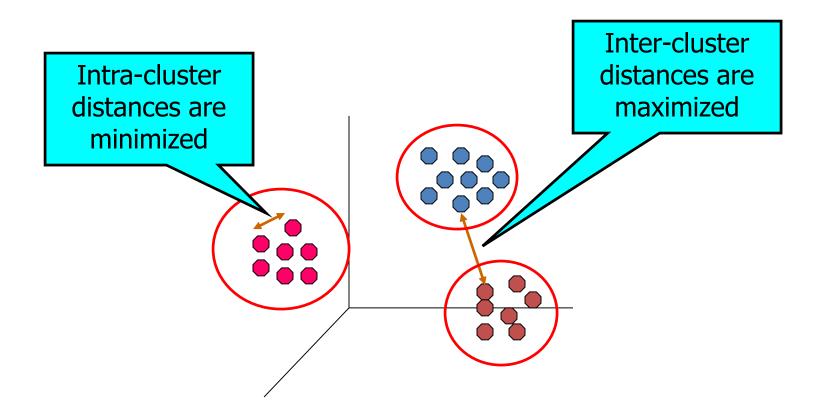
DATA MINING CLUSTERING

Dr. Mostafa Elmasry

CLUSTERING

What is a Clustering?

 In general a grouping of objects such that the objects in a group (cluster) are similar (or related) to one another and different from (or unrelated to) the objects in other groups



Applications of Cluster Analysis

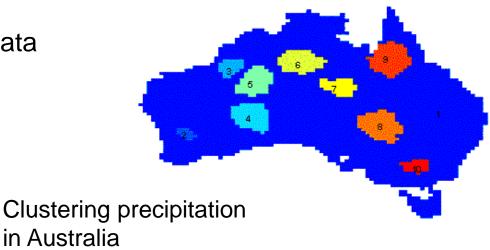
Understanding

 Group related documents for browsing, group genes and proteins that have similar functionality, or group stocks with similar price fluctuations

	Discovered Clusters	Industry Group
1	Applied-Matl-DOWN,Bay-Network-Down,3-COM-DOWN, Cabletron-Sys-DOWN,CISCO-DOWN,HP-DOWN, DSC-Comm-DOWN,INTEL-DOWN,LSI-Logic-DOWN, Micron-Tech-DOWN,Texas-Inst-Down,Tellabs-Inc-Down, Natl-Semiconduct-DOWN,Oracl-DOWN,SGI-DOWN, Sun-DOWN	Technology1-DOWN
2	Apple-Comp-DOWN,Autodesk-DOWN,DEC-DOWN, ADV-Micro-Device-DOWN,Andrew-Corp-DOWN, Computer-Assoc-DOWN,Circuit-City-DOWN, Compaq-DOWN, EMC-Corp-DOWN, Gen-Inst-DOWN, Motorola-DOWN,Microsoft-DOWN,Scientific-Atl-DOWN	Technology2-DOWN
3	Fannie-Mae-DOWN,Fed-Home-Loan-DOWN, MBNA-Corp-DOWN,Morgan-Stanley-DOWN	Financial-DOWN
4	Baker-Hughes-UP,Dresser-Inds-UP,Halliburton-HLD-UP, Louisiana-Land-UP,Phillips-Petro-UP,Unocal-UP, Schlumberger-UP	Oil-UP

Summarization

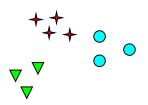
Reduce the size of large data sets



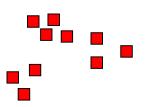
Notion of a Cluster can be Ambiguous

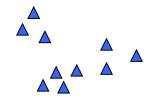


How many clusters?

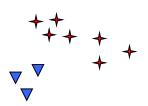


Six Clusters





Two Clusters Four Clusters

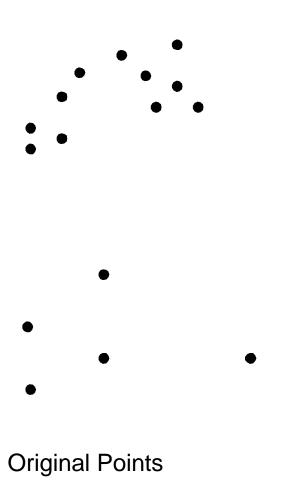


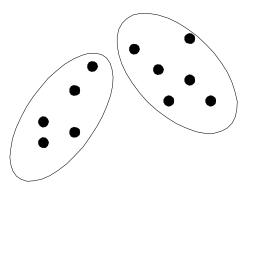


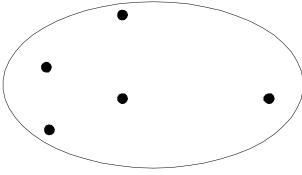
Types of Clusterings

- A clustering is a set of clusters
- Important distinction between hierarchical and partitional sets of clusters
- Partitional Clustering
 - A division data objects into subsets (clusters) such that each data object is in exactly one subset
- Hierarchical clustering
 - A set of nested clusters organized as a hierarchical tree

Partitional Clustering

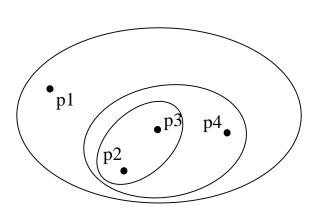




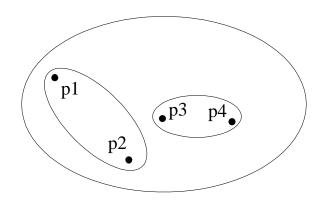


A Partitional Clustering

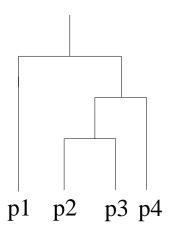
Hierarchical Clustering



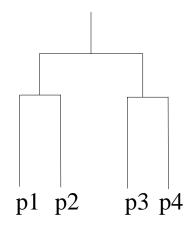
Traditional Hierarchical Clustering



Non-traditional Hierarchical Clustering



Traditional Dendrogram



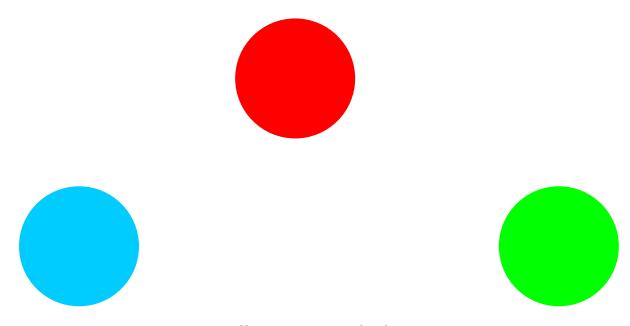
Non-traditional Dendrogram

Other types of clustering

- Exclusive (or non-overlapping) versus nonexclusive (or overlapping)
 - In non-exclusive clusterings, points may belong to multiple clusters.
 - Points that belong to multiple classes, or 'border' points
- Fuzzy (or soft) versus non-fuzzy (or hard)
 - In fuzzy clustering, a point belongs to every cluster with some weight between 0 and 1
 - Weights usually must sum to 1 (often interpreted as probabilities)
- Partial versus complete
 - In some cases, we only want to cluster some of the data

Types of Clusters: Well-Separated

- Well-Separated Clusters:
 - A cluster is a set of points such that any point in a cluster is closer (or more similar) to every other point in the cluster than to any point not in the cluster.



3 well-separated clusters

Types of Clusters: Center-Based

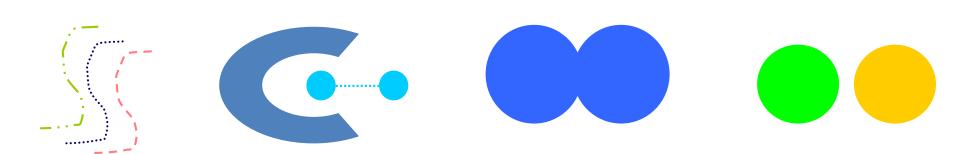
Center-based

- A cluster is a set of objects such that an object in a cluster is closer (more similar) to the "center" of a cluster, than to the center of any other cluster
- The center of a cluster is often a centroid, the minimizer of distances from all the points in the cluster, or a medoid, the most "representative" point of a cluster



Types of Clusters: Contiguity-Based

- Contiguous Cluster (Nearest neighbor or Transitive)
 - A cluster is a set of points such that a point in a cluster is closer (or more similar) to one or more other points in the cluster than to any point not in the cluster.



Clustering Algorithms

- K-means and its variants
- Hierarchical clustering

DBSCAN

K-MEANS

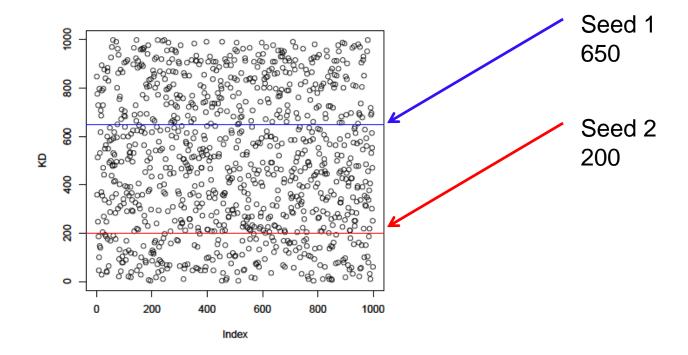
- Partitional clustering approach
- Each cluster is associated with a centroid (center point)
- Each point is assigned to the cluster with the closest centroid
- Number of clusters, K, must be specified
- The objective is to minimize the sum of distances of the points to their respective centroid

- What is clustering?
- Why would we want to cluster?
- How would you determine clusters?
- How can you do this efficiently?

- Strengths
 - Simple iterative method
 - User provides "K"
- Weaknesses
 - Often too simple → bad results
 - Difficult to guess the correct "K"

Basic Algorithm:

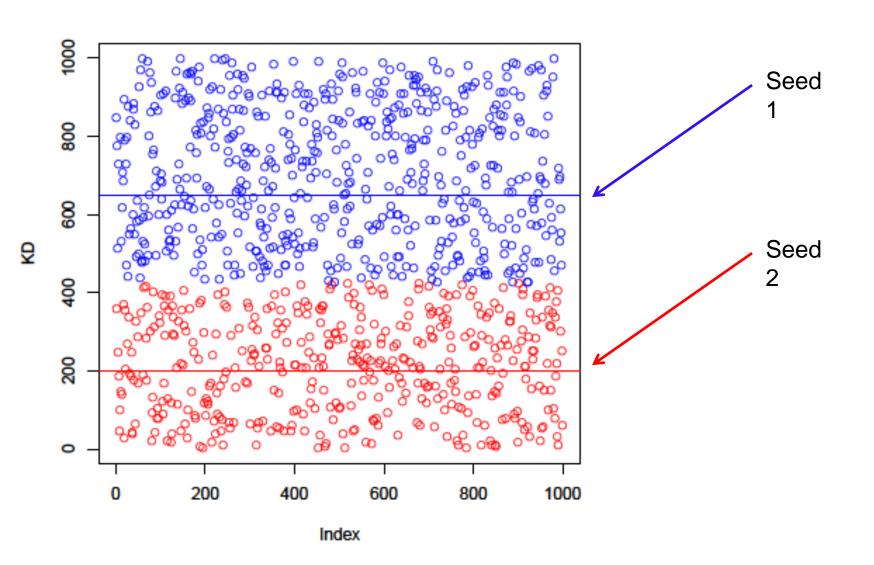
- Step 0: select K
- Step 1: randomly select initial cluster seeds



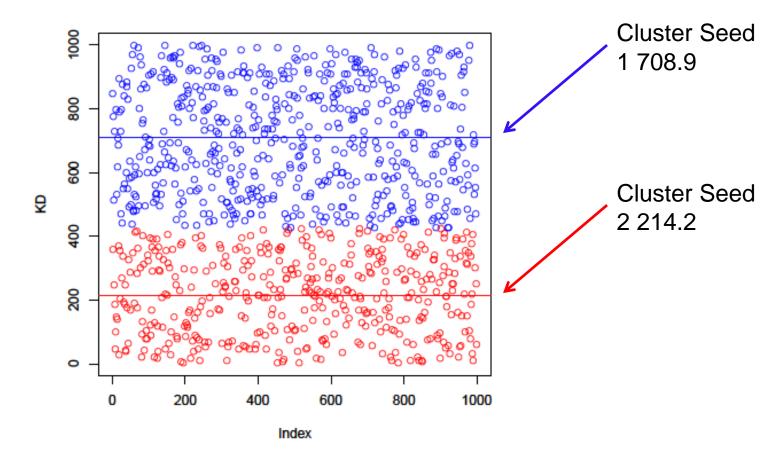
- An initial cluster seed represents the "mean value" of its cluster.
- In the preceding figure:
 - Cluster seed 1 = 650
 - Cluster seed 2 = 200

