

$$1) n = 20$$

$$p_{de} = 1 - 75/100 \\ = 0.25.$$

(a) Binomial distribution.

$$P(X=x) = \binom{n}{x} p^x (1-p)^{n-x}$$

$$\therefore P(X=4) = \binom{20}{4} p^4 (1-p)^{20-4} \\ = \binom{20}{4} 0.25^4 \times 0.75^{16} \\ = 0.1897.$$

(b) not more than 3 patients.

$$P(X \leq 3) = P(X=0) + P(X=1) + P(X=2) + P(X=3) \\ = \binom{20}{0} \times 0.25^0 \times 0.75^{20} + \binom{20}{1} \times 0.25^1 \times 0.75^{19} \\ + \binom{20}{2} \times 0.25^2 \times 0.75^{18} + \binom{20}{3} \times 0.25^3 \times 0.75^{17} \\ = 3.17 \times 10^{-3} + 0.02114 + 0.067 + 0.1339 \\ = \cancel{0.4151} 0.22521$$

Answer

$$2) X \sim N(0, 1)$$

$$E(X) = \mu = 0$$

$$V(X) = \sigma^2 = 1.$$

$$\therefore \sigma = 1.$$

$$\text{Now, } P(X > -1)$$

$$= P(-1 < X < \infty)$$

$$= P\left(\frac{-1 - \mu}{\sigma} < \frac{X - \mu}{\sigma} < \frac{\infty - \mu}{\sigma}\right)$$

$$= P\left(\frac{-1 - 0}{1} < Z < \infty\right)$$

$$= F(\infty) - F(-1)$$

$$= 1 - F(-1)$$

$$= 1 - 0.1587$$

$$= 0.8413 \quad \text{Answer}$$

Figure

