingle is a tright angled triangle, we need to show that the sum of the squotes of lengths of two sides equals to the squetze of the length of the Hitzd side,

50 let's check whether $[d(A,B)]^2 + [d(B,C)]^2 = [d(A,C)]^2$

From paret (b)
[d (A,B)] + [d (B,C)]

$$= (2\sqrt{5})^{2} + (\sqrt{5})^{2} = (4\times5)+5 = 20+5 = 25$$
$$= [d(A,e)]^{2}$$

So it follows that the given triangle is a tright handed triangle.

(d) Since the tright angle is at veritex B, then the sides AB and Be form the base and height of the triangle. It's arrea is

Arree = \frac{1}{2} Base x height = \frac{1}{2}(2\structure) \sqrt{5} = 5 \quad \qq \quad \quad \quad \quad \quad \quad \quad \quad \quad \quad

Exercise:

Plot each point and form the traingle ABC. Verify that the traingle is a tright trainle. Find its area:

1)
$$A = (-2,5)$$
; $B = (1,3)$; $C = (-1,0)$

11)
$$A = (6,3)$$
; $B = (3,-5)$ $C = (-1,5)$

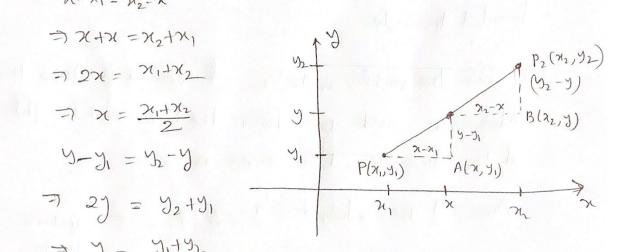
(1)
$$A=(4.3)$$
; $B=(4.1)$; $C=(2,1)$

Derive mid point formula fore a lineal segment

let P, and Pz be the endpoints of a line segment and let m=(x,y) be the midpoint on the line segment.

The triangles P. Am and PzMB are conjurcent so the corresponding sides are exual in length:

$$\exists x = \frac{x_1 + x_2}{2}$$



Example. If you have P,= (+3,-4) to and P2=(5,4) then find the midpoint of the line segment 50M: P1 = (3,-4), P2 = (5,4) Here N1 = 3, N2 = 5, J1 = 4, Y2 = 4

mid poind
$$(\gamma, \gamma) = \left(\frac{\gamma_1 + \gamma_2}{2}, \frac{\gamma_1 + \gamma_2}{2}\right)$$

$$= \left(\frac{3+5}{2}, -\frac{\gamma_1 + \gamma_2}{2}\right)$$

$$= (4, 0)$$

Exercise:

$$\mathbb{U} P_1 = (-3, 2), P_2 = (6, 0)$$

11)
$$P_1 = (-4, -3), P_2 = (2, 2)$$

Example

The diameter of a circle has endpoints

(1,-4) and (5,-4). Find the center of the circle.

Solm: The center of the circle is the center

or midpoint of its diameter. Thus the midpoint formula will yield the center Point,

$$\left(\frac{24+24}{2}, \frac{4+42}{2}\right) = \left(-\frac{1+45}{2}, -\frac{4-4}{2}\right)$$

$$= \left(\frac{4}{2}, -\frac{8}{2}\right)$$

$$= (2, -4)$$