

Problem-01: BFS Basic Algorithm

Breadth-First Search (BFS) is a graph traversal method that explores nodes layer by layer, starting from a given source.

It is widely used in shortest-path algorithms, level-order processing, and exploring connected components.

Intuition

Think of BFS like ripples in water:

01. Drop a stone (the starting node).
02. Waves spread outward.
03. Every point at the same radius is visited together.

This is exactly how BFS processes nodes — distance-wise

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Why BFS?

BFS is used when you need:

01. Shortest path in an unweighted graph
02. Level-by-level exploration
03. Minimum number of moves
04. Checking connectivity
05. Exploring all reachable nodes

Core Idea

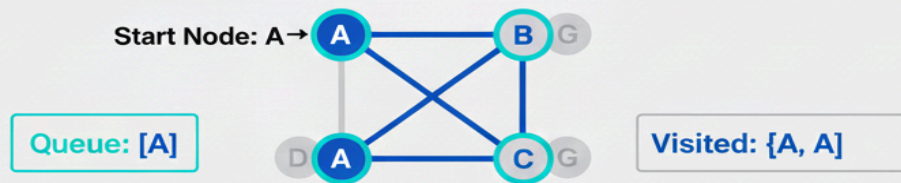
1. Maintain a queue to store nodes waiting to be processed.
2. Start from a chosen node.
3. Visit all its immediate neighbors.
4. Then visit neighbors of neighbors.
5. Continue until all reachable nodes are processed.

BFS = Explore closest first → then gradually go farther.

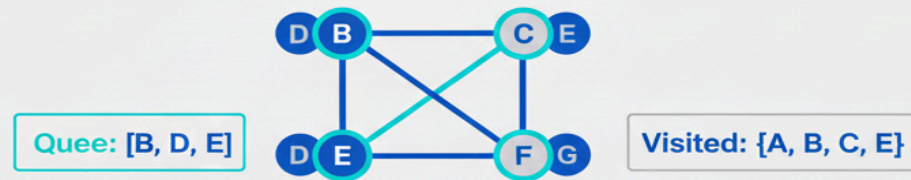
Algorithm Steps

1. Mark all nodes as unvisited.
2. Select a starting node.
3. Mark it visited, push it into the queue.
4. While the queue is not empty:
 - Remove the front node.
 - For each of its neighbors:
 - If not visited → mark visited → push into queue.

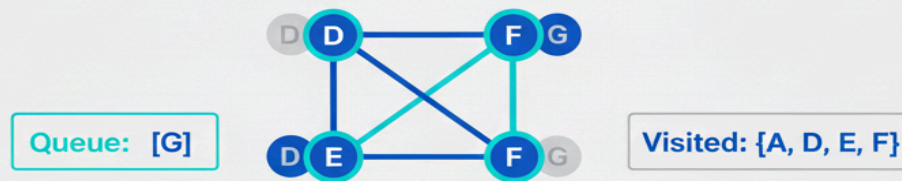
Step 1: Initiatlization



Step 2: Exploring Level 1 (B, C)



Step 4: Exploring Level 2 (D, E, G)



Queue Empty. Algorithm Terminates. ✓

Complexity

Time: $O(V + E)$

Space: $O(V)$

Where:

V = number of vertices

E = number of edges

Pseudocode:

```
BFS(start):  
    for each node:  
        visited[node] = false  
  
    create queue Q  
  
    visited[start] = true  
    Q.enqueue(start)  
  
    while Q is not empty:  
        u = Q.dequeue()  
  
        for each v in adjacency_list[u]:  
            if visited[v] == false:  
                visited[v] = true  
                Q.enqueue(v)
```