



## Assignment 1

Department of Electrical & Computer Engineering

North South University

*Submitted By*

**Name:** Mohammed Mahmudur Rahman

**Student ID:** 1520386043

**Course:** Electrical Circuits (EEE141)

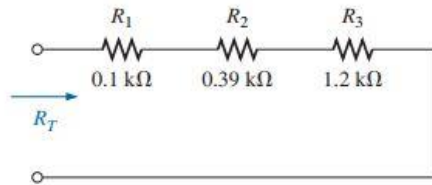
**Section:** 05

*Faculty Advisor*

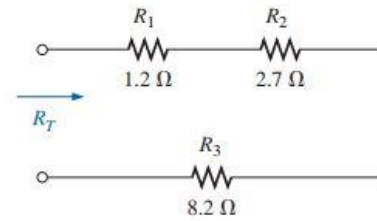
Syeda Sarita Hassan (SSH1)

## Question 5.2 (2)

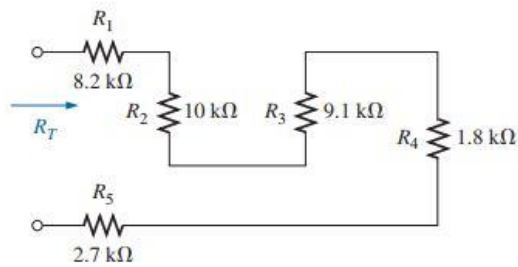
2. Find the total resistance  $R_T$  for each configuration in Fig. 5.86. Note that only standard resistor values were used.



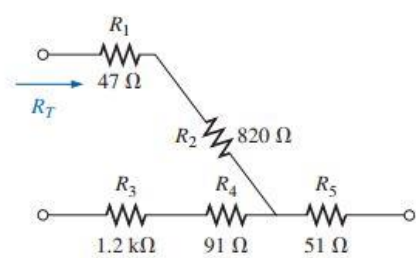
(a)



(b)



(c)



(d)

EEE141: (5.2, 5.3, 5.4, 5.5, 5.6, 5.7, 5.9)

5.2(2)

(a) ~~and~~ ~~the~~  $R_T = 1.69 \text{ k}\Omega$

(a) As it's a series circuit,

So total resistance,  $R_T = R_1 + R_2 + R_3$ .

$$= (0.1 + 0.39 + 1.2) \text{ k}\Omega$$

$$= 1.69 \text{ k}\Omega$$

(b) Since it's series circuit,

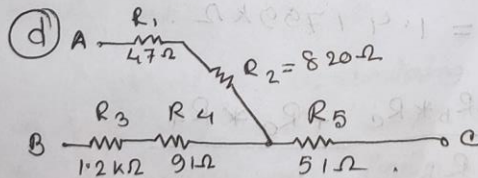
$$\text{So, } R_T = R_1 + R_2 + R_3 = (1.2 + 2.7 + 8.2) \Omega = 12.1 \Omega$$

(c) Since it's a series circuit,

$$\text{So, } R_T = R_1 + R_2 + R_3 + R_4 + R_5$$

$$= (8.2 + 10 + 0.1 + 1.8 + 2.7) \text{ k}\Omega$$

$$= 31.8 \text{ k}\Omega$$



Here,  $R_1, R_2$  are in series,

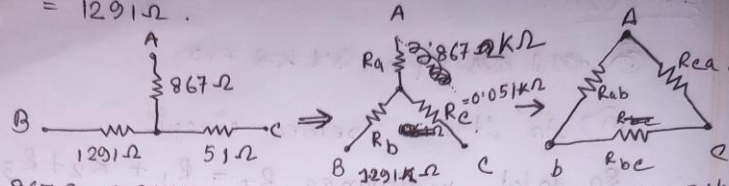
$$\text{So, } R_{12} = R_1 + R_2 = (47 + 820) \Omega = 867 \Omega$$

Again,  $R_3, R_4$  are in series,

$$\therefore R_{34} = 1.2 \text{ k}\Omega + 91 \Omega = 1.291 \text{ k}\Omega$$

$$\Rightarrow R_{34} = (1.2 \times 10^3) \Omega + 91 \Omega.$$

$$= 1291 \Omega.$$



$$R_a = 867 \Omega = 0.867 \text{ k}\Omega ; R_b = 1291 \Omega = 1.291 \text{ k}\Omega ; R_c = 0.051 \text{ k}\Omega$$

$$\text{Here, } R_{ab} = \frac{R_a \cdot R_b + R_b \cdot R_c + R_c \cdot R_a}{R_c}$$

$$= \frac{(0.867 \times 1.291) + (1.291 \times 0.051) + (0.051 \times 0.867)}{0.051}$$

$$= \frac{1.2294}{0.051} \text{ k}\Omega = 24.105 \text{ k}\Omega.$$

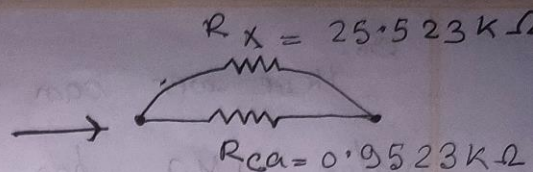
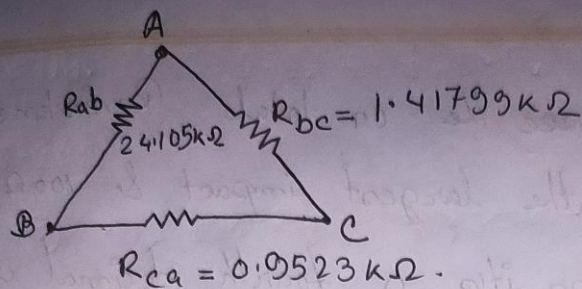
$$R_{bc} = \frac{R_a \cdot R_b + R_b \cdot R_c + R_c \cdot R_a}{R_a}$$