- Step 2: calculate distance from each object to each cluster seed.
- What type of distance should we use?
 - Squared Euclidean distance
- Step 3: Assign each object to the closest cluster

K-maane Cluetaring



 Step 4: Compute the new centroid for each cluster



- Iterate:
 - Calculate distance from objects to cluster centroids.
 - Assign objects to closest cluster
 - Recalculate new centroids
- Stop based on convergence criteria
 - No change in clusters
 - Max iterations

K-means Issues

- Distance measure is squared Euclidean
 - Scale should be similar in all dimensions
 - Rescale data?
 - Not good for nominal data. Why?
- Approach tries to minimize the within-cluster sum of squares error (WCSS)
 - Implicit assumption that SSE is similar for each group

WCSS

• The over all WCSS is given by: $\sum_{i=1}^k \sum_{x \in C_i} ||x - x||^2$

Bottom Line

- K-means
 - Easy to use
 - Need to know K
 - May need to scale data
 - Good initial method
- Local optima
 - No guarantee of optimal solution
 - Repeat with different starting values

 Problem: Given a set X of n points in a ddimensional space and an integer K group the points into K clusters C= {C₁, C₂,...,C_k} such that

$$Cost(C) = \sum_{i=1}^{k} \sum_{x \in C_i} dist(x, c)$$

is minimized, where c_i is the centroid of the points in cluster C_i

- Most common definition is with euclidean distance, minimizing the Sum of Squares Error (SSE) function
 - Sometimes K-means is defined like that
- Problem: Given a set X of n points in a ddimensional space and an integer K group the points into K clusters C= {C₁, C₂,...,C_k} such that

$$Cost(C) = \sum_{i=1}^{\kappa} \sum_{x \in C_i} (x - c_i)^2$$

is minimized, where c_i is the mean of the points in cluster C_i

K-means Algorithm

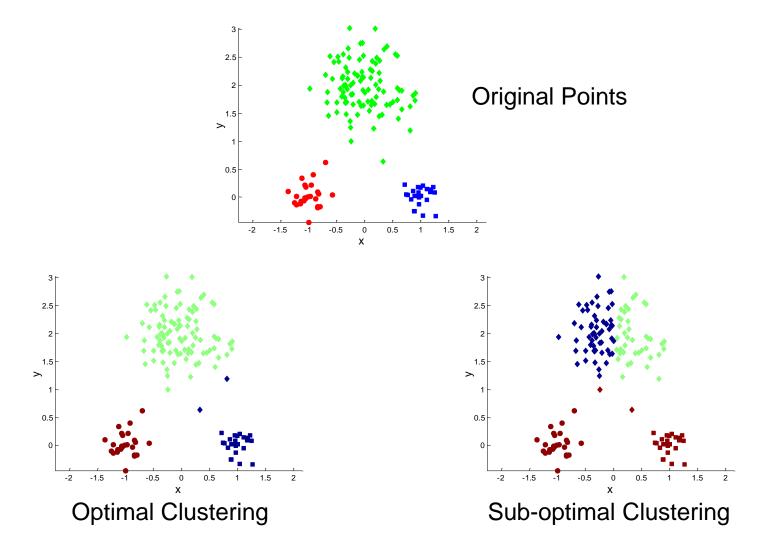
- Also known as Lloyd's algorithm.
- K-means is sometimes synonymous with this algorithm

- 1: Select K points as the initial centroids.
- 2: repeat
- 3: Form K clusters by assigning all points to the closest centroid.
- 4: Recompute the centroid of each cluster.
- 5: **until** The centroids don't change

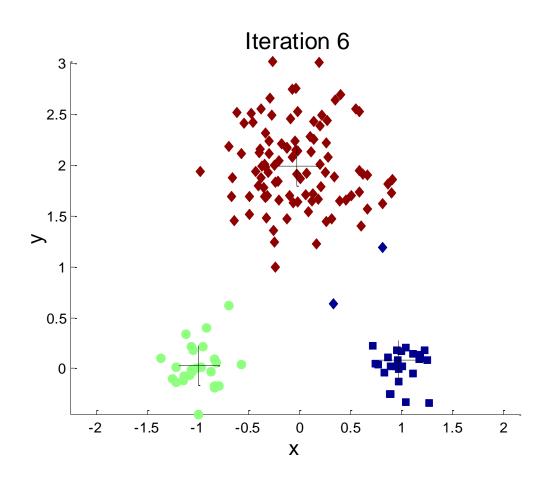
K-means Algorithm — Initialization

- Initial centroids are often chosen randomly.
 - Clusters produced vary from one run to another.

