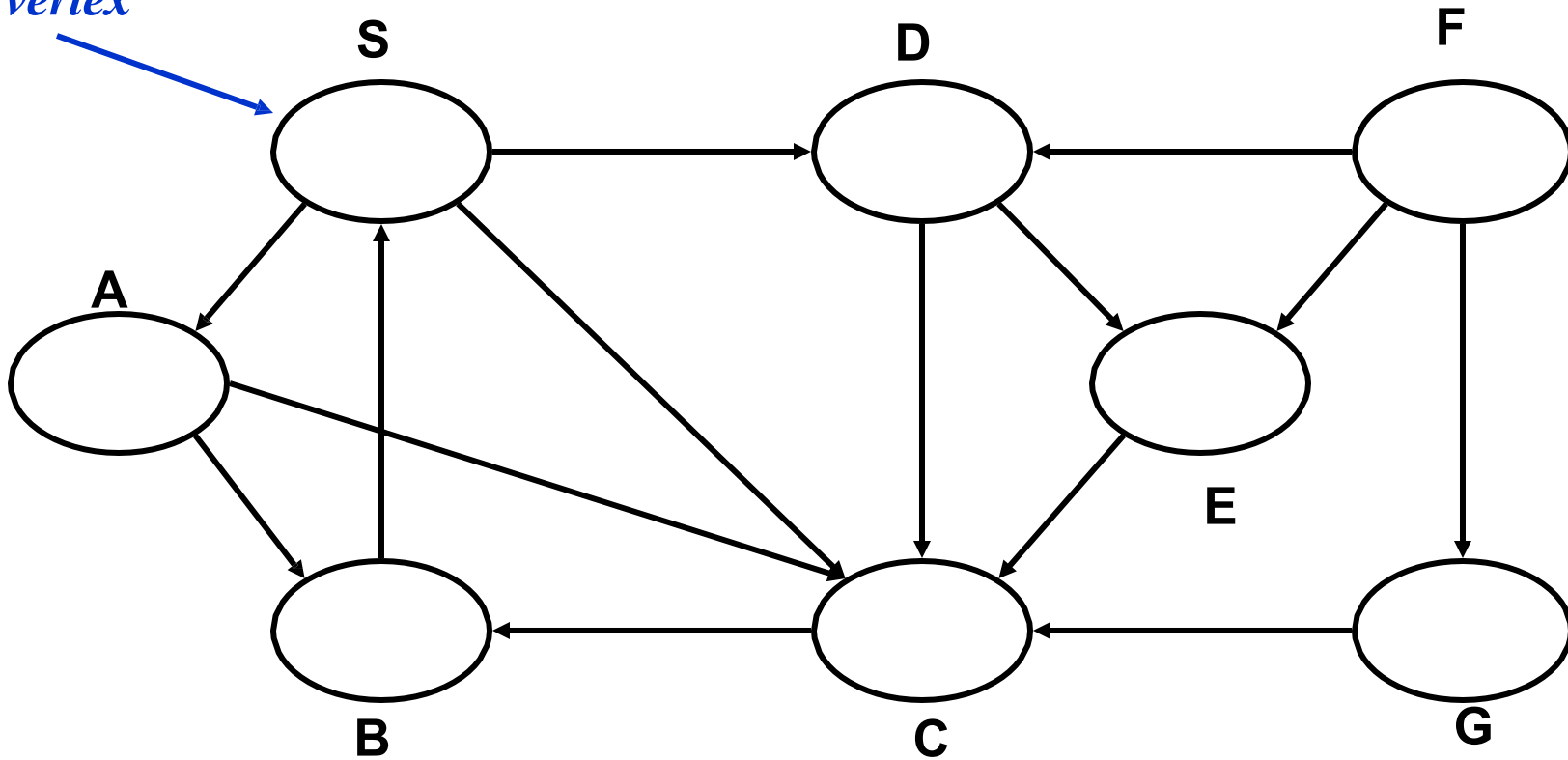




# DFS

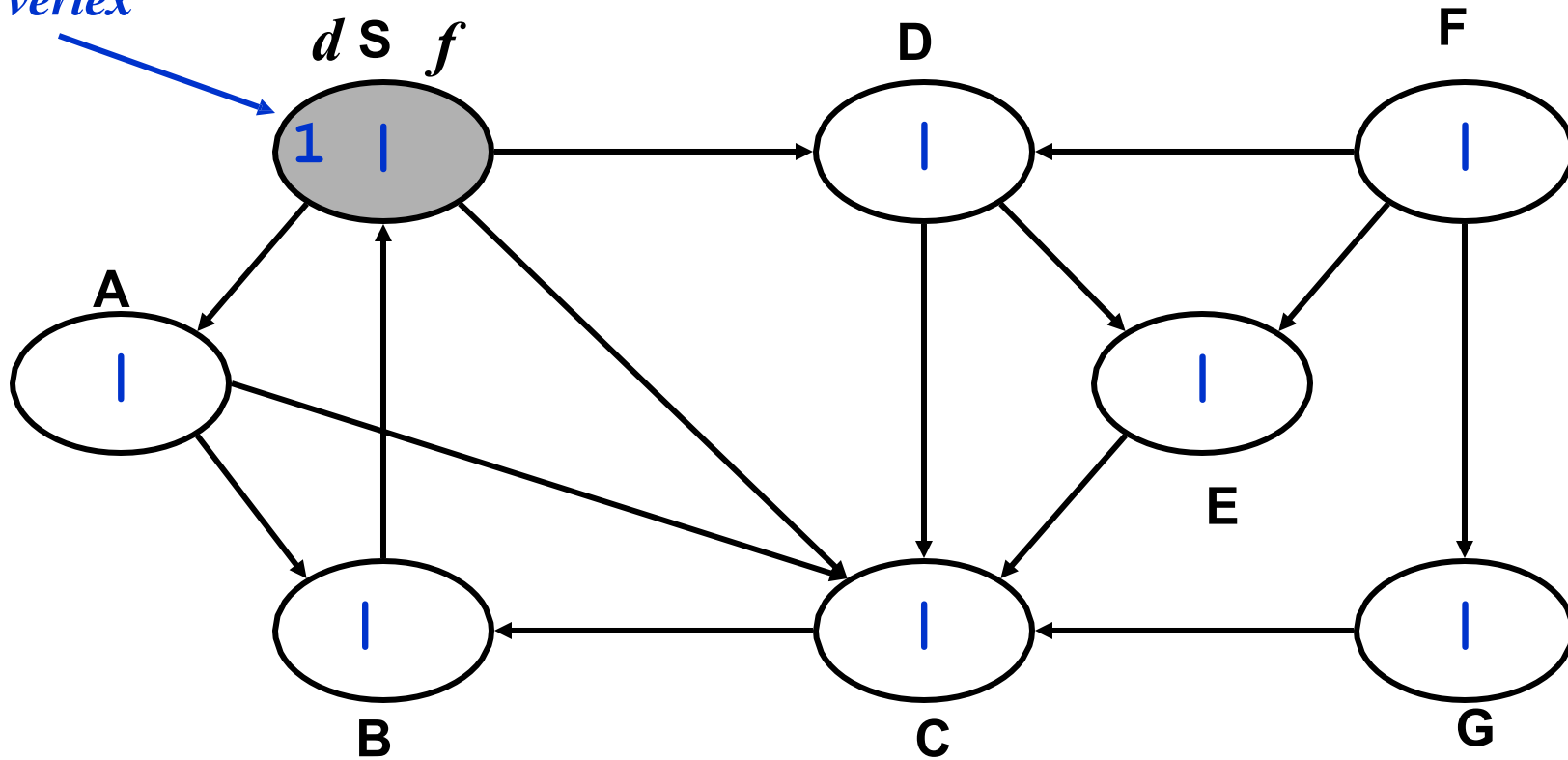
# DFS Example

*source  
vertex*



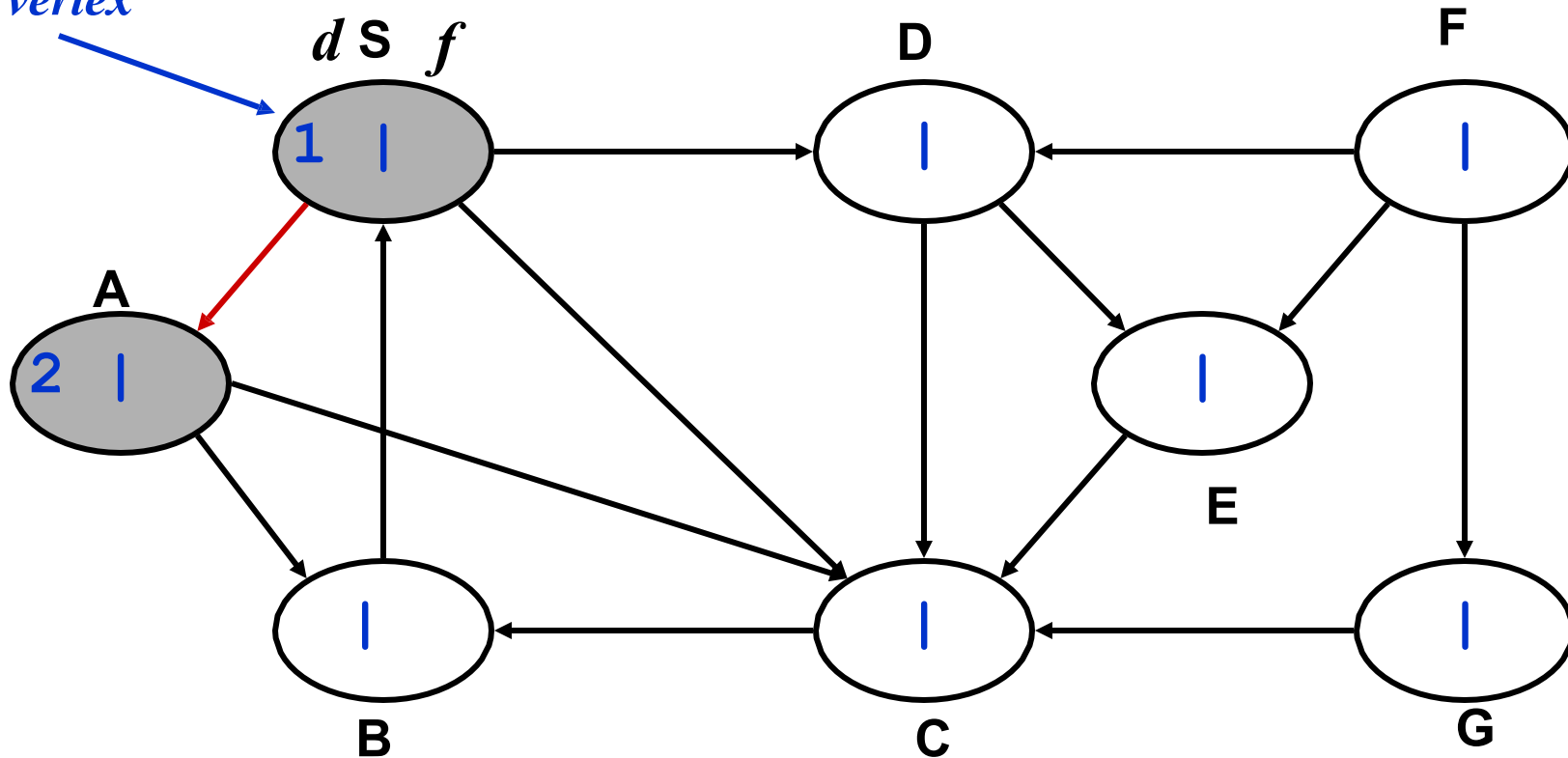
# DFS Example

*source  
vertex*



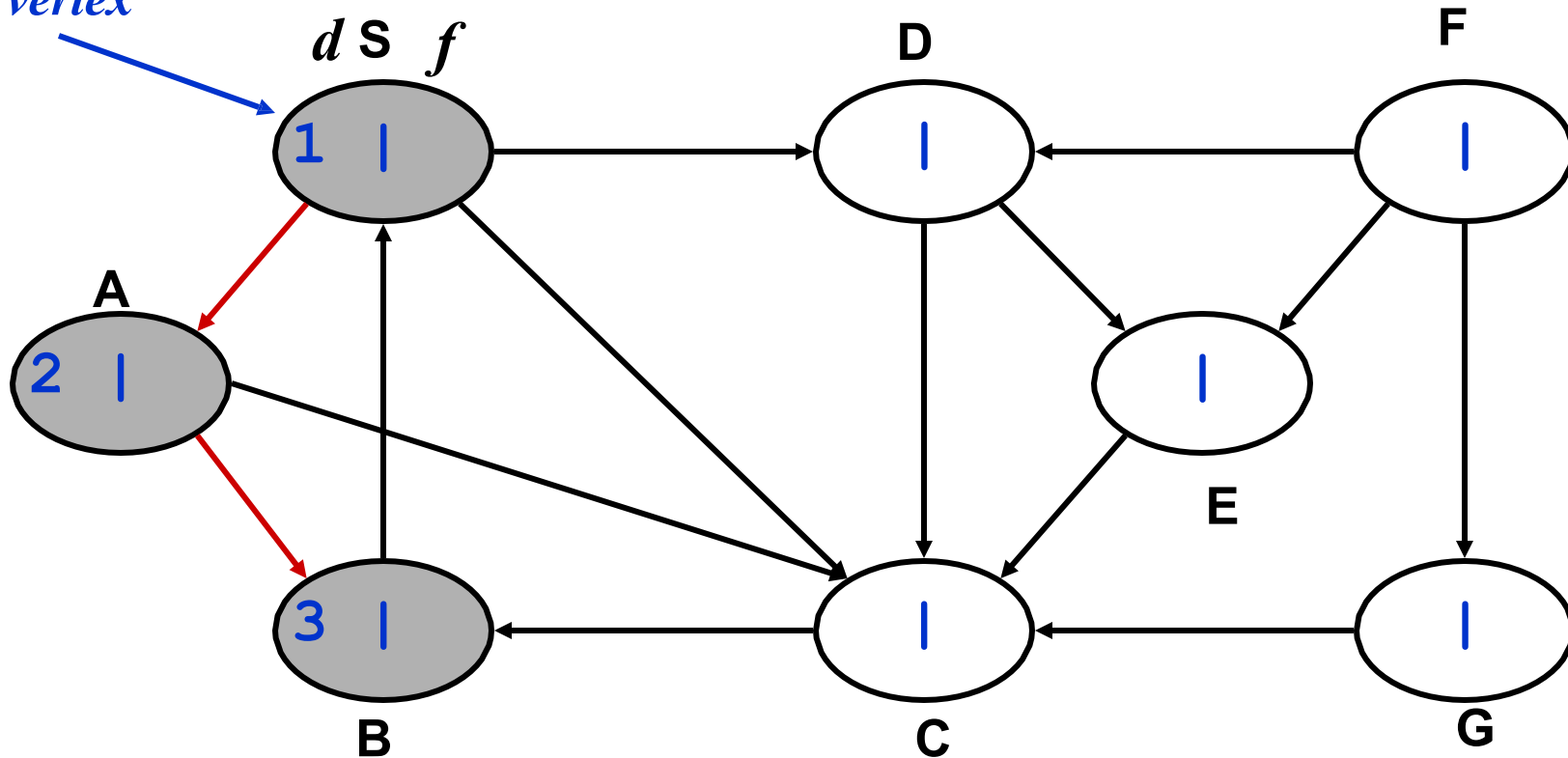
# DFS Example

*source  
vertex*



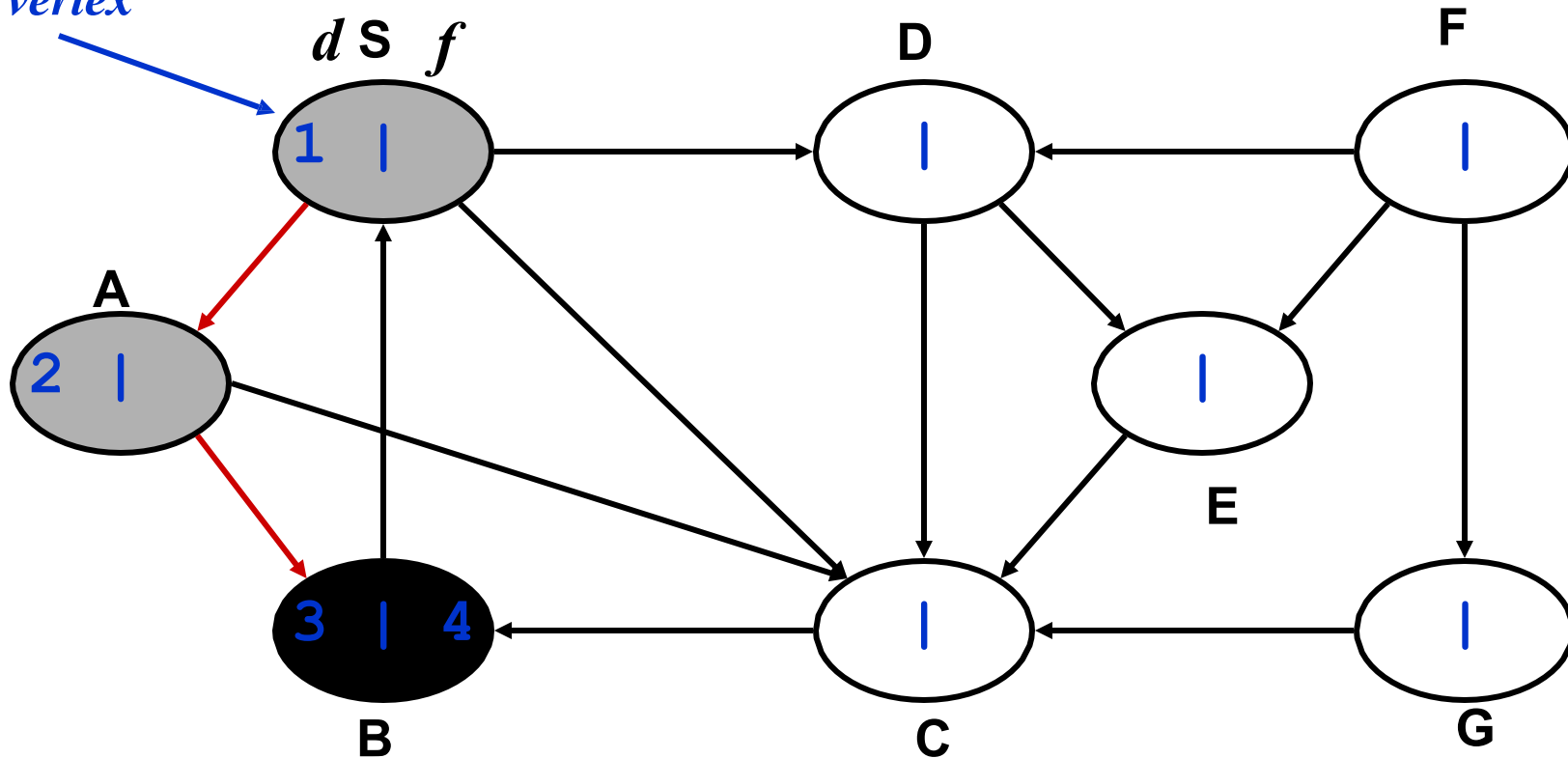
# DFS Example

*source  
vertex*



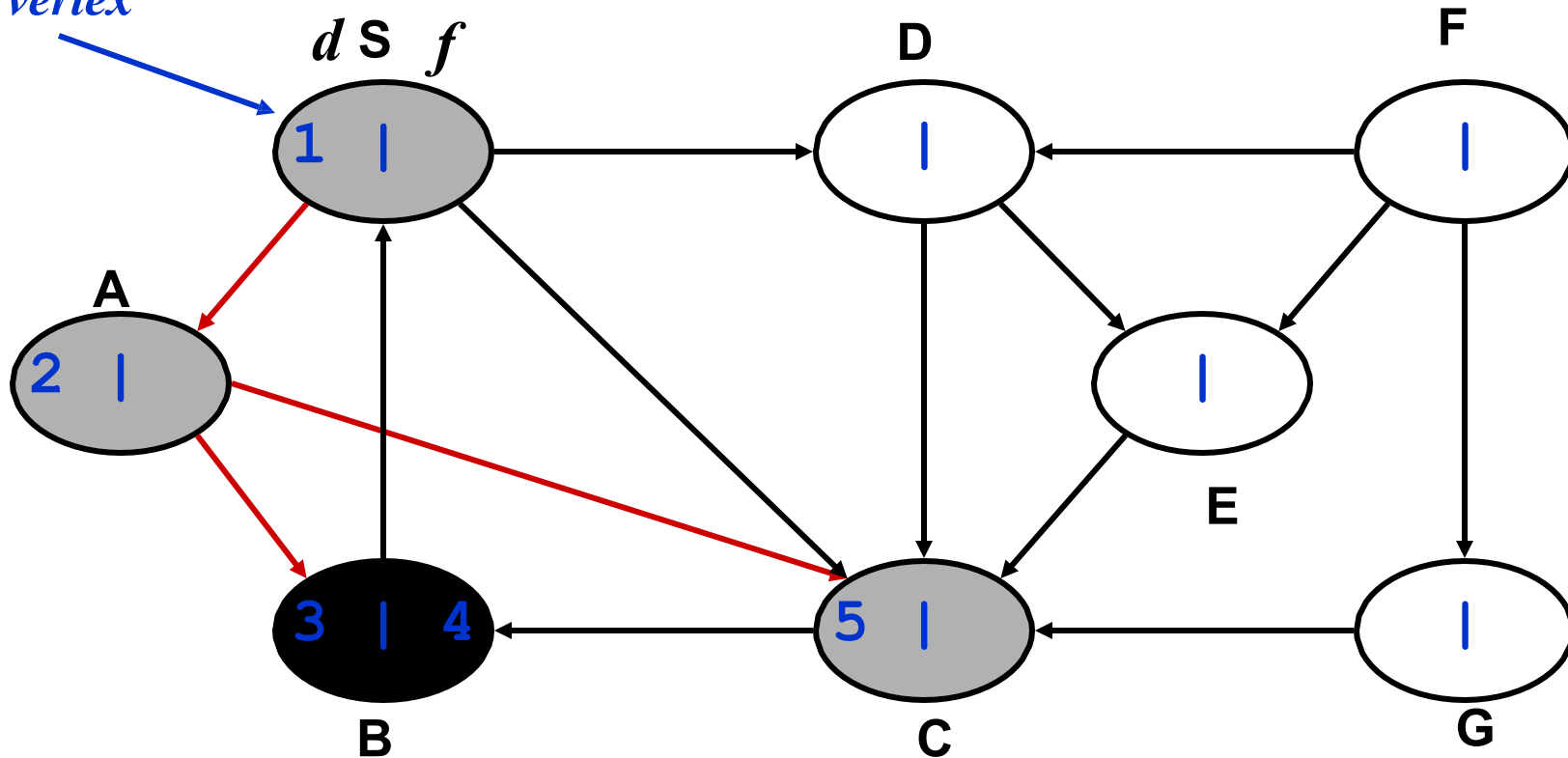
# DFS Example

*source  
vertex*



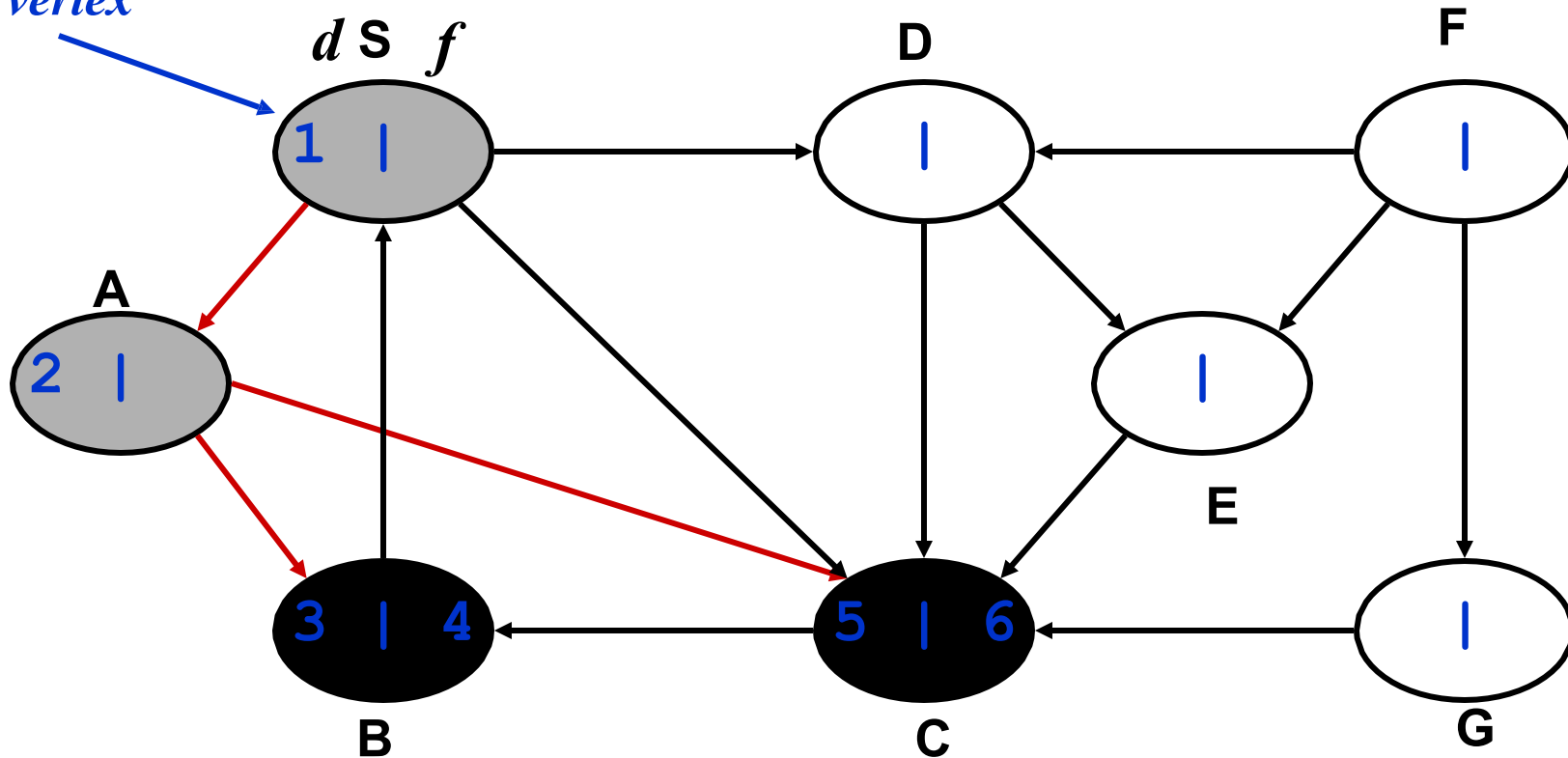
# DFS Example

*source  
vertex*



# DFS Example

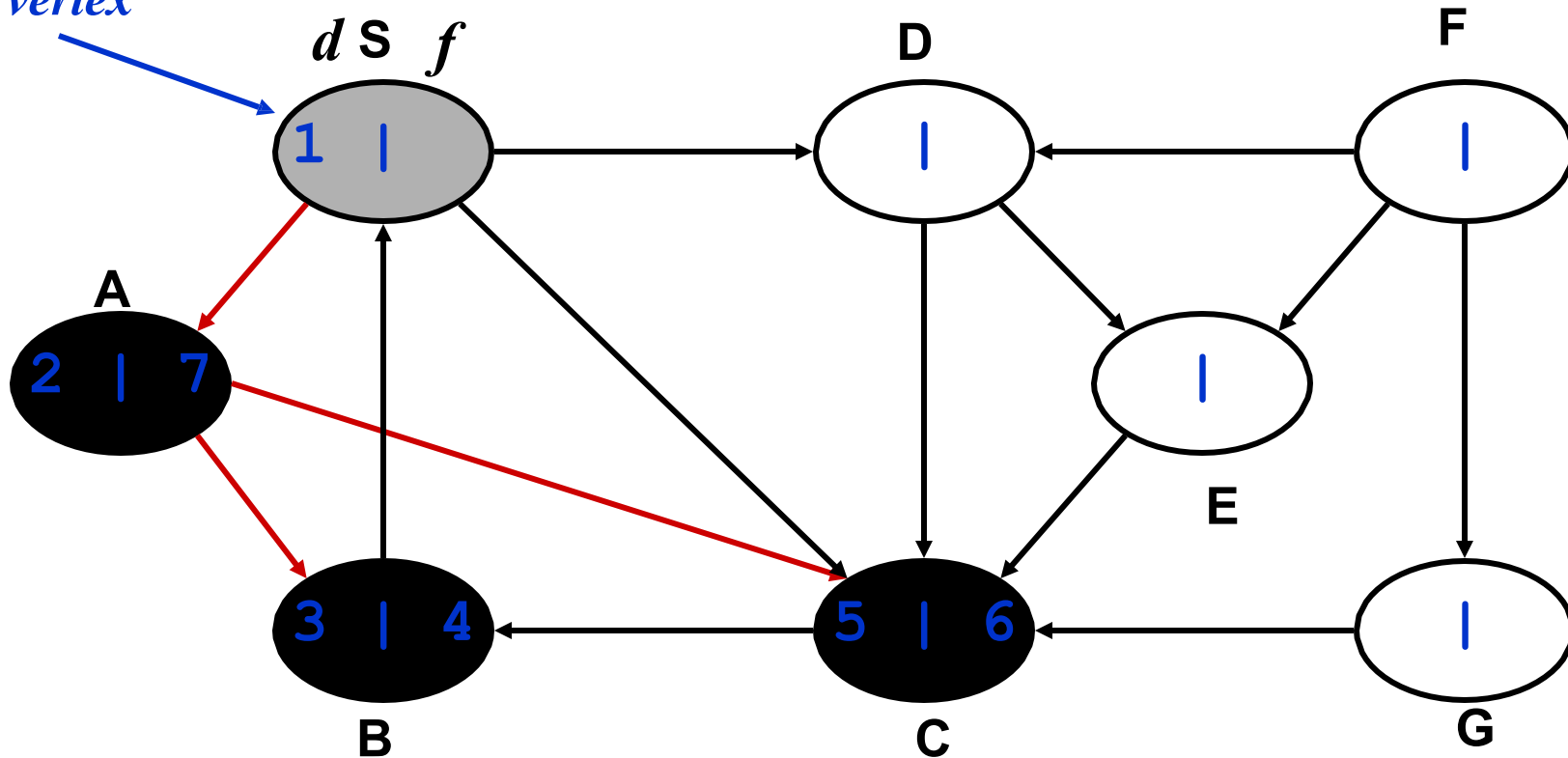
*source  
vertex*





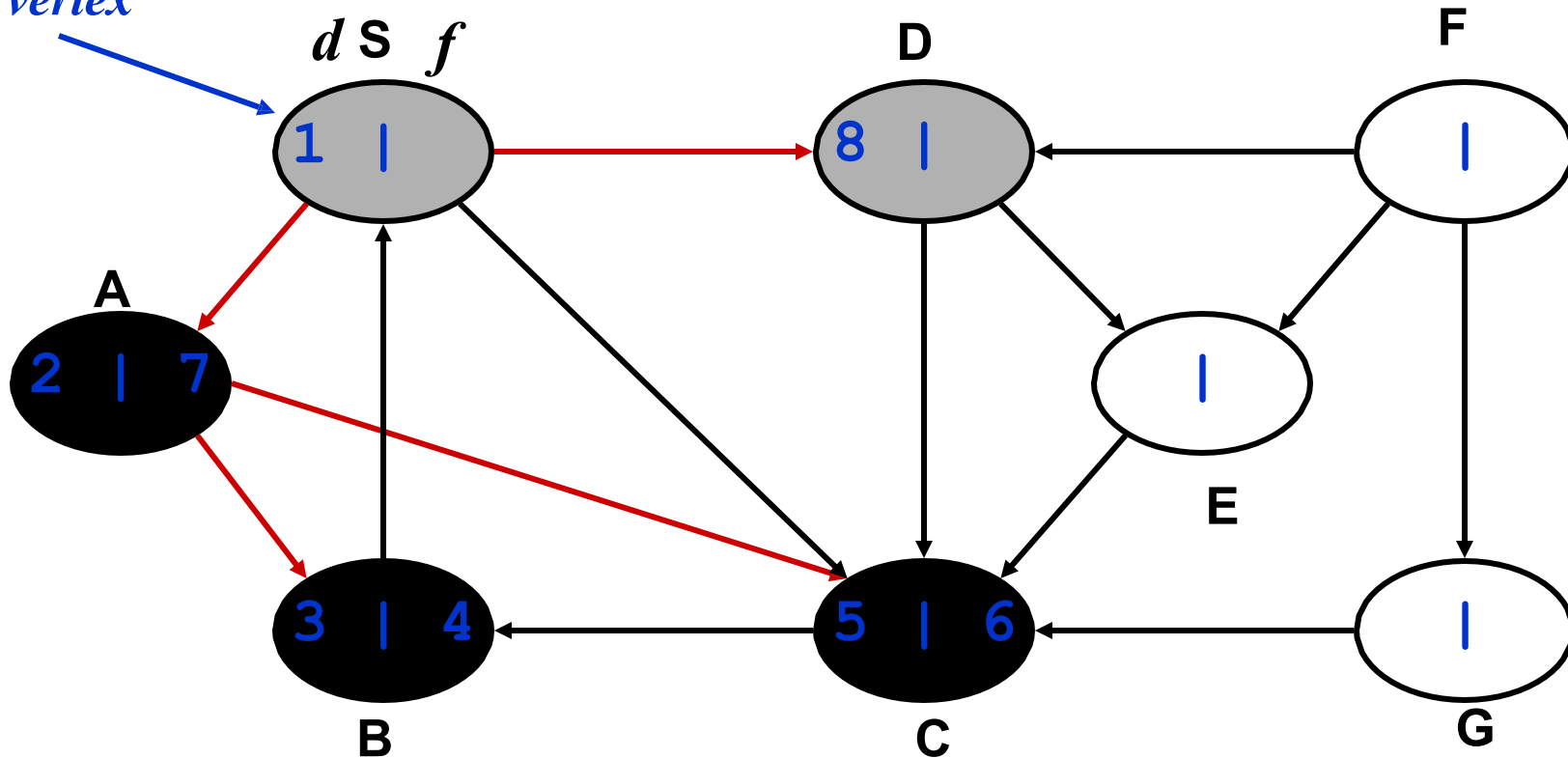
# DFS Example

*source  
vertex*



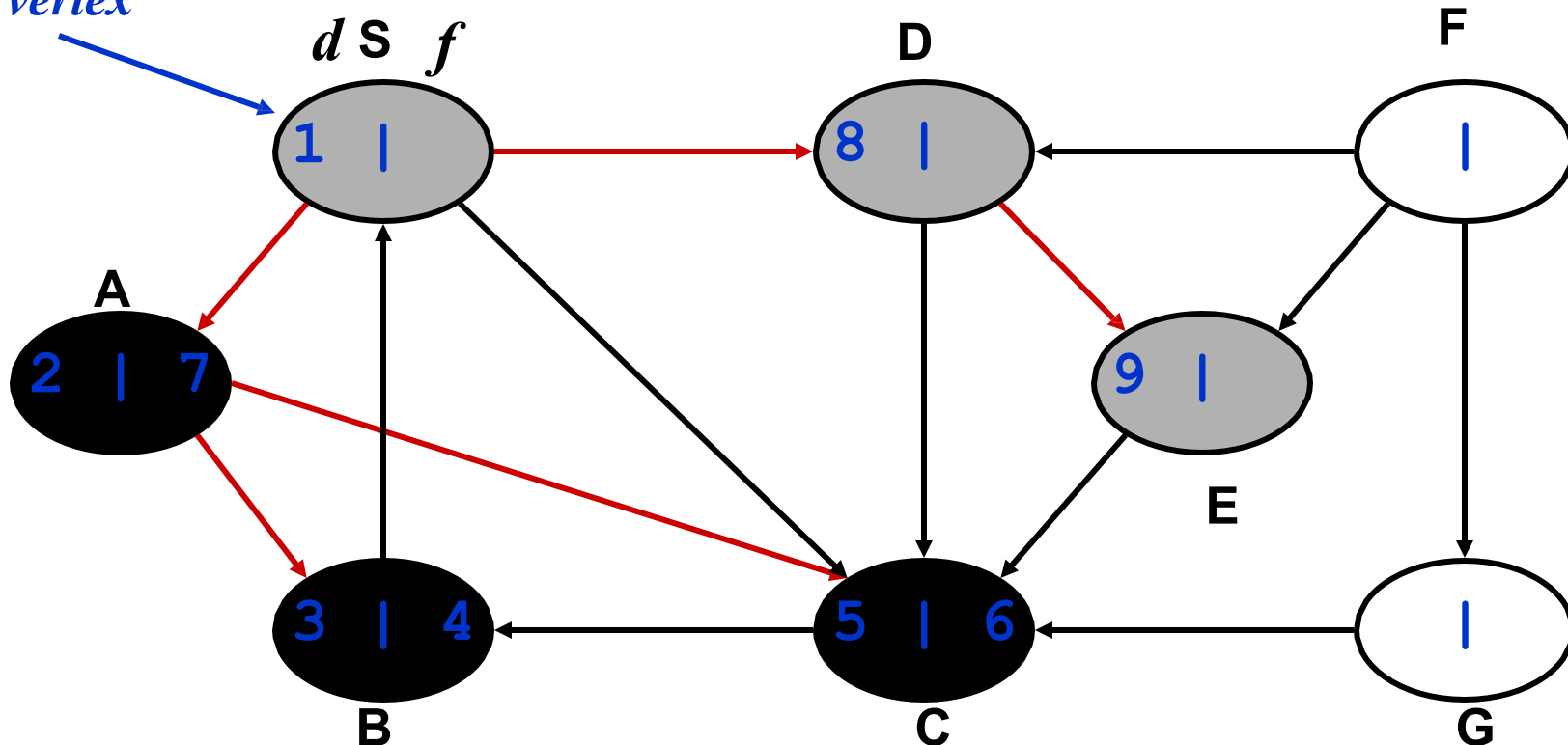
# DFS Example

*source  
vertex*



# DFS Example

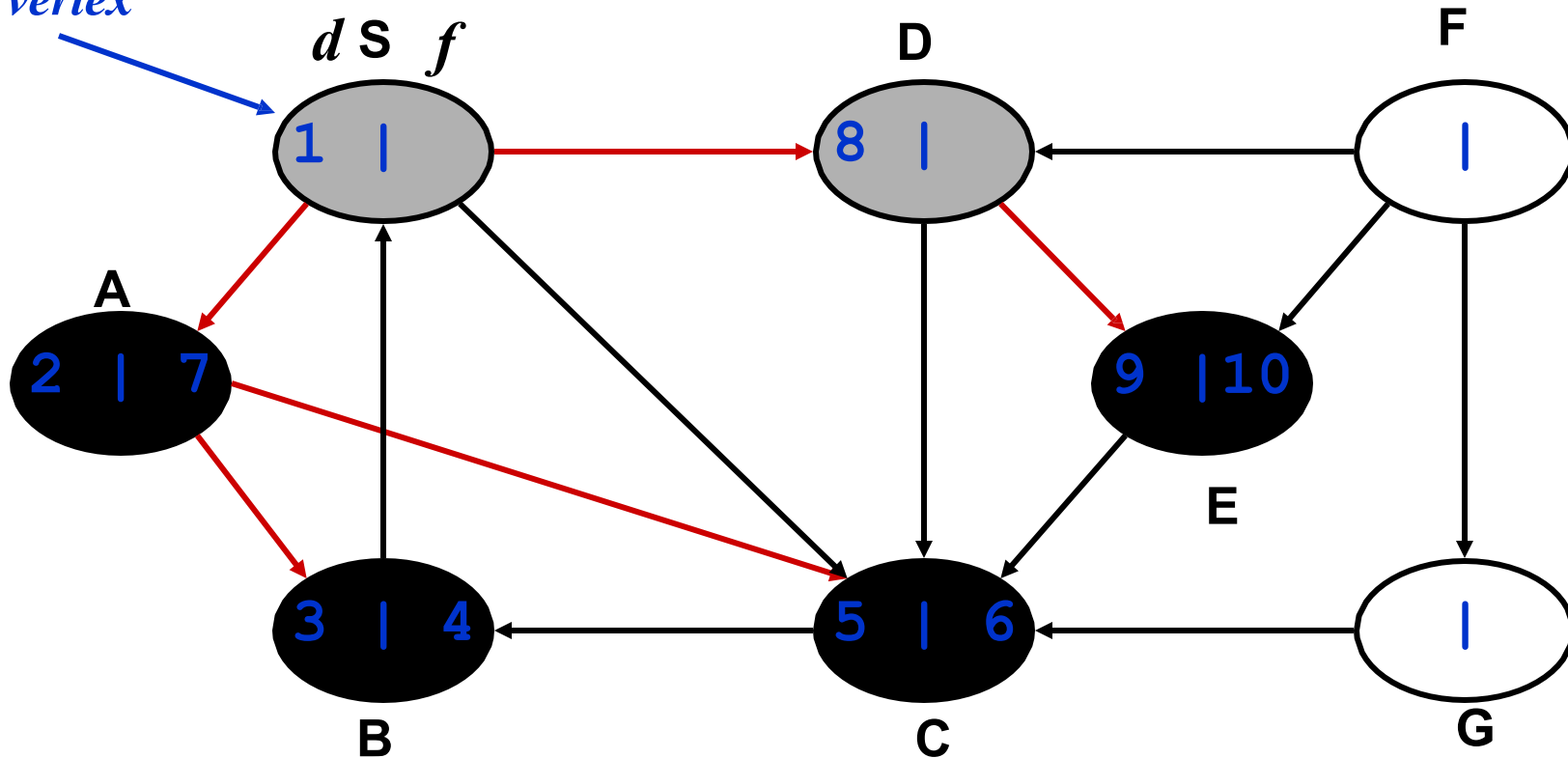
*source  
vertex*



*What is the structure of the grey vertices?  
What do they represent?*

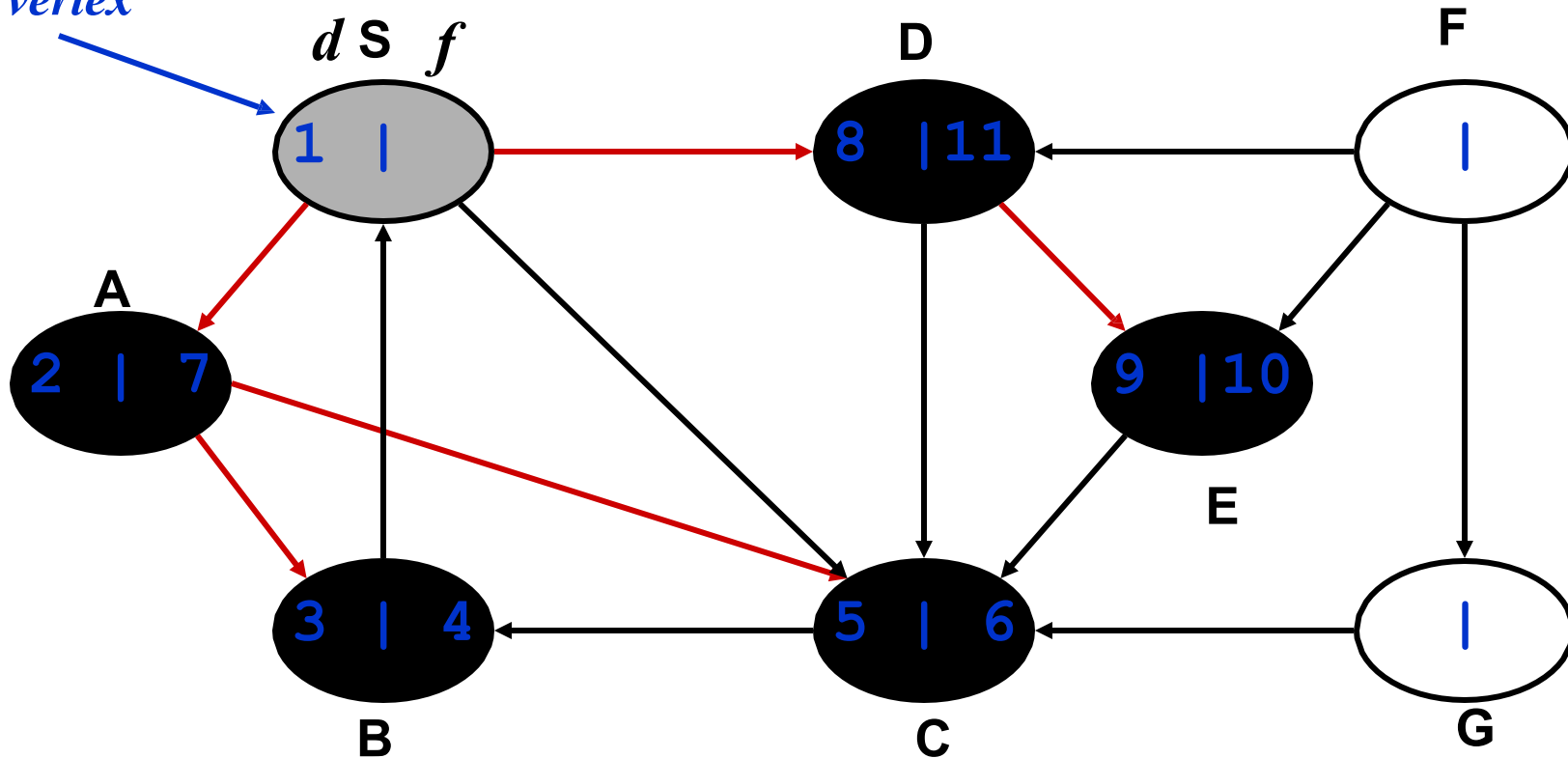