$$= \frac{1.2294}{0.867} = 1.41799 \text{ k}\Omega.$$

$$R_{ca} = \frac{R_a \cdot R_b + R_b \cdot R_c + R_c \cdot R_a}{R_b}$$

$$= \frac{1.2294}{1.291} = 0.9523 \text{ k}\Omega.$$

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Here,  $R_{ab}$ ,  $R_{bc}$  are in series.

$$\text{So, } R_{(ab+bc)} = R_x = (24.105 \text{ k}\Omega + 1.41799 \text{ k}\Omega) \\ = 25.52299 \text{ k}\Omega$$

Again,  $R_x$ ,  $R_{ca}$  are in parallel.

$$\text{So, } R_{x||ca} = \frac{R_x R_{ca}}{R_x + R_{ca}} = \frac{(25.523 \times 0.9523)}{25.523 + 0.9523} \text{ k}\Omega \\ = 0.918 \text{ k}\Omega$$



## Question NO: 5.2 (4)

4. For the circuit in Fig. 5.88, composed of standard values:
- Which resistor will have the most impact on the total resistance?
  - On an approximate basis, which resistors can be ignored when determining the total resistance?
  - Find the total resistance, and comment on your results for parts (a) and (b).

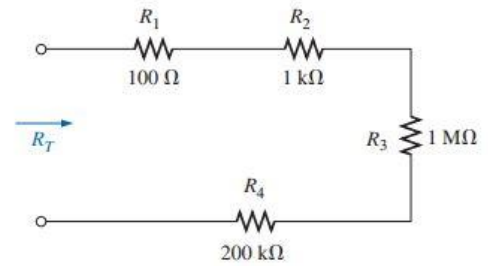


FIG. 5.88

$= 0.918\ \text{k}\Omega$

5.2 (4)

(a) Here,  $R_3$  has the most impact on the total resistance.

(b) When determining total resistance,  $R_1$  can be ignored on an approximate basis.

(c) As it's a series circuit,

$$\text{So, } R_T = R_1 + R_2 + R_3 + R_4 = 100 \times 10^{-6}\ \Omega + 1\ \text{k}\Omega + 1\ \text{M}\Omega + 200\ \text{k}\Omega$$

$$= 100 \times 10^{-6}\ \text{M}\Omega + 1 \times 10^{-3}\ \text{M}\Omega + 1\ \text{M}\Omega + 200 \times 10^{-3}\ \text{M}\Omega$$

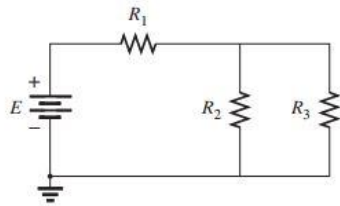
$$= 1.2011\ \text{M}\Omega$$

So, Here we can see the on total Resistance value  $1\ \text{M}\Omega$  has the largest impact &  $100\ \Omega$  has the least impact as it's a fourth decimal value.

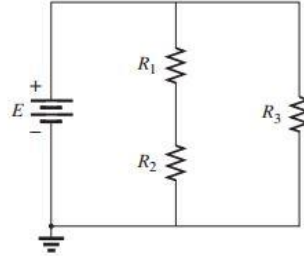
## Question 5.2 (1)

1. For each configuration in Fig. 5.85, find the individual (not combinations of) elements (voltage sources and/or resistors) that are in series. If necessary, use the fact that elements in

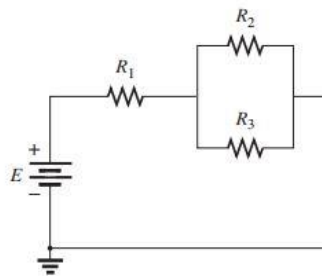
series have the same current. Simply list those that satisfy the conditions for a series relationship. We will learn more about other combinations later.



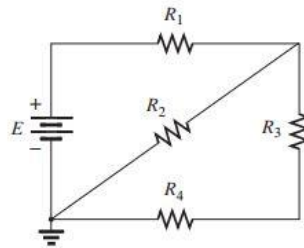
(a)



(b)

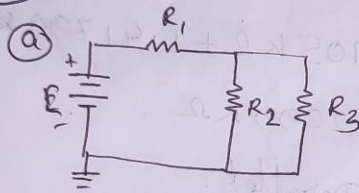


(c)

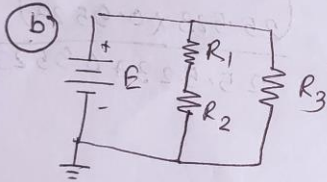


(d)

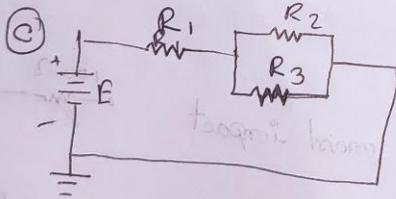
5.2(1)



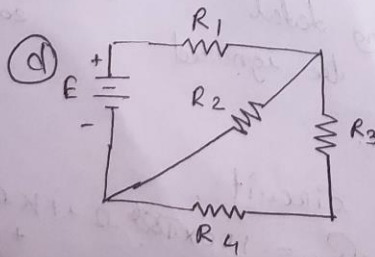
Here,  $E$  &  $R_1$  are in series.



Here,  $R_1$  &  $R_2$  are in series.



Here  $E$  &  $R_1$  are in series.



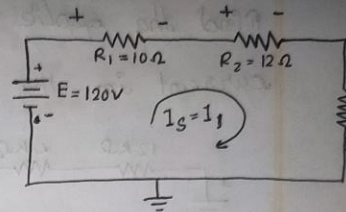
Here,  $E$ ,  $R_1$  are in series  
Again  $R_2$ ,  $R_4$  are in series.



5.3(7)

For the series configuration, find

- a) Total resistance.
- b) Total current.
- c) Voltage across each resistive elements



a) Here, Total Resistance,  $R_T = (10 + 12 + 18) \Omega = 40 \Omega$ .

b) As per Ohm's law, Current,  $I_s = \frac{E}{R_T} = \frac{120}{40} \text{ A} = 3 \text{ A}$ .

c) ~~App~~ Applying Ohm's law in each resistive elements we can obtain voltage across each of them.

$$\text{So, } V_{R_1} = I_1 R_1 = [(3 \text{ A})(10 \Omega)] \text{ V} = 30 \text{ V}$$

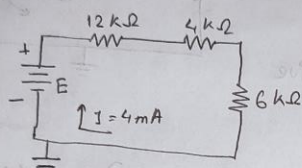
$$V_{R_2} = I_1 R_2 = [3 \text{ A} \times 12 \Omega] \text{ V} = 36 \text{ V}$$

$$V_{R_3} = I_1 R_3 = [18 \Omega \times 3 \text{ A}] = 54 \text{ V}$$

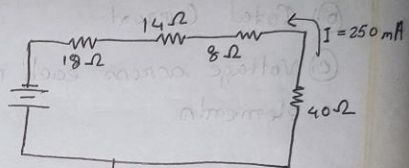
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5.3 (a)

Find the applied voltage necessary to develop the specified current in the following figures.



(a)



(b)

For figure (a), Total resistance,  $R_T = (12 + 4 + 6)\text{ k}\Omega$   
 $= 22\text{ k}\Omega$

From Ohm's law we can obtain required voltage  $E$ .

Here,  $E = I R_T = [4 \times 10^{-3}\text{ A} \times (22 \times 10^3)\text{ }\Omega] \text{ V}$   
 $= 88\text{ V}$

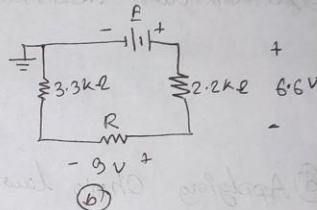
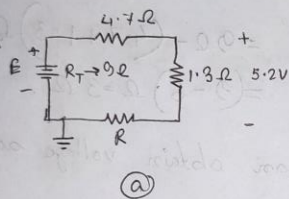
For figure (b) Total Resistance,  $R_T = (18 + 14 + 8 + 40)\text{ }\Omega$   
 $= 80\text{ }\Omega$

Here,  $E = I R_T = (250 \times 10^{-3})\text{ A} \times 80\text{ }\Omega = 20\text{ V}$

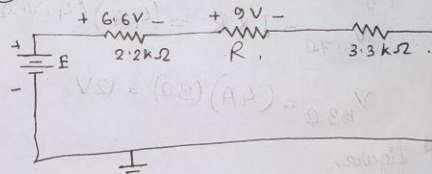
5.3 (10)

For each network in figure, determine:

- The current,  $I$ .
- The source Voltage,  $E$ .
- The unknown resistance.
- Voltage across each element.



Here, figure (b) can be drawn as:



a) for figure (a) current,  $I = \frac{V_R}{R} = \frac{5.2V}{1.3k\Omega} = 4A$ .

& for figure (b) current,  $I = \frac{V_R}{R} = \frac{6.6V}{2.2k\Omega} = \frac{6.6V}{2.2 \times 10^3 \Omega} = 3 \times 10^{-3} A$ .

b) for 1st figure,  $E = \frac{I}{R_T} = \frac{4A}{9k\Omega} \cdot R_T = (4 \times 9)V = 36V$ .

for 2nd figure, unknown Voltage Resistance,  $R = \frac{V_{unk}}{I} = \frac{9}{3 \times 10^{-3}} = 3000 \Omega = 3k\Omega$ .

$$\text{So, } R_T = 2.2 \text{ k}\Omega + 3 \text{ k}\Omega + 3.3 \text{ k}\Omega \\ = 8.5 \text{ k}\Omega$$

$$\text{So, } E = I \times R_T = (3 \times 10^{-3}) \times (8.5 \times 10^3) \text{ V} \\ = 25.5 \text{ V}$$

② Unknown Resistance,  $R_{\text{th}} = R_T - (R_1 + R_2)$

$$= 9 \Omega - (4.7 + 1.3) \Omega \\ = (9 - 6) \Omega = 3 \Omega$$

③ Applying Ohm's law we can obtain voltage across each element.

for 1st figure,

$$V_{4.7\Omega} = I \times R = (4 \text{ A}) (4.7 \Omega) = 18.8 \text{ V}$$

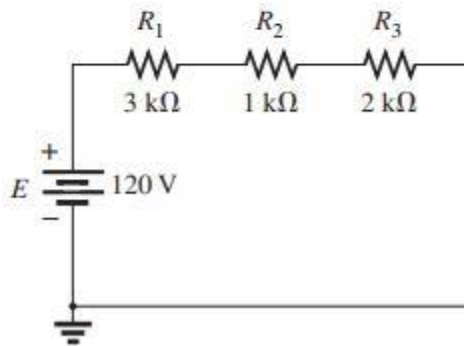
$$V_{3\Omega} = (4 \text{ A}) (3 \Omega) = 12 \text{ V}$$

for 2nd figure,

$$V_{3.3\text{k}\Omega} = I \times R = (3 \times 10^{-3} \text{ A}) \times (3.3 \times 10^3 \Omega) \\ = 9.9 \text{ V}$$

## Question 5.4 (12)

12. For the circuit in Fig. 5.96, constructed of standard value resistors:
- Find the total resistance, current, and voltage across each element.
  - Find the power delivered to each resistor.
  - Calculate the total power delivered to all the resistors.
  - Find the power delivered by the source.
  - How does the power delivered by the source compare to that delivered to all the resistors?
  - Which resistor received the most power? Why?
  - What happened to all the power delivered to the resistors?
  - If the resistors are available with wattage ratings of  $\frac{1}{2}$  W, 1 W, 2 W, and 5 W, what minimum wattage rating can be used for each resistor?



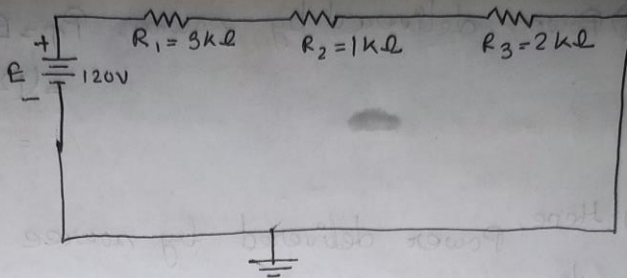
**FIG. 5.96**

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(9)

5.4 (12)



(a) Here, Total resistance,  $R_T = (3 + 1 + 2) \text{ k}\Omega$   
 $= 6 \text{ k}\Omega$ .

Total current,  

$$I_S = \frac{E}{R_T} = \frac{120 \text{ V}}{6 \text{ k}\Omega} = 20 \text{ mA}$$

Voltage across each element is,

$$V_{R_1} = (20 \text{ mA})(3 \text{ k}\Omega) = 60 \text{ V}$$

$$V_{R_2} = (I \cdot R_2) = (20 \text{ mA})(1 \text{ k}\Omega) = 20 \text{ V}$$

$$V_{R_3} = (I \cdot R_3) = (20 \text{ mA})(2 \text{ k}\Omega) = 40 \text{ V}$$

(b) As per law,

Power across a element,  $P = I^2 R$ .

So,

$$P_{R_1} = I_1^2 R_1 = (20 \text{ mA})^2 (3 \text{ k}\Omega) = 1.2 \text{ W}$$

$$P_{R_2} = I_2^2 R_2 = (20 \text{ mA})^2 (1 \text{ k}\Omega) = 0.4 \text{ W}$$

$$P_{R_3} = I_3^2 R_3 = (20 \text{ mA})^2 (2 \text{ k}\Omega) = 0.8 \text{ W}$$

Total Power delivered by source,  $P_T = P_{R_1} + P_{R_2} + P_{R_3}$   
 $= 1.2 \text{ W} + 0.4 \text{ W} + 0.8 \text{ W} = 2.4 \text{ W}$

① Power delivered by source,  $P_T = E \cdot I_s$   
 $= (120V)(20mA)$   
 $= 2.4W$

② Here, Power delivered by source = Power delivered to resistors =  $2.4W$ .

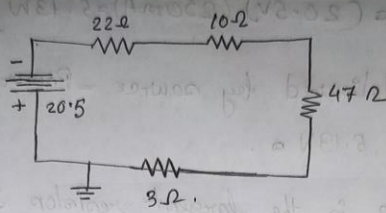
③ Resistor  $R_1$  received the most power. As it has the highest resistance therefore it consumed most power.

④ Power delivered to resistors are dissipated.

⑤ If the resistors are available with wattage ratings of  $0.5W$ ,  $1W$ ,  $2W$  &  $5W$ ,

minimum wattage ratings for each resistor would be,  $R_1 = 2W$ ,  $R_2 = 0.5W$ ,  $R_3 = 1W$ .

Q 5.4 (13)



(a) Total Resistance,  $R_T = (22 + 10 + 47 + 3)\Omega = 82\Omega$ .

Current,  $I_S = \frac{E}{R_T} = \frac{20.5V}{82\Omega} = 250mA$ .

Voltage across each element:

$$V_{R_1} = I_1 R_1 = (250mA)(22\Omega) = 5.5V$$

$$V_{R_2} = I_2 R_2 = (250mA)(10\Omega) = 2.5V$$

$$V_{R_3} = I_3 R_3 = (250mA)(47\Omega) = 11.75V$$

$$V_{R_4} = I_4 R_4 = (250mA)(3\Omega) = 0.75V$$

(b)  $P_{R_1} = I_1^2 R_1 = (250mA)^2 \cdot 22\Omega = 1.38W$

$$P_{R_2} = I_2^2 R_2 = (250mA)^2 (10\Omega) = 625mW$$

$$P_{R_3} = I_3^2 R_3 = (250mA)^2 (47\Omega) = 2.94W$$

$$P_{R_4} = I_4^2 R_4 = (250mA)^2 (3\Omega) = 187.5mW$$

(c)  $P_T = P_{R_1} + P_{R_2} + P_{R_3} + P_{R_4} = 1.38W + 625mW + 2.94W + 187.5mW$   
 $= 5.13W$



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d)  $P = EI_S = (20.5V)(250mA) = 5.13W$

e) Power delivered by source = Power received by resistor = 5.13W

f) A 47Ω is the largest resistor it received the most power

g) Power delivered to resistor are dissipated.

h) If the resistors are available with wattage rating of 1/2 W, 1 W, 2 W & 5 W minimum wattage for each resistor would be:

$R_1 \rightarrow 2W$

$R_2 \rightarrow 1/2 W$

$R_3 \rightarrow 5W$

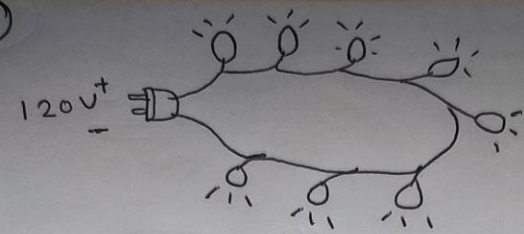
$R_4 \rightarrow 1/2 W$

### **Question No 5.4 (15)**

- 15.** Eight holiday lights are connected in series as shown in Fig. 5.99.
- a.** If the set is connected to a 120 V source, what is the current through the bulbs if each bulb has an internal resistance of  $28\frac{1}{2} \Omega$ ?
  - b.** Determine the power delivered to each bulb.
  - c.** Calculate the voltage drop across each bulb.
  - d.** If one bulb burns out (that is, the filament opens), what is the effect on the remaining bulbs? Why?



5.4 (15)



(a) Here, Total resistance,  $R_T = NR_1 = 8 \left( 28 \frac{1}{8} \Omega \right) = 225 \Omega$ .

So, current,  $I = E/R_T = 120V/225\Omega = 0.53A$ .

(b) Here,  $P = I^2 R = \left( \frac{8}{15} \right) (0.53)^2 \left( 28 \frac{1}{8} \right) = 8W$ .

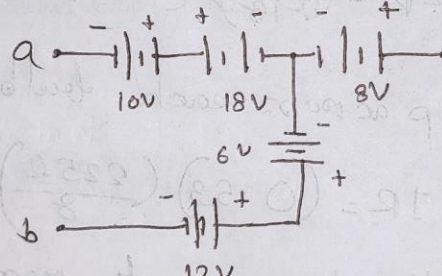
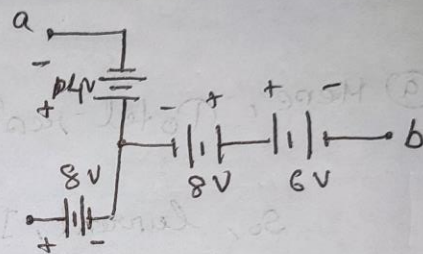
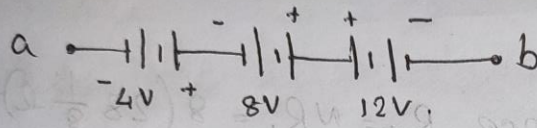
(c) Voltage drop across each bulb,

$$V = IR = (0.53) \left( \frac{225\Omega}{8} \right) = 15V.$$

(d) If one bulb burns out remaining bulbs will be turned off as the circuit would be opened in place of burned bulb.

5.5 (17)

Combine the series voltage source into a single voltage source between points a & b.



for figure (a),

$$V_{ab} = -4V - 8V + 12V = 0V$$

for figure (b)

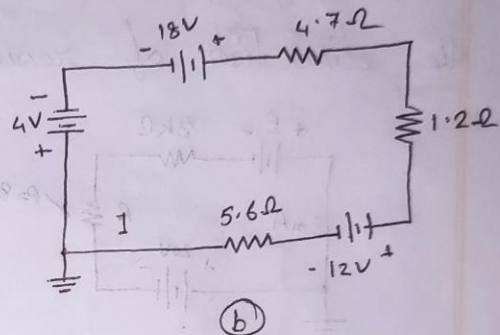
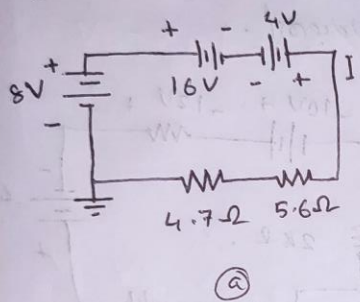
$$V_{ab} = -4V - 8V + 6V = -6V$$

for figure (c)

$$V_{ab} = -10V + 18V - 6V + 12V = 14V$$

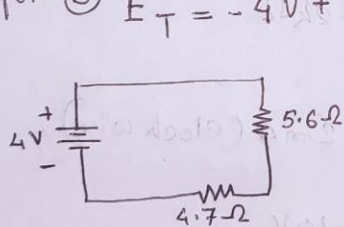
5.5(18)

Determine the current  $I$  & its direction for following figure. Before solving for  $I$ , redraw each figure with a single voltage source.

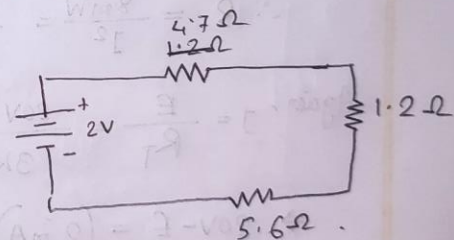


for (a)  $E_T = 16V - 4V - 8V = 4V$ .

& for (b)  $E_T = -4V + 18V - 12V = 2V$ .



a redrawn



b redrawn

for (a) redrawn,  $R_T = 5.6 + 4.7 = 10.3\Omega$ .

so,  $I = \frac{4V}{10.3\Omega} = 388.35 \text{ mA}$  (counter clockwise)

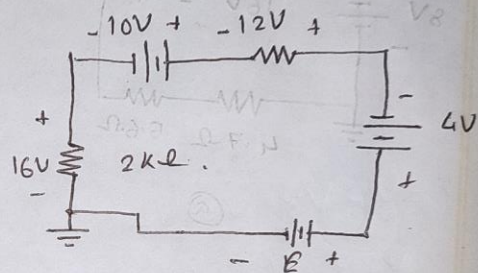
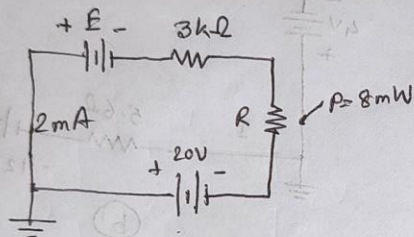
for (b) redrawn,  $R_T = (4.7 + 1.2 + 5.6) = 11.5\Omega$ .

so,  $I = \frac{2V}{11.5\Omega} = 173.91 \text{ mA}$  (clockwise)



5.5 (19)

Find the unknown voltage source & resistor for the networks in following figures. First, combine series voltage sources into a single source. Indicate the direction of resulting current.



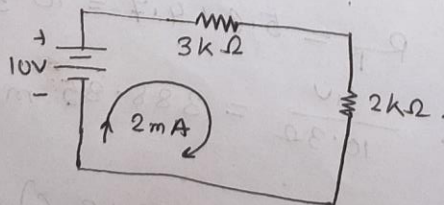
② Here,  $P = 8 \text{ mW} = I^2 R$ ,

$$\therefore R = \frac{8 \text{ mW}}{I^2} = \frac{8 \text{ mW}}{(2 \text{ mA})^2} = 2 \text{ k}\Omega$$

Again,  $I = \frac{E}{R_T} = \frac{20\text{V} - E}{3\text{k}\Omega + 2\text{k}\Omega} = 2 \text{ mA (clockwise)}$

$$\Rightarrow 20\text{V} - E = (2 \text{ mA})(5\text{k}\Omega) = 10\text{V}$$

$$\therefore E = 20\text{V} - 10\text{V} = 10\text{V}$$



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⑤ Here,

$$I = \frac{16V}{2k\Omega} = 8mA$$

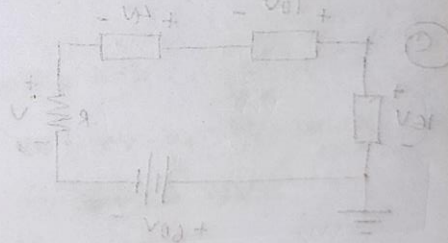
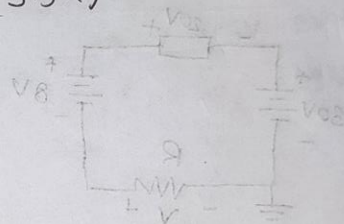
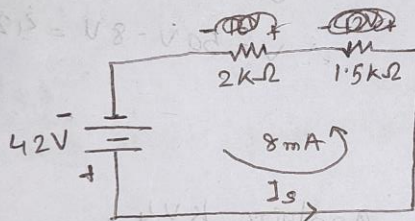
$$R = \frac{V}{I} = \frac{12V}{8mA} = 1.5k\Omega$$

$$I_s = \frac{E}{R_T} = \frac{E - 4 - 10V}{2k\Omega + 1.5k\Omega} = \frac{E - 14V}{3.5k\Omega} = 8mA$$

(Counter Clock wise).

$$\therefore E - 14 = (8mA)(3.5k\Omega)$$

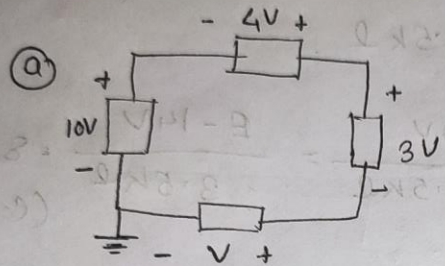
$$0 = V - V_8 \therefore E = 42V$$





5.6 (20)

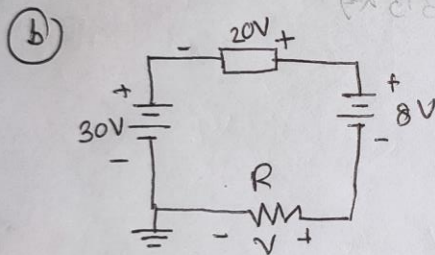
Using Kirchhoff's voltage law, find the unknown voltage.



Here, applying KVL,

$$+10V + 4V - 3V - V = 0$$

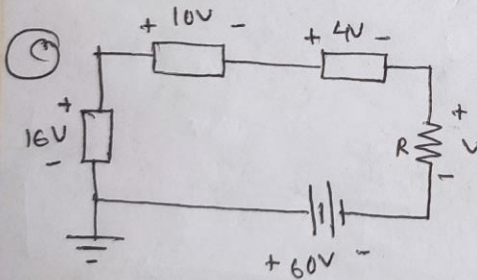
$$\therefore V = 14V - 3V = 11V$$



applying KVL,

$$+30V + 20V - 8V - V = 0$$

$$\therefore V = 50V - 8V = 42V$$



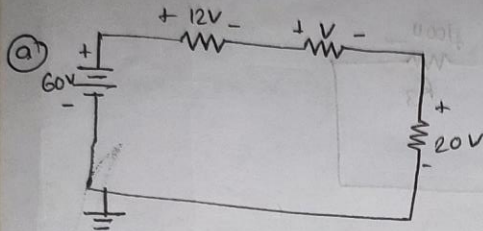
Applying KVL,

$$+16V - 10V - 4V - V + 60V = 0$$

$$\therefore V = 76V - 14V = 62V$$

5.6(21)

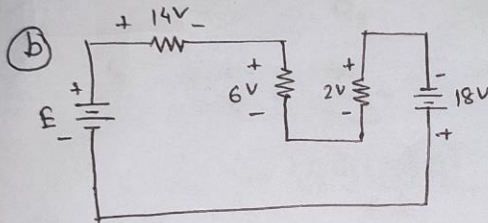
Using KVL, find the unknown voltage.



Applying KVL,

$$+60V - 12V - V - 20V = 0$$

$$\therefore V = 60V - 32V = 28V$$



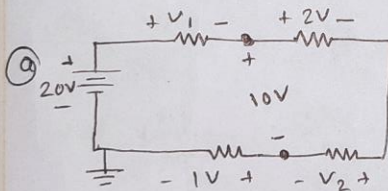
Applying KVL,

$$+E - 14V - 6V - 2V + 18V = 0$$

$$\therefore E = 22V - 18V = 4V$$

5.6(23)

Using KVL, find the unknown voltage.



Applying KVL,

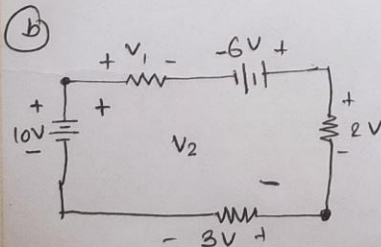
$$+20V - V_1 - 2V - 10V = 0$$

$$\therefore V_1 = 9V$$

Again,

$$+10V - 2V - V_2 = 0$$

$$\therefore V_2 = 8V$$



Applying KVL,

$$+10V - V_1 + 6V - 2V - 3V = 0$$

$$\therefore V_1 = 11V$$

Again,

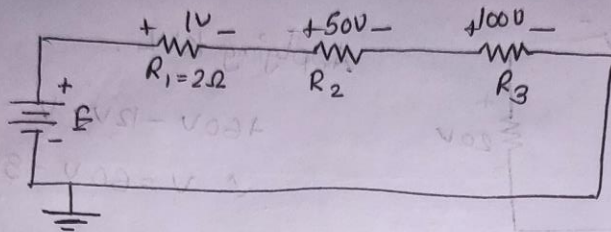
$$+10V - V_2 - 3V = 0$$

$$\therefore V_2 = 7V$$



5.7 (24)

Determine the values of unknown resistors.



Here,  $\frac{V_1}{R_1} = \frac{V_2}{R_2}$

$$\Rightarrow \frac{1V}{2\Omega} = \frac{50V}{R_2}$$

$$\therefore R_2 = \frac{(50V)(2\Omega)}{1V} = 100\Omega$$

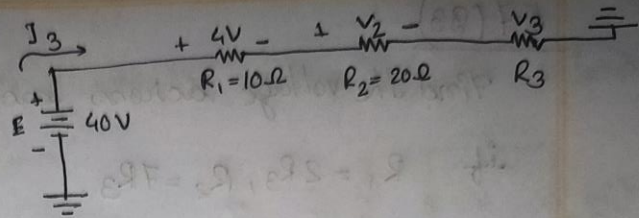
Again,  $\frac{V_1}{R_1} = \frac{V_3}{R_3}$

$$\Rightarrow \frac{1V}{2\Omega} = \frac{100V}{R_3}$$

$$\therefore R_3 = \frac{(100V)(2\Omega)}{1V} = 200\Omega$$

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5.7 (30)



- (a) Determine  $V_2$ .
- (b) Calculate  $V_3$ .
- (c) Determine  $R_3$ .

(a) Here,

$$\frac{V_1}{R_1} = \frac{V_2}{R_2}$$

$$\Rightarrow \frac{4V}{10\Omega} = \frac{V_2}{20\Omega}$$

$$\therefore V_2 = \frac{(4V)(20\Omega)}{10\Omega} = 8V$$

(b) Here,

$$V_3 = E - V_1 - V_2 = 40V - 4V - 8V = 28V$$

(c)

$$\frac{V_1}{R_1} = \frac{V_3}{R_3}$$

$$\Rightarrow \frac{4V}{10\Omega} = \frac{28V}{R_3}$$

$$\Rightarrow R_3 = \frac{(28V)(10\Omega)}{4V} = 70\Omega$$

5.7 (33)

Find the voltage across each resistor.

if  $R_1 = 2R_3$ ,  $R_2 = 7R_3$ .

Here, Total Resistance,  $R_T = R_1 + R_2 + R_3$   
 $= 2R_3 + 7R_3 + R_3$   
 $= 10R_3$ .

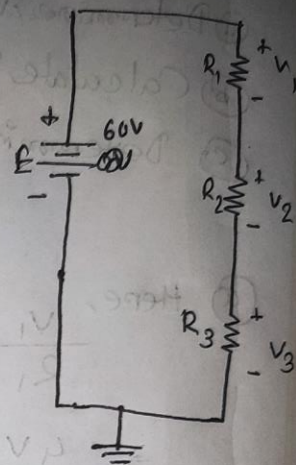
Again,

$$\frac{V_{R_3}}{R_3} = \frac{V_{total}}{R_{total}}$$

$$= V_{R_3} = \frac{V_{total}}{R_{total}} \times R_3 = \frac{60V}{10R_3} (R_3) = 6V.$$

$$V_{R_1} = 2V_{R_3} = 2(6V) = 12V.$$

$$V_{R_2} = 7V_{R_3} = 7(6V) = 42V.$$





5.9 (36)

Determine current  $I$  (with direction) & voltage  $V$  (with polarity) for the following figure.

for figure (a).



$$\text{Here, } V = 80V - 26V = 54V.$$

$$\& R_T = 6\Omega + 3\Omega = 9\Omega.$$

$$\therefore I = \frac{54V}{9\Omega} = 6A. \& V = IR = (6A)(3\Omega) = 18V$$

The direction would be Clockwise

as  $80V > 26V$ .

for figure (b).

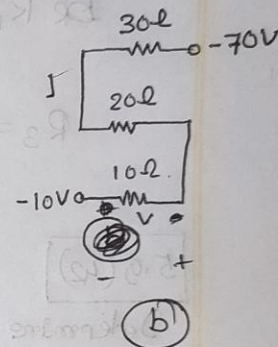
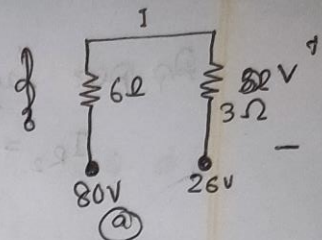
$$E = +70V - 10V = 60V.$$

$$R_T = 10\Omega + 20\Omega + 30\Omega = 60\Omega.$$

$$I = \frac{E}{R_T} = \frac{60V}{60\Omega} = 1A.$$

Direction is clock-wise

$$\text{Again, } V = IR = (1A)(10\Omega) = 10V.$$



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5.9 (39)

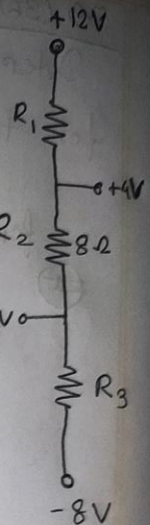
Find the level of Resistance  $R_1$  &  $R_3$

As per law,

$$I_{R_2} = \frac{V_{R_1} - V_{R_2}}{R_2} = \frac{4 - (-4)}{8\Omega} = \frac{8V}{8\Omega} = 1A$$

$$R_1 = \frac{V_{R_1}}{I} = \frac{12V - 4V}{1A} = \frac{8V}{1A} = 8\Omega$$

$$R_3 = \frac{V_{R_3}}{I} = \frac{8V - 4V}{1A} = \frac{4V}{1A} = 4\Omega$$



5.9 (42)

Determine  $V_0, V_4, V_7, V_{10}, V_{23}, V_{30}$

$V_{67}, V_{56}$  and  $I$  (magnitude & direction)

Here,  $V_0 = 0V$  (ground)

$$V_4 = -V_1 = -2V$$

$$= -(6mA \times 2k\Omega) = -12V$$

$$= -12V + 2V$$

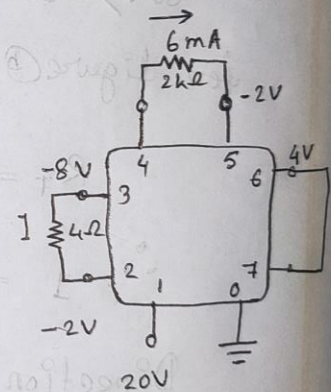
$$= -10V$$

$$V_7 = 4V$$

$$V_{10} = 20V - 0V = 20V$$

$$V_{23} = -2V + 8V = 6V$$

$$V_{30} = -8V - 0V = -8V$$



25.

$$V_{67} = 4V - 0V = 4V$$

$$V_{56} = -2V - 4V = -6V.$$

$$\text{Here, current, } I = \frac{V_{23}}{4\Omega} = \frac{6V}{4\Omega} = 1.5A$$

& the direction is clock-wise (↑).