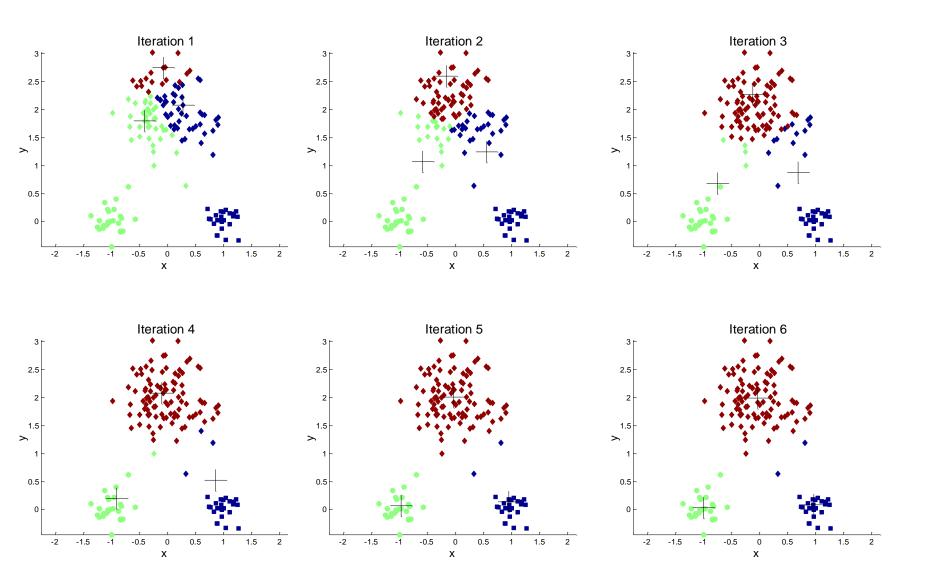
Two different K-means Clusterings



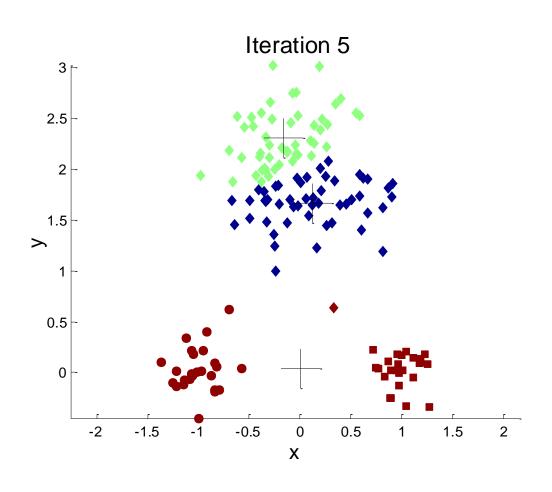
Importance of Choosing Initial Centroids



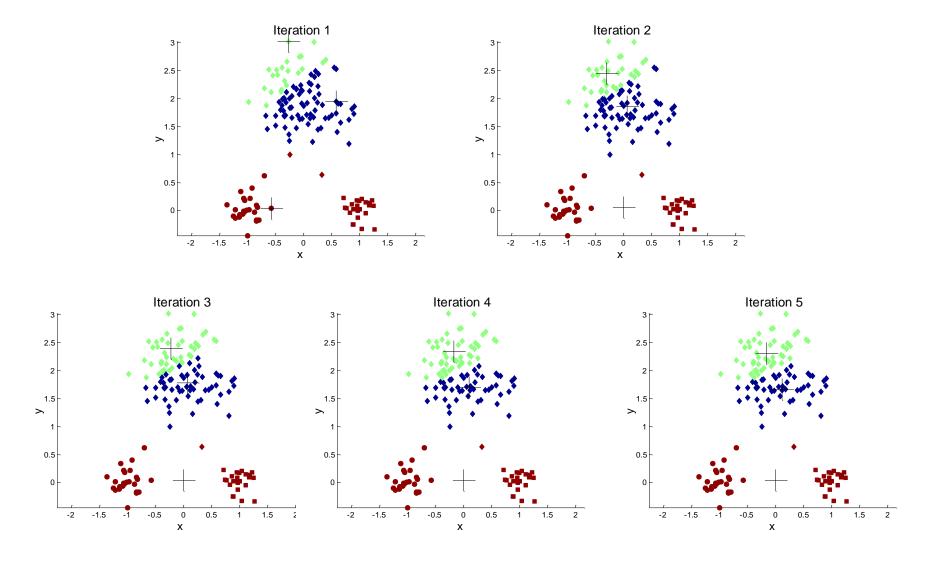
Importance of Choosing Initial Centroids



Importance of Choosing Initial Centroids



Importance of Choosing Initial Centroids ...



Dealing with Initialization

 Do multiple runs and select the clustering with the smallest error

 Select original set of points by methods other than random. E.g., pick the most distant (from each other) points as cluster centers (K-means++ algorithm)

K-means Algorithm – Centroids

- The centroid depends on the distance function
 - The minimizer for the distance function
- 'Closeness' is measured by Euclidean distance (SSE), cosine similarity, correlation, etc.
- Centroid:
 - The mean of the points in the cluster for SSE, and cosine similarity

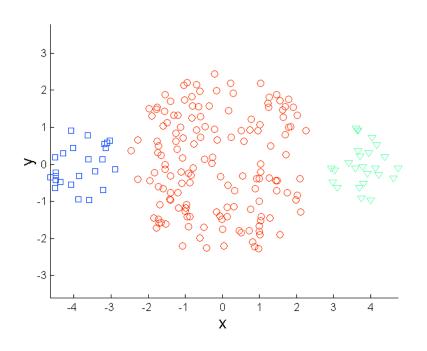
K-means Algorithm – Convergence

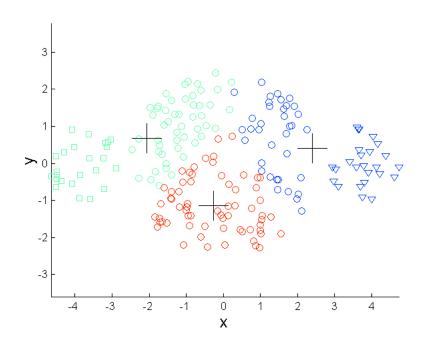
- K-means will converge for common similarity measures mentioned above.
 - Most of the convergence happens in the first few iterations.
 - Often the stopping condition is changed to 'Until relatively few points change clusters'
- Complexity is O(n * K * I * d)
 - n = number of points, K = number of clusters,
 I = number of iterations, d = dimensionality
- In general a fast and efficient algorithm

Limitations of K-means

- K-means has problems when clusters are of different
 - Sizes
 - Densities
 - Non-globular shapes
- K-means has problems when the data contains outliers.

Limitations of K-means: Differing Sizes

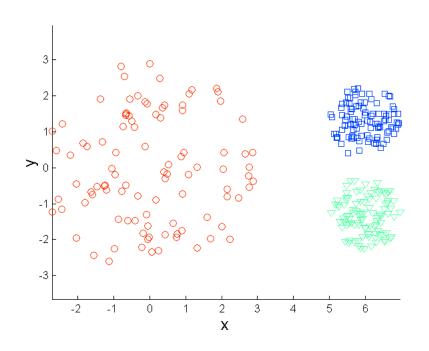


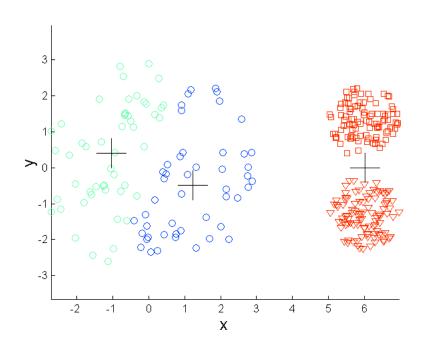


Original Points

K-means (3 Clusters)

