MAST30027 Modern Applied, Statistics Assignment2

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1.Introduction

1.1 Background

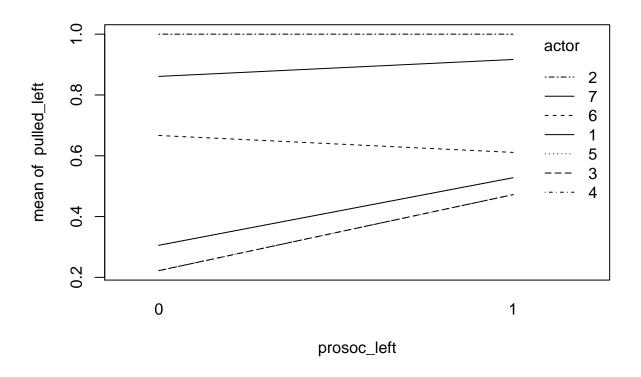
This report is about evaluating chimpanzees prosocial tendency by analysing and fitting model to the data. The experiment has has two options, one is prosocial option, when human students participate the experiment, they nearly always choose the prosocial option when another student sits on the opposite side of the table. The question is whether a focal chimpanzee behaves similarly, choosing the prosocial option more often when another animal is present.

1.2 Data

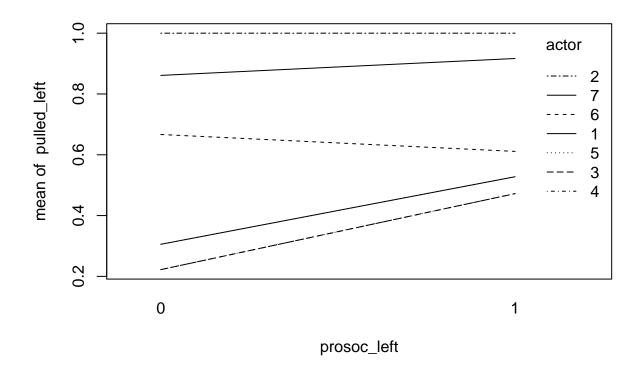
There are four attributes in the raw data. By looking through the dataset, it is found that every chimpanzee have the same number of instance if data (72 for each chimpanzee), therefore it is not tend to bias towards particular a chimpanzee. It should also be noted the data is also balanced in the two conditions and two prosoc left, each chimpanzee has 16 experiment on each combination of condition and prosoc left.

These are the 4 attributes in the raw dataset. actor (1 to 7) condition (0 or 1): prosoc left (0 or 1) pulled left (0 or 1) Load the dataset

```
dataset = read.delim("assign2.txt", header = TRUE, sep = " ")
with(dataset, interaction.plot(prosoc_left,actor,pulled_left))
```



with(dataset, interaction.plot(prosoc_left,actor,pulled_left))



2. Preprocessing

2.1Create New Attribute

Since the question is whether a focal chimpanzee choosing the prosocial option more often when another animal is present. Therefore, an new attribute "prosocial_action" is created, it means whether prosoc_left and pulled_left are same. If these two atributes are same, chimpanzee perform prosocially and prosocial_action has value TRUE and otherwise it has value FALSE.

```
dataset['prosocial_action'] = (dataset$prosoc_left == dataset$pulled_left)
#first10 rows in the dataset after adding new attribute prosocial_action
dataset[1:10,]
```

##		actor	${\tt condition}$	prosoc_left	<pre>pulled_left</pre>	<pre>prosocial_action</pre>
##	1	1	0	0	0	TRUE
##	2	1	0	0	1	FALSE
##	3	1	0	1	0	FALSE
##	4	1	0	0	0	TRUE
##	5	1	0	1	1	TRUE
##	6	1	0	1	1	TRUE
##	7	1	0	1	0	FALSE
##	8	1	0	1	0	FALSE
##	9	1	0	0	0	TRUE
##	10	1	0	0	0	TRUE

3. Visualization

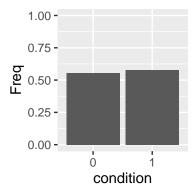
3.1Plot of the percentage of prosocial action for all chimpanzees

```
prosocial = xtabs(prosocial_action ~ condition, data = dataset)
(prosocial_percentage = transform(prosocial, Freq=Freq/252))
```

```
## condition Freq
## 1 0 0.5555556
## 2 1 0.5793651
```

The average percentage of choose prosocial increase from 0.5555556 to 0.5793651 in condition 1.

```
# generate the bar plot
library(ggplot2)
ggplot(data=prosocial_percentage,aes(x=condition,y=Freq))+
  coord_cartesian(ylim=c(0, 1))+
  geom_bar(stat="identity",position="dodge")
```



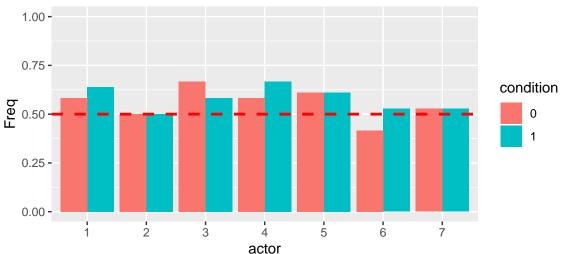
On average, chimapnzees choose the prosocial option more frequently in condition 1 (when there is another chimpanzee in opposite). But the increase is very small and plot each chimpanzee may helps to see the trend more clearly.

