

Question one

A-  $H_0: \mu_1 = \mu_2 = \mu_3 = \mu_4$

$H_a$ : at least one two of the mean are not equal

Source	SS	df	MS	$F_{comp}$
Treatment	$SSA = 13939$	$k-1 = 3$	$S_1^2 = 13939/3$	$F = \frac{S_1^2}{S^2} = 3.56$
Error	$SSE = 53376$	$N-k = 41$	$S^2 = 53376/41$	

~~Total~~  $F_{table} \Rightarrow (\alpha, k-1, N-k) F(0.05, 3, 41) = 2.84$

Reject  $H_0$

B-

$$b_k(\alpha; n_i) = \frac{1}{N} [n_1 b_k(\alpha; n_1) + \dots + n_k b_k(\alpha; n_k)]$$

$$= \frac{1}{45} [20 * 0.858 + 9 * 0.689 + 9 * 0.689 + 7 * 0.704]$$

$b_4 = 0.75$

~~$SP^2 = \frac{1}{N-k} \sum (n_i - 1) S_i^2$~~

$$SP^2 = \frac{1}{N-k} \sum_{i=1}^k (n_i - 1) S_i^2 = \frac{1}{41} [19 * 662.862 + 8 * 2219.781 + 8 * 2168.434 + 6 * 946.032]$$

$SP^2 = 1301.86$

$$b_{comp} = \frac{1}{SP^2} \left[ (S_1^2)^{n_1-1} + \dots + (S_k^2)^{n_k-1} \right]^{\frac{1}{N-k}}$$

$$= \frac{1}{1301.86} \left[ (662.862)^{19} + (2219.781)^8 + (2168.434)^8 + (946.032)^6 \right]^{\frac{1}{41}}$$

$= 0.85$

accept  $H_0$

Question two

هو هو سؤال الثاني في 2018

Question three

هو هو سؤال الثالث في 2018

Mustafa Abdelkarem Destr



Question one

A- ①  $H_0: \mu_1 = \mu_2 = \mu_3 = \mu_4$

$H_a$ : at least two of the means are not equal

②  $K = 4$   $n = 6$

Source of variation	sum of square	df	Meansquare	$F_{comp}$
treatment	SSA	$K-1$	$S_1^2 = \frac{SSA}{K-1}$	$F = \frac{S_1^2}{S^2}$
Error	SSE	$K(n-1)$	$S^2 = \frac{SSE}{K(n-1)}$	
total	SST	$Kn-1$		
SSA = 745	SSE = 2200	$K-1 = 3$	$K(n-1) = 20$	

$S_1^2 = \frac{745}{3} = 248.33$   $S^2 = \frac{2200}{20} = 110$   $F_{comp} = \frac{248.33}{110} = 2.2575$

$F_{table}(\alpha, K-1, K(n-1)) = F(0.05, 3, 20) = 3.10$   $F_{comp} < F_{table}$   
accept  $H_0$

B- ①  $H_0: \sigma_1^2 = \sigma_2^2 = \sigma_3^2 = \sigma_4^2$

$H_a$ : all variances are not equal

②  $K = 4$   $n = 6$   $N = 6 \times 4 = 24$

$b_K(\alpha; n_1, n_4) = \frac{1}{N} [n_1 b_K(\alpha; n_1) + \dots + n_K b_K(\alpha, n_K)]$

$= \frac{1}{24} [4 * n_K b_K(\alpha, n_K)] = \frac{1}{24} [4 * n_4 b_4(0.05; n_4)]$   
 $= 0.6559$   $4 * 6 * 0.6559$

$SP^2 = \frac{1}{N-K} \sum_{i=1}^K (n_i - 1) S_i^2$

$= \frac{1}{24-4} \sum_{i=1}^4 (n_i - 1) S_i^2 = \frac{1}{20} [(n_1 - 1) S_1^2 + (n_2 - 1) S_2^2 + (n_3 - 1) S_3^2 + (n_4 - 1) S_4^2]$

$= \frac{1}{20} [5 * 12.62 + 5 * 2.66 + 5 * 7.915 + 5 * 10.63] = 8.45625$

$b_{comp} = \frac{1}{SP^2} \left[ (S_1^2)^{n_1-1} * \dots * (S_K^2)^{n_K-1} \right]^{\frac{1}{N-K}} = \frac{1}{8.45625} \left[ (12.62)^5 * (2.66)^5 * (7.915)^5 * (10.63)^5 \right]^{\frac{1}{20}}$   
 $= 0.8620$

