

Chapter 3

Describing Syntax and Semantics

Chapter 3 Topics

Introduction

The General Problem of Describing Syntax

Formal Methods of Describing Syntax

Introduction

Syntax: the form or structure of the expressions, statements, and program units

Semantics: the meaning of the expressions, statements, and program units

Syntax and semantics provide a language's definition

Users of a language definition

Other language designers

Implementers

Programmers (the users of the language)

The General Problem of Describing Syntax: Terminology

A *sentence* is a string of characters over some alphabet

A *language* is a set of sentences

A *lexeme* is the lowest level syntactic unit of a language (e.g., *, sum, begin)

A *token* is a category of lexemes (e.g., identifier)

Formal Definition of Languages

Recognizers

A recognition device reads input strings over the alphabet of the language and decides whether the input strings belong to the language

Example: syntax analysis part of a compiler

- Detailed discussion of syntax analysis appears in Chapter 4

Generators

A device that generates sentences of a language

One can determine if the syntax of a particular sentence is syntactically correct by comparing it to the structure of the generator

BNF and Context-Free Grammars

Context-Free Grammars

- Developed by Noam Chomsky in the mid-1950s

- Language generators, meant to describe the syntax of natural languages

- Define a class of languages called context-free languages

Backus-Naur Form (1959)

- Invented by John Backus to describe Algol 58

- BNF is equivalent to context-free grammars

BNF Fundamentals

In BNF, abstractions are used to represent classes of syntactic structures--they act like syntactic variables (also called *nonterminal symbols*, or just *terminals*)

Terminals are lexemes or tokens

A rule has a left-hand side (LHS), which is a nonterminal, and a right-hand side (RHS), which is a string of terminals and/or nonterminals

Nonterminals are often enclosed in angle brackets

Grammar: a finite non-empty set of rules

A start symbol is a special element of the nonterminals of a grammar

BNF Rules

Examples of BNF rules:

`<ident_list> → identifier | identifier, <ident_list>`

`<if_stmt> → if <logic_expr> then <stmt>`

An abstraction (or nonterminal symbol) can have more than one RHS

`<stmt> → <single_stmt>
 | begin <stmt_list> end`

Describing Lists

Syntactic lists are described using recursion

$$\begin{aligned} \text{<ident_list>} &\rightarrow \text{ident} \\ &\quad | \text{ ident, <ident_list>} \end{aligned}$$

A derivation is a repeated application of rules, starting with the start symbol and ending with a sentence (all terminal symbols)

An Example Grammar

$\langle \text{program} \rangle \rightarrow \langle \text{stmts} \rangle$

$\langle \text{stmts} \rangle \rightarrow \langle \text{stmt} \rangle \mid \langle \text{stmt} \rangle ; \langle \text{stmts} \rangle$

$\langle \text{stmt} \rangle \rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$

$\langle \text{var} \rangle \rightarrow a \mid b \mid c \mid d$

$\langle \text{expr} \rangle \rightarrow \langle \text{term} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle - \langle \text{term} \rangle$

$\langle \text{term} \rangle \rightarrow \langle \text{var} \rangle \mid \text{const}$

An Example Derivation

$\langle \text{program} \rangle \Rightarrow \langle \text{stmts} \rangle \Rightarrow \langle \text{stmt} \rangle$
 $\Rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$
 $\Rightarrow a = \langle \text{expr} \rangle$
 $\Rightarrow a = \langle \text{term} \rangle + \langle \text{term} \rangle$
 $\Rightarrow a = \langle \text{var} \rangle + \langle \text{term} \rangle$
 $\Rightarrow a = b + \langle \text{term} \rangle$
 $\Rightarrow a = b + \text{const}$

Derivations

Every string of symbols in a derivation is a *sentential form*

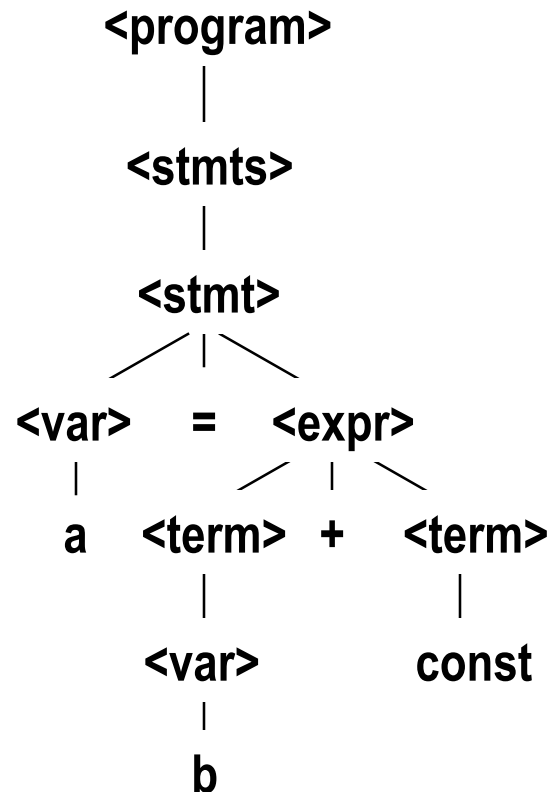
A *sentence* is a sentential form that has only terminal symbols

A *leftmost derivation* is one in which the leftmost nonterminal in each sentential form is the one that is expanded

A derivation may be neither leftmost nor rightmost

Parse Tree

A hierarchical representation of a derivation



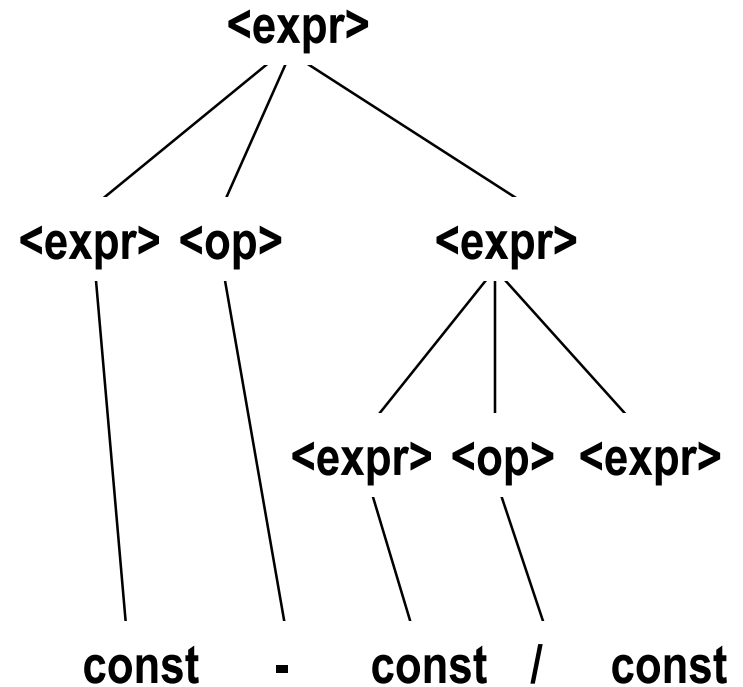
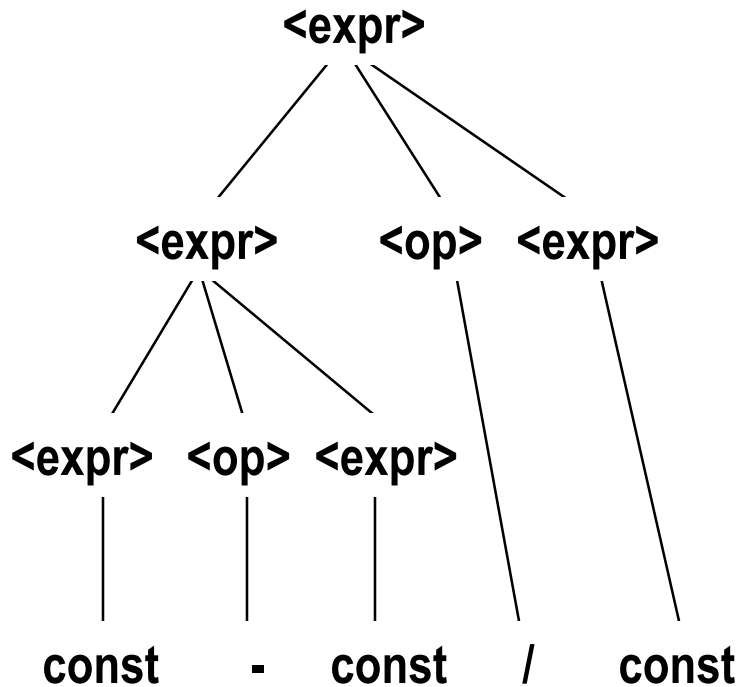
Ambiguity in Grammars

A grammar is *ambiguous* if and only if it generates a sentential form that has two or more distinct parse trees

An Ambiguous Expression Grammar

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle \langle \text{op} \rangle \langle \text{expr} \rangle \mid \text{const}$

