

Q-1 Part-125

P-1

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Ans to the Q no. 2

Given,

$$A = \begin{bmatrix} 5 & -7 & 1 \\ -7 & 8 & 2 \\ 1 & 2 & -4 \end{bmatrix}$$

$$A^2 = \begin{bmatrix} 5 & -7 & 1 \\ -7 & 8 & 2 \\ 1 & 2 & -4 \end{bmatrix} \begin{bmatrix} 5 & -7 & 1 \\ -7 & 8 & 2 \\ 1 & 2 & -4 \end{bmatrix}$$

$$= \begin{bmatrix} 25 + 49 + 1 & -35 - 56 + 2 & 5 - 14 - 4 \\ -35 - 56 + 2 & 49 + 64 + 4 & -7 + 16 - 8 \\ 5 - 14 - 4 & -7 + 16 - 8 & 1 + 4 + 6 \end{bmatrix}$$

$$> \begin{bmatrix} 75 & -89 & -13 \\ -89 & 117 & 1 \\ -13 & 1 & 21 \end{bmatrix}$$



$$2A = 2 \left[ \begin{array}{ccc|ccc} 5 & -7 & 1 & 1 & 0 & 0 \\ -7 & 8 & 2 & 1 & 1 & -4 \end{array} \right]$$

$$= \left[ \begin{array}{ccc|ccc} 10 & -14 & 2 & 2 & 0 & 0 \\ -14 & 16 & 4 & 2 & 2 & -8 \end{array} \right]$$

$$\text{tr}(A^T) = \left[ \begin{array}{ccc|ccc} 5 & -7 & 1 & 0 & 0 & 0 \\ -7 & 8 & 1 & 0 & 0 & 0 \\ 1 & 2 & -4 & 0 & 0 & 0 \end{array} \right]$$

$$\text{tr} = 5 \times 8 \times -4$$

$$= 36$$



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$$A^{-1} = 12A + 400(A^T)$$

$$\begin{bmatrix} 25 & -89 & -15 \\ -89 & 117 & 1 \\ -13 & 1 & 21 \end{bmatrix} + \begin{bmatrix} 10 & -14 & 2 \\ -14 & 16 & 4 \\ 2 & 2 & 8 \end{bmatrix} + 62$$

$$\begin{bmatrix} 85 & -103 & -11 \\ -103 & 133 & 5 \\ -11 & 5 & 29 \end{bmatrix} \quad + 36$$

$$= 941$$



Ans to the Q no-1

Given,

$$x_1 + 2x_2 - 3x_3 + 4x_4 = 2$$

$$2x_1 + 5x_2 - 2x_3 + x_4 = 1$$

$$5x_1 + 12x_2 - 7x_3 + 6x_4 = 3$$

Now, Augmented matrix for the eq<sup>n</sup> is

$$\left[ \begin{array}{cccc|c} 1 & 2 & -3 & 4 & 2 \\ 2 & 5 & -2 & 1 & 1 \\ 5 & 12 & -7 & 6 & 3 \end{array} \right]$$

Now,

$$R_2 = 2R_1 - R_2$$

$$R_3 = 5R_1 - R_3$$

$$\left[ \begin{array}{cccc|c} 1 & 2 & -3 & 4 & 2 \\ 2 & 5 & -2 & 1 & 1 \\ 5 & 12 & -7 & 6 & 3 \end{array} \right]$$



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$$= \begin{array}{ccc|ccc} 1 & 2 & -3 & 4 & 2 & \\ 0 & -1 & -4 & 2 & 3 & \\ 0 & -2 & -8 & 14 & 7 & \end{array}$$

$$R_2 = R_1 + R_2$$

$$R_3 = R_1 + R_3$$

$$\begin{array}{ccc|ccc} 1 & 2 & -3 & 4 & 2 & \\ 0 & 1 & -7 & 11 & 5 & \\ 0 & 0 & 5 & 18 & 9 & \end{array}$$