$b_{comp} > b_{table}$  accept  $H_0$

Question 20

A.  $\bar{y}_0 = 51.44$   $\bar{y}_1 = 53.5$   $\bar{y}_2 = 54.04$   $\bar{y}_3 = 49.38$

①  $H_0: \mu_0 = \mu_i$   $H_a: \mu_0 \neq \mu_i$

②  $|d_i| = \frac{\bar{y}_i - \bar{y}_0}{\sqrt{\frac{2s^2}{n}}}$

$d_1 = \frac{\bar{y}_1 - \bar{y}_0}{Q} = \frac{53.5 - 51.44}{1.6725 \cdot 0.9593} = 1.92$

$d_2 = \frac{\bar{y}_2 - \bar{y}_0}{Q} = \frac{54.04 - 51.44}{1.6725 \cdot 0.9593} = 2.71$

$Q = \sqrt{\frac{2s^2}{n}} = \sqrt{\frac{2 \cdot 2.3007}{5}}$

$= 1.6725 \cdot 0.9593$   $d_3 = \frac{\bar{y}_3 - \bar{y}_0}{Q} = \frac{49.38 - 51.44}{1.6725 \cdot 0.9593} = -2.14$

$v = k(n-1)$

$d_{table}(\frac{\alpha}{2}, k, v) = d(0.05, 3, 16) = 2.59$

$d_1, d_3 < d_{table}$  accept  $H_0$   $d_2 > d_{table}$  reject  $H_0$

B.  $H_0: \mu_1 = \mu_2 = \mu_3 = \mu_4 = \mu_5 = \mu_6$

$H_a: \text{The } \mu_i \text{ are not equal}$

Source of variation	SS	df	MS	$F_{comp}$
treatment	SSA	$k-1$	$S_1^2 = \frac{SSA}{k-1}$	$F = \frac{S_1^2}{S_2^2}$
blocks	SSB	$b-1$	$S_2^2 = \frac{SSB}{b-1}$	
Error	SSE	$(k-1)(b-1)$	$S_2^2 = \frac{SSE}{(k-1)(b-1)}$	
Total	SST			

$S_1^2 = 5.31$

$S_2^2 = 8.42$

$S_2^2 = 1.59$

$k=4$

$F_{comp} = \frac{S_1^2}{S_2^2} = \frac{5.31}{1.59} = 3.3396$

$b=6$

$F_{table}(\alpha, k-1, (k-1)(b-1)) = F(0.05, 3, 15) = 3.29$

$F_{comp}$

$F_{comp} > F_{table}$  reject  $H_0$



# Question three

A-  $H_0: \alpha_1 = \alpha_2 = \dots = \alpha_a = 0$

$H_a$ : at least one of the  $\alpha_i$  is not equal

$H_0: \beta_1 = \beta_2 = \dots = \beta_b = 0$

$H_a$ : at least one of the  $\beta_i$  is not equal

$H_0: (\alpha\beta)_{11} = (\alpha\beta)_{12} = \dots = (\alpha\beta)_{ab} = 0$

$H_a$ : at least one of the  $(\alpha\beta)_{ij}$  is not equal

$a=3$

$b=4$

$n=2$

Source	SS	df	MS
A	14.52	2	$S_1^2 = 14.52/2 = 7.26$
B	40.08	3	$S_2^2 = 40.08/3 = 13.36$
AB	22.16	6	$S_3^2 = 22.16/6 = 3.693$
Error	14.91	12	$S^2 = 14.91/12 = 1.2425$