# DFS Example

*source  
vertex*



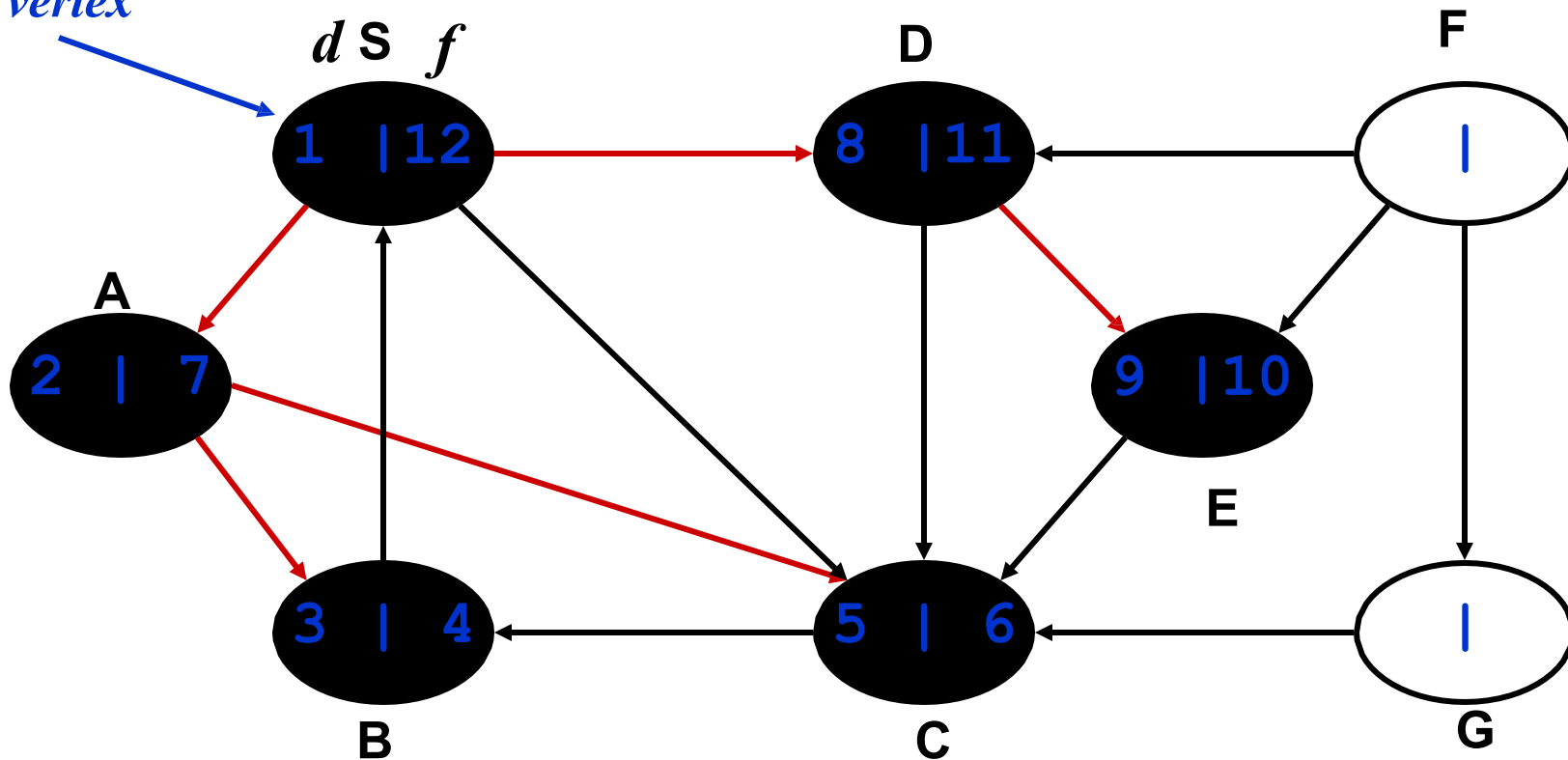
# DFS Example

*source  
vertex*



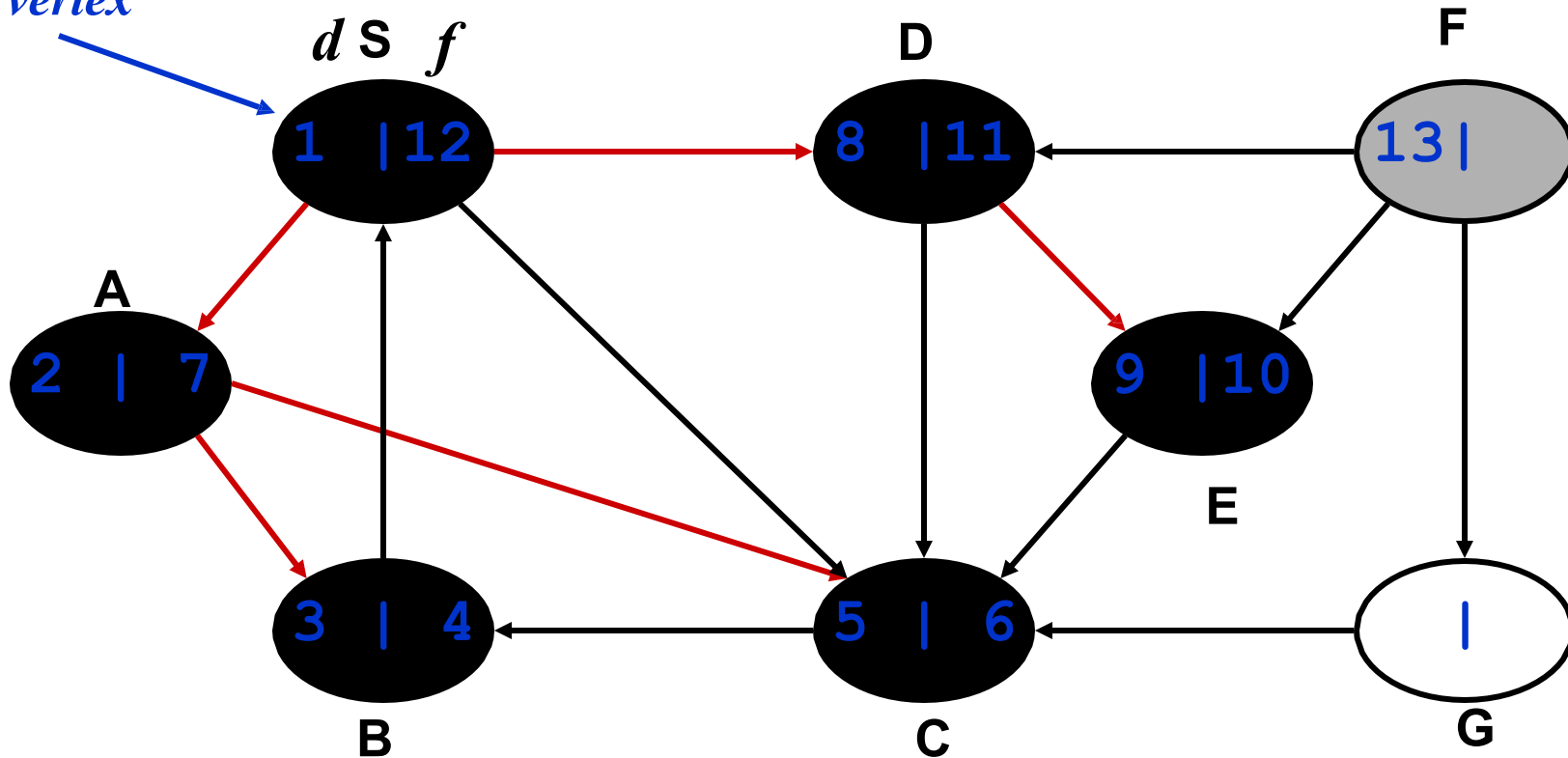
# DFS Example

*source  
vertex*



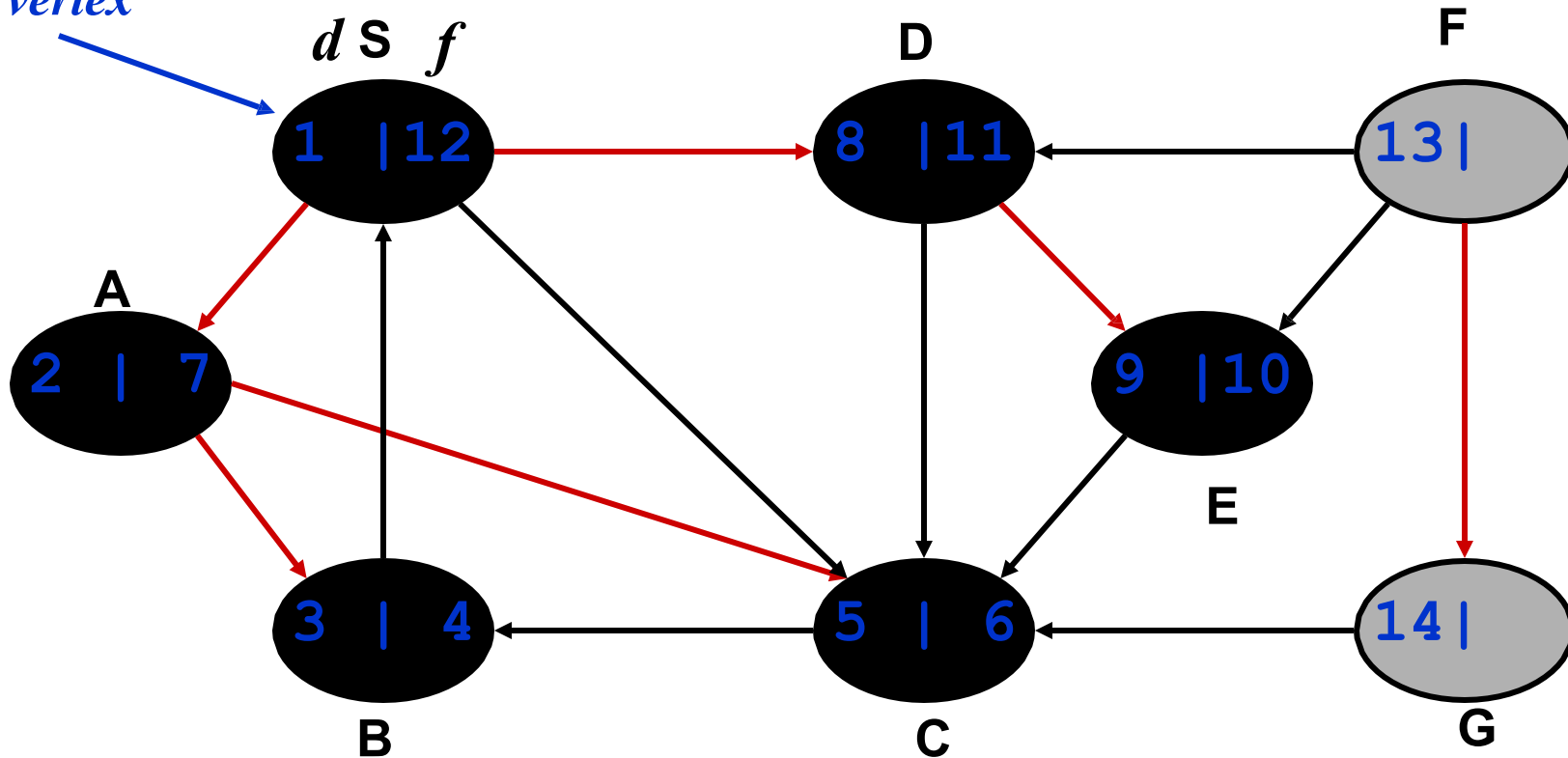
# DFS Example

*source  
vertex*



# DFS Example

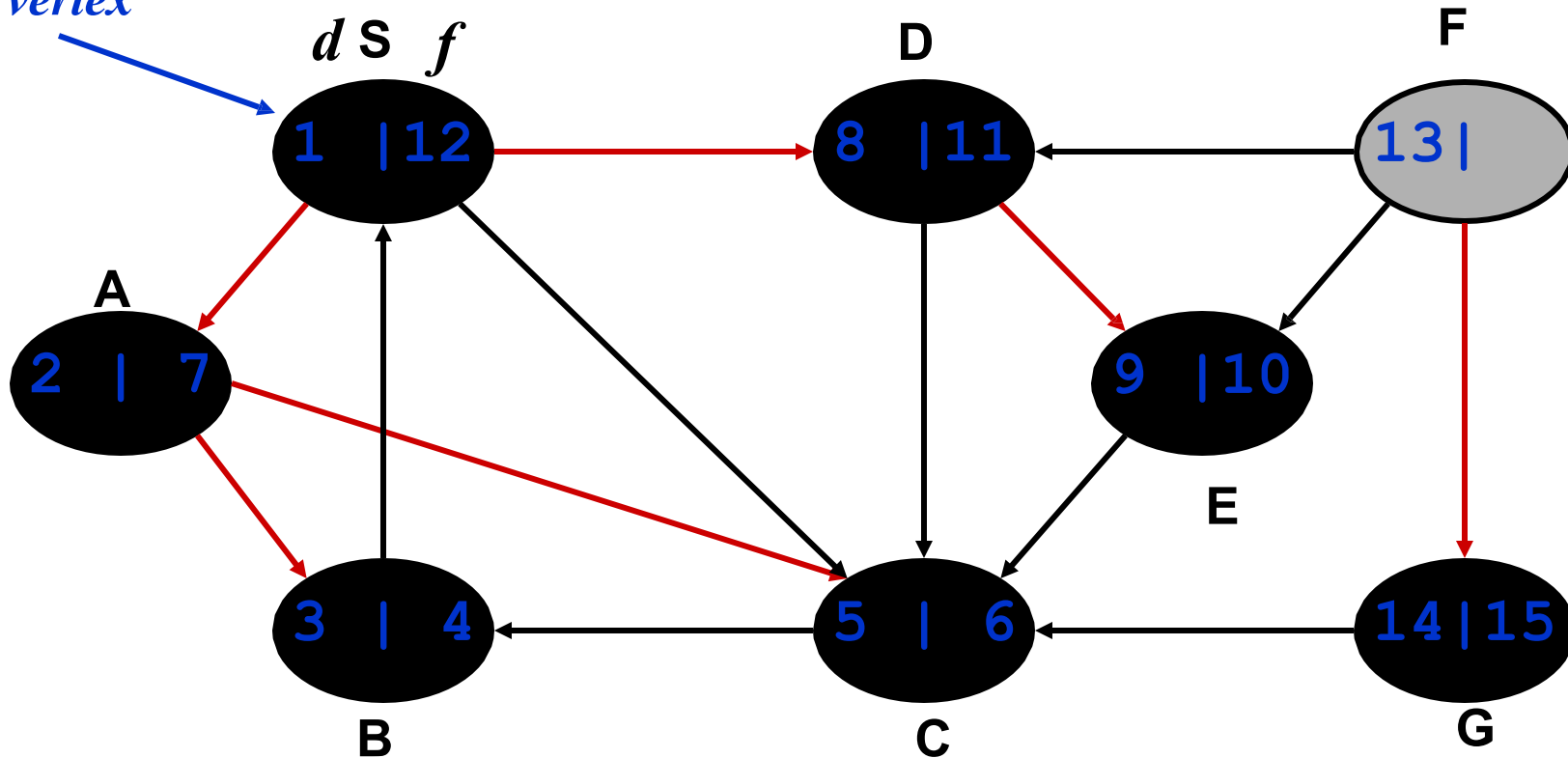
*source  
vertex*





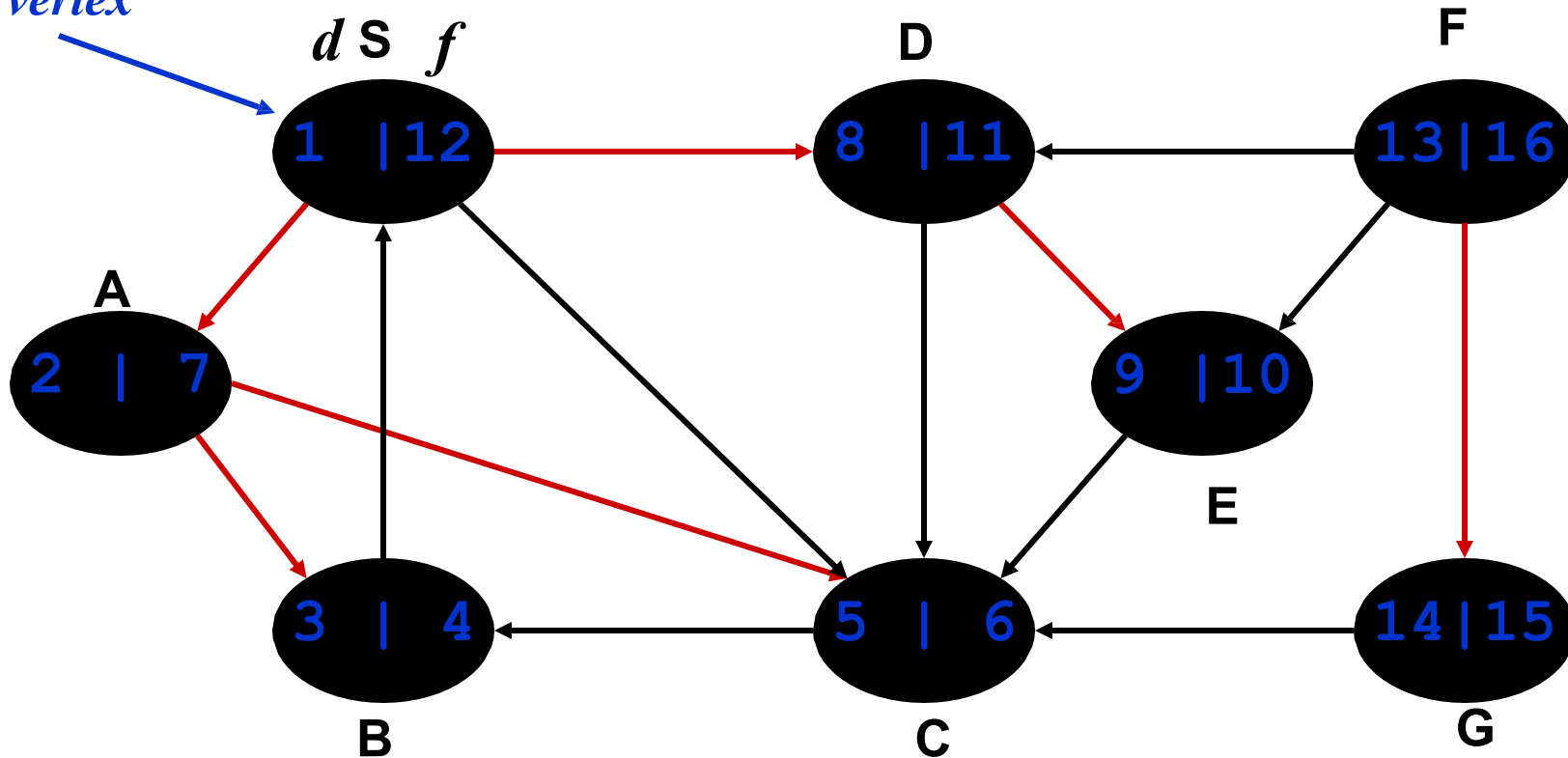
# DFS Example

*source  
vertex*



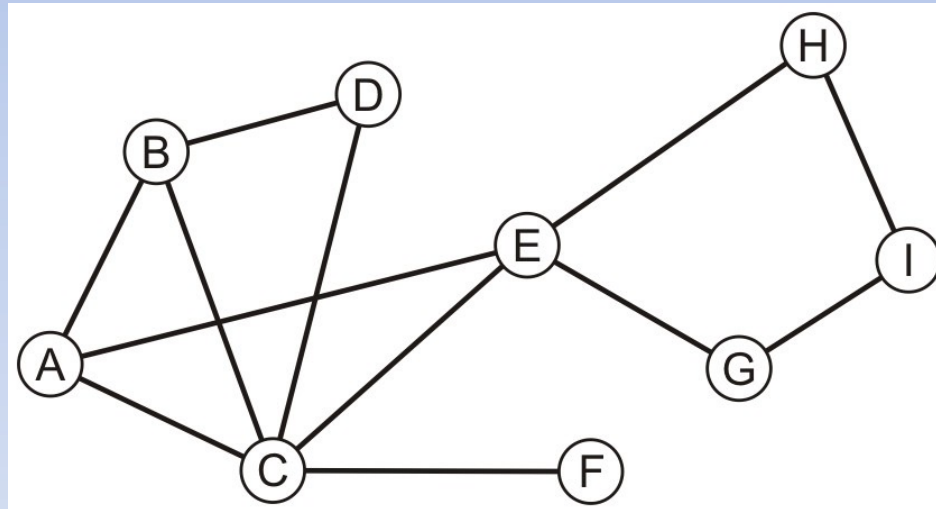
