



SECTION: 11

Course Name: MAT125(Quiz01- Fall 2020)

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Section: II

Quiz-01 (MATH125 - MEUSIR)

Ques no:

(1)

$$x_1 + 2x_2 - 3x_3 + 4x_4 = 2$$

$$2x_1 + 5x_2 - 2x_3 + x_4 = 1$$

$$5x_1 + 12x_2 - 7x_3 + 6x_4 = 3$$

- Augmented Matrix:

$$\begin{bmatrix} 1 & 2 & -3 & 4 & 2 \\ 2 & 5 & -2 & 1 & 1 \\ 5 & 12 & -7 & 6 & 3 \end{bmatrix}$$

S-1: Add $(-2 \times \text{row } 1)$ to row 2

$$\begin{bmatrix} 1 & 2 & -3 & 4 & 2 \\ 0 & 1 & 4 & -7 & -3 \\ 5 & 12 & -7 & 6 & 3 \end{bmatrix}$$

S-2: Add $(-5 \times \text{row } 1)$ to row 3

$$\begin{bmatrix} 1 & 2 & -3 & 4 & 2 \\ 0 & 1 & 4 & -7 & -3 \\ 0 & 2 & 8 & 14 & 7 \end{bmatrix}$$

S-3: Add $(-2 \times \text{row } 2)$ to row 3:

$$\begin{bmatrix} 1 & 2 & -3 & 4 & 2 \\ 0 & 1 & 4 & -7 & -3 \\ 0 & 0 & 0 & 0 & -1 \end{bmatrix}$$

S-4: Divide row 3 by -1 :

$$\begin{bmatrix} 1 & 2 & -3 & 4 & 2 \\ 0 & 1 & 4 & -7 & -3 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

S-5: Add $(3 \times \text{row } 3)$ to row 2:

$$\begin{bmatrix} 1 & 2 & -3 & 4 & 2 \\ 0 & 1 & 4 & -7 & -3 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

S-6:

Add $(-2 \times \text{row } 3)$ to row 1:

$$\begin{bmatrix} 1 & 2 & -3 & 4 & 0 \\ 0 & 1 & 4 & -7 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

S-7:

Add $(-2 \times \text{row } 2)$ to row 1

$$\begin{bmatrix} 1 & 0 & -11 & 18 & 0 \\ 0 & 1 & 4 & -7 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

② Here,

$$A = \begin{bmatrix} 5 & -7 & 1 \\ -7 & 8 & 2 \\ 1 & 2 & -4 \end{bmatrix}$$

Now,

$$A^2 + 2A + \text{tr}(A)I$$

$$A^2 =$$

$$\begin{pmatrix} 5 & -7 & 1 \\ -7 & 8 & 2 \\ 4 & 2 & 4 \end{pmatrix}$$

$$=$$

$$\begin{pmatrix} 75 & -89 & -5 \\ -89 & 117 & 17 \\ -5 & 17 & 21 \end{pmatrix}$$

$$2A =$$

$$\begin{pmatrix} 10 & -14 & 2 \\ -14 & 16 & 4 \\ 2 & 4 & 8 \end{pmatrix}$$

$$A^T =$$

$$\begin{pmatrix} 5 & -7 & 1 \\ -7 & 8 & 2 \\ 4 & 2 & 4 \end{pmatrix}$$

$$\text{tr}(A)I =$$

$$\begin{pmatrix} 5 & -7 & 1 \\ -7 & 8 & 2 \\ 4 & 2 & 4 \end{pmatrix}$$

$$= 25 + 2 + 17 = 44$$

$$\therefore A^2 + 2A + \text{tr}(A)I$$

$$= \begin{pmatrix} 75 & -89 & -5 \\ -89 & 107 & 17 \\ -5 & 17 & 21 \end{pmatrix} + \begin{pmatrix} 10 & -11 & 2 \\ -14 & 16 & 4 \\ 2 & 4 & 8 \end{pmatrix}$$

= Undefined.

$$\begin{pmatrix} 5 & -7 & 8 \\ -7 & 8 & 2 \\ 8 & 2 & 4 \end{pmatrix}$$

~~116 288~~

$$= \begin{pmatrix} 90 & -110 & -2 \\ -110 & 141 & 23 \\ -2 & 23 & 33 \end{pmatrix}$$

(Ans)