Total

$F_1 = \frac{S_1^2}{S^2} = \frac{7.26}{1.24} = 5.85$

$F_2 = \frac{S_2^2}{S^2} = \frac{13.36}{1.24} = 10.77$

$F_3 = \frac{S_3^2}{S^2} = \frac{3.69}{1.24} = 2.97$

$F_{table}(\alpha, df, ab(n-1)) \Rightarrow F_1(0.05, 2, 12) = 3.89$

$F_1, F_2$  reject  $H_0, H_0' = F_2(0.05, 3, 12) = 3.49$

$F_3$  accept  $H_0'' = F_3(0.05, 6, 12) = 3.00$

B-  $a=3$   $b=3$   $c=2$

Source	SS	df	MS	$F_{comp}$
A	$SSA = 13.98$	$a-1 = 2$	$S_1^2 = 13.98/2$	$F_1 = \frac{13.98/2}{1.2}$
B	$SSB = 10.18$	$b-1 = 2$	$S_2^2 = 10.18/2$	$F_2 = \frac{10.18/2}{1.2}$
C	$SSC = 1.19$	$C-1 = 1$	$S_3^2 = 1.19/1$	$F_3 = \frac{1.19/1}{1.2}$
AB	$SSAB = 4.77$	$(a-1)(b-1) = 4$	$S_4^2 = 4.77/4$	$F_4 = \frac{4.77/4}{1.2}$
AC	$SSAC = 2.91$	$(a-1)(c-1) = 2$	$S_5^2 = 2.91/2$	$F_5 = \frac{2.91/2}{1.2}$
BC	$SSBC = 3.63$	$(b-1)(c-1) = 2$	$S_6^2 = 3.63/2$	$F_6 = \frac{3.63/2}{1.2}$
ABC	$SSABC = 4.91$	$(a-1)(b-1)(c-1) = 4$	$S_7^2 = 4.91/4$	$F_7 = \frac{4.91/4}{1.2}$
Error	$SSE = 21.6$	$abc(n-1) = 18$	$S^2 = 21.6/18$	

$F_{table}(\alpha, df, abc(n-1)) \Rightarrow F_1 = 3.32$   $F_2 = 3.32$   $F_3 = 4.17$   $F_4 = 2.69$

$F_5 = 3.32$   $F_6 = 3.32$   $F_7 = 2.69$

Compare  $F_{comp} > F_{table}$  reject  $H_0$

# Final Exam 22-1-2020

Question one

A-

هو سؤال الثاني A في 2018

B-  $\bar{y}_1 = 26.9$

$\bar{y}_2 = 49.4$

$\bar{y}_3 = 51.6$

$y_4 = 44.1$

$\bar{y}_3 - \bar{y}_1 = 24.7$   
rej

$\bar{y}_2 - \bar{y}_1 = 22.5$   
rej

$\bar{y}_4 - \bar{y}_1 = 17.2$   
rej

$\bar{y}_3 - \bar{y}_2 = 2.2$   
acc

$\bar{y}_2 - \bar{y}_4 = 5.3$   
rej

$\bar{y}_3 - y_4 = 7.5$   
rej

$q_{table}(\alpha, k, v)$   $k=4$   
 $n=k-1$   
 $=3$   
 $v=4(3-1)$   
 $=8$

$q_{table}(0.05, 4, 8) = 4.53$   
 $q_{comp} = q_{table} * \sqrt{\frac{s^2}{n}} = 4.53 * \sqrt{\frac{3.84}{3}} = 5.125$   
 $= 5.13$

قارن بين الفروق بينها الفرق الأكبر ارفعية

Question two

A&B

هو سؤال الاول في 2018

Question three

A- هو سؤال الثاني B في 2018

B- هو سؤال الثالث A في 2018

Mostafa Abdel Kader





Final Exam 17-3-2021

Question one

A & B

سؤال الأول في 2017

Question two

A-  $H_0: M_1 = M_2$

$H_a: M_1 \neq M_2$

$\bar{y}_5 = 16.75$   $\bar{y}_1 = 19.84$   $\bar{y}_3 = 14.50$   $\bar{y}_6 = 22.90$   $\bar{y}_4 = 23.20$   $\bar{y}_2 = 14.50$