# DFS Example

*source  
vertex*



# Example

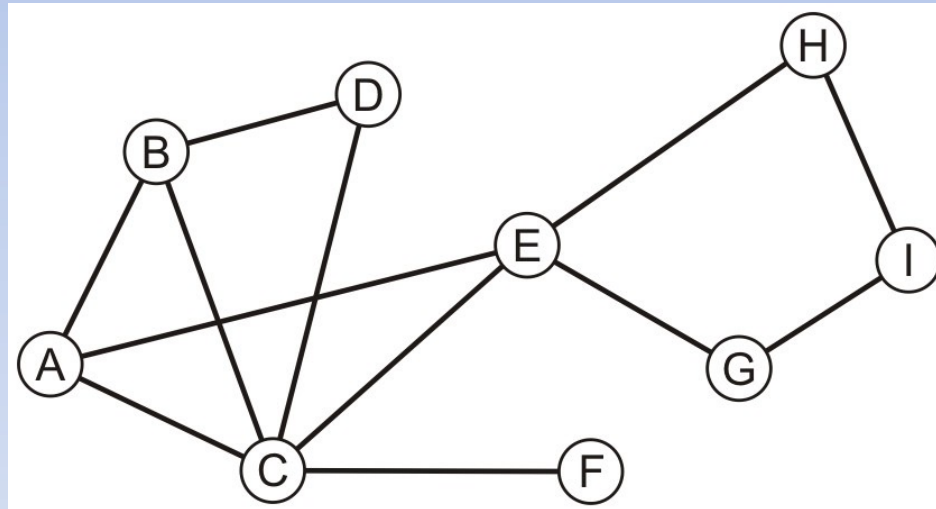
Consider this graph



# Example

Performing a breadth-first traversal

- Push the first vertex onto the queue

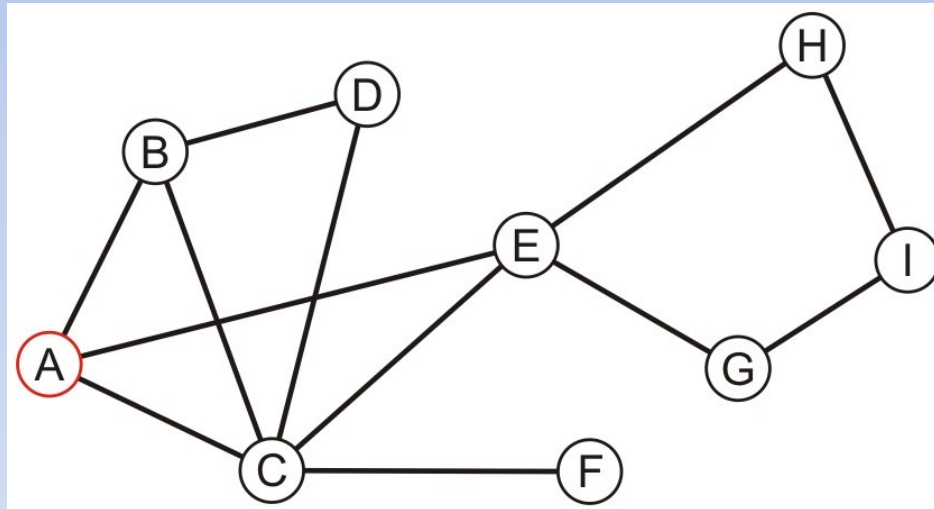


# Example

Performing a breadth-first traversal

- Pop A and push B, C and E

A



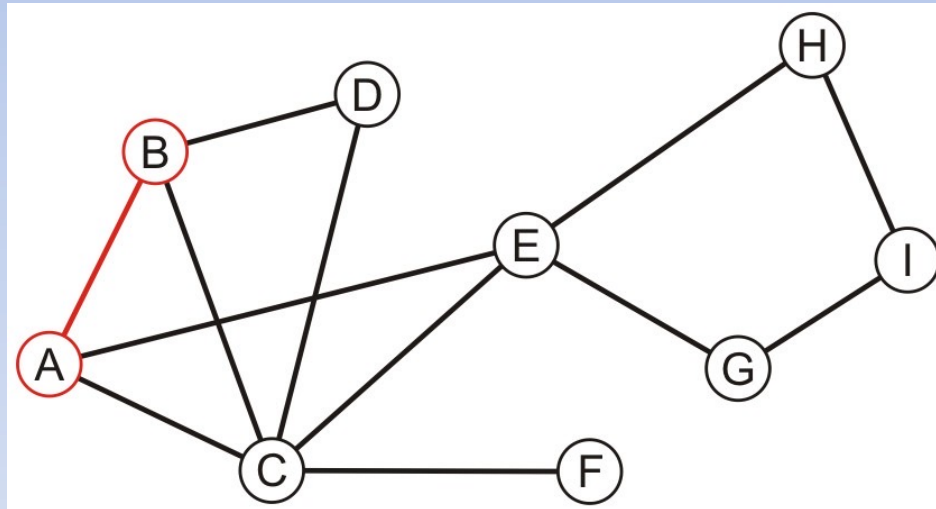
B	C	E			
---	---	---	--	--	--

# Example

Performing a breadth-first traversal:

- Pop B and push D

A, B



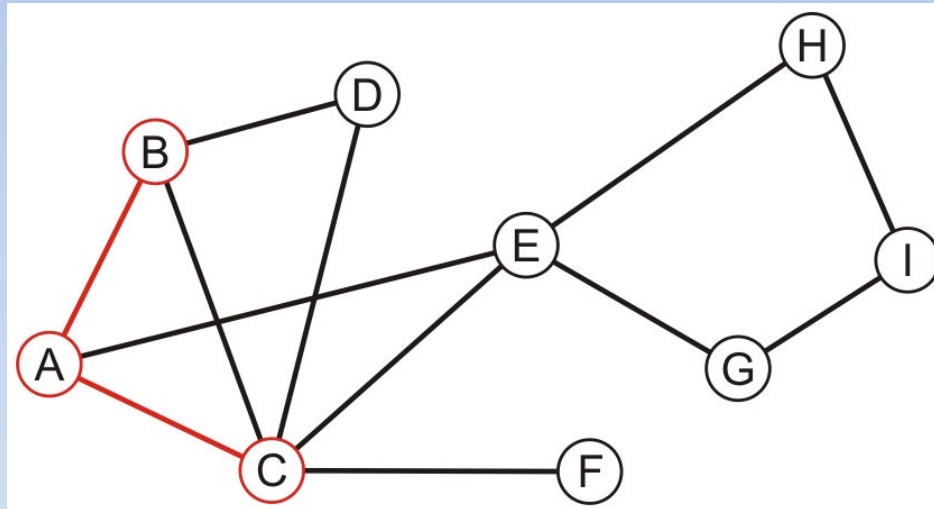
C	E	D			
---	---	---	--	--	--

# Example

Performing a breadth-first traversal:

- Pop C and push F

A, B, C



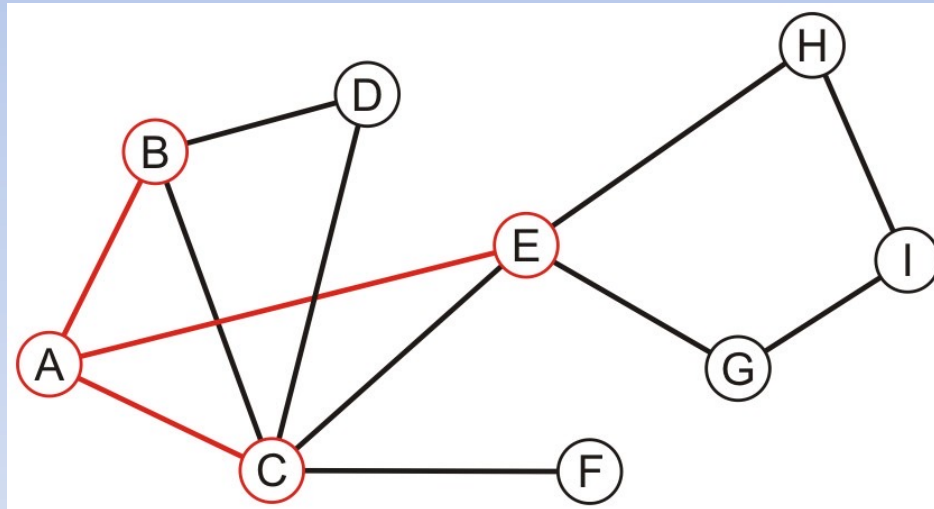
E	D	F			
---	---	---	--	--	--

# Example

Performing a breadth-first traversal:

- Pop E and push G and H

A, B, C, E



D	F	G	H		
---	---	---	---	--	--

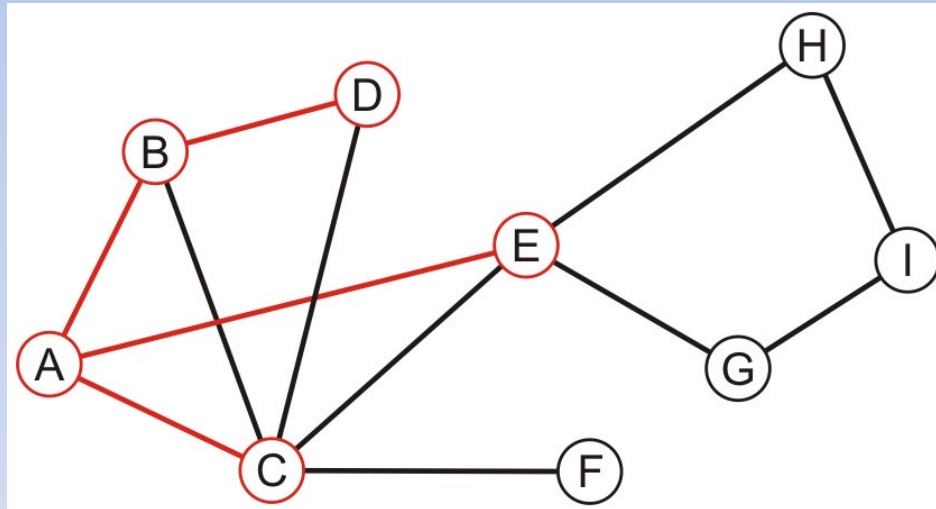


# Example

Performing a breadth-first traversal:

- Pop D

A, B, C, E, D



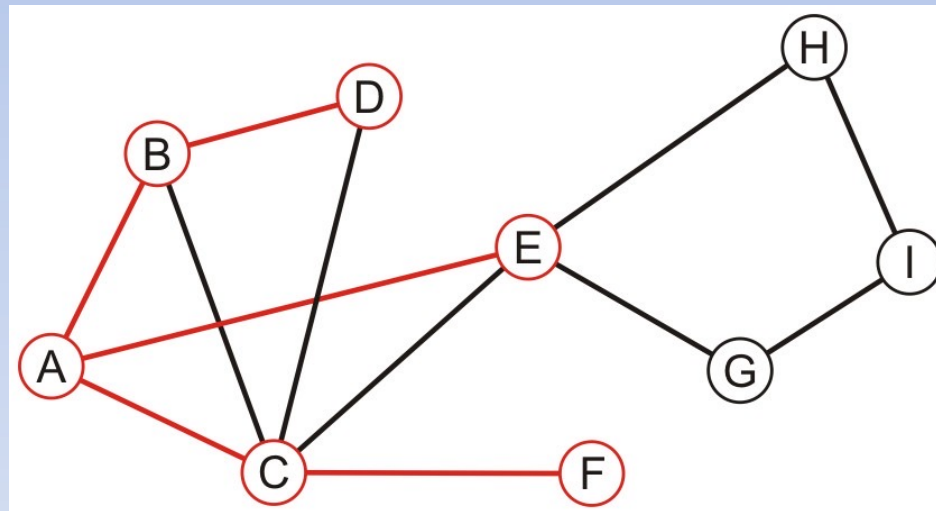
F	G	H			
---	---	---	--	--	--

# Example

Performing a breadth-first traversal:

- Pop F

A, B, C, E, D, F



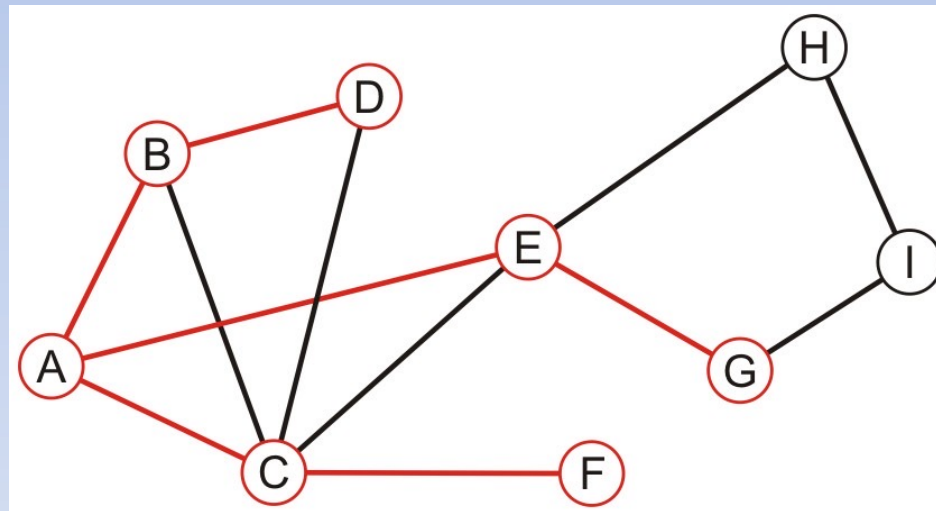
G	H				
---	---	--	--	--	--

# Example

Performing a breadth-first traversal:

- Pop G and push I

A, B, C, E, D, F, G



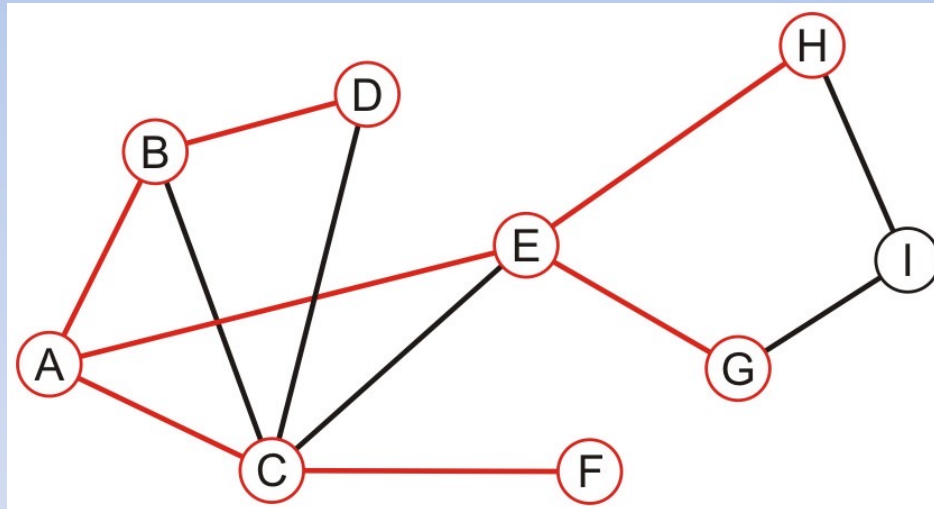
H	I				
---	---	--	--	--	--

# Example

Performing a breadth-first traversal:

- Pop H

A, B, C, E, D, F, G, H

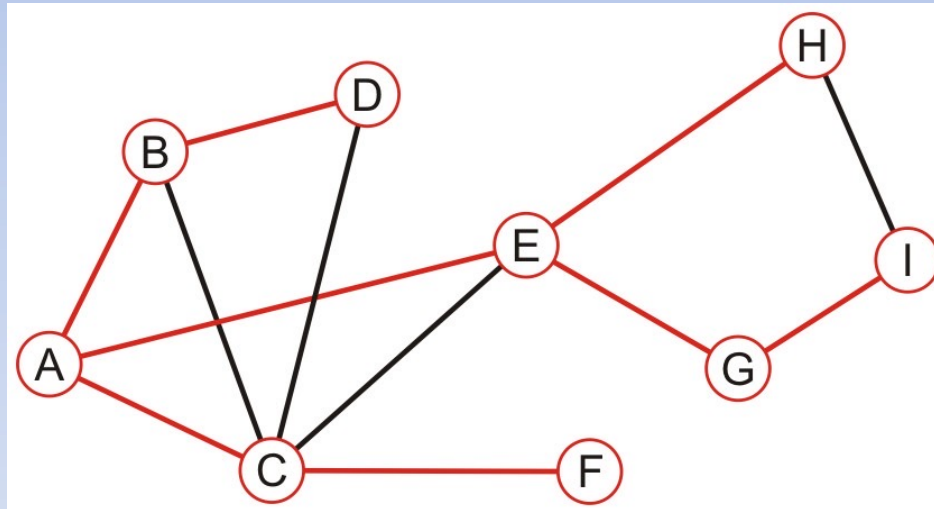


# Example

Performing a breadth-first traversal:

- Pop I

A, B, C, E, D, F, G, H, I

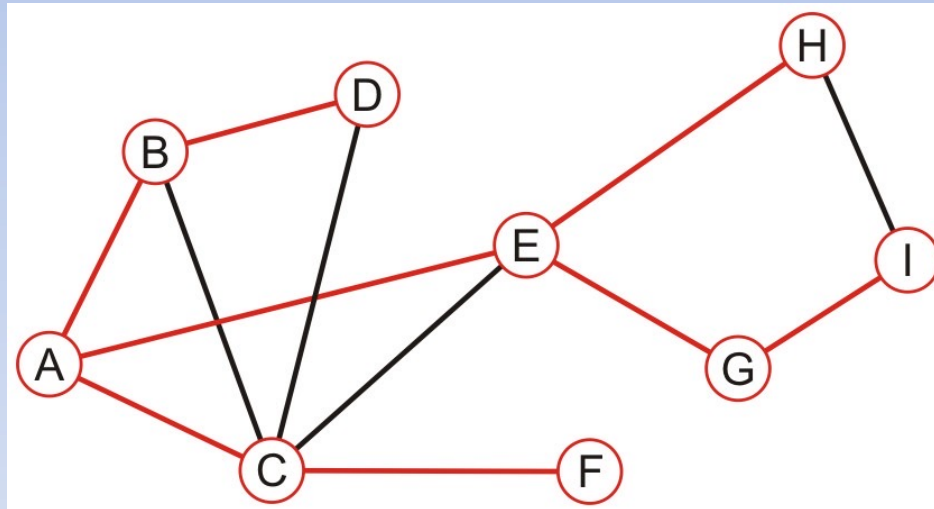


# Example

Performing a breadth-first traversal:

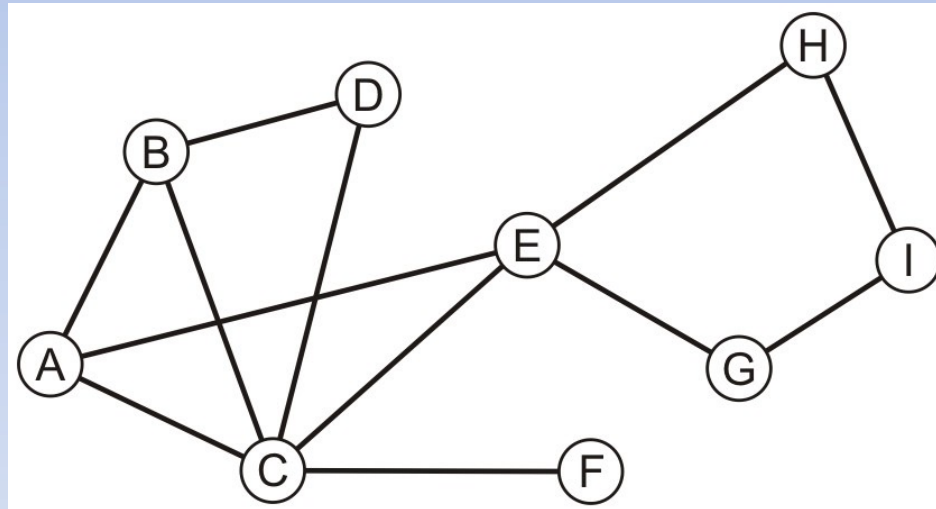
- The queue is empty: we are finished

A, B, C, E, D, F, G, H, I



# Example

Perform a recursive depth-first traversal on this same graph

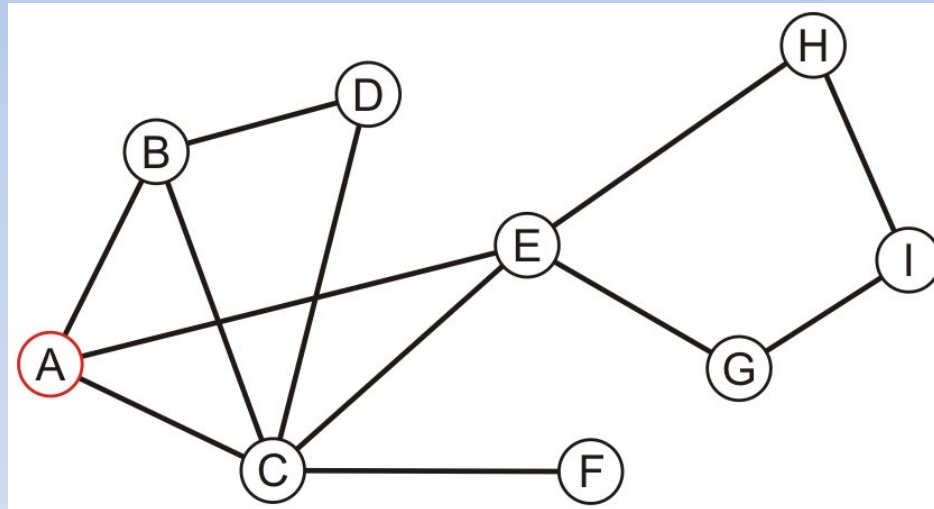


# Example

Performing a recursive depth-first traversal:

- Visit the first node

A

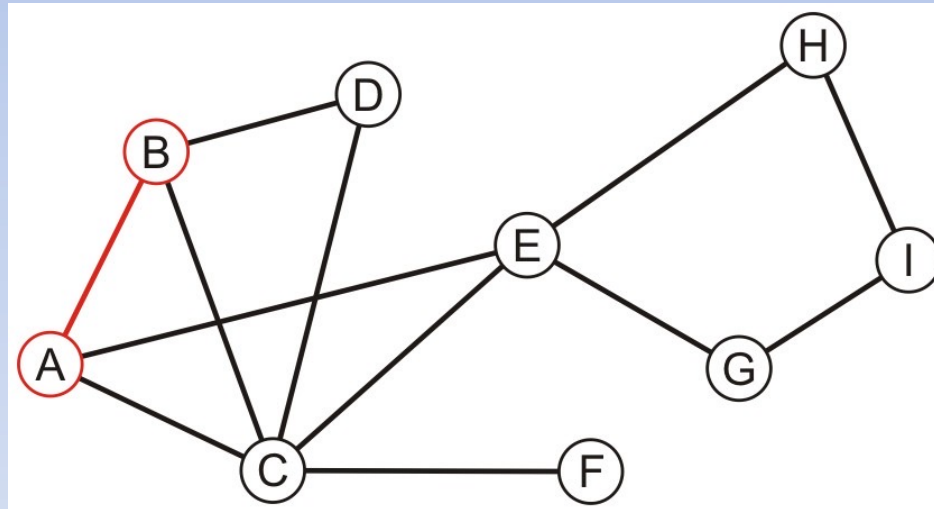




# Example

Performing a recursive depth-first traversal:

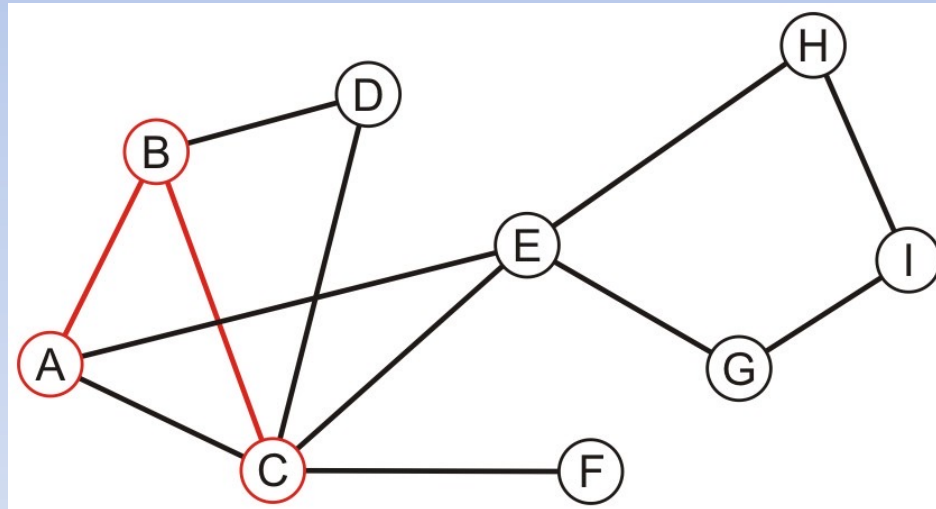
- A has an unvisited neighbor  
A, B



# Example

Performing a recursive depth-first traversal:

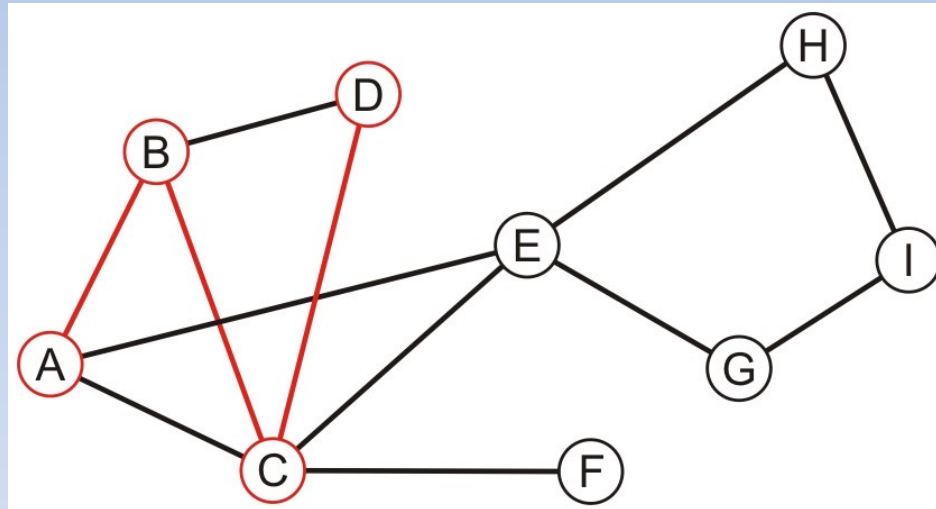
- B has an unvisited neighbor  
A, B, C



# Example

Performing a recursive depth-first traversal:

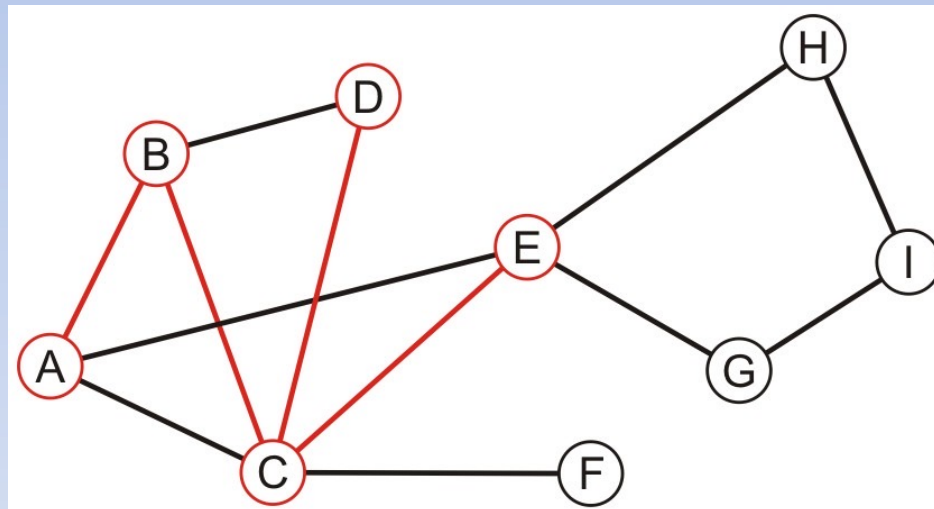
- C has an unvisited neighbor  
A, B, C, D