3.2Plot of the percentage of prosocial action for each chimpanzee

```
prosocial = xtabs(prosocial_action ~ actor + condition, data = dataset)
prosocial_percentage = transform(prosocial, Freq=Freq/36)

# generate the bar plot
library(ggplot2)
ggplot(data=prosocial_percentage,aes(x=actor,y=Freq,fill=condition))+
    coord_cartesian(ylim=c(0, 1))+
    geom_bar(stat="identity",position="dodge")+
    ggtitle("Plot of the percentage of prosocial action for each actor")+
    geom_hline(yintercept=0.5, linetype=2, color = "red",size = 1)
```





The plot show the percentage of prosocial action for each chimpanzee on two conditions. It can be seen that most chimpanzee tend to choos the prosocial optional in both condition. 3 of 7 chimpanzees dose not change the frequency of choosing. Three actors choose prosocial option more frequently while one actor perform differently. However, we cannot make conclusion based on the plot and models need to be fit.

3.3 Outlier

From the plot in 3.2, the second chimpanzee (actor 2) show strange result. In both conditions, it chooses proaction option at exactly at 0.5. By looking back through the dataset. It can be found that the it always choose the left one regardless of other factors. There is no similar behaviour like this among other chimpanzees and it might be an outlier.

```
# Second chimpanzee always pulled the left lever
xtabs(~prosoc_left+pulled_left, data = dataset[dataset$actor == 2,])
              pulled_left
##
  prosoc_left
##
             0 36
##
# Other chimpanzees pulled both left and right lever
# for example chimpanzees 1
xtabs(~prosoc_left+pulled_left, data = dataset[dataset$actor == 1,])
##
              pulled_left
##
  prosoc_left 0 1
##
             0 25 11
##
             1 17 19
```

This might be an error in data collection process and might be nomal behaviour among chimpanzee species. Based on the data, I cannot decided which one it should be. This problem should be checked with the zoologist and experts with domain knowledges to decided whether to remove data from chimpanzee 2. In this report, assume it is not an error and thus the include data from chimpanzee 2.

3. Test dependency of prosocial_action, condition and actor

Using three way contengency table to test the mutually independency of the 3 factors. Poisson regression is used because poisson regression with log link will gives chi-square distribution. $H0 = \text{prosocial_action } \& \text{condition } \& \text{ actor are independent } H2 = \text{prosocial_action } \& \text{ condition } \& \text{ actor are not independent } H2 = \text{prosocial_action } \& \text{ condition } \& \text{ actor are not independent } H2 = \text{prosocial_action } \& \text{ condition } \& \text{ actor are not independent } H2 = \text{prosocial_action } \& \text{ condition } \& \text{ actor are not independent } H2 = \text{prosocial_action } \& \text{ condition } \& \text{ actor are not independent } H2 = \text{prosocial_action } \& \text{ condition }$

```
x = xtabs( ~ condition + prosocial_action + actor, data = dataset)
(x = data.frame(x))
```

```
##
       condition prosocial action actor Freq
                               FALSE
## 1
                0
                                           1
                                                15
## 2
                1
                               FALSE
                                           1
                                                13
## 3
                0
                                TRUE
                                           1
                                                21
## 4
                1
                                TRUE
                                           1
                                                23
## 5
                0
                                           2
                                                18
                               FALSE
## 6
                1
                               FALSE
                                           2
                                                18
                0
                                           2
## 7
                                TRUE
                                                18
                                           2
## 8
                1
                                TRUE
                                                18
## 9
                0
                               FALSE
                                           3
                                                12
                                           3
## 10
                1
                               FALSE
                                                15
                                           3
## 11
                0
                                TRUE
                                                24
                                TRUE
                                           3
## 12
                1
                                                21
                0
                                           4
## 13
                               FALSE
                                                15
## 14
                1
                               FALSE
                                           4
                                                12
                0
                                           4
                                                21
## 15
                                TRUE
                                           4
## 16
                1
                                TRUE
                                                24
                0
                                           5
## 17
                               FALSE
                                                14
## 18
                               FALSE
                                           5
                1
                                                14
## 19
                0
                                TRUE
                                           5
                                                22
## 20
                1
                                TRUE
                                           5
                                                22
                0
## 21
                               FALSE
                                           6
                                                21
## 22
                               FALSE
                                           6
                                                17
                1
## 23
                0
                                TRUE
                                           6
                                                15
                                           6
## 24
                1
                                TRUE
                                                19
## 25
                0
                               FALSE
                                           7
                                                17
## 26
                                           7
                1
                               FALSE
                                                17
                                           7
## 27
                0
                                TRUE
                                                19
                                TRUE
## 28
                                           7
                                                19
```

The cell counts need to be at least 5 for the deviance to has chi-square distribution as describe in the lectue. From the data count above, it can be seen that the minimum count is 13.

```
#fit poisson model
model0 = glm(Freq ~ condition + prosocial_action + actor, family = poisson, data = x)
#deviance of the poission regression model
deviance(model0)
## [1] 9.704807
```

```
#degrees of freedom
df.residual(model0)
```

[1] 19

```
# calculate the p-value
pchisq(deviance(model0), df = df.residual(model0), lower.tail = FALSE)
```

[1] 0.9598556

The p-value is 0.9598556, it is much larger than 0.05, thus we cannot reject H0 and prosocial_action & condition & action are independent. Since we are interested in whether prosocial_action is related the condition (whether there is another chimpanzee in another side), from the result we can say that prosocial_action is independent of condition. And chimpanzee don't behave similarly as human.

4. Testing confounding factors

actor, prosoc_left and pulled_left might be confounding factors

4.1 Testing whether actor is confounding factor

 $\mathrm{H0}: \mathrm{prosocial_action} + \mathrm{condition} + \mathrm{actor} \ \mathrm{are} \ \mathrm{independet} \ \mathrm{H1}: \mathrm{prosocial_action} + \mathrm{condition} + \mathrm{actor} \ \mathrm{are} \ \mathrm{dependet}$

```
#test all 3 factor are independent
x = xtabs( ~ prosocial_action + condition + actor, data = dataset)
model1 = glm(Freq~ prosocial_action + condition + actor, family = poisson,data = x )
deviance(model1)
```

```
## [1] 9.704807
```

```
pchisq(deviance(model1), df = df.residual(model1), lower.tail = FALSE)
```

```
## [1] 0.9598556
```

p-value = 0.9598556, thus prosocial_action, condition and actor are independent, thus actor is not and confounding a factor.

4.2 Testing whether pulled left is confounding factor

 ${
m H0: prosocial_action + condition + pulled_left}$ are independet ${
m H1: prosocial_action + condition + pulled_left}$ are dependet

```
#test all 3 factor are independent
x = xtabs( ~ prosocial_action + condition + pulled_left, data = dataset)
model1 = glm(Freq~ prosocial_action + condition + pulled_left, family = poisson,data = x )
deviance(model1)
```

```
## [1] 1.685609
```

```
pchisq(deviance(model1), df = df.residual(model1), lower.tail = FALSE)
```

```
## [1] 0.7933302
```

p-value = 0.7933302, thus prosocial_action, condition and pulled_left are independent, thus pulled_left is not and confounding a factor.

4.3 Testing whether prosoc_left is confounding factor

 $\mathrm{H0}: \mathrm{prosocial_action} + \mathrm{condition} + \mathrm{prosoc_left}$ are independet $\mathrm{H1}: \mathrm{prosocial_action} + \mathrm{condition} + \mathrm{prosoc}$ left are dependet

```
#test all 3 factor are independent
x = xtabs( ~ prosocial_action + condition + prosoc_left, data = dataset)
model1 = glm(Freq~ prosocial_action + condition + prosoc_left, family = poisson,data = x)
deviance(model1)
```

```
## [1] 14.43789
```

```
pchisq(deviance(model1), df = df.residual(model1), lower.tail = FALSE)
```

```
## [1] 0.006020994
```

p-value = 0.006020994, reject H0, thus 3 factors prosocial_action, condition and prosoc_left are dependent.

 ${
m H0: prosoc_left}$ is independent of prosocial_action and condition ${
m H1: prosoc_left}$ is dependent of prosocial_action and condition

```
#test if prosoc_left is independent of prosocial_action and condition
model2 = glm(Freq~ prosocial_action * condition + prosoc_left, family = poisson,data = x )
deviance(model2)
## [1] 14.14685
pchisq(deviance(model2), df = df.residual(model2), lower.tail = FALSE)
## [1] 0.002711932
p-value = 0.002711932, reject H0,thus prosoc_left is dependent of prosocial_action and condition
H0:prosocial_action and condition are conditionally independent of prosoc_left H1:prosocial_action and
```