Limitations of K-means: Differing Density

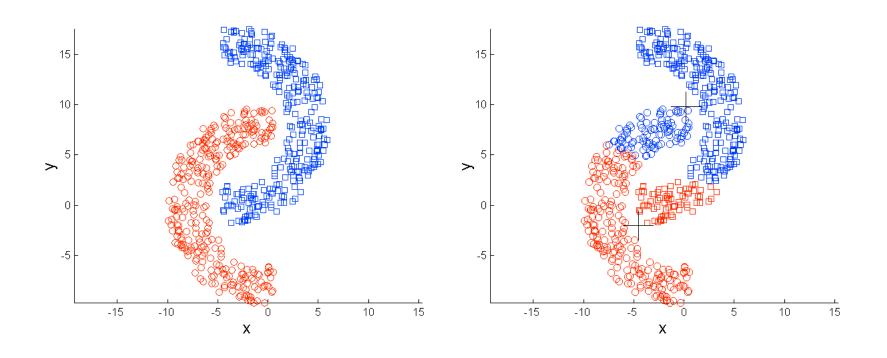




Original Points

K-means (3 Clusters)

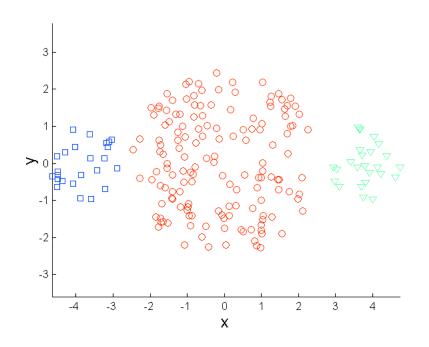
Limitations of K-means: Non-globular Shapes

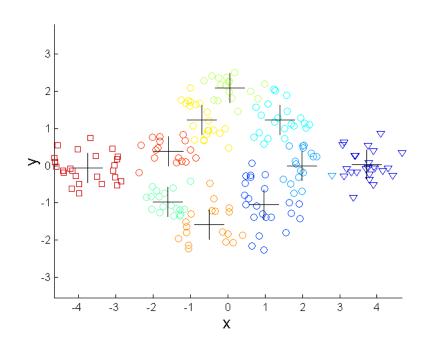


Original Points

K-means (2 Clusters)

Overcoming K-means Limitations



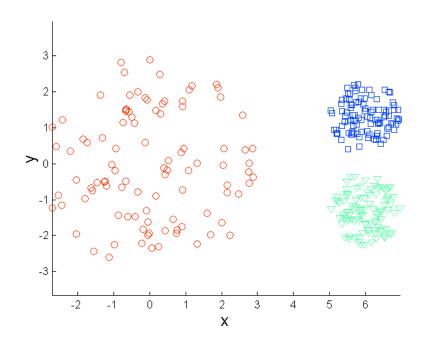


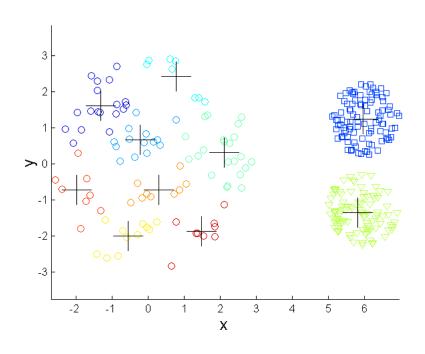
Original Points

K-means Clusters

One solution is to use many clusters. Find parts of clusters, but need to put together.

Overcoming K-means Limitations

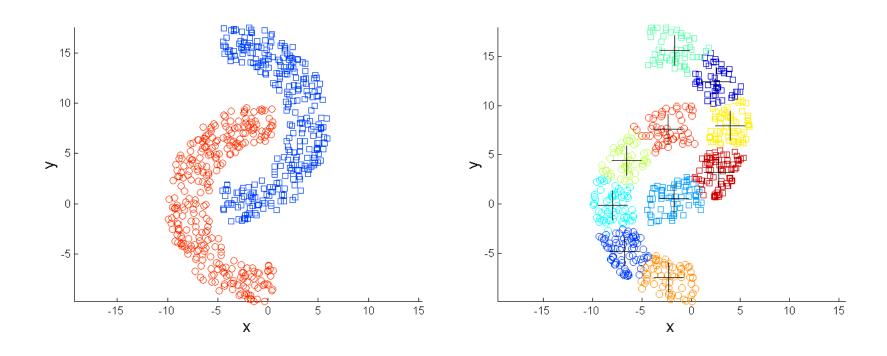




Original Points

K-means Clusters

Overcoming K-means Limitations



Original Points

K-means Clusters