# Example

Performing a recursive depth-first traversal:

- D has no unvisited neighbors, so we return to C  
A, B, C, D, E

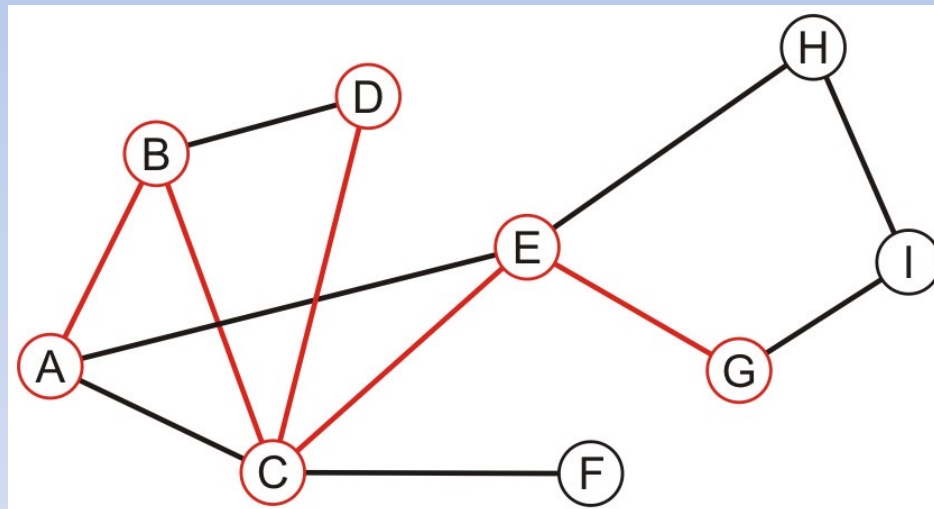


# Example

Performing a recursive depth-first traversal:

- E has an unvisited neighbor

A, B, C, D, E, G

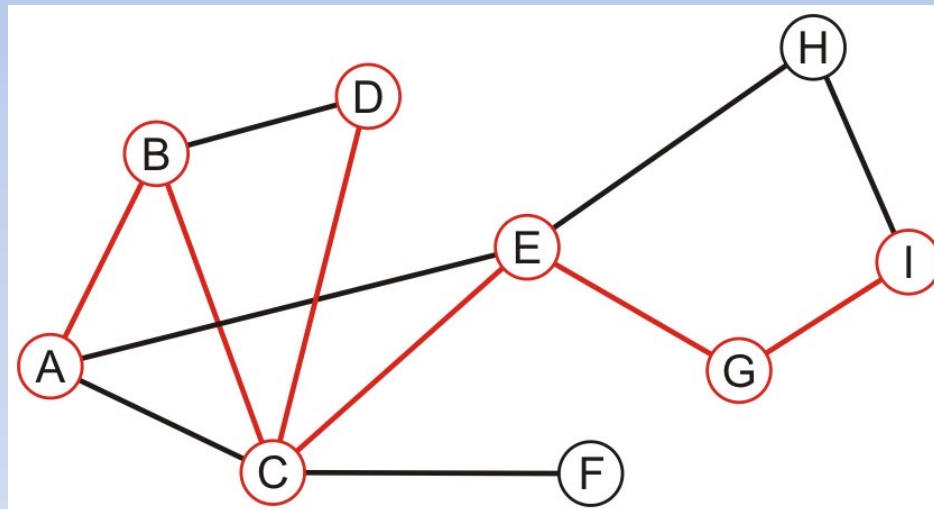


# Example

Performing a recursive depth-first traversal:

- F has an unvisited neighbor

A, B, C, D, E, G, I

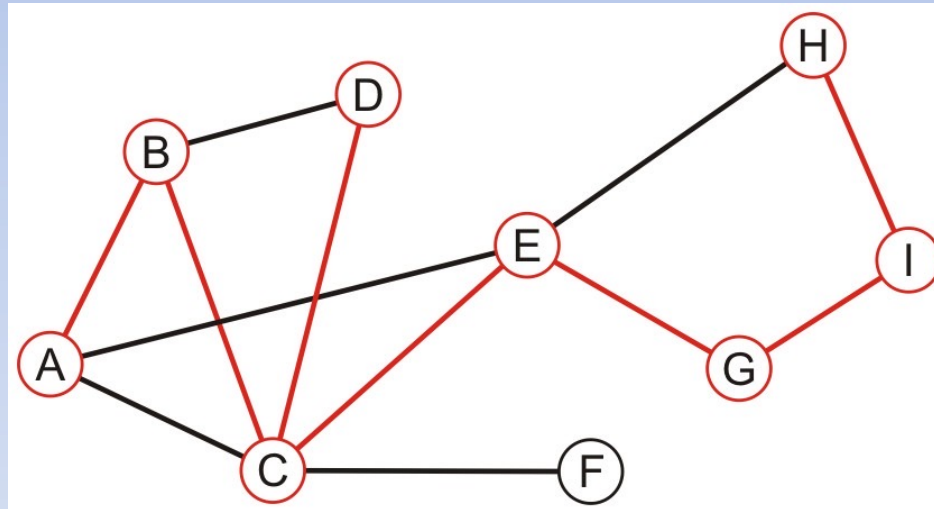


# Example

## Performing a recursive depth-first traversal:

- H has an unvisited neighbor

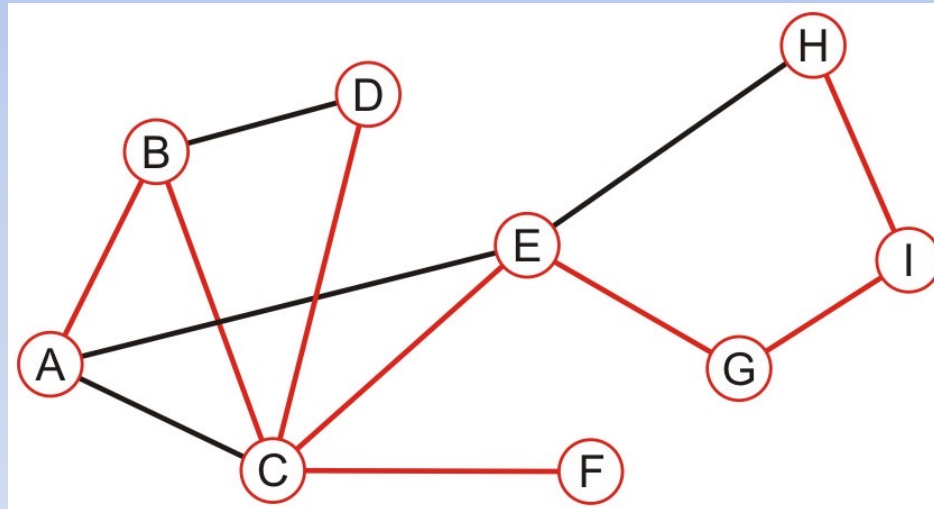
A, B, C, D, E, G, I, H



# Example

Performing a recursive depth-first traversal:

- We recurse back to C which has an unvisited neighbour  
A, B, C, D, E, G, I, H, F

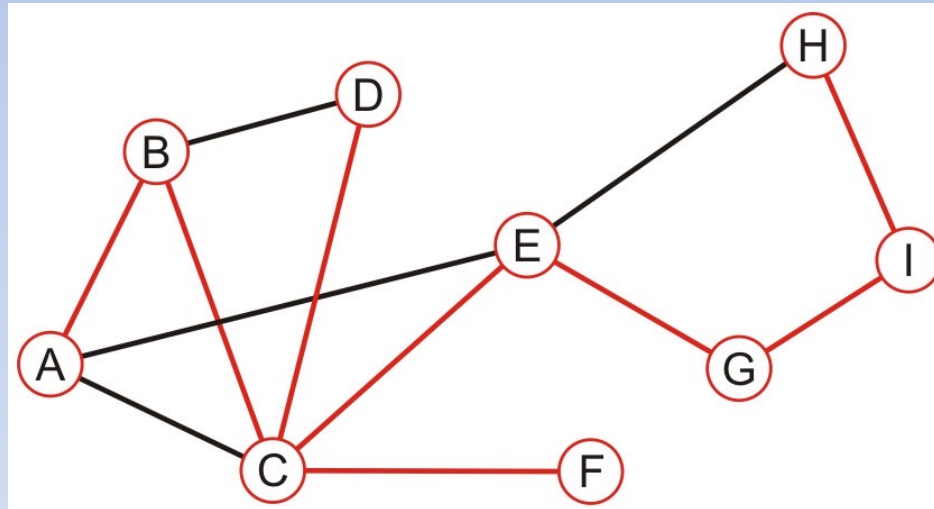




# Example

Performing a recursive depth-first traversal:

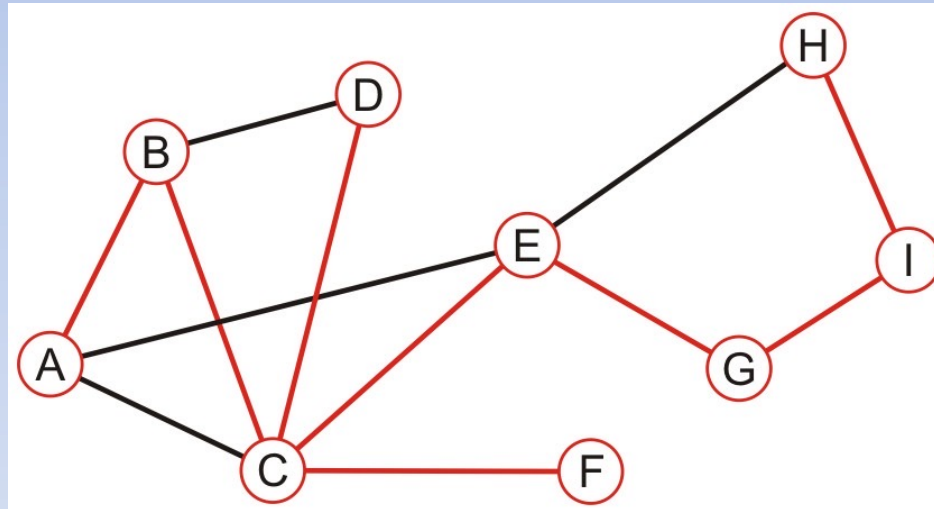
- We recurse finding that no other nodes have unvisited neighbours  
A, B, C, D, E, G, I, H, F



# Comparison

Performing a recursive depth-first traversal:

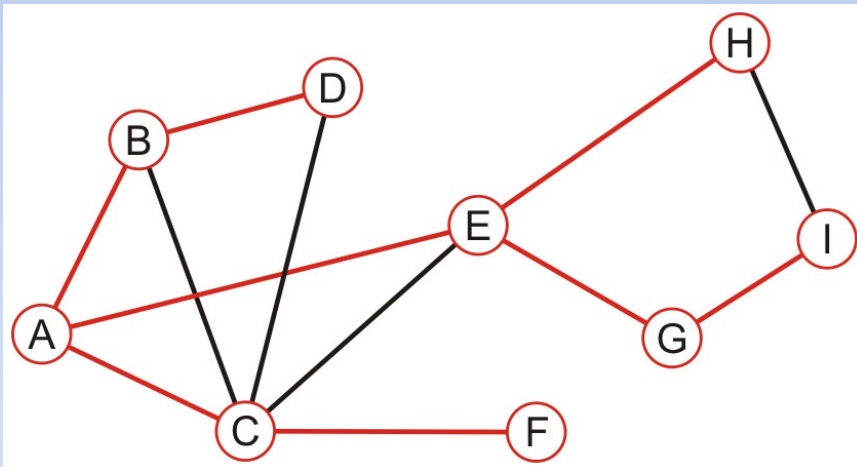
- We recurse finding that no other nodes have unvisited neighbours  
A, B, C, D, E, G, I, H, F



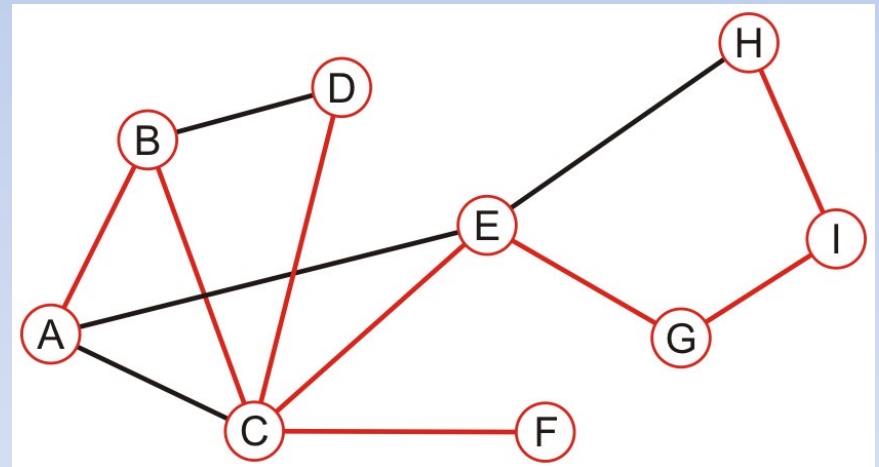
# Comparison

The order in which vertices can be traversed differ greatly

*A, B, C, E, D, F, G, H, I*



*A, B, C, D, E, G, I, H, F*



# Applications

Applications of tree traversals include:

- Determining connectiveness and finding connected sub-graphs
- Determining the path length from one vertex to all others
- Testing if a graph is bipartite
- Determining maximum flow
- Cheney's algorithm for garbage collection