 $H0:prosocial_action$ and condition are conditionally independent of prosoc_left $H1:prosocial_action$ and condition are conditionally dependent of prosoc_left

```
#test if prosocial_action and condition are conditionally independent of prosoc_left
model3 = glm(Freq~ prosocial_action * prosoc_left + condition * prosoc_left, family = poisson,data = x
deviance(model3)

## [1] 1.443903
pchisq(deviance(model3), df = df.residual(model3), lower.tail = FALSE)

## [1] 0.4858032
```

p-value = 0.4858032, p-value > 0.05, fail to reject H0, thus prosocial_action and condition are independent conditional on prosoc left

5. Conclusion

Question of interest is the relationship between condition and pulled_left and prosoc_left, we can combine the data over all 7 chimpanzees.

```
cta = xtabs( ~ prosoc_left + condition + pulled_left, data = dataset)
##pearson's chisquared test
summary(cta)

## Call: xtabs(formula = ~prosoc_left + condition + pulled_left, data = dataset)
## Number of cases in table: 504
## Number of factors: 3
## Test for independence of all factors:
## Chisq = 10.877, df = 4, p-value = 0.02798
```

The chisquare statistic is 10.877, with 4 degrees of freedom and p-value 0.02798. It is less than 0.05 thus is significant. Thus the three factors dependent.

Then test it for each chimpanzee.

Chimpanzee 1

```
# generate data for champanzee 1
data1 = dataset[dataset$actor == 1,]
x = data.frame(xtabs( ~ prosocial_action + condition, data = data1))

#using poisson regression to build model
model = glm(Freq~prosocial_action + condition, family = poisson,data = x )
deviance(model)
```

[1] 0.2339193

```
df.residual(model)
## [1] 1
pchisq(deviance(model), df = df.residual(model), lower.tail = FALSE)
## [1] 0.6286328
```

Chimpanzee 2

Chimpanzee 2 performed a little wired compare to other chimpanzees, it always pull on the left lever and might whatever other factors are. It might be an outlier

```
# generate data for champanzee 1
data2 = dataset[dataset$actor == 2,]
x = data.frame(xtabs( ~ prosocial_action + condition, data = data2))

#using poisson regression to build model
model = glm(Freq~prosocial_action + condition, family = poisson,data = x )
deviance(model)

## [1] -1.332268e-15

df.residual(model)

## [1] 1

pchisq(deviance(model), df = df.residual(model), lower.tail = FALSE)

## [1] 1
```

Chimpanzee 3

```
# generate data for champanzee 3
data3 = dataset[dataset$actor == 3,]
x = data.frame(xtabs( ~ prosocial_action + condition, data = data3))

#using poisson regression to build model
model = glm(Freq~prosocial_action + condition, family = poisson,data = x )
deviance(model)

## [1] 0.534171

df.residual(model)

## [1] 1
pchisq(deviance(model), df = df.residual(model), lower.tail = FALSE)

## [1] 0.4648585
```

Chimpanzee 4

```
# generate data for champanzee 4
data4 = dataset[dataset$actor == 4,]
x = data.frame(xtabs( ~ prosocial_action + condition, data = data4))
#using poisson regression to build model
```

```
model = glm(Freq~prosocial_action + condition, family = poisson,data = x )
deviance(model)
## [1] 0.534171
df.residual(model)
## [1] 1
pchisq(deviance(model), df = df.residual(model), lower.tail = FALSE)
## [1] 0.4648585
Chimpanzee 5
# generate data for champanzee 1
data5 = dataset[dataset$actor == 5,]
x = data.frame(xtabs( ~ prosocial_action + condition, data = data5))
#using poisson regression to build model
model = glm(Freq~prosocial_action + condition, family = poisson,data = x )
deviance(model)
## [1] 1.332268e-15
df.residual(model)
## [1] 1
pchisq(deviance(model), df = df.residual(model), lower.tail = FALSE)
## [1] 1
Chimpanzee 6
data6 = dataset[dataset$actor == 6,]
x = data.frame(xtabs( ~ prosocial action + condition, data = data6))
#using poisson regression to build model
model = glm(Freq~prosocial_action + condition, family = poisson,data = x )
deviance(model)
## [1] 0.8935135
df.residual(model)
## [1] 1
pchisq(deviance(model), df = df.residual(model), lower.tail = FALSE)
## [1] 0.344527
Chimpanzee 7
data7 = dataset[dataset$actor == 7,]
x = data.frame(xtabs( ~ prosocial_action + condition, data = data6))
#using poisson regression to build model
```

```
model = glm(Freq~prosocial_action + condition, family = poisson,data = x )
deviance(model)

## [1] 0.8935135

df.residual(model)

## [1] 1

pchisq(deviance(model), df = df.residual(model), lower.tail = FALSE)

## [1] 0.344527

""
```

Note that the echo = FALSE parameter was added to the code chunk to prevent printing of the R code that generated the plot.

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