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Course: CSE 410

Quiz-04

Decision tree:

ID3 algorithm:

ID3 algorithm is one of the algorithm that uses in building decision tree.

ID3 algorithm selects the best feature at each step while building a decision tree. It selects the features with the highest or maximum gain.

Taking supplies as the attribute.

$$\text{Entropy} = -P + \log_2 P + \dots - P \log_2 P$$

~~$$= -\left[\frac{9}{19} \log_2 \left(\frac{9}{19}\right) + \frac{7}{19} \log_2 \left(\frac{7}{19}\right) + \frac{3}{19} \log_2 \left(\frac{3}{19}\right)\right]$$~~

Here, we will take log to base 2.
Here total 12 Yes/No.
out of which 4 Yes and 8 No.

$$\begin{aligned}\therefore E(S) &= - \left[\frac{4}{12} \log\left(\frac{4}{12}\right) + \left(\frac{8}{12} \log\left(\frac{8}{12}\right)\right) \right] \\ &= 0.1589 - 0.1165 \\ &= 0.0424\end{aligned}$$

Now, we calculate the average weighted entropy.

~~Here,~~ Here, we have 7 Yes and 5 No.

$$\begin{aligned}E(W) &= - \left[\frac{7}{12} \log\left(\frac{7}{12}\right) \right] + \left(\frac{5}{12} \log\left(\frac{5}{12}\right) \right) \\ &= 0.1367 - 0.1589 \\ &= -0.0217.\end{aligned}$$

$$\begin{aligned}\text{min}(\text{supply}, E) &= 0.0424 - \frac{8}{12} \log \frac{8}{12} - \\ &\quad - \frac{4}{12} \log \frac{4}{12} - \frac{8}{12} \log \frac{5}{12} \\ &= 0.4362\end{aligned}$$

$$\begin{aligned} \text{Gain}(\text{Weather}, E) &= 0.0924 - \frac{4}{12} \log \frac{4}{12} - \frac{6}{12} \log \frac{6}{12} \\ &\quad - \frac{4}{12} \log \frac{4}{12} \\ &= 0.5109 \end{aligned}$$

$$\begin{aligned} \text{Gain}(\text{Worked}, E) &= 0.0924 - \frac{7}{12} \log \frac{7}{12} - \frac{5}{12} \log \frac{5}{12} \\ &= 0.3374 \end{aligned}$$

$$\text{Gain}(\text{supply shopped}, E) = 0.0924$$

Decision tree:

