Homework 1 Due Date: Sunday, 10 March 2024

- 1) i) Write down the state space equations (differential equations) for the following robots. For each robot identify the state variables and the control variables.
 - a) Unicycle model
 - b) Differential drive robot
 - c) Simplified car model
 - ii) For a given robot, what do the state variables and control variables represent? Please explain.
 - iii) Describe the differences in dynamics between these robot models.
- 2) Simulate the differential equations for the unicycle robot model using Euler's method for $t \in [0, 10]$ and time step $\Delta t = 0.1$. Use the following control input:

$$w = 1 \quad 0 \le t \le 10$$

$$\omega = \begin{cases} 3 & 0.5 \le t \le 1.5 \\ -3 & 2 \le t \le 3 \\ -3 & 4 \le t \le 5 \\ 3 & 6 \le t \le 7 \\ -3 & 8 \le t \le 9 \end{cases}$$

With initial conditions x(0) = 0, y(0) = 0, $\theta(0) = 1$.

- a) Plot x vs y, x vs t, y vs t and θ vs t. Submit your code and plots.
- b) If you plot x vs y for each time step, you'll create a movie of the robot moving in 2D space.

Feel free to simulate different initial conditions and control input sequences to gain a greater understanding.

3) Simulate the state space equations for the differential drive robot model using Euler's method for t $\in [0, 10]$ and time step $\Delta t = 0.1$. Use the following control input:

$$\omega_l = \begin{cases} 12 & 4 \leq t \leq 6 \\ 12 & 6 \leq t \leq 8 \\ 1 & all \ other \ t \end{cases} \quad \omega_r = \begin{cases} 12 & 0.5 \leq t \leq 1.5 \\ 12 & 2 \leq t \leq 4 \\ 1 & all \ other \ t \end{cases}$$

With r = 0.1, L = 1 and initial conditions x(0) = 0, y(0) = 0, $\theta(0) = 1$.

- a) Plot x vs y, x vs t, y vs t and θ vs t. Submit your code and plots.
- b) If you plot x vs y for each time step, you'll create a movie of the robot moving in 2D space.

Feel free to simulate different initial conditions and control input sequences to gain a greater understanding.