$\bar{y}_4 - \bar{y}_5 = 6.45$

$\bar{y}_6 - \bar{y}_5 = 6.15$

$k = 6$

$Q = \sqrt{\frac{s^2}{n}} = \sqrt{\frac{2.45}{5}} = 0.7$

$\bar{y}_4 - \bar{y}_1 = 3.36$

$\bar{y}_6 - \bar{y}_1 = 3.06$

$n = k - 1$

$\bar{y}_4 - \bar{y}_3 = 8.7$

$\bar{y}_6 - \bar{y}_3 = 8.4$

$= 5$

$\bar{y}_4 - \bar{y}_6 = 0.3$

$\bar{y}_6 - \bar{y}_2 = 8.4$

$\bar{y}_4 - \bar{y}_2 = 8.7$

$q_{table}(\alpha, k, v) = q(0.05, 6, 24) = 4.37$   
 $v = k(n-1)$

$\bar{y}_4 - \bar{y}_5 = 6.45$   
rej

$\bar{y}_6 - \bar{y}_5 = 6.15$   
rej

$\bar{y}_1 - \bar{y}_5 = 3.09$   
rej

$\bar{y}_5 - \bar{y}_3 = 2.25$   
acc

$\bar{y}_4 - \bar{y}_1 = 3.36$   
rej

$\bar{y}_6 - \bar{y}_1 = 3.06$   
rej

$\bar{y}_1 - \bar{y}_3 = 5.34$   
rej

$\bar{y}_5 - \bar{y}_2 = 2.25$   
acc

$\bar{y}_4 - \bar{y}_3 = 8.7$   
rej

$\bar{y}_6 - \bar{y}_3 = 8.4$   
rej

$\bar{y}_1 - \bar{y}_2 = 5.34$   
rej

$\bar{y}_5 - \bar{y}_2 = 2.25$   
acc

$\bar{y}_4 - \bar{y}_6 = 0.3$   
acc

$\bar{y}_6 - \bar{y}_2 = 8.4$   
rej

$\bar{y}_4 - \bar{y}_2 = 8.7$   
rej

$q_{comp} = q_{table} * Q = 4.37 * 0.7 = 3.059$

بعد كده قاربت بالفروق لو الفرق أكبر ارفض  $H_0$

Mohamed Abdelade



B. using Duncan test  $H_0: \mu_i = \mu_j$   $H_a: \mu_i \neq \mu_j$

	$\bar{y}_2$	$\bar{y}_3$	$\bar{y}_5$	$\bar{y}_1$	$\bar{y}_6$
$\bar{y}_4$	$\bar{y}_4 - \bar{y}_2 = 8.7$ $R_6$	$\bar{y}_4 - \bar{y}_3 = 8.7$ $R_5$	$\bar{y}_4 - \bar{y}_5 = 6.45$ $R_4$	$\bar{y}_4 - \bar{y}_1 = 3.36$ $R_3$	$\bar{y}_4 - \bar{y}_6 = 0.3$ $R_2$
$\bar{y}_6$	$\bar{y}_6 - \bar{y}_2 = 8.4$ $R_5$	$\bar{y}_6 - \bar{y}_3 = 8.4$ $R_4$	$\bar{y}_6 - \bar{y}_5 = 6.15$ $R_3$	$\bar{y}_6 - \bar{y}_1 = 3.06$ $R_2$	
$\bar{y}_1$	$\bar{y}_1 - \bar{y}_2 = 5.34$ $R_4$	$\bar{y}_1 - \bar{y}_3 = 5.34$ $R_3$	$\bar{y}_1 - \bar{y}_5 = 3.09$ $R_2$		
$\bar{y}_5$	$\bar{y}_5 - \bar{y}_2 = 2.25$ $R_3$	$\bar{y}_5 - \bar{y}_3 = 2.25$ $R_2$			
$\bar{y}_3$	$\bar{y}_3 - \bar{y}_2 = 0$ $R_2$				

$$Q = \sqrt{\frac{S^2}{n}} = \sqrt{\frac{2.45}{5}} = 0.7$$

$$R_p = r_p \sqrt{\frac{S^2}{n}} = r_p Q$$

P	2	3	4	5	6
$r_p$	2.919	3.066	3.160	3.226	3.276
$R_p$	2.043	2.116	2.212	2.258	2.293

قارن القيم بالفروق. لو الفرق اكبر ارفض افرو

$R_6 \Rightarrow \text{reject}$   $R_5, R_5 \Rightarrow \text{reject}$   $R_4, R_4, R_4 \Rightarrow \text{reject}$   
 $R_3, R_3, R_3, R_3 \Rightarrow \text{reject}$   $R_2 = 3.06 = 3.09 = 2.25 \Rightarrow \text{reject}$   
 $R_2 = 0.3 \Rightarrow \text{accept } H_0$

Question three

A, B هو سؤال الثالث في 2017 و 2018

look you

Mostafa Abdelkareem

تو بسمجة المنهج والامتحان

بسم الله يا رب ارزقنا الخير

خرجنا اعضاء من الجيش

Mostafa Abdelkareem