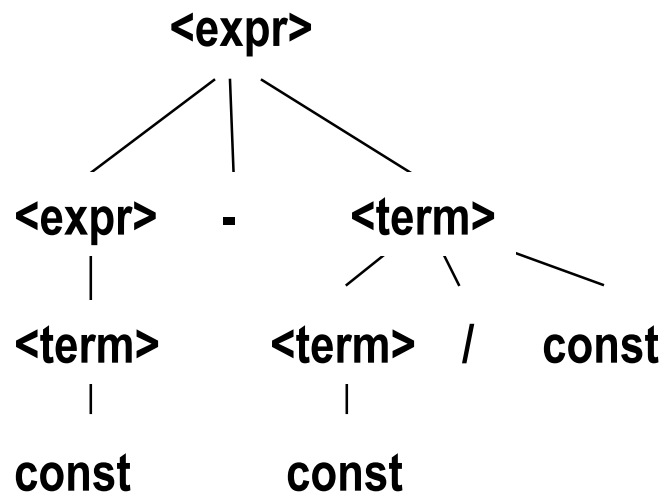
$\langle \text{op} \rangle \rightarrow / \mid -$



An Unambiguous Expression Grammar

If we use the parse tree to indicate precedence levels of the operators, we cannot have ambiguity

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle - \langle \text{term} \rangle \mid \langle \text{term} \rangle$
 $\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle / \text{const} \mid \text{const}$

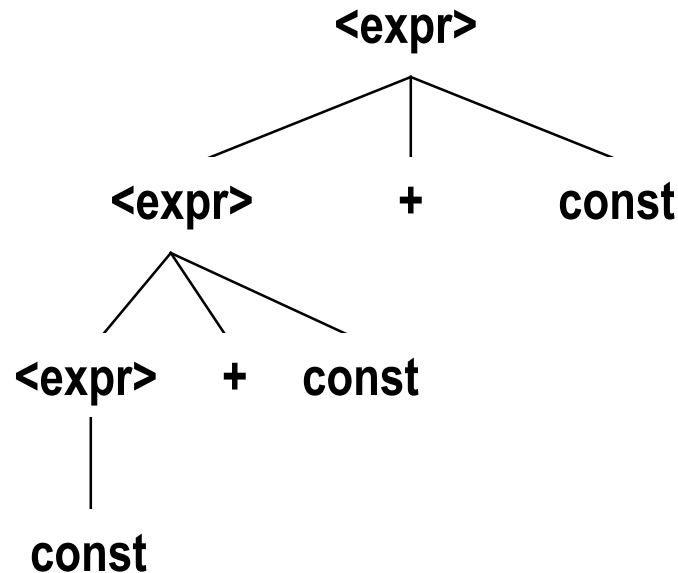


Associativity of Operators

Operator associativity can also be indicated by a grammar

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \langle \text{expr} \rangle \mid \text{const}$ (ambiguous)

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \text{const} \mid \text{const}$ (unambiguous)



Extended BNF

Optional parts are placed in brackets []

`<proc_call> -> ident [(<expr_list>)]`

Alternative parts of RHSs are placed inside parentheses and separated via vertical bars

`<term> → <term> (+|-) const`

Repetitions (0 or more) are placed inside braces { }

`<ident> → letter {letter|digit}`

BNF and EBNF

BNF

$$\begin{aligned}\langle \text{expr} \rangle &\rightarrow \langle \text{expr} \rangle + \langle \text{term} \rangle \\ &\quad | \langle \text{expr} \rangle - \langle \text{term} \rangle \\ &\quad | \langle \text{term} \rangle\end{aligned}$$
$$\begin{aligned}\langle \text{term} \rangle &\rightarrow \langle \text{term} \rangle * \langle \text{factor} \rangle \\ &\quad | \langle \text{term} \rangle / \langle \text{factor} \rangle \\ &\quad | \langle \text{factor} \rangle\end{aligned}$$

EBNF

$$\begin{aligned}\langle \text{expr} \rangle &\rightarrow \langle \text{term} \rangle \{ (+ \mid -) \langle \text{term} \rangle \} \\ \langle \text{term} \rangle &\rightarrow \langle \text{factor} \rangle \{ (* \mid /) \langle \text{factor} \rangle \}\end{aligned}$$

Recent Variations in EBNF

Alternative RHSs are put on separate lines

Use of a colon instead of =>

Use of _{opt} for optional parts

Use of `one of` for choices

Summary

BNF and context-free grammars are equivalent meta-languages

Well-suited for describing the syntax of programming languages